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ON THE TIME VARIATION OF DUST EXTINCTION AND GAS ABSORPTION FOR
TYPE IA SUPERNOVAE OBSERVED THROUGH NON-UNIFORM INTERSTELLAR MEDIUM

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ABSTRACT

For Type Ia supernovae (SNe Ia) observed through a non-uniform interstellar medium (ISM) in its host galaxy, we investigate whether the non-uniformity can cause observable time variations in dust extinction and in gas absorption due to the expansion of the SN photosphere with time. We show that, owing to the steep spectral index of the ISM density power spectrum, sizable density fluctuation amplitudes at the length scale of typical ISM structures ($\gtrsim 10$ pc) will translate to much smaller fluctuations on the scales of a SN photosphere. Therefore the typical amplitude of time variation due to non-uniform ISM, of absorption equivalent widths and of extinction, would be small. As a result, we conclude that non-uniform ISM density should not impact cosmology measurements based on SNe Ia. We apply our predictions based on the ISM density power law power spectrum to the observations of two highly reddened SNe Ia, SN 2012cu and SN 2014J.

Keywords: ISM — supernovae: general, dust, extinction, ISM: structure, ISM: general, cosmology: miscellaneous

1. INTRODUCTION

One of the remaining systemic uncertainties for Type Ia Supernovae (SNe Ia) as a distance indicator is dust extinction. From measurements of wavelength-dependent extinction and polarimetry, the extragalactic dust obscuring light from SNe Ia in a number of cases appears to have different properties compared with dust in the interstellar medium (ISM) of the Milky Way (MW): both the total-to-selective extinction ratio, R_V , and the Serskowski polarization parameter λ_{max} (Serkowski et al. 1975) are often found to be significantly lower (e.g., Phillips et al. 2013; Amanullah et al. 2014; Patat et al. 2015; Zelaya et al. 2017; but see Amanullah et al. 2015 and Huang et al. 2017 for an example of high extinction but MW-like R_V).

To account for the “peculiar” dust properties for SNe Ia, it has been suggested that scattered light by dust in a circumstellar medium (CSM) associated with an SN Ia may provide an explanation for both the low values of R_V (Wang 2005; Patat et al. 2006; Goobar 2008) and λ_{max} (Patat et al. 2015; Hoang 2017). Observationally, CSM indeed seems to be present for at least some SNe Ia, as evidenced by the detection of SN-CSM interactions (e.g. Hamuy et al. 2003; Aldering et al. 2006; Dilday et al. 2012), blueshifted and time-varying Na I or K I absorption features (e.g., Patat et al. 2007; Simon et al. 2009; Fox & Filippenko 2013; Sternberg et al. 2014; Graham et al. 2015), and the imbalance between the blue- and redshifted Na I absorption components (Sternberg et al. 2011; Foley et al. 2012; Maguire et al. 2013; Phillips et al. 2013). On the other hand, stringent limits on CSM density has been placed on two of the nearest SNe Ia, SN 2011fe and SN 2014J (e.g., Chomiuk et al. 2012; Pérez-Torres et al. 2014; Margutti et al. 2014; Brown et al. 2015; Harris et al. 2016; Johansson et al. 2017). Indeed, for most SNe Ia, observational evidence points in the direction of interstellar dust being at least the dominant cause for extinction, including those that are highly reddened (e.g., Patat et al. 2007; Chotard et al. 2011; Phillips et al. 2013; Patat et al. 2015; Maeda et al. 2016; Zelaya et al. 2017; Huang et al. 2017; Bulla et al. 2017). The low values of R_V and λ_{max} for some SNe Ia may then be the result of the dust grain size distribution in some of the host galaxies being different from the MW and/or possibly having been altered by SN radiation (e.g., Hoang 2017). In short, the nature and properties of extragalactic dust toward SNe Ia have been a long standing puzzle, and a deeper understanding is important for cosmology, SN progenitor (for a recent review, see, e.g., Maoz et al. 2014), and ISM studies.

One possible approach that can help unravel this puzzle is to explore whether or how the extinction and the EWs of absorption features for SNe Ia may vary with time. For CSM, Wang (2005) and Brown et al. (2015) showed that by including multiply scattered photons the visual extinction, A_V , would decrease with time, owing to the delayed arrival of short-wavelength photons. To-date this has not been observed for dust in the CSM (though it may have been detected for dust in the ISM (Bulla et al. 2017)). The EWs for some of the absorption features are also expected, and actually observed, to change over time due to variable CSM ionization conditions induced by SN radiation (e.g., Patat et al. 2007). However, the EWs are not expected to vary in the same way as A_V . In fact, for some absorption features, no variation is expected (Patat et al. 2007; Graham et al. 2015).

