

A Case Study on Investigation of Component Age Dependent Reliability Models

EC JRC Network on Use of Probabilistic Safety Assessments (PSA) for Evaluation of Aging Effects to the Safety of Energy Facilities.

Task 4.

A.Antonov, V.Chepurko, A.Polyakov, A. Rodionov

EUR 23079 EN - 2008





The Institute for Energy provides scientific and technical support for the conception, development, implementation and monitoring of community policies related to energy. Special emphasis is given to the security of energy supply and to sustainable and safe energy production.

European Commission Joint Research Centre Institute for Energy

Contact information

Address: PO Box 2, NL-1755 ZG Petten

E-mail: andrei.rodionov@jrc.nl

Tel.: 0224 56 54 57 Fax: 0224 56 56 21

http://ie.jrc.ec.europa.eu http://www.jrc.ec.europa.eu

Legal Notice

Neither the European Commission nor any person acting on behalf of the Commission is responsible for the use which might be made of this publication.

A great deal of additional information on the European Union is available on the Internet. It can be accessed through the Europa server http://europa.eu/

EUR 23079 EN ISSN 1018-5593

Luxembourg: Office for Official Publications of the European Communities

© European Communities, 2008

Reproduction is authorised provided the source is acknowledged

Printed in Netherlands

A Case Study on Investigation of Component Age Dependent Reliability Models

EC JRC Network on Use of Probabilistic Safety Assessments (PSA) for Evaluation of Aging Effects to the Safety of Energy Facilities.

Task 4.

A.Antonov, V.Chepurko, A.Polyakov, A. Rodionov

Abstract

The report presents the results of a case study on "Investigation of component age dependent reliability models" implemented by INPE and JRC IE in the frame of EC JRC Ageing PSA Network Task 4 activities. Several cases of Generalized Linear Model were proposed and investigated for the cases of continues and discrete data. The Fisher Chi-2 minimization approach was applied for goodness of fit test and parameters elaboration. Finally, uncertainty analysis was done for estimated parameters and model extrapolations. The results were analyzed and compared with other approaches.

Context

1. Introduction.	4
1.1. General background. 1.2. Task specification.	4 5
2. Initial data sets	5
3. Models and approach.	6
3.1 Models applied in case of data set 1. 3.2 Models applied in case of data set 2 3.3 Proposed approach 3.4 Goodness of fit test and parameters estimation 3.5 Parameters uncertainties 3.6 Trend verification	6 6 6 6 7 8
3.7 Model uncertainties and extrapolations	9
4. Results of calculations	9
4.1 Presentation of the results 4.2. Results analysis and interpretation 4.2.1. Identification of component susceptible to ageing 4.2.2. Comparison with results of non-parametric inversion test 4.2.3. Impact of burn-in failures 4.2.4. Comparison with other parametrical methods 4.2.5. Uncertainties of extrapolation.	9 13 13 14 15 16
5. Conclusions and recommendations	21
References	22
List of figures	23
List of tables	23
Annex 1	
Annexe 2	
Annexe 3	
Annex 4	
Annexe 5	
Annexe 6	
Annexe 7	

1. Introduction

1.1. General background.

IAEA PRIS data concerning aging profile of nuclear generation shows that actually (on the date of 3/08/2007) 115 units are between 30 and 40 years in operation and 213 are between 20 and 30 years old, which in total represent about 3/4 of 438 reactors operated worldwide.

More and more utilities, nowadays, move to the long-term operation policy. In USA, for example, at July 2006, approximately one-half of the licensed plants either have received, or are under review for license renewal.

What means that in the next decade the aging management and life extension issues will became one of the key points of nuclear safety.

The PSA as a safety evaluation tool could be more integrated into these programs to help with identification and prioritization of ageing issues and optimization of ageing management activities. For applying PSA to characterize potential risks associated with ageing effects, PSA should be as realistic as practical and appropriate support data should be available for the review.

- If PSA could be applied for ageing assessments?
- How realistically PSA models reflect important ageing issues?
- If any modifications or revisions of PSA assumptions are needed to apply PSA approach for risk-informed decision making in case of ageing evaluation?
- What data are available and how representative they are with regards to the important ageing issues? These and other related issues are under consideration of EC JRC Network on the Use of Probabilistic Safety Assessment (PSA) for the Evaluation of Ageing Effects on the Safety of Energy Facilities (Ageing PSA).

The initial motivation behind the Ageing PSA Network was the fact that current standard PSA tools do not adequately address important ageing issues, which could have a significant impact on the conclusions drawn from PSA studies and applications where plants are operated at an advanced age or long term.

The knowledge resulting from the Ageing PSA Network should help PSA developers and users:

- to incorporate the effects of equipment ageing into current PSA tools and models to perform engineering analysis,
- where PSA cannot be applied (where there are no or inadequate probabilistic ageing models or a lack of data, etc.), to specify and prioritise reliability monitoring actions/approaches to ensure that any decrease in the reliability of SSC is identified and corrected in time,
- to promote the use of PSA for ageing management and risk-informed applications for nuclear power plants.

The Ageing PSA Network is under development as part of JRC FP-7 institutional Project No 52101 "Analysis and Management of Nuclear Accidents" (AMA).

One of the tasks identified for the Network working plan relates to the reliability and data analysis for active components. The expected results is a demonstration the methods to elaborate the reliability parameters for Aging PSA model and classify the data needed. The results will help

- to improve reliability and maintenance data collection system,
- to choose the appropriate reliability model for the parameters estimation,
- to address ageing and maintenance effects in component failure models.
- to evaluate the model uncertainties.

The Case Study presented in the report was performed in collaboration between EC JRC Institute for Energy and Obninsk State Technical University of Nuclear Power Engineering from Russian Federation.

1.2. Task specification

The goal of the study is a demonstration of methods to build up and assess the component agedependent reliability models.

The following tasks were performed:

- verification of models validity,
- parameters estimation,
- identification of increasing trend,
- characterisation of uncertainties of estimated parameters and hole model,
- assessment on possible extrapolation and uncertainties of extrapolation.

2. Initial data sets

To demonstrate the method applicability and compare the results with other case studies JRC proposes to use two data sets:

- Data set 1, presented in Annexe 1, is a binned data on failure rates estimated at the bins. These data characterise component failure modes as fail to function, fail to run etc. The data correspond to the continuously distributed times to failure,
- Data set 2, described in Annexe 2, is a binned data on failure probability on demand per bin. This data set represents the failures on demand which could be described by discrete distributions.

All data in the data sets are "virtual". However, the statistic, which is provided for the case study is quite close to the real operating experience data collected on the French [], German or US power generation plants []. In particular, data include large samples that represent of components from the same technological group.

Binned data on failure rates for standby or continuously operated components (data set 1).

The failure rates were calculated on equal one-year intervals, sequence of which represents the time in operation or age of the component. This data has two particularities:

- there are some intervals without failures, consequently, failure rates are estimated as equal to 0,
- the cumulated operating time is different from one interval to another, this leads to the differences in confidence intervals for failure rates.

