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Abstract

In the present work, the numerical assesment of vibroacoustic (VA) performance of Fibre Metal Laminates (FML) with mid-plane center delamination is presented. A fluid structure interaction study has been done using Finite Element Method (FEM). Experimental validation is performed on aluminium panel for verifying the correctness of Finite Element idealization procedure to simulate the fluid-structure interaction. Delamination is introduced in the FE model of FML panel and VA analysis is subsequently carried out. Sound Transmission Loss

(STL) is computed on the panel with center delamination and without delamination. The Over All Sound Pressure Level (OASPL) shows that the presence of delamination (40%) in FML has not changed the total energy of the transmitted sound, when compared to aluminium and composites. However, in the narrow frequency bands (150-200 Hz, 200-250 Hz) the sound transmission nature has been significantly affected due to local delamination modes, participating in the fluid-structure interaction process.

Keywords: Fibre Metal Laminate (FML), Vibroacoustic (VA), Delamination, Fluid-Structure Interaction, Sound Pressure Level (SPL), Sound Transmission Loss (STL), Over All Sound Pressure Level (OASPL)

1.0 Introduction

Fiber metal laminates are hybrid materials, composed of fibrous composites (GFRP) together with alternate metallic (Aluminium) layers. FML have found large application in aircraft structures, namely fuselage skin, cargo bay, floor board amongst others. Assessment of FML properties, especially fatigue characteristics, fire resistance, damage tolerance has become very important research area for its qualification as aircraft materials and there have been considerable amount of studies reported in this direction [1]. FML panels are fabricated by stacking the laminae of aluminium and glass fibre reinforced plastic. Occurrence of delamination in these panels is possible either during manufacturing process or under operational loadings, therefore numerical assesment of delamination in FML is of importance and has been extensively studied [2, 3]. The effects of delamination length and orientation angle on the natural frequency of symmetric composite beams are investigated, analytically and numerically. It has been found that when delamination length increases, frequencies decrease and subject to change due to orientation angle, shape and location [4-6]. Various analytical models and numerical analyses for the free vibration of delaminated composites are reviewed [7, 8].

Theoretical and experimental analysis of the influence of debonding on the flexural stiffness and natural frequency is analyzed [9]. Observations are made on the effects of delamination size and its location around the cutout on the natural frequency of a thick square laminate; a substantial decrease in natural frequencies is observed [10]. The possibility of delamination detection using nonlinear interaction in the delaminated region is explored [11]. In functionally graded beams with a single delamination, the natural frequencies are affected

when the beam has longer delamination [12]. Vibro-thermography experiments have been carried out to detect the delamination type of defects to assess the impact severity in FML [13]. Delamination in FML and its influence on the buckling failure has been investigated numerically as a specific failure mode [14].

Vibro-acoustic coupling has become a critical parameter with the introduction of new light-weight materials such as composites. Much works are presented on the vibroacoustic front where acoustic response of panels with attached passive sound insulation materials has been discussed [15]. A coupled structural-acoustic analysis procedure for industrial application has been developed in [16]. Transmission loss of multilayer composite panels is predicted under SEA (statistical energy analysis) frame work using wave theory [17]. Vibro-acoustic interactions between the structure and acoustic media are considered in calculating the sound transmission loss for a long cylindrical stiffened shell, subjected to a plane wave incidence [18]. Other notable studies can be seen in this promising area, addressing the dynamic instability of delaminated composite plates [19, 20], delamination growth in FML[21-23] and VA analysis of multi-layer composite panels [24], characterization of cellular material structure [25] and VA behaviour in biosourced composites [26].

Sound Transmission Loss (STL) is one of the most important measurements in determining a material's effectiveness at isolating sound. There have been very limited studies reported for evaluating the VA characteristics of FML in terms of sound transmission loss and the distributed Sound Pressure Level (SPL). FAR (Federation of Aviation Regulation) authority has laid stringent norms on the noise levels inside the fuselage cabin [27]. The recent works on the damage tolerant capability of FML to enhance its structural performance have not considered the VA characteristics [1-3, 28-29].

Making appropriate choice of the materials for aircraft structures from acoustic point of view has been imperative. There are limited studies made on evaluation of FML panel's response under acoustic loadings and its potential in sound transmission [30, 31]. As the overheads of experimental trials are usually very high and time-consuming, it is apparent that computational modelling of the behaviour of FML to acoustic loads would be of enormous interest and benefit to the aerospace industries and this forms the primary focus of this work.

In the present work we are evaluating the VA performance of FML with aluminium and composite, in the presence of delamination. For this purpose, the work is carried out in three stages; in the 1st stage VA procedure is validated using FEM, where a numerical model of the

impedance tube with aluminium panel placed in between the sender and receiver chamber are modeled and the procedure is validated with the literature [16]. In the 2nd stage, a VA test facility is built to measure the STL of the aluminium panel and the experimental results are compared with the finite element analysis. In the 3rd stage, delamination modeling procedure in composite is validated with the literature [19], based on these validated procedures the delaminations are introduced in composites, two layered AL and FML and their VA performance, in terms of STL, SPL and OASPL of different frequency bands of interest within 0-250 Hz is evaluated using the digital impedance tube. The paper is organized as follows; section 2 briefly discusses the governing equations of fluid structure coupling, section 3 explains the numerical modelling of impedance tube and the experimental measure of STL; also highlights the delamination modeling procedure in panels. Section 4 deals with the results & discussion in the presence of delamination and its effect on VA performance of FML/Composite & AL panels individually. Section 5 presents the observations on the results obtained and finally section 6 gives the conclusion to the work carried out.

2.0 Vibroacoustic Modelling of FML in ANSYS

In VA analysis, the governing equations of structure and fluid are used, along with the required coupling load vectors. In the formulation of fluid-structure interaction problems, the structural system is modeled using the Rayleigh-Ritz approach and the fluid is idealized with Galerkin's method.

The acoustic wave equation is given by

$$\frac{1}{c^2} \frac{\partial^2 P}{\partial t^2} - \{L\}^T (\{L\} P) = 0 \quad (1)$$

where, c is speed of sound in fluid medium in time t , P is the acoustic pressure and L is the matrix operator (gradient and divergence).

The Galerkin based FE procedure is applied to form the element matrices by discretizing the wave Eqn.(1). In fluid-structure interaction problem, the fluid pressure load acting at the interface is added to the dynamic equilibrium equation. The structural equation in its final form can be presented as

$$[M_e] \{\ddot{u}_e\} + [C_e] \{\dot{u}_e\} + [K_e] \{u_e\} = \{F_e\} + \{F_e^{pr}\} \quad (2)$$

where M_e , C_e and K_e are the mass, damping and stiffness matrices respectively; \ddot{u}_e, \dot{u}_e and u_e are the acceleration, velocity and displacement vectors respectively. F_e is the applied load vector and F_e^{pr} is the fluid pressure load vector.

