



<b>Title</b>	<b>A molecular line survey of the extreme carbon star crl3068 at millimeter wavelengths</b>
<b>Author(s)</b>	<b>Zhang, Y; Kwok, S; Nakashima, JI</b>
<b>Citation</b>	<b>The Astrophysical Journal, 2009, v. 700 n. 2, p. 1262-1281</b>
<b>Issued Date</b>	<b>2009</b>
<b>URL</b>	<b><a href="http://hdl.handle.net/10722/179717">http://hdl.handle.net/10722/179717</a></b>
<b>Rights</b>	<b>Creative Commons: Attribution 3.0 Hong Kong License</b>

## A MOLECULAR LINE SURVEY OF THE EXTREME CARBON STAR CRL 3068 AT MILLIMETER WAVELENGTHS

YONG ZHANG, SUN KWOK, AND JUN-ICHI NAKASHIMA

Department of Physics, University of Hong Kong, Pokfulam, Hong Kong; zhangy96@hku.hk, sunkwok@hku.hk, junichi@hku.hk  
Received 2009 January 22; accepted 2009 May 28; published 2009 July 13

### ABSTRACT

We present the results of a molecular line survey of the extreme carbon star CRL 3068. The observations were carried out with the Arizona Radio Observatory (ARO) 12 m telescope and the Heinrich Hertz Submillimeter Telescope (SMT) at the  $\lambda$  2 mm and  $\lambda$  1.3 mm atmospheric windows. The observations cover the frequency bands from 130 to 162 GHz and 219.5 to 267.5 GHz. The typical sensitivities achieved are  $T_R < 15$  mK and  $T_R < 7$  mK for the ARO 12 m and SMT, respectively. Seventy-two individual emission features belonging to 23 molecular species and isotopologues were detected. Only three faint lines remain unidentified. The species  $c$ -C<sub>3</sub>H, CH<sub>3</sub>CN, SiC<sub>2</sub>, and the isotopologues, C<sup>17</sup>O, C<sup>18</sup>O, HC<sup>15</sup>N, HN<sup>13</sup>C, C<sup>33</sup>S, C<sup>34</sup>S, <sup>13</sup>CS, <sup>29</sup>SiS, and <sup>30</sup>SiS are detected in this object for the first time. Rotational-diagram analysis is carried out to determine the column densities and excitation temperatures. The isotopic ratios of the elements C, N, O, S, and Si have also been estimated. The results are consistent with stellar CNO processing and suggest that CRL 3068 is more carbon rich than IRC+10216 and CIT 6. It is also shown that the chemical composition in CRL 3068 is somewhat different from that in IRC+10216 with a more extensive synthesis of cyclic and long-chain molecules in CRL 3068. The results will provide valuable clues for better understanding circumstellar chemistry.

*Key words:* circumstellar matter – ISM: molecules – line: identification – radio lines: stars – stars: AGB and post-AGB – stars: individual (CRL 3068) – surveys

### 1. INTRODUCTION

As a star evolves up the asymptotic giant branch (AGB), copious amount of material at its outer layers are ejected into space through stellar winds and form an expanding circumstellar envelope. Through millimeter-wave and infrared (IR) spectroscopy, we have learned that circumstellar envelopes around evolved stars are very efficient chemistry factories that produce organic and inorganic molecules over very short timescales. However, our understanding of the interactions between molecular processes, chemical environment, and local physical conditions is far from complete. In oxygen- and carbon-rich environments, the reaction routes are clearly different. In oxygen-rich objects, the circumstellar chemistry is believed to be dominated by OH and H<sub>2</sub>O molecules, and the chemical complexity of the oxygen-rich environments has been demonstrated by Ziurys et al. (2007). In carbon-rich objects, a large fraction of oxygen atoms are locked in CO and C-bearing compounds such as hydrocarbons and cyanopolynes are efficiently reprocessed. Among the carbon-rich objects, the nearby AGB star IRC+10216 has been extensively studied (see, e.g., Cernicharo et al. 2000; He et al. 2008, and references therein), with more than 60 molecular species detected.

This paper is one of a series of studies devoted to the understanding of circumstellar chemistry of evolved stars. In previous work, we have presented the spectra of the AGB stars IRC+10216 (He et al. 2008) and CIT 6 (Zhang et al. 2009) and the planetary nebula (PN) NGC 7027 (Zhang et al. 2008) obtained using the Arizona Radio Observatory (ARO) 12 m telescope and the Heinrich Hertz Submillimeter Telescope (SMT). In the present study, we report a molecular line survey of the carbon-rich circumstellar envelope CRL 3068 using the same telescope settings with the aiming at exploring the molecular constituents and chemistry processes in an extremely carbon-rich environment.

The carbon-rich AGB star CRL 3068 (AFGL 3068, IRAS 23166+1655, LL Peg) is a long-period variable with a very long pulsation period of 696 days (Le Bertre et al. 1995). It has a high C/O abundance ratio of 1.38 (Winters et al. 1997) and has been taken as a prototype of extreme carbon stars (Volk et al. 1992). Jones et al. (1978) investigated the IR spectrum of CRL 3068 and detected an SiC absorption feature at 11.3  $\mu$ m. The presence of SiC absorption was further confirmed by Clément et al. (2003) based on the *Infrared Space Observatory* (ISO) observations. The fact that the SiC feature is in self-absorption suggests that the circumstellar envelope of CRL 3068 is extremely optically thick. This is supported by the very low color temperature of the dust emission component ( $\sim 300$  K, see, e.g., Lebofsky & Rieke 1977; Volk et al. 1992; Omont et al. 1993). Le Bertre et al. (1995) found that the dust continuum spectrum of CRL 3068 in the wavelength range 1–50  $\mu$ m is consistent with a dust opacity law of  $\propto \lambda^{-1.3}$ .

Based on a consistent time-dependent hydrodynamical model, Winters et al. (1997) determined the distance to CRL 3068 to be 1.2 kpc, the time-averaged outflow velocity as 14.7 km s<sup>-1</sup>, and the average mass-loss rate as  $1.2 \times 10^{-4} M_{\odot} \text{ yr}^{-1}$ . The distance derived by Winters et al. (1997) is close to a more recent value of 1.05 kpc reported by Yuasa et al. (1999) and Menzies et al. (2006). The derived mass-loss rate of Winters et al. (1997) is 2–10 times higher than those obtained using CO lines (Knapp & Morris 1985; Volk et al. 1993; Schöier et al. 2002; Woods et al. 2003; Teyssier et al. 2006) and that by fitting the dust continuum (Volk et al. 1992). The H I line at 21 cm was detected by Gérard & Le Bertre (2006), who estimated that the H I emission in CRL 3068 is extended over a region  $\sim 8'$  in diameter. Mauron & Huggins (2006) imaged the extended circumstellar envelope of CRL 3068 in the optical and were able to trace the galactic scattered light out to a distance of  $\sim 40''$  from the star. They estimated the expansion timescale of the envelope to be 15,200 yr. The optical image

was characterized by a remarkable spiral pattern traced out to  $12''$  from the center, suggesting that binary companions might play a role in shaping the circumstellar envelope. The scenario of binary-induced outflow was further confirmed by the near-IR adaptive optics images obtained with the Keck II telescope, which showed that the central region of CRL 3068 is composed of two components separated by a distance of  $0''.11$  (Morris et al. 2006). Neri et al. (1998) mapped the CO (1–0) emission, which revealed a compact inner envelope and a surrounding detached bipolar shell.

Molecular lines in CRL 3068 at millimeter wavelengths have been explored by several authors. Relatively strong CO (1–0) line emission has been detected by Knapp & Morris (1985) and Nyman et al. (1992). HC<sub>3</sub>N lines were first detected by Jewell & Snyder (1984). Nguyen-Quang-Rieu et al. (1988) discovered the HCN (1–0) and H<sup>13</sup>CN (1–0) line emission. Sopka et al. (1989) reported the observations of CO, <sup>13</sup>CO, HCN, H<sup>13</sup>CN, HC<sub>3</sub>N, and HNC in this object. Wannier et al. (1991) discovered relatively faint emission from C<sub>3</sub>H<sub>2</sub>. Radio observations toward CRL 3068 in the frequency ranges between 39–47 GHz and 85–91 GHz were carried out with the Nobeyama 45 m radio telescope by Fukasaku et al. (1994), and the molecular species C<sub>2</sub>H, HC<sub>5</sub>N, C<sub>4</sub>H, and SiS were detected in this object for the first time. Woods et al. (2003) reported a molecular line survey made with the SEST 15 m and Onsala 20 m telescopes. The molecular species in CRL 3068 that were detected positively in their survey observation include CO, <sup>13</sup>CO, CN, HCN, H<sup>13</sup>CN, HNC, C<sub>2</sub>H, HC<sub>3</sub>N, C<sub>3</sub>N, CS, and SiS.

