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# Dispa-SET 2.0: unit commitment and power dispatch model

*Description, formulation, and implementation*

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**Abstract**

Most analyses of the future European energy system conclude that in order to achieve energy and climate change policy goals it will be necessary to ramp up the use of renewable energy sources.

The stochastic nature of those energies, together with other sources of short- and long-term uncertainty, already have significant impacts in current energy systems operation and planning, and it is expected that future energy systems will be forced to become increasingly flexible in order to cope with these challenges. Therefore, policy makers need to consider issues such as the effects of intermittent energy sources on the reliability and adequacy of the energy system, the impacts of rules governing the curtailment or storage of energy, or how much backup dispatchable capacity may be required to guarantee that energy demand is safely met.

Many of these questions are typically addressed by detailed models of the electric power sector with a high level of technological and temporal resolution. This report describes one of such models developed by the JRC's Institute for Energy and Transport: Dispa-SET 2.0, a unit commitment and dispatch model of the European power system aimed at representing with a high level of detail the short-term operation of large-scale power systems. The new model is an updated version of Dispa-SET 1.0, in use at the JRC since 2009.

## Table of Contents

1	Introduction .....	4
2	Description and formulation .....	4
2.1	Notation .....	4
2.1.1	Sets .....	4
2.1.2	Parameters .....	5
2.1.3	Variables .....	7
2.2	Equations .....	7
2.2.1	Objective function .....	8
2.2.2	Demand-related constraints .....	9
2.2.3	Power output bounds .....	11
2.2.4	Minimum up and down times .....	12
2.2.5	Storage-related constraints .....	13
2.2.6	Emission limits .....	14
2.2.7	Network-related constraints .....	14
2.2.8	Curtailement .....	15
2.2.9	Load shedding .....	15
3	Implementation .....	15
3.1	Rolling horizon .....	16
3.2	Data sources .....	16
4	Illustrative results .....	16
4.1	Model inputs and parameters .....	17
4.2	Simulations .....	19
4.2.1	Base case .....	19
4.2.2	Increasing VRE penetration scenarios .....	20
5	Conclusions and future work .....	21
6	References .....	23

## 1 Introduction

Most analyses of the future European energy system conclude that in order to achieve energy and climate change policy goals it will be necessary to ramp up the use of renewable energy sources.

The stochastic nature of those energies, together with other sources of short- and long-term uncertainty, already have significant impacts in current energy systems operation and planning, and it is expected that future energy systems will be forced to become increasingly flexible in order to cope with these challenges. Therefore, policy makers need to consider issues such as the effects of intermittent energy sources on the reliability and adequacy of the energy system, the impacts of rules governing the curtailment or storage of energy, or how much backup dispatchable capacity may be required to guarantee that energy demand is safely met.

Many of these questions are typically addressed by detailed models of the electric power sector with a high level of technological and temporal resolution. This report describes one of such models developed by the JRC's Institute for Energy and Transport: Dispa-SET 2.0, a unit commitment and dispatch model of the European power system. The new model is an updated version of Dispa-SET 1.0, in use at the JRC since 2009. The aim of this new version is to represent with a high level of detail the short-term operation of large-scale power systems. To that purpose we consider that the system is managed by a central operator with full information on the technical and economic data of the power plants, the demand, and the transmission network. This model is formulated as a tight and compact mixed-integer program, implemented in GAMS [1] and solved with CPLEX [2].

The rest of the report is organized as follows: section 2 describes the formulation of the model, section 3 explains how the model is implemented in GAMS, section 4 shows an illustrative example of the output produced by the model, and finally section 5 outlines the main conclusions of this work and presents forthcoming improvements to the model.

## 2 Description and formulation

The following sections detail the notation used throughout the report to describe the model, beginning with a list of the sets, parameters, and variables included. The second part describes the foundations of the model and each of the constraints considered.

### 2.1 Notation

#### 2.1.1 Sets

Table 1 lists the sets used in the model, corresponding to all the indices used in parameters, variables and equations.

**Table 1: list of sets**

Name	Description
d	Days
f	Fuel types
h	Hours
i	Time step in the solving loop
l	Transmission lines between nodes
mk	Mk={DA,2U,2D} (day-ahead, up and down reserves <sup>1</sup> )
n	Zones within each country (currently one zone, or node, per country)
p	Pollutants
t	Power generation technologies
tr(t)	Renewable power generation technologies
u	Units
s(u)	Storage units (including hydro reservoirs)

### 2.1.2 Parameters

Table 2 contains the list of parameters used in the model (highlighted in green in the equations).

**Table 2: list of parameters**

Name	Units	Description
AvailabilityFactor $H_{u,i}$	%	Percentage of nominal capacity available
CommittedInitial $u$	n.a.	Initial commitment status
CostFixed $u$	€/h	Fixed costs
CostLoadShedding $h,n$	€/MWh	Shedding costs
CostRampDown $u$	€/MW	Ramp-down costs
CostRampUp $u$	€/MW	Ramp-up costs
CostShutDown $u$	€/h	Shut-down costs
CostStartUp $u$	€/h	Start-up costs
CostVariable $H_{i,u}$	€/MWh	Variable costs
Curtailement $i,n$	n.a.	Curtailement indicator {binary: 1 allowed}
Demand $H_{i,n,mk}$	MW	Hourly demand in each zone
Duration	h	Duration of period $i$ (1 hour always)
Efficiency $u$	%	Power plant efficiency
EmissionMaximum $n,p$	tP	Emission limit per zone for pollutant $p$
EmissionRate $u,p$	tP/MW	Emission rate of pollutant $p$ from unit $u$
FlexibilityDown $u$	MW/h	Available fast <sup>2</sup> shut-down ramping capacity
FlexibilityUp $u$	MW/h	Available fast start-up ramping capacity
FlowMaximum $H_{i,l}$	MW	Line limits
FlowMinimum $H_{i,l}$	MW	Minimum flow
FuelPrice $H_{i,n,f}$	€/F	Fuel price per zone
Fuel $u,f$	n.a.	Fuel type used by unit $u$ {binary: 1 $u$ uses $f$ }

<sup>1</sup> In this report the term "reserves" refer to the aggregated needs for secondary and tertiary reserves.

<sup>2</sup> Ramping capacity that may be available within an hour, from fast-starting units.