The complete finite element equations for the fluid-structure interaction problem are given in matrix form as

$$\begin{bmatrix} [M_e] & [0] \\ [M^{fs}] & [M_e^p] \end{bmatrix} \begin{Bmatrix} \{\ddot{u}_e\} \\ \{\ddot{P}_e\} \end{Bmatrix} + \begin{bmatrix} [C_e] & [0] \\ [0] & [C_e^p] \end{bmatrix} \begin{Bmatrix} \{\dot{u}_e\} \\ \{\dot{P}_e\} \end{Bmatrix} + \begin{bmatrix} [K_e] & [K^{fs}] \\ [0] & [K_e^p] \end{bmatrix} \begin{Bmatrix} \{u_e\} \\ \{P_e\} \end{Bmatrix} = \begin{Bmatrix} \{F_e\} \\ \{0\} \end{Bmatrix} \quad (3)$$

where

$[M^{fs}] = \rho_0 [R_e]^T$, is the fluid mass matrix and

$[K^{fs}] = -[R_e]$, is the fluid stiffness matrix.

In fluid-structure interaction analysis, the acoustic fluid element will generate all the submatrices with superscript p in addition to the coupling submatrices $\rho_0 [R_e]^T$ and $[R_e]$. Submatrices without a superscript will be generated by the compatible structural element used in the model.

Coupled structural acoustic analysis is carried out using shell and solid elements in ANSYS, a general purpose finite element software. Two layers of shell elements are modelled between the source and receiver cavities and the appropriate DOF's are accordingly coupled. The upstream and downstream acoustic cavities are modelled using FLUID30 element and the structure is modelled by SHELL63 element. The interface between the upstream and downstream sections does not share common nodes and they are structurally and acoustically isolated. Anechoic termination is applied at both the ends of the numerical impedance tube. The upstream and downstream panels are further connected using coupling equations. A harmonic analysis has been conducted using the frontal solver. The fluid elements from acoustic cavity are selected and then the sound pressure level is subsequently plotted.

2.1 Modeling FML with Delamination for VA characterization

Delamination may be initiated in FML, when FML is loaded along its in-plane direction; particularly if the interface layer (adhesive) between aluminium and bridging prepreg lamina is loaded considerably. For higher load levels debonding sets on; therefore the aluminium

layer and prepreg are gradually getting separated, resulting in delamination. In FML, interlaminar delamination might occur at any interface i.e. at the interface between two glass/epoxy layers or between aluminium and glass/epoxy (refer to Figure 1). Experimental observations have shown that the delamination may grow at the resin rich layer between the two structural layers. It's initiation however might be due to matrix failure inside the glass/epoxy layer. When sound is transmitted through these delaminated panels, there will be considerable amount of change expected in the STL, compared to panels without delaminations. To assess the VA performance, delaminations are thus introduced between GFRP prepregs and aluminium sheets of FML at the mid plane in the center of the laminate. The material data and laminate details are presented in Table 1 (a and b) is used in the analysis. The finite element analysis is carried out to verify the change in STL due to this mid plane delamination. Figure 1 explains the location of the simulated delamination in the FML

2.2 Validation of delamination procedure

To establish the correctness of the finite element procedure for modeling delamination, a validation problem is chosen from the literature. For this purpose a composite beam is modeled in ANSYS using layered solid element. The cantilevered beam is made of T300/934 graphite/epoxy material with a $[0^0/90^0]_{2s}$ stacking sequence. The dimensions of the 8 layered beam are $127 \times 12.7 \times 1.016 \text{ mm}^3$. The material properties of the lamina are: $E_{11}=134 \text{ GPa}$, $E_{22}=10.3 \text{ GPa}$, $E_{33}=10.3 \text{ GPa}$, $\nu_{12}=0.33$, $\nu_{23}=0.33$, $\nu_{13}=0.33$, $G_{12}=5.0 \text{ GPa}$, $G_{23}=2.0 \text{ GPa}$, $G_{13}=5.0 \text{ GPa}$, $\rho=1480 \text{ Kg/m}^3$. The delamination is assumed to occur at the mid-plane of the laminate and its size is considered to be 50.8 mm length (40%). Figure 2 pictorially presents the location of the delamination in the thickness direction of the laminate.

Delamination is simulated in the layered solid element model by operating the respective coupling equations in between the layers. The free vibration frequencies of the beam have been compared with the open literature. The results of the present analysis are compared very well with the reported values [19]. This validation has ensured the correctness of the delamination modeling procedure. The results are presented in Table 2. The importance of delamination in dynamics can be very well observed from the change in the dynamic behavior of cantilever beam with additional local modes introduced by delamination. These local modes due to delamination certainly would change the VA characteristics of the FML/composite panels.

3.0 VA Simulation and Experimental Validations

This section explains the finite element modelling of the impedance tube with aluminium panel and vibroacoustic measurements in VA test facility to measure the STL and compare the test results with the finite element analysis of the VA setup. The validated delamination procedure (see sections 2.2) has been applied to aluminium, composite and FML panels. A comparison is made in terms of VA performance parameters (STL/ OASPL) among the aircraft panel structures.

3.1 Vibroacoustic behaviour of Aluminium Panel: Numerical studies

The numerical study from [16] has been taken for the validation of VA analysis procedure. To carry out VA analysis, a complete fluid- structure finite element analysis has been carried out, representing aircraft panel, placed in between sender- receiver acoustic cavities with anechoic termination boundaries (numerical model of impedance tube; refer to figure 3). The model consists of a central Aluminum (AL) panel and fluid (air) on either side of the panel. The AL panel is made using double layer shell elements and the fluid domain is constructed using acoustic element. The ends of the duct are anechoically terminated. This is achieved by specifying that the elements at the end of the duct have got an infinite absorption through their material properties. The VA analysis has been carried out by introducing an equivalent noise source at a distance of 1.5 meters from the aircraft panel. A low frequency, fluid structure interaction study is performed within 250 Hz bandwidth. The simply supported boundary condition is applied as in [16] with the same material properties, loading and mesh size. The interaction of the fluid and the structure is considered at the interface, which causes the acoustic pressure to exert a force on the structure and the structural motions effectively produce the fluid load.

The results in the form of sound pressure level (dB), are obtained after performing the vibroacoustic analysis on the aluminium panel. The obtained results are subsequently compared with the results available in literature [16], The results are presented in Table 3. The comparison shows that the obtained results are in exact matching with the published results.

3.2 Vibroacoustic Measurement of Aluminium Panel: Experimental studies

In the next stage the result of the finite element analysis has been compared with experimentally measured sound transmission loss. Figure 4 shows the picture of the experimental set up, where both sender and receiver chambers can be seen. Figure 5 represents an equivalent FE model of this facility. The dimensions and material are given in

Table 4. Vibration testing has been performed on the aluminium panel (all edges are clamped) before exciting the specimen by acoustic loading to establish the frequency spectrum of the receiving chamber as well as the aluminium panel in order to verify any structural coupling takes place between them. When the mechanical input is applied through an impulse hammer, the source chamber is detached and also the receiver chamber is unclosed. After the vibration testing, source chamber is attached with receiving chamber. A band limited random noise (0 to 200 Hz; 96.84 dB SPL measured at source) is generated and the same is supplied through a signal conditioner to the speaker. Thus, the generated low frequency noise is allowed to travel as a plane wave in the source chamber to acoustically excite the plate in order to produce its vibro-acoustic modes.

