

Elasticity of hydrous ringwoodite at mantle conditions: Implication for water distribution in the lowermost mantle transition zone

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1 **Abstract**

2 The mantle transition zone (MTZ) is potentially a geochemical water reservoir
3 because of the high H₂O solubility in its dominant minerals, wadsleyite and ringwoodite.
4 Whether the MTZ is wet or dry fundamentally impacts our understanding of the deep-
5 water distribution, geochemical recycling, and the pattern of mantle convection.
6 However, the water content in the MTZ inferred from previous studies remains disputed.
7 Seismic observations such as velocity anomalies were used to evaluate the water
8 content in the MTZ, but the hydration effect on the velocities of MTZ minerals under
9 appropriate pressure (P) and temperature (T) conditions is poorly constrained. Here we
10 investigated the elastic properties and velocities of hydrous ringwoodite at high P-T
11 conditions using first-principles calculations. Our results show that the hydration
12 effects on elastic moduli and velocities of ringwoodite are significantly reduced by
13 pressure but strongly enhanced by temperature. The incorporation of 1.0 wt% water
14 into ringwoodite decreases the compressional and shear velocities of the pyrolitic
15 mantle by -1.0% and -1.4% at the conditions of MTZ, respectively. Using results from
16 seismic tomography and together with the topography of the 660-km discontinuity, we
17 evaluate the global distribution of water in the lower MTZ. We find that about 80% of
18 the MTZ can be explained by varying water content and temperature, however, the
19 remaining 20% requires the presence of high-velocity heterogeneities such as
20 harzburgite. Our models suggest an average water concentration of ~0.2 wt% in the
21 lower MTZ, with an interregional variation from 0 to 0.9 wt%. Together with our
22 previous work, we conclude that the water concentration in the MTZ likely decreases
23 with depth globally and the whole MTZ contains the equivalent of about one ocean
24 mass of water.

25

26 **Keywords:** elasticity of hydrous ringwoodite, first-principles calculations, mantle
27 transition zone, water content

28 **1. Introduction**

29 Earth's mantle transition zone (MTZ) is the region between 410 and 660 km and
30 is mainly composed of wadsleyite, ringwoodite, and majorite. It separates the upper
31 mantle from the lower mantle and plays an important role in mantle flow and slab
32 subduction processes (Ballmer et al., 2015; Bercovici and Karato, 2003). It is widely
33 accepted that the MTZ is potentially a large reservoir of water because wadsleyite and
34 ringwoodite can store more than one weight percent of water in the form of hydroxyl
35 (Fei and Katsura, 2020; Inoue et al., 2010, 1995; Jacobsen et al., 2005; Ohtani, 2015;
36 Smyth, 1987). The discovery of a hydrous ringwoodite inclusion with ~1.4 wt% water
37 in a natural 'superdeep' diamond from Brazil (Pearson et al., 2014) confirms
38 experimental results and implies that the MTZ is at least locally hydrated. Such an
39 interpretation is also supported by the findings of ice-VII inclusions in natural
40 'superdeep' diamonds (Tschauner et al., 2018), although again these inclusions are
41 unlikely to be representative of the whole MTZ.

42 The actual amount of water and its spatial distribution in the MTZ are of great
43 importance for understanding the structure and chemical composition of the deep
44 mantle (Bercovici and Karato, 2003; Schmandt et al., 2014; Tauzin et al., 2010). Many
45 studies have devoted significant effort to constraining the realistic hydration state of the
46 MTZ based on electrical conductivity (Huang et al., 2005; Munch et al., 2020; Yoshino
47 et al., 2008), but the estimated water concentration differs by more than one order of
48 magnitude between these studies. For instance, some studies suggested a nearly
49 anhydrous MTZ (Yoshino et al., 2008), whereas others argued that the MTZ is
50 substantially more hydrated (Huang et al., 2005; Irifune, 1998; Karato, 2011; Kelbert
51 et al., 2009), although even these studies do not agree on how much water the MTZ
52 contains. This disagreement is probably due to large uncertainties in both the
53 magnetotelluric observations and the experimentally measured electrical conductivity
54 of MTZ minerals. In contrast to previous studies on conductivity, a nearly water-
55 saturated MTZ model was recently proposed by comparing mineral viscosity data with

56 the observed mantle viscosity profile (Fei et al., 2017). In addition, the seismic
57 detection of partial melting above 410 km or below 660 km has also been used to infer
58 regional-scale water variability (Schmandt et al., 2014; Tauzin et al., 2010; Wei and
59 Shearer, 2017). Seismic observations of the variation in the depths of the 410-km and
60 660-km discontinuities have also been exploited in order to constrain the water content
61 of the MTZ. This is because the pressure of the olivine to wadsleyite and the post-spinel
62 phase transitions responsible for the 410 and 660 km discontinuities respectively vary
63 with water content (Higo et al., 2001; Wood, 1995). Again, conflicting conclusions
64 were obtained by different studies (Blum and Shen, 2004; Gao et al., 2010; Houser,
65 2016; Meier et al., 2009), probably because the transition pressures are also
66 significantly affected by temperature.

67 Because the incorporation of water lowers the sound velocities of minerals, the
68 observed seismic velocities in the MTZ can potentially be used to estimate its water
69 content. For instance, in a pyrolitic mantle, wadsleyite should contain ~0.9 wt% water
70 at the top of the MTZ to match both the density and seismic velocity jumps across the
71 410-km discontinuity (Wang et al., 2019). In principle, the density and velocity jumps
72 across the 660-km discontinuity could also be used to infer the water content in the
73 lower part of the MTZ. However, the complexity of phase transitions at ~ 660 km
74 (Hirose, 2002) hampers the accurate estimate of the relationship between velocity
75 contrasts and ringwoodite hydration. Instead, multiple seismic observations such as the
76 depth of the 660-km discontinuity and the seismic velocity anomalies within the MTZ
77 have been combined together to infer the hydration state of the MTZ, but yet again
78 there is a large discrepancy in the amount of water between different studies (Houser,
79 2016; Mao et al., 2012; Schulze et al., 2018; Suetsugu et al., 2006).

80 One possible explanation for why so many studies using similar seismic
81 observations of the transition zone come to different conclusions is that the effect of
82 hydration on seismic wave velocities has not been well quantified. Experimental studies
83 have reported the elastic properties and/or sound velocities of hydrous ringwoodite up

84 to 22 GPa but only up to 673 K (Jacobsen and Smyth, 2006; Mao et al., 2012; Schulze
85 et al., 2018; Wang et al., 2006). Moreover, even the results at ambient conditions can
86 differ markedly between different studies (Mao et al., 2012; Schulze et al., 2018).
87 Extrapolating results to different pressures and temperature is also problematic. For
88 instance, Schulze et al. (2018) suggested that the hydration effect on the sound
89 velocities of ringwoodite may be significantly weakened by pressure, while Mao et al.
90 (2012) argued that temperature may strongly enhance the hydration-induced velocity
91 reduction for compressional wave velocities of ringwoodite. This implies that
92 extrapolation of low-temperature data to the P-T conditions of the MTZ could result in
93 large uncertainties and contradictory conclusions.

94 In this study, we investigate the elastic properties and velocities of hydrous
95 ringwoodite at the P-T conditions of the MTZ using first-principles calculations with
96 the same computational details as those in our previous studies for the elasticity of
97 anhydrous ringwoodite (Núñez Valdez et al., 2012) and wadsleyite (Núñez-Valdez et
98 al., 2013; Wang et al., 2019). Together with elastic data for anhydrous ringwoodite
99 (Núñez Valdez et al., 2012), we obtain the reduction in velocities of ringwoodite due to
100 water over a wide range of pressures and temperatures and use that to quantify the effect
101 of water on the velocities of a pyrolitic mantle at MTZ conditions. Combining mineral
102 physics with seismological observations, we then estimate the water concentration and
103 temperature anomaly in the lower MTZ using Monte Carlo simulations.

104

105 **2. Method**

106 Following Barron and Klein (1965), elastic constants can be derived from the
107 relationship between the Helmholtz free energy and strain:

$$108 \quad C_{ijkl}^T = \frac{1}{V} \left(\frac{\partial^2 F}{\partial e_{ij} \partial e_{kl}} \right) + \frac{1}{2} P (2\delta_{ij}\delta_{kl} - \delta_{il}\delta_{kj} - \delta_{ik}\delta_{jl}) \quad (1)$$

109 Here, e_{ij} ($i, j = 1, 3$) are infinitesimal strains, P is pressure, δ_{ij} refers to the
110 Kronecker delta symbol, and F is the Helmholtz free energy. Within the quasi-
111 harmonic approximation (QHA), F can be written as:

$$\begin{aligned}
112 \quad F(e_{ij}, V, T) &= U(e_{ij}, V) + \frac{1}{2} \sum_{q,m} \hbar \omega_{q,m}(e_{ij}, V) \\
113 \quad &+ k_B T \sum_{q,m} \ln \left\{ 1 - \exp \left[- \frac{\hbar \omega_{q,m}(e_{ij}, V)}{k_B T} \right] \right\} \quad (2)
\end{aligned}$$

114 where V is equilibrium volume and T is temperature. Parameters ω , q , and m
115 represent the vibrational frequencies, the phonon wave vector, and the normal index,
116 respectively. \hbar , k_B are reduced Planck and Boltzmann constants. The first, second,
117 third terms in Eq. (2) are the static internal, zero-point, and vibrational energy
118 contributions, respectively. As such, this conventional method requires the calculations
119 of vibrational properties of many strained configurations, which requires significant
120 computational effort. Wu and Wentzcovitch (2011) developed a semi-analytical method
121 that only needs the vibrational properties of unstrained configurations to calculate the
122 high P-T elasticity, which consequently reduces the computational work to the level of
123 less than one-tenth of the conventional method. This approach has been successfully
124 applied to the thermal elasticity of many minerals (Duan et al., 2019; Hao et al., 2019;
125 Hu et al., 2016; Núñez-Valdez et al., 2013; Núñez Valdez et al., 2012; Qian et al., 2018;
126 Shukla et al., 2016, 2015; Wang et al., 2019, 2020; Wang and Wu, 2018; Wu et al., 2013;
127 Wu and Wang, 2016; Wu and Wentzcovitch, 2011; Yang et al., 2017; Yang and Wu,
128 2014; Zou et al., 2018), and so we use it to obtain the elastic properties of hydrous
129 ringwoodite at high P-T conditions in this study. The adiabatic bulk modulus K_S and
130 shear modulus G are obtained by using the Voigt-Reuss-Hill averages,
131 and compressional wave velocity (V_P) and shear wave velocity (V_S) are from elastic
132 moduli and density using $V_P = \sqrt{(K_S + \frac{4}{3}G)/\rho}$ and $V_S = \sqrt{G/\rho}$.

133 First-principles calculations were performed using the Quantum Espresso package
134 (Giannozzi et al., 2009) based on the density functional theory (DFT), adopting the
135 local density approximation (LDA) for the exchange-correlation function, unless noted
136 otherwise. The pseudopotentials of Mg, Si, H, and O are described in our previous
137 studies (Duan et al., 2019; Hu et al., 2016; Wang et al., 2019). The cutoff energy for the
138 plane wave was 70 Ry. The structures of hydrous ringwoodite were optimized under

139 different pressures using the variable cell-shape damped molecular dynamics approach
140 (Wentzcovitch, 1991) with a $2 \times 2 \times 2$ k-point mesh. The dynamical matrices for relaxed
141 structures were calculated using density functional-perturbation theory (DFPT) (Baroni
142 et al., 2001) with a $2 \times 2 \times 2$ q-point mesh and were extrapolated to a denser q mesh to
143 obtain the vibrational density of states. Elastic tensors at static conditions were
144 calculated from the stress-strain relationship. The calculated Helmholtz free energy
145 versus volume was fitted by the isothermal third-order finite strain equation of state,
146 which was used to calculate thermodynamic parameters including pressure. The
147 volume versus pressure relationship was fitted by the Birch-Murnaghan third-order
148 equation of state.