These particularities were taken into account during data analysis.

Failure on demand data (data set 2).

For these data time in operation means number of demands. Failure probability on demand calculated per equal bins. Each bin represents an interval of number of demands and it isn't equal to the same time periods in case of pulling different groups of components in the same sample.

These data have the same particularities as data set 1:

- there are some intervals without failures, consequently, failure probabilities are estimated as equal to 0,
- the cumulated number of demands is different from one interval to another, this leads to the differences in confidence intervals for failure probabilities.

These particularities were taken into account during data analysis.

3. Models and approach.

3.1 Models applied in case of data set 1.

For continuous time to failure (failure rate) variable it was proposed to apply following statistical models:

- 1. Constant failure rate : $\varphi(\vec{\theta};t)$ =Const;
- 2. Linear failure rate : $\varphi(\vec{\theta};t) = \theta_1 + \theta_2 t$;
- 3. Log-linear or exponential failure rate : $\ln \varphi(\vec{\theta};t) = \theta_1 + \theta_2 t$;

Nota: for this model all calculations were done supposing $\ln \varphi(\vec{\theta};t) = \ln(\theta_1) + \theta_2 t$. Estimated interception parameter "a" presented in the results, corresponds to θ_1 and not to $\theta_1^* = \ln \theta_1$. In these terms failure rate function is $\varphi(\vec{\theta};t) = \theta_1 \exp(\theta_2 t)$.

4. Power-low (Weibull) failure rate model : $\varphi(\vec{\theta};t) = \theta_1 t^{\theta_2}$

For models 2-4 the fact that parameter $\theta_2 > 0$ means positive trend in time, i.e. component failure rate increases with age of the component.

3.2 Models applied in case of data set 2

For discrete failures per demand the following models were applied:

- 1. Constant: $\varphi(\vec{\theta};t)$ =Const;
- 2. Logit: $\varphi(\vec{\theta};t) = \frac{\exp(\theta_1 + \theta_2 t)}{1 + \exp(\theta_1 + \theta_2 t)};$
- 3. Probit: $\varphi(\vec{\theta};t) = \Phi(\theta_1 + \theta_2 t)$;
- 4. Exponential: $\varphi(\vec{\theta};t) = \exp(\theta_1 + \theta_2 t)$,

Here $\Phi(x) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{x} \exp\left(-\frac{u^2}{2}\right) du$ - is a normal distribution function N(0;1).

3.3 Proposed approach

The applied approach is the same for continuously and discreetly distributed data. The difference is only with interpretation of "time" which is a time in operation for continuous functions and number of demands for discrete functions.

To choose the model, which better fits with observed data, first, the goodness of fit test was performed using Fisher's criterion χ^2 , then confidence limits for model parameters $\vec{\theta} = (\theta_1; \theta_2)$ and for resulting function $\varphi(\vec{\theta};t)$ were constructed.

To check the trend in failure rate (probability per demand) function, the hypothesis test was performed for selected model.

3.4 Goodness of fit test and parameters estimation

The hypothesis of a parametric model form describing the behaviour of a failure rate parameter in time t is tested with the help of Fisher's criterion χ^2 , the statistic of which is:

6

$$\chi^{2}(\vec{\theta}) = \sum_{i=1}^{s} \frac{\left[\nu(\Delta_{i}) - \varphi(\vec{\theta}; t_{i})T_{i}\right]^{2}}{\varphi(\vec{\theta}; t_{i})T_{i}}, \tag{1}$$

where $\varphi(\vec{\theta};t)$ is one of the fore functions proposed to describe the failure rate $\lambda(t)$.

Here

 $\Delta_1, \Delta_2, ..., \Delta_s$ is the selected X-axis division,

 $\nu(\Delta_i)$ is the number of failures per interval Δ_i ,

 T_i is the cumulated operating time of all components been in operation within the interval Δ_i .

The hypothesis to be tested is presented as follows:

$$H_0: \exists \vec{\theta}: \quad \lambda_i = \varphi(\vec{\theta}; t_i), \tag{2}$$

where λ_i is the averaged failure rate per interval Δ_i .

To calculate the statistic, an unknown value of $\vec{\theta}$ is substituted by an estimate $\vec{\theta}$ obtained using the method of minimum χ^2 :

$$\widehat{\vec{\theta}} = \arg\min_{\vec{\theta}} \chi^2(\vec{\theta}). \tag{3}$$

The criterion for testing a hypothesis of conformity is a simple comparison of p - value and a chosen confidence level α . Here, a p - value is calculated as:

$$p = \int_{z}^{\infty} f_{\chi_{s-r}^2}(t) dt, \qquad (4)$$

where

$$z=\chi^2\left(\widehat{\vec{\theta}}\right);$$

 $f_{\chi^2_{s-r}}(t)$ is the density of distribution χ^2 with s-r degrees of freedom,

s is the number of group intervals Δ_i (where $\nu(\Delta_i)$ should differ from 0),

r is the number of estimated parameters. For constant failure rate model (model 1 in 3.1 and 3.2) r = 1, for other proposed models (2 – 4 in 3.1 and 3.2) r = 2.

The hypothesis (2) is accepted in case, if $p > \alpha$, otherwise it is rejected. Besides, if the hypothesis (2) is accepted for several models, preference is to be given to the model with a greater p - value.

The method is described in various statistical books, for example in references [2-5].

The detailed procedure of parameters estimation and model verification by using EXEL software is provided in a file procedure.doc.

3.5 Parameters uncertainties

In case of two parameters model (models 2-4 in 3.1 and 3.2) the task of definition of confidence intervals for each of parameter is transformed in a task of definition of confidence areas.

When constructing the confidence areas the following statistic was used:

$$\chi^{2}(\vec{\theta}) = \sum_{i=1}^{s} \frac{\left[\nu(\Delta_{i}) - \varphi(\vec{\theta}; t_{i}) \cdot T_{i}\right]^{2}}{\varphi(\vec{\theta}; t_{i}) \cdot T_{i}}.$$

Let $1-\varepsilon$ be the confidence level of a confidence area. Solving the equation

$$\varepsilon = \int_{\mu_{\varepsilon}}^{\infty} f_{\chi_{s}^{2}}(t) dt$$

with a given ε value, determined is the parameter μ_{ε} .

Then a transcendental inequality was solved by numerical methods:

$$\chi^{2}(\vec{\theta}) = \sum_{i=1}^{s} T_{i} \frac{\left[\frac{\nu(\Delta_{i})}{T_{i}} - \varphi(\vec{\theta}; t_{i})\right]^{2}}{\varphi(\vec{\theta}; t_{i})} \leq \mu_{\varepsilon}.$$
 (5)

To construct the ellipsoids of concentration (confidence areas for $\vec{\theta}$), Compaq Visual Fortran Professional with a Graphor graphic package, or MatLab can be applied. Isolines are easily plotted in these packages.