Name	Units	Description
LineNode <sub>i,n</sub>	n.a.	Line-zone incidence matrix {-1,+1}
LoadShedding <sub>n,h</sub>	MW	Load that may be shed per zone in 1 hour
Location <sub>u,n</sub>	n.a.	Location {binary: 1 <i>u</i> located in <i>n</i> }
M	minute	Time in which fast units may be started up or shut down
MarkupH <sub>i,u</sub>	€/MWh	Mark-up term added to the variable cost
OutageFactor <sub>u,h</sub>	%	Outage factor (100 % = full outage) per hour
Ownership <sub>u,g</sub>	n.a.	Ownership indicator {binary: 1 <i>u</i> owned by <i>g</i> }
PartLoadMin <sub>u</sub>	%	Percentage of nominal capacity needed for stable generation
PermitPrice <sub>p</sub>	€/tP	Permit price for pollutant <i>p</i>
PowerCapacity <sub>u</sub>	MW	Installed capacity
PowerInitial <sub>u</sub>	MW	Power output before initial period
PowerMinStable <sub>u</sub>	MW	Minimum power for stable generation
PowerMustRunH <sub>u,i</sub>	MW	Minimum power output
PriceH <sub>i,n,mk</sub>	€/MWh	Electricity price per market and zone
PriceTransmissionH <sub>i,l</sub>	€/MWh	Price of transmission between zones
RampDownMaximum <sub>u</sub>	MW/h	Ramp down limit
RampShutDownMaximum <sub>u</sub>	MW/h	Shut-down ramp limit
RampStartUpMaximum <sub>u</sub>	MW/h	Start-up ramp limit
RampUpMaximum <sub>u</sub>	MW/h	Ramp up limit
Reserve <sub>t</sub>	n.a.	Reserve provider {binary: 1 if <i>t</i> may provide reserve}
StorageCapacity <sub>s</sub>	MWh	Storage capacity (reservoirs)
StorageChargingCapacity <sub>s</sub>	MW	Maximum charging capacity
StorageChargingEfficiency <sub>s</sub>	%	Charging efficiency
StorageDischargeEfficiency <sub>s</sub>	%	Discharge efficiency
StorageInflowH <sub>i,s</sub>	MWh	Storage inflows
StorageInitial <sub>s</sub>	MWh	Storage level before initial period
StorageMinimum <sub>s</sub>	MWh	Minimum storage level
StorageOutflowH <sub>i,s</sub>	MWh	Storage outflows (spills)
Technology <sub>u,t</sub>	n.a.	Technology type {binary: 1: <i>u</i> belongs to technology type <i>t</i> }
TimeDownInitial <sub>u</sub>	h	Hours down before initial period
TimeDownLeft_Initial <sub>u</sub>	h	Time down remaining at initial time
TimeDownLeft_JustStopped <sub>i,u</sub>	h	Time down remaining if started at time <i>i</i>
TimeDownMinimum <sub>u</sub>	h	Minimum down time
TimeDown <sub>u,h</sub>	h	Number of hours down
TimeUpInitial <sub>u</sub>	h	Number of hours up before initial period
TimeUpLeft_Initial <sub>u</sub>	h	Time up remaining at initial time
TimeUpLeft_JustStarted <sub>i,u</sub>	h	Time up remaining if started at time <i>i</i>
TimeUpMinimum <sub>u</sub>	h	Minimum up time
TimeUp <sub>u,h</sub>	h	Number of hours up
VOLL <sub>Power</sub>	€/MWh	Value of lost load due to power deficits
VOLL <sub>Reserver</sub>	€/MWh	Value of lost load due to reserve deficits
VOLL <sub>Ramp</sub>	€/MWh	Value of lost load due to ramp deficits

### 2.1.3 Variables

Table 3 contains the list of variables considered in the model. All the variables are defined as positive variables, except  $CommittedH_{i,u}$ , which is binary.

**Table 3: list of variables**

Name	Units	Description
$CommittedH_{i,u}$	n.a.	Unit committed at hour $h \in \{1,0\}$
$CostRampDownH_{i,u}$	€/MWh	Ramp-down cost
$CostRampUpH_{i,u}$	€/MWh	Ramp-up cost
$CostShutDownH_{i,u}$	€/h	Shut-down cost if $u$ is de-committed
$CostStartUpH_{i,u}$	€/h	Start-up cost if $u$ is committed
$CurtailedPowerH_{i,n}$	MW	Power curtailed at zone $n$
$FlowH_{i,l}$	MW	Flow through lines
$LostLoad\_MaxPower_{i,n}$	MW	Deficit in terms of maximum power
$LostLoad\_MinPower_{i,n}$	MW	Power exceeding the demand
$LostLoad\_RampDown_{i,u}$	MW	Deficit in terms of ramping down
$LostLoad\_RampUp_{i,u}$	MW	Deficit in terms of ramping up
$LostLoad\_Reserve2D_{i,n}$	MW	Deficit in reserve down
$LostLoad\_Reserve2U_{i,n}$	MW	Deficit in reserve up
$MaxRamp2D_{i,u}$	MW/h	Maximum fast ramp-down capability
$MaxRamp2U_{i,u}$	MW/h	Maximum fast ramp-up capability
$PowerH_{i,u}$	MW	Power output from unit $u$
$ShedLoadH_{h,n}$	MW	Shed load (voluntary) per zone and hour
$StorageInputH_{i,s}$	MWh	Energy charged into storage unit $s$
$StorageLevelH_{i,s}$	MWh	Energy stored by storage unit $s$
$SystemCostsH$	€	Total system costs

## 2.2 Equations

The aim of this model is to represent with a high level of detail the short-term operation of large-scale power systems solving the so-called unit commitment problem. To that aim we consider that the system is managed by a central operator with full information on the technical and economic data of the generation units, the demands in each node, and the transmission network.

The unit commitment problem considered in this report is a simplified instance of the problem faced by the operator in charge of clearing the competitive bids of the participants into a wholesale day-ahead power market. In the present formulation the demand side is an aggregated input for each node, while the transmission network is modelled as a transport problem between the nodes (that is, the problem is network-constrained but the model does not include the calculation of the optimal power flows).

The unit commitment problem consists of two parts: i) scheduling the start-up, operation, and shut down of the available generation units, and ii) allocating (for each period of the simulation horizon of the model) the total power demand among the available generation units in such a way that the overall power system costs is minimized. The first part of the problem, the unit scheduling during several periods of time, requires the use of binary variables in order to represent the start-up and shut down decisions, as well as the

consideration of constraints linking the commitment status of the units in different periods. The second part of the problem is the so-called economic dispatch problem, which determines the continuous output of each and every generation unit in the system. Therefore, given all the features of the problem mentioned above, it can be naturally formulated as a mixed-integer linear program (MILP). The formulation of the model presented in this report is based upon publicly available modelling approaches [3, 4, 5]. Since our goal is to model a large European interconnected power system, we have implemented a so-called tight and compact formulation, in order to simultaneously reduce the region where the solver searches for the solution and increase the speed at which the solver carries out that search. Tightness refers to the distance between the relaxed and integer solutions of the MILP and therefore defines the search space to be explored by the solver, while compactness is related to the amount of data to be processed by the solver and thus determines the speed at which the solver searches for the optimum. Usually tightness is increased by adding new constraints, but that also increases the size of the problem (decreases compactness), so both goals contradict each other and a trade-off must be found.

