

## **Faculty of Mechanical Engineering**

# INVESTIGATION OF IMPACT STRAIN SIGNAL CHARACTERISTICS FOR MATERIAL BEHAVIOUR PREDICTION FROM CHARPY TEST

Nurlaela binti Muhammad Said

Master of Science in Mechanical Engineering

### INVESTIGATION OF IMPACT STRAIN SIGNAL CHARACTERISTICS FOR MATERIAL BEHAVIOUR PREDICTION FROM CHARPY TEST

#### NURLAELA BINTI MUHAMMAD SAID

### A thesis submitted in fulfilment of the requirements for the degree of Master of Science in Mechanical Engineering

### **Faculty of Mechanical Engineering**

#### UNIVERSITI TEKNIKAL MALAYSIA MELAKA

#### DECLARATION

I declare that this thesis entitled "Investigation of Impact Strain Signal Characteristics for Material Behaviour Prediction from Charpy Test" is the result of my own research except as cited in the references. The thesis has not been accepted for any degree and is not concurrently submitted in candidature of any other degree.

Signature	:	Ball
Name	:	Nurlaela binti Muhammad Said
Date	:	18.11.2019

#### APPROVAL

I hereby declare that I have read this thesis and in my opinion this thesis is sufficient in terms of scope and quality for the award of Master of Science in Mechanical Engineering.

:

:

:

Signature

Supervisor Name

Date

\_\_\_\_

Dr. Mohd Basri bin Ali

### DEDICATION

To my lovely husband, Mohammad Afnan Emy bin Mazlan and my beloved parents, Muhammad Said bin Menjong and Bungatia binti Barohe

#### ABSTRACT

This thesis investigates impact strain signal analysis during Charpy impact test. Impact strain signals were used to examine strain signal patterns under various parameters. It is includes the correlation between energy absorbed with power spectrum density (PSD) and area under strain-time graph at different material, impact speed and thickness of material. Thickness effect on impact duration is presents as well. Besides that, stress-strain curve is relates with the impact strain signal. Recently, the number of accident on highway has been increased due to loss of structure integrity to withstand high impact load. Therefore, materials that have ability to provide adequate protection to passengers from harmful and improve occupants' survivability during crash event are needed. Tough material with high energy absorption capability is required to reduce damage on structure when high impact energy is applied. Impact test is often performed to determine toughness of material by determine the amount of energy absorbs. However, most of energy absorbed is not accurate and only calculated as an estimation value. This scenario brings an idea to correlate the energy absorbed with strain energy by installing strain gauge to striker hammer that connected to data acquisition system (SOMAT eDAQ). Besides that, mechanical testing of tensile test is carried out to obtain the material behaviour and to identify the material properties that being used in calculation of impact duration. Results indicate a great correlation is observed between energy absorbed with strain energy. Strain energy is directly proportional to the energy absorbed. In term of material's type, Aluminium 6061-T6 shows a good energy absorber compared to the Magnesium AM60 because aluminium is more ductile than magnesium. Impact duration of experiment, theory and previous study shows a same pattern where it was increased if material's thickness is increased but decreased when applied speed is increased. Relation of strain signal from Charpy test and stress-strain curve from tensile test shows a great finding where the material deforms and fracture points is identified through the strain pattern and stress-strain curve. Aluminium 6061-T6 has the highest of energy absorbed, maximum strain and strain energy under PSD graph compared to Magnesium AM60. This concludes that characteristics of strain signal from Charpy test needs to be classified as an alternative method to predict properties of a material.