149 Dry ringwoodite (${}^{\text{IV}}\text{A}{}^{\text{VI}}\text{B}_2\text{O}_4$) has a normal spinel structure with space group Fd-
150 $3m$, in which the six-coordinated B site (16d) is occupied by Mg atom and the four-
151 coordinated A site (8a) is occupied by Si atom. There are three possible mechanisms
152 for the incorporation of hydrogen into ringwoodite (Blanchard et al., 2009; Li et al.,
153 2009; Panero, 2010): (1) $\text{V}_{\text{Mg}}'' + 2\text{H}^{**}$, which is a Mg vacancy charge balanced by two
154 H atoms; (2) $\text{V}_{\text{Si}}'''' + 4\text{H}^{****}$, a Si vacancy charge balanced by four H atoms; (3) Mg_{Si}''
155 $+ 2\text{H}^{**}$, a Si vacancy occupied by a Mg atom charge balanced by two H atoms. Previous
156 first-principles calculations (Panero, 2010) found that these three substitution
157 mechanisms exist in ratios of 65:25:10 respectively, and so hydrogen is mainly
158 incorporated into ringwoodite through the mechanism $\text{V}_{\text{Mg}}'' + 2\text{H}^{**}$ (Hernández et al.,
159 2013). Results of fitting experimental data on hydrous ringwoodite also show that the
160 three defects exist in a ratio of 75:14:11 (Panero, 2010). This is also supported by more
161 recent experimental results from nuclear resonance spectroscopy (Grüninger et al.,
162 2017). Thus, we adopt the substitution mechanism $\text{V}_{\text{Mg}}'' + 2\text{H}^{**}$ to construct the initial
163 structure of hydrous ringwoodite with 1.63 wt% water ($\text{Mg}_{15}\text{Si}_8\text{O}_{30}(\text{OH})_2$), where the
164 sites for two H atoms were determined by following the experimental results
165 from pulsed neutron diffraction (Purevjav et al., 2014) (Fig. S1). In order to estimate
166 the effect of the mechanisms (2) and (3), we calculated the elastic properties of hydrous

167 ringwoodite with the substitution $V_{Si}'''' + 4H^{****}$ and $Mg_{Si}'' + 2H^{**}$ at static conditions
168 (Table S1). Our results show that the relative difference in the elastic moduli and sound
169 velocities of hydrous ringwoodite between the mechanism (1) and the mixing
170 mechanism with the ratios of 65:25:10 and/or 75:14:11 is less than 0.4% at the pressures
171 of MTZ.

172 At ambient pressure, the calculated frequencies of OH stretching modes are ~ 2250
173 cm^{-1} , lower than the experimental measurements (Thomas et al., 2015 and references
174 therein), although the experimental infrared spectrum of hydrous ringwoodite consists
175 of several broad bands for OH stretching modes. This is mainly because the LDA
176 overestimates the H-O bond lengths and there are different hydration mechanisms
177 involved in experimental samples (Li et al., 2009). However, vibrational frequencies of
178 dry ringwoodite can be well predicted by the LDA (Wu et al., 2015). Although
179 the generalized gradient approximation (GGA) is better than LDA for predicting the H-
180 O bonding, LDA is more suitable for calculating elastic properties of many silicate
181 minerals including hydrous wadsleyite (Wang et al., 2019). In order to check the
182 influence of the exchange-correlation function on the hydration effect in ringwoodite,
183 we also calculated the elastic properties of ringwoodite using the GGA at static
184 conditions (Table S2). The results show that the water effects on elastic moduli and
185 velocities of ringwoodite predicted by the GGA are similar to those from the LDA
186 calculations (Table S2).

187 Experiments show that the incorporation of hydrogen into ringwoodite does not
188 affect its space group symmetry, suggesting a disordered distribution of Mg vacancies.
189 In contrast, the presence of a Mg vacancy in $Mg_{15}H_2Si_8O_{32}$ ringwoodite breaks its high
190 symmetry in our calculations. In order to account for the effect of disorder, we averaged
191 the elastic constants over all possible symmetrically equivalent sites for Mg vacancy
192 by following the method used in Núñez-Valdez et al. (2010), and the final elastic tensor
193 has the Fd-3m symmetry and can be fully described by C_{11} , C_{12} , and C_{44} .

194

195 3. Results

196 3.1 Elasticity of hydrous ringwoodite at high P-T conditions

197 The elastic properties, density, and sound velocities of hydrous ringwoodite with
198 1.63 wt% H₂O (Mg₁₅H₂Si₈O₃₂) at high P-T conditions are shown in Fig. 1 and their
199 fitting parameters are reported in Table S3 and Table S4. At ambient conditions, C₁₁,
200 C₁₂, C₄₄, K_S, and G of Mg₁₅H₂Si₈O₃₂ ringwoodite are 8-10% lower than those of
201 Mg₂SiO₄ ringwoodite (Núñez Valdez et al., 2012). Elastic moduli show noticeable
202 nonlinear dependences on pressure, which consequently results in nonlinear pressure
203 dependences of sound velocities (Fig. 1). At 300 K, the first pressure derivatives of K_S,
204 G, V_P, and V_S ($\partial K_S/\partial P$, $\partial G/\partial P$, $\partial V_P/\partial P$, and $\partial V_S/\partial P$) decrease from 4.72, 1.53, 0.0735
205 km s⁻¹ GPa⁻¹, and 0.0231 at km s⁻¹ GPa⁻¹ 0 GPa to 4.11, 0.73, 0.0404 km s⁻¹ GPa⁻¹,
206 and 0.0043 km s⁻¹ GPa⁻¹ at 20 GPa, respectively. In contrast, the elastic moduli and
207 wave velocities show almost linear dependences on temperature, but the temperature
208 effect at high pressure is much weaker than that at low pressure (Fig. 1). The first
209 temperature derivatives of K_S, G, V_P, and V_S ($\partial K_S/\partial T$, $\partial G/\partial T$, $\partial V_P/\partial T$, and $\partial V_S/\partial T$)
210 change from -24.1 MPa/K, -14.5 MPa/K, -0.523×10^{-3} km s⁻¹ K⁻¹, and -0.297×10^{-3} km
211 s⁻¹ K⁻¹ at 0 GPa to -18.1 MPa/K, -8.7 MPa/K, -0.275×10^{-3} km s⁻¹ K⁻¹, and -0.143×10^{-3}
212 km s⁻¹ K⁻¹ at 20 GPa. The elastic moduli and sound velocities of hydrous wadsleyite
213 with 1.63 wt% water also show nonlinear dependences on pressure but almost linear
214 dependences on temperature, and the temperature effect also noticeably reduces at high
215 pressure compared to that at low pressure (Wang et al., 2019). The pressure and
216 temperature derivatives of elastic moduli and wave velocities of Mg₁₅H₂Si₈O₃₂
217 ringwoodite are also comparable with those of Mg₁₅H₂Si₈O₃₂ wadsleyite (Wang et al.,
218 2019). As such, extrapolating low P-T experimental data to high P-T conditions needs
219 to consider these nonlinear pressure effects.

220

221 3.2 Comparisons between theoretical and experimental results

222 In order to compare our results for hydrous ringwoodite with the experimental

223 measurements, the elastic moduli and density are interpolated linearly from
224 ringwoodite with 1.63 wt% water to the previously calculated elasticity of anhydrous
225 ringwoodite (Núñez Valdez et al., 2012) (Fig. S2). Similarly, the effect of iron on the
226 elastic moduli and density are also taken into account using the linear interpolation from
227 the results of Fe-bearing to Fe-free ringwoodite (Núñez Valdez et al., 2012). The
228 combined effects of iron and water content on elastic moduli and density of ringwoodite
229 are estimated by adding the two separate effects together. This strategy is also supported
230 by previous experimental measurements for hydrous Fo89 (Fo, the Mg_2SiO_4 fraction)
231 and Fo100 ringwoodite (Schulze et al., 2018; Wang et al., 2006), which show that the
232 hydration effect is independent of the presence of iron in ringwoodite. Meanwhile, by
233 fitting large datasets of experimental results, Wang et al. (2018) also found co-linear
234 dependences between elastic moduli of ringwoodite and Fe and H₂O concentrations.
235 Similarly, previous theoretical and experimental studies also found that the
236 incorporation of H₂O shows similar reductions on the elastic moduli of Fe-free and Fe-
237 bearing wadsleyite (Wang et al., 2019).

238 The calculated density and elastic properties of hydrous ringwoodite with variable
239 iron and water contents are compared with experimental results in Fig. 2 and Fig. 3,
240 respectively. Our results for the density of hydrous ringwoodite show excellent
241 agreement with previous experimental data (Chang et al., 2015; Jacobsen et al., 2004;
242 Jacobsen and Smyth, 2006; Mao et al., 2012; Schulze et al., 2018; Wang et al., 2006;
243 Ye et al., 2012), with a discrepancy between theoretical and experimental results of less
244 than 1.3% (Fig. 2). This small difference is likely caused by two factors: the mild
245 underestimated volume from LDA calculations (Núñez-Valdez et al., 2013; Núñez
246 Valdez et al., 2012; Wang et al., 2019) and the uncertainties of iron and water contents
247 in experimental samples (Chang et al., 2015). Nevertheless, these comparisons present
248 strong evidence for the reliability of our calculations.

249 The predicted elastic moduli of hydrous ringwoodite also show good agreements
250 with the experimental results of Jacobsen and Smyth (2006) and Wang et al. (2006) at

251 different pressures and 300 K (Fig. 2a and 2b). Experimental results from two Brillouin
252 spectroscopy studies (Mao et al., 2012; Schulze et al., 2018) are in marked
253 disagreement on elastic moduli and sound velocities, especially at high pressures.
254 Although the measured G of hydrous ringwoodite in Mao et al. (2012) is consistent
255 with our results, K_S deviates from our theoretical predictions at high pressure (Fig. 2c).
256 In contrast, the comparison between this work and Schulze et al. (2018) suggests a good
257 agreement in K_S , but the measured G of ringwoodite, especially for Fo89 ringwoodite
258 with 1.04 wt% and 1.71 wt% water, is slightly larger than our predictions (Fig. 2d). It
259 should be noted that experimental values in Schulze et al. (2018) have significant scatter
260 (Fig. 2d), but as well as the experimental uncertainty, the discrepancies in G may also
261 be due to the slightly different dependences of G on iron content between experimental
262 and theoretical studies (Núñez Valdez et al., 2012). In contrast, experimental and
263 theoretical studies are in better agreement over the effect of iron on ringwoodite K_S ,
264 while the results of Mao et al. (2012) show marked disagreement with the results of this
265 study and Schulze et al. (2018). It has also been suggested that different mechanisms
266 for hydrogen incorporation between the studied ringwoodite samples – possibly caused
267 by differences in the synthesis procedure – may be responsible for the discrepancies
268 between experiments (Schulze et al., 2018). However, as discussed earlier, hydrogen
269 is mostly incorporated into ringwoodite through the substitution mechanism
270 $V_{Mg}''+2H^{**}$ (Grüniger et al., 2017; Panero, 2010), which is also supported by the
271 chemical compositions of ringwoodite samples (Jacobsen and Smyth, 2006; Mao et al.,
272 2012; Schulze et al., 2018; Wang et al., 2006) and the dependence of volume on
273 hydration (Schulze et al., 2018). The main reasons for the discrepancies between this
274 study and some experiments and between different experiments are unclear, and further
275 well-designed experiments are needed to clarify this problem.

276

277 **3.3 Water effect on the elastic moduli and velocities of ringwoodite**

278 The current calculations were conducted using the same computational methods,

279 as far as possible, as in previous works on the elasticity of anhydrous hydrous (Núñez
280 Valdez et al., 2012). Together, these calculations provide self-consistent and high-
281 quality data to quantify the hydration effect on elasticity and wave velocities of
282 ringwoodite at high P-T conditions without extrapolation. Our results show that at
283 ambient conditions one weight percent of water dissolved into ringwoodite reduces K_S
284 and G by 5.1% and 6.0%, respectively, consistent with previous experimental
285 observations within uncertainty (Jacobsen and Smyth, 2006; Mao et al., 2012; Schulze
286 et al., 2018; Wang et al., 2006). These reductions in K_S and G result in a 2.3% decrease
287 in V_P and a 2.5% decrease in V_S , which also agree well the recent experimental data
288 (Table S5, Schulze et al., 2018). Such a hydration effect on elastic moduli and wave
289 velocities of ringwoodite is similar to that of wadsleyite (Wang et al., 2019).

290 Compared to ambient pressure, the effect of water on lowering elastic moduli and
291 sound velocities of ringwoodite is reduced at high pressures (Fig. 4 and Fig. S2-S3). At
292 25 GPa and 300 K, the presence of 1.0 wt% water in ringwoodite only decreases K_S , G ,
293 V_P , and V_S by 1.4%, 3.2%, 0.7%, and 1.3%, respectively. The recent experimental and
294 theoretical works (Buchen et al., 2018; Schulze et al., 2018; Wang et al., 2019) also
295 found a significant decrease in the hydration effect on elastic properties and sound
296 velocities in ringwoodite and wadsleyite. However, the hydration effect is strongly
297 enhanced at elevated temperatures (Fig. 4 and Fig. S2-S3). At 25 GPa and 2000 K, the
298 reductions in K_S , G , V_P , and V_S are increased to 3.3%, 4.8%, 1.7%, and 2.2%,
299 respectively, which are much greater than those at 25 GPa and 300 K. Similar results
300 have also been found in wadsleyite (Wang et al., 2019). Thus, we conclude that the
301 hydration effect on elastic moduli and wave velocities of nominally anhydrous minerals
302 at low P-T conditions cannot be simply applied to the mantle conditions, and the
303 extrapolation may cause large uncertainties.