Microphones (GRAS 1/2" ICP type) are placed both in source and receiving chambers to measure the sound pressure levels. It is evident from the observed results that around 6 dB reduction is noticed from source to receiver; which clearly shows the ability of material in radiating the sound through vibrating modes. Table 5 presents the SPL measured in the source chamber (from the panel at Mic 3; $x = 300$ mm, $y = 300$ mm, $z = 150$ mm) and in the receiver (from the panel at Mic 4; $x=300$ mm, $y = 300$ m, $z = 150$ mm). A good correlation has been observed between the simulation and experiment, which validates the developed numerical VA scheme in the low frequency region.

4.0 Numerical Analysis

In this section the results of the sound transmission loss analysis on various panels like AL, composite and FML with and without delamination are discussed.

4.1 Delamination and its effect on vibroacoustic performance of aircraft panels

The vibroacoustic performance and characteristics of delaminated panels (AL/composite/FML) are evaluated. The panel is modelled inside the impedance tube finite element model (see Figure 3), where the STL of aluminium panel has been already validated. The present study is conducted on three panels, namely the first one is an aluminium panel made of two layers with void introduced in between them; the second panel is a symmetric cross ply composite laminate and the third panel is fiber metal laminate. The study has focused on delaminated and undelaminated panels modeling, followed by VA analysis to evaluate the influence of delamination on sound transmission loss in isotropic, composite and fiber metal

laminate to a near field acoustic load (94 dB, 0-250 Hz sine sweep). Table 6 presents the frequencies of the delaminated modes of AL, composites and FML.

4.2 Sound transmission loss on AL panel with void

The aluminium panel is modelled with 1.5 mm thickness. Two layers, each having 0.75 mm thickness, are assumed to be attached and the constraint equation between these layers is applied to simulate them as a single panel. To examine the effect of void or debonding between the panels on the VA performance, a void of 40% is introduced in the central region. A moderate change in the STL values are noticed when there is a void in the AL panel. The STL and the Overall Sound Pressure Level (OASPL) throughout the frequency band of 0 Hz to 250 Hz are plotted in Figure 6 (a and b). From the SPL plot, it can be seen that there is no drastic change noticed in the SPL level upto 125 Hz; but after that there has been a significant change taken place. The OASPL has confirmed this fact, which is observed in the band of 170 to 210 Hz (refer to Figure 6b). It is interesting to note that the local modes introduced due to void, actually appear in the frequency band 170 to 210 Hz.

Therefore, it can be understood that the noise radiation is influenced by debonding/ or delamination, in particular the local delamination modes radiate the sound considerably.

4.3 Effect of delamination on STL in composite panel

A symmetric GFRP laminate with a layup sequence of $[0/90/90/0]_T$ and ply thickness 0.375 mm is considered. The material data in Table 1 is used. The same modeling scheme is adopted as in the case of AL panel and a mid-plane delamination is introduced in the laminate. VA results are presented in Figure 7 (a and b), which shows a considerable change in the STL between 150 to 210 Hz due to the presence of delamination mode (157 Hz). However, the OASPL has indicated only a moderate change in the overall band of 0 to 250 Hz other than 140 to 160 Hz band, where the influence of delamination mode (157 Hz) is noticed. Therefore, it is obvious that the delamination mode alters the SPL distribution.

4.4 Effect of delamination on STL in FML

The FML panel is made up of alternate layers of aluminium (2 layers, thickness 0.5 mm) and GFRP prepreg (2 layers, ply thickness 0.25 mm). To examine the effect of delamination between the layers of AL and GFRP on the VA performance, it is introduced in the central interface region of the FML panel. Figure 8 (a and b) shows the two local delamination modes (108.7 Hz & 234.65 Hz) that are seen in the frequency band of 0 to 250 Hz. The STL results are presented in Figure 9 (a and b). The SPL plot indicates the change in STL due to

delamination in the frequency scale. The OASPL shows that the presence of delamination (40%) in FML has not changed the total energy of the transmitted sound; however, in the narrow frequency bands (150-200 Hz, 200-250 Hz) the sound transmission nature has been significantly modified. Further, it can be seen that the noise radiation pattern of the local delamination modes is different. The first local delamination mode transmits more energy, with respect to undelaminated case.

Figure 10 (a and b) presents the overall scenario of VA characteristics of isotropic, composite and FML panels in terms of STL and OASPL. The VA performance of FML has been observed to be good in comparison to aluminium and composite laminate.

5.0 Results and Discussion

The following major observations are made from the above numerical studies:

- The numerical impedance model has been found suitable to simulate the VA behaviour of panels made of different class of materials.
- The influence of low frequency structure borne noise on vibrating panels has been studied to estimate the sound transmission loss and very useful engineering data namely SPL and OASPL of different aircraft quality materials is generated.
- Three types of aircraft panels, namely aluminium, composite laminate and hybrid laminate (FML) are examined for their STL performance, where the hybrid laminate FML is found to be efficient in filtering the transmitting noise.
- The presence of delamination in laminated/FML structures has effected the STL performance. These local delamination modes influence the transmitted noise to get distributed with near by global modes, around its local frequency.
- In general the symmetric breathing delamination mode transmits higher energy than the antisymmetric one in FML hybrid laminate. (Refer to figure 11 a and b).

6.0 Conclusion

A numerical model of an impedance tube with aluminium panel placed in between the sender and receiver chamber is made and VA procedure is validated with the literature. VA test facility is built to measure the STL of the aluminium panel and further experimental results are compared with the finite element analysis. A validated delamination modeling procedure is introduced in composites. The VA performance of aluminium, composite and FML panels is evaluated in the frequency band of 0 to 250 Hz, in terms of STL, SPL and OASPL. In

general, the FML has shown a good VA performance by relatively transmitting lower SPL. The presence of delamination modes has modified significantly the STL around its natural frequencies in a narrow bandwidth of 10 to 50 Hz. The first delamination mode (1-1) and the second mode (1-2) have displayed a different tendency in transmitting the sound (< 250 Hz). Therefore, it is understood that the presence of damage and its dynamics have a definite role in deciding the VA characteristics of aircraft panels subjected to low frequency structure borne noises.