### 2.2.1 Objective function

The goal of the unit commitment problem is to minimize the total power system costs (expressed in € in equation 1), which are defined as the sum of different cost items, namely: start-up and shut-down, fixed, variable, ramping, transmission-related and load shedding (voluntary and involuntary) costs.

<b>1</b>	$\min \text{SystemCostH} = \sum_{\forall u,i} \left( \begin{aligned} & \text{CostStartUp}_{H_{i,u}} + \text{CostShutDown}_{H_{i,u}} + \\ & \text{CostFixed}_u \cdot \text{Committed}_{H_{i,u}} + \\ & \text{CostVariable}_{H_{i,u}} \cdot \text{Power}_{H_{i,u}} + \\ & \text{CostRampUp}_{H_{i,u}} + \text{CostRampDown}_{H_{i,u}} + \\ & \text{PriceTransmission}_{H_{i,l}} \cdot \text{Flow}_{H_{i,l}} + \\ & \sum_n (\text{CostLoadShedding}_{H_{i,n}} \cdot \text{ShedLoad}_{H_{i,n}}) + \\ & \text{VOLL}_{\text{Power}} \cdot \sum_n (\text{LostLoad\_MaxPower}_{H_{i,n}} + \text{LostLoad\_MinPower}_{H_{i,n}}) + \\ & \text{VOLL}_{\text{Reserve}} \cdot \sum_n (\text{LostLoad\_Reserve2U}_{H_{i,n}} + \text{LostLoad\_Reserve2D}_{H_{i,n}}) + \\ & \text{VOLL}_{\text{Ramp}} \cdot \sum_u (\text{LostLoad\_RampUp}_{H_{i,u}} + \text{LostLoad\_RampDown}_{H_{i,u}}) \end{aligned} \right) \cdot \text{Duration}$
----------	--

The costs terms related to start-up and shut-down are above zero whenever the units change their commitment status:

<b>2</b>	$\begin{aligned} i = 1: \\ & \text{CostStartUp}_{H_{i,u}} \geq \text{CostStartUp}_u \cdot (\text{Committed}_{H_{i,u}} - \text{CommittedInitial}_u) \\ & \text{CostShutDown}_{H_{i,u}} \geq \text{CostShutDown}_u \cdot (\text{CommittedInitial}_u - \text{Committed}_{H_{i,u}}) \\ i > 1: \\ & \text{CostStartUp}_{H_{i,u}} \geq \text{CostStartUp}_u \cdot (\text{Committed}_{H_{i,u}} - \text{Committed}_{H_{i-1,u}}) \\ & \text{CostShutDown}_{H_{i,u}} \geq \text{CostShutDown}_u \cdot (\text{Committed}_{H_{i-1,u}} - \text{Committed}_{H_{i,u}}) \end{aligned}$
----------	--

In the previous equation, as in some of the following, a distinction is made between the equation for the first and subsequent periods. The equation for the first period takes into



account the commitment status of the unit before the beginning of the simulation, which is part of the information fed into the model.

Ramping costs are computed in the same manner:

<b>3</b>	$i = 1:$ $CostRampUpH_{i,u} \geq CostRampUp_u \cdot (PowerH_{i,u} - PowerInitial_u)$ $CostRampDownH_{i,u} \geq CostRampDown_u \cdot (PowerInitial_u - PowerH_{i,u})$ $i > 1:$ $CostRampUpH_{i,u} \geq CostRampUp_u \cdot (PowerH_{i,u} - PowerH_{i-1,u})$ $CostRampDownH_{i,u} \geq CostRampDown_u \cdot (PowerH_{i-1,u} - PowerH_{i,u})$
----------	--

It should be noted that in case of start-up and shut-down, the ramping costs are added to the objective function. Using start-up, shut-down and ramping costs at the same time should therefore be performed with care.

In the current formulation all other costs (fixed and variable) are considered as exogenous parameters. The variable production costs (in €/MW), are determined by fuel and emission prices corrected by the efficiency (which is considered to be constant for all levels of output in this version of the model) and the emission rate of the unit (equation 4):

<b>4</b>	$CostVariable_{i,u} =$ $Markup_{i,u} + \sum_{n,f} \left( \frac{Fuel_{u,f} \cdot FuelPrice_{i,n,f} \cdot Location_{u,n}}{Efficiency_u} \right) + \sum_p (EmissionRate_{u,p} \cdot PermitPrice_p)$
----------	--

The previous equation includes an additional mark-up parameter that is used for calibration and validation purposes.

Transmission costs are also considered to be exogenous, and they result from multiplying the energy flows through the network by the corresponding transmission price (exogenous).

As regards load shedding, the model considers the possibility of voluntary load shedding resulting from contractual arrangements between generators and consumers. Additionally, in order to facilitate tracking and debugging of errors, the model also considers some variables representing the capacity the system is not able to provide when the minimum/maximum power, reserve, or ramping constraints are reached. These lost loads are a very expensive last resort of the system used when there is no other choice available. The different lost loads are assigned very high values (with respect to any other costs). This allows running the simulation without infeasibilities, thus helping to detect the origin of the loss of load. In a normal run of the model, without errors, all these variables are expected to be equal to zero.

## 2.2.2 Demand-related constraints

The main constraint to be met is the supply-demand balance, for each period and each zone, in the day-ahead market (equation 5). According to this restriction, the sum of all the power produced by all the units present in the node (including the power generated by the storage units), the power injected from neighbouring nodes, and the curtailed power from intermittent sources is equal to the load in that node, plus the power consumed for energy storage, minus the load interrupted and the load shed.

<b>5</b>	$ \begin{aligned} & \sum_u (PowerH_{i,u} \cdot Location_{u,n}) \\ & + \sum_l (FlowH_{i,l} \cdot LineNode_{i,n}) \\ & - Curtailment_n \cdot CurtailedPowerH_{i,n} \\ & = DemandH_{n,n,DA} + \sum_r (StorageInputH_{n,s} \cdot Location_{r,n}) \\ & \quad - ShedLoadH_{i,n} - LostLoad\_MaxPower_{i,n} + LostLoad\_MinPower_{i,n} \end{aligned} $
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Besides that balance, the reserve requirements (upwards and downwards) in each node must be met as well. The reserve requirements considered in this model are an aggregation of secondary and tertiary reserves, which are typically brought online in periods shorter than an hour, the time step of this model. Therefore, additional equations and constraints must be defined for representing the up/down ramping requirements, by computing the ability of each unit to adapt its power output in periods below 60 minutes.

For each power plant, the ability to increase its power is the ramp-up capability if it is already committed or the nominal power if it is stopped and its starting time is lower than  $M$  minutes (equation 6). This is to take into account that fast starting units could provide reserve (hydro units for secondary reserve, gas turbine for tertiary reserve).