In this paper, we present spectra of CRL 3068, representing the most complete molecular line survey of this carbon-rich envelope so far. The remaining parts of this paper are organized as follows: the observations and data reduction are described in Section 2; in Section 3, we present the identification and measurements of detected molecular lines; Section 4 gives the column densities and abundances of detected species; in Section 5, the implication of our findings on circumstellar chemistry is discussed; and our conclusions are summarized in Section 6.

## 2. OBSERVATIONS AND DATA REDUCTION

### 2.1. The ARO 12 m Observations

The spectral line survey at the  $\lambda$  2 mm window was carried out during the period from 2007 December to 2008 January with the ARO 12 m telescope at Kitt Peak. The 2 mm dual-channel SIS receivers were employed, operated in single sideband dual polarization mode. The image rejection ratio is larger than 18 dB on most of the occasions. The system noise temperatures were typically 250–550 K. The spectrometer back ends employed are two 256 channel filter banks (FBs) with a channel width of 1 MHz and a millimeter autocorrelator (MAC) with 3072 channels and 195 kHz per channel. The observations were made in beam switching mode with an azimuth beam throw of  $2'$ . We checked the pointing every 2–3 hr by observations of planets. The pointing accuracy was better than  $15''$  at normal weather conditions. The scanned frequency range was from 130.0 to 163.9 GHz with a few gaps. The half-power beamwidth (HPBW) is about  $40''$  at this frequency range. Typical on-source integration times ranged from 70 to 90 minutes for each frequency setting. For  $\lambda$  2 mm observations, we gave priority to the frequency ranges covering the strong lines as observed in IRC+10216 (Cernicharo et al. 2000). Only a few extremely faint lines in the spectra of IRC+10216 fall within the gaps of our

spectra. The temperature scale was given in term of  $T_R^*$ , which was calibrated by the chopper-wheel method, and corrected for atmospheric attenuation, radiative loss, and rearward and forward scattering and spillover. The main beam brightness temperature was determined using  $T_R = T_R^*/\eta_m^*$ , where  $\eta_m^*$  is the corrected beam efficiency ( $\sim 0.75$ ).

We used the CLASS software package in GILDAS<sup>1</sup> for the data reduction. After discarding the bad scans, we obtained the co-adding spectra from individual scans. On some occasions, the MAC spectra might suffer severe effects from the bandpass irregularities, and thus for some frequency coverages the signal-to-noise ratios might be relatively low due to the exclusion of these scans. The baseline was determined by low-order polynomial fits to the line-free regions of the spectra. In order to improve the signal-to-noise ratio, the spectra were smoothed and rebinned to a frequency resolution of 1 MHz, corresponding a velocity resolution of  $\sim 2$  km s<sup>-1</sup>. The MAC spectra are presented in Figure 1. The typical rms noise temperature is less than 15 mK in main beam temperature unit.

### 2.2. The SMT Observations

The spectral line survey at the  $\lambda$  1.3 mm window was made using the SMT 10 m telescope located on Mt. Graham in 2008 January. For the observations, we utilized the ALMA Band 6 (211–275 GHz) sideband-separating SIS mixing-preamp, yielding a typical image rejection ratio of  $> 20$  dB and a system noise temperature of  $\sim 150$  K. The 2048 channel acousto-optical spectrometer (AOS) and the 1024 channel Forbes filter banks (FFBs) were used simultaneously and were configured to provide a channel width of 500 kHz and 1 MHz, respectively. A beam switching mode was applied with a separation between the ON and OFF beams of  $2'$  in azimuth. The pointing was checked every 2 hr on nearby planets and was found to be accurate to within  $10''$ . The complete frequency range from 219.5 to 267.5 GHz was covered, with typical on-source integration time of 30 minutes at each frequency band. The beam size at this frequency range is about  $30''$ . The data were calibrated to the  $T_A^*$  temperature scale, which was corrected for atmospheric attenuation. The main beam temperature was derived using  $T_R = T_A^*/\eta_{mb}$ , where  $\eta_{mb}$  is the main beam efficiency ( $\sim 0.7$ ).

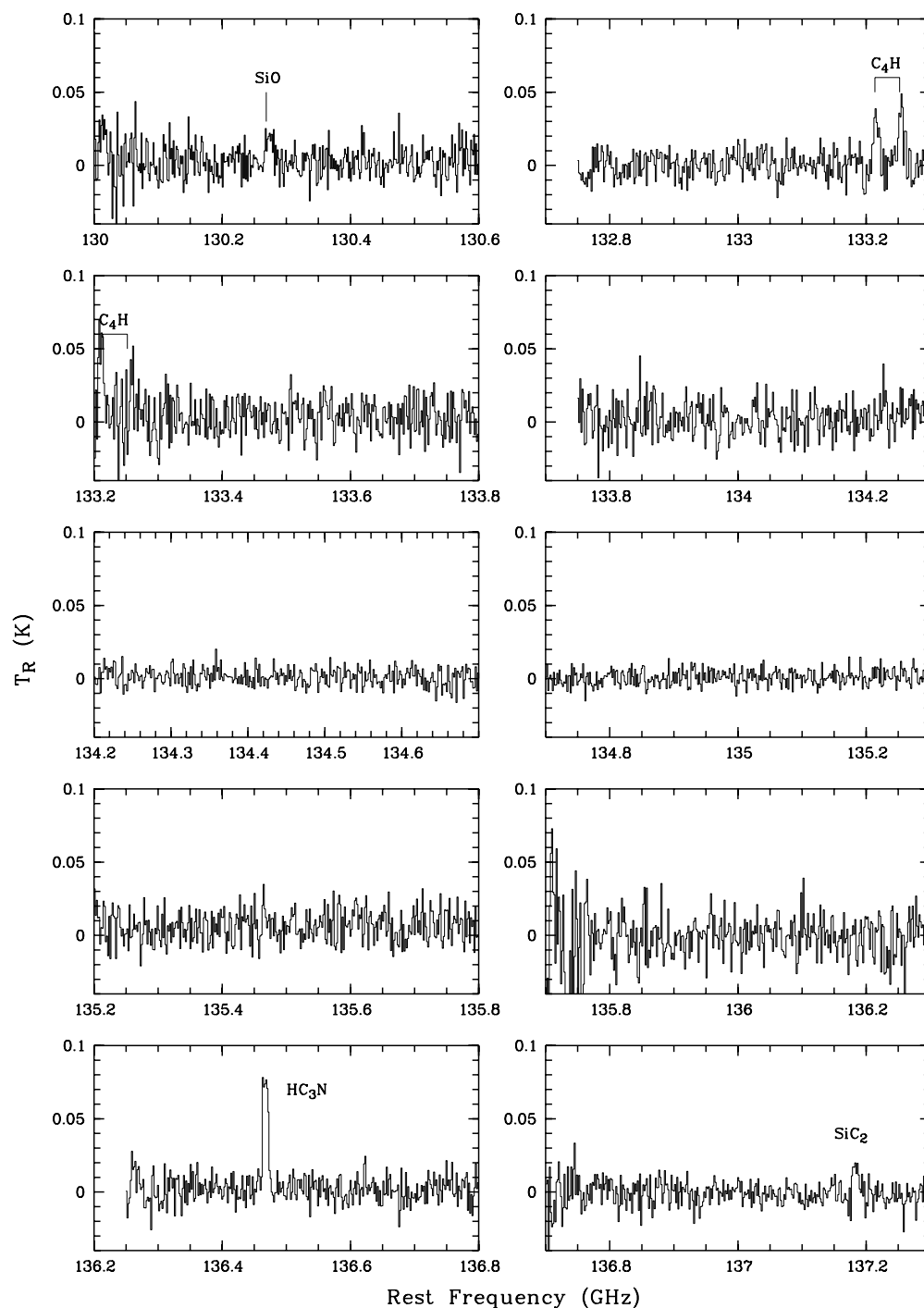
The procedure of data reduction was same as that for the 12 m data. Since there is no gap in the  $\lambda$  1.3 mm survey region, all the spectral bands were merged together. Figure 2 gives the FFB spectra, which have been smoothed and rebinned by a factor of 3, yielding a frequency resolution of 3 MHz, corresponding a velocity resolution of 3.7 km s<sup>-1</sup>, and a typical rms temperature of 5 mK in main beam temperature unit.

