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Modeling and on-line measurement of the surface potential of electrospun membranes for the control of the fiber diameter and the pore size

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Abstract

Electrospinning is a widespread technology enabling the fabrication of nanofibrous materials for a wide range of applications, some of them on an industrial scale. It is shown that the online measurement of the surface potential V located over the nanofibrous membrane gives useful information on the ongoing process and on the local fibrous morphology. A model is proposed to describe the kinetics of the evolution of V during electrospinning and its decay once the production is stopped. In the case of poly(lactic acid) nanofibers, whatever the tested processing conditions, the surface potential is shown to rely on the fiber diameter and the inter-fibers pore size. A scaling law is proposed $\phi_f \propto \left[\frac{\tau}{dV/dt}\right]^{0,21}$ showing that the fiber diameter ϕ_f is a function of the time τ , characteristic of the initial behavior of the surface potential, and the slope dV/dt measured at the steady state. In combination with the current measurement, it is an efficient and robust method for the online monitoring of the process of electrospinning. Furthermore, the method gives information on the residual charges stored in the fibrous material which is an important feature for the elaboration, by electrospinning in-situ charging, of electrets for filtering applications.

1. Introduction

Electrospinning is a widespread technology enabling the fabrication of nanofibrous materials with most of the polymers available on the market and for a wide range of applications such as filtration [1], tissue engineering [2], and biomedical applications [3–5]. The principle of the process consists in subjecting a polymer solution droplet to a high electric field in the order of 1 kV/cm which induces the emission of a liquid jet toward a grounded counter-electrode, the socalled collector, located about 10-20 cm away from the jet emission. During its flight in the air, the electrified and charged jet is experiencing whipping movements allowing an efficient stretching and the solvent evaporation. A continuous fiber having a diameter in the range of 100-1000 nm is pseudo-randomly deposited in the form of a non-woven membrane. By playing with the material properties (polymer molar mass, concentration, nature of the solvents...) as well as the processing parameters (applied voltage, solution flow rate, jet emission-to-collector distance, collector geometry, air temperature and humidity...), membranes with various morphological and physical properties (fiber diameter, membrane pore size, polymer crystallinity, mechanical properties...) can be elaborated [6-8]. Because electrospinning is currently emerging in the industry, it is thus of prime importance to provide a robust online process monitoring.

Several articles deal with the effect of solution and processing parameters on the current reflecting the amount of charges carried by the electrospun jet [9–11]. Current measurement is easy to implement. Indeed, by installing a resistor between the collector and the ground, the measurement of the difference of potential through the resistor allows calculating the electrospinning current thanks to the Ohm's law. Nevertheless, the current is mainly related to the processing conditions, such as the imposed electric field and solution flow rate and its conductivity. It doesn't give any information neither on the amount of charges remaining in the membrane during and after electrospinning nor on the internal structure of the fibrous membrane. The online measurement of the surface potential resulting from the residual charges accumulating in the membrane during its fabrication may be an efficient way to get complementary information on the membrane during its fabrication. Such online control could help (i) to fine tune the processing conditions which can fluctuate during the time of production and (ii) to have an immediate action on the process when these fluctuations occur. Researchers highlighted that residual charges remaining on the deposited fiber may represent an important amount of the total charges carried by the fiber just before its landing on the collector[12]. In electrospinning, charges are present due to dipole orientation, space charge separation and direct injection of charges into the fibers [13–16]. Understanding, how charges accumulate on the membrane during its fabrication and how charges dissipate through its thickness is also necessary for applications dealing with electret filters for air cleaning [1]. Indeed, in addition to the well-known specific properties of nanofibrous membranes (i.e. small diameter, high specific surface area and tortuous porous structures) adapted for filtration applications, electrostatic forces may also play an important role on the air filtration performance thanks to the presence of charged fibers enhancing the efficiency to adsorb or repel the dust [1,12,16-19]. For biomedical applications, such electrets may also be interesting as they improve cell spreading and proliferation [20]. Moreover, it was reported that charge transfer and accumulation through

the membrane, as well as charge dissipation, occurring in the process of electrospinning may impact the morphology of fibers and the inner structure of the membrane [21–26]. Indeed, it was shown that residual charges carried by the fibers may form an electrostatic template [2] driving the deposition of the incoming electrospun jet allowing the fabrication of membranes with various morphologies through self-assembling processes [27,28] or with the help of patterned collectors [29,30].

In this article, the evolution of the surface potential during in-situ charging by electrospinning and after stopping electrospinning is studied as a function of various processing parameters (applied voltage on the emitter, polymer concentration in the solution and ambient relative humidity). An original model of the in-situ charging is proposed and shows the correlation between the characteristic features of the surface potential variation with the porous morphology of the fabricated membrane. The study of the surface potential decay measured after stopping electrospinning is also discussed with the help of a double exponential model. Finally, the experimental results, supported by the model, demonstrate that the online measurement of the surface potential could be an efficient way to monitor the process of electrospinning regarding the final morphology of the nanofibrous membrane and its building during processing.

