 powering a Reverse Osmosis (RO) desalination system usin Computational Fluid Dynamics (CFD) and Taguchi method Mohammad Hassan Khanjanpour, Akbar A. Javadi* Department of Engineering, University of Exeter, Exeter, EX4 4QF, UK. *Corresponding author *Akbar A. Javadi Tel: +44 1392 723640, Email: A.A.Javadi@exeter.ac.uk Email: A.A.Javadi@exeter.ac.uk A.Javadi@exeter.ac.uk A.Javadi A.Javadi@exeter.ac.uk A.Javadi A.Javadi	1	Optimization of a Horizontal Axis Tidal (HAT) turbine for
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26 Abstract

27 Horizontal Axis Tidal (HAT) turbines can be used to power RO (reverse osmosis) desalination 28 systems. The greatest weakness of these turbines is the high price of design, development, and 29 manufacturing. Traditionally, optimization of turbine geometry is achieved by running several 30 numerical models of the turbine which can become time consuming and expensive. The Taguchi-31 CFD (Computational Fluid Dynamics) approach has recently been introduced as an inexpensive 32 and rapid tool for optimizing industrial devices. This technique can be used as a straightforward 33 solution for optimization of geometry of HAT turbines. In this work, a conceptual design of a tidal 34 power reverse osmosis (TPRO) desalination unit was proposed. Subsequently, the geometry of the 35 HAT turbine, which can power the whole desalination system, was optimized with combination 36 of only 16 CFD simulations using the Taguchi method. The effects of blade size, number of blades, 37 hub radius, and hub shape were studied and optimized. The Taguchi results revealed that the most 38 important parameters influencing the power output of HAT turbine are the number of blades, size 39 of blade, hub radius, and hub shape respectively. Moreover, the results of the superposition model 40 showed that the minimum signal-to-noise ratio (SNR) is 21% less than the amount achieved in the 41 Taguchi approach. The power coefficient (C_p) of the optimized HAT turbine was 0.44 according 42 to the results of CFD simulations, which was 10% higher than that of the baseline model (0.40) at 43 tip speed ratio (TSR) of 5. The weight of the optimized model was less than the baseline model by 44 17%. The results of this study provide a comprehensive guidance for horizontal turbine 45 optimization process.

Keywords: HAT Turbine, Desalination, Taguchi method, ANOVA, signal-to-noise ratio,
Computational fluid dynamics.

49	Nomencla	ture (alphabetical order)		
	ANOVA	Analysis of variance	RO	Reverse osmosis
50	A_t	Area of the blades (m^2)	R	Turbine radius (m)
50	C_p	Power coefficient	S	Area of a blade (m^2)
	C_m^r	Torque coefficient	SNR	Signal-to-noise ratio
51	ED	Electrodialysis	SST	Shear Stress Transport
	ERD	Energy recovery device	Т	Torque (N.m)
52	G	Calculated response	TPRO	Tidal power reverse osmosis
	HAT	Horizontal Axis Tidal	TSR	Tip speed ratio
53	L	Distance from center of hub (m)	T_c	computed response
	MVC	Mechanical vapor compression	T_q	Target quality
	n	number of experiments	U_{∞}	Water velocity (m/s)
54	n_b	Number of blades	VAT	Vertical Axis Tidal
	OA	Orthogonal array	X	Quadratic loss factor
55	Р	Power output (W)	α	Solidity ratio
55	P_n	Nominal output power (W)	β	Impact of each factor
56	PISO	Pressure Implicit Splitting of Operator	ρ	Water density (kg/m ³)
	PV	Photovoltaic	ψ	Mean of total mean SNRs
57	Q	Indicator blade	ψ^t	Predicted SNR
	QLF	Quadratic loss function	Ψ ω	Angular velocity (rad/s)
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65 **1. Introduction**

66 Water crisis is among the serious challenges that threatens human society's sustainable 67 development [1, 2]. According to a new report by WHO and UNICEF, by 2025, 1.8 billion people 68 will be living in countries or regions with absolute water scarcity [3, 4]. Even countries that are 69 currently rich in water resources, will face water shortage in future. Figure 1 shows the water 70 availability indicators due to climate change and population growth in the UK for 2050s [5]. The 71 indicator of water availability, which varies from -1 to 1, identifies the ratio of excess water 72 consumption over water supply of the most challenging months during the prediction period. It 73 can be seen from Figure 1 that, even a country like UK will experience water scarcity in coming 74 decades. Fortunately, since about 71% of the Earth's surface is covered with water [6], one of the 75 solutions for world's water crisis can be seawater desalination. However, seawater desalination 76 requires a significant amount of energy [7-10].

77 Most of the existing desalination systems are powered by energy from burning of fossil fuels [11, 78 12]. Renewable energy, in many cases, can be utilized to power desalination devices [13, 14]. Tidal 79 energy, utilizing ocean tidal currents, provides a reliable renewable resource with the advantage 80 of being highly predictable many years into the future and significantly greater in its energy density 81 compared to wind and solar energies, albeit intermittent on a daily or twice-daily time-scale [15]. 82 Ocean powered seawater desalination has become a new approach for desalination due to the 83 above-mentioned advantages [16-22]. However, the development of ocean powered seawater 84 desalination technologies is at its infancy and more investigation is needed before fully operational 85 systems are deployed and implemented.

87 Zhao and Liu [23] carried out a theoretical study on a tidal-powered solar distillation system. In 88 their innovative design, instead of running pumps with electricity, tidal energy was used to produce 89 energy for vacuum extraction as well as water intake. They performed hydrodynamic and thermal 90 analysis for the water intake and drainage system powered by tidal energy. Their proposed system 91 can only work efficiently in locations with a tidal level greater than 2 m, however, using storage 92 tank can stabilize energy requirement when tidal energy is used for powering water pump. A wave-93 powered RO desalination system was developed by Sharmila et al. [24] in India. Since 94 waves are transient and irregular source of energy throughout the year, it is essential to predict the 95 behavior of the system at various wave energy rates. Thus, they theoretically simulated the wave 96 energy profile and based on the obtained profile, they designed and developed a wave converter 97 that was suitable for the desalination system. Unlike wave energy which is influenced by speed of 98 the wind, the strength of tidal energy is influenced by the location and shape of the Earth which 99 makes tidal energy quite predictable [25]. Ling et al. [26] carried out an economic analysis of a 100 TPRO desalination system where the productivity of the desalination system and cost of freshwater 101 were compared with other methods. It was concluded that the TPRO desalination system could 102 save water costs between 30- 40% compared to the traditional RO system.

Tidal turbines, including the Vertical Axis Tidal (VAT) turbine and Horizontal Axis Tidal (HAT) turbine, can be used to power desalination systems. A HAT turbine contains a radial axis rotor which is parallel to the water stream. With its drag or lift style blades, which are usually perpendicular to the rotational axis, it can convert the kinetic energy of water to mechanical energy [27]. In VAT turbines, the radial axis rotor is perpendicular to the water stream and, similar to HAT turbines, their blades can be either drag or lift style [28]. Since the greatest weakness of tidal 109 turbines is the high cost of development and fabrication, using an inexpensive Taguchi method can110 be helpful for turbine developers to reduce design costs.

111 The Taguchi method, also known as the Robust Design method, is one of the powerful 112 optimization techniques in product design [29]. The fundamental principle of the Taguchi method 113 is to increase the efficiency of a product by reducing the number of tests required without 114 eliminating any parameters [30]. The Taguchi approach provides Orthogonal Arrays (OA) for the 115 execution of minimal tests to include a wide variety of variables for improved decision-making. It 116 also uses the signal-to-noise ratio (SNR) to measure the divergence of the output, from the target 117 value. The SNR is a criterion for quality assessment, and the OA is to provide minimal design 118 parameters simultaneously [31]. The target quality of performance is a key factor in the Taguchi 119 approach and must be indicated for each optimization procedure. It is possible to integrate the 120 Taguchi method with Computational Fluid Dynamic (CFD) models (the same way as other 121 optimization models have been combined with CFD [e.g., 32, 33]) to predict optimized factors.

122 Wang et al. [34] improved the performance of a vertical wind turbine by using the CFD-Taguchi 123 method. They characterized design parameters such as wave amplitude, wavelength, and twist 124 angle while the objective function was the power coefficient (C_p) . For the Taguchi method they 125 used a standard L9 (3⁴) OA. By accomplishing only nine CFD tests, they improved the output of 126 the vertical axis wind (VAW) turbine by 18%. Recently, Khanjanpour and Javadi [35], optimized the efficiency of a VAT turbine combining a mixed-level L_{18} (6¹*3³) Taguchi with 18 CFD 127 128 simulations. They studied the effects of ratio of chord/radius, maximum camber, camber position, 129 and twist angle on the performance of the VAT turbine. Their findings showed that, compared to 130 the initial design, the power output for the optimized VAT turbine was enhanced by 24%.