3.6 Trend verification

As it was previously mentioned, for models 2-4 in chapters 3.1 and 3.2, the fact that parameter $\theta_2 > 0$ means positive trend in time, i.e. component failure rate or probability per demand increases with age of the component. A verification of presence of trend was done by formal hypothesis test presented below.

The null hypothesis (absence of trend) is defined as: H_0 : $\theta_2 = 0$

Alternative hypothesis is $H_1: \theta_2 > 0$

Test for hypothesis about θ_2 is intimately related to the confidence intervals for this parameter.

So, the hypothesis H_0 is rejected in favor of hypothesis H_1 at significance level ε if and only if the $100(1 - \varepsilon)\%$ confidence interval for θ_2 is entirely upper then zero.

The visual verification could be performed using confidence areas for $\vec{\theta}$ defined in chapter 3.5. Numerical solution to define a confidence interval is proposed below.

The χ^2 statistic with fixed parameter θ_1 could be used:

$$\chi^{2}\left(\widehat{\theta}_{1}, \theta_{2}\right) = \sum_{i=1}^{s} \frac{\left[\nu\left(\Delta_{i}\right) - \varphi\left(\widehat{\theta}_{1}, \theta_{2}; t_{i}\right) \cdot T_{i}\right]^{2}}{\varphi\left(\widehat{\theta}_{1}, \theta_{2}; t_{i}\right) \cdot T_{i}},\tag{6}$$

here $\hat{\theta}_1$ is the mean point estimation of θ_1 obtained by solving equation (3).

Then the same procedure as it is described in chapter 3.5 could be applied. Solving the equation

$$\varepsilon = \int_{u_{s}}^{\infty} f_{\chi_{s-1}^{2}}(t) dt$$

with a given $\,\mathcal{E}\,$ value, determined is the parameter $\,\mu_{\varepsilon}\,$.

It should be noted that the number of degrees of freedom has decreased by 1.

Then a transcendental inequality is solved by numerical methods:

$$\chi^{2}\left(\widehat{\theta}_{1}, \theta_{2}\right) = \sum_{i=1}^{s} T_{i} \frac{\left[\frac{\nu\left(\Delta_{i}\right)}{T_{i}} - \varphi\left(\widehat{\theta}_{1}, \theta_{2}; t_{i}\right)\right]^{2}}{\varphi\left(\widehat{\theta}_{1}, \theta_{2}; t_{i}\right)} \leq \mu_{\varepsilon}.$$
(7)

A solution of (7) is the confidence interval for parameter θ_2 : $(\underline{\theta}_2; \overline{\theta}_2)$. It should be stressed, that calculation of lower and upper bounds of confidence interval $(\underline{\theta}_2; \overline{\theta}_2)$ is possible, if p-level of point estimates $\vec{\theta}$ meets the condition: $p > \varepsilon$.

More detailed description of the numerical solution realized in EXEL is presented in file procedure.doc.

3.7 Model uncertainties and extrapolations

The following approach is applied to construct the confidence interval for a trend line. To construct the upper limit at moment *t* the extreme problem is solved

$$\varphi(\vec{\theta};t) \to \max_{\alpha}$$
, (8)

with the restriction

$$\chi^{2}\left(\vec{\theta}\right) = \sum_{i=1}^{s} T_{i} \frac{\left[\frac{\nu\left(\Delta_{i}\right)}{T_{i}} - \varphi\left(\vec{\theta}; t_{i}\right)\right]^{2}}{\varphi\left(\vec{\theta}; t_{i}\right)} \leq \mu_{\varepsilon}.$$

To construct the lower limit at time t the extreme problem is solved

$$\varphi(\vec{\theta};t) \to \min_{\vec{\theta}},$$
 (9)

with the restriction

$$\chi^{2}\left(\vec{\theta}\right) = \sum_{i=1}^{s} T_{i} \frac{\left[\frac{\nu\left(\Delta_{i}\right)}{T_{i}} - \varphi\left(\vec{\theta}; t_{i}\right)\right]^{2}}{\varphi\left(\vec{\theta}; t_{i}\right)} \leq \mu_{\varepsilon}.$$

As soon as chosen trend φ functions have no local extreme points, restrictions of the inequality type can be substituted by the following equality:

$$\chi^{2}(\vec{\theta}) = \sum_{i=1}^{s} T_{i} \frac{\left[\frac{\nu(\Delta_{i})}{T_{i}} - \varphi(\vec{\theta}; t_{i})\right]^{2}}{\varphi(\vec{\theta}; t_{i})} = \mu_{\varepsilon},$$

since the solution will be inside of confidence ellipse area.

4. Results of calculations

4.1 Presentation of the results

Data set 1.

In case of continuous distributions the results of goodness-of-fit test (fitted model parameters $\vec{\theta} = (\theta_1; \theta_2)$ and p-values) are presented in a Table 1.

More detailed presentation of the results is provided in Annex 3 and in the EXEL files: $CS2006_2_TA1_F1$, $CS2006_2_TA2_F1$, $CS2006_2_TA3_F1$, $CS2006_2_TA4_F1$.

The graphical interpretation of parameters and models uncertainties are provided in Annex 5.

Table 1. Summary of parameters estimation for data set 1.

Component	Parameters		Comments			
group	1 drumeters	Constant	Linear	Log-linear	Weibull	Comments
	Θ_1	0.030	0.012	0.015	0.013	31 116
#3	$ heta_2$		0.0017	0.0637	0.0017	No model fit with the data
	p-value	0.002	0.006	0.006	0.003	Will the data
	Θ_1	0.023	0.014	0.013	0.014	31 116
#6	$ heta_2$		0.0010	0.0539	0.2179	No model fit with the data
	p-value	0	0	0	0	uro anu