#### ABSTRAK

Tesis ini mengkaji analisis isyarat terikan impak ketika ujikaji Charpy. Isyarat terikan impak digunakan untuk mengenalpasti corak isyarat terikan dengan pelbagai parameter. Ia termasuklah korelasi di antara tenaga serapan dengan kuasa kepadatan spektrum (PSD) dan kawasan di bawah graf terikan-masa pada jenis bahan, kelajuan impak dan ketebalan bahan yang berbeza. Kesan ketebalan bahan kepada tempoh impak juga dibentangkan. Selain itu, lekuk tegasan-terikan dihubungkaitkan dengan isyarat terikan. Pada masa kini, bilangan kemalangan di lebuh raya telah meningkat disebabkan kehilangan struktur integriti untuk menahan beban impak yang tinggi sangat diperlukan. Oleh itu, bahan yang mempunyai keupayaan untuk memberikan perlindungan yang mencukupi kepada penumpang daripada keadaan membahayakan dan meningkatkan daya hidup penumpang semasa berlakunya kemalangan. Bahan yang kuat dan mempunyai keupayaan penyerapan tenaga yang tinggi sangat diperlukan untuk mengurangkan kerosakan pada struktur apabila dikenakan tenaga impak yang tinggi. Ujian impak kerap kali dilakukan untuk menentukan kekuatan bahan dengan menentukan jumlah penyerapan tenaga. Walau bagaimanapun, kebanyakan tenaga yang diserap tidak tepat dan hanya dikira sebagai nilai anggaran. Senario ini telah memberi idea untuk menghubungkaitkan tenaga yang diserap dengan tenaga terikan dengan memasang tolok terikan pada tukul mesin Charpy yang disambungkan dengan sistem pemerolehan data (SOMAT eDAQ). Selain itu, ujian mekanikal iaitu ujian tegangan dijalankan untuk untuk mengenal pasti tingkah laku mekanikal dan sifat-sifat bahan yang digunakan dalam pengiraan tempoh impak. Keputusan menunjukkan korelasi yang baik dapat diperhatikan di antara tenaga serapan dengan tenaga terikan. Tenaga terikan berkadar terus dengan tenaga serapan. Jenis bahan menunjukkan Aluminium 6061-T6 adalah penyerap tenaga yang baik berbanding dengan Magnesium AM60 kerana aluminium lebih mulur daripada magnesium. Oleh itu, aluminium mempunyai kawasan elastik dan plastik yang banyak sebelum patah. Keputusan tempoh impak daripada eksperimen, teori dan kajian terdahulu menunjukkam corak yang sama di mana ia meningkat apabila ketebalan bahan meningkat manakala menurun apabila halaju yang dikenakan meningkat. Hubungkait di antara isyarat terikan daripada ujian Charpy dan lekuk tegasan-terikan daripada ujian tegangan menunjukkan keputusan yang baik apabila titik bentuk dan titik patah bahan dapat dikenalpasti melalui isyarat terikan dan lekuk tegasan-terikan. Aluminium 6061-T6 mempunyai tenaga serapan, terikan maksimum dan tenaga terikan di bawah graf PSD yang tertinggi berbanding Magnesium AM60. Disimpulkan bahawa ciri-ciri isyarat terikan daripada ujian Charpy perlu diklasifikasi sebagai kaedah alternatif untuk meramal sifatsifat bahan.

#### ACKNOWLEDGEMENTS

Firstly, I would like to express my deepest appreciation to all those who encouraged and supported me to complete this thesis report. First and foremost, a special gratitude I give to my main supervisor, Dr. Mohd Basri bin Ali for his contribution in suggestions, guideline, supervision and encouragement to coordinate my research study especially in writing this report. Futhermore, I would also like to acknowledge with much appreciation to Dr. Kamarul Ariffin bin Zakaria as my co-supervisor for sharing his knowledge and constant advises to inspire me throughout this study.

Particularly, I would also like to express my gratitude to all the laboratory technician, Encik Wan Saharizal bin Wan Harun for his helpful and guideline to completed my experimental testing.

I gratefully acknowledge to my financial funding from the Ministry of Higher Education (MOHE) for sponsoring this research work under FRGS/2/2013/TK01/FKM/03/3/F00173 research grant and scholarship from MyBrain15 through the duration of my study.

Last but not least, many thanks go to my lovely husband and parents who have provided me through moral and emotional support in completing this study. I am also grateful to my other family members and friends, Rosmia binti Mohd Amman, Siti Nur Rabiatutadawiah binti Ramli, Zailinda binti Abdullah, Fadrah Hanim binti Ad Suhadak and Noor Dina binti Ghazali who have supported me along the way. Thanks for all your encouragement.