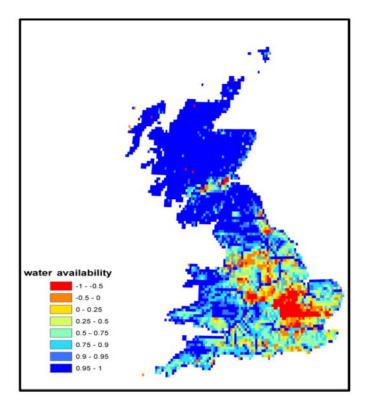




Figure 1. Water availability indicator for 2050s in the UK [5].

133 The main objective of the current work is to design and optimize the geometry of a HAT turbine 134 for powering a desalination system. Review of the previous research shows that the influence of 135 combinations of size of blades, number of blades, hub radius, and hub shape on the power output 136 of HAT turbines has not been investigated. The goal of optimization of these factors is to find a 137 lighter, cheaper and smaller turbine which can be used in shallow water. For this purpose, the 138 Taguchi method is used to optimize the turbine in order to identify a cost-effective geometry for 139 use in a RO desalination system. By using the Taguchi method and only 16 CFD simulations, the 140 effects of size of blades, number of blades, hub radius, and hub shape on power output of HAT 141 turbine are studied. Finally, a new range of optimized variables is defined and evaluated. 142 In addition, the dynamics of the fluid flow across the optimized and initial turbines is studied and 143 compared.

In what follows, the design of the desalination system is presented in Section 2. In Section 3, the details of a preliminary design of the baseline HAT turbine are given. Section 4 presents CFD simulation of the baseline turbine and validation of the model. In Section 5 the Taguchi method and the superposition model are used to find the optimum parameters of the turbine. In Section 6, a comprehensive CFD simulation of the baseline and the optimized cases is presented. Finally, Section 7 presents the conclusions and some recommendations for future work.

2. Design of the desalination system

151 2.1. Location of the desalination system

152 One of the prerequisites of development of a tidal seawater desalination system is to find coastal 153 areas with high-speed current, particularly in regions with low salinity, as salinity can affect the 154 energy consumption of RO unit [36]. Figure 2 illustrates the current speed and seawater surface 155 salinity around the UK. From this figure, it can be seen that there are numerous locations, which 156 are suitable for tidal-powered desalination system, especially in the straits and in narrow places 157 that have an appropriate space for harnessing tidal energy. The coastline of South East England is 158 suitable for installation of a TPRO desalination system; not only it has low salinity and high current 159 speed, but also in future it will have a higher demand for water (see Figure 2). Accordingly, for 160 the rest of this research, the mean tidal current velocity and salinity of water are assumed as 1 m/s 161 and 30 ppt respectively.

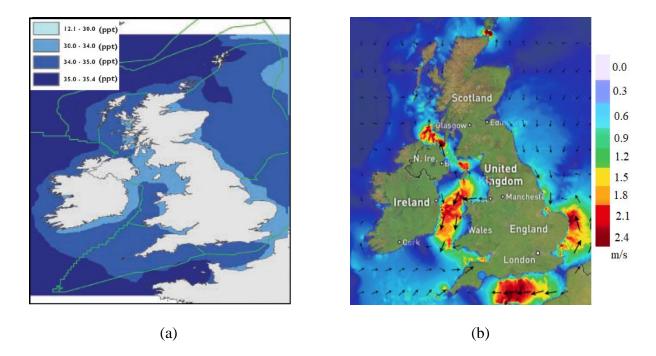


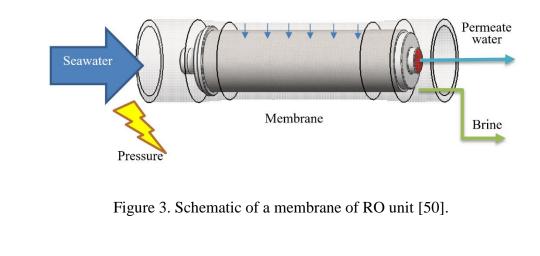
Figure 2. (a) The current speed [37] and (b) seawater surface salinity around UK [38].

163 2.2. RO unit

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164 A wide range of desalination technologies are available for producing fresh water from seawater. 165 Although some desalination devices are available commercially, most of them are in 166 the early stage of research and development. The selection of appropriate technology is affected 167 by the nature of the water source, the amount of collected water, and most importantly, the total 168 energy consumption [39]. The three most common systems that can be combined with sea power 169 are reverse osmosis (RO), electrodialysis (ED), and mechanical vapor compression (MVC) [40]. 170 The best desalination method which can be combined with tidal energy is Reverse Osmosis [41, 171 42]. Figure 3 shows a schematic of a membrane of a reverse osmosis unit. RO is a process where 172 pressurized seawater flows through a semipermeable membrane, separating freshwater from saline 173 water. The chemical potential of the solute, depending on temperature, salinity and pressure, is to 174 be equal on both sides of the membrane. By adding an external pressure to one side of the

175 membrane, clean water will flow to the other side to restore the chemical potential. The products 176 of the RO process are freshwater and the residue (concentrate or brine) of high salinity. The RO 177 method has unique advantages such as adjustable size and low price (almost 25% less than thermal 178 options), therefore, in this study RO is selected for the desalination system [43]. Recently, there 179 has been significant research on the use of RO system for sustainable water production [44-47]. 180 The characteristics of the membrane identify its capacity to enable water to be preferentially 181 transported over the solute. To ensure that water passes through the membrane, the pressure 182 difference between the feed part and the membrane permeate side should be considerably higher 183 than the osmotic pressure. This working pressure of RO must be about 3-5 bar according to existing 184 studies [48], however, several qualified RO industries are designing innovative products which 185 could be utilized with much less pressure [49].



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189 2.3 Conceptual design of the TPRO desalination system

A schematic of the conceptual design of TPRO desalination system using HAT turbine is
illustrated in Figure 4, adapted from reference [51]. The main components of the design and their
functions are as follows:

(1) Tidal turbine: powers the high-pressure pump and fills the water storage tank, (2) Water storage
tank: stabilizes the driving energy, (3) High-pressure pump: moves and pressurizes water from the
sea to the RO unit and water tank, (4) RO unit: desalinates saline water, (5) Booster pump: pumps
output water from energy recovery device (ERD) to the RO unit, (6) ERD: recovers the energy of
water output of RO unit, and (7) PV (Photovoltaic) panel and battery: provide the required
electricity for the booster pump.

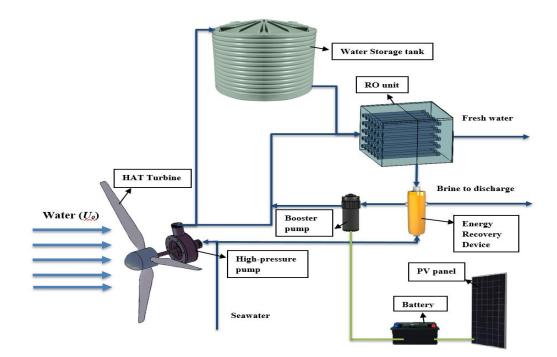


Figure 4. Schematic of the RO desalination system using a HAT turbine.

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The HAT tidal turbine extracts energy from the sea and runs the high-pressure water pump in order to provide the hydraulic pressure needed for the RO unit. In the proposed conceptual design, there is no need to convert kinetic energy to electricity in a generator, and then electricity to kinetic energy in an electric motor and finally use the kinetic energy to pressurize water in a pump. The kinetic energy is used directly to pressurize the water in the RO system. Moreover, the electricity harnessed from tidal power is usually wasted due to limited consumption during off-peak hours.
With proposed conceptual design, the turbine uses tidal energy to run a water pump and when the
system has adequate pressurized water, the energy of the movement can be stored in the water
storage tank to stabilize the driving energy.

Most of the components of the proposed system are available in the market and various companies offer these goods on a large scale. However, tidal turbine which is the most expensive and complex part is not supplied as a whole package. Therefore, in this study the tidal turbine is selected to be optimized to identify the smallest and cheapest geometry, which can provide the required power for the desalination system.

214 2.4. Energy required for desalination

In this section, the pressure required for desalinating 1 m³/h is determined. Some assumptions are necessary to estimate this pressure. The proposed conceptual desalination system has three major energy requirements: (1) energy for the RO unit, which has the highest energy consumption in the desalination systems [52-56], (2) energy for pumping of the seawater from the nearshore to the system, and (3) electricity consumption in the booster pump, which is used after ERD to pump water to the RO unit.