Component			Models				
group	Parameters	Constant	Linear	Log-linear	Weibull	Comments	
	Θ_1	0.029	0.017	0.018	0.016		
#6.1	$ heta_2$		0.0011	0.0415	0.2697	No model fit with the data	
	p-value	0.006	0.014	0.015	0.012	with the data	
	θ_1	0.019	0.010	0.011	0.009	Log-linear fits	
#7	$ heta_2$		0.0010	0.0546	0.3414	the best (slow	
	p-value	0.019	0.542	0.567	0.360	ageing)	
	Θ_1	0.019	0.004	0.007	0.003	Log-linear fits	
#7.1	θ_2		0.0012	0.0792	0.7255	the best (slow	
	p-value	0.041	0.429	0.492	0.365	ageing)	
	Θ_1	0.015	0.011	0.012	0.007	Weibull fits the	
#8.1	Θ_2		0.0004	0.0161	0.3073	best (slow	
	p-value	0.057	0.051	0.046	0.100	ageing)	
	Θ_1	0.021	0.009	0.012	0.006	Weibull fits the	
#11.1	$ heta_2$		0.0012	0.0503	0.5482	best (slow	
	p-value	0.203	0.278	0.271	0.303	ageing)	
	Θ_1	0.003	0.001	0.002	0.001	All models fit the	
#13.3	$ heta_2$		0.0002	0.0426	0.4667	data, but Weibull fits the best	
	p-value	0.748	0.762	0.728	0.793		
	Θ_1	0.00028	0.00035	0.00034	0.00028	All models fit the data, but const.	
#14.1	θ_2		-0.00001	-0.02360	0.00001	fits the best (no	
	p-value	0.967	0.938	0.934	0.926	ageing)	
	Θ_1	0,000	0,000	0,000	0,001	All models fit the	
#16.2	Θ_2		0,0000	-0,0670	-0,3802	data (no ageing)	
	p-value	0,923	0,995	0,987	0,948	(2 2)	
	Θ_1	0.002	0.003	0.003	0.003		
#17.1	$ heta_2$		-0.0001	-0.0880	-0.3929	All models fit the data (no ageing)	
	p-value	0.912	0.976	0.962	0.920	data (no agemg)	
	θ_1	0.039	0.061	0.071	0.081	W. 7. 11.0° 4	
#19.1	$ heta_2$		-0.0030	-0.0914	-0.4775	Weibull fits the best (no ageing)	
	p-value	0.493	0.669	0.704	0.873	*****(
	Θ_1	0.045	0.073	0.158	0.311		
#30.1	Θ_2		-0.0023	-0.0992	-0.7772	No ageing	
	p-value	0.023	0.102	0.108	0.045		
	Θ_1	0.005	0.004	0.004	0.004	All models fit the	
#32.2	Θ_2		0.0002	0.0333	0.1223	data, but const. fits the best	
	p-value	0.543	0.534	0.532	0.489		
	Θ_1	0,025	0,021	0,020	0,022	All models fit the	
#34.1	Θ_2		0,0003	0,0148	0,0379	data, but const.	
	p-value	0,807	0,773	0,778	0,758	fits the best	
	Θ_1	0,055	0,024	0,024	0,024	Log-linear fits	
#35.1	θ_2	,	0,0027	0,0704	0,3551	the best (slow	
	p-value	0,008	0,079	0,148	0,028	ageing)	
	Θ_1	0,094	0,122	0,121	0,120		
#36.2	θ_2	0,074			-	No ageing	
- 	p-value	0.220	-0,0023	-0,0213	-0,1020		
#20 1	-	0,229	0,242	0,232	0,194	Log linear fits	
#38.1	Θ_1	0,006	0,003	0,003	0,003	Log-linear fits	

Component		Models								
group	Parameters	Constant	Linear	Log-linear	Weibull	Comments				
	θ_2		0,0002	0,0487	0,2676	the best (slow				
	p-value	0,437	0,495	0,519	0,424	ageing)				
	Θ_1	0,067	0,006	0,013	0,005	No model fit				
#39.1	Θ_2		0,0045	0,1099	0,9965	with the data				
	p-value	0,001	0,023	0,071	0,021	with the data				
	Θ_1	0,020	0,009	0,010	0,008	Log-linear fits				
#43.1@	$ heta_2$,	0,0013	0,0761	0,4249	the best (slow				
	p-value	0,893	0,906	0,911	0,890	ageing)				
	Θ_1	0,001	0,002	0,002	0,002					
#44.1	$ heta_2$,	-0,0001	-0,1251	-0,4689	No ageing				
	p-value	0,298	0,761	0,663	0,360					
	θ_1	0,008	0,011	0,013	0,017					
#45@	θ_2	,	-0,0003	-0,0522	-0,4009	No ageing				
	p-value	0,862	0,923	0,946	0,954					
	Θ_1	0,006	0,003	0,002	0,004	Log-linear fits				
#47.1	$ heta_2$	0,000	0,0003	0,0817	0,2051	the best (slow				
	p-value	0,112	0,150	0,214	0,085	ageing)				
	Θ_1	0,001	0,001	0,001	0,003					
#48.2	$ heta_2$	0,001	0,0000	-0,0433	-0,5343	No ageing				
	p-value	0,189	0,112	0,184	0,362					
	Θ_1	0,001	0,002	0,002	0,004					
#48.3	$ heta_2$	0,001	-0,0001	-0,0716	-0,6499	No ageing				
	p-value	0,045	0,074	0,116	0,543					
	Θ_1	0,001	0,001	0,001	0,001					
#49.5	$ heta_2$	0,001	0,0000	-0,0176	0,0592	No ageing				
	p-value	0,810	0,728	0,721	0,714					
	Θ_1	0,011	0,010	0,010	0,010					
#50	$ heta_2$	0,011	0,0001	0,0125	0,0693	No ageing				
	p-value	0,828	0,727	0,727	0,725					
	Θ_1	0,025	0,006	0,006	0,004					
#55	$ heta_2$	0,005	-0,0001	-0,0073	0,1833	No ageing				
	p-value	0,422	0,294	0,293	0,305					
	Θ_1	0,021	0,029	0,026	0,015					
#56	$ heta_2$	0,021	-0,0007	-0,0164	0,1504	No ageing				
	p-value	0,176	0,137	0,131	0,130					
	Θ_1	0,021	0,022	0,022	0,022					
#56.1	$ heta_2$	0,021	-0,0001	-0,0058	-0,0206	No ageing				
	p-value	0,889	0,853	0,853	0,851					
	Θ_1	0,029	0,026	0,026	0,031					
#57	$ heta_2$	0,027	0,002	0,020	-0,0167	No ageing				
	p-value	0,902	0,864	0,865	0,861	2 3				
#58	θ_1	0,902 0,017	0,864	0,863	0,881	No ageing				
	θ_2	0,017	-0,0007	-0,0499	-0,3202	5 5				
	- 2		-0,000/	-U,U 4 33	-0,3202					

Component	Parameters		Comments			
group	ratameters	Constant	Linear	Log-linear	Weibull	Comments
	p-value	0,666	0,694	0,702	0,723	
	Θ_1	0,057	0,012	0,017	0,008	Log-linear fits
#59.1	Θ_2		0,0030	0,0782	0,7312	the best (slow
	p-value	0,257	0,482	0,561	0,438	ageing)
	Θ_1	0,151	0,059	0,066	0,039	Log-linear fits
#59.1@WR	Θ_2		0,0068	0,0575	0,5348	the best (slow
	p-value	0,031	0,138	0,187	0,113	ageing)
	Θ_1	0,052	0,037	0,037	0,034	Log-linear fits
#62.2	θ_2		0,0015	0,0326	0,1923	the best (slow
	p-value	0,854	0,859	0,864	0,844	ageing)
	Θ_1	0,002	0,003	0,003	0,004	
#63.1	θ_2		-0,0001	-0,0479	-0,3450	No ageing
	p-value	0,778	0,742	0,741	0,759	
	Θ_1	0.046	0.075	0.104	0.116	Log-linear fits
#65	Θ_2		-0.0027	-0.0830	-0.4365	the best (no
	p-value	0.005	0.458	0.539	0.073	ageing)

Data set 2.