## 3. OBSERVATIONAL RESULTS

### 3.1. The Overall Survey

The spectra together with line identifications are shown in Figures 1 and 2. Note that some features in these figures are not real but caused by bandpass irregularities or bad channels. A total of 75 distinct emission features (including a few uncertain ones) were detected in our survey observations. The most intense line detected in our survey is the CO (2–1) transition, followed by the HCN (3–2) transition. Apart from these two transitions, the others have integrated intensities of less than 10 K km s<sup>-1</sup>. The molecular lines detected in the high-frequency window

<sup>1</sup> GILDAS is developed and distributed by the Observatoire de Grenoble and IRAM.



**Figure 1.** Spectrum of CRL 3068 in the frequency range 130–163 GHz obtained with the ARO 12 m telescope. The spectra have been smoothed to a frequency resolution of 1 MHz.

are a factor of about 2 more than those detected in the low-frequency window. This is partially due to the fact that the ARO 12 m telescope has a larger beam size than the SMT and thus the 12 m data are more likely to be affected by the beam dilution. The molecular line databases that are used for line identifications include the archives of molecular line frequencies derived from the theoretical calculations of the JPL catalog (Pickett et al. 1998)<sup>2</sup> and the Cologne database for molecular spectroscopy (CDMS; Müller et al. 2001, 2005),<sup>3</sup> and those

from previous observations of other sources (e.g., Cernicharo et al. 2000; Pardo et al. 2007; He et al. 2008; Zhang et al. 2009, and the NIST Recommended Rest Frequencies for Observed Interstellar Molecular Microwave Transitions<sup>4</sup>). We identified 11 main molecular species, including CO, CS, C<sub>2</sub>H, C<sub>4</sub>H, *c*-C<sub>3</sub>H, CH<sub>3</sub>CN, CN, HCN, SiC<sub>2</sub>, SiO, and SiS, and 12 rare isotopologues, including <sup>13</sup>CO, C<sup>17</sup>O, C<sup>18</sup>O, C<sup>33</sup>S, C<sup>34</sup>S, <sup>13</sup>CS, HC<sup>15</sup>N, H<sup>13</sup>CN, HN<sup>13</sup>C, HC<sub>3</sub>N, <sup>29</sup>SiS, and <sup>30</sup>SiS. Only three fairly weak features remain unidentified. Several transitions are

<sup>2</sup> <http://spec.jpl.nasa.gov>

<sup>3</sup> <http://www.ph1.uni-koeln.de/vorhersagen/>

<sup>4</sup> <http://physics.nist.gov/cgi-bin/micro/table5/start.pl>

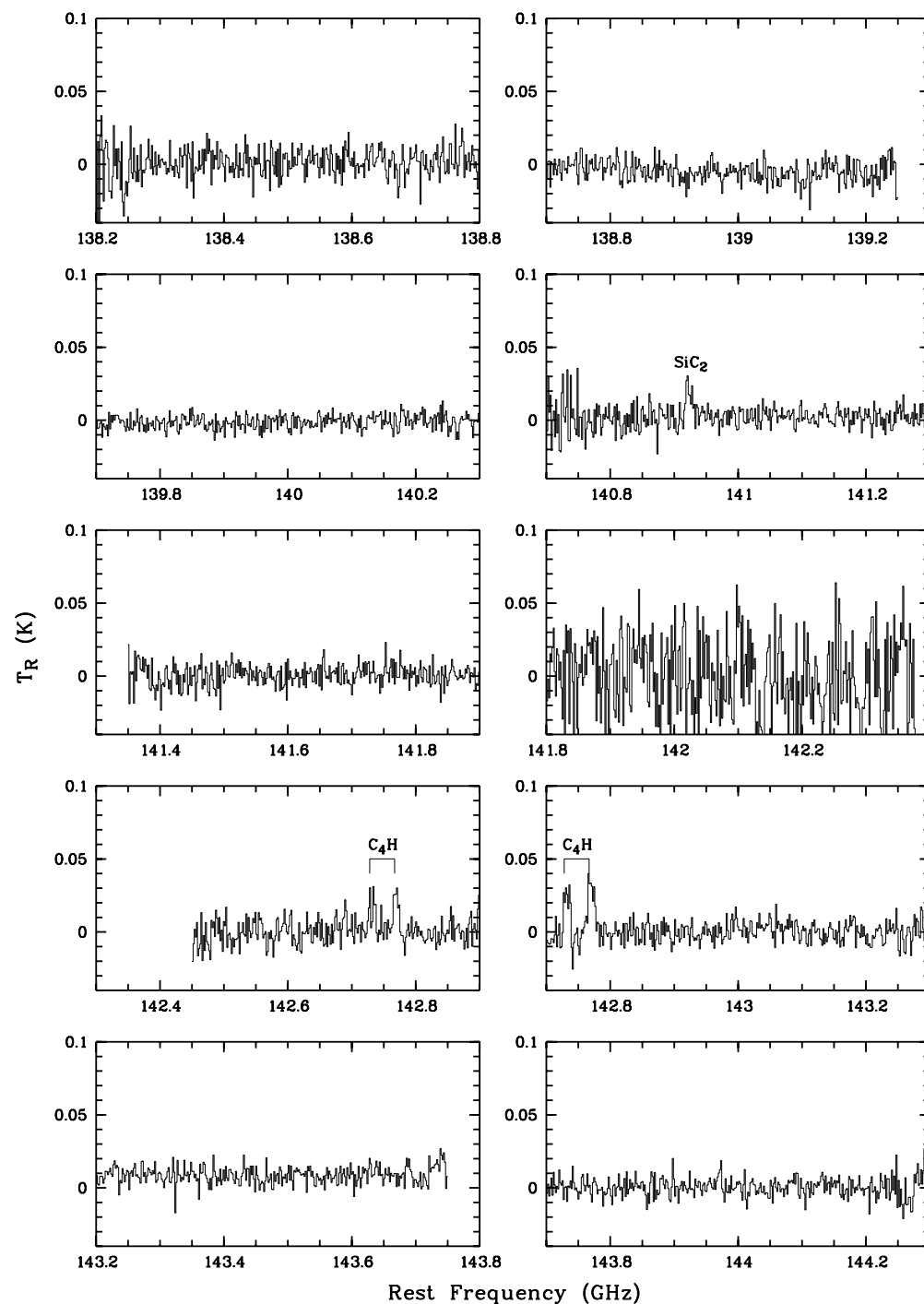


Figure 1. (Continued)

new detection in CRL 3068. A full list of line identifications and measurements is presented in Table 1. Columns 1–3 give the identified species, transitions, and frequencies, respectively. The rms noise levels are given in Column 4. Columns 5 and 6 list the peak and integrated intensities. Column 7 gives the line widths (FWHM) obtained by fitting Gaussian line profiles. For blended lines, Table 1 gives the intensities and widths of the combined features.

Figure 3 shows the cumulative number of detected lines exceeding a given integrated intensity. For comparison, the figure also plots the results for the spectra of IRC+10216 and CIT 6 which were obtained in the same observation project (He

et al. 2008; Zhang et al. 2009). The shapes of these curves in Figure 3 are similar with each other although that of CRL 3068 seems to be slightly steeper than the other two. This suggests that the differences between the three objects can be mostly a distance effect, and the detection of a large number of lines in IRC+10216 does not imply that IRC+10216 is unique or richer in molecular content than the other two.