<b>6</b>	$MaxRamp2U_{i,u} \leq RampUpMaximum_u \cdot CommittedH_{i,u} + FlexibilityUp_u \cdot (1 - CommittedH_{i,u})$
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The parameter  $FlexibilityUp_u$  is the maximum ramp rate reachable by the unit in  $M$  minutes in case of cold start:

<b>7</b>	$ \begin{aligned} & \text{If } RampStartUpMaximum_u \geq PowerMinStable_u \cdot \frac{60}{M} \\ & \text{Then } FlexibilityUp_u = RampStartUpMaximum_u \\ & \text{Else } FlexibilityUp_u = 0 \end{aligned} $
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The maximum ramping rate is also limited by the available capacity margin between current and maximum power output (equation 8).

<b>8</b>	$MaxRamp2U_{i,u} \leq (PowerCapacity_u \cdot AvailabilityFactorH_{u,i} - PowerH_{i,u}) \cdot \frac{60}{M}$
----------	--

The same applies to ramping down capabilities within periods below 60 minutes.

<b>9</b>	$MaxRamp2D_{i,u} \leq \max(RampDownMaximum_u, FlexibilityDown_u) \cdot CommittedH_{i,u}$
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The parameter  $FlexibilityDown_u$  is defined as the maximum ramp down rate at which the unit can shut down in  $M$  minutes.

In case the unit cannot be shut-down in  $M$  minutes (and only in this case) the maximum ramping down capability is limited by the capacity margin between actual and minimum power:

<b>10</b>	$ \begin{aligned} & \text{If } RampShutDownMaximum_u < PowerMinStable_u \cdot \frac{60}{M} \\ & \text{Then } MaxRamp2D_{i,u} \leq (PowerH_{i,u} - PowerMinStable_u \cdot CommittedH_{i,u}) \cdot \frac{60}{M} \\ & \text{Else } MaxRamp2D_{i,u} \leq PowerH_{i,u} \cdot \frac{60}{M} \end{aligned} $
-----------	--

The reserve requirements are defined by the users. In case no input is provided a default formula is used to evaluate the needs for secondary reserves as a function of the

maximum expected load for each day. The default formula is described by equation 11, as defined by ENTSO-E [6, 7]:

<b>11</b>	$Demand_{i,n,2U} = \sqrt{10 \cdot \max_h(Demand_{i,n,DA}) + 150^2} - 150$
-----------	---

Down reserves are defined as 50% of the upward margin:

<b>12</b>	$Demand_{i,n,2D} = 0.5 \cdot Demand_{i,n,2U}$
-----------	---

The reserve demand should be fulfilled at all times by all the plants allowed to participate in the reserve market:

<b>13</b>	$Demand_{i,n,2U} \leq \sum_{u,t} (MaxRamp2U_{i,u} \cdot Technology_{u,t} \cdot Reserve_t \cdot Location_{u,n}) + LostLoad\_Reserve2UH_{i,n}$
-----------	--

The same equation applies to downward reserve requirements (2D).

### 2.2.3 Power output bounds

The minimum power output is determined by the must-run or stable generation level of the unit if it is committed:

<b>14</b>	$PowerMustRunH_{i,u} \cdot CommittedH_{i,u} \leq PowerH_{i,u}$
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On the other hand, the output is limited by the available capacity, if the unit is committed:

<b>15</b>	$PowerH_{i,u} \leq PowerCapacity_u \cdot AvailabilityFactorH_{i,u} \cdot CommittedH_{i,u}$
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The power output in a given period also depends on the output levels in the previous and the following periods and on the ramping capabilities of the unit. If the unit was down, the ramping capability is given by the maximum start up ramp, while if the unit was online the limit is defined by the maximum ramp up rate. Those bounds are given by equation 16:

<b>16</b>	$  \begin{aligned}  & i = 1: \\  & \quad PowerH_{i,u} \leq \\  & \quad \quad PowerInitial_u \\  & \quad \quad + CommittedInitial_u \cdot RampUpMaximum_u \\  & \quad \quad + (1 - CommittedInitial_u) \cdot RampStartUpMaximum_u \\  & \quad \quad + LostLoad\_RampUpH_{i,u} \\  & i > 1: \\  & \quad PowerH_{i,u} \leq \\  & \quad \quad PowerH_{i-1,u} \\  & \quad \quad + CommittedH_{i-1,u} \cdot RampUpMaximum_u \\  & \quad \quad + (1 - CommittedH_{i-1,u}) \cdot RampStartUpMaximum_u \\  & \quad \quad + LostLoad\_RampUpH_{i,u}  \end{aligned}  $
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And by equation 17:

17	$i = 1:$	$\begin{aligned} Power_{H_{i,u}} \leq & PowerCapacity_u \cdot AvailabilityFactor_{H_{i,u}} \cdot Committed_{H_{i,u}} \\ & + (1 - Committed_{H_{i,u}}) \cdot RampShutDownMaximum_u \\ & + LostLoad\_RampDown_{H_{i,u}} \end{aligned}$
	$i < card(i):$	$\begin{aligned} Power_{H_{i,u}} \leq & PowerCapacity_u \cdot AvailabilityFactor_{H_{i,u}} \cdot Committed_{H_{i+1,u}} \\ & + (1 - Committed_{H_{i+1,u}}) \cdot RampShutDownMaximum_u \\ & + LostLoad\_RampDown_{H_{i,u}} \end{aligned}$

Similarly, the ramp down capability is limited by the maximum ramp down or the maximum shut down ramp rate:

18	$i = 1:$	$\begin{aligned} PowerInitial_u - Power_{H_{i,u}} \leq & Committed_{H_{i,u}} \cdot RampDownMaximum_u \\ & + (1 - Committed_{H_{i,u}}) \cdot RampShutDownMaximum_u \\ & + LostLoad\_RampDown_{H_{i,u}} \end{aligned}$
	$i > 1:$	$\begin{aligned} Power_{H_{i-1,u}} - Power_{H_{i,u}} \leq & Committed_{H_{i,u}} \cdot RampDownMaximum_u \\ & + (Committed_{H_{i-1,u}} - Committed_{H_{i,u}}) \cdot RampShutDownMaximum_u \\ & + LostLoad\_RampDown_{H_{i,u}} \end{aligned}$

While the ramp up limitation is defined by:

19	$i = 1:$	$\begin{aligned} PowerInitial_u - Power_{H_{i,u}} \leq & CommittedInitial_u \cdot RampUpMaximum_u \\ & + (Committed_{H_{i,u}} - CommittedInitial_u) \cdot RampStartupMaximum_u \\ & + LostLoad\_RampUp_{H_{i,u}} \end{aligned}$
	$i > 1:$	$\begin{aligned} Power_{H_{i,u}} - Power_{H_{i-1,u}} \leq & Committed_{H_{i-1,u}} \cdot RampUpMaximum_u \\ & + (Committed_{H_{i,u}} - Committed_{H_{i-1,u}}) \cdot RampStartupMaximum_u \\ & + LostLoad\_RampUp_{H_{i,u}} \end{aligned}$