2. Materials and methods

2.1 Materials and solution preparation

PLA (Mw=180kDa, Natureworks) was used as received, Dichloromethane (DCM), N, N-Dimethylformamide (DMF), benzyltriethylammonium chloride (TEBAC salt) were purchased from Sigma-Aldrich. PLA/DCM/DMF solution was prepared by dissolving PLA in DMF/DCM (50:50 v/v) with stirring 24h prior to electrospinning. The PLA electrospinning parameters are shown in Table 1.

The addition of TEBAC salt (0.5% w/w) in PLA solution was studied for monitoring purposes. PLA and TEBAC were added in DMF/DCM in a glass bottle with magnetical stirring overnight at room temperature. The conditions of electrospinning PLAsalt-S2 were identical to those of PLA-S2 (see Table 1).

	Concentration	Voltage	Relative	Average
	(w/w)	Voltage	humidity	fiber diameter (nm)
PLA-S1	7%	25kV	38%±2%	323 ± 169
PLA-S2	9%	25kV	$38\% \pm 2\%$	445 ± 97
PLA-S3	11%	25kV	$38\% \pm 2\%$	546 ± 127
PLA-S4	13%	25kV	$38\%{\pm}2\%$	659 ± 77
PLA-S5	9%	15kV	$38\% \pm 2\%$	572 ± 229
PLA-S6	9%	20kV	$38\%{\pm}2\%$	571 ± 154
PLA-S7	9%	30kV	$38\% \pm 2\%$	407 ± 67
PLA-S8	9%	25kV	$28\%{\pm}2\%$	271 ± 99
PLA-S9	9%	25kV	$48\%{\pm}2\%$	515 ± 81
PLA-S10	9%	25kV	58%±2%	730 ± 133
PLAsalt-S2	9%	25kV	38%±2%	182 ± 40

Table 1 Preparation parameters of PLA fibers and resulting fiber diameter

2.2 Electrospinning process

Fig. 1 presents the sketch of the experimental setup of electrospinning. The polymer solutions were fed by a syringe pump (Fischer scientific) at 1 mL/h with a stainless steel needle having an inner diameter of 0.5 mm. The needle was electrically connected to a DC power supply (Spellman SL10). The needle-to-collector distance was fixed at 15 cm. The cylindrical collector (diameter = 110 mm and width = 30 mm) was mounted around the rotor connected to the ground, an insulating Teflon ring was fixed between the collector and the rotor to avoid any

charge transfer directly from the collector to the rotor. The collector was electrically connected to a metallic ring at a distance of 20 cm from the collector to avoid any fibers deposition on this ring. The metallic ring was mechanically linked to the rotor by a thick insulating ring of Teflon. A resistor of 500 M Ω was installed between the ring and the rotor connected to the ground allowing the calculation of the electrospinning current from the measurement of the potential of the metallic ring, thanks to the Ohm's law. The velocity of rotation of the rotor was set at 120 rpm.

To measure the surface potential at the top surface of the membrane, a non-contacting electrostatic voltmeter ESVM₁ (Trek Model 347-3-H-CE) connected to a computer for data acquisition was used. The measurement is based on a field-nulling technique for non-contacting voltage measurement achieving direct current stability and high accuracy, with no need for fixed probe-to-surface spacing. The technique allows an accurate measurement of the surface potential of stationary or moving surfaces. The measurement range is 0 to \pm 3 kV with an accuracy of 0.1% of the full range. The probe (Probe 1) of the voltmeter (probe model 6000B-7C with a speed of response of 4.5 ms for 1 kV step) having a disc surface of 11.2 mm diameter was placed 2 mm below the surface of the collector as shown in Fig 1. An acquisition rate of 30 measurements/s was chosen.

To measure the potential at the bottom of the membrane connected to the metallic ring, a noncontacting electrostatic voltmeter ESVM₂ (Trek Model 323-H-CE) connected to a computer for data acquisition was used. The measurement range is 0 to \pm 100 V with an accuracy of 0.05% of the full range. The probe (Probe 2) of the voltmeter (probe model 6000B-16 with a speed of response of 300 ms for 100 V step) having a square surface of 9.5×9.5 mm² was placed 2 mm below the surface of the supplementary ring as shown in Fig 1. An acquisition rate of 30 measurements/s was chosen.

2.3 SEM measurements

The morphology of fibers and particles was studied by scanning electron microscopy (SEM) (Vega-3, Tescan). The samples were gold coated (sputter Quorum Q 150 RS, Quorum Technologies) for 2 min before SEM characterization. Fiber diameters are given in Table 1.