For ISM, Patat et al. (2010, P10) and Förster et al. (2013, F13) simulated column density maps following a power law power spectrum and argued that due to the non-uniformity of the column density and the expansion of the projected SN photosphere, the Na I absorption EW and extinction, respectively, would likely vary with time. The effects were forecast to be detectable for the EW and

significant for extinction. In contrast to the CSM scenario, if time variations of both are detected for a SN Ia, they should be correlated.

In this paper, we re-examine the effects of non-uniform ISM density on extinction and absorption EWs, for two purposes. First, to determine whether the observation of time variation of extinction and absorption EWs can be used to distinguish the two major extragalactic dust scenarios for SNe Ia. Second, for SN cosmology, it is important to determine the magnitude of time variation for extinction due to interstellar dust with non-uniform column density. This is especially true as the sum of the observational evidence so far suggests that, though the extragalactic dust properties may be peculiar (i.e., not MW-like) for SNe Ia, the extinction is likely caused predominantly, if not exclusively, by dust in the host galaxy ISM and not CSM associated with SNe. Our main departure from P10 and F13 concerns the appropriate level of ISM variation on the scale of a SN Ia photosphere at a given average column density.

This paper is organized as follows. In § 2, using observations of MW dust emission, we present a way to determine the normalization for the typical ISM column density fluctuations on the scale of SN photospheres at a given column density. In § 3, we compare the predictions based on this normalization with the observations of two SNe Ia with high extinction, SN 2012cu and SN 2014J. We also discuss SN 2006X, using it to contrast the observational signatures of non-uniform ISM and a light echo. We conclude in § 4. Throughout this paper, we assume constant dust-to-gas ratio (e.g., Padoan et al. 1997; Miville-Deschênes et al. 2007). For simplicity, all SN phases are taken relative to B -band maximum.

2. ISM DENSITY POWER SPECTRUM NORMALIZATION

ISM column density variations on scales from $\gtrsim 10$ pc to ~ 500 AU have been shown to follow a power law power spectrum, having a spectral index γ typically between -2.5 and -3.6 (e.g., Gautier et al. 1992; Schlegel et al. 1998; Deshpande 2000; Padoan et al. 2006; Miville-Deschênes et al. 2007; Roy et al. 2010). On smaller scales, column density variations down to $\lesssim 10$ AU have been observed (e.g., Dieter et al. 1976; Diamond et al. 1989; Heiles 1997; Weisberg & Stanimirović 2007; Lazio et al. 2009; Stanimirović et al. 2010). The same kind of power law behavior is found for the small scale fluctuations (e.g., Gibson 2007; Roy et al. 2012). Deshpande et al. (2000, D00) used 1D simulations to demonstrate that a scale-free power law power spectrum with $\gamma = -2.75$ extending from a few pc down to AU scales can explain the frequency of small scale structures in H I. More recently, Dutta et al. (2014) found for ISM density fluctuations on ~ 10 AU scales that the spectral index is the same as that for pc scale fluctuations and the upper limit for the amplitude is consistent with the pc scale fluctuation amplitude. This bolsters the suggestion made by D00 that ISM density fluctuations on scales from a few pc down to $\lesssim 10$ AU can be described by a scale-free, statistically isotropic and homogeneous power law power spectrum.

2.1. Summary of Relevant Results in P10 and F13

P10 pointed out that if there are ISM structures on such small scales in the MW then SNe Ia can be used to probe small-scale fluctuations in the host galaxy ISM. The SN photospheres have diameters of up to ~ 800 AU during the photospheric phase (within 100 days after explosion (P10)). As the photosphere (and its projection, the photodisk) of a SN Ia expands, its light is essentially sampling the average enclosed ISM column density. Thus, for example, the Na I absorption feature may vary with time (this would apply to the absorption of other atomic or molecular species if their column

density is in the right range; see Section 3.2). Following the suggestion in D00 that the power law power spectrum extends down to $\lesssim 10$ AU scales, P10 explored this possibility by simulating ISM column density maps with a width of 1024 AU and $\gamma = -2.8$. P10 considered the cases where the peak-to-peak fluctuation amplitudes were $\Delta N = \langle N \rangle$ and $2\langle N \rangle$, and showed in each case that there could be observable variations of EW(Na I) between phases of -10 and $+50$ days, depending on the mean density, $\langle N \rangle$. During this period, the photodisk increases from approximately 120 AU to 640 AU across (P10).

In a similar way, F13 simulated dust column density maps. Compared with P10, they used $\gamma = -2.75$ (slightly shallower), a width of 2048 AU (twice as large), and a peak-to-peak fluctuation amplitude of $\Delta N = 2\langle N \rangle$ (similar). They found that the SN extinction, which is proportional to the mean column density over the photodisk, would likely vary with time by a substantial amount over a period spanning 140 days from the time of explosion. Their Figure 8 showed especially dramatic variations within 60 days after explosion, corresponding to a phase of approximately 43 days (e.g., Hayden et al. 2010). This is the period when most light curve measurements for cosmology applications are made.