304

305 **4. Discussion**

306 **4.1 Hydration effect on velocity reductions in a pyrolitic mantle**

307 Combining our results with previous studies (Gréaux et al., 2019; Irifune et al.,
308 2008; Núñez Valdez et al., 2012), we estimated the hydration effect on the wave
309 velocities of a pyrolitic mantle (58% ringwoodite (10 mol% Fe) + 35% majorite (the
310 ‘pyrolite minus olivine’ composition) + 7% calcium perovskite) (Irifune et al., 2010) as
311 a function of water content in ringwoodite and temperature anomaly at the conditions
312 of the lower MTZ (Fig. 5). Here we do not consider the hydration effect in majorite
313 because its water solubility does not exceed 0.1 wt% (Ohtani, 2015), which should be
314 a negligible effect on the modeling results. We find that the incorporation of 1.0 wt%
315 water into ringwoodite would decrease the sound velocities of the pyrolitic mantle by -
316 1.0% in V_P and -1.4% in V_S at the conditions of the lower MTZ (Fig. 5). Such ΔV_P and
317 ΔV_S magnitudes can be also produced by increasing the temperature by 230 K (Fig. 5),
318 showing that the presence of a negative temperature anomaly can make the hydration
319 effect invisible. In addition, the presence of 0.2 wt% water in ringwoodite can only
320 produce ΔV_P and ΔV_S anomalies of -0.3%, so it is unlikely that such small amounts of
321 water can be identified by seismic observations (Houser, 2016).

322 Schulze et al. (2018) also estimated the dependence of velocity reduction in a
323 pyrolitic mantle on ringwoodite hydration and found that the V_S would only decrease
324 by about 0.3% for the incorporation of 1.0 wt% water into ringwoodite at the conditions
325 of the MTZ. This value is much lower than our results, mainly because they assumed
326 the effect of water on the elastic moduli of ringwoodite at ambient temperature would
327 be appropriate at the temperature of the MTZ. Instead, the hydration effect is strongly
328 enhanced by increasing temperature (Fig. 4 and Fig. S2-S3). Mao et al. (2012) predicted
329 that the presence of 1.0 wt% water in ringwoodite would decrease V_P and V_S by 7.0%
330 and 4.5% at the conditions of the lower MTZ, respectively. Such velocity reductions
331 lead to a ΔV_P of about -4.2% and a ΔV_S of -2.5% for a pyrolitic composition, much
332 larger than our predictions. This again is due to the significant differences in the results
333 of hydrous ringwoodite between this study and Mao et al. (2012) (Fig. 3) and a large
334 extrapolation to MTZ conditions.

335 We also estimated the effects of ringwoodite hydration and temperature on the
336 V_P/V_S ratio for a pyrolitic composition (Fig. S4). Our results show that the
337 incorporation of 1.0 wt% water into ringwoodite only increases the V_P/V_S ratio of
338 pyrolite by $\sim 0.3\%$, suggesting that the V_P/V_S anomaly ($\Delta(V_P/V_S)$) is not significantly
339 sensitive to water content. Previous seismological work (Li et al., 2013) found a V_P/V_S
340 anomaly of $> +2.1\%$ in the lower MTZ beneath Northeast China and ascribed it as a
341 result of hydrous MTZ. However, according to our results, such a $\Delta(V_P/V_S)$ cannot be
342 caused by the presence of water in the MTZ, and other reasons such as the partial
343 melting induced by upwelling (Tang et al., 2014) may account for the high V_P/V_S ratio.
344 The hydration state of the MTZ would certainly be hard to identify by the $\Delta(V_P/V_S)$.
345

346 **4.3 Mapping the amount of water in the lower MTZ**

347 The presence of water lowers the seismic velocities (Fig. 5) and deepens the 660-
348 km discontinuity simultaneously (Higo et al., 2001). Increasing temperature also results
349 in negative velocity anomalies, but in contrast to water, temperature will elevate the
350 660-km discontinuity to shallower depths (Bina and Helffrich, 1994; Fei et al., 2004;
351 Higo et al., 2001; Irifune, 1998; Yu et al., 2007). Thus, the observed topography of the
352 660-km discontinuity and seismic velocity anomalies in the lower MTZ could result
353 from the combined effects of water amount and temperature variations.

354 In order to constrain the water content in the MTZ, Houser (2016) compared the
355 topography of the 410- and 660-km discontinuities and shear wave velocities within the
356 MTZ, with literature mineral physics data. That work concluded that the transition is
357 mostly dry. However, several problems exist with the mineral physics used in that study.
358 First, as we point out above, the extrapolation of experimental data at low temperature
359 to the MTZ's temperature may lead to large uncertainties in estimating the hydration
360 effect on ringwoodite's sound velocities. And, as discussed in section 4.1 and 4.2,
361 significant differences in hydration effect exist between different experimental studies.
362 Second, Houser (2016) used the hydration effect on ringwoodite rather than that on

363 pyrolite to estimate the relationship between ΔV_S and water content; this alone is likely
364 to bias the results to systematically lower water contents. Third, the temperature profile
365 of the transition was assumed to be the same everywhere. These shortcomings may
366 account for the inference that very few seismic observations match the predictions from
367 mineral physics in Houser (2016). Even for these locations where seismic observations
368 could be explained by the presence of water, the water concentration from the
369 topography of the 660-km discontinuity is different from the one from the shear wave
370 velocity anomalies (Houser, 2016).

371 We therefore decided to use our elastic data calculated in this work with the
372 seismic observations in Houser (2016) to map out the water concentration in the lower
373 MTZ. The seismic observations on the depth variation of the 660-km discontinuity (Δd)
374 and the V_S anomalies (ΔV_S) in the lower MTZ are taken as targets to match. Unlike
375 Houser (2016), we do not also use the depth variation of the 410-km discontinuity
376 (which also depends on water content and temperature) as one of the constraints
377 because the hydration state of the MTZ may vary with depth. The dependence of ΔV_S
378 on water content and temperature expected in pyrolite are derived from our study, and
379 the effects of water and temperature on the depth of the 660-km discontinuity are
380 determined using literature data. The temperature effect on the depth of the 660-km
381 discontinuity is adopted as -0.06 km/K and the effect of ringwoodite hydration on the
382 depth of the 660-km discontinuity is adopted as $+6$ km/wt% (Higo et al., 2001, Fig. S5).
383 Solutions for water content and temperature anomaly were determined using a Monte
384 Carlo simulation, in which 70000 initial inputs were randomly produced in the ranges
385 of 0-1.6 wt% for water content and -800-+800 K for temperature anomaly. The outputs
386 were kept if they match the observed ΔV_S within 0.3% and Δd within 3 km (Fig. S6).
387 The final amount of water in the lower MTZ is estimated by the product of water
388 content in ringwoodite and the fraction of ringwoodite (58%).

389 We found that $\sim 79\%$ of the bins that have observations of both ΔV_S and Δd (blue
390 areas in Fig. 6a) can be satisfied by a pyrolitic mantle with variable amounts of water

391 and temperature. We also find that the water concentration within 57% of the bins
392 exceeds 0.1 wt% (Fig. 8). In contrast, Houser (2016) found that only 8% of the bins
393 with high-quality data are consistent with the presence of water based on the same
394 seismic observations, but the water concentration estimated from ΔV_S is much lower
395 than the one constrained from Δd . Our modeling results show that the water
396 concentration and temperature anomaly in the lower MTZ vary from 0 to 0.9 wt% and
397 from -350 K to +350 K (Fig. 7), respectively. The average temperature anomaly is -
398 29 ± 21 K and the average water concentration is 0.25 ± 0.06 wt%. If the remaining 21%
399 of bins are dry, the lower MTZ is somewhat hydrous, with about 0.2 ± 0.04 wt% water.
400 As discussed above, the difference between our results and those of Houser (2016) is
401 probably due to the mineral physics data and because we allowed the temperature of
402 the transition zone to vary laterally.

403 Globally, there is no evident correlation between the modeled water concentration
404 and temperature anomaly, but the maximum water concentration decreases with
405 increasing temperature anomaly (Fig. S7) and does not exceed the water solubility in
406 ringwoodite determined by experimental studies (Fei and Katsura, 2020 and references
407 therein). The temperature anomaly and the water content in the lower MTZ vary by
408 region. In general, the temperature anomaly in the western Pacific ranges from -300 K
409 to -50 K, while the central and eastern Pacific is somewhat hotter. The lower MTZ
410 beneath the Philippine Sea and the Hawaiian Islands, and North Asia is quite hydrous,
411 which is also supported by the high conductivity anomalies beneath these regions
412 (Shimizu et al., 2010). In particular, the high conductivity beneath the Philippine Sea
413 cannot be explained only by the temperature effect and the region would contain 0.5-
414 1.0 wt% water in the lower MTZ (Shimizu et al., 2010), if the cause of the high
415 conductivity is due to the presence of water. Such an estimate is consistent with our
416 model (Fig. 7a). In addition, other studies (Kelbert et al., 2009; Munch et al., 2018;
417 Semenov and Kuvshinov, 2012) also found high conductivity anomalies in the lower
418 MTZ beneath North Asia, which can be explained by our predicted water amount in

419 this region (Fig. 7a). The substantial amount of water in the lower MTZ beneath these
420 local regions may have resulted in seismic anomalies at the top of the lower mantle
421 if there is a downward flow (Bercovici and Karato, 2003; Schmandt et al., 2014), which
422 might be detected by further seismic studies.

423 The remaining 21% of bins where ΔV_S and Δd cannot be explained by our models
424 (red areas in Fig. 6a) can be divided into three groups: (1) $-\Delta d, +\Delta V_S$; (2) $-\Delta d, -\Delta V_S$;
425 (3) $+\Delta d, +\Delta V_S$. In principle, the pattern of $(-\Delta d, +\Delta V_S)$ cannot be produced by the
426 variations in water content and temperature because $-\Delta d$ can be only produced by the
427 positive temperature anomaly, which cannot produce $+\Delta V_S$ with or without water. For
428 the regions with $(-\Delta d, -\Delta V_S)$ and $(+\Delta d, +\Delta V_S)$, the Δd within these bins could be caused
429 by temperature anomalies, but the observed ΔV_S exceeds the range predicted by mineral
430 physics and the presence of water will widen the ΔV_S difference between seismic
431 observations and mineral models even further (Fig. 6b). Thus, these bins cannot be
432 matched by varying water content and temperature within reasonable ranges and
433 require high-velocity heterogeneities to explain their ΔV_S . Harzburgite, which is
434 composed of $\sim 80\%$ ringwoodite and 20% majorite at the conditions of the MTZ, is
435 found to have higher velocities than pyrolite in the lower MTZ (Gréaux et al., 2019)
436 and could be a candidate for such heterogeneities. However, we cannot rule out the
437 possibility of the presence of heterogeneities in other regions where the seismic
438 observations are consistent with the current mineral models. If there is harzburgite,
439 more water is needed to explain the observed ΔV_S (Fig. 6b).

440 We also find similar results for the hydration state of the lower MTZ using other
441 seismic models. For instance, using the topography of the 660-km discontinuity from
442 Guo and Zhou (2020) and shear wave velocity anomaly within the lower MTZ from
443 the S40RTS model (Ritsema et al., 2011), most of the bins with observations of both
444 ΔV_S and Δd can be explained by our models (Fig. S8) (84% in this case versus 79%
445 above). The water concentration varies from 0 to 0.9 wt%, which is the same as with
446 the Houser (2016) tomography, and the temperature anomaly is also similar, varying

447 from -550 K to +300 K (Fig. S8). Despite some small-scale local mismatches due to
448 the difference between the two seismic models, the average water concentration is
449 0.18 ± 0.05 wt% and the average temperature anomaly is -23 ± 26 K, both of which
450 similar to the results inferred from Houser's seismic models.

451 Our results suggest that globally the lower MTZ is somewhat hydrous, with about
452 0.2 ± 0.04 wt% water. Such an amount of water is consistent with the magnetotelluric
453 model in Kelbert et al. (2009) within the uncertainty, although large discrepancies still
454 exist between different magnetotelluric studies (Huang et al., 2005; Kelbert et al., 2009;
455 Yoshino et al., 2008). Based on the mantle viscosity profile inferred from the postglacial
456 rebound data, Fei et al. (2017) suggested a nearly water-saturated MTZ (1-2 wt% water),
457 especially at the lowest reaches of the MTZ, significantly higher than the amount
458 estimated in this study. This may be because the viscosity model predicted by mineral
459 physics in Fei et al. (2017) did not consider the effect of majorite, which is one of the
460 major minerals in the MTZ. Also, it should be noted that the viscosity profile for the
461 MTZ inferred from the geoid and postglacial rebound data differs by one order of
462 magnitude between independent studies (Čížková et al., 2012). As such, the viscosity
463 may not be a good sensor for the water content in the MTZ.