3. Results

Fig. 2a shows the potential at the bottom of the fibers mat and the surface potential V over the membrane recorded during t_{spin} = 300 s of electrospinning PLA in the case of PLA-S2 conditions (see Table 1) and after stopping electrospinning (for $t > t_{spin}$). The measurement of the potential of the collector (Probe 2, see Fig. 1 and 2a), i.e. the potential below the membrane, corresponds to the difference of potential through the resistor R and allows the calculation of the current *i*, induced by the flow of charges through the membrane, thanks to the Ohm's law. The current *i* is constant during the time of electrospinning demonstrating that the electrospun jet brings a constant amount of charges per unit time. However, the surface potential (Probe 1, see Fig. 1 and 2a) increases along the time of production due to residual charges accumulating in the membrane. During the first time of electrospinning, $t \le 15$ s, the surface potential is almost constant. Indeed, as observed in Fig. 2b in the case of fibers deposited after a short time $t_{spin} = 5 s$, the fibers are in good contact with the collector favoring an efficient charge dissipation which results in poor charge accumulation and thus only a slight increase of the surface potential. For a larger time $t_{spin} = 30 s$, Fig. 2c shows that the direct electric contact with the collector is lost between the incoming jet and the layer of fibers deposited in the very first time. The suspended fiber strands cannot release their charges anymore: the surface potential starts to increase significantly. Then, a steady state behavior is reached during which the surface potential increases significantly and linearly as a function of time. The slope dV/dt is thus constant during this period and the fibrous and porous morphology of the produced membrane is stable. When electrospinning is stopped at t_{spin} , the current is no longer brought by the electrospun jet leading immediately to the return at 0V of the collector's potential. During the same time, after having instantaneously decreased of a value of Ri, the surface potential over the membrane continues to decrease slowly due to the release of the charges stored during electrospinning. In order to get more insight into these experimental results, a model allowing the prediction of the evolution of the surface potential of the membrane during electrospinning is proposed.



Fig. 1. Sketch of the experimental setup allowing the measurement of the membrane surface potential (Probe 1) and the potential at the bottom of the membrane (Probe 2).



Fig. 2. Electrospinning in the case of PLA-S2 conditions. a) Evolution of the surface potential over the membrane (Probe 1) and on the collector (i.e. at the membrane-collector interface, Probe 2) during $t_{spin} = 300 \ s$ of electrospinning and after stopping electrospinning at t_{spin} . SEM pictures obtained after b) $t_{spin} = 5 \ s$, c) $t_{spin} = 30 \ s$ and $t_{spin} = 300 \ s$ under PLA-S2 conditions.

3.1 In-situ charging under different parameters during electrospinning

Evolution of the membrane surface potential during electrospinning: a model

Electrospinning can be seen as a process allowing the layer by layer building of a porous membrane. The electric behavior is depicted in Fig. 3. At time t, when the jet, having a linear charge density λ , enters in contact with the top surface of the membrane, it starts to release its charges towards the ground along the electrical circuit formed by the interconnected fibers. At the same time, the freshly deposited fiber starts to build the layer of pores located at the top

surface of the membrane. The elementary domain of this interconnected circuit is the pore which is a small volume of air surrounded by charged fiber segments. Consequently, one pore may be modeled by a parallel resistor-capacitor circuit (Fig. 3) having a characteristic time $\tau = R_p C_p$. The capacitance C_p may be linked with the pore size, the capacitor being made of a dielectric, the air, surrounded by the charged electrodes, the fiber strands. The resistance R_p of the elementary circuit may be linked with the intrinsic resistivity of the fiber, the quality of the fiber-fiber contact points and the number of contact points per unit volume of membrane. During the deposition process, the electrospun jet brings a constant amount of charges per unit time, thus the elementary current i_p flowing through the $R_p C_p$ circuit is constant during time t.



Fig. 3. Charge accumulation during electrospinning. The fibers form an interconnected electrical circuit and the pore can be modeled by a resistor-capacitor R_pC_p circuit.

If the $R_p C_p$ circuit is formed at time t', it is thus subjected to the following difference of potential $du_{(t)}$:

$$du_{(t)} = \left(1 - e^{-(t-t')/\tau}\right)i_p R_p \tag{1}$$

Assuming that the membrane has an electrical resistance R_m and a surface S_m , an average of $P = S_m/D_p^2$ pores of diameter D_p forms an elementary porous layer of membrane made of $P R_p C_p$ circuits in parallel (depicted in red in Fig. 3). The equivalent resistance of such elementary porous layer is thus $dR_m = R_p/P$ and the equivalent capacitance is $dC_m = PC_p$.