Neither P10 or F13 made clear how the fluctuation amplitudes for their simulated ISM density maps were chosen. In the next subsection we will set the normalization for the power spectrum based on MW dust emission observations and this will in turn provide the typical amplitude of fluctuation on the scale of a SN photodisk.

2.2. Normalization for ISM Fluctuations

Given a power law power spectrum for a 2D density field, $P(k) \sim k^\gamma$, one can compute the structure function (Lee & Jokipii 1975), $S(d)$, which is the variance for two points separated by a distance d :

$$S(d) = \sigma^2(d) \sim d^{-\gamma-2} \quad (1)$$

This is approximately the same as the variance within a disk with diameter d (see, e.g., Brunt & Heyer 2002). This result can be obtained by exploiting the approximate equivalence between a circular tophat window function with diameter d in configuration space, corresponding to the photodisk, and a circular tophat window function with a diameter $\sim 1/d$ in k -space, and then integrating $P(k)$ outside of this window function.

Miville-Deschênes et al. (2007, MD07) re-analyzed the IRAS data for 55% of the sky. From the intensity map of the 100 μm emission from cirrus clouds, they found a power law for the power spectrum at the pc scale (see below concerning the conversion from angular to physical scales) with $\gamma = -2.9 \pm 0.2$. Using the relationship between the power spectrum and the structure function, they provided the following normalization for the RMS of the 100 μm emission in the regime $\langle I_{100} \rangle > 10$ MJy/sr ¹,

$$\sigma_{I_{100}}(\theta) = 0.1 \langle I_{100} \rangle^{1.55} \left(\frac{\theta}{12.5^\circ} \right)^{-\gamma/2-1} \quad (2)$$

where I_{100} is the intensity of the 100 μm emission and θ the angular scale of interest.

¹ Note the power in Equation (18) of MD07 should be 1.55 instead of 1.5. This follows from Equation (8) in MD07. Otherwise there would be a 10% mismatch for the normalization at the $\langle I_{100} \rangle = 10$ MJy/sr boundary.

2.2.1. Normalization for Extinction Fluctuations

The 100 μm emission can be converted to extinction using the precepts of Schlegel et al. (1998)

$$\langle A_V \rangle \approx 0.050 \langle I_{100} \rangle$$

Thus the condition $\langle I_{100} \rangle > 10 \text{ MJy/sr}$ corresponds to $\langle A_V \rangle > 0.5 \text{ mag}$.

To place these results on the scale of a SN photosphere, we also need to convert the angular reference scale used in MD07 (12.5°) to a physical scale. The distances to the cirrus clouds found in the literature are typically between 100 pc and 750 pc (Benjamin et al. 1996; Grant & Burrows 1999; Szomoru & Guhathakurta 1999), with one group reporting a distance of 1.8 kpc (Jackson et al. 2002). These distances are consistent with a minimum distance set by the “local cavity” reported by Welsh et al. (2010, and references therein) — roughly within a 80 pc radius around the solar system, there is little Na I, often used as a tracer for dust. Thus conservatively we use a distance of 80 pc, which converts 12.5° to approximately 18 pc; using larger distances would further suppress the implied density fluctuations on the scale of a SN photosphere. In addition, the fact that MD07 dealt with fixed angular scale meant variance on larger and larger physical scales were added in the integral for the total variance along the line of sight, whereas we need a fixed physical reference scale. One can work out the geometric correction factor, $1/\eta = \sqrt{-\gamma - 1}(h/H)^{-\gamma/2-1}$, where h and H are the lower and upper limits of the integral for the total variance. Taking the lower limit of $h = 80 \text{ pc}$, η is typically between 1.5 and 3, depending on whether one sets the upper limit H to be 750 pc or 1.8 kpc, and depending on the value of γ .

We can now rewrite Equation 2 as

$$\sigma_{A_V}(d) = \left(\frac{0.52}{\eta} \right) \langle A_V \rangle^{1.55} \left(\frac{d}{18 \text{ pc}} \right)^{-\gamma/2-1}, \quad \langle A_V \rangle > 0.5 \text{ mag.} \quad (3)$$

To get a better sense of the expected fluctuation amplitude for A_V , we will use 800 AU as the reference scale, which is the extent of the photodisk at the end of the photospheric phase. Assuming a typical value of $\gamma = -2.9$, we obtain,

$$\sigma_{A_V}(d) = \left(\frac{0.012}{\eta} \right) \langle A_V \rangle^{1.55} \left(\frac{d}{800 \text{ AU}} \right)^{0.45}, \quad \langle A_V \rangle > 0.5 \text{ mag.} \quad (4)$$

The comparison between Equations 3 and 4 shows that a key factor in this conversion is $\left(\frac{800 \text{ AU}}{18 \text{ pc}} \right)^{-\gamma/2-1} = 0.022$ for $\gamma = -2.9$.