For the discrete data the results of parameters estimation and goodness-of-fit test are presented in a Table 2. Detailed presentation is provided in Annex 4 and correspondent EXEL file: CS2006_2_DS2_ABC_DEF. The graphical interpretation of uncertainties is given in Annex 6. The presented cases are those where initial data contains more than 10 failures per component group. For other groups the results could be found in EXEL file CS2006_2_DS2_R01.

Table 2. Summary of parameters estimation for data set 2.

Component	Parameters		Models					
group	rarameters	Constant	Logit	Probit	Exponential	Comments		
	Θ_1	0.003	-5.63	-2.69	-5.63	G		
U_C	θ_2		-5.16E-04	-1.71E-04	-5.13E-04	Constant model fits the best		
	p-value	0.26	0.15	0.15	0.15	into the oest		
	θ_1	0.004	-3.88	-2.08	-3.88			
U_D	θ_2		-8.11E-03	-2.78E-03	-8.11E-03	Decreasing trend (no ageing)		
	p-value	0.09	0.67	0.68	0.67			
	Θ_1	0.0018	-5.50	-2.66	-5.50			
U_F	θ_2		-1.19E-03	-3.60E-04	-1.19E-03	Decreasing trend (no ageing)		
	p-value	0.57	0.89	0.88	0.89	(no ugenig)		
	Θ_1	1.46E-05	-11.01	-4.15	-11.00	N. 116.		
ABC	θ_2		-2.38E-05	-5.30E-06	-2.38E-05	No model fits with the data		
	p-value	0.03	0.05	0.05	0.05	William and autu		
	Θ_1	0.00013	-8.54	-3.55	-8.54	D :		
DEF	θ_2		-0.00084	-0.00021	-0.00084	Decreasing trend (no ageing)		
	p-value	0.53	0.86	0.86	0.86	(88)		

4.2. Results analysis and interpretation

4.2.1. Identification of component susceptible to ageing

Analysis of results could be performed in three stages:

- on the first stage, the component groups for which one or more proposed models fit well with the data could be selected. It was decided to consider all models where p-value is more then 0,1.
- secondly, component groups for which best fitted model shows negative "ageing" parameter $(\theta_2 < 0)$ could be ignored for following assessment,
- then, component groups with positive ageing trends could be identified by comparing the "ageing" parameter (θ_2) and its confidence intervals with zero. In case if the lower bound of 90% confidence interval for "ageing" parameter θ_2 is above 0, the ageing trend could be assumed.

The confidence intervals for "ageing" parameter were calculated as it is described in chapter 3.6. Annex 7 represents the results of calculations. The following paragraphs present the results of the screening.

Data set 1.

The results of the screening show that from 37 component groups from Data Set 1 the positive ageing trend could be assumed for 10 component groups listed below:

- #7 (best fitted model is log-linear with $\theta_2 = 0.055$),
- #7.1 (best fitted model is log-linear with $\theta_2 = 0.079$),
- #8.1 (best fitted model is Weibull, p = 0.1, with θ_2 = 0.31),
- #11.1 (best fitted model is Weibull with $\theta_2 = 0.55$),
- #13.3 (best fitted model is Weibull with $\theta_2 = 0.47$),
- #35.1 (best fitted model is log-linear, p=0.15, with $\theta_2 = 0.07$),
- #38.1 (best fitted model is log-linear with $\theta_2 = 0.049$),
- #47.1 (best fitted model is log-linear with $\theta_2 = 0.082$),
- #59.1 (best fitted model is log-linear with $\theta_2 = 0.078$),
- #59.1@WR (best fitted model is log-linear with $\theta_2 = 0.057$).

For 2 component groups log-liner model with positive ageing parameter was identified as well fitted, but the value of 90% low bound of "ageing" parameter is below zero.

- #43.1 (best fitted model is log-linear with $\theta_2 = 0.076$),
- #62.2 (best fitted model is log-linear with $\theta_2 = 0.033$).

For following 10 component groups the best fitted model is constant: #14.1, #32.2, #34.1, #49.5, #50, #55, #56, #56.1, #57, #63.1.

For the rest 16 component groups the situations are as following: even no model fits with the data, i.e. p-value is very small (for example, component groups #3, #6, #6.1, etc.), or negative "ageing" parameter are obtained (see for example, #17.1, #19.1, #30.1, etc.).

For better understanding of obtained results and importance of ageing trends, relative increasing in failure rate in time with regard to constant failure rate are presented in Table 3.

Table 3. Failure rate increasing.

Component group	Best fitted model	Parameters : θ_1 θ_2	φ=с	φ (θ, 10) / φ=c	$\varphi (\theta, 20) / \varphi = c$	$\varphi (\theta, 30) / \varphi = c$
#7	log- linear	0.011 0.0546	0.019	0.58	1.73	2.98
#7.1	log- linear	$0.007 \\ 0.0792$	0.019	0.37	1.80	3.96
#8.1	Weibull	0.007 0.3073	0.015	0.95	1.17	1.33
#11.1	Weibull	0.006 0.5482	0.021	1.01	1.48	1.84
#13.3	Weibull	0.001 0.4667	0.003	0.98	1.35	1.63
#35.1	log- linear	$0.024 \\ 0.0704$	0.055	0.44	1.78	3.61
#59.1@	log- linear	0.066 0.0575	0.151	0.44	1.38	2.45

These figures show that application of constant failure rate model could provide underestimated unavailability values in case of aged NPPs. The interception point of constant and time-dependent failure rates corresponds to the plant ages between 10 and 20 years. Taking into account the delay between data collection, parameters estimation and PSA update it could lead to underestimation in final PSA results.

In presented data examples the data collection covers the ages window between 0 and 20 years in operation. Now, if 10 years periodicity of PSA update will be assumed and for the 30-years examination this data set will be applied, the underestimate of failure rates could rise up to the factor 4 (see $\varphi(\theta, 30) / \varphi = c$ for component group #7.1, for example).

Of cause, it is true in case if the trend will continue in time.

Data set 2.

There are no component groups in this data set, which show increasing trend of failure rate. The following analysis does not include the examples from data set 2, but the main conclusions of the analysis provided in chapter 4.2.7 could be valid for discrete data as well.

4.2.2. Comparison with results of non-parametric inversion test

A non-parametric inversion test was performed for most of component groups. As a result increasing failure rates were identified for component groups: #3, #6, #6.1, #7, #11.1, #39.1, #43.1, #45, #47.1, #50.1, #56, #58, #62.2.

For component groups #7, #7.1, #11.1, #43.1, #47.1 and #62.2 conclusions of inversion test were confirmed by parametrical modeling. The results of goodness of fit test for component groups #3, #6, #6.1 and #39.1 show that no model fit with the data. For the rest cases parametrical models do not confirm the ageing trend.