## 2.2.4 Minimum up and down times

The operation of the generation units is limited as well by the amount of time the unit has been running or stopped. Due to the physical characteristics of the generators, once a unit is started up it cannot be shut down immediately, while if the unit is shut down it may not be started immediately. These constraints can be expressed naturally in a non-linear form as:

20	$(TimeUp_{u,y,m,d,h-1} - TimeUpMinimum_u) \cdot (Committed_{H_{h-1,u}} - Committed_{H_{h,u}}) \geq 0$
21	$(TimeDown_{u,y,m,d,h-1} - TimeDownMinimum_u) \cdot (Committed_{H_{h-1,u}} - Committed_{H_{h,u}}) \leq 0$

That is, the value of the time counter with respect to the minimum up time and down times determines the commitment status of the unit. In order to model the previous constraints linearly, it is necessary to keep track of the number of hours the unit must be online at the beginning of the simulation for having been online less than the minimum up time:

22	$TimeUpLeft\_Initial_u = \min\{card(i), (TimeUpMinimum_u - TimeUpInitial_u) \cdot CommittedInitial_u\}$
----	---

If the unit is initially started up, it has to remain committed until reaching the minimum up time:

<b>23</b>	$\sum_{i=1}^{TimeUpLeft\_Initial_u} (1 - CommittedH_{i,u}) = 0$
-----------	---

If the unit is started during the considered horizon, the time it has to remain online is *TimeUpMinimum*, but cannot exceed the time remaining in the simulated period. This is expressed in equation 24 and is pre-calculated for each time step of the period.

<b>24</b>	$TimeUpLeft\_JustStarted_{i,u} = \min\{card(i) - ord(i) + 1, TimeUpMinimum_u\}$
-----------	---

The equation imposing the unit to remain committed is written:

<b>25</b>	$  \begin{aligned}  & i = 1: \\  & \sum_{ii=i}^{i+TimeUpLeft\_JustStarted_{i,u}-1} CommittedH_{ii,u} \geq \\  & \quad TimeUpLeft\_JustStarted_{i,u} \cdot (CommittedH_{i,u} - CommittedInitial_u) \\  & i > 1: \\  & \sum_{ii=i}^{i+TimeUpLeft\_JustStarted_{i,u}-1} CommittedH_{ii,u} \\  & \quad \geq TimeUpLeft\_JustStarted_{i,u} \cdot (CommittedH_{i,u} - CommittedH_{i-1,u})  \end{aligned}  $
-----------	---

The same method can be applied to the minimum down time constraint:

<b>26</b>	$TimeDownLeft_u = \min\{24, (TimeDownMinimum_u - TimeDownInitial_u) \cdot (1 - CommittedInitial_u)\}$
-----------	---

Related to the initial status of the unit:

<b>27</b>	$\sum_{i=1}^{TimeDownLeft_u} CommittedH_{i,u} = 0$
-----------	--

The *TimeDownLeft\_JustStopped* parameter is computed by:

<b>28</b>	$TimeDownLeft\_JustStopped_{i,u} = \min\{card(i) - ord(i) + 1, TimeDownMinimum_u\}$
-----------	---

Finally, the equation imposing the time the unit has to remain de-committed is defined as:

<b>29</b>	$  \begin{aligned}  & i = 1: \\  & \sum_{hh=h}^{i+TimeDownLeft\_JustStopped_{i,u}-1} (1 - CommittedH_{h,u}) \\  & \quad \geq TimeDownLeft\_JustStopped_{i,u} \cdot (CommittedInitial_u - CommittedH_{i,u}) \\  & i > 1: \\  & \sum_{hh=h}^{i+TimeDownLeft\_JustStopped_{i,u}-1} (1 - CommittedH_{h,u}) \\  & \quad \geq TimeDownLeft\_JustStopped_{i,u} \cdot (CommittedH_{i-1,u} - CommittedH_{i,u})  \end{aligned}  $
-----------	---

## 2.2.5 Storage-related constraints

Generation units with energy storage capabilities (mostly large hydro reservoirs and pumped hydro storage units) must meet additional restrictions related to the amount of energy stored. Storage units are considered to be subject to the same constraints as non-

storage power plants. In addition to those constraints, storage-specific restrictions are added for the set of storage units (i.e. a subset of all units). These restrictions include the storage capacity, inflow, outflow, charging, charging capacity, charge/discharge efficiencies, etc. Discharging is considered as the standard operation mode and is therefore linked to the  $PowerH$  variable, common to all units.

The first constrain imposes that the energy stored by a given unit is bounded by a minimum value:

<b>30</b>	$StorageMinimum_s \leq StorageLevelH_{i,s}$
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And the storage capacity:

<b>31</b>	$StorageLevelH_{i,s} \leq StorageCapacity_s$
-----------	--

The energy added to the storage unit is limited by the charging capacity. Charging is allowed only if the unit is not producing (discharging) at the same time (i.e. if th  $CommittedH$ , corresponding to the "normal" mode, is equal to 0).

<b>32</b>	$StorageInputH_{i,s} \leq StorageChargingCapacity_s \cdot (1 - CommittedH_{i,s})$
-----------	---

Charge and discharge are limited by the level of charge of the storage unit:

<b>33</b>	$\frac{PowerH_{i,s}}{StorageDischargeEfficiency_s} + StorageOutflowH_{i,s} - StorageInflowH_{i,s} \leq StorageLevelH_{i,s}$
<b>34</b>	$StorageInputH_{i,s} \cdot StorageChargingEfficiency_s - StorageOutflowH_{i,s} + StorageInflowH_{i,s} \leq StorageCapacity_s - StorageLevelH_{i,s}$

Besides, the energy stored in a given period is given by the energy stored in the previous period, net of charges and discharges:

<b>35</b>	$i = 1: StorageLevelInitial_s + StorageInflowH_{i,s} + StorageInputH_{i,s} \cdot StorageChargingEfficiency_s$ $= StorageLevelH_{i,s} + StorageOutflowH_{i,s} + \frac{PowerH_{i,s}}{StorageDischargeEfficiency_s}$ $i > 1: StorageLevelH_{i-1,s} + StorageInflowH_{i,s} + StorageInputH_{i,s} \cdot StorageChargingEfficiency_s$ $= StorageLevelH_{i,s} + StorageOutflowH_{i,s} + \frac{PowerH_{i,s}}{StorageDischargeEfficiency_s}$
-----------	---

### 2.2.6 Emission limits

The operating schedule also needs to take into account any cap on the emissions (not only CO<sub>2</sub>) from the generation units existing in each node:

<b>36</b>	$\sum_u (PowerH_{i,u} \cdot EmissionRate_{u,p} \cdot Location_{u,n}) \leq EmissionMaximum_{n,p}$
-----------	--

### 2.2.7 Network-related constraints

The flow of power between nodes is limited by the capacities of the transmission lines:

<b>37</b>	$FlowMinimumH_{i,l} \leq FlowH_{i,l}$
-----------	---------------------------------------

<b>38</b>	$FlowH_{i,l} \leq FlowMaximumH_{i,l}$
-----------	---------------------------------------

In this model a simple transport-problem approach is followed.