The normalization for $\langle I_{100} \rangle < 10 \text{ MJy/sr}$ has a different dependence on $\langle I_{100} \rangle$ (MD07). Most SNe Ia used as cosmological probes have $A_V < 0.5 \text{ mag}$, corresponding to this case. Analogous to Equations 3 and 4, then we have,

$$\sigma_{A_V}(d) = \left(\frac{0.35}{\eta} \right) \langle A_V \rangle \left(\frac{d}{18 \text{ pc}} \right)^{-\gamma/2-1}, \quad \langle A_V \rangle < 0.5 \text{ mag} \quad (5)$$

$$\sigma_{A_V}(d) = \left(\frac{0.0078}{\eta} \right) \langle A_V \rangle \left(\frac{d}{800 \text{ AU}} \right)^{0.45}, \quad \langle A_V \rangle < 0.5 \text{ mag.} \quad (6)$$

Just as with Equation 4, in the conversion from using 18 pc as the reference length to 800 AU for Equation 6, for convenience we set $\gamma = -2.9$. If we assume that this $\sigma_{A_V}(d)$ - $\langle A_V \rangle$ relationship for the

MW applies to SN host galaxies, then Equations 4 and 6 make clear that during the photospheric phase the extinction due to non-uniform interstellar dust is not expected to vary much for a SN Ia.

Finally, it is instructive to see how the extinction fluctuation RMS depends on the phase. Employing the equation for the diameter of the photodisk t days after explosion given by P10, in terms of the phase T ($= t + 17.4$; e.g., Hayden et al. 2010), for $\gamma = -2.9$, we can write:

$$\sigma_{A_V}(T) \sim \left(\frac{(7.0 + 10.6 e^{-(T-17.4)/36.5}) (T - 17.4)}{800 \text{ AU}} \right)^{0.45} \quad (7)$$

2.2.2. Normalization for Column Density Fluctuations

To find the typical normalization for the column density fluctuations, we follow similar steps as in Section 2.2.1. From Lagache et al. (2000), we obtain the conversion from $\langle I_{100} \rangle$ to $N(\text{H I})$ and given the ratio of $N(\text{Na I})/N(\text{H I})$ is approximately constant for the MW (e.g., Murga et al. 2015), we find

$$N(\text{Na I}) = 0.5 \times 10^{12} \langle I_{100} \rangle \text{ cm}^{-2} \quad (8)$$

From this relation, we obtain the RMS of the column density fluctuation,

$$\sigma_N(d) = \left(\frac{d}{18 \text{ pc}} \right)^{-\gamma/2-1} \text{ cm}^{-2} \begin{cases} \left(\frac{1.5 \times 10^{11}}{\eta} \right) \left(\frac{\langle N \rangle}{10^{12}} \right)^{1.55} & , \quad \langle N \rangle > 5 \times 10^{12} \text{ cm}^{-2} \\ \left(\frac{3.5 \times 10^{11}}{\eta} \right) \left(\frac{\langle N \rangle}{10^{12}} \right) & , \quad \text{otherwise} \end{cases} \quad (9a)$$

$$(9b)$$

Using a reference length of 800 AU (convenient for SN), and the typical value of $\gamma = -2.9$, the RMS of the Na I column density is given by,

$$\sigma_N(d) = \left(\frac{d}{800 \text{ AU}} \right)^{0.45} \text{ cm}^{-2} \begin{cases} \left(\frac{3.3 \times 10^9}{\eta} \right) \left(\frac{\langle N \rangle}{10^{12}} \right)^{1.55} & , \quad \langle N \rangle > 5 \times 10^{12} \text{ cm}^{-2} \\ \left(\frac{7.8 \times 10^9}{\eta} \right) \left(\frac{\langle N \rangle}{10^{12}} \right) & , \quad \text{otherwise} \end{cases} \quad (10a)$$

$$(10b)$$

which makes clear the typical amplitude of fluctuations around $\langle N \rangle$ for SNe Ia.

3. COMPARISON WITH OBSERVATIONS

In this section we compare the predictions from the previous section with the observations of two well-observed, highly reddened SNe Ia, SN 2012cu and SN 2014J. We also discuss SN 2006X, a third highly reddened SN Ia, and contrast our predictions with the effects of a light echo.

3.1. SN 2012cu

SN 2012cu has one of the highest extinction values ($A_V \approx 2.9$ mag) for a SN Ia (Amanullah et al. 2015; Huang et al. 2017). Several lines of observational evidence point to dust in the ISM as the dominant, and possibly the only, source for the extinction (Huang et al. 2017).