Energy consumption for modern RO desalination systems is between 2000-4000 Wh/m³ [17, 57, 58]. By using a more efficient ERD, the energy consumption inside the RO unit can be assumed as 2400 Wh/m3 for seawater with salinity of 30 ppt [59]. The energy usage for transferring seawater to RO unit and the storage tank in a standard desalination system is about 200 Wh/m³ [60]. According to Khanjanpour and Javadi [61], changes in roughness of the blades due to sticky sea animals and corrosion can decrease the performance of tidal turbines by about 20%. In

227 addition, CFD simulations considering rigid body geometries, ignores the turbine blade 228 hydroelastic behavior. Accordingly, vibration and deformation can adversely influence the 229 performance of the turbines. Therefore, an additional 10% is added to the energy consumption due 230 to this shortcoming of CFD simulations in order to determine the required power [62]. Finally, the 231 total energy that should be provided by the turbine is estimated as 3440 Wh/m³. It should be noted 232 that this is a safe value for the worst-case scenario, and obviously, if the amount of roughness and 233 deformation can be controlled by using better materials, this value could be less than 3440 Wh/m³. 234 A Photovoltaic (PV) panel and a battery storage are proposed to power booster pump.

3. Preliminary design of the baseline HAT turbine

236 As mention above, the HAT turbine is designed to provide 3440 W to power RO desalination 237 system for producing 1 m³/h freshwater. The well-known equations of horizontal turbines are used 238 to estimate this power. The real power output is described as the power coefficient (C_p) multiplied 239 by nominal power output (P_n) (Eq. 1) [63]. The nominal power output can be calculated from the 240 turbine geometry as well as the flow characteristics based on the particular application [64]. For 241 initial design of the baseline HAT turbine, some basic assumptions are considered based on the literature. According to the experimental work by Bahaj et al. [65], the maximum value of C_p of 242 243 0.3 is considered for the tidal turbine, as a safe estimate, to determine the baseline turbine 244 geometry.

$$245 \qquad P = P_n C_n \tag{1}$$

246 where *P* is power output, P_n is nominal power, and C_p is power coefficient.

247 The nominal power can be calculated as [66]:

248
$$P_n = \frac{\rho 2\pi R^2 U_{\infty}^3}{2}$$
 (2)

249 where ρ is the water density, U_{∞} is the velocity of water, and *R* is the turbine radius (distance 250 between the center of hub to the blade tip).

With the above-mentioned values for the power output and maximum power coefficient, and considering the inlet water velocity as 1 m/s, the initial parameters of the baseline HAT turbine are determined as summarized in Table 1.

Table 1. Initial parameters of HAT Turbine

Total length of blade	Root length	Type of hydrofoil	Hub radius	Number of blades
1.2 m	0.24 m	NACA 0018	0.2 m	3

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256 The related literature [67-69] has been used to design an efficient blade in order to achieve highest 257 hydrodynamic performance. Accordingly, a model blade of 1.2 m is designed for the baseline 258 turbine with SOLIDWORKS 2017, using the methodology outlined in [70]. The blade is designed 259 by using NACA 0018 profile with different distances from the hub circle and different twist angles. 260 According to previous publications, the distance from the hub circle to the root airfoil chord is 261 selected as 0.24 m, which is 20 % of the total blade length, and the twist angles for root and tip sections are varied from 18° to 3°. Details of the NACA 0018 stations and designed blade are 262 263 presented in Table 2 and Figure 5. Using the values in Table 1 and the designed blade, the baseline 264 HAT turbine is designed in the SOLIDWORKS software, the details of which are shown in Figure

265 6.

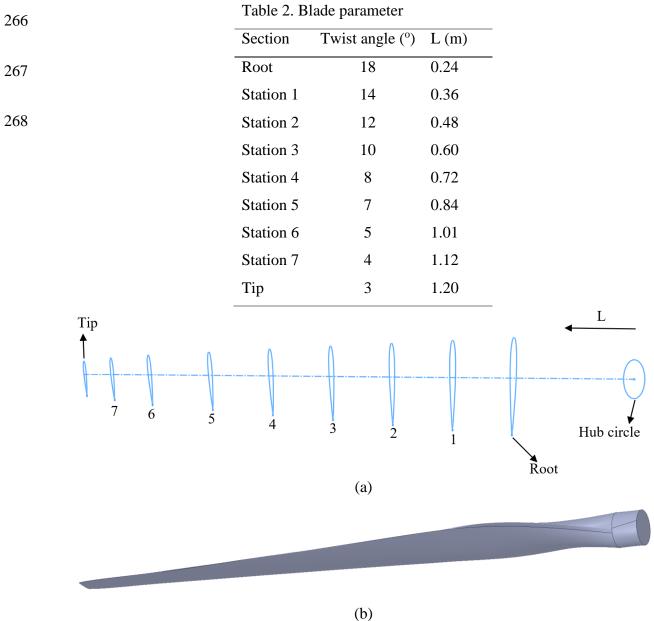


Figure 5. (a) Definition of the NACA 0018 stations and (b) designed blade.

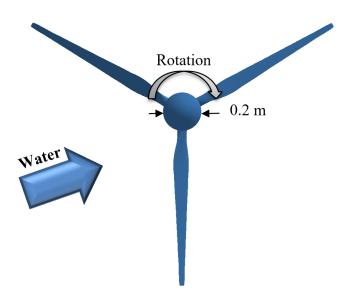




Figure 6. 3D design of the baseline HAT turbine.

272 **4. CFD simulation and validation of the baseline turbine**

273 Figure 7 shows the details of the computational domain, mesh intensity around the turbine, and 274 boundary conditions. An unstructured mesh is built around the turbine and a structured one over 275 the entire computational domain by using the ICEM 2019 software. A three-dimensional transient 276 model is built for CFD simulations of the HAT turbine using ANSYS Fluent. In addition, a sliding 277 mesh method is used for simulating the movement of the fluid around the turbine. For the CFD 278 simulations in ANSYS Fluent, the Shear Stress Transport (SST) k-ω turbulence method and the 279 Pressure Implicit with Splitting of Operator (PISO) algorithm are implemented [71]. A computer 280 with 28-core Intel CPU E5-2680 v4 Processors, 256GB RAM is used to run the CFD simulation.

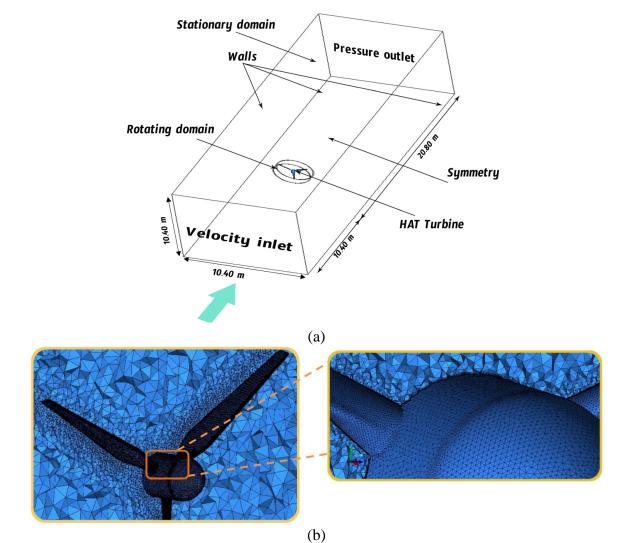


Figure 7. (a) Computational domain and boundary conditions and (b) mesh intensity over the turbine.

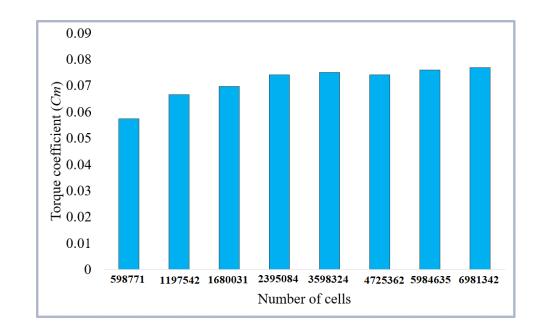
A mesh sensitivity analysis is carried on by generating eight different meshes (from 598,771 cells to 6,981,342) for the baseline design using ICEM CFD software. Using Eq. 3 and the CFD simulation results, the torque coefficient (C_m) is determined for each case with varying numbers of cells and the results are presented in Figure 8. The study revealed that beyond 2,395,084 cells, the standard deviation of the torque coefficient is around 1.0%. As the computational time of the numerical analysis increases dramatically with the number of cells, 2,395,084 is selected for the

rest of the CFD simulations. The simulation time with 2,395,084 cells is 46 hours by using theabove-mentioned computer.

290
$$C_m = \frac{T}{0.5\rho A_l U_{\infty}^2}$$
 (3)

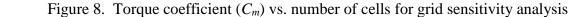
291 where C_m is the torque coefficient, T is the torque, and A_t is the area of the blades.