Consequently, the elementary layer of pores has the same difference of potential $du_{(t)}$ as a single pore as well as the same characteristic time $\tau = dR_m dC_m = R_p C_p$. Furthermore, the current flowing through the elementary layer of pores corresponds to the total electrospinning current i. Thus, a porous layer of thickness dy at position y and formed at time t', is subjected to the following difference of potential at time t:

$$du_{(t)} = \left(1 - e^{-(t-t')/\tau}\right) i dR_m$$
⁽²⁾

The surface potential at time t of the membrane having a thickness h(t) is the sum of the potential $du_{(t)}$ of all elementary layers plus the difference of potential through the resistor R used for the measurement of the current:

$$V(t) = Ri + \int_0^{h(t)} du_{(t)} = Ri + \int_0^t (1 - e^{-(t-t')/\tau}) i \frac{dR_m}{dt'} dt'$$
(3)

It is assumed that the rate of resistance $\dot{R}_m = \frac{dR_m}{dt'}$ and the characteristic time τ are constant. Thus, after integration of equation (3), the surface potential can be expressed as:

$$V(t) = Ri + \left[t - \tau \left(1 - e^{-t/\tau}\right)\right] i\dot{R}_m$$
(4)

Fig. 4 shows the trend of V as a function of t and how the parameters i, τ and \dot{R}_m can be graphically obtained. It is seen that:

$$V(t \ll \tau) \sim V(y=0) = V_0 = Ri \tag{5}$$

 V_0 corresponds to the potential at the collector-membrane interface (i.e. at the position y = 0) and can be easily measured in order to get the current *i*.

When $t \ll \tau$, the surface potential is almost constant. Indeed, the characteristic time is the time it takes to completely charge a layer of characteristic thickness h_{τ} . When $t \gg \tau$, all the layers located below the upper layer of fibers of characteristic thickness h_{τ} are completely charged and are equivalent to a resistive layer of interconnected fibers having a thickness of $h(t) - h_{\tau}$. Under this condition, the surface potential evolves linearly with time:

$$V(t \gg \tau) \sim Ri + [t - \tau]i\dot{R}_m \tag{6}$$



Fig. 4. Theoretical evolution of the membrane surface potential as a function of the time and the characteristic parameters V_0 , *i*, τ and \dot{R}_m of the curve.

Effect of applied voltage during electrospinning

Experimental curves of the surface potential as a function of time for various applied voltages are given in Fig. S1b of Supp. Data. Fig. 5a shows that the current, corresponding to the amount of charges brought by the jet per unit time, increases obviously with the applied voltage. The final slope of the surface potential, corresponding to $\frac{dV}{dt} = i\dot{R}_m$, is almost constant from 15 kV to 25 kV (Fig. 5b). An increase of $i\dot{R}_m$ is observed for the highest voltage, i.e. at 30 kV, meaning that for this condition the resistance of the membrane increases faster than in the other cases. It was observed by SEM that when the voltage increases continuously, a more intense electrostatic force acts on the jet resulting in thinner fibers and more efficient solvent evaporation (see Table 1 and Fig. S1a of Supp. data). Indeed, for the lowest applied voltage, fusion among fibers at their contact points is observed resulting in an overall lower membrane electrical resistance. From Fig. 5b, it is also shown that the characteristic time τ decreases gradually with the increase of the voltage, with a value changing from 79s to 21s when increasing the applied voltage at the emitter from 15kV to 30kV. Furthermore, it is shown that the fiber diameter decreases with the applied voltage (Fig. 5a and 5c) resulting thus to a

decrease of the average pore size of the fibrous mesh.[31] As shown in the previous section, the characteristic time relies on the average pore size having each a capacitance directly correlated with their size. Thus, a decrease in the fiber diameter results in the production of membranes with smaller pores and consequently a decrease of the capacitance C_p and the characteristic time τ .



Fig. 5. a) Evolution of the current (red triangles) and the fiber diameter (blue discus) as a function of the applied voltage. b) Characteristic time τ (red triangles) and slope $\frac{dv}{dt} = i\dot{R}_m$ (blue discus) as a function of the applied voltage. c) SEM pictures of PLA fibers prepared at different applied voltages (PLA-S5, S6, S2 and S7 conditions, scale bar = 10 µm).