Table 1. Predicted RMS within the Photodisk for SN 2012cu at Representative Phases

Phase	0 days (at max)	+23.2 days	+82.6 days
γ	$\sigma_{A_V}(240 \text{ AU})$	$\sigma_{A_V}(430 \text{ AU})$	$\sigma_{A_V}(800 \text{ AU})$
-2.9 (typical)	0.018	0.024	0.033
-2.5 (lowest)	0.13	0.15	0.17

Huang et al. (2017) found SN 2011fe and SN 2012cu to be good spectroscopic twins (see Fakhouri et al. 2015). Their observations were also closely matched in phase for 10 epochs between -6.8 and $+23.2$ days. Using SN 2011fe as the template, the extinction was determined to be $A_V = 2.944$ mag with a RMS of 0.043 ± 0.010 mag. This RMS around the time-averaged A_V across the 10 phases likely has some contribution from the fact that SN 2012cu and SN 2011fe are not perfect twins, as discussed in Huang et al. (2017). Non-uniform interstellar dust, however, could also contribute to the apparent variation. Below we explore the implication of this possibility.

Between the phases of -6.8 and $+23.2$ days, the photodisk has a diameter between 160 and 430 AU (P10). To calculate the expected RMS for the fluctuation within a disk of 430 AU, $\sigma_{A_V}(430 \text{ AU})$, we will set $d = 430$ AU and $\langle A_V \rangle = 2.944$ mag, and assume $\eta = 2$, in Equation 3. The results are summarized in Table 1. For completeness we also show $\sigma_{A_V}(240 \text{ AU})$ (at maximum) and $\sigma_{A_V}(800 \text{ AU})$ (corresponding to a phase of approximately 82.6 days, the end of the photospheric phase).

The predicted $\sigma_{A_V}(430 \text{ AU})$ is not quite the same as what was observed, which is the RMS of the observed A_V over time. The variation across the phases are correlated for a given SN because the SN photodisk at any given phase encloses a smaller photodisk at an earlier observed phase. However, the value for this quantity sets the upper limit for how much the extinction *can* vary across phases up to 23.2 days.

Two things are made clear in Table 1: 1) even for the shallowest value of $\gamma = -2.5$, the variation is much smaller than what is assumed in F13 (where the peak-to-peak amplitude was set to be $\Delta N = 2\langle N \rangle$ on the scale of 2048 AU, or equivalently, $\Delta A_V = 2\langle A_V \rangle$, and corresponds to a RMS of $\sigma_{A_V} \approx 14\% \times \langle A_V \rangle$ on the scale of 430 AU); 2) the small observed RMS around the time-averaged A_V for SN 2012cu is consistent with the expectation for a scale-free power law power spectrum, even though it may be difficult to separate exactly the contributions from non-uniform dust vs. small differences in the intrinsic spectra between SN 2012cu and SN 2011fe.

Note that Table 1 provides the upper limits for the contribution from non-uniform interstellar dust to the RMS for the observed A_V across phases for SN 2012cu, even if observations earlier than -6.8 days for SN 2012cu were included.

Finally, for $A_V < 0.5$ mag (relevant for SNe Ia typically used in a cosmological study), the RMS fluctuation from Equation 5 is typically on the order of 0.01 mag or below, even for the shallowest value of $\gamma = -2.5$, and even if the phase coverage spans the entire photospheric phase (~ 100 days after explosion).

3.2. SN 2014J

SN 2014J has an extinction of $A_V = 1.9$ (e.g., Amanullah et al. 2014; Foley et al. 2014; Gao et al. 2015). Despite having a low R_V of $1.4 - 1.7$, here too, many lines of evidence point to dust in the ISM as the dominant, and likely the only, source for the extinction (Kawabata et al. 2014; Margutti et al. 2014; Pérez-Torres et al. 2014; Patat et al. 2015; Brown et al. 2015; Maeda et al. 2016; Johansson et al. 2017; Bulla et al. 2017; also see Appendix).

3.2.1. ISM Absorption Variations

P10 made detailed, quantitative predictions for the amplitudes of EW(Na I) variation by simulating ISM maps for a width of 1024 AU and a spectral index of $\gamma = -2.8$. They considered different combinations of average column density values ($\langle N \rangle = 10^{11}, 10^{12}$, and 10^{13} cm^{-2}), peak-to-peak fluctuation amplitudes ($\Delta N = \langle N \rangle$ and $2\langle N \rangle$), and Doppler parameter values ($b = 1$ and 5 km s^{-1}). The results are tabulated in their Table 2. They pointed out that for $N > 10^{13} \text{ cm}^{-2}$, the absorption will be saturated and that as a result, in this case, the EW will only weakly vary with column density fluctuations. The largest EW variation is achieved for the average column density of $\sim 10^{12} \text{ cm}^{-2}$. For the same column density fluctuation amplitude, a higher value of b would result in greater variation in EW.