From the other hand, inversion test does not identify ageing trends in case of #8.1, #13.3, #35.1, #38.1, #59.1 and #59.1@. This again shows the weakness of non-parametrical tests and the necessity to apply different methods for ageing detection.

4.2.3. Impact of burn-in failures

Visual examination of data permits to suppose existence of burn-in failures for certain component groups, for example: #3, #6, #6.1, #7.1, #32.2, #35.1, #38.1, 39.1, #45@, #48.2, #48.3.

Additional examination was done for these component groups by excluding first intervals from data sets.

The results for groups #3, #6, #6.1 show an increase of "ageing" parameter, but p-value still resides very low.

Results of calculation for other component groups are presented in Table 4.

Table 4. Impact of burn-in failures.

Component group	Best fitted model	Parameters : θ_1 θ_2 p-value	φ=с	φ (θ, 10) / φ=c	$\phi \left(\theta ,20\right) /\phi =c$	φ (θ, 30) / φ=c
#7.1	log- linear	0.007 0.0792 0.49	0.019	0.81	1.80	3.96
#7.1 /burn- in failures excluded	linear	0.0014 0.0015 0.47	0.019	0.86	1.65	2.44
#32.2	const	0.005 0.54	0.005	1	1	1
#32.2 /burn-in failures excluded	Weibull	0.0018 0.49 0.65	0.005	1.11	1.56	1.91
#35.1	log- linear	0.024 0.0704 0.15	0.055	0.88	1.78	3.61
#35.1/burn- in failures excluded	log- linear	0.015 0.1 0.35	0.054	0.76	2.05	5.58
#38.1	log- linear	0.0032 0.049 0.52	0.006	0.53	1.42	2.32
#38.1/burn- in failures excluded	Weibull	0.00024 1.22 0.58	0.006	0.66	1.55	2.54
#39.1	log- linear	0.013 0.11 0.07	0.067	0.58	1.75	5.26
#39.1/burn- in failures excluded	Log- linear	0.0032 0.18 0.14	0.075	0.26	1.56	9.45
#45.@	Weibull	0.017 -0.40 0.954	0.078	0.87	0.66	0.56
#45@/burn-	Log-	0.00031	0.0048	0.68	1.30	1.92

in failures excluded	linear	2.97E-04 0.999				
#48.2	Weibull	0.017 -0.40 0.36	0.078	0.87	0.66	0.56
#48.2/burn- in failures excluded	Const	0.00068	0.00068	1	1	1
#48.3	Weibull	0.0035 -0.65 0.54	0.0011	0.72	0.46	0.35
#48.3/burn- in failures excluded	Log- liner	0.00021 0.081 0.997	0.00064	0.74	1.66	3.74

Consideration of burn-in failures could improve the result of goodness of fit test, as for example in case of group #39.1, which was initially excluded from the screening because of very small p-value. Results of additional examination permit to conclude about the existence of ageing trend for this component group.

Consideration of burn-in failures (excluding them from data) could change the conclusion about existence or absence of ageing trend, as for example in case of groups #32.2, #45@, #48.2 and #48.3. Three of these groups (#32.2, #45@, #48.3) could be added to the list of components with identified ageing trend.

For group #32.2 the conclusion of first calculation was that failure rate is *constant* with significance level 0.54 but all others models also fitted quite well. Neglecting of burn-in failures leads to the conclusion that *Weibull* model fits the best (p-value = 0.64) but the constant failure rate still fits good with p-value = 0.51. Choice of constant failure rate model could lead to underestimation of unavailability for 30-years aged component by factor 1,9 ($\varphi(\theta, 30)/\varphi$ =const.) in comparison with Weibull model.

In case of component group #48.3 where conclusion from the first examination is an existence of *decreasing trend* (i.e. reliability of component is increasing with time), the consideration of burn-in failures changed the conclusion to opposite one: i.e. existence of *increasing trend*.

In some cases the burn-in failures do not impact a lot to the time-dependent models extrapolations, so the calculated failure rate values are close to each other.

An example is the group #38.1. Here, analysis of complete data set provides best fitted log-linear model with significance level 0.52. Excluding burn-in failures from the analysis gives a conclusion that Weibull fits the best with significance level 0.58. Comparison of failure rate extrapolations up to the age of 30 years for both of these models with constant failure rate (which is the same in both of the cases) provides about the same level of underestimation: 2.32 in case of complete sample and 2.54 in case where the burn-in failures neglected.

In one case, group #39.1, the excluding of burn-in failures has led to increasing in failure rate by order of magnitude in comparison with constant failure rate value.

All those examples show the importance of consideration of burn-in failures in the ageing assessment.

4.2.4. Comparison with other parametrical methods

The results of the calculations were compared with estimations by other parametrical methods in the frame of Ageing PSA Task Group 4 activities.

As the alternative methods the Bayesian analysis with non informative priors and Stochastic Expectation Maximization were chosen.

In case of Bayesian analysis the same sets of binned data were analyzed.

To check the validity of the model, it was used the posterior predictive distribution for the number of failures in each bin to compare observed and replicated chi-square statistics. The overlap probability, is referred to here as a Bayesian p-value.

Analysis was done by free-available software WinBUGS [6].

The calculations were performed for two component groups #3 and #7.1. The results of calculation are presented in Table 5.

Table 5. Comparative parameters estimation (frequentist vs Bayesian).

Component	Parameters		Comments			
group	rarameters	Constant	Linear	Log-linear	Weibull	Comments
#10	Θ_1	0.030	0.012	0.015	0.013	27 116
#3 Chi-2 min.	Θ_2		0.0017	0.0637	0.0017	No model fit with the data
Ciii 2 iiiii.	p-value	0.002	0.006	0.006	0.003	with the data
442	Θ_1	0.023	0.007	0.01	0.007	
#3 Bayesian	Θ_2		0.002	0.07	0.62	No model fit with the data
Buyesian	p-value	0.004	0.01	0.01	0.007	with the data
	Θ_1	0.019	0.004	0.007	0.003	
#5.1	θ_2		0.0012	0.0792	0.7255	Log-linear fits
#7.1 Chi-2 min.	θ_2 90% conf.		(8.8E-4,	(0.059,	(0.63, 0.82)	the best (slow
	interval		0.0017)	0.099)	(0.03, 0.82)	ageing)
	p-value	0.041	0.429	0.492	0.365	
	Θ_1	0.017	0.004	0.007	0.003	
<i>47.</i> 1	Θ_2		0.001	0.079	0.814	Log-linear fits
#7.1 Bayesian	θ_2 90% conf. interval		(7.0E-4, 0.002)	(0.04, 0.12)	(0.41, 1.27)	the best (slow ageing)
	p-value	0.046	0.41	0.47	0.33	

In case of component group #3 the Bayesian analysis leads to the same conclusion as a frequentist one that no model fit with the data (for all models the p-value is very small). That could be the reason of slight difference in parameters estimation.