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Table 1 (a) **Material properties used in the analysis for case studies**

	Aluminium (for FML Only) [3]	Prepreg (GFRP for FML Only) [3]	CFRP-UDC
E₁ (GPa)	72.4	48.9	150
E₂(GPa)	72.4	5.5	9.0
G₁₂(GPa)	27.6	5.55	4.0
v₁₂	0.33	0.33	0.35
ρ(kg/m³)	2780	2471	1600

Table 1 (b) **Thickness,orientation and stacking sequence used in the case studies**

	Panel Thickness (mm)	Ply Thickness (mm)	Orientation
Aluminium	1.5	0.75	[0/0] _T
Composite	1.5	0.375	[0/90/90/0] _T
FML[AL/Prepreg/AL]	1.5	0.5/0.25/0.25/0.5	[0/0/90/0] _T

Table 2: Comparison of first and second frequency with and without delamination

	Experimental [19]	FSDT [19]	CLT [19]	HSDT [19]	NASTRAN 3D [19]	Present
Intact (Mode 1)	79.75	81.86	81.88	82.12	81.75	81.932
50.8 mm (Mode 1) (Delaminated)	76.75	76.81	76.36	76.48	75.14	76.584
Intact (Mode 2)				513.30	510.70	513.09
50.8 mm (Mode 2) (Delaminated)				469.02	478.66	466.35

Table 3: Validation for VA Simulation

Result	Max Displacement, m	Min SPL, dB	Max SPL, dB	Noise reduction across the panel, dB
Present analysis	0.741×10^{-6}	68.989	91.822	22.92
[16]	0.741×10^{-6}	68.989	91.822	22.92

Table 4: Dimensions and material data

Material	Young's Modulus	Density ρ (Kg/m ³)	Poisson's Ratio	Dimensions (m)
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E (GPa)				
Aluminium	70	2700	0.3	0.5×0.5×0.001

Material	Velocity of Sound (C, m/s)	Density (ρ, kg/m³)	Dimensions (m)	
Air	340	1.25	0.4×0.4×0.66	

Table 5: Comparison of noise reduction obtained through analysis and experiment

Method	SPL at Mic 3, dB (Source chamber)	SPL at Mic 4, dB (Receiver chamber)	Noise reduction across the panel, dB
Experiment	96.84	90.35	6.49
Analysis	96.81	90.70	6.11

Table 6: Delamination modes in panel (< 250 Hz)

	Mode 1 in Hz	Mode 2 in Hz
Aluminium (2 layers)	190.23 (coupled)	215.38
Composite	157.51	-
FML	108.7	234.65

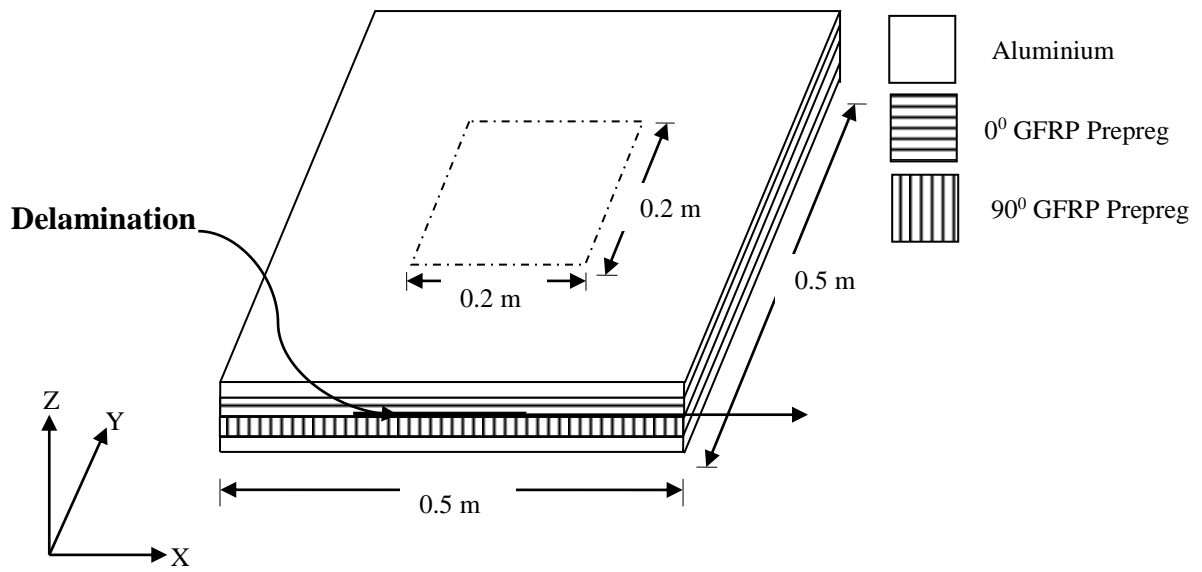


Figure 1: FibreMetal Laminate with delamination

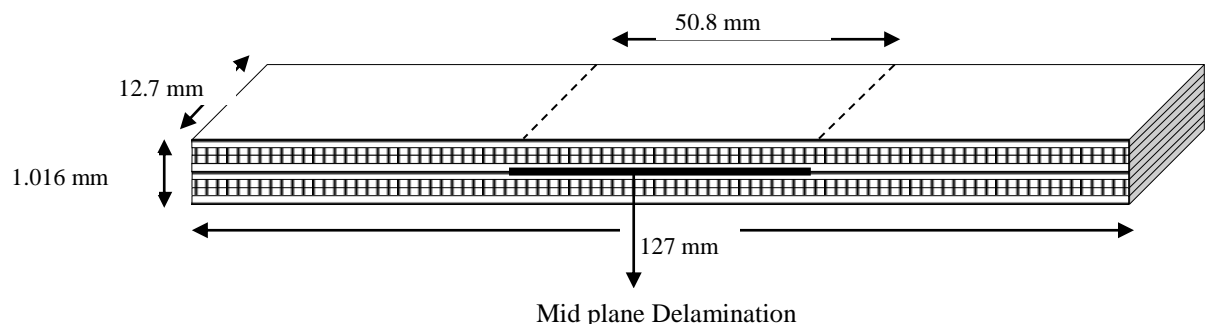


Figure 2: Delamination in composite beam [19]