464 Our previous work found that wadsleyite in a pyrolitic mantle should contain ~ 0.9
465 wt% water to match the density and seismic velocity jumps across the 410-km
466 discontinuity, suggesting a hydrous uppermost MTZ with a water concentration of ~ 0.5
467 wt% (Wang et al., 2019). This implies that the water concentration in the MTZ may
468 decrease with depth globally, from ~ 0.5 wt% in the upper part to ~ 0.15 - 0.2 wt% in the
469 lower part, which may partly contribute to the observed velocity gradients in the MTZ
470 (Thio et al., 2016). Accordingly, the MTZ contains about one ocean mass equivalent
471 water.

472

473 **5. Conclusion**

474 We investigated the elastic properties and velocities of hydrous ringwoodite

475 containing 1.63 wt% water at high P-T conditions using first-principles calculations
476 within the LDA. Our results show that the elastic moduli of the hydrous ringwoodite
477 are 8-10% lower than those of dry ringwoodite at ambient conditions. Elastic moduli
478 and wave velocities show noticeable nonlinear dependences on pressure, with their
479 pressure derivatives decreasing with increasing pressure. In contrast, the elastic moduli
480 and wave velocities show almost linear dependences on temperature, but the
481 temperature effect at high pressure is much weaker than that at low pressure. The
482 calculated elastic moduli and density of hydrous ringwoodite with variable water
483 contents agree well with most of the experimental data.

484 Our calculations were conducted using the same computational methods as in
485 previous works on the elasticity of anhydrous ringwoodite (Núñez Valdez et al., 2012)
486 and hence provided self-consistent and high-precision data to estimate the hydration
487 effect on the elasticity and velocities of ringwoodite. At ambient conditions, one weight
488 percent of water dissolved into ringwoodite reduces the K_S , G , V_P , and V_S by 5.1%,
489 6.0%, 2.3%, and 2.5%, respectively. The hydration effect is significantly reduced at
490 high pressures but strongly enhanced at elevated temperatures. At 25 GPa and 2000 K,
491 the reductions in K_S , G , V_P , and V_S caused by the presence of 1.0 wt% water are 3.3%,
492 4.8%, 1.7%, and 2.2%, respectively. Combining our results with previous studies, we
493 find that the incorporation of 1.0 wt% water into ringwoodite would decrease the wave
494 velocities of the pyrolitic mantle by -1.0% in V_P and -1.4% in V_S at MTZ conditions.

495 We evaluated the amount of water in the lower MTZ using the seismic
496 observations on the depth variation of the 660-km discontinuity (Δd) and the V_S
497 anomalies (ΔV_S) in the lower MTZ from previous seismic models. Most bins with ΔV_S
498 and Δd can be matched by our models and the remaining bins require high-velocity
499 heterogeneities such as harzburgite to explain their ΔV_S . The average water
500 concentration in the lower MTZ is 0.2 ± 0.04 wt%, with an interregional variation from
501 0 to 0.9 wt%. Together with our previous work on the water content in the upper MTZ
502 (Wang et al., 2019), we suggest that the water concentration in the MTZ likely changes

503 with depth globally and the whole MTZ contains about one ocean mass equivalent
504 water.

505

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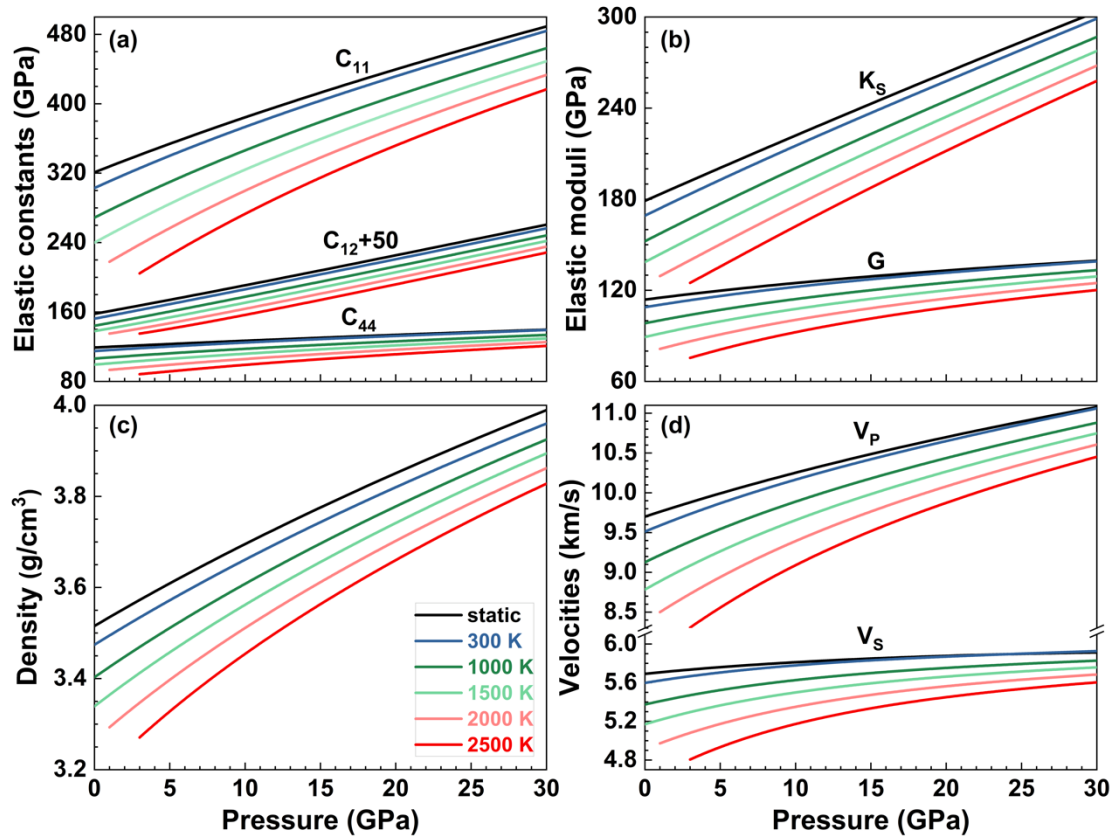
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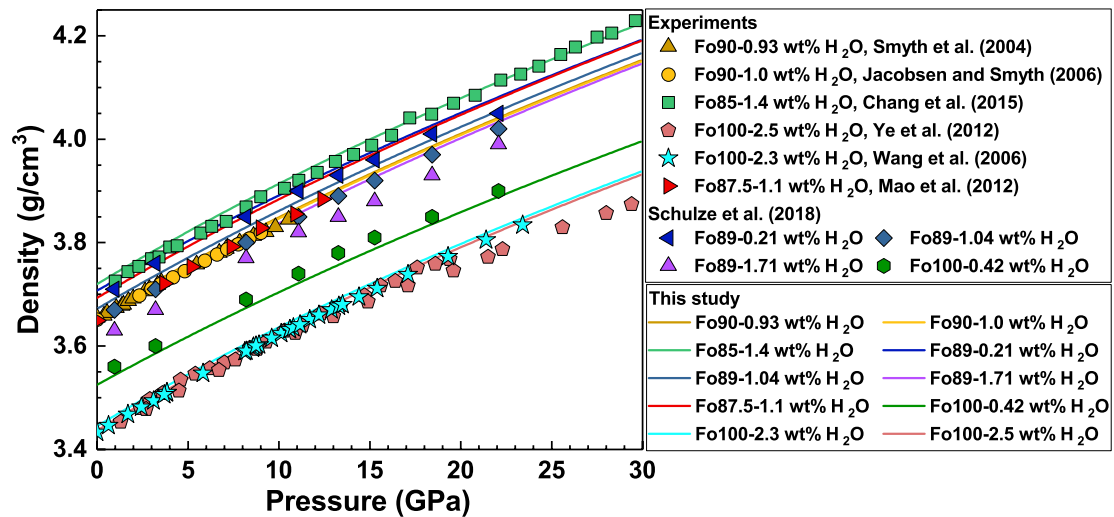
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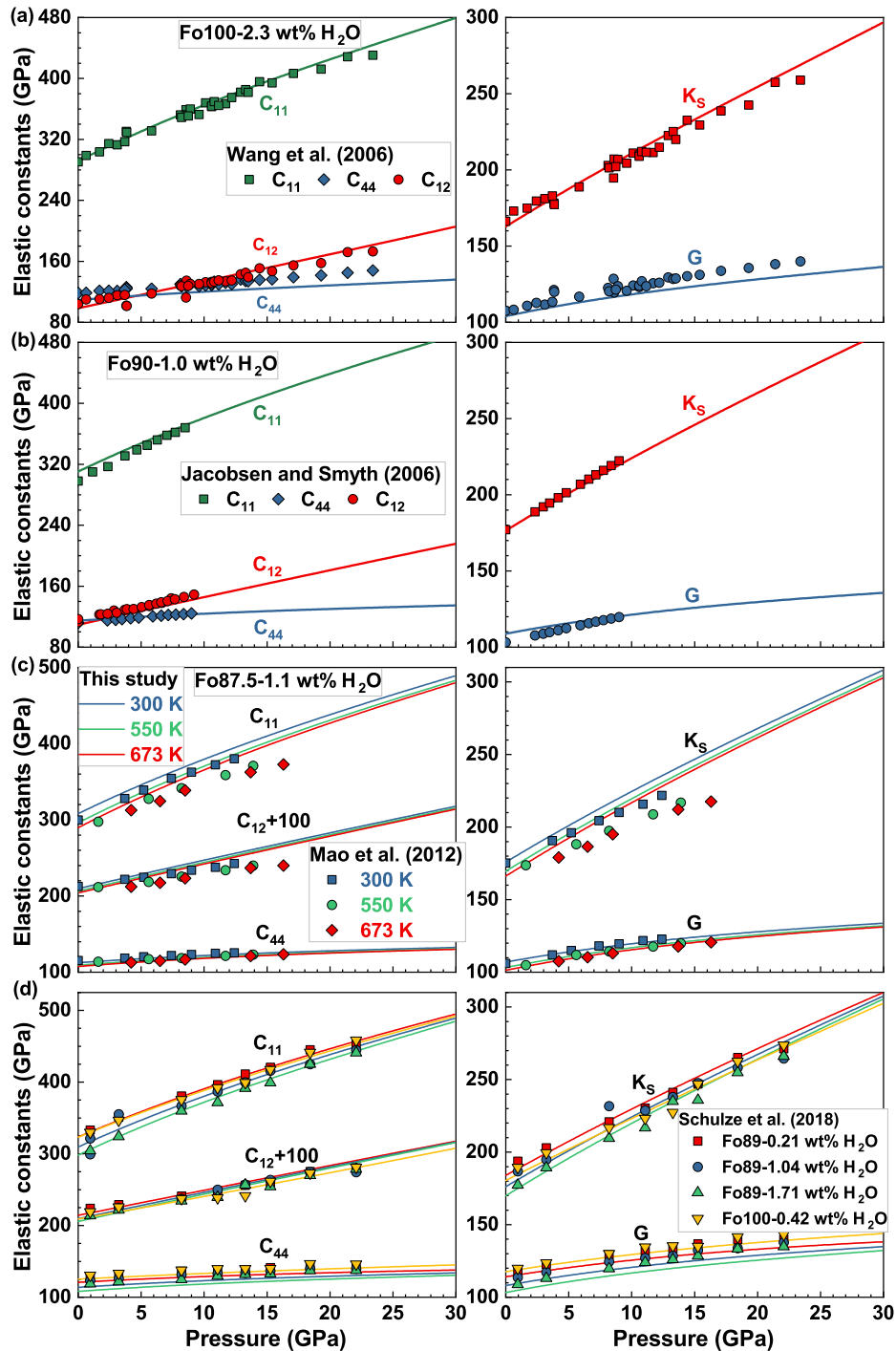
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791 **Figure 1.** Elastic moduli, density, and velocities of hydrous ringwoodite with 1.63 wt%
 792 H₂O (Mg₁₅H₂Si₈O₃₂) at different pressures and temperatures. (a) elastic constants (C_{11} ,
 793 C_{12} , and C_{44}), (b) bulk and shear moduli (K_S and G), (c) density, and (d) compressional
 794 and shear wave velocities (V_P and V_S).