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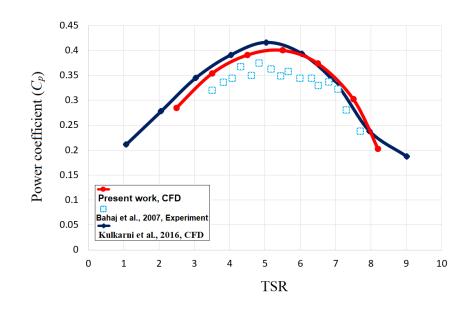


295 One of the common methods to validate CFD model for turbines simulation is assessing C_p against 296 TSR. The power coefficient (C_p) of a HAT turbine can be determined as follows [69]:

$$297 C_p = (TSR)C_m (4)$$

Using Eqs. 3 & 4 and the CFD results, the values of power coefficient at various TSRs are determined and the results are shown in Figure 9. Also, the variations of C_p with TSR for an experimental work reported by Bahaj et al. [65] and a CFD study by Kulkarni [70] are provided in
Figure 9 to validate the current CFD model. According to Figure 9, the results of the current CFD
model are in good agreement with the experimental and CFD results of [64] and [69], both in terms
of values and patterns.

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Figure 9. Variation of C_p with Tip speed ratio (TSR), used for model validation.

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308 **5. Taguchi method**

The Taguchi method offers an affordable and effective way for minimal series of experiments to find optimal parameters of a system [72]. It uses a signal-to-noise ratio (SNR) to quantify the difference in responses. The Taguchi method is commonly employed for a wide range of optimization problems. The identification of the optimum factors and levels can be divided into 7 stages [73].

- 314 Stage 1: Determination of the objective function
- To determine the objective function, a quadratic loss function (QLF) (Eq. 5) is defined to calculate the divergence of a variable from its target quality [74].

317
$$QLF = X(T_c - T_q)^2$$
 (5)

318 where X is the quadratic loss factor, T_q is the target quality, and T_c is the computed response.

The QLF can estimate quality loss in a meaningful way [34, 35]. In this study, power output is considered as the quality target in the objective function. For calculating SNR, there are three approaches in the Taguchi method: Larger is the better, Nominal is the Best, and Smaller is the better [75]. Because the aim of this analysis is to minimize the Quality Loss Function, in this research the Smaller the better SNR formula is used as follows [76]:

324 Smaller is the better:
$$SNR = -10 \log \frac{1}{n} \sum_{i=1}^{n} (G_i)^2$$
 (6)

- 325 where n: the number of experiments; G: the calculated response.
- 326 To quantify a parameter's deviation from its target value, the QLF can normally be modified to an327 SNR as [77]:

328
$$SNR = 10\log(T_c - T_q)^2$$
 (7)

According to the results presented in section 2.4, by replacing power output and target quality, the objective function can be redefined as:

$$331 \quad SNR = 10\log(P - 3440)^2 \tag{8}$$

333 Stage 2: Definition of factors and levels

The Taguchi method is employed to analyze the impacts of different factors (control factors), in order to optimize the main parameters of a system. The objective of this method is to estimate the optimal combination of control factors and their levels. A horizontal turbine consists of two main parts: the hub and the blades. The solidity ratio, which is the most important factor affecting turbine performance [78, 79], is described as the ratio of the total turbine blade area over the swept area [80]. The solidity ratio for HAT turbine can be calculated as [81, 82]:

$$340 \qquad \alpha = \frac{n_b S}{\pi r^2} \tag{9}$$

341 where α is the solidity ratio, n_b is the number of blades, and S is the area of a blade.

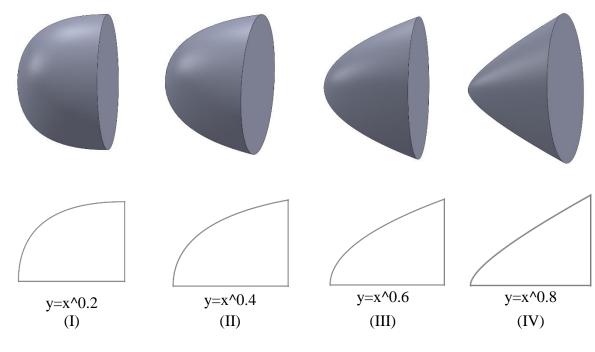
According to Eq. 9, the solidity ratio varies greatly with the blade size and the number of blades.
Thus, optimization of this ratio is accomplished by changing these two factors. On the other hand,
the type of hub can be changed based on the hub radius and shape of the hub.

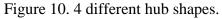
In this work, four factors are considered to be optimized including size of blade (A), number of blades (B), hub radius (C), and hub shape (D). In addition, for each factor four levels are considered.

348 Due to the submergence of the tidal turbines in water, their working conditions vary from the wind 349 turbines; HAT turbines face higher torque and pressure than horizontal axis wind (HAW) turbines. 350 Therefore, tidal turbines must have smaller blades to avoid vibration and deformation 351 which unfavorably affect the turbine efficiency [83-85]. Accordingly, four sizes of blade including 352 0.7b, 0.8b, 0.9b, and 1.0b (b is the size of blade according to Tables 1 and 2) for HAT turbine are 353 chosen as four levels of factor A. The levels of number of blades (B) are selected as 3, 4, 5, and 6. For the hub radius (C) (the third factor), 0.125, 0.175, 0.150, and 0.200 m are chosen as the levels. Also, for the hub shape (factor D) four different levels (I, II, III, and IV) with four parabola equations are considered in order to test and find the optimum configuration. The selected shapes of hub and their corresponding parabolic equations are shown in Figure 10. The hub shapes vary from a conical shape with equation $y=x^0.8$ to a hemisphere with equation $y=x^0.2$.

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365 All the factors and levels are summarized in Table 3.

Table 3. Specified factors and levels

Factors	Coded levels									
A: Size of blade	0.7b	0.8b	0.9b	1.0b						
B: Number of blades	3	4	5	6						
C: Hub radius (m)	0.125	0.175	0.150	0.200						
D: Hub shape	Ι	II	III	IV						

366

367 Stage 3: Orthogonal Array

368 The Taguchi method employs a structured orthogonal array (OA) in design of experiments. By 369 utilizing structured orthogonal array, the Taguchi method can substantially decrease the number 370 of experiments [86]. The orthogonal array (OA) is a sort of test in which columns are "orthogonal" 371 to each other for the independent factors. The data of the constructed experiment can be examined 372 using both the Taguchi and analysis of variance (ANOVA) methods [87]. According to the 373 previous stage, the OA should be adapted for the four factors at the four-level experiment design. 374 For all identified factors and their levels, the feasible orthogonal array is L16 (4^4) which is built as seen in Table 4. According to Table 4, instead of 256 possible cases (4*4*4*4=256), 16 CFD 375 376 simulations are evaluated to minimize the geometry of the designed HAT turbine with the four 377 factors, each in four levels.

378

379

380

383					
	Table 4. Selected	L ₁₆ (4 ⁴) OA o	of the set facto	rs and levels	
384	No.	А	В	С	D
	Test 1	1	1	1	1
	Test 2	1	2	2	2
385	Test 3	1	3	3	3
	Test 4	1	4	4	4
296	Test 5	2	1	2	3
386	Test 6	2	2	1	4
	Test 7	2	3	4	1
387	Test 8	2	4	3	2
001	Test 9	3	1	3	4
	Test 10	3	2	4	3
388	Test 11	3	3	1	2
	Test 12	3	4	2	1
• • • •	Test 13	4	1	4	2
389	Test 14	4	2	3	1
	Test 15	4	3	2	4
390	Test 16	4	4	1	3

391 Stage 4: Computational Fluid Dynamics (CFD) analysis

Figure 11 shows the 16 different cases which have been modelled with SOLIDWORKS software, in accordance with the specifications described in Table 3 and the designed orthogonal array (Table 4). As described in stage 1 of the Taguchi method, in this work, power output (*P*) is used as the objective function (OF). The power output of each case can be measured by torque coefficients (C_m) using Eq. 10. Accordingly, all the torque coefficients at different azimuth angles and TSR=5 are determined from the CFD simulations and the results are plotted in Figure 12.

$$398 \qquad P = 0.5C_m \rho A_t U_{\infty}^3 \omega \tag{10}$$

399 where ω is angular velocity, and A_t is area of the blades.

400

Figure 12 demonstrates the variations of instantaneous torque coefficient (C_m) in one revolution at TSR=5 for 16 HAT turbine cases as well as the baseline turbine after the steady state condition is attained. The maximum and minimum average torque coefficients (C_m) correspond to cases 4 and 9 which are 0.125 and 0.08 respectively. The value of C_m (0.125) obtained for case 4 is 25% higher than that of the baseline case, which is 0.10.