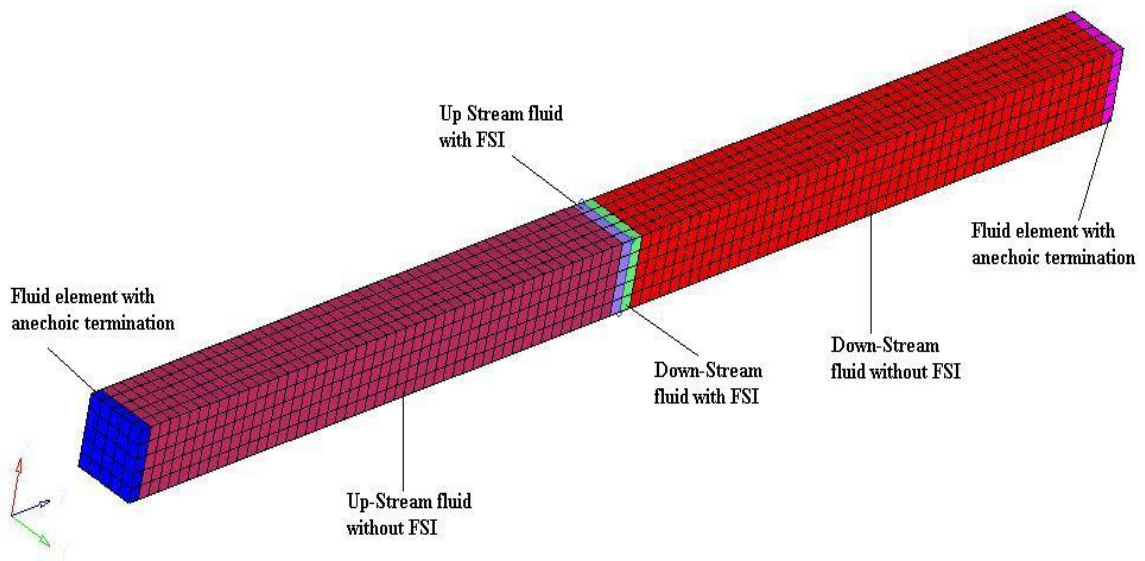
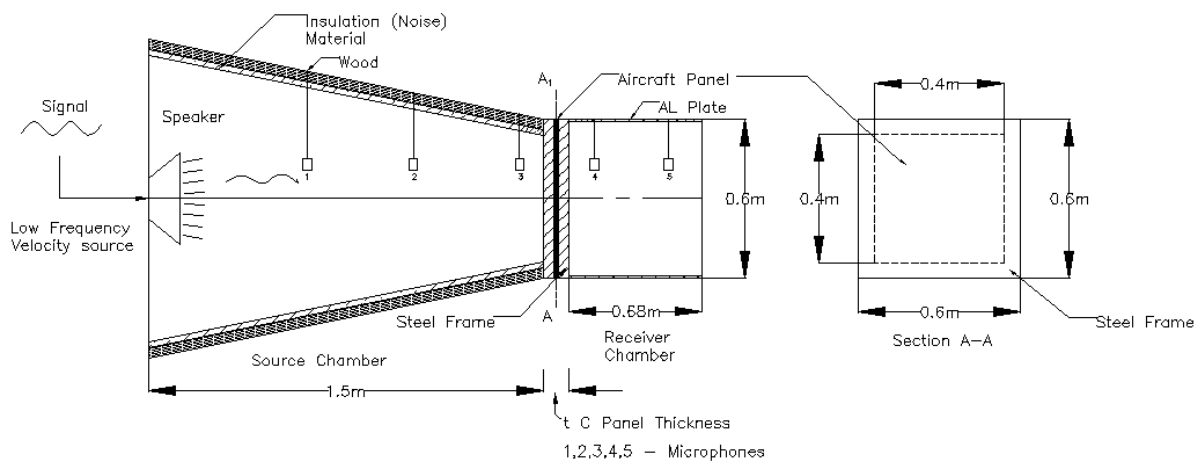


Figure 3: Finite element model of the digital impedance tube



(a)



(b)

Figure 4: Vibroacoustic test facility at CSIR-NAL/India (a) Experimental setup of VA facility (b) Schematic details of the test facility

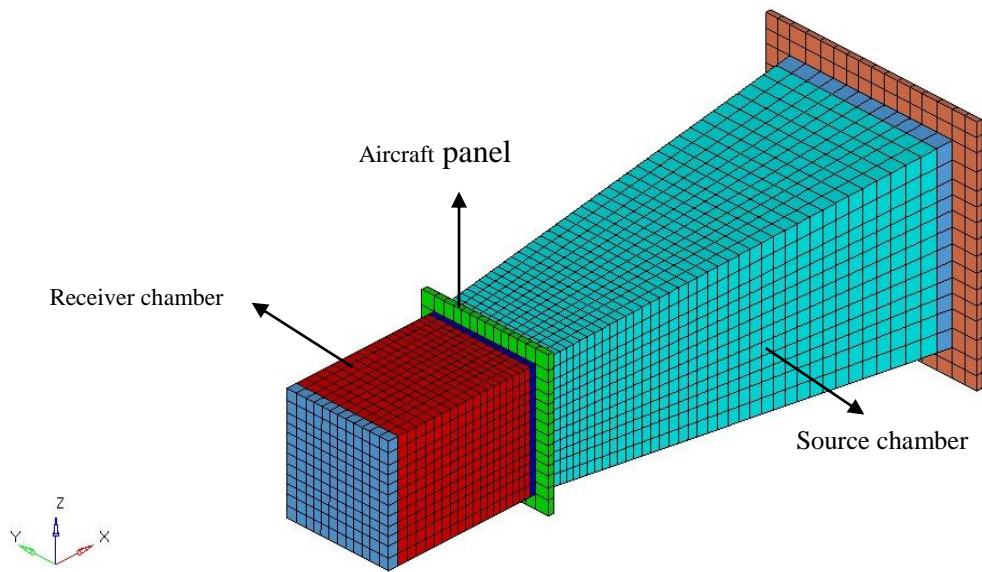
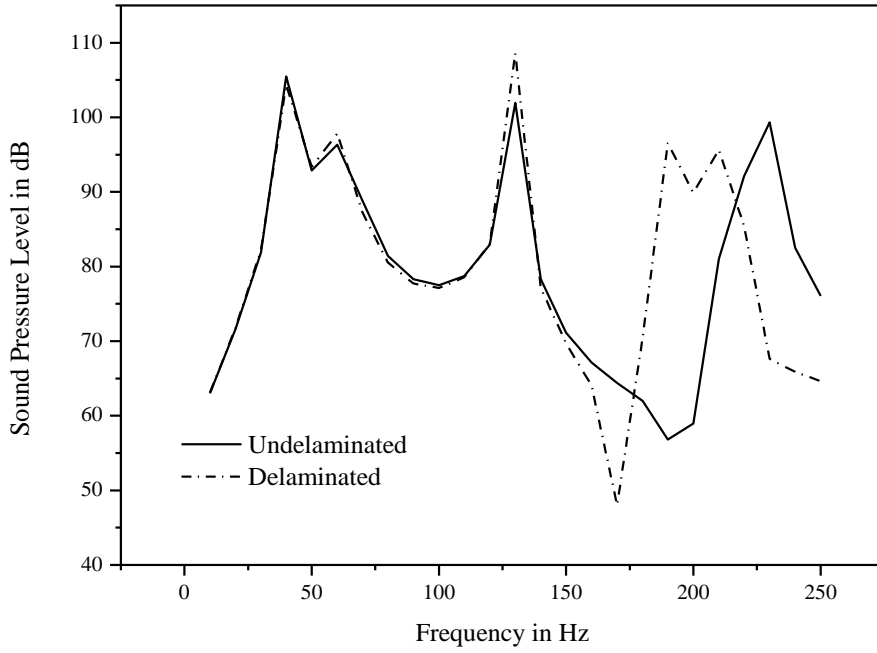
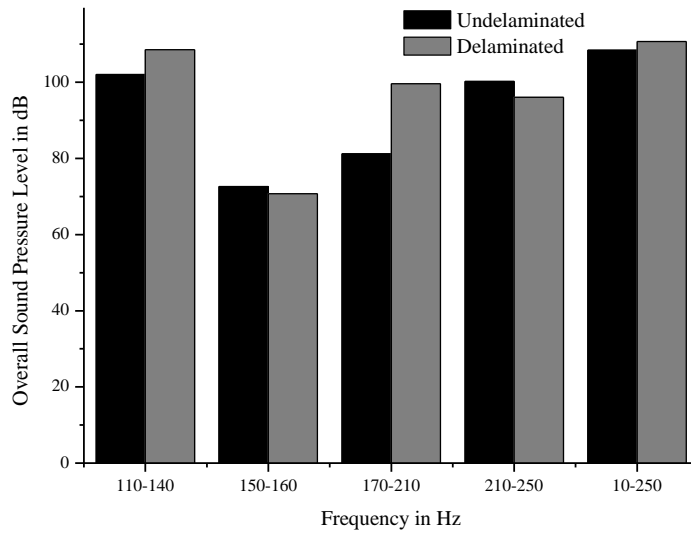