Based on the predictions of P10, it was already clear that attempting to detect small scale density fluctuations of the foreground ISM in the host galaxy by measuring EW variations would be challenging. Even with an optimal parameter combination, the RMS of the EW variation is \sim a few mÅ (see their Table 2).

To calculate the column density fluctuation RMS based on the normalization determined in this paper, we set $d = 640 \text{ AU}$, the maximum photosdisk extent in P10 at a phase of +50 days, and $\langle N \rangle = 10^{12} \text{ cm}^{-2}$, with $\gamma = -2.8$ (same as used in P10) and $\eta = 2$, and obtain $\sigma_N(640 \text{ AU}) = 5.5 \times 10^9 \text{ cm}^{-2}$ from Equation 9b. This is much lower than the RMS values used by P10. For the same mean column density, the level of EW variation is approximately proportional to the fluctuation RMS of the column density (P10). Thus even under the optimal combination of parameters in P10, the RMS of EW variation would be $\lesssim 0.1 \text{ mÅ}$.

The comparison between the density fluctuation levels chosen by P10 and F13 and our predictions (using $\gamma = -2.9$) are presented in Figure 1.

EW(Na I) would not be very responsive to column density variations if the Na I absorption is saturated. For a SN with multiple non-overlapping absorbing components, among which at least some have an average column density in the neighborhood of 10^{12} cm^{-2} , the EW fluctuation RMS due to the different components will add in quadrature. Thus for the same high total column density, a SN with the optimal component distribution would have the highest variation in EW(Na I). SN 2014J is close to such a case. But even in this case, the total RMS for EW variation would still be very small (our rough estimate is $\lesssim 0.2 \text{ mÅ}$). In general, for a multi-component absorption system, if the b values are small, ΔEW would be negligible for each component. On the other hand, if the b 's are large, fewer non-overlapping, unsaturated components can fit into the available “velocity space” of a galaxy (on the order of hundreds of km/s). Thus it is difficult to see a scenario in which the total RMS would rise to even 1 mÅ for SNe Ia due to ISM with non-uniform density.

For the Na I absorption system, Foley et al. (2014), Ritchey et al. (2015), and Graham et al. (2015) showed that there were no detectable EW variation between phases -11 to $+47$ days. Maeda et al.

(2016) determined the Na I absorption for SN 2014J to be *exclusively* in the ISM. They did not see variation in the absorbing systems toward the SN out to a phase of +255.1 days (or within a pencil beam of ~ 0.02 pc). Furthermore they presented evidence for ISM column density variation on the scale of 20 pc by observing the diffuse light of the host galaxy (M82) around the SN. These findings are consistent with the predictions of this paper.