The power output (P) of each case is calculated using Eq. 10 and the results are presented in Table 5. For example, two of the highest values of power output (4002 and 3600 W, corresponding to deigns 4 and 16 respectively) are related to turbines with 6 blades and the two lowest power outputs (2809 and 2907 W, corresponding to deigns 9 and 13 respectively) are related to 3-blade turbine. Increasing of the number of blades provides greater torque; however, the maximum power output of a turbine must have a finite number of blades [66].

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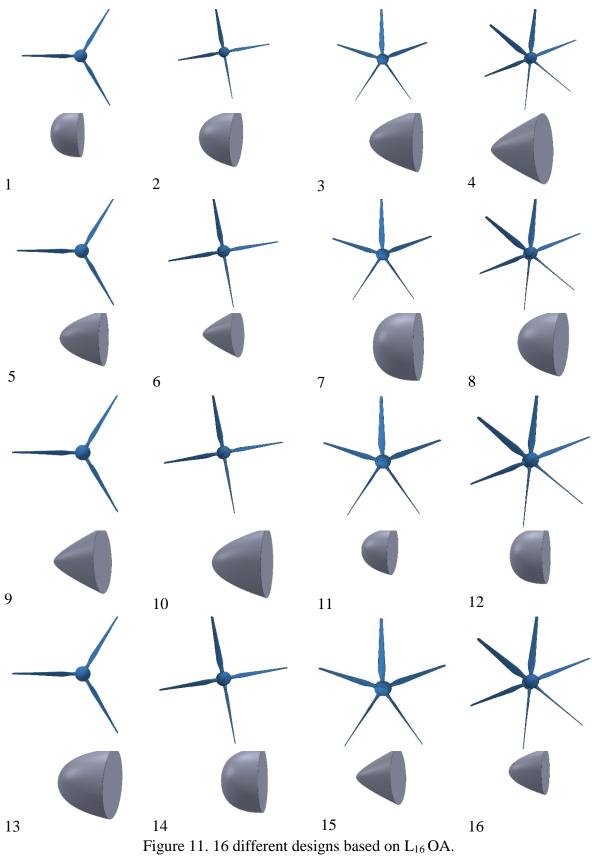
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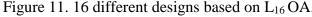
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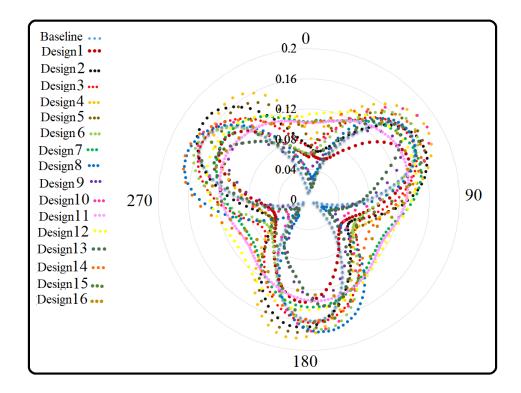
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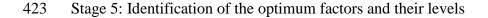
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421 Figure 12. Changes in torque coefficient of all cases for one revolution (0-360°) at TSR=5.
422



424 Eq. 8 is used to calculate the SNR of 16 different designs, according to the data shown in Table 3, 425 and the results are presented in Table 4. According to Eq. 8, the smallest value of SNR occurs 426 when there is the smallest difference between the power output and the target quality. From Table 427 5, it can be seen that the lowest SNR (32) corresponds to design 6, which has the smallest 428 difference between the power output (3476 W) and the target quality (3440 W). The Taguchi 429 method is utilized in the next step to evaluate the order of effect and the optimum combination of 430 the factors to be achieved in the optimized model. For all the factors and their levels, the mean 431 SNR is calculated and the results are plotted in Figure 13. For example, the mean SNR of A1 is

432	computed from the mean values of all level 1 of factor A [$(53+43.5+39.7+55)/4=47.8$]. The results
433	show that power output of the combination A2, B2, C1, and D4 can provide the target quality with
434	smallest geometry. An indicator (β) is determined, as the distance between each factor's top and
435	bottom mean SNRs in Figure 13, to identify the order of influence of all four factors. For variables
436	A, B, C, and D, the values of this indicator are 11.32, 12.2, 6.1 and 5.72 respectively. This clearly
437	indicates that factor B (number of blades) is the main factor amongst all the evaluated factors,
438	influencing the turbine's power output. On the other hand, factors C (hub radius) and D (hub shape)
439	have the smallest effect on hydrodynamic performance of the HAT turbine.

Table 5. L₁₆OA

No.	Size of	Number of	Hub	Hub shape	P (W)	SNR
	blade (A)	blades (B)	radius (C)	(D)		
Baseline	b	3	0.200	III	3417	N/A
Test 1	0.7b	3	0.125	Ι	2993	53
Test 2	0.7b	4	0.150	II	3589	43.5
Test 3	0.7b	5	0.175	III	3536	39.7
Test 4	0.7b	6	0.200	IV	4002	55
Test 5	0.8b	3	0.150	III	3537	39.8
Test 6	0.8 b	4	0.125	IV	3479	32
Test 7	0.8b	5	0.200	Ι	3338	40.1
Test 8	0.8b	6	0.175	II	3490	34
Test 9	0.9b	3	0.175	IV	2809	56
Test 10	0.9b	4	0.200	III	3298	43
Test 11	0.9b	5	0.125	II	3349	39.1
Test 12	0.9b	6	0.150	Ι	3589	43.5
Test 13	1.0b	3	0.200	II	2907	54.5
Test 14	1.0b	4	0.175	Ι	2998	52.9
Test 15	1.0b	5	0.150	IV	3500	35.6
Test 16	1.0b	6	0.125	III	3600	44.1

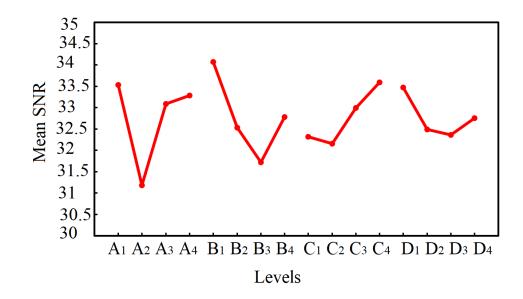


Figure 13. Mean SNR (smaller is the better) for different factors and levels.

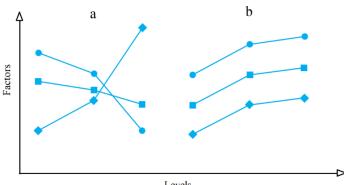
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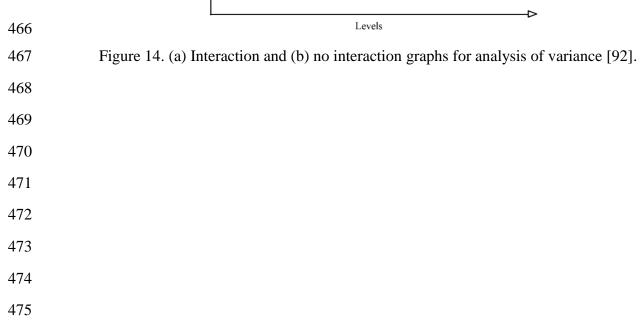
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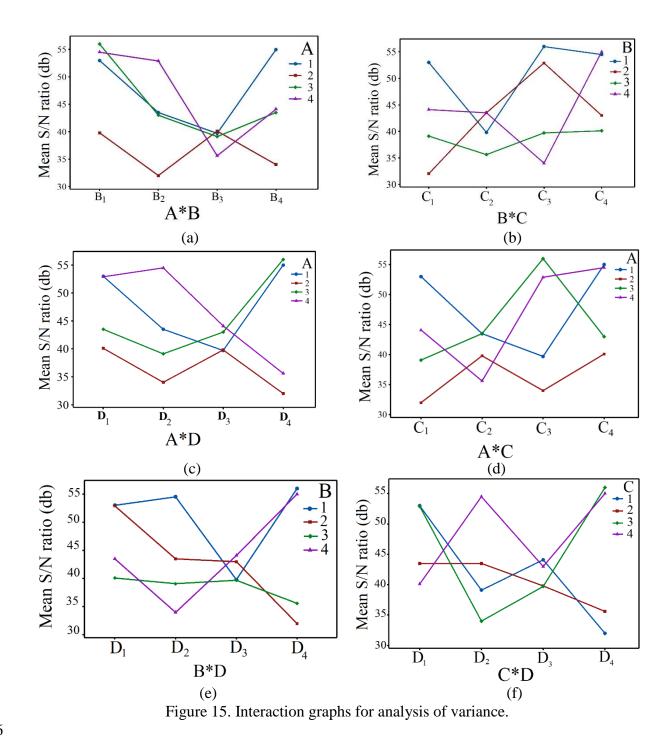
446 Stage 6: Analysis of Variance (ANOVA)

447 In this stage, the interaction of all factors and with their levels is analyzed by using ANOVA. The 448 objective of ANOVA analysis is to evaluate the interaction between factors with respect to the 449 overall variation of all variables. There are different classical approaches for ANOVA analysis for 450 unbalanced data. In this paper, two-way interaction is used. In general, the difference between two-451 way, three-way, and four-way interaction is negligible and most of the relevant literature have used 452 two-way interaction [88-90]. The relationship plot of ANOVA can be used to display the 453 interaction between the factors in different levels [91, 92]. According to the obtained interaction 454 plots, two different potential options (a: parallel and b: non-parallel) can be considered (Figure 455 14). In parallel patterns, a certain interaction will not happen and can be ignored, whilst the 456 interaction in non-parallel trends is important and should be considered. By using the SNRs listed 457 in Table 5, the relationship between each of two variables is measured and presented in Figure 15 458 [34, 35].