Figure 5:Finite element model of VA test facility



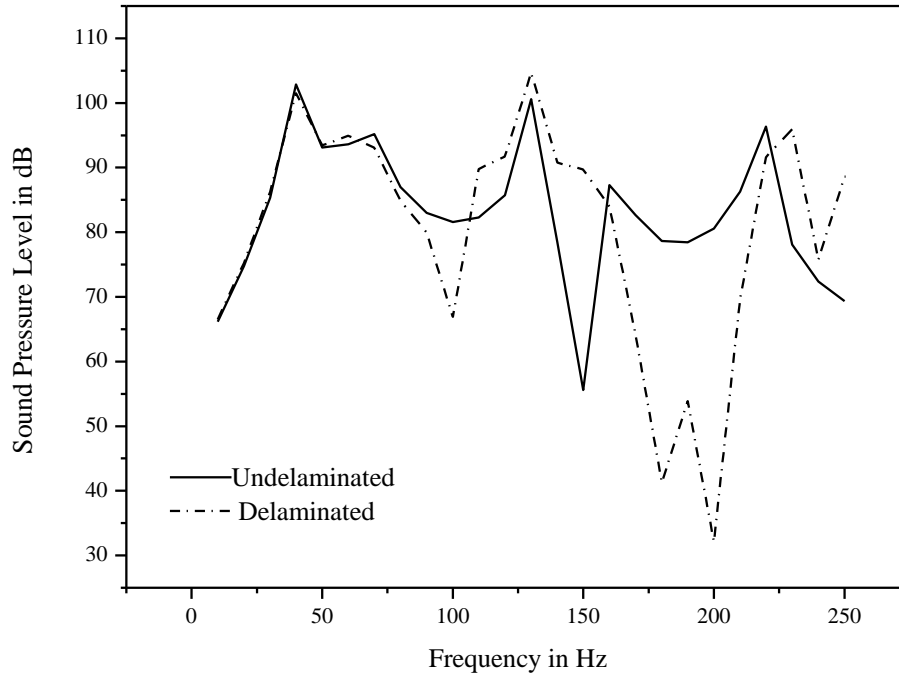
(a)



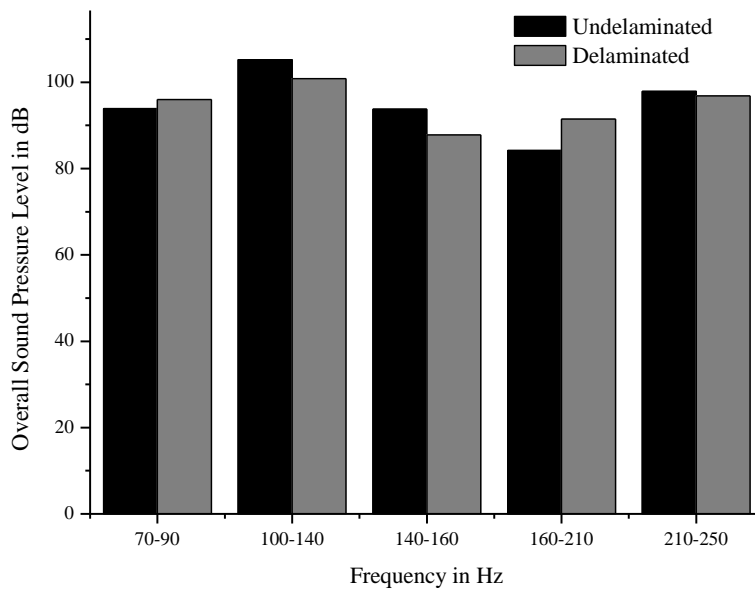
(b)

Figure 6: (a) Plot of frequency versus Sound Pressure Level in Aluminium panel

(b) Plot of frequency versus Overall Sound Pressure Level in Aluminium panel



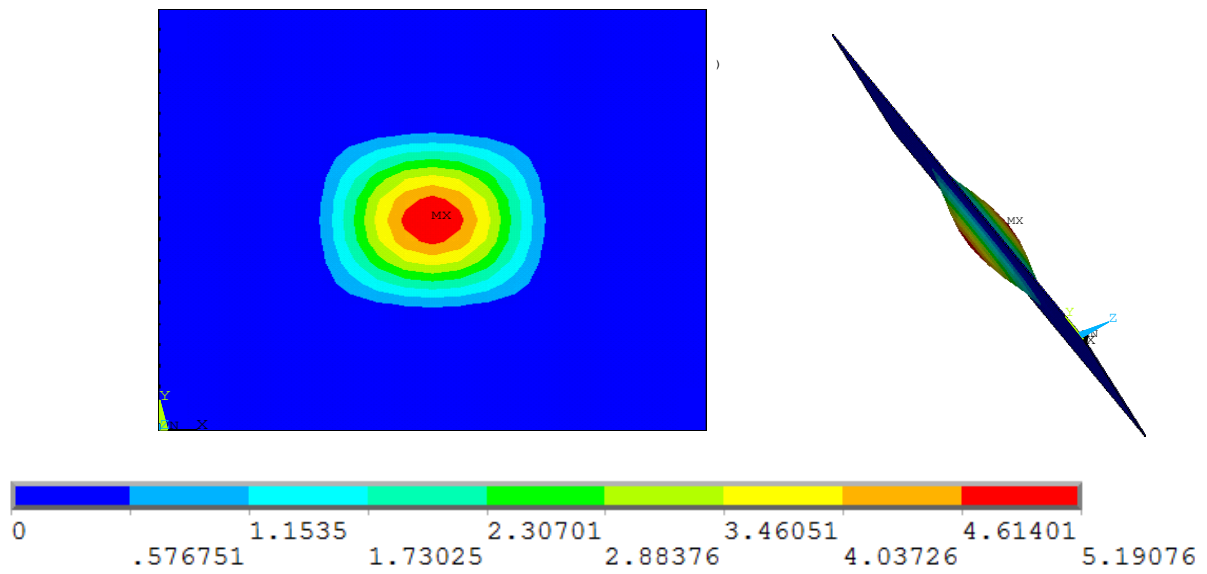
(a)