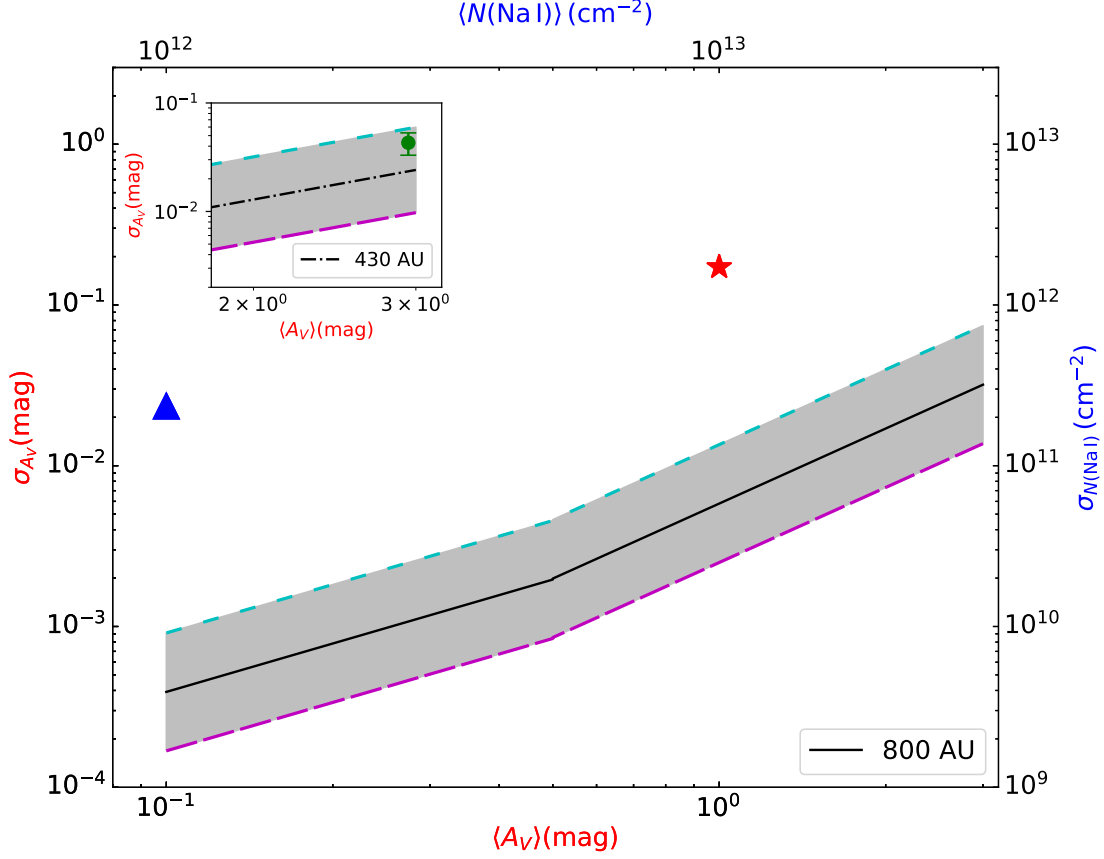


Figure 1. The solid line represents the RMS at the 800 AU scale using $\gamma = -2.9 \pm 0.2$ from MD07 (Equation 4), with the cyan (short-dashed) and magenta (long-dashed) lines marking the shallow and steep ends of the 1σ spread, respectively. The blue triangle indicates the RMS value used in the simulations of P10 (for $N(\text{Na I})$), and the red asterisk, the RMS used in the simulations of F13 (for A_V), respectively, translated to the 800 AU scale. The inset shows the density fluctuations at the smaller scale of 430 AU (shifted downward from the RMS for the 800 AU scale by about 25%), corresponding to the phase of 23.2 days. The green dot with error bars shows the RMS variation of the observed A_V across phases for SN 2012cu and therefore will be smaller than the RMS at the latest observed phase shown here.

3.2.2. Extinction Variations

Brown et al. (2015) examined the time variation of the extinction for SN 2014J. They found that if they modeled and applied scattering by circumstellar dust to SN 2011fe, used as the template, the observations of SN 2014J do not agree with the model predictions. The unavailability of a good twin for SN 2014J at the present limits quantitative measurements of the A_V variation. Here we will just state that, given the observed A_V value of 1.9 mag, the expected upper limits on the RMS for A_V

variation over the phase range of -10 to $+50$ days are: 0.014 mag for $\gamma = -2.9$, and 0.11 mag for $\gamma = -2.5$.

We note that light echoes have been observed for SN 2014J (Crotts 2015; Yang et al. 2017) at late phases (> 200 days). Bulla et al. (2017) confirmed the estimate for the distance between the SN and dust given by Yang et al. (2017), and in their analysis concluded the distance is too large for the echoed light to enter the line of sight during the range of phases (approximately -5 to $+25$ days) covered by Brown et al. (2015).

In summary, for SN 2012cu and SN 2014J, both of which are highly reddened, there is little evidence for the time variation of either extinction (SN 2012cu) or EW(Na I) (SN 2014J). This is consistent with the small level of variations due to non-uniform ISM density we have predicted.

3.3. SN 2006X

SN 2006X is a highly reddened SN Ia that exhibited variable Na I absorption and variation in the observed $E(B - V)$. The variation in Na I absorption has been attributed either to CSM (Patat et al. 2007) or a highly specialized ISM configuration (Chugai 2008). Since we predict no detectable variation in Na I absorption due to random non-uniformity of the Na I column density across an expanding SN photodisk, we agree that the observed Na I absorption variation must be due to other causes. The observed change in $E(B - V)$ over a phase range of -4 to $+35$ days has been interpreted as resulting from a light echo (Bulla et al. 2017), a conclusion that is consistent with the spatially resolved light echo seen from late-time imaging with *HST* (Wang et al. 2008; Crotts & Yourdon 2008). These analyses agree that the dust causing the light echo has an inferred distance $\gtrsim 20$ pc in the foreground, placing it in the ISM. The observational signatures of non-uniform ISM are quite different from those of a light echo, as we now describe.

The scattered photons arriving from a light echo are delayed with respect to the direct light, producing both a brightening and a bluer color. Because the delayed photons arrive from an earlier portion of the light curve, the color and brightness (and the inferred color excess and extinction) become more strongly perturbed after maximum light. In addition, the perturbations change smoothly with phase. However, for the case of non-uniform dust, the observed extinction has a random scatter whose amplitude about the mean decreases with time. This occurs because each new epoch has a subset of its photodisk that backlights the same region of ISM that was backlit by the previous epoch. Thus, the extinction distribution across the photodisk at a new epoch will include the (area-averaged) extinction deviations of earlier epochs. As a result, the observable extinction deviations with respect to the (area-averaged) extinction for the largest photodisk observed (i.e., the extinction at the last observed epoch) will be larger for earlier epochs.