Effect of Polymer concentration during electrospinning

As shown in Fig. 6a, the polymer concentration in the solution does not impact significantly the current, the values varying from 0.09 μ A to 0.13 μ A when changing the concentration from 7% to 13%. Actually, the current is the consequence of complex mechanisms. Indeed, regarding the polymer alone, at constant solution feeding rate (i.e. 1 mL/h), an increase of the polymer concentration results in the increase of the fiber flow rate increasing thus the rate of charges landing on the collector and consequently the current. Concurrently, increasing the concentration induces the enlargement of the solution viscosity decreasing thus the efficient production of fiber and consequently, the current. In our case, these two phenomena being in competition resulted in a current which is almost constant with the concentration. However, as shown in Fig. 6b and Fig. S2b of Supp. Data, τ increases gradually and significantly from 8 s to 200 s when the concentration increases from 7% to 13% whereas the slope $i\dot{R}_m$ is almost constant with, however, a small increase observed for the highest studied concentration. Once again, the characteristic time seems to be in good correlation with the size of the pores being proportional with the fiber diameter (Fig. 6c). Thus, as shown in Fig. 6a, increasing the polymer concentration induces the enlargement of the fiber diameter due to high solution viscosities and thus leads to remarkable increase of τ but with a low effect on the slope $\frac{dV}{dt} = i\dot{R}_m$. It is also worth noting that for the highest concentration C = 13%, a lag time of 37 s was used to fit adequately the experimental curve of the surface potential. The presence of this lag time could be explained because at high concentration solvent can remain in the fiber when it lands on the collector. This residual solvent could enhance the electrical contact between the first layer of fibers and the collector. Thus, this first fibrous layer could have a very low resistance inducing no rise of the surface potential during this lag time.



Fig. 6. a) Evolution of the current (red triangles) and the fiber diameter (blue discus) as a function of the polymer concentration. b) Characteristic time τ (red triangles) and slope $\frac{dV}{dt} = i\dot{R}_m$ (blue discus) as a function of the polymer concentration in the solution. c) SEM images of PLA fibers fabricated from polymer solutions at various concentrations (PLA-S1, S2, S3 and S4 conditions, scale bar = 10 µm).

Effect of Ambient relative humidity during electrospinning

No significant effect of the ambient relative humidity (RH) on the current was observed (Fig. 7a). The current being influenced by many parameters, it is complex to draw any conclusion. In contrary, the two main parameters, τ and $i\dot{R}_m$, describing the surface potential model evolve significantly with RH (see Fig. 7b and Fig. S3b of Supp. Data). First, a gradual increase of τ was observed. Once more, it can be noticed that τ increases with the pore size of the membrane. Indeed, as measured by SEM, the fiber diameter increases sharply with RH (Table 1, Fig. 7a and 7c) resulting in the formation of larger pores [31]. It was also observed an effect of RH on the slope $i\dot{R}_m$ of the curves representing the surface potential as a function of time. A significant decrease of $i\dot{R}_m$ is firstly observed when RH increases from 28% to 48%. Then, the slope $\frac{dV}{dt} = i\dot{R}_m$ is rising sharply when increasing RH from 48% to 58%. These results show that RH mainly affects the electrical resistance rate of the membrane \dot{R}_m instead of $i\dot{R}_m$, the current being indeed almost constant with RH. The membrane resistance R_m is linked with the resistivity of the polymer, here PLA, the quality of the fiber-fiber contact points and the number of contact points per unit volume of membrane. As shown in Fig. S3a of Supp. Data, all these features seem to change as a function of RH explaining thus the complex trend of $i\dot{R}_m$.



Fig. 7. a) Evolution of the current (red triangles) and the fiber diameter (blue discus) as a function of the relative humidity. b) Characteristic time τ (red triangles) and slope $\frac{dv}{dt} = i\dot{R}_m$ (blue discus) as a function of the relative humidity. c) SEM images of PLA fibers fabricated from various ambient relative humidity (PLA-S8, S2, S9 and S10 conditions, scale bar = 10

3.2 Decay of the surface potential of the membrane after stopping the fiber production – mechanism of residual charges dissipation

Surface potential decay: a model

In this section, the stored charges release mechanism is studied over after stopping electrospinning. When the power supply connected to the emitter is switched-off, the jet is no more produced, the current is thus equal to zero and no more charges are deposited. Since the current is null, no charges are released to the ground. However, a decrease of the surface potential over time is observed as shown in Fig. 8. Several mechanisms of charge release can explain the surface potential decay. First, charges located at the topmost surface of the membrane are subjected to ion neutralization with air. This charge release phenomenon may occur at short times, characterized by a time denoted τ_s . Second, charges mostly located at the surface of the fibers, but inside the porosity of the membrane, should release their charges within each pore having already participated to the kinetic of in-situ charging by electrospinning. It is thus expected that this second characteristic time of decay, denoted τ_m , is in the same order than the characteristic time τ measured during in-situ charging. This medium characteristic time τ_m is expected to be higher than τ_s . Third, in-situ electrospinning may lead the production of charges efficiently trapped in the bulk of the fibers. Indeed, although electrospinning of PLA leads to the fabrication of fibers with low crystallinity [29], charges may be trapped inside the fibers between amorphous and crystalline domains. This charge release phenomenon may occur at long times characterized by a time denoted τ_l . Thus, although a double exponential fitting was proposed in the literature for fibrous membranes charged by corona effect[32], it is expected that the surface potential decay may be modeled by the sum of three exponential functions as follows:

$$V(t) = A_s e^{-\left(\frac{t-t_{spin}}{\tau_s}\right)} + A_m e^{-\left(\frac{t-t_{spin}}{\tau_m}\right)} + A_l e^{-\left(\frac{t-t_{spin}}{\tau_l}\right)}$$
(7)



Fig. 8. Surface potential decay after stopping electrospinning carried out under the conditions of PLA-S2 (see Table 1). Experimental data (grey line), model with two characteristic times only (short dashed blue line), model with 2 characteristic times and one asymptote (dashed green line), model with three characteristic times only (dashed-point red line).