### 3.2. Individual Molecules

The details of the molecules detection in CRL 3068 are described below. Here, we compare these detections with the

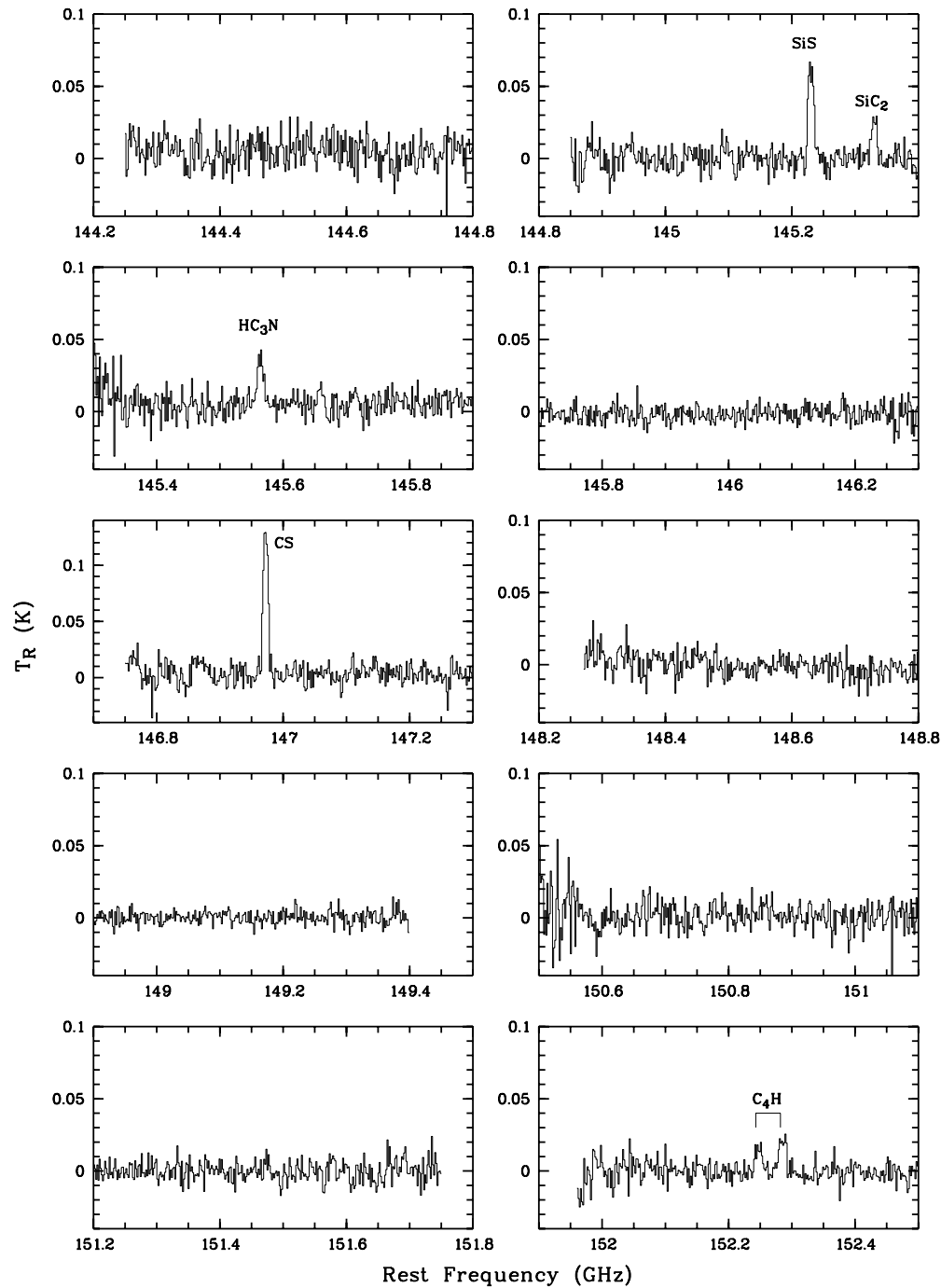


Figure 1. (Continued)

spectra of IRC+10216 and CIT 6, which are, respectively, from He et al. (2008) and Zhang et al. (2009) if no statement is issued.

### 3.2.1. CO

The  $J = 2-1$  transitions of CO and its isotopologues  $^{13}\text{CO}$ ,  $\text{C}^{17}\text{O}$ , and  $\text{C}^{18}\text{O}$  were detected by the SMT. The CO (2-1) transition is the strongest line detected in this survey, with an integrated intensity of  $35.9 \text{ K km s}^{-1}$ . This line has been observed by Volk et al. (1993) using the 15 m JCMT. They obtained an integrated intensity of  $\int T_A^* dv = 40.2 \text{ K km s}^{-1}$  (i.e.,  $\int T_R dv = 57.4 \text{ K km s}^{-1}$ ), slightly larger than our result. A higher integrated intensity of the CO (2-1) line

was detected by Groenewegen et al. (1996) using the IRAM telescope. However, considering the larger beam size of the SMT compared to those of JCMT and IRAM, these intensity discrepancies are insignificant. The  $^{13}\text{CO}$  (2-1) line has also been detected by Groenewegen et al. (1996) and Bujarrabal et al. (1994). Our result yields an intensity ratio of  $I(^{13}\text{CO } 2-1)/I(^{12}\text{CO } 2-1) = 0.14$ , larger than the values of 0.10 and 0.07 found in IRC+10216 and CIT 6. This reflects different  $^{13}\text{C}/^{12}\text{C}$  isotopic ratios and/or different optical depth effects on the three objects. The faint  $\text{C}^{17}\text{O}$  and  $\text{C}^{18}\text{O}$  lines are only marginally above the detection limit. The two rare isotopologues should be new detections for this object. The CO line shows a narrower profile than the isotopic lines which can be explained by the fact that the former is optically thick.

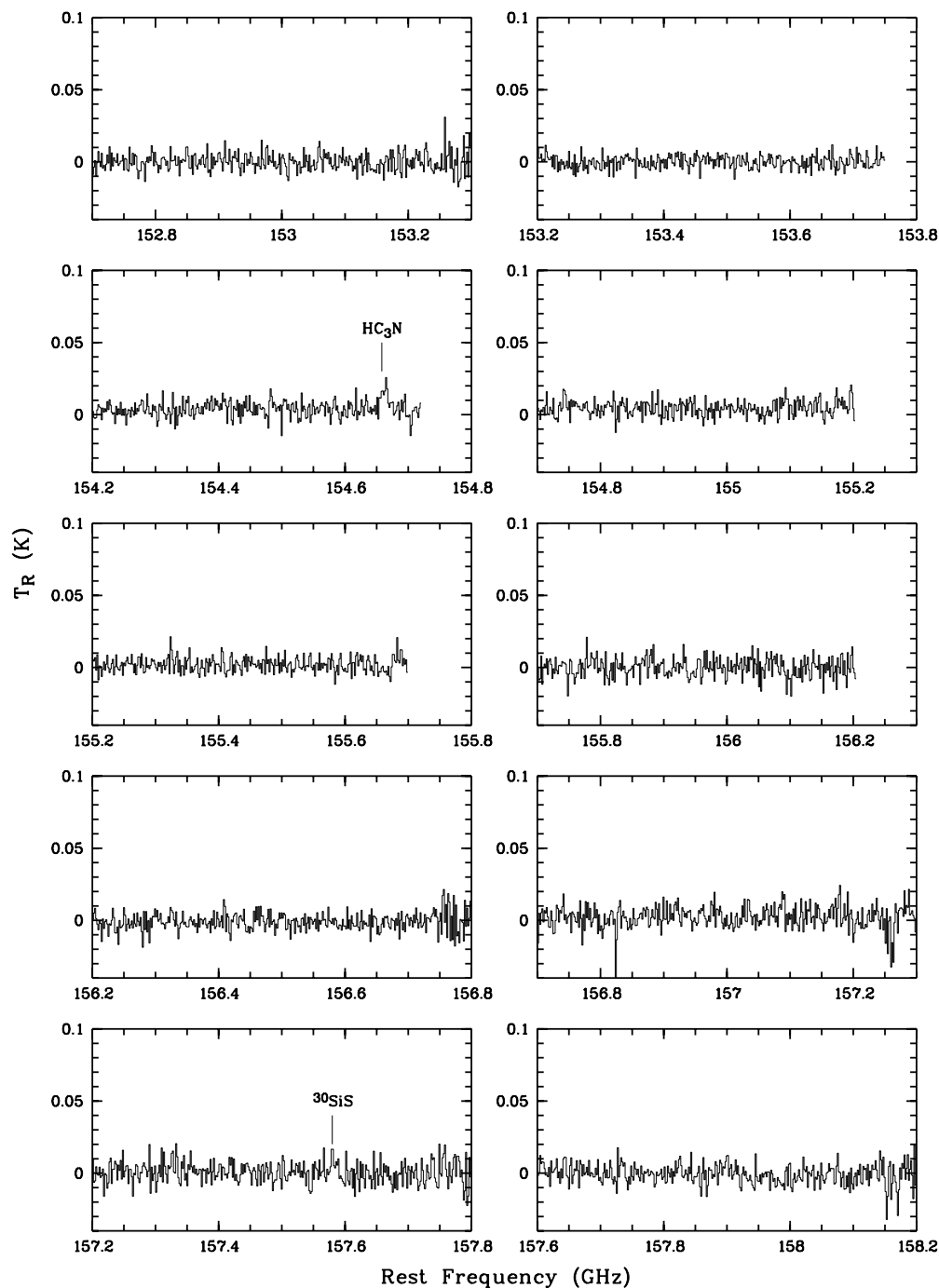


Figure 1. (Continued)