Ł

### TABLE OF CONTENTS

#### DECLARATION APPROVAL **DEDICATION** i ABSTRACT ii ABSTRAK iii ACKNOWLEDGEMENTS iv **TABLE OF CONTENTS** LIST OF TABLES vi viii LIST OF FIGURES LIST OF APPENDICES XV LIST OF ABBREVIATIONS xvi LIST OF SYMBOLS xviii LIST OF PUBLICATIONS xxi

PTE	R	
INT	RODUCTION	1
1.1	Introduction	1
1.2	Background of study	1
1.3	Problem statement	4
1.4	Objectives	5
1.5	Scopes	6
1.6	Thesis outline	6
LIT	ERATURE REVIEW	8
2.1	Introduction	8
2.2	Impact	8
	2.1.1 Charpy impact test	11
	2.1.2 Impact duration	12
2.2	Energy absorption of structures	18
	2.2.1 Effect of notch and geometry of material	23
	2.2.2 Effect of yield strength and ductility of material	29
	2.2.3 Effect of strain rate and temperature	30
	2.2.4 Effect of fracture mechanism	38
	2.2.5 Effect of impact condition	41
2.3	Strain	43
	2.3.1 Strain signal	46
	2.3.2 Strain energy	54
2.4	Signal processing approach	57
2.5	Summary	61
MF	THODOLOGY	62
3 1	Introduction	62
3.1	Flow chart	62
3.2	Material selection and preparation	64
	PTE INT 1.1 1.2 1.3 1.4 1.5 1.6 LIT 2.1 2.2 2.2 2.2 2.3 2.4 2.5 2.4 2.5 MEC 3.1 3.2 3.3	PTER         INTRODUCTION         1.1       Introduction         1.2       Background of study         1.3       Problem statement         1.4       Objectives         1.5       Scopes         1.6       Thesis outline         LITERATURE REVIEW         2.1       Introduction         2.2       Impact         2.1.1       Charpy impact test         2.1.2       Impact duration         2.2       Energy absorption of structures         2.1.1       Effect of notch and geometry of material         2.2.2       Effect of strain rate and temperature         2.2.3       Effect of strain rate and temperature         2.4       Effect of fracture mechanism         2.5.2       Effect of impact condition         2.3       Strain         2.3.1       Strain signal         2.3.2       Strain nergy         2.4       Signal processing approach         2.5       Summary         METHODOLOGY         3.1       Introduction         3.2       Flow chart         3.3       Material selection and preparation

3.3 Material selection and preparation3.4 Charpy impact test

PAGE

	3.4.1 Strain gauge installation	71
2.5	3.4.2 Set up on Somat eDAQ Experimental work on tensile test	74 80
3.5	Data analysis	81
5.0	3.6.1 Energy absorbed and strain signal analysis	82
	3.6.2 Method of energy correlation and comparison	86
	3.6.3 Analysis of thickness effect on impact duration	86
	3.6.4 Analysis on relation of strain signal pattern and stress-strain curve	88
3.7	Method of impact strain signal characteristics and classification	88
3.8	Summary	89
RES	SULT AND DISCUSSION	90
4.1	Introduction	90
4.2	Charpy test analysis	90
	4.2.1 Energy absorption behaviour	91
	4.2.2 Impact strain signal behaviour	95
	4.2.2.1 Maximum strain behaviour	100
	4.2.2.2 Impact duration analysis	102
	4.2.2.3 Area under strain-time ( $\varepsilon$ -t) graph	105
	4.2.2.4 Area under Power Spectrum Density (PSD) graph	106
4.3	Correlation of energy absorbed with Power Spectrum Density (PSD)	109
4.4	Correlation of energy absorbed with area under strain-time graph	111
4.5	The effect of material thickness on impact duration	112
4.6	Tensile test analysis	114
	4.6.1 Material behaviour from tensile test	114
17	4.0.2 Relation of impact strain signal pattern with success-strain curve	171
4.7	Summary	121
7.0	Summary	1
COI	NCLUSION AND RECOMMENDATION	124
5.1	Conclusion	124
5.2	Contribution of study	125
5.3	Recommendations	126

4.

5.

REFERENCES	127
APPENDICES	141

.

### LIST OF TABLES

TABLE	TITLE	PAGE
2.1	Comparison of technique for measuring impact duration (Roberts et	
	al., 2001)	
2.2	Dimension of specimen geometry (Verleysen et al., 2009)	36
3.1	Properties of material	64
3.2	Dimension of tensile specimen	66
3.3	Charpy machine model SI-1 specifications	68
3.4	The properties of strain gauge	72
3.5	Mass of Charpy specimen at different thickness	87
3.6	Material properties for impact duration calculation	88
4.1	Average energy absorbed of Aluminium 6061-T6 at different	92
	parameters	
4.2	Average energy absorbed of Magnesium AM60 at different	92
	parameters	
4.3	Percentage increment of energy absorbed due to thickness	94
	increment at different impact speed	
4.4	Percentage decrement of energy absorbed due to speed increment	95
	(3.35 m/s to 5.18 m/s) for each thickness	
4.5	Average maximum strain of Aluminium 6061-T6 at different	100