### 2.2.8 Curtailment

If curtailment of intermittent generation sources is allowed in one node, the amount of curtailed power is bounded by the output of the renewable (*tr*) units present in that node:

<b>39</b>	$CurtailedPowerH_{i,n} \leq \sum_{u,tr} (PowerH_{i,u} \cdot Technology_{u,tr} \cdot Location_{u,n}) \cdot Curtailment_n$
-----------	--

### 2.2.9 Load shedding

If load shedding is allowed in a node, the amount of shed load is limited by the shedding capacity contracted on that particular node (e.g. through interruptible industrial contracts).

<b>40</b>	$ShedLoad_{i,n} \leq LoadShedding_{i,n}$
-----------	--

## 3 Implementation

The model is implemented in GAMS and solved with CPLEX. The code is structured in blocks as follows:

- Definition of datasets and options
- Definition of sets
- Definition of parameters
- Data import from Excel
- Definition of variables
- Assignments of initial values to specific parameters
- Declaration and definition of equations
- Model definition (list of equations included in the model)
- Solve loop (related to date-based inputs)
  - Definition of current and next day
  - Assignment of parameter values (from date-based parameters to loop-indexed parameters)
  - Definition of "must run" levels as a function of the minimum stable generation and the availability factor
  - Definition of time counters to keep track the amount of time units are online and offline
  - Solve statement
  - Update of time counters
  - Assignment of final values to initial values for the next day
- Definition of output parameters
- Assignment of values to output parameters.
- Export of outputs to Excel

### 3.1 Rolling horizon

The mathematical problem described in the previous sections could in principle be solved for a whole year split into time steps of one hour, but with all likelihood the problem would become extremely demanding in computational terms when attempting to solve the model with a realistically sized dataset. Therefore, the problem is split into smaller optimization problems that are run recursively throughout the year. Figure 1 shows an example of such approach, in which the optimization horizon is one day, with a look-ahead (or overlap) period of one day. The initial values of the optimization for day  $j$  are the final values of the optimization of the previous day. The look-ahead period is modelled to avoid issues related to the end of the optimization period such as emptying the hydro reservoirs, or starting low-cost but non-flexible power plants. In this case, the optimization is performed over 48 hours, but only the first 24 hours are conserved.

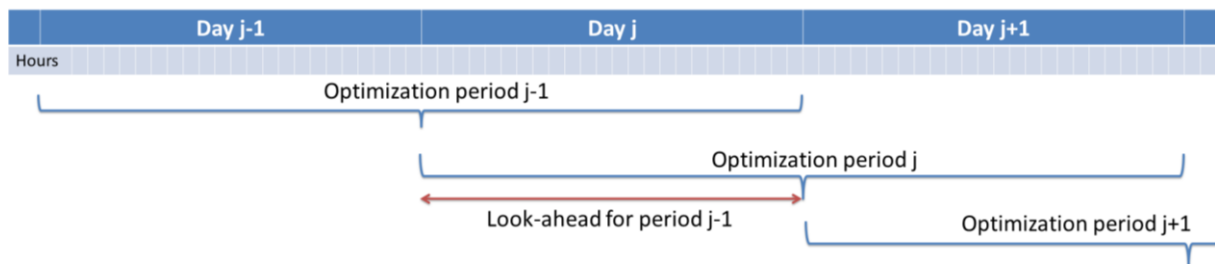


Figure 1: time horizons of the optimization with look-ahead period

### 3.2 Data sources

The sources of information consulted for developing the case study shown in section 4 are listed below

- Basic generation unit data (capacity, location, fuel, technology type, etc.) from Platts' World Electric Power Plant database [8].
- Demand and availability data from TSOs [9, 10]
- Fossil fuel prices from IEA [11].
- Plant ramping parameters from VGB Powertech [12], VDE [13], and scientific literature [14, 15, 16].
- Plant availability from VGB KISSY reports [12].

## 4 Illustrative results

To illustrate how the Dispa-SET model can be used to evaluate the impact of variable renewable energy (VRE) on the power system, a particular area is modelled using historical data as input. The selected area is the Belgian power system, due to the availability of data on loads, generation, and interconnections on this area.

The selected time period for the simulation is a one year period running from October 1<sup>st</sup> 2012, till September 30<sup>th</sup> 2013. The selection of the 2012-2013 winter instead of 2013-2014 is made in consideration of the fact that the latter was very mild, which might not be representative of usual operating conditions.

During the considered period, the net offtake was 81.06 TWh. The minimum and maximum loads are 5.9 GW and 13.4 GW, respectively. The net imports are significant and amounted



to 14.2 TWh, as Belgium was importing from France and the Netherlands during most of the time. The analysis was conducted using the 15-min data for the Belgian Transmission grid, operated by Elia [10], including:

- Vertical load data
- Power generation disaggregated by fuel type
- Interconnections and storage (pumped hydro) throughout the year
- VRE (wind and solar) generation and forecasts

There were 120 units connected to the transmission grid and subject to CIPU contracts (Contract for the Injection of Production Units), some of which have been disconnected between 2012 and 2013.

The relevant data include the type of power plant, minimum and maximum capacity, starting time, ramp up and down times, and minimum up and down times. When possible, the characteristics of the individual power plants they have been gathered from the power plants utilities. Generic values from the literature [16, 13, 17]) have also been used when no other data was available.

Fuel costs have been obtained using the Quarterly IEA statistics [11].

#### 4.1 Model inputs and parameters

Data sources for such a unit commitment model are diverse and most generally not standardized. A pre-processing tool is therefore necessary to format the data according to Table 1 and Table 2. This tool is written in Python and takes as input the data tables in various formats. The output is a “.gdx” file readable by GAMS.

The hourly load curve is averaged from the available 15-min data. A residual load is defined as the load seen by the Belgian TSO during 2012-2013 when interconnections have been added and when the effect of additional VRE capacity has been subtracted:

<b>41</b>	$Load_{residual} = Load - P_{wind} - P_{solar} - Losses_{grid} + Interconnections$
-----------	--

It was decided to include the interconnections into the residual load because of the difficulty to model them without a proper model of the neighbouring countries, and because the line capacity limits are not known. This methodology ensures that the imports are at its maximum level during the most critical hours of the year.

$P_{wind}$  and  $P_{solar}$  are the historical VRE generation curves scaled according to the installed capacity in the considered scenario. The grid losses are evaluated as a function of the current load using a calibrated polynomial curve.

Since this model focuses on the available technical flexibility and not on accurate market modelling, it is run using the measured historical data, and not the day-ahead forecasted load and VRE production. This can be partly justified by the fact that a fraction of the forecast errors can be solved on the intra-day market. This perfect foresight hypothesis is however optimistic and a more detailed stochastic simulation should be performed to refine the results.