Comparison of the results for group #7.1 shows that Bayesian approach with non informative priors provides numerical results similar (or very close) to frequentist analysis: the calculated model parameters for best fitted models (linear and non-linear) are the same and the p-values are very close to each other. The 90% confidence interval is a little bit more tight in case of frequentist analysis, but still comparative with figures provided by Bayesian estimation.

Stochastic Expectation Maximization (SEM) [7] method was applied for the times to failure data, which were used to develop initial data sets from Annex 1. The SEM algorithm was realized only for Weibull model parameters estimation and has some limits from application point of view. The algorithm provides the point estimations only.

The comparison was done for three component groups: #8.1, #11.1 and 13.3. For these groups the goodness of fit test identified the Weibull as best fitted model. The results of the calculations are presented in Table 6.

In all three cases the SEM provides more conservative estimation of "ageing" parameter. As a consequence, the extrapolated values of failure rates are much higher. For example in case of component group #13.3, the "ageing" parameter estimated by SEM more then twice higher of those estimated with Chi-2 minimization approach.

One possible explanation of this difference is that times to failure data are more informative that binned one. But more detailed investigation of this issue is necessary.

Table 6. Comparative parameters estimation (Chi-2 min. vs SEM).

Component group	Best fitted model	Parameters : θ_1 θ_2	ф=с	φ (θ, 10) / φ=c	$\phi \left(\theta ,20\right) /\phi =c$	φ (θ, 30) / φ=c
#8.1 Chi-2	Weibull	0.007 0.31	0.015	0.95	1.17	1.33
#8.1 SEM	Weibull	0.0059 0.43	0.015	1.06	1.43	1.70
#11.1 Chi-2	Weibull	0.006 0.55	0.021	1.01	1.48	1.84
#11.1 SEM	Weibull	0.0023 0.92	0.021	0.91	1.72	2.50
#13.3 Chi-2	Weibull	0.001 0.47	0.003	0.98	1.35	1.63
#13.3 SEM	Weibull	0.00025 1.12	0.003	1.10	2.39	3.76

4.2.5. Uncertainties of extrapolation.

To apply developed time dependent reliability models in PSA it is necessary to perform some predictive estimation of failure rates. Uncertainties of predictive extrapolations and impact of the choice of the model to extrapolation results were analyzed in the frame of the study. The Annex 5 provides a graphical interpretation of parameters and models uncertainties.

Table 7 presents the results of relative increase of extrapolated failure rate with regards to constant failure rate model.

Table 7. Failure rate extrapolations with different time dependent models.

Component group	Fitted model	Parameters :				
		Θ_1	$\varphi = c$	$\varphi(\theta, 10) / \varphi = c$	$\varphi(\theta, 20)/\varphi = c$	$\varphi(\theta, 30) / \varphi = c$
		Θ_2				
		p-value				
		0.004				
#7.1	linear	0.0012	0.019	0.84	1.47	2.11
		0.43				
47 1	log-	0.007	0.010	0.27	1.00	2.06
	linear	0.0792 0.49	0.019	0.37	1.80	3.96
		0.49				
#7.1	Weibull	0.003	0.019	0.85	1.41	1.89
// / · I	Welloun	0.73	0.01)	0.03	1.11	1.07
		0.009				
#43.1	linear	0.0013	0.02	1.10	1.75	2.40
		0.906				
	log-	0.01				
#43.1	linear	0.076	0.02	1.07	2.29	4.89
		0.911				
#43.1	Weibull	0.008	0.02	1.08	1.45	1.73
		0.43				

		0.89				
#38.1	linear	-0.0010 0.0005	0.006	0.69	1.54	2.39
		0.58				
#38.1	log- linear	0.00150 0.092 0.53	0.006	0.63	1.57	3.95
#38.1	Weibull	0.00024 1.22 0.58	0.006	0.66	1.55	2.54

Comparison of results of extrapolation leads to the conclusion that in all of the cases the most conservative estimation is provided by log-linear model.

This is an important observation. The p-values (used here as a criteria for choice of the model) are quite close in all presented cases, but the extrapolated up to the 30-years age failure rates are different. For example in case of component group #43.1 the difference in estimation using log-linear and linear model is more then of factor 2. If log-linear calculation is compared with result of Weibull model the difference rises up to the factor 2.8.

From the other side, log-linear model provides more uncertain extrapolations. This is shown in the Figures 1-6.

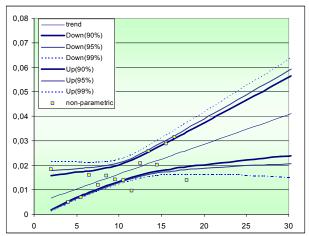


Figure 1. Component group #7.1 – linear extrapolation.

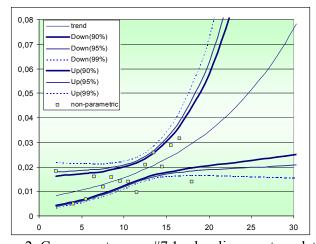


Figure 2. Component group #7.1 – log-linear extrapolation.

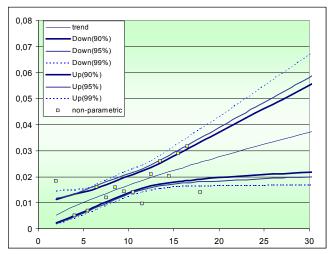


Figure 3. Component group #7.1 – Weibull extrapolation.

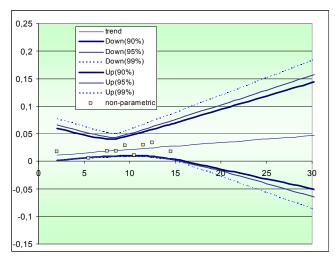


Figure 4. Component group #43.1 – linear extrapolation.

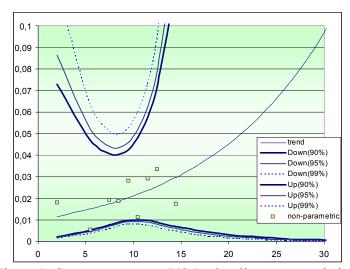


Figure 5. Component group #43.1 – log-linear extrapolation.

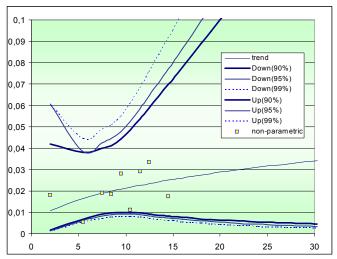


Figure 6. Component group #43.1 – Weibull extrapolation.

The following issues are open and have to be discussed:

- what model to chose for extrapolation if several time-dependent models fit well with the data,
- how to take into account the extrapolation uncertainties when introduce parameters into PSA model,
- and, what are the ways to reduce the uncertainties.