parameters

4.14

- 4.6 Average maximum strain of Magnesium AM60 at different 101 parameters
- 4.7 Average impact duration of Aluminium 6061-T6 at different 103 parameters
- 4.8 Average impact duration of Magnesium AM60 at different 103 parameters
- 4.9 Average area under ε-t graph of Aluminium 6061-T6 at different 105 parameters
- 4.10 Average area under ε-t graph of Magnesium AM60 at different 105 parameters
- 4.11 Average area under PSD of Aluminium 6061-T6 at different 107 parameters
- 4.12 Average area under PSD graph of Magnesium AM60 at different 107 parameters
- 4.13 Impact duration from experiment, theory and previous study 114

117

Tensile strength of material

- 4.15 Ultimate, yield and fracture load of material under tensile test 118
- 4.16 Strain energy and energy absorbed under tensile test
  4.17 Mechanical properties of tensile specimen
  118
- 4.18 Characterization and classification of impact strain signal 122

vii

### LIST OF FIGURES

FIGURE	TITLE	PAGE
2.1	Model of mechanical system in collision between two masses	10
	(Rajalingham and Rakheja, 2000)	
2.2	Configuration of Charpy V-notch test	12
2.3	Impact time in load-time curve in instrumented Charpy test (Kruger	15
	2003)	
2.4	Crash pulse duration, Tp and $\Delta V$ identification from graph (Linder	17
	and Krafft, 2003)	
2.5	Velocity profile of a car during impact (Njuguna, 2011)	18
2.6	Spring mass model under low velocity impact of sandwich beam	20
	(Daniel et al., 2012)	
2.7	Potential energy from Charpy test	22
2.8	Specimen with different notch position in HAZ: (a) 0.5 mm; (b) 1.0	23
	mm; (c) 1.5 mm from fusion line (Jang et al., 2008)	
2.9	Comparison of energy absorbed between experiment and computed	24
	(Jang et al. 2008)	
2.10	Peeling of bonded elastic strip (Serizawa et al., 2001)	24
2.11	Effect of shape of notch tip on load-displacement curve (Serizawa et	25
	al., 2001)	

.

### viii

- 2.12 Figure 2.12: Effect of notch depth on energy absorbed of maraging 25 steel 300 (Madhusudhan et al., 2018)
- 2.13 Temperature dependence of absorbed energy as a function of V- 26 notch dimensions for different size of miniaturized Charpy specimen: (a) 3.3 mm, (b) 2 mm, (c) 1.5 mm and (d) 1 mm (Kurishita et al., 1993)
- 2.14 The load-displacement curve of square tube for width (a) 30 mm and 28
  (b) 50 mm at different thicknesses (Marzbanrad et al., 2010)
- 2.15 Effect of core thickness: (a) 20 mm; (b) 30 mm and (c) 40 mm on 29 impact performance (Sawal and Akil, 2011)
- 2.16 Experimental technique used for high strain rate deformation 31 (Ramesh, 2008)
- 2.17 Strain rate at different type of loading (Othman and Marzouk, 2016) 31
- 2.18 Effect of temperature on energy absorption of chromium-containing 32
   dual phase 3CR12 steel (Weiss et al., 1990)
- 2.19 Engineering stress-strain curves of low carbon steel sheets at 33 various strain rates (Paul et al., 2014)
- 2.20 Dissipated energy of square section (Q2,Q4), hexagonal section (E1, 34
  E3) and double-cell section (C2, C3) at speed of 9 m/s (Peroni et al., 2002)
- 2.21 Deflection rate effect of TRIP steel on J-integral (Pham and 35 Iwamoto, 2015)
- 2.22 Schematic diagram of specimen geometry (Verleysen et al., 2009) 36
- 2.23 Stress-strain curve in centre of specimen at different geometries 36

ix

(Verleysen et al., 2009)