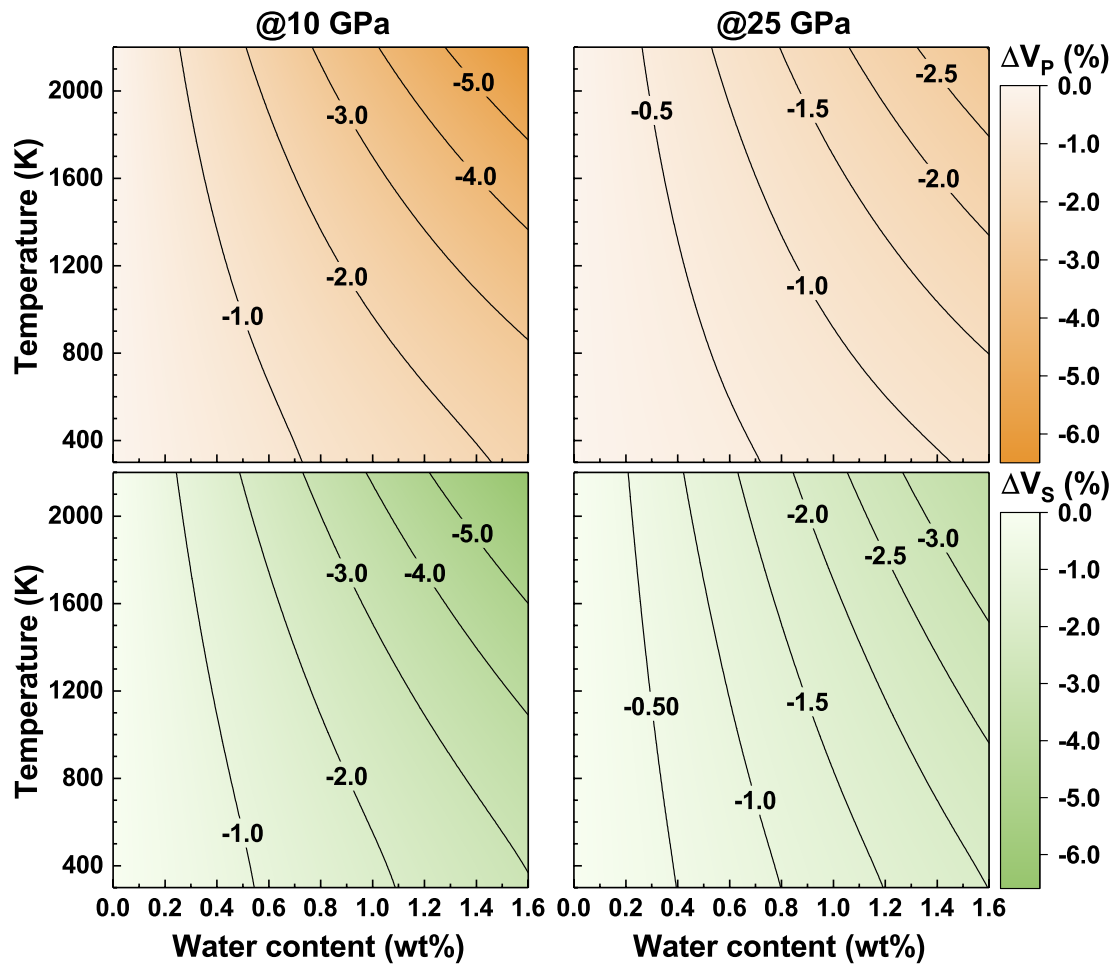
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796 **Figure 2.** Comparisons of the density of hydrous ringwoodite between theoretical
 797 results and experimental measurements (Chang et al., 2015; Jacobsen et al., 2004;
 798 Jacobsen and Smyth, 2006; Mao et al., 2012; Schulze et al., 2018; Wang et al., 2006;
 799 Ye et al., 2012) (scattered points). Solid lines represent the density of
 800 hydrous ringwoodite with different water and Fe contents using linear interpolation
 801 from calculated results of $\text{Mg}_{15}\text{Si}_8\text{O}_{30}(\text{OH})_2$ ringwoodite in this study and anhydrous
 802 ringwoodite (Fo100 and Fo87.5) in previous work (Núñez Valdez et al., 2012). The Fe
 803 content of ringwoodite is marked by the Mg_2SiO_4 fraction (Fo). The combined effect is
 804 estimated by adding the water and Fe effects together.



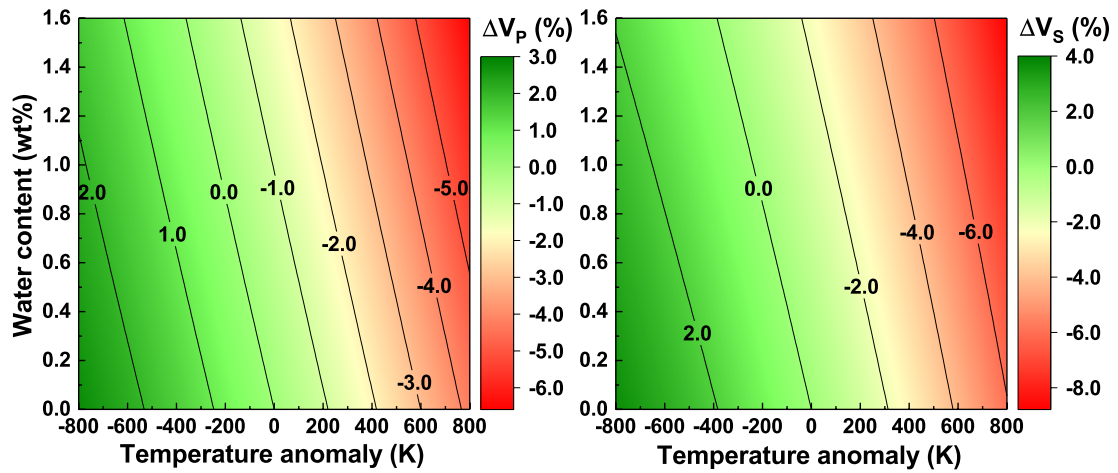
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806 **Figure 3.** Comparisons of the elastic properties of hydrous ringwoodite between
 807 theoretical results and experimental measurements (Jacobsen and Smyth, 2006; Mao et
 808 al., 2012; Schulze et al., 2018; Wang et al., 2006) (scattered points). Solid lines
 809 represent the theoretical results estimated using linear interpolation from calculated
 810 results of $\text{Mg}_{15}\text{Si}_8\text{O}_{30}(\text{OH})_2$ ringwoodite in this study and anhydrous ringwoodite
 811 (Fo100 and Fo87.5) in previous work (Núñez Valdez et al., 2012).



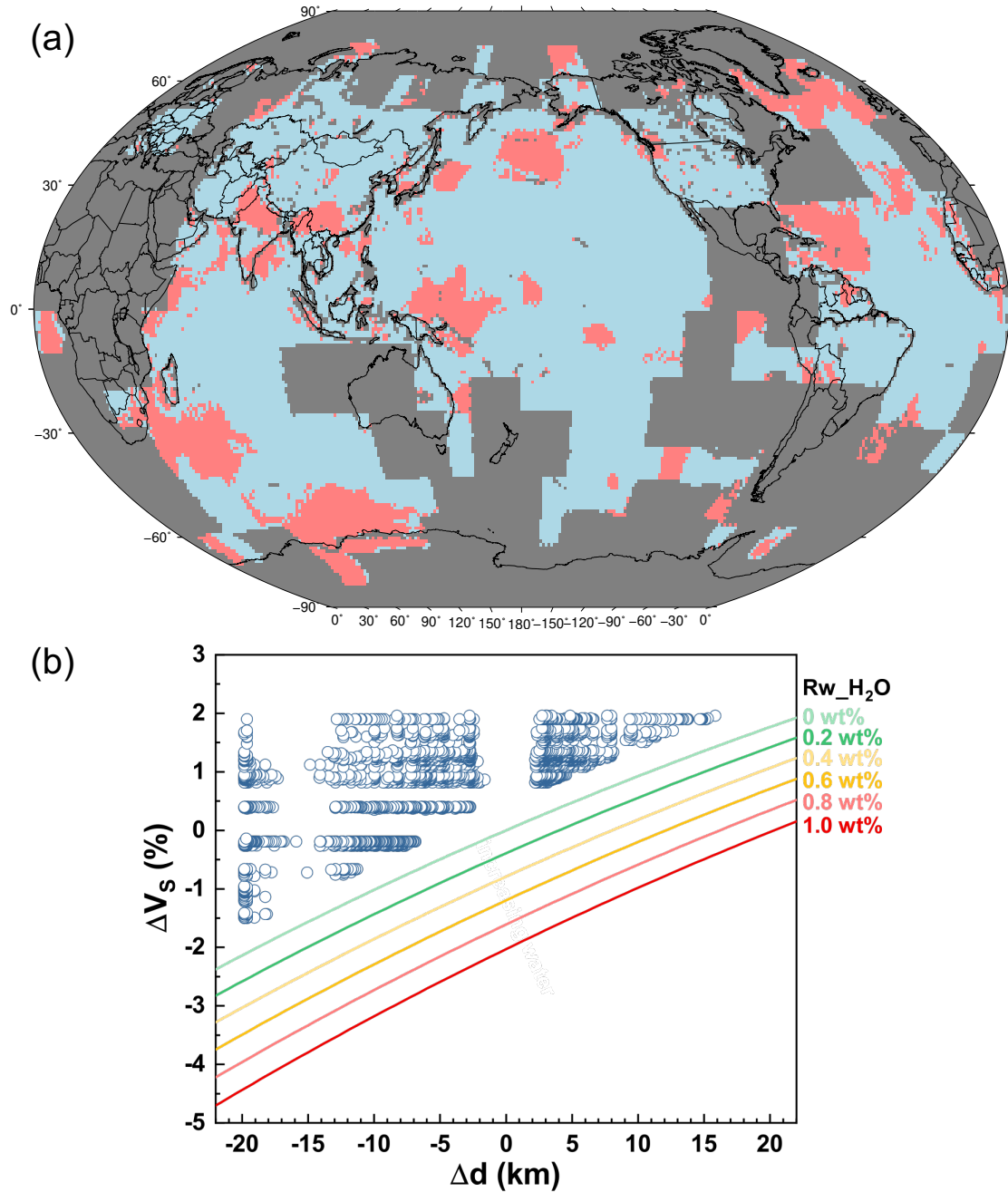
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813 **Figure 4.** Velocity reductions in ringwoodite as a function of water content at different
 814 temperatures and pressures (10 GPa and 25 GPa). The velocity contrasts (ΔV_P and ΔV_S)
 815 refer to the V_P and V_S differences between hydrous and anhydrous ringwoodite.



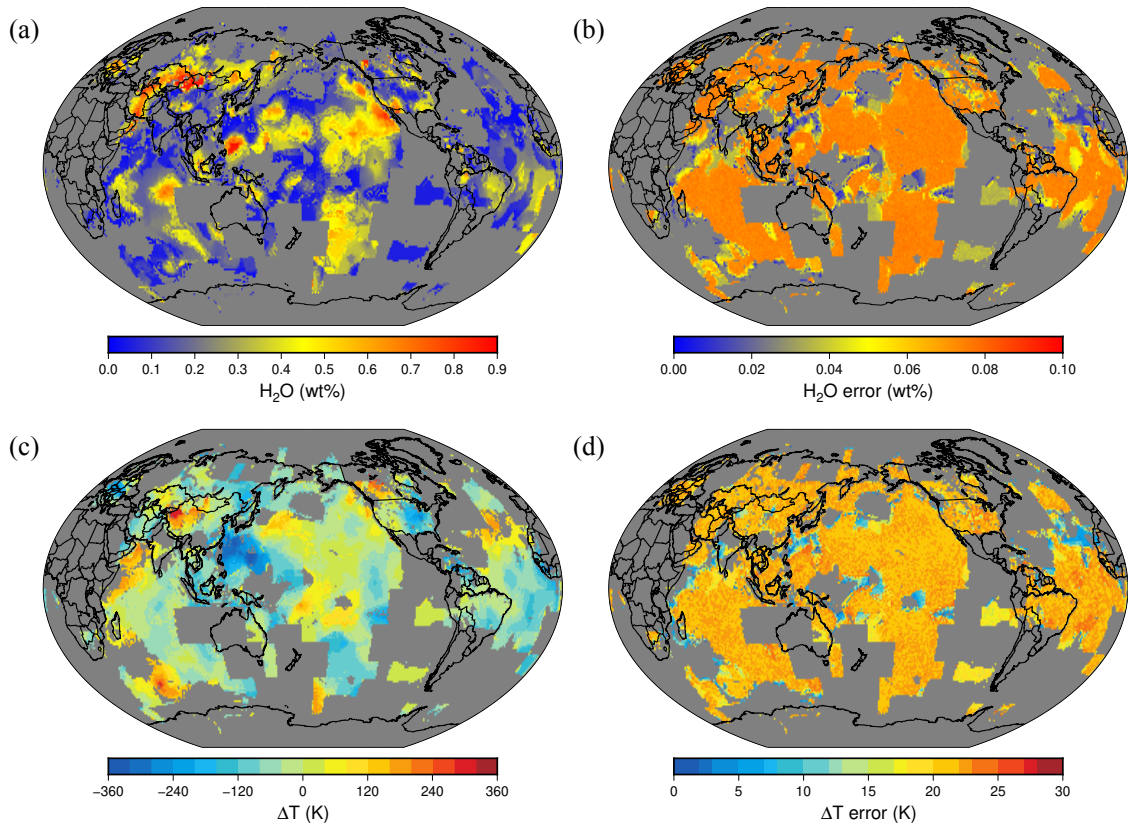
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817 **Figure 5.** Velocity anomalies (ΔV_P and ΔV_S) in pyrolite caused by ringwoodite
 818 hydration and temperature anomaly at 23.5 GPa. Under the conditions of the MTZ,
 819 pyrolite consists of $\sim 57\%$ ringwoodite, 35% majorite, and 8% calcium perovskite
 820 (Irifune et al., 2010). The velocities of anhydrous pyrolite are taken as the references to
 821 calculate ΔV_P and ΔV_S . The temperature anomaly is with respect to the normal mantle
 822 temperature from Brown and Shankland (1981).