### 3.2.2. CS

The  $J = 3-2$  and  $J = 5-4$  transitions of CS were detected by the ARO 12 m and the SMT, respectively. The two CS lines toward this source have also been detected by Bujarrabal et al. (1994) using the IRAM telescope. In the  $\lambda$  1.3 mm window, we for the first time, detected the  $J = 5-4$  isotopic transitions of  $C^{33}S$ ,  $C^{34}S$ , and  $^{13}CS$ , among which the  $C^{33}S$  ( $5-4$ ) line emission is relatively faint and its measurement is uncertain. The  $J = 3-2$  isotopic transitions lie in the  $\lambda$  2 mm region, but are below our detection limit. The two main lines have a similar width but are narrower than the isotopic lines, suggesting that the main lines are optically thick. We obtained the intensity ratios of  $I(^{13}CS\ 5-4)/I(^{12}CS\ 5-4) = 0.09$  and  $I(C^{34}S\ 5-4)/I(C^{32}S\ 5-4) =$

0.13, larger than the corresponding values of 0.03 and 0.07 in IRC+10216. The trend is the same as that found for the  $I(^{13}CO\ 2-1)/I(^{12}CO\ 2-1)$  ratio.

### 3.2.3. $C_2H$

Fukasaku et al. (1994) detected  $C_2H$  in this object through the  $N = 1-0$  transition. Their detection was further confirmed by Woods et al. (2003). The  $N = 3-2$  transition is split in six hyperfine-structure lines grouped in three fine-structure groups, which lie in our survey range. The two strong main components,  $3_{7/2}-2_{5/2}$  and  $3_{5/2}-2_{3/2}$ , are clearly detected in the 2 mm window. The  $3_{7/2}-2_{5/2}$  transition is blended with a considerably weaker  $SiC_2$  line. The faint  $3_{5/2}-2_{5/2}$  transition

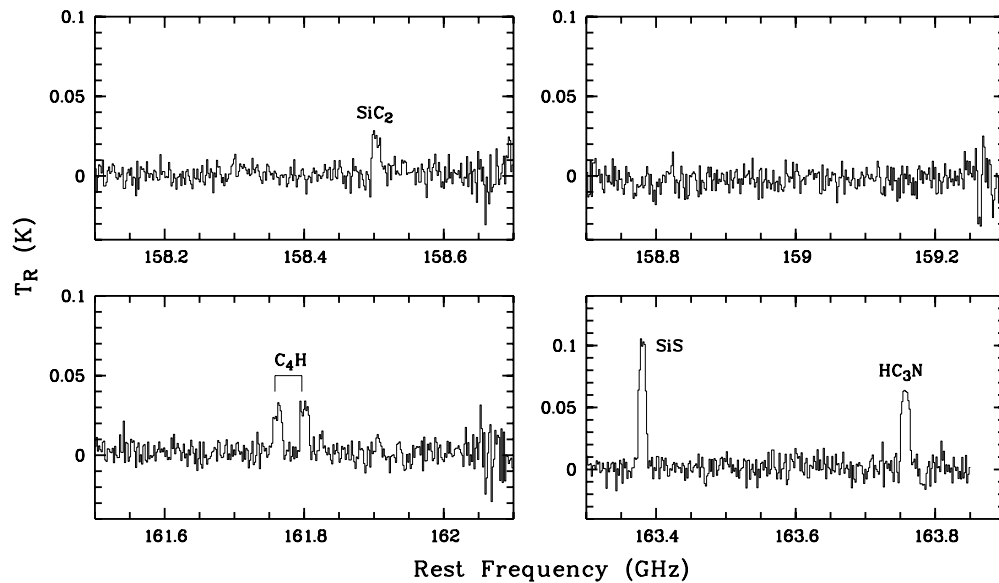


Figure 1. (Continued)

is overwhelmed by noise. We obtained the intensity ratio of  $I(\text{C}_2\text{H } 3_{7/2-2_{5/2}})/I(\text{C}_2\text{H } 3_{5/2-2_{3/2}}) = 1.7$ , in good agreement with the values of 1.4 and 1.5 found in IRC+10216 and CIT 6, respectively.

#### 3.2.4. $\text{C}_4\text{H}$

The  $N = 10-9$  transition of  $\text{C}_4\text{H}$  in this object has been detected by Fukasaku et al. (1994). Due to fine-structure interaction, every rotational transition of  $\text{C}_4\text{H}$  is split into two components, which have similar intensities. A total of 12 favorable lines of  $\text{C}_4\text{H}$  lie in our survey range. The eight  $\text{C}_4\text{H}$  lines in the  $\lambda$  2 mm window were clearly detected. The four lines in the  $\lambda$  1.3 mm window are too faint to obtain reliable measurements. In Table 1, we only give an uncertain detection of the  $\text{C}_4\text{H}$  (24–23 a,b) lines, which is the strongest transition of  $\text{C}_4\text{H}$  in the  $\lambda$  1.3 mm window. We found that these high- $J$   $\text{C}_4\text{H}$  lines are at least three times fainter than those in the  $\lambda$  2 mm window. In IRC+10216, however, these  $\text{C}_4\text{H}$  transitions have a similar strength (see Table 9 of He et al. 2008). This cannot be completely attributed to different beam dilution effects in the two objects, and can be a reflection of the different physical conditions of the two carbon envelopes.

#### 3.2.5. $c\text{-C}_3\text{H}$

The cyclopropynylidyne radical ( $c\text{-C}_3\text{H}$ ) has not been detected in CRL 3068 before this work. Here, we report the first tentative detection of this species. Six favorable transitions of  $c\text{-C}_3\text{H}$  lie in our survey region. Only the strongest two transitions are discovered in our spectra with relatively weak strengths.  $c\text{-C}_3\text{H}$  has been detected in IRC+10216, whereas there is no evidence for the corresponding lines of  $c\text{-C}_3\text{H}$  in CIT 6.

#### 3.2.6. $\text{CH}_3\text{CN}$

There was no report of the detection of  $\text{CH}_3\text{CN}$  in this object before this work. Woods et al. (2003) estimated the intensity upper limit of the  $(6_1-5_1)$  transition. Here, we present the first detection of  $\text{CH}_3\text{CN}$  in this object. There are a total of 14 favorable  $\text{CH}_3\text{CN}$  transitions in our survey region. The strongest two fine-structure groups are clearly detected in the  $\lambda$  1.3 mm window, but the others are below our detection limit. This species was also detected in IRC+10216 and CIT 6.

#### 3.2.7. $\text{CN}$

The cyanogen radical (CN) is one of the most abundant molecules in envelopes of carbon-rich stars. CN in CRL 3068 has been discovered by Woods et al. (2003) and Bachiller et al. (1997) in the  $N = 1-0$  and  $N = 2-1$  transitions. There are three  $N = 2-1$  fine-structure groups of CN present in our survey region. They are split into total of 18 hyperfine-structure components. All the three groups were apparently observed in the  $\lambda$  2 mm window. The weakest one around 226.33 GHz should be a new detection. Our observations suggest the intensity ratio of the fine-structure groups around 226.87 GHz and 226.69 GHz to be 1.6, in excellent agreement the value of 1.4 obtained by Bachiller et al. (1997). The value is also consistent with those found in IRC+10216 and CIT 6.