2.24	Energy absorbed-displacement curve for (a) circular and (b) stepped				
	tube (Higuchi et al., 2014)				

- 2.25 Effect of mesh size and impact direction on energy absorbed at (a)
  42
  90°, (b) 13° impact test (Zainuddin et al., 2016)
- 2.26 (a) Impact energy and (b) dynamic fracture toughness for sandwich
   43 GFRP- polyurethane foam-GFRP structures at different impact testing (Srivastava, 2012)
- 2.27 Deformation of strain 44
- 2.28Structure of foil type strain gauge45
- 2.29 Classification of signals (Nuawi et al, 2009) 47
- 2.30Deforms energy of paper cup under free fall (Shah and Abakr, 2007)48
- 2.31Deforms energy of steel cup under free fall (Shah and Abakr, 2007)48
- 2.32Plastic strain of paper cup under free fall (Shah and Abakr, 2007)48
- 2.33Plastic strain of steel cup under free fall (Shah and Abakr, 2007)49
- 2.34 Impact localization on composite plate (Hiche et al., 2011) 49
- 2.35 Principle strain responses at location (a) one and (b) two (Kruger, 50 2003)
- 2.36 Strain gage results with and without blade rubbing at running speeds
  52 of (a) 5 Hz, (b) 10 Hz and (c) 16.7 Hz (Trethewey and Cafeo, 1992)
- 2.37 Load history of sandwich beam at different (a) PVC foam cores 53 density, (b) facesheet properties and (c) energy level of balsa wood core (Daniel et al., 2012)
- 2.38 Strain history of sandwich beam at different (a) PVC foam core 54

density, (b) energy level for core Divinycell H80 and (c) maximum tensile strain for stiffer balsa wood core (Daniel et al., 2012)

- 2.39 Modulus of resilience and modulus of toughness in stress-strain 55 curve
- 2.40 Strain signal plot of Aluminium 6061-T6 for 5 mm at speed: (a) 3.35 56 m/s and (b) 5.18 m/s (Ali et al., 2011)
- 2.41 Strain signal plot of Aluminium 6061-T6 for 10 mm at speed: (a) 57
  3.35 m/s and (b) 5.18 m/s (Ali et al., 2011)
- 2.42 The PSD plot of Element 837 at different frequency (a) 50 kHz, (b) 59
  100 kHz and (c) 150 kHz (Abdullah et al., 2011)
- 2.43 PSD for each damage retained of suspension and bracket 60 components (Rahim et al., 2018)
- 2.44 Distribution of the PSD among the different percentage of CNT in 61AZ31B magnesium alloy (Abdullah et al., 2015)
- 3.1 Flow chart presents the activities involved in research study 63
- 3.2 Detailed dimension of Charpy specimen (Ali et al., 2014) 65

- 3.3 Marked Charpy specimen
- 3.4Marked tensile specimen66
- 3.5 Apparatus and instrument used in Charpy test: (a) Charpy machine
  406 J, (b) Strain gauge, (c) Data acquisition system (eDAQ), (d)
  Computer as result display
- 3.6 Configuration of specimen on anvils
  3.7 Schematic diagram of experimental set up for instrumented Charpy
  70 test

3.8	Flow chart of Charpy test	70
3.9	Strain gauge installation basic procedures	71
3.10	Strain gauge cement	73
3.11	Strain gauge position on striker after installation	73
3.12	Dimension of strain gauge position on striker	73
3.13	Setup on specific preferences	74
3.14	Hardware setup	75
3.15	Transducer and massage channel setup	76
3.16	Setup on 120 Ohm quarter bridge	76
3.17	Setup on the bridge channel for (a) first and (b) second pages	76
3.18	Computed channel setup	78
3.19	Elapsed time on computed channel	78
3.20	Data mode setup on time history	79
3.21	TCE test control panel	80
3.22	Machine of Instron model 8872	81
3.23	Reading scale of energy absorbed in Charpy machine	82
3.24	Impact strain signal in InField software	83
3.25	Method to identify maximum strain and impact duration	84
3.26	Area under strain-time graph using OriginPro7	84
3.27	Method of strain signal analysis in time domain and frequency	85
	domain	
3.28	Digital analytical balance	87
4.1	Specimens of Aluminium 6061-T6 (a) before and (b) after impact	91
	test	