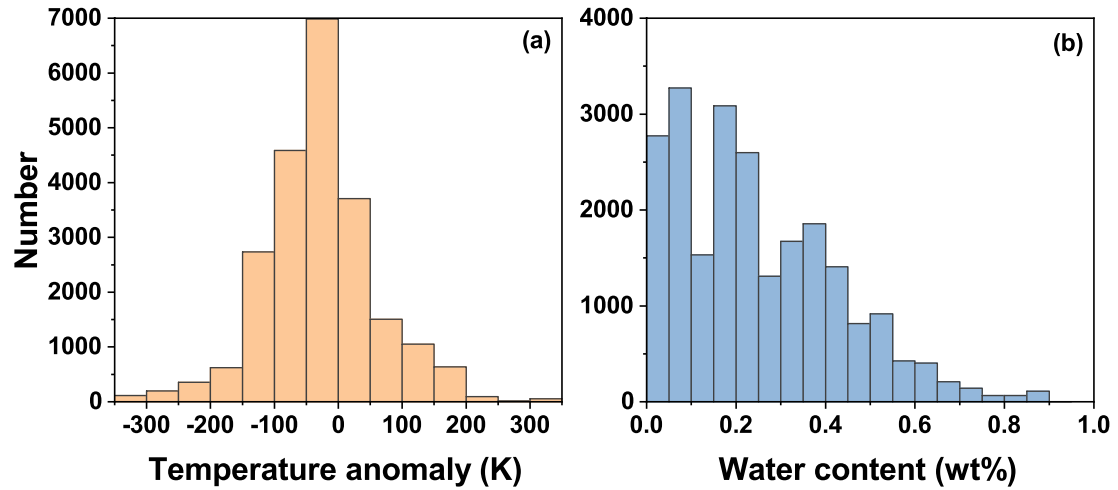
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824 **Figure 6.** (a) Regions covered by the seismic observations (the depth variation of 660-
 825 km discontinuity (Δd) and the shear velocity anomaly (ΔV_s)). The blue areas (79%)
 826 represent the bins with Δd and ΔV_s that can be matched by our models and the red areas
 827 (21%) are the remaining bins that are not consistent with the current mineral models.
 828 (b) the ΔV_s and Δd within the remaining 21% of bins (open circles) compared to the
 829 predictions from mineral physics (lines). Rw_{H_2O} refers to the water concentration in
 830 ringwoodite.



831

832 **Figure 7.** Water concentration (H₂O wt%) and temperature anomaly (ΔT (K)) in the
 833 lower MTZ inferred from the depth variation of 660-km discontinuity and the shear
 834 velocity anomaly. (a) the map of water concentration and (b) the standard error of H₂O
 835 amount; (c) the map of temperature anomaly and (d) the standard error of ΔT.



836

837 **Figure 8.** Distributions of temperature anomaly and water content from each bin with
 838 the observed ΔV_s and Δd that are consistent with the mineral physics model. The
 839 average temperature anomaly and water concentration are -29 ± 21 K and 0.25 ± 0.06
 840 wt%, respectively.

841 **Table S1.** Density, elastic moduli, and sound velocities of hydrous ringwoodite with
842 different substitution mechanisms at static conditions.

Substitutions	Pressure (GPa)	density (g/cm ³)	K _S (GPa)	G (GPa)	V _P (km/s)	V _S (km/s)
Mechanism 1 Mg ₁₅ H ₂ Si ₈ O ₃₂ V _{Mg} " +2H** 1.63 wt% H ₂ O	0	3.536	183.9	115.1	9.767	5.705
	5	3.628	205.5	121.1	10.057	5.777
	10	3.713	226.6	126.3	10.313	5.831
	15	3.793	247.0	130.2	10.530	5.859
	20	3.867	267.7	132.8	10.724	5.860
	30	4.004	308.5	140.6	11.130	5.926
Mechanism 2 Mg ₃₂ Si ₁₅ H ₄ O ₆₄ V _{Si} " +4H**** 1.62 wt% H ₂ O	0	3.539	179.2	110.6	9.607	5.590
	5	3.632	202.2	121.7	10.016	5.788
	10	3.719	223.7	127.9	10.297	5.865
	15	3.799	246.0	133.0	10.556	5.916
	20	3.874	266.1	137.3	10.768	5.953
	30	4.011	306.8	143.8	11.148	5.987
Mechanism 3 Mg ₁₆ H ₂ Si ₇ O ₃₂ Mg _{Si} " +2H** 1.64 wt% H ₂ O	0	3.418	178.3	109.4	9.738	5.657
	5	3.509	200.0	115.3	10.040	5.732
	10	3.593	221.5	119.8	10.301	5.774
	15	3.671	241.9	123.7	10.528	5.806
	20	3.744	261.9	126.7	10.727	5.817
	30	3.879	300.3	131.3	11.069	5.818
*(1):(2):(3)=65:25:10 1.63 wt% H ₂ O	0	3.525	182.1	113.4	9.724	5.672
	5	3.617	204.1	120.7	10.045	5.775
	10	3.703	225.4	126.0	10.308	5.834
	15	3.782	246.2	130.2	10.536	5.868
	20	3.857	266.7	133.3	10.735	5.879
	30	3.993	307.3	140.5	11.128	5.930

***(1):(2):(3)=75:14:11 1.63 wt% H ₂ O	0	3.524	182.6	113.8	9.741	5.684
	5	3.616	204.4	120.5	10.049	5.773
	10	3.701	225.7	125.8	10.310	5.830
	15	3.780	246.3	129.9	10.534	5.861
	20	3.855	266.8	132.8	10.731	5.868
	30	3.991	307.4	140.0	11.126	5.923

843 There are three possible mechanisms for the incorporation of hydrogen into
844 ringwoodite (Panero, 2010): (1) $V_{Mg}'' + 2H^{*}$, Mg vacancy with charge balanced by
845 two H atoms; (2) $V_{Si}'''' + 4H^{*}$, Si vacancy with charge balanced by four H atoms;
846 (3) $Mg_{Si}'' + 2H^{*}$, Si vacancy is occupied by Mg atom with charge balanced by two H
847 atoms. Previous first-principles calculations (Panero, 2010) found that the three
848 substitution mechanisms exist in ratios of 64:25:10 for (1):(2):(3). Results of a least
849 squares fit to existing experimental data on hydrous ringwoodite show the three defects
850 in ratios of 75:14:11 (Panero, 2010).

851 *Results of hydrous ringwoodite with the substitution mechanism ratios of 65:25:10.

852 **Results of hydrous ringwoodite with the substitution mechanism ratios of 75:14:11.

853 Table S2. The water effects on the elastic moduli, density, and sound velocities of
 854 ringwoodite calculated within LDA and GGA at static conditions.

	P (GPa)	GGA					LDA				
		K _S (GPa)	G (GPa)	V _P (km/s)	V _S (km/s)	density (g/cm ³)	K _S (GPa)	G (GPa)	V _P (km/s)	V _S (km/s)	density (g/cm ³)
Anhydrous ringwoodite (Mg ₂ SiO ₄)	0	176.3	118.6	9.791	5.831	3.490	196.3	124.6	10.018	5.874	3.611
	5	197.8	125.4	10.091	5.915	3.584	217.4	130.9	10.293	5.949	3.700
	10	218.6	131.3	10.356	5.981	3.671	238.3	135.3	10.523	5.982	3.782
	15	237.6	136.4	10.574	6.030	3.752	257.7	139.2	10.719	6.007	3.858
	20	257.8	140.8	10.789	6.066	3.828	278.5	142.8	10.920	6.026	3.932
	25	277.3	144.8	10.983	6.093	3.900	298.1	145.4	11.084	6.028	4.000
Hydrous ringwoodite (Mg ₁₅ H ₂ Si ₈ O ₃₂)	0	163.1	107.8	9.487	5.623	3.408	183.9	115.1	9.767	5.705	3.536
	5	184.4	115.1	9.815	5.730	3.508	205.5	121.1	10.057	5.777	3.628
	10	205.4	121.2	10.100	5.804	3.599	226.6	126.3	10.313	5.831	3.713
	15	226.3	126.6	10.358	5.864	3.683	247.0	130.2	10.530	5.859	3.793
	20	246.5	131.6	10.590	5.913	3.762	267.7	132.8	10.724	5.860	3.867
	25	266.8	135.9	10.806	5.951	3.836	288.0	136.2	10.918	5.880	3.938
Reductions per weight of water	0	-8.1	-6.7	-0.186	-0.127	-0.050	-7.6	-5.8	-0.154	-0.103	-0.046
	5	-8.2	-6.3	-0.170	-0.114	-0.047	-7.3	-6.0	-0.145	-0.105	-0.044
	10	-8.0	-6.2	-0.157	-0.109	-0.044	-7.2	-5.6	-0.128	-0.093	-0.042
	15	-6.9	-6.0	-0.132	-0.102	-0.042	-6.6	-5.6	-0.116	-0.091	-0.040
	20	-6.9	-5.7	-0.122	-0.093	-0.040	-6.6	-6.1	-0.120	-0.102	-0.040
	25	-6.5	-5.5	-0.109	-0.087	-0.039	-6.2	-5.6	-0.101	-0.091	-0.038

856 **Table S3.** Elastic moduli and velocities of hydrous ringwoodite with 1.63 wt% H₂O
857 (Mg₁₅H₂Si₈O₃₂) and their first and second derivatives with respect to pressure and
858 temperature. The polynomial fitting equation is $M = M_0 + \left(\frac{\partial M}{\partial P}\right) \cdot P + \left(\frac{\partial M}{\partial T}\right) \cdot (T -$
859 $300) + \left(\frac{\partial^2 M}{\partial P^2}\right) \cdot P^2 + \left(\frac{\partial^2 M}{\partial T^2}\right) \cdot (T - 300)^2 + \left(\frac{\partial^2 M}{\partial P \partial T}\right) \cdot P \cdot (T - 300), M =$
860 $C_{11}, C_{12}, C_{44}, K_S, G, V_P,$ and V_S .

Parameters	C ₁₁	C ₁₂	C ₄₄	K _S	G
M_0 (GPa)	304.3	102.9	115.3	170.0	109.2
$\frac{\partial M}{\partial P}$	7.60	3.28	1.06	4.72	1.53
$\frac{\partial M}{\partial T}$ (MPa/K)	-47.5	-12.4	-12.2	-24.1	-14.5
$\frac{\partial^2 M}{\partial P^2}$ ($\times 10^{-3}$ GPa ⁻¹)	-58.4	6.3	-9.9	-15.3	-19.9
$\frac{\partial^2 M}{\partial P \partial T}$ ($\times 10^{-3}$ K ⁻¹)	0.856	0.023	0.189	0.301	0.291
$\frac{\partial^2 M}{\partial T^2}$ ($\times 10^{-6}$ GPa K ⁻¹)	-3.09	-0.59	-0.62	-1.43	-0.90
	V _P			V _S	
M_0 (km s ⁻¹)	9.526			5.603	
$\frac{\partial M}{\partial P}$ (km s ⁻¹ GPa ⁻¹)	0.0735			0.0231	
$\frac{\partial M}{\partial T}$ ($\times 10^{-3}$ km s ⁻¹ K ⁻¹)	-0.523			-0.297	
$\frac{\partial^2 M}{\partial P^2}$ ($\times 10^{-3}$ km s ⁻¹ GPa ⁻²)	-0.828			-0.471	
$\frac{\partial^2 M}{\partial P \partial T}$ ($\times 10^{-6}$ km s ⁻¹ GPa ⁻¹ K ⁻¹)	12.4			7.7	
$\frac{\partial^2 M}{\partial T^2}$ ($\times 10^{-6}$ km s ⁻¹ K ⁻²)	0.041			-0.025	

861

862 **Table S4.** Equation of state of hydrous ringwoodite 1.63 wt% H₂O (Mg₁₅H₂Si₈O₃₂).
863 The relationship between pressure and volume is fitted by the third-order Birch-
864 Murnaghan equation: $P(V) = 3K_{T0}f(1 + 2f)^{5/2}(1 + 3/2(K'_{T0} - 4)f)$, where $f =$
865 $1/2[(V_0/V)^{2/3} - 1]$, P is pressure, V_0 is the volume at ambient pressure, V is high-
866 pressure volume, and K_{T0} and K'_{T0} are the isothermal bulk modulus and its pressure
867 derivative.