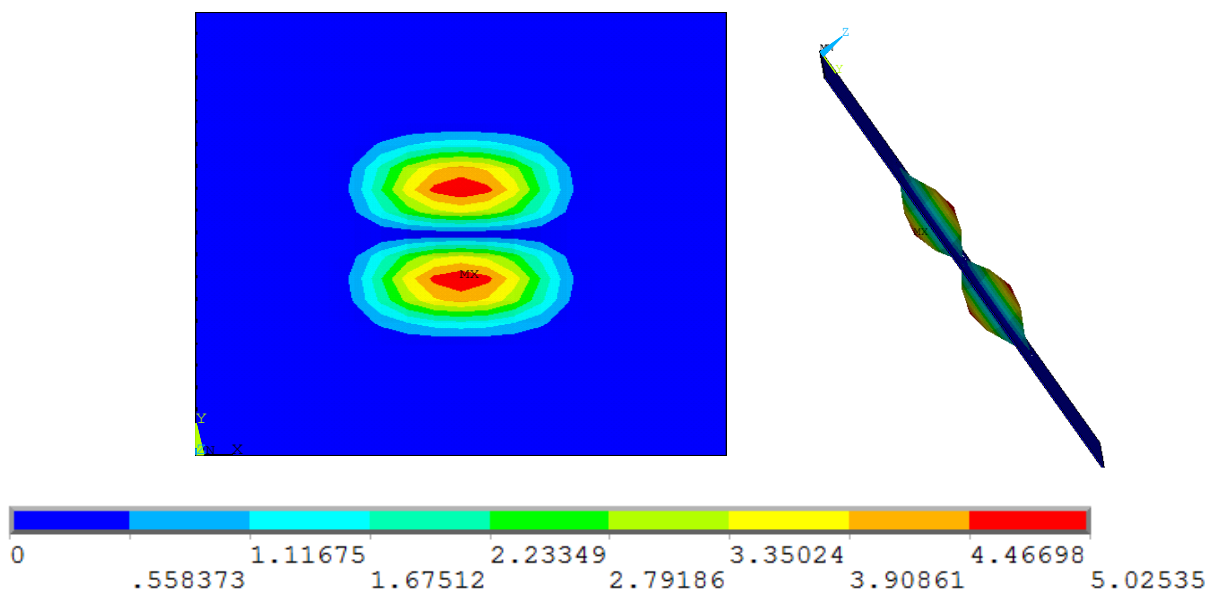
(b)

Figure 7 (a) Plot of frequency Vs SPL in composite panel with and without delamination

(b) Plot of frequency Vs OASPL in composite panel with and without delamination

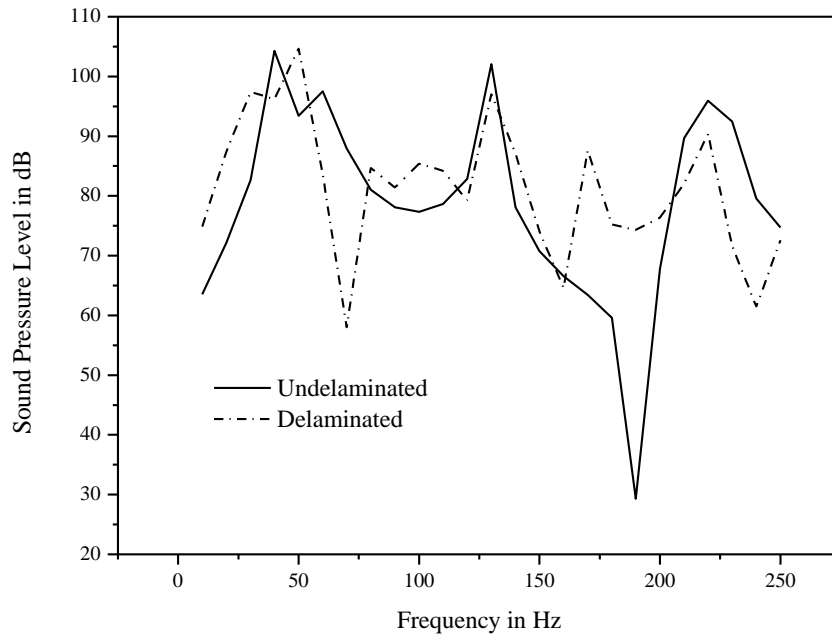


(a)

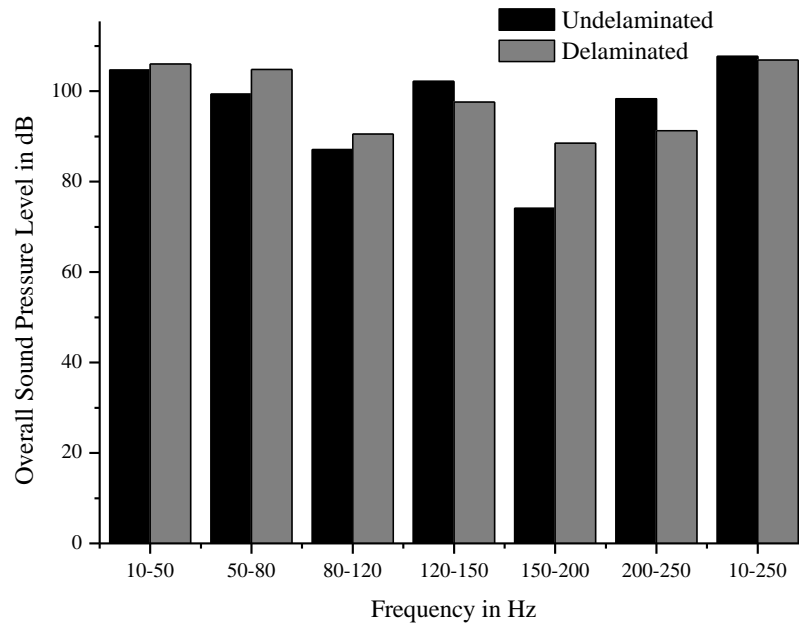


(b)

Figure 8: Delamination modes in FML (a) Local 1st breathing Mode in panel with center delamination (b) Local 2nd breathing Mode in panel with center delamination