Fig. 8 shows the surface potential decay obtained after stopping electrospinning carried out under the conditions of PLA-S2 with a long time of acquisition of 2000 s. The model described by Eqn. 7 fits perfectly the experimental data. After fitting by a least square method, the obtained times were respectively $\tau_s = 11$ s, $\tau_m = 104$ s and $\tau_l = 2183$ s. A double exponential model was tested in order to compare the fitting quality:

$$V(t) = A_1 e^{-\left(\frac{t - t_{spin}}{\tau_1}\right)} + A_2 e^{-\left(\frac{t - t_{spin}}{\tau_2}\right)}$$
(8)

Using Eqn. 8, one characteristic time is obviously lost, leading to bad fitting as shown in Fig. 8. In this case, the obtained characteristic times were $\tau_1 = 51$ s and $\tau_2 = 1187$ s. Another model can be proposed, using also two characteristic times but introducing an asymptote V_{∞} instead of the long time as introduced in the model described by Eqn. 7. The model is the following:

$$V(t) = V_{\infty} + A_s e^{-\left(\frac{t-t_{spin}}{\tau_s}\right)} + A_m e^{-\left(\frac{t-t_{spin}}{\tau_m}\right)}$$
(9)

Eqn. 9 also allows a good fitting of the experimental data as V_{∞} can also be linked to the behavior at long times whereas τ_s and τ_m play the same role as in the model using three characteristic times. Using Eqn. 9, the least square method gave the corresponding characteristic times: $\tau_s = 17$ s and $\tau_m = 166$ s. Because in the next part, all measurements of the surface potential decay were carried out during a time of 150 s, the three exponential model didn't allow a good estimation of the long time τ_l . Thus, the model using two characteristic times with an asymptote V_{∞} (Eqn. 9) was chosen to fit the experimental data and only the behavior at short and medium times was studied. Furthermore, the following normalized weight factors were also studied as a function of the processing conditions:

$$A_{s}\% = \frac{100 A_{s}}{V_{\infty} + A_{s} + A_{m}} \tag{10}$$

$$A_m \% = \frac{100 A_m}{V_\infty + A_s + A_m}$$
(11)

$$V_{\infty}\% = \frac{100 V_{\infty}}{V_{\infty} + A_s + A_m} \tag{12}$$

Effect of Applied voltage on the surface potential decay after stopping electrospinning

Fig. 9 presents both τ_s and τ_m obtained from Eqn. 9 to fit the surface potential decay measured after applying various voltages on the emitter. The curves giving the surface potential decay as a function of time for various applied voltage are given in Fig. S4 of Supp. Data. It should be mentioned that the two exponentials are needed to fit adequately all experimental data. The normalized weight factors are not influenced by the applied voltage whereas the medium decay process is preponderant compared to the short one. The discharged of the top surface, characterized by the short time τ_s being in the order of 10 s, is a little bit faster for the membranes produced for the highest voltage. Indeed, the highest applied voltage led to the production of membranes with the thinnest fibers and consequently having the largest surface area offered to the ions of the air for a quick decay. It is also shown that the short time decay is around ten times faster than the medium one. A slow decrease of the medium time with applied voltage is observed. Moreover, τ_m is of the same order of magnitude than the characteristic time τ determined from the modeling of the surface potential during in-situ charging by electrospinning. These features seem to show that τ_m and τ rely on the same physical mechanisms originating from the effect of the pores of the membrane on the kinetic of the surface potential. However, the effect of applied voltage on τ_m is weaker than what was observed for τ during electrospinning. Although efficient charge injection is expected in the bulk of the fibers produced for the highest applied voltage, it is observed that V_{∞} %, characterizing the amount of bulk charges, is surprisingly constant with applied voltage. However, such result must be taken with caution because the measurements were carried out along short period, i.e.150 s, that don't allow a precise description of the kinetic at long times.



Fig. 9. a) Short τ_s (blue discus) and medium τ_m (red triangles) times and b) normalized weight factors (A_s : blue discus, A_m : red triangles, V_{∞} : green squares) as a function of applied voltage on the emitter.