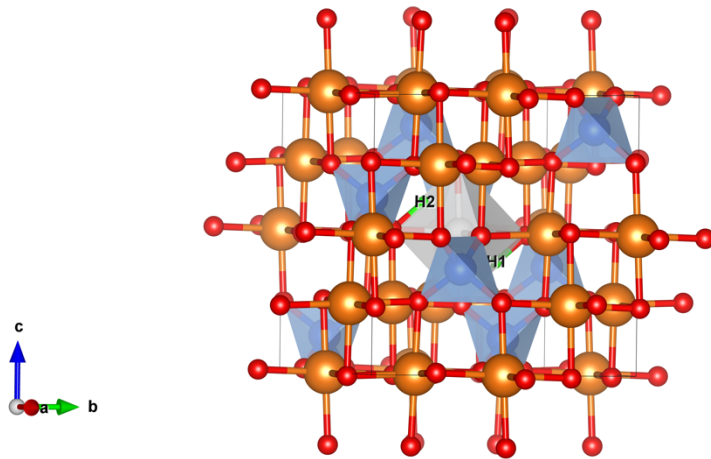
Temperature (K)	Pressure range (GPa)	V_0 (Å ³)	K_{T0} (GPa)	K'_{T0}
300	0-30	527.408	169.0	4.64
1000	0-30	538.459	148.0	4.91
1500	2-30	548.745	131.0	5.17
2000	3-40	561.258	112.6	5.50
2500	4-30	577.102	92.5	5.94

868

869 **Table S5.** Sound velocities of hydrous ringwoodite in Schulze et al. (2018) as a function
 870 of pressure and water content at 300 K. The polynomial fitting equation is: $V_{P/S} =$
 871 $p00 + p10 \cdot C_{H2O} + p01 \cdot P + p11 \cdot P \cdot C_{H2O} + p02 \cdot P^2$, where p00, p10, p01, p11,
 872 and p02 are polynomial fitting parameters (with 95% confidence bounds), C_{H2O} is
 873 water content, and P is pressure.

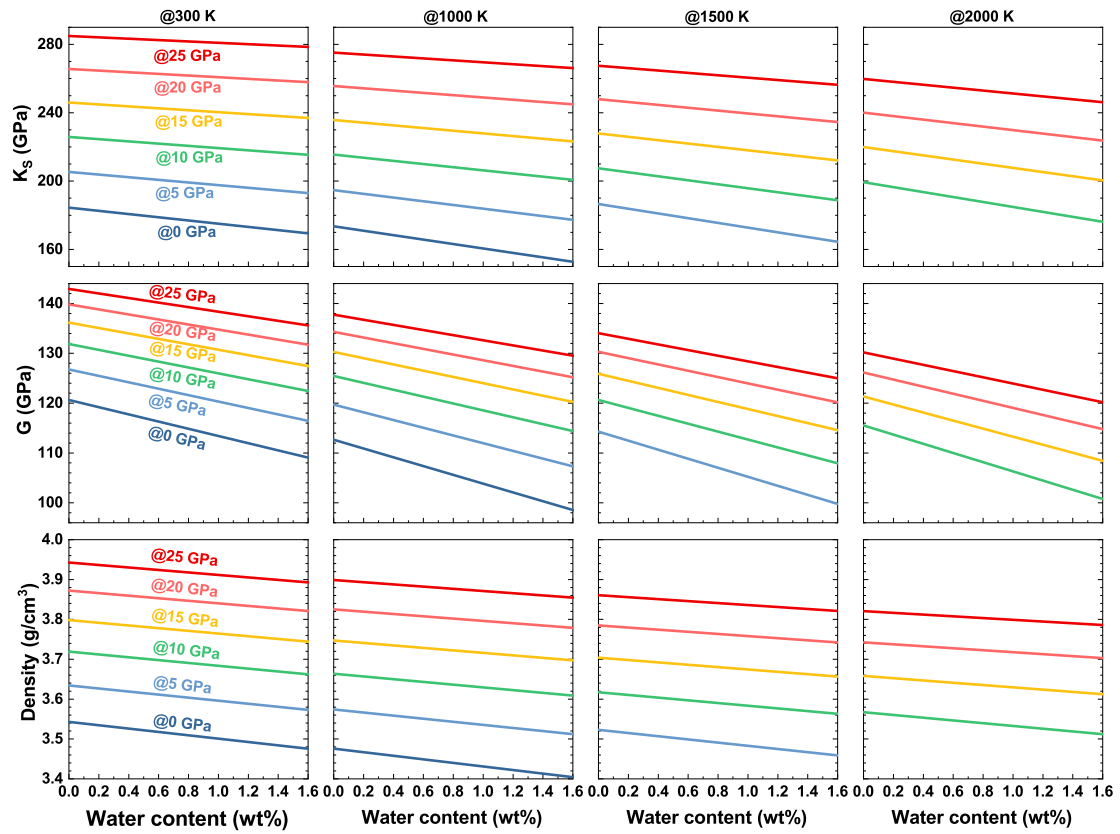
Parameters	V_P (km/s)	V_S (km/s)
p00	9.718±0.070	5.662±0.034
p10	-0.1955±0.0538	-0.1164±0.0256
p01	0.05807±0.00978	0.02081±0.00465
p11	0.006849±0.004019	0.002982±0.001909
p02 ($\times 10^{-3}$)	-0.6953±0.3837	-0.4406±0.1824

874



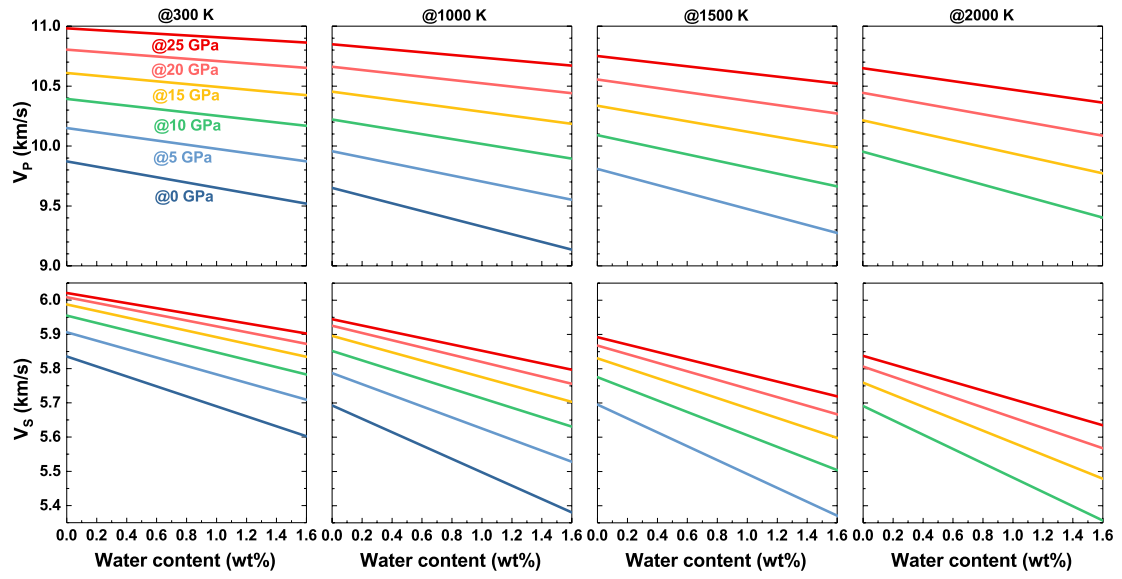
875

876 **Figure S1.** The relaxed structure of hydrous ringwoodite with 1.63 wt% water
877 ($\text{Mg}_{15}\text{Si}_8\text{O}_{30}(\text{OH})_2$). The initial configure was generated through the substitution
878 mechanism $V_{\text{Mg}}'' + 2\text{H}^{**}$, which is the main mechanism for the incorporation of
879 hydrogen into ringwoodite (Grüninger et al., 2017; Panero, 2010). The sites occupied
880 by H atoms are derived from the experimental results of pulsed neutron diffraction
881 (Purevjav et al., 2014).



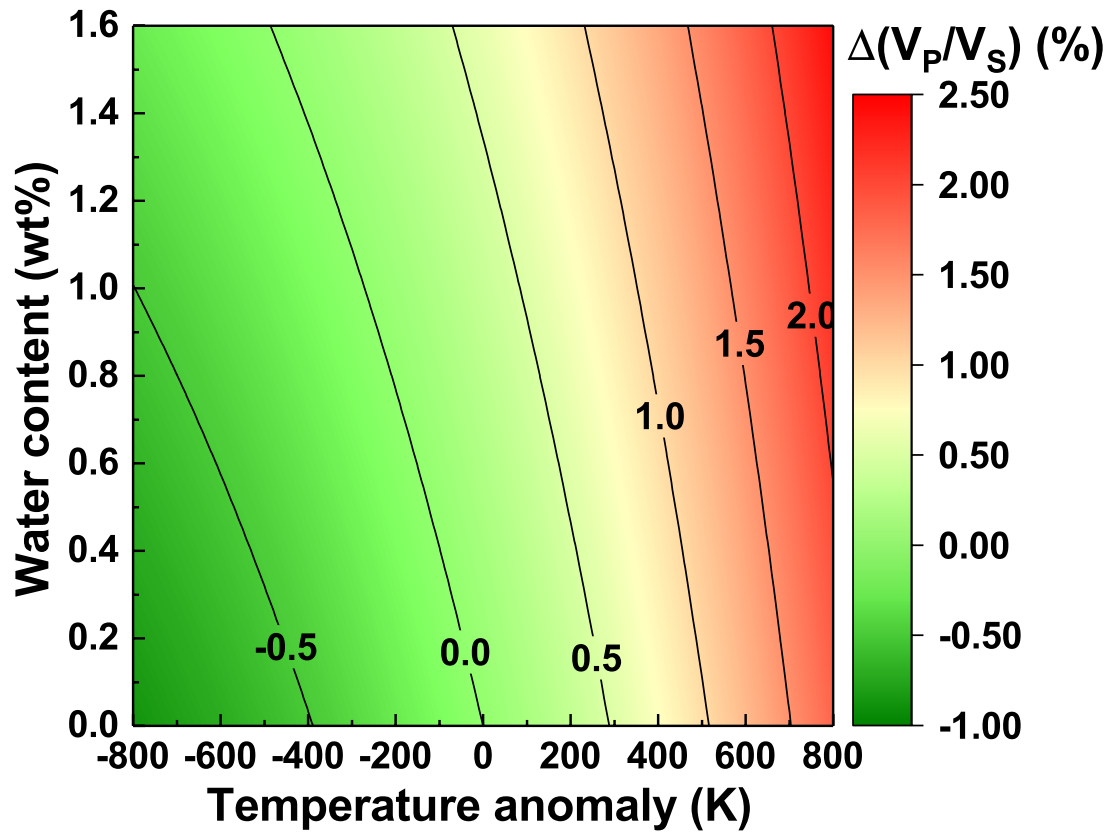
882

883 **Figure S2.** Elastic moduli (K_s and G) and density of ringwoodite as a function of water
 884 content at different pressures (0 GPa, 5 GPa, 10 GPa, 15 GPa, 20 GPa, and 25 GPa)
 885 and temperatures (300 K, 1000 K, 1500 K, and 2000 K). The elasticity of anhydrous
 886 ringwoodite is derived from Núñez Valdez et al. (2012).



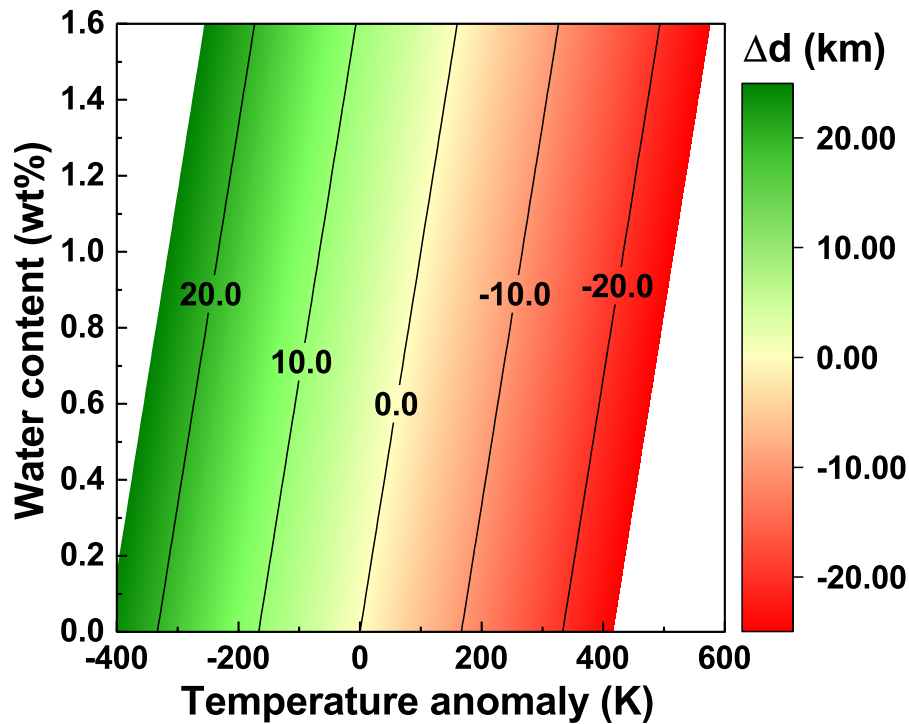
887

888 **Figure S3.** Compressional and shear wave velocities (V_P and V_S) of ringwoodite as a
 889 function of water content at different pressures (0 GPa, 5 GPa, 10 GPa, 15 GPa, 20 GPa,
 890 and 25 GPa) and temperatures (300 K, 1000 K, 1500 K, and 2000 K).