In the interpretation of ANOVA interaction plots, when interaction exists amongst the factors, the lines will be non-parallel [92]. By assessing the obtained ANOVA interaction plots (Figure 15), it can be seen that there is an interaction between each pair of factors due to non-parallel lines. Between the assessed variables, the interaction between number of blades (factor B) and other factors is very strong due to the number of non-parallel lines in comparison to other interactions. This is also highlighted in the results of the Taguchi method, where factor B has the greatest effect on the power output of the HAT turbine (stage 5).









The superposition model sues SNRs, which are obtained from the Taguchi method, to estimate all possible ratios outside the orthogonal array. In this study, the superposition model (according to [35]) is used to predict the SNRs of all responses (4*4*4*4=256). Considering the percentage of errors is close to zero and can be neglected [34], the superposition model for the four-level fourfactor problem will be:

486
$$\psi^{t}(A_{i}, B_{i}, C_{k}, D_{l}) = \psi + (\psi_{Ai} - \psi) + (\psi_{Bi} - \psi) + (\psi_{Ck} - \psi) + (\psi_{Dl} - \psi)$$
 (11)

487 where ψ^t is the predicted SNR, ψ is the mean of total mean SNRs, ψ_{Ai} is the mean SNRs of 488 factor A at level i, ψ_{Bj} is the mean SNRs of factor B at level j, ψ_{Ck} is the mean SNRs of factor C at 489 level k, and ψ_{Dl} is the mean SNRs of factor D at level 1.

490 The obtained equation is solved using MATLAB software and the results are shown in Table 6. It 491 can be seen from this table that the lowest SNR is for case 103 and its value is 25.01. This value 492 is for combination of factors A2, B3, C2, and D3. The obtained SNR value for the combination 493 A2, B3, C2, and D3 is almost 21% less than the amount obtained in the Taguchi method (case 6, 494 SNR=32). In should be noted that in Table 6, the SNR value for the obtained combination by the 495 Taguchi method (A2, B2, C1, and D4) is calculated as 33.68, which is more than the minimum 496 value of the Table. Therefore, combination of factors A2, B3, C2, and D3 that is provided by the 497 superposition model, is used to build a HAT turbine as the final optimized model and it is simulated 498 using the CFD method described in section 4.

499

Tabl	le (<u>6. P</u>		ictic	on of s		-to-	noi	se (<u>SN</u>		<u>all a</u> c	hie	vab			binati	ons					
No.	А	В	С	D	SNR	NO.	Α	В	С	D	SNR	No.	А	В	С	D	SNR	No.	А	В	С	D	SNR
1	1	1	1	1	55.71	65	2	1	1	1	44.38	129	3	1	1	1	53.31	193	4	1	1	1	54.68
2	1	1	1	2	51.11	66	2	1	1	2	39.78	130	3	1	1	2	48.71	194	4	1	1	2	50.08
3	1	1	1	3	49.98	67	2	1	1	3	38.66	131	3	1	1	3	47.58	195	4	1	1	3	48.96
4	1	1	1	4	52.98	68	2	1	1	4	41.66	132	3	1	1	4	50.58	196	4	1	1	4	51.96
5	1	1	2	1	54.26	69 70	2	1	2	1	42.93	133	3	1	2	1	51.86	197	4	1	2	1	53.23
6 7	1 1	1 1	2	2	49.66	70 71	2	1	2	2 3	38.33	134	3 3	1 1	2	2 3	47.26	198	4	1	2	2 3	48.63
8	1	1	2 2	3 4	48.53 51.53	71	2 2	1 1	2 2	3 4	37.21 40.21	135 136	3 3	1	2 2	3 4	46.13 49.13	199 200	4 4	1 1	2 2	3 4	47.51 50.51
9	1	1	3	1	59.31	72	2	1	3	1	40.21	130	3	1	3	1	56.91	200	4	1	3	1	58.28
10	1	1	3	2	54.71	74	2	1	3	2	43.38	137	3	1	3	2	52.31	201	4	1	3	2	53.68
11	1	1	3	3	53.58	75	2	1	3	3	42.26	139	3	1	3	3	51.18	202	4	1	3	3	52.56
12	1	1	3	4	56.58	76	2	1	3	4	45.26	140	3	1	3	4	54.18	204	4	1	3	4	55.56
13	1	1	4	1	61.81	77	2	1	4	1	50.48	141	3	1	4	1	59.41	205	4	1	4	1	60.78
14	1	1	4	2	57.21	78	2	1	4	2	45.88	142	3	1	4	2	54.81	206	4	1	4	2	56.18
15	1	1	4	3	56.08	79	2	1	4	3	44.76	143	3	1	4	3	53.68	207	4	1	4	3	55.06
16	1	1	4	4	59.08	80	2	1	4	4	47.76	144	3	1	4	4	56.68	208	4	1	4	4	58.06
17	1	2	1	1	47.73	81	2	2	1	1	36.41	145	3	2	1	1	45.33	209	4	2	1	1	46.71
18	1	2	1	2	43.13	82	2	2	1	2	31.81	146	3	2	1	2	40.73	210	4	2	1	2	42.11
19	1	2	1	3	42.01	83	2	2	1	3	30.68	147	3	2	1	3	39.61	211	4	2	1	3	40.98
20	1	2	1	4	45.01	84	2	2	1	4	33.68	148	3	2	1	4	42.61	212	4	2	1	4	43.98
21	1	2	2	1	46.28	85	2	2	2	1	34.96	149	3	2	2	1	43.88	213	4	2	2	1	45.26
22	1	2 2	2	2	41.68	86	2 2	2	2	2	30.36	150	3	2	2	2	39.28	214	4	2	2	2	40.66
23	1		2	3	40.56	87	2	2	2	3	29.23	151	3	2	2	3	38.16	215	4	2	2	3	39.53
24	1	2	2	4	43.56	88	2	2	2	4	32.23	152	3	2	2	4	41.16	216	4	2	2	4	42.53
25	1	2	3	1	51.33	89	2	2	3	1	40.01	153	3	2	3	1	48.93	217	4	2	3	1	50.31
26	1	2 2	3	2	46.73	90	2	2	3	2	35.41	154	3	2	3	2	44.33	218	4	2	3	2	45.71
27 28	1	2	3	3 4	45.61	91 92	2	2	3 3	3 4	34.28	155	3	2	3 3	3 4	43.21	219	4	2	3 3	3 4	44.58
28 29	1 1	2 2	3 4	4	48.61 53.83	92 93	2 2	2 2	3 4	4	37.28 42.51	156 157	3 3	2 2	3 4	4	46.21 51.43	220 221	4 4	2 2	3 4	4	47.58 52.81
30	1	2	4	2	49.23	93 94	$\frac{2}{2}$	2	4	2	42.31 37.91	157	3	2	4	2	46.83	221	4	2	4	2	48.21
31	1	2	4	3	48.11	95	2	2	4	3	36.78	159	3	$\frac{2}{2}$	4	3	45.71	223	4	2	4	3	47.08
32	1	2 2 2	4	4	51.11	96	2	2	4	4	39.78	160	3	2	4	4	48.71	223	4	2	4	4	50.08
33	1	3	1	1	43.51	97	2	3	1	1	32.18	161	3	3	1	1	41.11	225	4	3	1	1	42.48
34	1	3	1	2	38.91	98	2	3	1	2	27.58	162	3	3	1	2	36.51	226	4	3	1	2	37.88
35	1	3	1	3	37.78	99	2	3	1	3	26.46	163	3	3	1	3	35.38	227	4	3	1	3	36.76
36	1	3	1	4	40.78	100	2	3	1	4	29.46	164	3	3	1	4	38.38	228	4	3	1	4	39.76
37	1	3	2	1	42.06	101	2	3	2	1	30.73	165	3	3	2	1	39.66	229	4	3	2	1	41.03
38	1	3	2	2	37.46	102	2	3	2	2	26.13	166	3	3	2	2	35.06	230	4	3	2	2	36.43
39	1	3	2	3	36.33	103	2	3	2	3	25.01	167	3	3	2	3	33.93	231	4	3	2	3	35.31
40	1	3	2	4	39.33	104	2	3	2	4	28.01	168	3	3	2	4	36.93	232	4	3	2	4	38.31
41	1	3	3	1	47.11	105	2	3	3	1	35.78	169	3	3	3	1	44.71	233	4	3	3	1	46.08
42	1	3	3	2	42.51	106	2	3	3	2	31.18	170	3	3	3	2	40.11	234	4	3	3	2	41.48
43	1	3	3	3	41.38	107	2	3	3	3	30.06	171	3	3	3	3	38.98	235	4	3	3	3	40.36
44	1	3	3	4	44.38	108	2	3	3	4	33.06	172	3	3	3	4	41.98	236	4	3	3	4	43.36
45	1	3	4	1	49.61	109	2	3	4	1	38.28	173	3	3	4	1	47.21	237	4	3	4	1	48.58
46	1	3	4	2	45.01	110	2	3	4	2	33.68	174	3	3	4	2	42.61	238	4	3	4	2	43.98
47 48	1 1	3 3	4	3 4	43.88	111	2 2	3 3	4	3 4	32.56	175	3 3	3 3	4	3 4	41.48	239	4	3 3	4 4	3 4	42.86
48 49	1	3 4	4 1	4	46.88 49.03	112 113	2	3 4	4 1	4	35.56 37.71	176 177	3 3	3 4	4 1	4	44.48 46.63	240 241	4 4	3 4	4	4	45.86 48.01
49 50	1	4	1	2	49.05	115	2	4	1	2	33.11	177	3 3	4	1	2	40.03	241 242	4	4	1	2	48.01
50 51	1	4	1	3	44.43	114	2	4	1	3	31.98	178	3	4	1	3	40.91	242	4	4	1	3	42.28
52	1	4	1	4	45.31	115	$\frac{2}{2}$	4	1	4	34.98	179	3	4	1	4	40.91	243 244	4	4	1	4	42.28
52 53	1	4	2	1	40.31	117	$\frac{2}{2}$	4	2	1	36.26	180	3	4	2	1	45.18	244	4	4	2	1	46.50
54	1	4	2	2	42.98	118	2	4	2	2	31.66	182	3	4	2	2	40.58	246	4	4	2	2	41.90
55	1	4	2	3	41.86	119	2	4	2	3	30.53	183	3	4	2	3	39.46	240	4	4	2	3	40.8
56	1	4	2	4	44.86	120	2	4	2	4	33.53	184	3	4	2	4	42.46	248	4	4	2	4	43.8
57	1	4	3	1	52.63	120	2	4	3	1	41.31	185	3	4	3	1	50.23	249	4	4	3	1	51.6
58	1	4	3	2	48.03	121	2	4	3	2	36.71	186	3	4	3	2	45.63	250	4	4	3	2	47.0
59	1	4	3	3	46.91	123	2	4	3	3	35.58	187	3	4	3	3	44.51	251	4	4	3	3	45.8
	1	4	3	4	49.91	124	2	4	3	4	38.58	188	3	4	3	4	47.51	252	4	4	3	4	48.8
60	1	4	4	1	55.13	125	2	4	4	1	43.81	189	3	4	4	1	52.73	253	4	4	4	1	54.1
60 61	1						•						2										
	1	4	4	2	50.53	126	2	4	4	2	39.21	190	3	4	4	2	48.13	254	4	4	4	2	49.51
61	1 1 1		4 4	2 3	50.53 49.41	126 127	2 2	4	4	2	39.21 38.08	190 191	3 3	4 4	4 4	2	48.13 47.01	254 255	4	4	4	2 3	49.51 48.38