Effect of Polymer concentration on the surface potential decay

Fig. 10 shows τ_s and τ_m in the case of membranes produced at various polymer concentrations. The curves giving the surface potential decay as a function of time for various polymer concentrations are shown in Fig. S5 of Supp. Data. The normalized weight factors are not significantly influenced by the polymer concentration. As observed for τ during in-situ charging, τ_m increases with the polymer concentration. However, the trend of τ_m is much less pronounced than for τ . No tendency can be draw for the short time decay.



Fig. 10. a) Short τ_s (blue discus) and medium τ_m (red triangles) times and b) normalized weight factors (A_s : blue discus, A_m : red triangles, V_∞ : green squares) as a function of polymer

concentration.

Effect of Ambient relative humidity on the surface potential decay

Fig. 11 shows τ_s and τ_m obtained to fit the surface potential decay measured for various ambient relative humidity (RH). The curves giving the surface potential decay as a function of time for various RH are shown in Fig. S6 of Supp. Data. Compared with the effect of the two previous parameters (applied voltage and polymer concentration) on the characteristic times, the effect of RH is more pronounced. This should be explained by the fact that RH is imposed not only during in-situ charging by electrospinning but also after stopping electrospinning. As observed for τ , τ_m increases with RH, τ_m being in the same order of magnitude than τ . Furthermore, it is worth noting that the fact that RH influences almost only the charges located on the surface of the fibers confirms that the mechanism leading to the surface potential decay at medium time τ_m is due to the release of surface charges and not to bulk charges inside the fibers. Finally, a significant increase of V_{∞} % is observed for the highest RH showing that a high amount of bulk charges, having the longest characteristic times, are stored in the matrix of the fibers. Indeed, because PLA is a hydrophobic polymer, diffusion of water into the electrospun jet results in the rapid precipitation of PLA [33]. Such rapid precipitation may lead to a high amount of defects in the polymer matrix explaining thus the high amount of charges which are usually trapped in the defects [16].



Fig. 11. a) Short τ_s (blue discus) and medium τ_m (red triangles) times and b) normalized weight factors (A_s : blue discus, A_m : red triangles, V_∞ : green squares) as a function of relative humidity

4. Discussion

Although the measurement of the surface potential decay allows to finally dissociating the kinetic in three fundamental mechanisms of charge release, it only gives an average behavior over the entire thickness of the membrane. In contrary, the measurement of the surface potential during in-situ charging by electrospinning is mainly sensitive to the kinetic of charge release at

medium times but with a much higher accuracy. Indeed, the medium time τ_m , obtained from the fitting of the surface potential decay measured after stopping electrospinning, is of the same order of magnitude than the time τ measured during electrospinning. Both τ_m and τ follow the same behavior as a function of the studied processing parameters: a decrease with increasing voltage and the opposite when increasing either the polymer concentration or the ambient relative humidity. However, the characteristic time τ revealed to be much more sensitive than τ_m . Such difference can be explained by the fact that the surface potential measured during electrospinning takes into account a continuously fresh deposited top surface which immediately starts to release its charges. Thus, τ may be more related to the combination of the release at short times (~ 10 s) of charges located on the top surface and the release at medium times (~ 100 s) of the charges located in the pores just below the top surface under construction. In fact, in the proposed model of in-situ charging by electrospinning (Eqn. 4), the τ value can be related to the electrical characteristics at the different length scales: (i) the pore, (ii) the elementary layer having the surface of the membrane and the thickness of one pore and (iii) the whole membrane under building. Each of them is related to the pore structure of the membrane:

$$\tau = dR_m dC_m = R_p C_p = R_m C_m \tag{13}$$

Assuming that the membrane electrical resistance R_m evolves linearly with time:

$$R_m = \dot{R}_m t \tag{14}$$

And using equations 13 and 14, it is possible to give an estimation of the membrane capacitance C_m :

$$C_m = \frac{\tau}{\dot{R}_m t} \tag{15}$$

Because the number of elementary layers in the thickness of the membrane is proportional to the time of deposition and that the current is constant during time, dR_m and dC_m scale as:

$$dR_m \propto \dot{R}_m \propto dV/dt \tag{16}$$

$$dC_m \propto \frac{\tau}{\dot{R}_m} \propto \frac{\tau}{dV/dt} \tag{17}$$

Thus, knowing that the average number of pores *P* for one elementary layer of membrane of surface S_m is $P = S_m/D_p^2$ and that the characteristic size of a pore D_p is proportional to the fiber diameter $D_p \sim \phi_f$,[31] the resistance and the capacitance of a pore scale respectively as:

$$R_p \propto \frac{dV/dt}{\phi_f^2} \tag{18}$$

$$C_p \propto \frac{\phi_f^2 \tau}{dV/dt} \tag{19}$$



Fig. 12. a) Correlation between C_p and the fiber diameter ϕ_f . b) Correlation between the fiber diameter ϕ_f and $\tau/(dV/dt)$. Green triangles correspond to the experimental points obtained

from polymer concentrations C = 7 %, 9 %, 11 % and 13 %, blue squares from relative humidity RH = 28 %, 38 %, 48 % and 58 % and red discus from applied voltages = 15 kV, 20 kV, 25 kV and 30 kV.