The introduction of variable renewable on the grid entails increased ramping rates at different time scales (e.g. 15 min, 1 hours, 6 hours, etc.). The model time step being one hour, it is not straightforward to simulate the 15-min ramping needs. This is addressed by considering them as reserve constraints: the maximum 15-min ramp up/down rate is

computed for each hour of the simulation, and the required flexible capacity to fulfil this demand is put aside (i.e. not available for load following). This is performed using the reserve constraint of Dispa-SET: the automatic Frequency Restoration reserves ( $FRR_a$ ), the manual Frequency Restoration reserves ( $FRR_m$ ), and the 15-min ramping requirements are merged into one single variable:

<b>42</b>	$Reserve_{up/down} = FRR_a + \max(FRR_m, Ramping_{15,max,up/down})$
-----------	---

The “max” function ensures that enough flexibility is made available for ramping, but also that enough tertiary reserve ( $FRR_m$ ) was contracted in case the ramping needs are low.

The values of  $FRR_a$  and  $FRR_m$  are imposed using the Elia 2018 reserve study [18]. This study presents the advantage of evaluating the reserve needs with increased penetration of VRE, which is of particular relevance in the scope of this work. An  $FRR_a$  value of 140 MW is recommended for the base case (the year 2013), and a value of 172 MW is recommended for 2018, with a nominal capacity of VRE which has increased from 3.2 to 8 GW in the meantime. The required secondary reserves can therefore be expressed as a linear function of the VRE capacity with the following equation:

<b>43</b>	$FRR_a = 140 + \frac{172 - 140}{8 - 3.2} \cdot (P_{VRE} - 3.2)$
-----------	---

A similar approach is used for the evaluation of the tertiary reserve ( $FRR_m$ ) needs. These needs are one order of magnitude higher than for the secondary reserve, with values up/down around 1000 MW.

As aforementioned, data is provided for 120 CIPU units connected to the transmission grid. However, some of these units present a low capacity and a high flexibility, such as the turbojets whose output power does not exceed a few MW and which can reach full power in less than 15 minutes. For these units, a unit commitment model with a time step of 1 hour is unnecessary and computationally inefficient. Therefore, these units are merged into one single, highly flexible unit with averaged characteristics.

The minimum and maximum capacities of new aggregated units (indicated by \*) are given by:

<b>44</b>	$P_{min}^* = \min_j(P_{j,min})$ $P_{max}^* = \sum_j(P_{j,max})$
-----------	---

The unit marginal (or variable cost) is given by:

<b>45</b>	$Cost_{variable}^* = \frac{\sum_j(P_{j,max} \cdot Cost_{variable,j})}{P_{max}^*}$
-----------	---

The start-up/shut-down costs are transformed into ramping costs (example with ramp-up):

<b>46</b>	$Cost_{RampUp}^* = \frac{\sum_j(P_{j,max} \cdot Cost_{RampUp,j})}{P_{max}^*} + \frac{\sum_j(Cost_{startUp,j})}{P_{max}^*}$
-----------	--

Other characteristics, such as the plant efficiency, the minimum up/down times or the CO<sub>2</sub> emissions are averaged. It should however be noted that only very similar units are aggregated, which does not lead to significant averaging errors since their characteristic are equal or very close to one another. Using this methodology, the number of units could be significantly reduced, from 120 to 45.

The main model assumptions, inputs and parameters are summarized in Table 4.

**Table 4: modeling assumptions**

Time Step	1 hour
Simulation period	8760 hours (1/10/2012 to 30/09/2013)
Optimality criteria of the MILP solver	4%
Costs taken into account	Fuel Costs
Minimum up/down times	Depending on the unit type, from 0 to 24 hours
Technologies participating to reserve market	CCGT, Gas Turbines, Turbojets, Diesels
Load Shedding	331 MW with large TSO-connected industries
Power Curtailment	Not allowed, except if residual load <0
Nodes and line capacities	One single node (copper plate hypothesis)
Outages	Historical values
Load curve, VRE and interconnections	Historical values (possibly scaled)
Fuel Prices	Historical values

## 4.2 Simulations

To illustrate the model capabilities, different “what if” scenarios are defined and simulated. A “base scenario” is first defined, corresponding to the period 2012-2013. This allows comparing the simulation results with the actual generation data. Then, different simulations are performed with increasing share of VRE to evaluate the flexibility of the system.

### 4.2.1 Base case

The base scenario corresponds to the actual state of the park and of the consumption during the year 2012-2013. The comparison between simulation and historical data is available in Figure 2 and Figure 3. A fair agreement between both trends is stated. It should be noted that wind is not displayed because it has been netted from the load.

The whole simulation showed that the power system was able to meet the demand (in terms of ramping and max capacity) without issue in the base case. However, it is interesting to note that load shedding had to be activated two times during the simulation, on January 17th at 9h45 (71 MW) at 18h45 (303 MW). This date indeed corresponds to the only day in the year during which the TSO had to activate the interruptible load contracts. It should also be noted that this results was obtained without tuning the model parameters.