Table 6. Prediction of signal-to-noise (SNR) of all achievable combinations

503 **6. Fluid dynamics study**

504 With the combinations obtained from the superposition model and Table 3, the optimized turbine 505 is designed in SOLIDWORKS 2017. The initial SOLIDWORKS design shows that the weight of 506 optimized design is 17% less than the baseline design; hence it requires less material and can be 507 manufactured cheaper. A comprehensive CFD simulation of the baseline and the optimized 508 designs is carried out using ANSYS Fluent 2019 (as described in section 2) and the results are 509 presented in this section. Using Eq. 10 and the CFD results, the power output of the optimized 510 turbine is calculated to be 3830 W, which is suitable for the mentioned desalination system to produce $1 \text{ m}^3/\text{h}$ freshwater (see section 2.4). 511

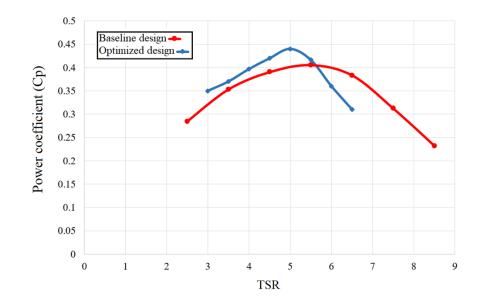
512 Figure 16 shows a comparison of the variations of power coefficient (C_p) with TSR for the baseline 513 and optimized HAT turbines. When comparing the performance of the presented HAT turbines at 514 various tip speed ratios (TSRs), the change of the blade size and number of blades helps to increase 515 the power coefficient (C_p) , however, after a particular TSR, the power output of the turbines 516 decreases due to the increased turbulence. According to the obtained results, at TSR=5, C_p of the 517 optimized model is 0.44, while for the baseline design it is 0.40 (it is 10% more for the optimized 518 model). Moreover, the optimized 5-blade HAT turbine performs better at lower TSR (3-5.5) and 519 the baseline 3-blade HAT turbine works better at higher TSR (5.5-6.5). To further investigate this, 520 it is necessary to simulate both turbines at different TSRs. Figure 17 shows the streamline contours 521 across the revolving turbine in four different tip speed ratios (TSRs). The contour plots explicitly 522 illustrate that the velocity deficiency is dependent on the TSRs which are provided by different 523 inlet velocities. The water rotates the HAT turbine and the passing stream rotates in an inverse 524 direction of the turbine. While water moves through the turbine, the turbine absorbs the energy of 525 the water and hence there is a difference in the velocity of the upstream and downstream. The

higher the inlet velocity, the greater is the difference in velocity. In both turbines, the flow runs normally at low TSRs and from upstream to downstream. In the baseline turbine, according to Figure 17, there is a heavy turbulence in the streamline distributions when the TSR changes from 5.5 to 6.0. However, in the optimized turbine this occurs after TSR=5.0 and the streamlines of downstream face a huge turbulence. These results provide further evidence for the findings in Figure 16, which show the optimized turbine has better performance at lower TSRs.

532 The vorticity contours of the CFD simulations of both turbines through a cross section (YZ plane) 533 at azimuth angles of 40°, 80°, and 120° are presented in Figure 18. For these contours to be 534 comparable, one of the turbine blades is marked with letter Q (indicator blade) and the value of 535 azimuth angle is defined according to this indicator blade. The results show that the (three-blade) 536 baseline turbine experiences greater vortex and wake in comparison with the optimized (five-537 blade) turbine, which results in better performance. The vorticity is indeed greater on the top of 538 the blades due to rotational impact of the turbine blades, and the velocity gradient is much wider. 539 The lower magnitude of vorticity at the bottom of the blades can be attributed to the separation of 540 the flow on the blade surface, and it is very visible at the proximity of turbine hub. For both 541 turbines, the energy contribution of blades near the hub is less than the section near the tip portion. 542 The CFD simulation in ANSYS Fluent considers the solid parts as rigid body and it does not 543 consider the deformation and vibration. However, in reality, the increase in the vortex at the end 544 of the turbine blades causes an increase in vibration as well as deformation, which reduces the 545 lifetime and the efficiency of the turbine. This further confirms the superiority of the optimized 546 turbine, which has smaller blades (20% smaller) than the baseline turbine.

547 Finally, to better understand and compare the effect of different hubs on hydrodynamic 548 performance of the HAT turbines, the velocity contours at three different azimuth angles on the

549 ZX plane are shown in Figure 19. All contours are plotted at TSR of 5.0. As can be seen from this 550 Figure, type III hub, which is used in the optimized model (compared to the type I (baseline 551 model)), can be used to suppress the flow separation at different azimuth angles. On the other hand, 552 in the baseline model, after water hits the nose of the hub, it causes separation and turbulence 553 immediately, which can reduce the kinetic energy of water and the efficiency of the turbine. It can 554 be concluded that the combination of the number of turbine blades and the type of hub can affect 555 the performance of the turbine, as predicted in the previous section by the ANOVA method.