To summarize, the contrast between these phenomena is:

- For a light echo, earlier phases will have values more consistent with each other, while later phases will show brightening and bluer colors. This will result in large variations in the inferred $E(B - V)$ and A_V for highly reddened SNe if the dust distance is in the right range (Bulla et al. 2017).
- For non-uniform ISM dust, the later phases will have values more consistent with each other while earlier phases will show larger and random (but correlated) variations. (For example, see Figure 8 for F13: while the variations in F13 are over-stated, as discussed here, the trends are

qualitative correct). This effect is independent of the distance between the SN and foreground dust, and we find that typically it will be small even for highly reddened SNe.

4. CONCLUSIONS

Even though there is clear evidence for ISM density fluctuations on scales 10 AU or even below, we show that due to the steep spectral index of the ISM column density power spectrum and because the SN photodisk is much smaller ($\lesssim 800$ AU in diameter) than the typical ISM structure ($\gtrsim 10$ pc), substantial variations on $\gtrsim 10$ pc scales translate to much smaller fluctuations on the scale of SN photodisk. We provide a way to set the normalization for ISM density fluctuations on length scales relevant to SNe Ia based on MW dust emission observations (Miville-Deschênes et al. 2007). We have found that the expected time variations of EW(Na I) and A_V for SNe Ia due to non-uniform ISM would be typically much smaller than the predictions in Patat et al. (2010) and Förster et al. (2013), respectively. The observations of two SNe Ia highly reddened by at least mostly interstellar dust, SN 2012cu and SN 2014J, are consistent with the results of our analysis. The observed color variations for SN 2006X have been attributed to a light echo (Bulla et al. 2017) rather than non-uniform ISM, and so are also consistent with our analysis.

We therefore conclude, if non-uniform ISM density in the SN host galaxy follows a scale-free power law power spectrum:

1) The expected variation of extinction for SNe Ia with $A_V < 0.5$ mag is negligible and is certainly smaller than what is currently scientifically relevant for SN cosmology. This, combined with mounting evidence that interstellar dust is likely the dominant source of reddening for SNe Ia, significantly reduces the concern about time variation of extinction for SNe Ia due to non-uniform dust density in cosmological studies.

2) For the study of extragalactic ISM density non-uniformity, it may be possible to detect small variations in extinction across phases for a highly reddened SN. The RMS can be as large as ~ 0.1 mag over a phase range of, say, from -10 to $+50$ days, with the shallowest spectral index ($\gamma = -2.5$). A larger phase coverage would be better for this purpose (earlier observations would especially help as it allows the observation to sample closer to the full extent of the photodisk at the last observed phase). Huang et al. (2017) demonstrated that in order for such a detection to be feasible, it is important to not only have an unreddened SN that is well-twinning with the dust-obscured SN, but the observed phases of these two SNe need to be closely matched.

3) It is very unlikely for the EW of the ISM absorption features to vary with time in any significant way ($\sigma_{\text{EW}} \lesssim 1 \text{ m\AA}$), even for highly reddened SNe Ia with optimal velocity component distribution. Thus any detection of temporal variation in the absorption EW is likely due to other causes.

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APPENDIX

 R_V FOR RAYLEIGH SCATTERING

In the course of this study, we encountered a comment in Foley et al. (2014) concerning the lowest possible R_V in the limit of Rayleigh scattering. As is well known, for molecules and small dust particles ($\lesssim 10$ nm for optical wavelengths; Kruegel 2003), the scattering cross section depends on the wavelength as λ^{-4} . Contribution from Rayleigh scattering has been invoked as a possible explanation for the sharp blue rise in spectropolarimetry for sight lines toward certain stars (Andersson et al. 2013) in the MW (scattering by a reflection nebula) and toward SN 2014J (Patat et al. 2015; Hoang 2017), respectively. In the limit of Rayleigh scattering, R_V would be given by $R_V^{Rayleigh} = (A_B/A_V - 1)^{-1} = (\sigma_B/\sigma_V - 1)^{-1} = ((\lambda_B/\lambda_V)^{-4} - 1)^{-1} \approx 0.81$ (e.g., Bessell 1990). If the refractive index is complex, in addition to scattering, there is absorption, which goes as $\sim \lambda^{-1}$ (Kruegel 2003). In this case the net power, p , for extinction due to small dust particles would be between -1 and -4 . For SN 2014J, $R_V \approx 1.4$ and the effective power p is between -2.4 and -2.1 (Amanullah et al. 2014), whose absolute value is well below the Rayleigh scattering limit. Therefore while the R_V value may be extreme for SN 2014J by MW standards, it is not physically forbidden based on the wavelength dependence of Rayleigh scattering, and does not rule out pure ISM dust on this basis alone.

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