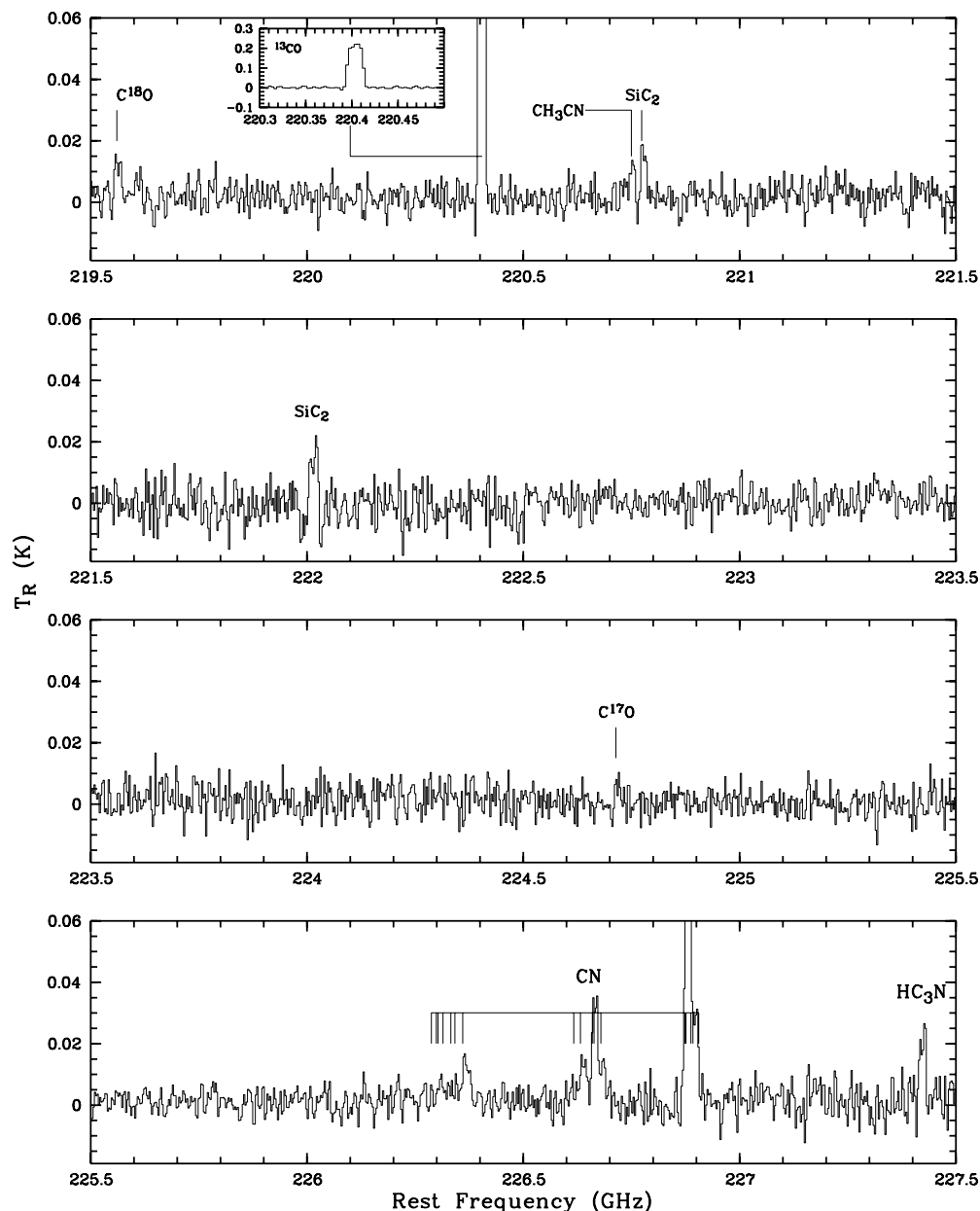
#### 3.2.8. $\text{HCN}$

The  $J = 3-2$  transitions of HCN and its isotopologues  $\text{HC}^{15}\text{N}$  and  $\text{H}^{13}\text{CN}$  were clearly detected with well defined profiles in the  $\lambda$  2 mm window. The HCN ( $3-2$ ) transition is the second strongest line after the CO ( $3-2$ ) transition in our survey. A few vibrationally excited lines of HCN have been detected in IRC+10216 and CIT 6. The strongest two are detected in the spectra of CRL 3068. To our knowledge, this is the first detection of vibrationally excited lines in this object. We discovered the isotopologue  $\text{HC}^{15}\text{N}$  for the first time. The intensity ratio of  $I(\text{HC}^{15}\text{N } 3-2)/I(\text{H}^{13}\text{CN } 3-2)$  is 0.027, which is slightly higher than the value of 0.016 obtained in IRC+10216. We also obtained the intensity ratio of  $I(\text{H}^{13}\text{CN } 3-2)/I(\text{H}^{12}\text{CN } 3-2) = 0.60$ , larger than the values of 0.16 and 0.41 found in IRC+10216 and CIT 6. The larger isotopologue-to-main line ratios in CRL 3068 are also found for CO and CS (see above). Consequently, we infer that the lines in this extreme carbon star are more optically thick than those in IRC+10216 and CIT 6.

#### 3.2.9. $\text{HNC}$

HNC has been detected in CRL 3068 (Sopka et al. 1989; Fukasaku et al. 1994; Woods et al. 2003). This species can be produced through a similar way to HCN. HNC can also be enhanced through ion-molecular reactions or be transferred into HCN in high temperature. An abundance comparison of





**Figure 2.** Spectrum of CRL 3068 in the frequency ranges 219.5–267.5 GHz obtained with the SMT 10 m telescope. The spectra have been smoothed to a frequency resolution of 3 MHz.

HNC with HCN can provide some insight into circumstellar chemistry. Although no HNC line lies in our survey region, we conclusively detected its isotopologue  $\text{HN}^{13}\text{C}$  in the  $J = 3-2$  transition for the first time. Our observations suggest the intensity ratio  $I(\text{H}^{13}\text{CN } 3-2)/I(\text{HN}^{13}\text{C } 3-2)$  to be 19.3, about an order of magnitude lower than that in IRC+10216. This implies that HNC has been enhanced in CRL 3068.  $\text{HN}^{13}\text{C}$  was not detected in CIT 6.

### 3.2.10. $\text{HC}_3\text{N}$

Cyanoacetylene ( $\text{HC}_3\text{N}$ ) has been commonly detected in carbon-rich circumstellar envelopes. The presence of  $\text{HC}_3\text{N}$  in CRL 3068 has been confirmed (Jewell & Snyder 1984; Sopka et al. 1989; Bujarrabal et al. 1994; Fukasaku et al. 1994; Woods et al. 2003). Nine  $\text{HC}_3\text{N}$  transitions from  $J = 15-14$  to  $J = 29-28$  lie in the frequency range of our survey. All of them were detected in our spectra. Most of these high- $J$  transitions are new detections.

### 3.2.11. $\text{SiC}_2$

$\text{SiC}_2$  is the species having the most emission lines in our survey. Including possible detections and blended features, a total of 23  $\text{SiC}_2$  transitions were detected. These  $\text{SiC}_2$  lines are relatively weak with peak brightness temperatures less than 40 mK. We cannot find previous papers reporting on the detections of  $\text{SiC}_2$  in CRL 3068. Woods et al. (2003) failed to discover  $\text{SiC}_2$  in this object and estimated an intensity upper limit of the  $\text{SiC}_2$  ( $5_{0,5}-4_{0,4}$ ) transition.

### 3.2.12. $\text{SiO}$

$\text{SiO}$  in CRL 3068 has been detected by Bujarrabal et al. (1994) in the  $J = 2-1$  and  $J = 3-2$  transitions. In our survey, the  $J = 3-2$  and  $J = 6-5$  transitions were detected. The  $\text{SiO}$  ( $6-5$ ) transition was also detected in our spectra of IRC+10216 and CIT 6. We found that the relative intensity of the  $\text{SiO}$  transition in CRL 3068 is much lower than those in IRC+10216 and CIT 6.