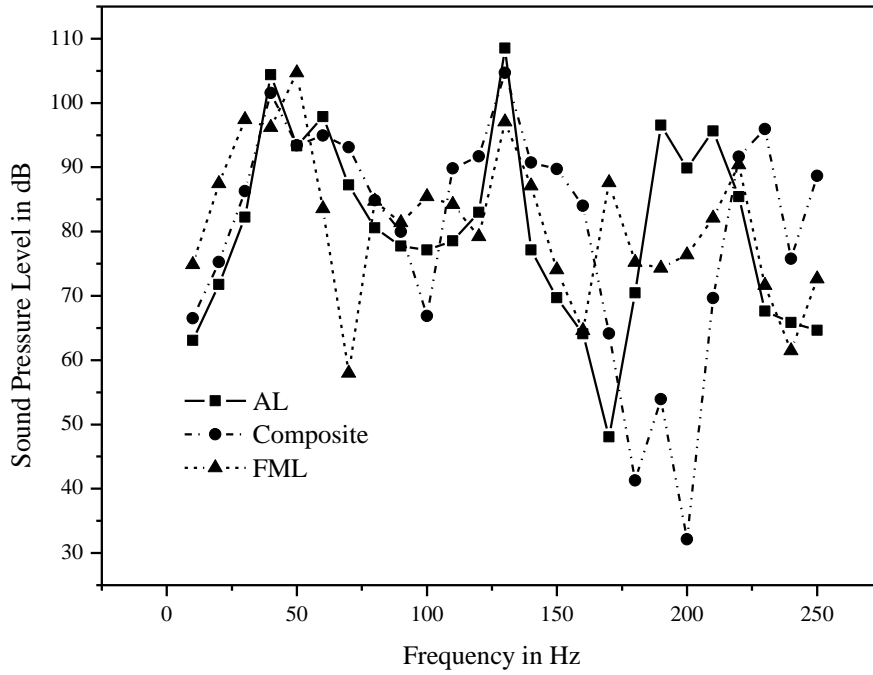
(a)



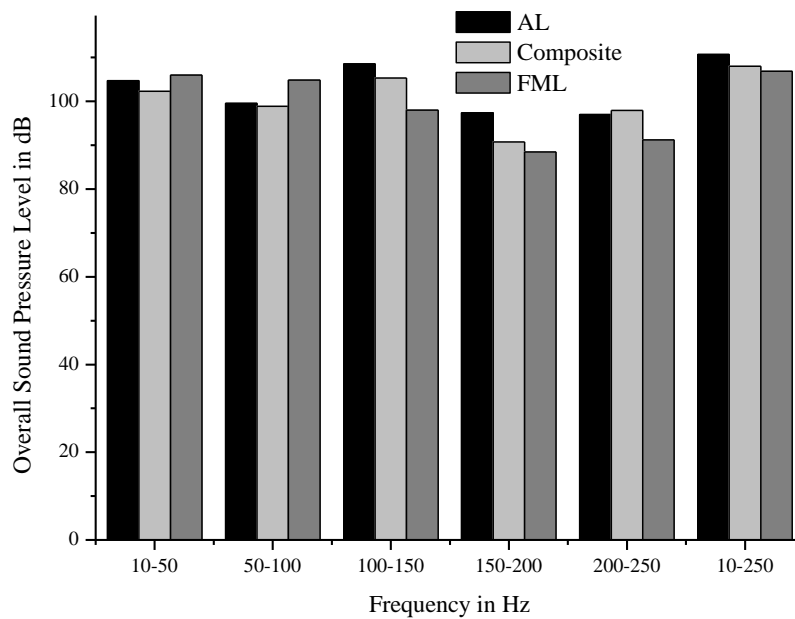
(b)

Figure 9 (a) Plot of frequency versus Sound Pressure Level in FML panel with and without delamination

(b) Plot of frequency versus Overall Sound Pressure Level in FML panel with and without delamination

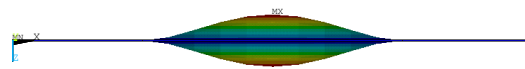
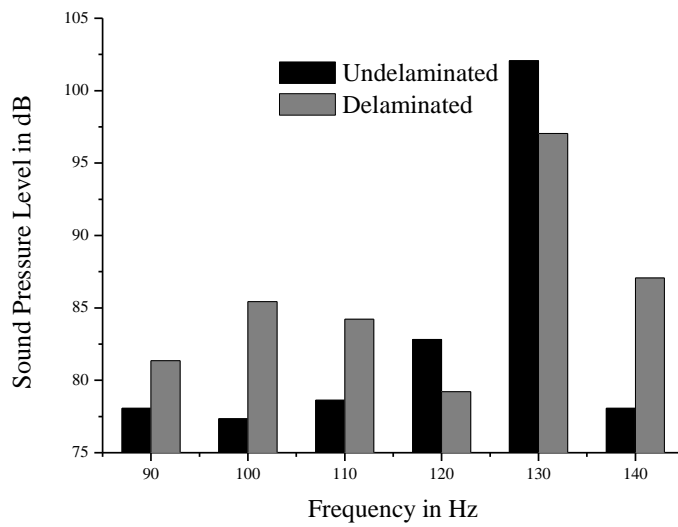


(a)

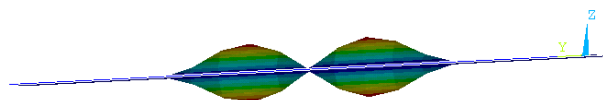
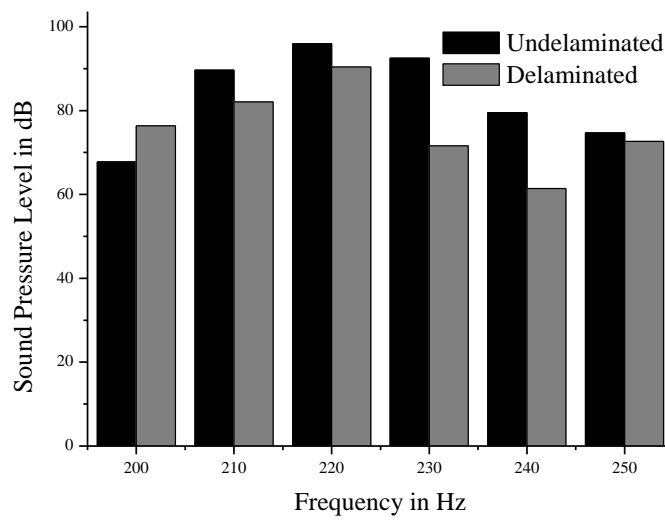


(b)

Figure 10 (a) Plot of frequency versus Sound Pressure Level of delaminated FML compared with delaminated AL and composite Panel **(b)** Plot of frequency versus Overall Sound Pressure Level of delaminated FML compared with delaminated AL and composite Panel



(a)



(b)

Figure 11. SPL comparison of 1st and 2nd delamination modes (a) Symmetric Breathing Mode (b) Antisymmetric Breathing Mode