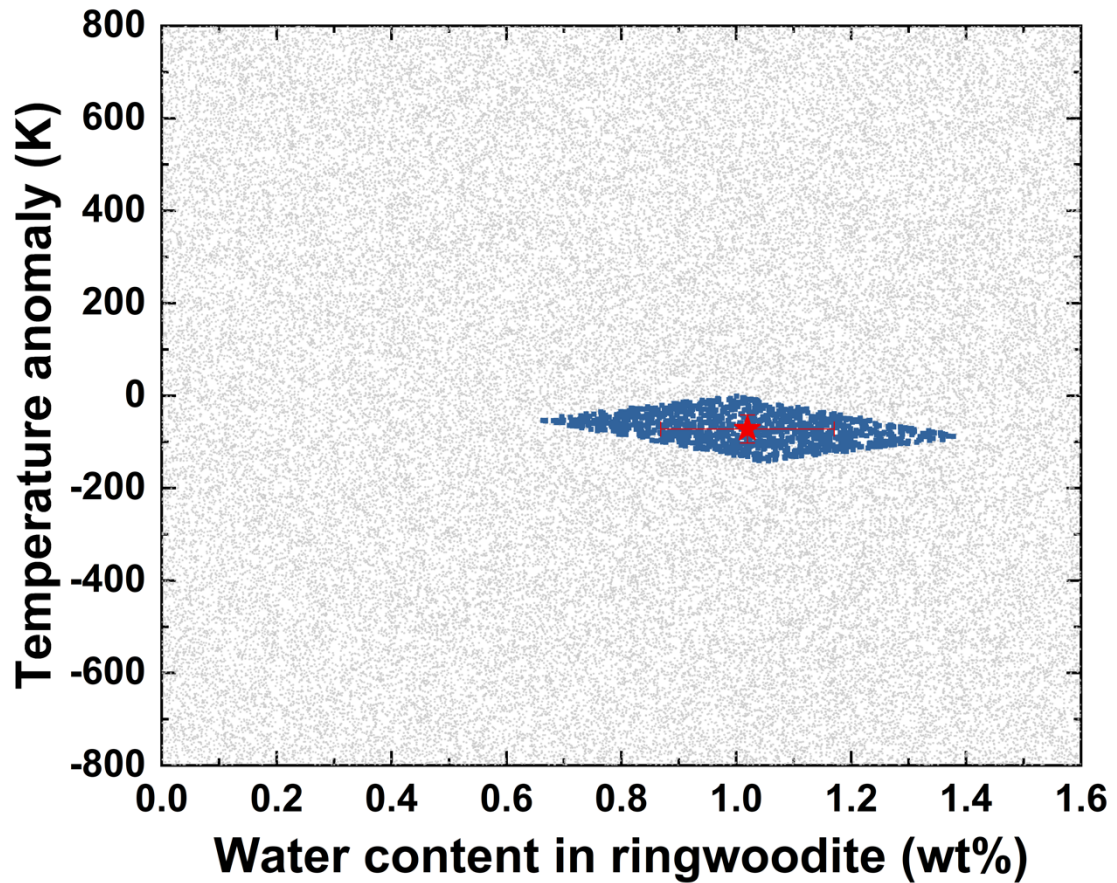
891

892 **Figure S4.** V_P/V_S anomalies ($\Delta(V_P/V_S)$) in pyrolite caused by ringwoodite hydration
 893 and temperature anomaly at 23.5 GPa. Under the conditions of the MTZ, pyrolite
 894 consists of $\sim 57\%$ ringwoodite, 35% majorite, and 8% calcium perovskite (Irifune et
 895 al., 2010). The V_P/V_S of anhydrous pyrolite is taken as the reference to calculate
 896 $\Delta(V_P/V_S)$. The temperature anomaly is with respect to the normal mantle temperature
 897 from Brown and Shankland (1981).



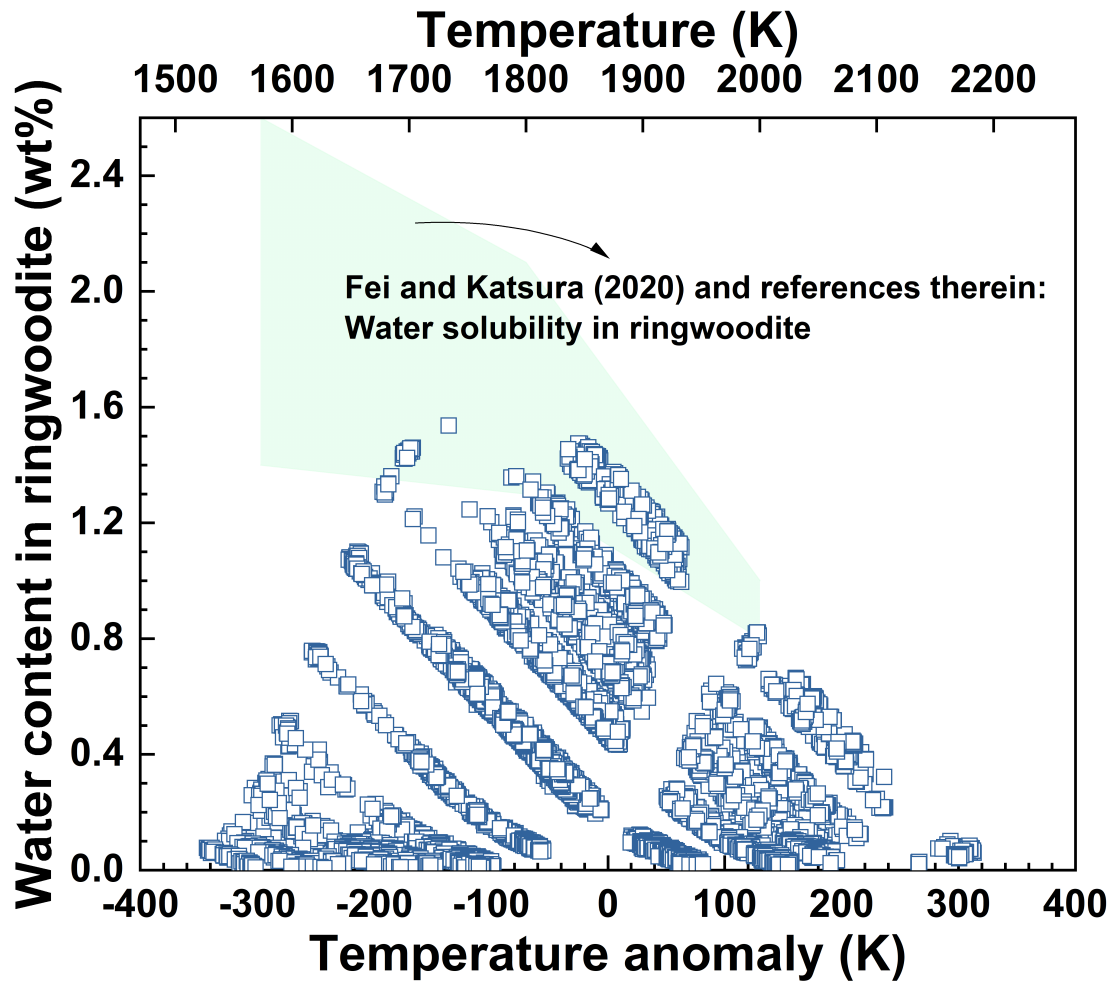
898

899 **Figure S5.** Depth variations in the 660-km discontinuity as a function of ringwoodite
 900 hydration and temperature anomaly. The effect of temperature on the depth of the 660-
 901 km discontinuity (-0.06 km/K) is derived from the Clapeyron slope of the post-spinel
 902 phase transition (Bina and Helffrich, 1994; Fei et al., 2004; Higo et al., 2001; Irifune,
 903 1998; Yu et al., 2007). The effect of ringwoodite hydration on the depth of the 660-km
 904 discontinuity is adopted as 6 km/wt% (Higo et al., 2001).



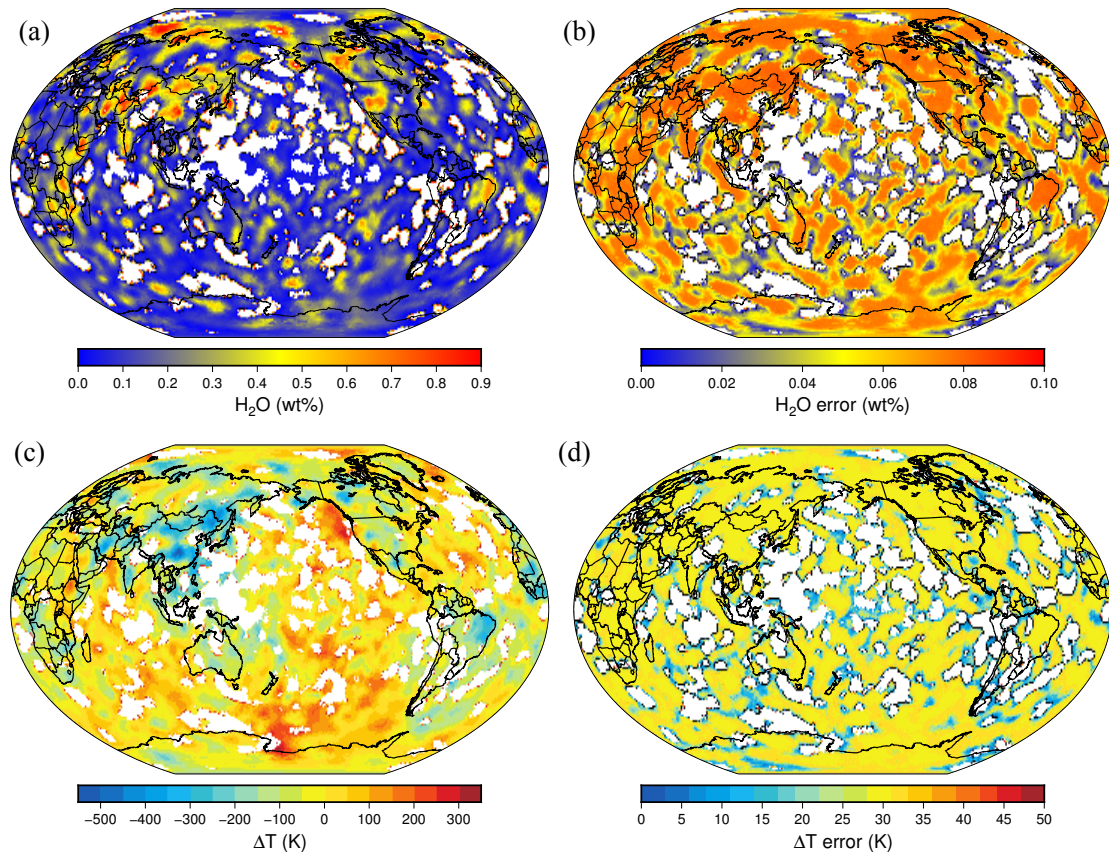
905

906 **Figure S6.** An example of Monte Carlo simulations to find out the solutions for water
 907 content in ringwoodite and temperature anomaly. The observed ΔV_s and Δd values are
 908 -1.0% and 9 km, respectively. 70000 initial inputs (grey points) were randomly
 909 produced in the ranges of 0-1.6 wt% for water content in ringwoodite and -800-+800 K
 910 for temperature anomaly. Blue points are the results that can match the observed ΔV_s
 911 within 0.3% and Δd within 3 km, and the red star refers to the average value.



912

913 **Figure S7.** The water content in ringwoodite and temperature anomaly inferred from
 914 the depth variation of 660-km discontinuity and the shear velocity anomaly compared
 915 with the water solubility in ringwoodite (blue areas) from experimental measurements
 916 Fei and Katsura (2020).



917

918 **Figure S8.** Water concentration (H_2O wt%) and temperature anomaly (ΔT (K)) in the
 919 lower MTZ inferred from the topography of 660-km discontinuity in Guo and Zhou
 920 (2020) and the shear velocity anomaly from the S40RTS model (Ritsema et al., 2011).
 921 (a) the map of water concentration and (b) the standard error of H_2O amount; (c) the
 922 map of temperature anomaly and (d) the standard error of ΔT . About 84% of the bins
 923 with ΔV_s and Δd can be explained by our models. The white areas are the remaining
 924 bins that are not consistent with the current mineral models. The average water
 925 concentration is 0.18 ± 0.05 wt% and the average temperature anomaly is -23 ± 26 K.