5. Conclusions and recommendations

- 1) Proposed approach permitted to identify the component groups with increasing failure rate and to choose best fitted reliability model. The following 10 component groups were identified as susceptible for ageing:
 - #7 (best fitted model is log-linear with $\theta_2 = 0.055$),
 - #7.1 (best fitted model is log-linear with $\theta_2 = 0.079$),
 - #8.1 (best fitted model is Weibull, p = 0.1, with $\theta_2 = 0.31$),
 - #11.1 (best fitted model is Weibull with $\theta_2 = 0.55$),
 - #13.3 (best fitted model is Weibull with $\theta_2 = 0.47$),
 - #35.1 (best fitted model is log-linear, p=0.15, with $\theta_2 = 0.07$),
 - #38.1 (best fitted model is log-linear with $\theta_2 = 0.049$),
 - #47.1 (best fitted model is log-linear with $\theta_2 = 0.082$),
 - #59.1 (best fitted model is log-linear with $\theta_2 = 0.078$),
 - #59.1@WR (best fitted model is log-linear with $\theta_2 = 0.057$).
- 2) In addition, for 2 component groups log-liner model with positive ageing parameter was identified as well fitted, but the value of 90% low bound of "ageing" parameter is below zero:
 - #43.1 (best fitted model is log-linear with $\theta_2 = 0.076$),
 - #62.2 (best fitted model is log-linear with $\theta_2 = 0.033$).
- 3) Examination of the impact of burn-in failures provided fore additional groups to the list of components susceptible for ageing :
 - #32.2 (best fitted model is Weibull with $\theta_2 = 0.46$),
 - #39.1 (best fitted model is log-linear with $\theta_2 = 0.18$),
 - #45@ (best fitted model is log-linear with $\theta_2 = 0.0003$),
 - #48.3 (best fitted model is log-linear with $\theta_2 = 0.081$).

For these gropes 90% confidence intervals for estimated parameters were not examined.

- 4) Consideration of burn-in failures could improve the result of goodness of fit test, as for example in case of group #39.1, and could change the conclusion about existence or absence of ageing trend, as for example in case of groups #32.2, #45@, #48.2 and #48.3.
- 5) The results of the calculations were compared with estimations by other parametrical methods: Bayesian analysis with non informative priors and Stochastic Expectation Maximization (SEM). Bayesian analysis was performed with the same representation of data, i.e. binned data, when SEM calculations were done by using times to failure type data. Bayesian approach with non informative priors provides numerical results similar (or very closes) to those obtained by frequentist analysis.
- 6) The SEM algorithm applied for times to falure type data provides more conservative estimation of "ageing" parameter. As a consequence, the extrapolated values of failure rates are much higher of those estimated with Chi-2 minimization approach.

 One possible explanation of this difference is that times to failure data are more informative that binned one. But more detailed investigation of this issue is necessary.
- 7) The impact of the choice of the model to extrapolation results were analyzed. Comparison of results of extrapolation leads to the conclusion that in all of the examined cases the most conservative estimation is provided by log-linear model.

 From the other side, log-linear model provides more uncertain extrapolations.
- Trom the other side, log iniear moder provides more uncertain extrapolations.
- 8) With regards to extrapolation of failure rate functions the following issues are open and have to be discussed:
 - what model to chose for extrapolation if several time-dependent models fit well with the data,
 - how to take into account the extrapolation uncertainties when introduce parameters into PSA model,
 - and, what are the ways to reduce the uncertainties.

References

- [1] C. Atwood, O. Cronval, M. Patrik, A. Rodionov. Models and data used for assessing the ageing of systems, structures and components (European Network on Use of Probabilistic Safety Assessment (PSA) for Evaluation of Ageing Effects to the Safety of Energy Facilities). EUR 22483 EN, EC DG JRC Institute for Energy, Petten, 2007.
- [2] Cramer H. Mathematical methods of statistics, Princeton Univ. Press, Princeton, N.-Y. 1946.
- [3] Bickel P., Doksum K. Mathematical Statistics. Basic Ideas and Selected Topics. V.1 New Jersey. 2001.
- [4] Kendall M. G., Stuart A. The Advanced Theory of Statistics, V.2, Charles Griffin and Co., London, N.-Y. 1961.
- [5] Rao C. Linear Statistical Inference and Its Applications. John Wiley and Sons, N.-Y. 1973.
- [6] WinBUGs Bayesian inference Using Gibbs Sampling software. http://www.mrc-bsu.cam.ac.uk/bugs/welcome.shtml
- [7] Bacha M, Celeux G, Idée E, Lannoy A. & Vasseur D : Estimation de modèles de durées de vie fortement censurées. Eyrolles 1998.

List of figures				
Figure 1. Component group #7.1 – linear extrapolation.	19			
Figure 2. Component group #7.1 – log-linear extrapolation.				
Figure 3. Component group #7.1 – Weibull extrapolation.	20			
Figure 4. Component group #43.1 – linear extrapolation.	20			
Figure 5. Component group #43.1 – log-linear extrapolation.	20			
Figure 6. Component group #43.1 – Weibull extrapolation.	21			
List of tables				
Table 1. Summary of parameters estimation for data set 1.	9			
Table 2. Summary of parameters estimation for data set 2.	12			
Table 3. Failure rate increasing.	14			
Table 4. Impact of burn-in failures.	15			
Table 5. Comparative parameters estimation (frequentist vs Bayesian).	17			
Table 6. Comparative parameters estimation (Chi-2 min. vs SEM).	18			
Table 7. Failure rate extrapolations with different time dependent models.	18			

European Commission

EUR 23079 EN - Joint Research Centre - Institute for Energy

Title: A Case Study on Investigation of Component Age Dependent Reliability Models. EC JRC Network on Use of Probabilistic Safety Assessments (PSA) for Evaluation of Aging Effects to the Safety of Energy Facilities. Task 4.

Author(s): A.Antonov, V.Chepurko, A.Polyakov, A.Rodionov Luxembourg: Office for Official Publications of the European Communities 2008 – 213 pp. – 21 x 29.7 cm EUR – Scientific and Technical Research series – ISSN 1018-5593

Abstract

The report presents the results of a case study on "Investigation of component age dependent reliability models" implemented by INPE and JRC IE in the frame of EC JRC Ageing PSA Network Task 4 activities. Several cases of Generalized Linear Model were proposed and investigated for the cases of continues and discrete data. The Fisher Chi-2 minimization approach was applied for goodness of fit test and parameters elaboration. Finally, uncertainty analysis was done for estimated parameters and model extrapolations. The results were analyzed and compared with other approaches.

The mission of the JRC is to provide customer-driven scientific and technical support for the conception, development, implementation and monitoring of EU policies. As a service of the European Commission, the JRC functions as a reference centre of science and technology for the Union. Close to the policy-making process, it serves the common interest of the Member States, while being independent of special interests, whether private or national.



Bar code