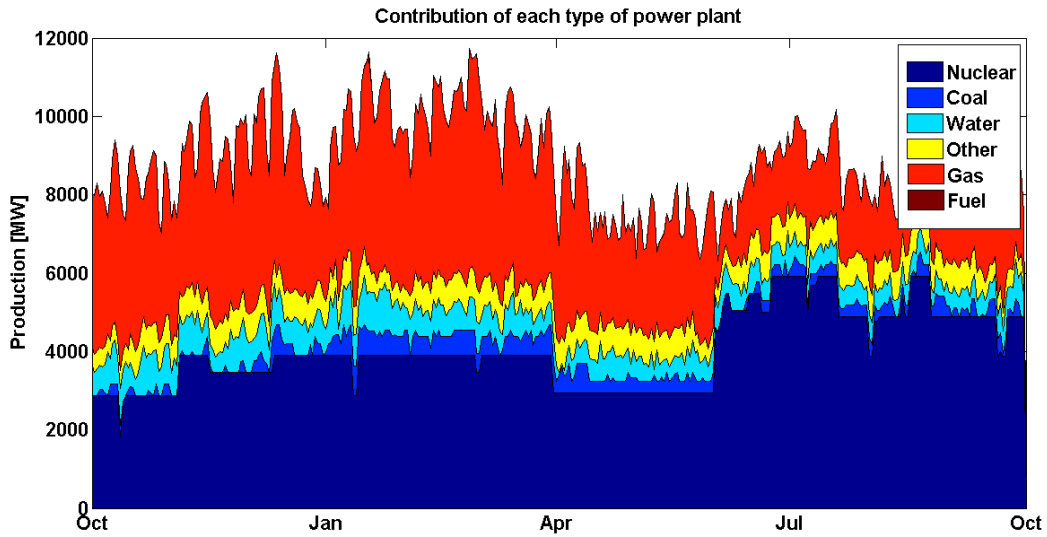


Figure 2: simulated generation throughout the year

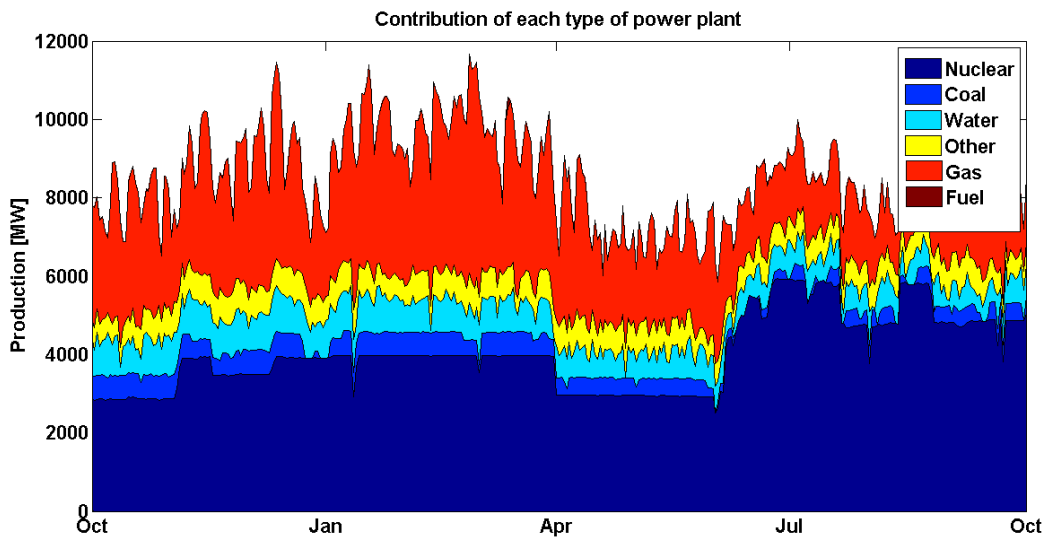


Figure 3: historical values of generation throughout the year

#### 4.2.2 Increasing VRE penetration scenarios

In these scenarios, all power plants are kept online as in the period 2012-2013, and the share of VRE is increased. The nominal installed power of wind and PV is increased successively by 4, 8 and 12 GW with respect to the base case, assuming an equal share between the two technologies.

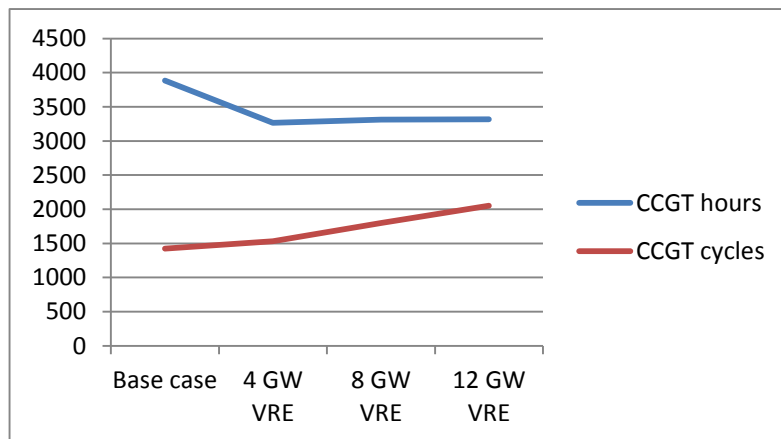
**Table 5: characteristics of the residual with different VRE penetration scenarios**

		<b>Base Case</b>	<b>4 GW VRE</b>	<b>8 GW VRE</b>	<b>12 GW VRE</b>
Additional VRE	Share of total [%]	0.00	8.50	17.00	25.50
Load	Max power [GW]	11.97	11.64	11.54	11.40
	Min power [GW]	3.93	2.43	0.00	0.00
Ramping, 15 minutes	Up [GW/h]	4.99	5.59	8.88	13.03
	Down [GW/h]	4.71	4.8	8.91	13.36
Ramping, 1 hour	Up [GW/h]	2.08	2.46	2.87	3.60
	Down [GW/h]	2.09	2.09	2.46	3.56
Ramping, 6 hours	Up [GW/h]	0.78	0.81	0.911	1.10
	Down [GW/h]	0.63	0.65	0.851	9.50

Table 5 summarizes the characteristic of the residual load in the different scenarios. The provided ramping values are maximum values for the whole year. It can be stated that VRE do not have a significant influence on the maximum load, but decrease the minimum residual load, which becomes null for 8 GW of additional VRE, corresponding to 17% of the total yearly consumption. The maximum ramping constraints are shown for 3 different timeframes, and logically increase with the amount of VRE.

Simulations results indicate that enough technical flexibility is available for the base case and the 2 first scenarios. However, for the “12 GW VRE” scenario, ramping capabilities are insufficient during 3 time periods for downward ramping and 2 time periods for upwards ramping.

Furthermore, Figure 4 shows the impact of VRE penetration on the operation of CCGT plants throughout the year. The number of start-ups logically increases with the share of renewables. However, the number of operating hours only decreases for the 4GW case compared to the base case. It then slightly increases. This is due to the flexibility required for balancing VRE generation, which lead to optimization problem to commit CCGT plants instead of other units such as nuclear plants.



**Figure 4: number of ON/OFF cycles throughout the year and average number of operating hours for CCGT plants**

## 5 Conclusions and future work

This document has described the formulation and implementation of Dispa-SET 2.0, a unit commitment and dispatch model of the power system developed by the Joint Research Centre's Institute for Energy and Transport. The model aims at representing with a high

level of detail the short-term operation of large-scale power systems, in order to be able of addressing properly different research topics relevant for supporting European energy policy making, such as the impact of increasing penetration of renewable energy sources.

To illustrate the model capabilities, a simulation has been run using historical data for the case of Belgium. The comparison between the historical data and the simulation indicates a fairly good agreement. Additional simulations have also been performed to assess the impact of increasing shares of VRE. Results indicate that there is enough technical flexibility available to balance a significant amount of renewable (up to 8 GW, corresponding to an additional share of 17%). For higher penetration scenarios, more flexibility would be required, e.g. by increased investments in flexible units (OCGT, Turbojets, CCGT, etc.), storage or demand response measures.

This preliminary work will be continued shortly by developing the code in order to cover all EU member states, add more basic features, build a European dataset to feed the model, and develop input/output interfaces for final users. In the longer-term, some other envisaged improvements would be:

- The inclusion of a better representation of reserve needs, distinguishing between different types of reserves (secondary and tertiary).
- The addition of a capacity planning module.
- The addition of new constraints (e.g. hydropower and water requirements for cooling).
- The addition of stochastic features.
- The linkage with the JRC-EU-TIMES energy system model [19].

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