### xii

4.2	Specimens of Magnesium AM60 (a) before and (b) after impact test	91
4.3	A graph of average energy absorbed at different parameters for	93
	Aluminium 6061-T6 and Magnesium AM60	
4.4	Average strain-time graph of Aluminium 6061-T6 at 3.35 m/s for	96
	different thickness	
4.5	Average strain-time graph of Aluminium 6061-T6 at 5.18 m/s for	96
	different thickness	
4.6	Average strain-time graph of Magnesium AM60 at 3.35 m/s for	97
	different thickness	
4.7	Average strain-time graph of Magnesium AM60 at 5.18 m/s for	97
	different thickness	
4.8	Average PSD graph of Aluminium 6061-T6 at speed of 3.35 m/s for	98
	different thickness	
4.9	Average PSD graph of Aluminium 6061-T6 at speed of 5.18 m/s for	98
	different thickness	
4.10	Average PSD graph of Magnesium AM60 at speed of 3.35 m/s for	99
	different thickness	
4.11	Average PSD graph of Magnesium AM60 at speed of 5.18 m/s for	99
	different thickness	
4.12	Maximum strain at different parameters	102
4.13	Impact duration at different parameters	104
4.14	Effect of thickness and speed on area under strain-time graph	106
4.15	Effect of thickness and speed on area under PSD graph	108
4.16	Correlation of energy absorbed with PSD at speed of 3.35 m/s	110

4.17	Correlation of energy absorbed with PSD at speed of 5.18 m/s	110
4.18	Correlation of energy absorbed with strain-time at speed of 3.35 m/s	111
4.19	Correlation of energy absorbed with strain-time at speed of 5.18 m/s	112
4.20	Stress-strain curve of Aluminium 6061-T6	116
4.21	Stress-strain curve of Magnesium AM60	116
4.22	Relation of impact strain signal with stress-strain curve for (a)	120
	Aluminium 6061-T6 (b) Magnesium AM60 (c) Carbon steel 1050	
	(Ali et al., 2015)	

xiv

### LIST OF APPENDICES

APPENDIX	IX TITLE	
А	Result of Energy Absorbed and Impact Signal Parameters	141

 $\mathbf{x}\mathbf{v}$ 

### LIST OF ABBREVIATIONS

ASTM	-	American Society for Testing and Materials
CNT	-	Carbon nanotube
CVN	-	Charpy V-notch
DBT	-	Ductile-brittle transition
EA	-	Energy absorbed
FBG	-	Fibre Bragg grating
FEA	-	Finite element analysis
FEM	-	Finite element method
FFT	-	Fast Fourier Transform
GF	-	Gage factor
GFRP	-	Glass fibre reinforced plastic
HAZ	-	Heat Affected Zone
ISO	-	International Organization for Standardization
KCV	-	notch toughness
LYS	-	Low yield strength
PSD	-	Power Spectrum Density
PVC	-	Polyvinyl chloride
PZT	-	Piezoelectric ceramic material
TRIP	-	Transformation induced plasticity
UKM	-	Universiti Kebangsaan Malaysia

xvi

USE - Upper shelf energy
UTM - Universal Testing Machine
VA - Variable amplitude

xvii

## LIST OF SYMBOLS

I	Ŧ	-	Area
C		-	Damper of viscous damping coefficient
(	$C_t$	-	Total compliance
ŧ	2	-	Strain
ł	Ξ	-	Young Modulus
1	Eabs tot	-	Total energy absorbed
]	З <sub>ь</sub>		Bending energy
]	Ec	-	Contact energy
]	Ed	-	Deformation energy
]	E <sub>del</sub>	-	Delamination energy
]	E <sub>frac</sub>	-	Fracture energy
]	E <sub>k</sub>	-	Kinetic energy
]	Em	-	Membrane energy
]	E <sub>petal</sub>	-	Petaling energy
]	Es	-	Shear energy
1	F	-	Force
i	G(jω)	-	Frequency spectrum
	J	-	Impulse
	k	-	Spring stiffness
	kь	-	Bending spring constant

xviii

k <sub>c</sub>	-	Contact spring constant
k <sub>eq</sub>	-	Equivalent spring constant
k <sub>m</sub>	-	Membrane spring constant
k <sub>s</sub>	-	Shear spring constant
М	-	Total mass
ms	-	miliseconds
N	-	Shape parameter
Р	-	Instantaneous crushing load
р	-	Linear momentum
P <sub>m</sub>		Mean crushing load
$\mathbf{P}_{max}$	-	Maximum load
P <sub>xx</sub>	-	Power spectral density
R	-	Radius of spherical impactor
r <sub>o</sub>	-	Scale parameter
r <sub>xx</sub>	-	Autocorrelation function
S	-	Car crush
t	-	Impact duration
t <sub>c</sub>	-	Contact time
T <sub>p</sub>	-	Crash pulse duration
v	-	Poison's ratio
v	-	Velocity
Vc	-	Closing velocity
w	-	Vertical deflection
γ	-	Surface potential
ρ	-	Density

xix