In order to verify the proposed scaling law, all data points obtained in the various operating conditions (applied voltage, polymer concentration and ambient relative humidity) were represented in graphs. The first one, gives $\frac{\phi_f^2 \tau}{dV/dt}$ as a function of the measured fiber diameter ϕ_f (Fig. 12a). Because of Eqn. 19, this graph is proportional to the graph of the pore capacitance C_p versus ϕ_f . It is shown that whatever the processing condition (highlighted by the different

symbols in the graph), C_p is well correlated with the fiber diameter (Fig. 12a). The following scaling law can thus be obtained for electrospinning of PLA on a flat collector:

$$C_p \propto \phi_f^{4.87} \tag{20}$$

Consequently, the fiber diameter can also be plotted as a function of $\frac{\tau}{dv/dt}$ and a good correlation is obtained (Fig. 12b) giving thus ϕ_f as a function of only the physical quantities obtained from the measurement of the surface potential:

$$\phi_f \propto \left[\frac{\tau}{dV/dt}\right]^{0.21}$$
 (21)

It is thus shown for the first time that the measurement of the surface potential, thanks to the use of an electrostatic voltmeter, is a simple method giving accurate information at the local scale of the nanofiber diameter of an electrospun membrane. Moreover, such a method should allow the detection of variations in the porous morphology and/or membrane's quality during its fabrication. In order to illustrate such feature, 0.5wt% of TEBAC salt was added in the PLA solution and electrospun under the conditions PLAsalt-S2 (see Table 1) which are equivalent to the PLA-S2 standard conditions without salt. The addition of the salt brings a high amount of charges in the electrospun jet which explains the significant increase of the current (0.74 µA for PLAsalt-S2 calculated from V at t = 0 s compared to 0.1 µA for PLA-S2). Moreover, as opposed to the pure PLA system (see Fig. 2a), the addition of TEBAC perturbs significantly the evolution of the surface potential V. Indeed, Fig. 13a shows that the surface potential does not increase linearly with time as it was observed in the case of PLA-S2 as well as for all other studied pure PLA systems. The accumulation rate of charges in the membrane, characterized by the slope dV/dt, is thus not constant during electrospinning. Fig. 13b shows indeed that the salt is not homogeneously distributed which could explain that the charges are not regularly brought by the jet explaining the observed instabilities. The on-line measurement of the surface

potential seems to be an efficient way for the monitoring of the electrospinning stability and quality of the produced membrane.



Fig. 13. Effect of the addition of a salt in the solution on the stability of the surface potential obtained during electrospinning with conditions PLAsalt-S2 (see Table 1). a) Evolution of the surface potential. b) SEM picture of PLA fibers with TEBAC salt. The two rings highlight fiber domains having no salt particles on their surface.

5. Conclusion

Here, we showed that the measurement of the surface potential of the membrane can be easily carried out online during the process of electrospinning using an electrostatic voltmeter. A model was proposed to follow the kinetics of the surface potential during in-situ charging by electrospinning for various operating conditions. The model is characterized by a characteristic time τ , linked to the formation of an elementary porous layer of the membrane and by the slope dV/dt, measured at steady state, and related to the electrical resistance of the membrane induced by the fiber resistivity and the quality and the density of fiber-fiber contact points. The kinetic of the surface potential decay after stopping electrospinning was also studied. Three characteristic times can be identified during scaffold discharge. A short time τ_s , having a value in the range of ten seconds, can be correlated to the rapid charge release occurring on the topmost surface of the membrane. A medium time τ_m , having a value of several tens of seconds up to more than one hundred of seconds, relies on the charge release inside each pore of the membrane. The times τ_m and τ , having the same physical origin, they are in the same order of magnitude. However, τ obtained from in-situ charging during electrospinning, is more sensitive to the processing conditions. Finally, the long time τ_l , being at least one order of magnitude higher than the medium time, characterizes the release of the charges trapped in the bulk of the fibers.

The measurement of the surface potential allows thus the detection of variations in the porous morphology of the membrane during its fabrication. Furthermore, in combination with the measurement of the current, it is an efficient and complementary method to get more insight into the overall process of electrospinning for a robust online monitoring. Last but not least, the method also gives immediate information on the residual charges stored in the fibrous membrane which is an important feature for the elaboration, by electrospinning in-situ charging, of electrets for filtering applications.

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