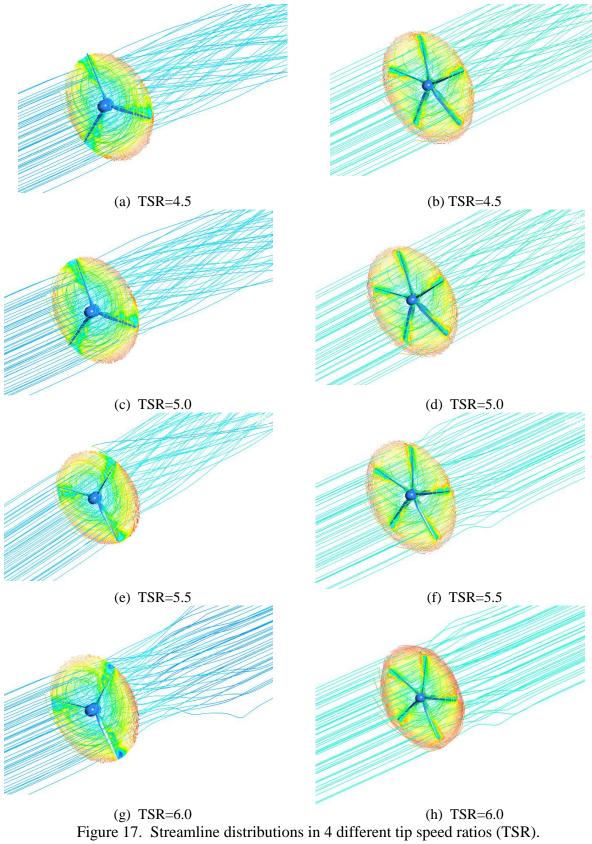


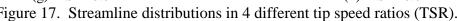
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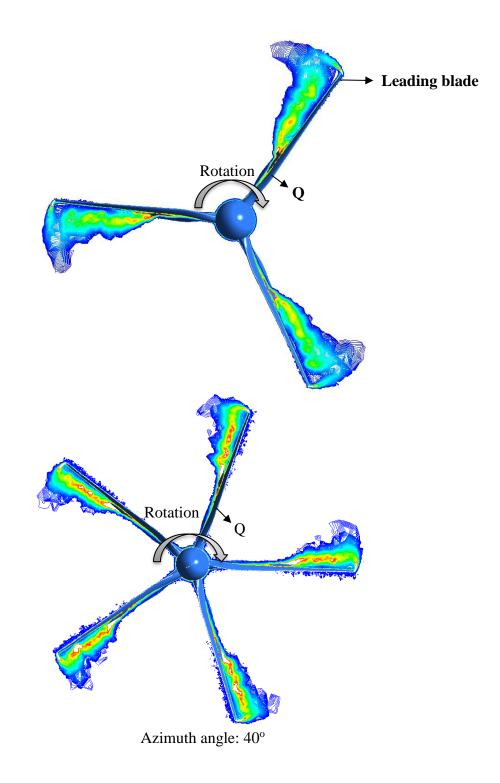
557 Figure 16. Variation of power coefficient (C_p) with tip speed ratio (TSR) of baseline and

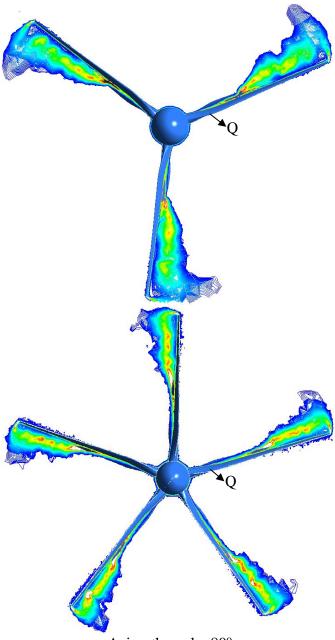
558

optimized designs

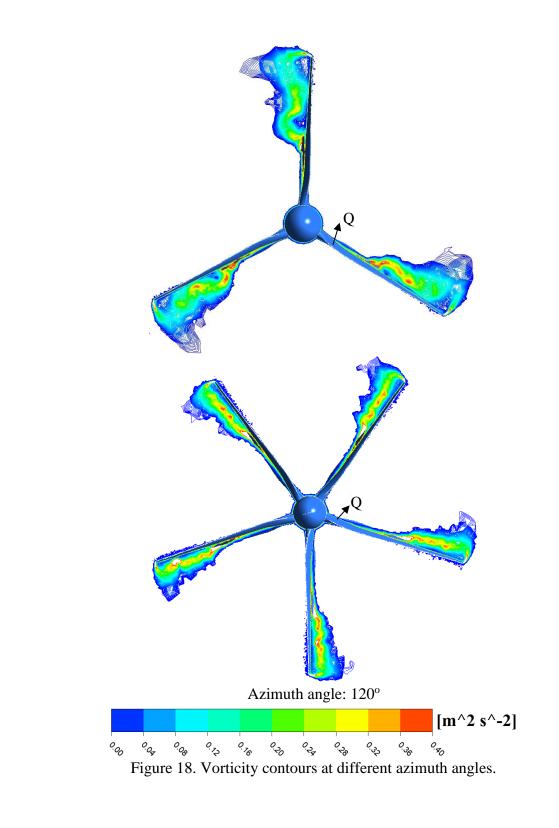








Azimuth angle: 80°



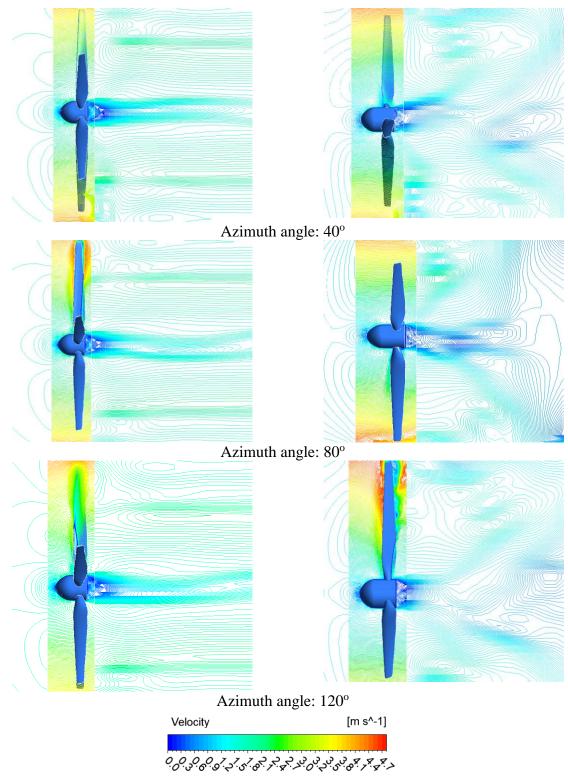


Figure 19. Velocity distribution at different azimuth angles (left: optimized model and right: baseline model).

565 **7. Conclusion**

The Taguchi method and extensive CFD simulations were utilized in this study to minimize the geometry of a HAT turbine, designed to power a desalination system. The results show that the Taguchi method is an effective tool for optimization of complex HAT turbines by using only few experiments. The main conclusions of this paper can be summarized as follows:

570 (1) The optimum combination of the tested factors by the Taguchi method was achieved as (design 571 6): size of blade: 0.8b; number of blades: 4; hub radius: 0.125 m; and hub shape: type IV. The 572 β indicator of variables A, B, C, and D, was calculated as 11.32, 12.2, 6.1 and 5.72 573 respectively. This indicates that number of blades (B) is the main influential factor among the 574 four assessed factors. The hub radius (C) and hub shape (D) have the least influence on the 575 HAT turbine's hydrodynamic output.

576 (2) The results from ANOVA analysis showed that all four parametric variables have vivid
577 interactions with each other. Among the analyzed factors, the interaction of the number of
578 blades (B) and other variables was stronger.

(3) The results of the superposition model showed that the minimum SNR was 25.01 for design 103, which was 21% less than the value achieved in the Taguchi approach. This value was for the combination of size of blade: 0.8b; number of blades: 5; hub radius: 0.150 m; and hub shape: type III. The weight of optimized model was 17% less than the baseline model, indicating that the optimized model would require less material and can be made cheaper.

585 (4) According to the CFD simulations, C_p of the optimized model was 0.44, which was 10% higher

than the baseline model (0.40) at tip speed ratio (TSR) of 5. The optimized HAT turbine works

587 better at lower TSR (3-5.5) and the baseline HAT turbine performs better at higher TSR (5.5588 6.5).

The impacts of deformation of the HAT turbine were not considered in this study. In addition, the efficiency of a HAT turbine is affected by the roughness of the turbine blades, which can be considered as a variable in the Taguchi approach, and its individual effects can be studied and compared with other variables. Moreover, an economic analysis of HAT turbines based on different materials is a potential area for future work.

594 **Declaration of Competing Interest**

595 The authors declare that they have no known competing financial interests or personal 596 relationships that could have appeared to influence the work reported in this paper.

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