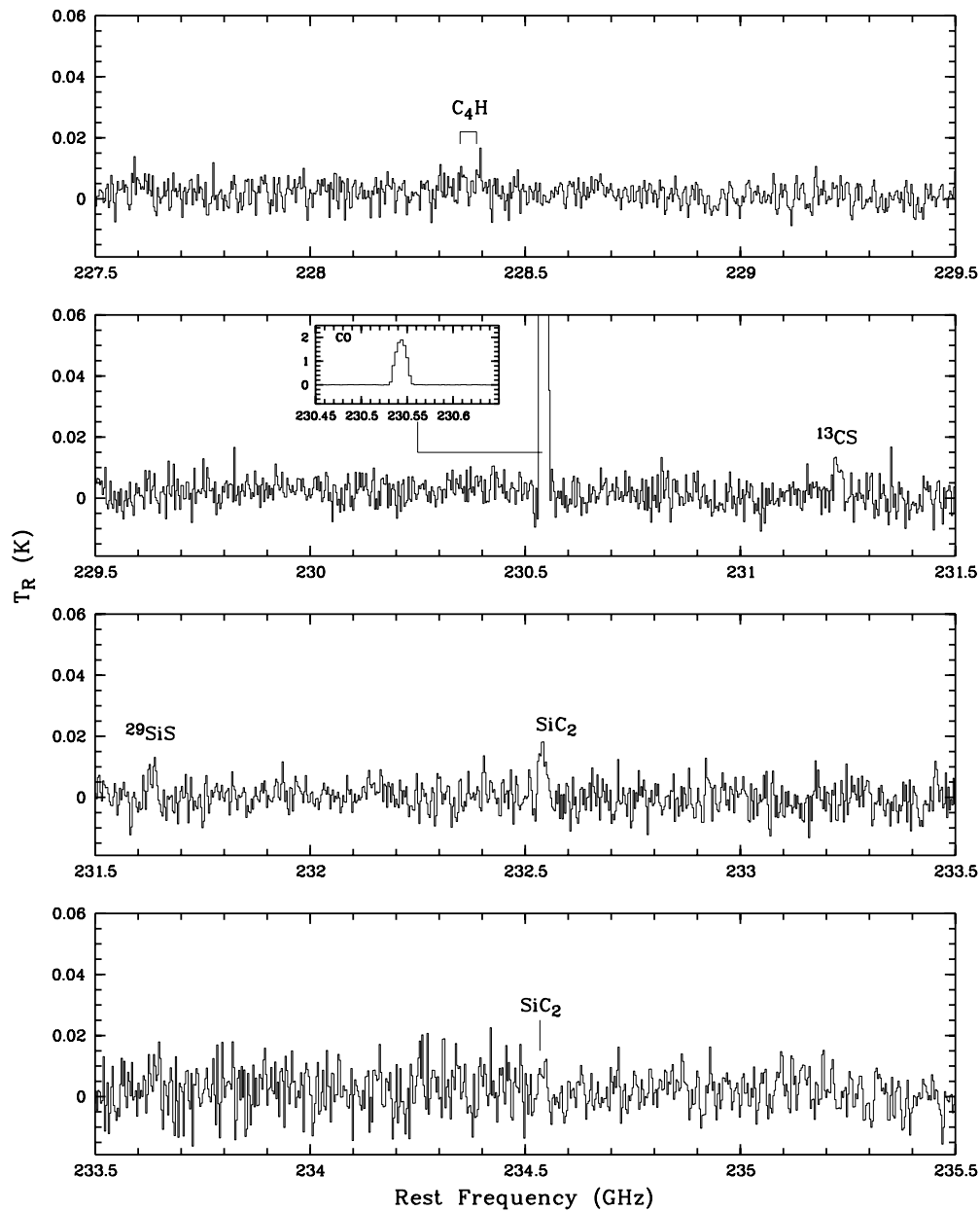


Figure 2. (Continued)

The intensity ratio of  $I(\text{SiO } 3-2)/I(^{13}\text{CO } 3-2)$  in CRL 3068 is 0.1, an order of magnitude lower than the values of 1.1 and 1.0 found in IRC+10216 and CIT 6. Its isotopic transitions  $^{29}\text{SiO}$  and  $^{30}\text{SiO } (3-2)$  lie in the surveyed range but are overwhelmed by noise.

### 3.2.13. SiS

The  $J = 6-5$  and  $J = 5-4$  transitions of SiS in CRL 3068 have been previously observed by Bujarrabal et al. (1994), Fukasaku et al. (1994), and Woods et al. (2003). In this survey, we conclusively detected four SiS transitions with higher  $J$  (8-7, 9-8, 13-12, and 14-13) transitions. We also report the first possible detection of the isotopologues  $^{29}\text{SiS}$  and  $^{30}\text{SiS}$ .

### 3.2.14. Unidentified Lines

Three weak lines detected at  $3\sigma-8\sigma$  noise levels remain unidentified. The 264067 MHz line probably corresponds to the

U264072 line detected in IRC+10216 and the other two U lines have no corresponding detection in IRC+10216 and CIT 6. We also searched the NIST frequency table and found that the two features at 245982 MHz and 255108 MHz seem to be associated the U lines at 245993 MHz and 255158 MHz detected in Sgr B2(N) (Nummelin et al. 1998).

### 3.3. Line Profiles

Since the circumstellar envelopes of AGB stars are expanding, molecular line profiles can provide significant insight into the nature of the lines as well as the kinematic structure of the envelopes. The lines arising from a spherical envelope might have four characteristic profile shapes (see, e.g., Habing & Olofsson 2003; Kwok 2006): (1) a flat-topped line profile resulting from optically thin, spatially unresolved emission; (2) a parabolic line profile resulting from optically thick, spatially unresolved emission; (3) a double-peaked line profile resulting from optically thin, spatially resolved emission; and

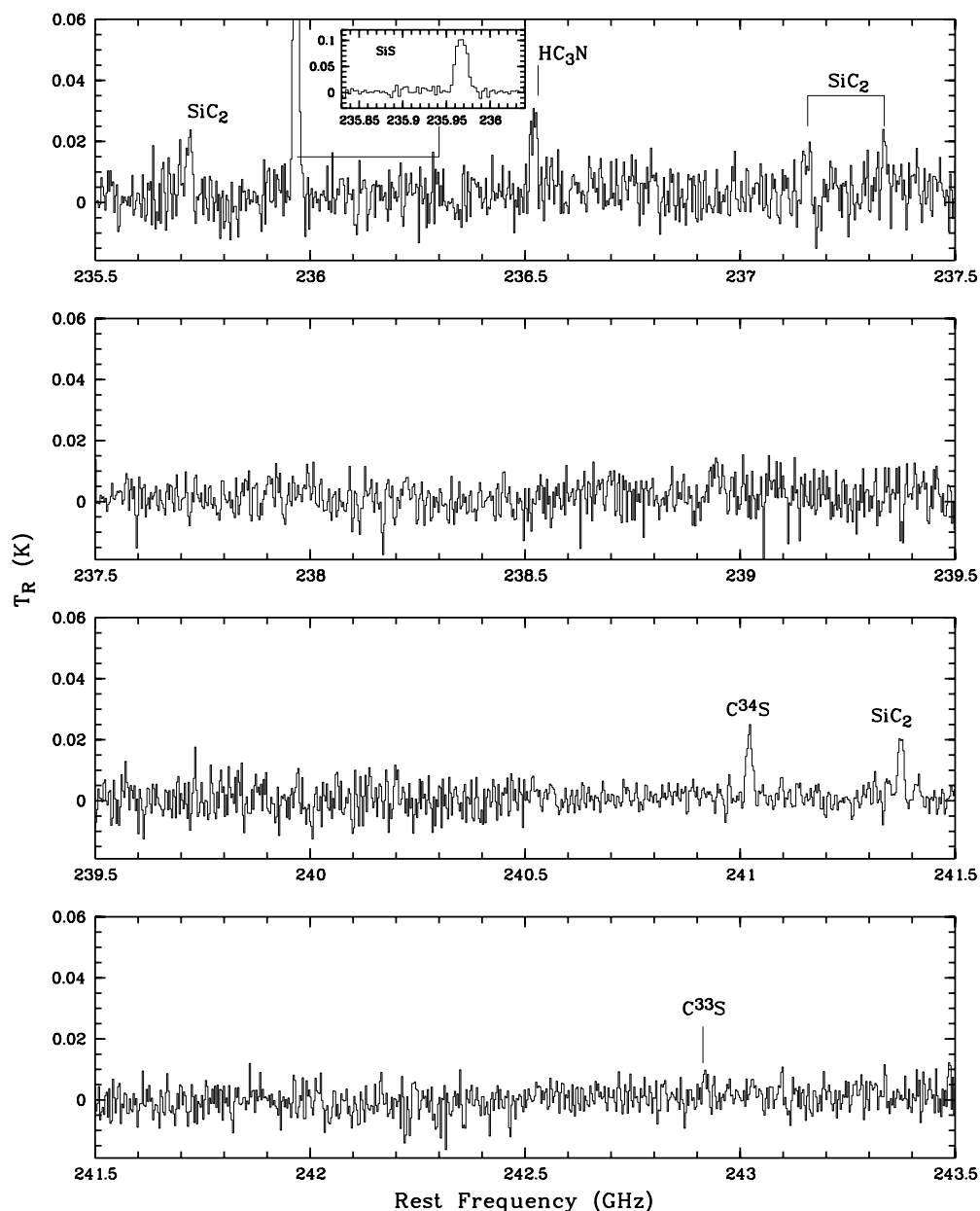


Figure 2. (Continued)

(4) a smoothed parabolic (or seemingly flat-topped) line profile resulting from optically thick, spatially resolved emission. Our observations show that most of the detected lines are unresolved. The profiles of the CO, CS, and HCN emission lines appear to be parabolic, indicating that they are optically thick. The  $^{13}\text{CO}$  line shows a rectangular profile, suggesting that it is likely optically thin. Some of the lines, such as vibrationally excited lines of HCN, exhibit fairly narrow profiles, probably because they are excited in a compact region close to the central star. The different widths for different emission lines seem to suggest that the expansion velocity of the envelope is not constant.

#### 3.4. Nondetection

Compared with the spectra of IRC+10216, the nondetected molecular species in our survey region include AlCl, AlF, MgNC, NaCN, NaCl, PN,  $\text{C}_2\text{S}$ ,  $\text{C}_3\text{H}$ , *c*- $\text{C}_3\text{H}_2$ ,  $\text{C}_3\text{N}$ ,  $\text{C}_3\text{S}$ , *l*- $\text{C}_4\text{H}_2$ ,  $\text{H}_2\text{CO}$ , SiC, and SiN. All the emission lines from these

species are weak in IRC+10216 and are estimated to have an integrated-intensity upper limit of  $0.2 \text{ K km s}^{-1}$  in CRL 3068. If the line intensities relative to the  $^{13}\text{CO}$  (2–1) transition in CRL 3068 are the same as those in IRC+10216, all these lines are well below our detection limit. Therefore, we cannot draw the conclusion that the molecular species in CRL 3068 are less abundant than in IRC+10216.

#### 4. COLUMN DENSITIES AND ABUNDANCES

For comparison, we have applied the same approach as used in our previous papers (Zhang et al. 2008, 2009) to calculate the column densities and abundances of the molecules detected in our spectra. This will minimize the effects of systematic errors when we compare the results in different objects.

The excitation temperatures ( $T_{\text{ex}}$ ) and column densities ( $N$ ) were deduced using the standard rotational-diagram analysis. Under the assumption that the lines are optically thin, the

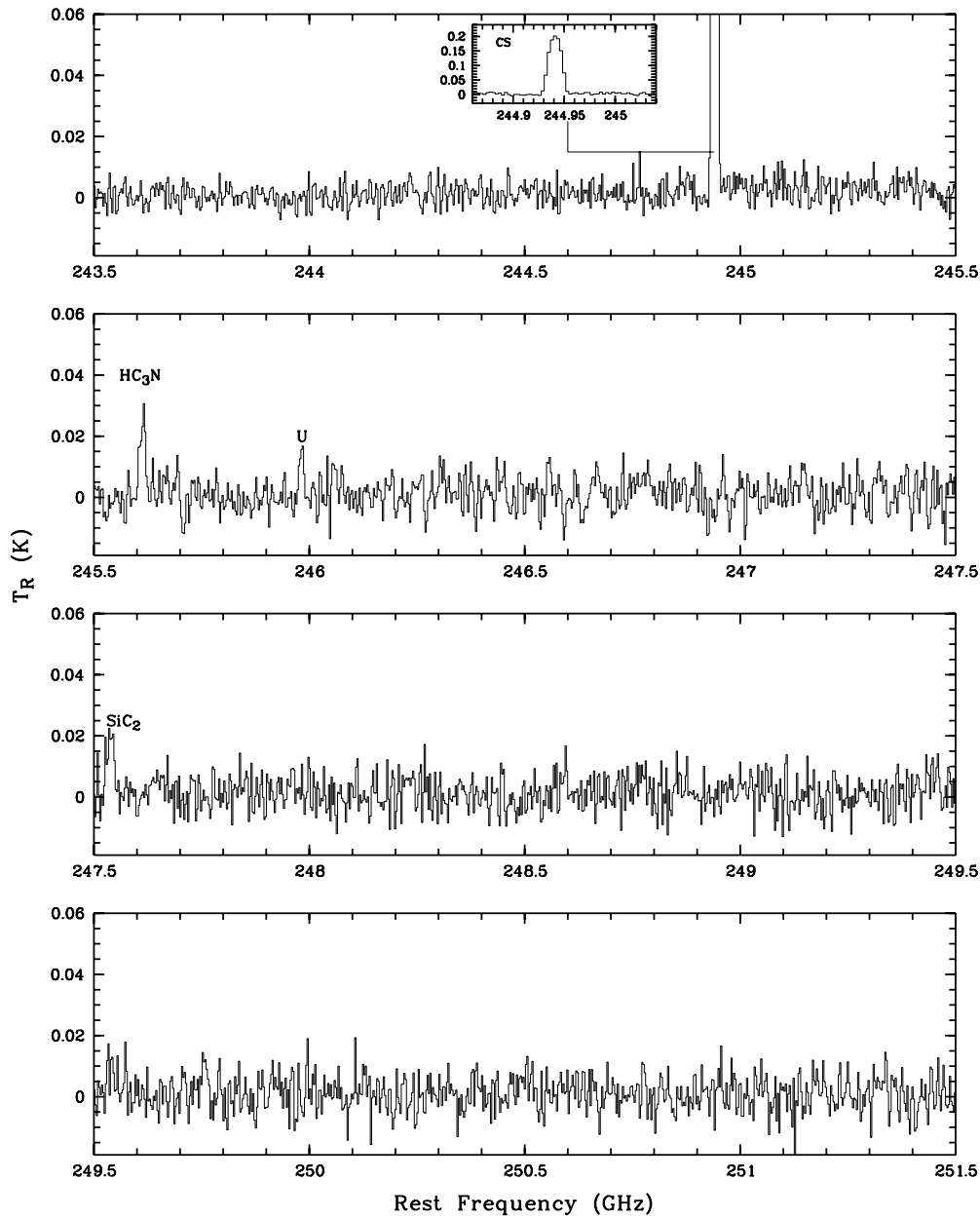


Figure 2. (Continued)

level populations are in local thermal equilibrium (LTE), and  $T_{\text{ex}} \gg T_{\text{bg}}$ , where  $T_{\text{bg}}$  is the cosmic background radiation temperature (2.7 K), we have the relation,

$$\ln \frac{N_u}{g_u} = \ln \frac{3k \int T_s dv}{8\pi^3 \nu S \mu^2} = \ln \frac{N}{Q(T_{\text{ex}})} - \frac{E_u}{kT_{\text{ex}}}, \quad (1)$$

where  $N_u$ ,  $g_u$ , and  $E_u$  are the population, degeneracy, and excitation energy of the upper level,  $\int T_s dv$  is the integration of the source brightness temperature over the velocity,  $S$  is the line strength,  $\mu$  is the dipole moment,  $\nu$  is the line frequency, and  $Q$  is the rotational partition function. If several transitions arising from levels covering a wide energy range are observed,  $T_{\text{ex}}$  and  $N$  can be determined using a straight-line fit to  $N_u/g_u$  versus  $E_u/kT_{\text{ex}}$ . Departure from the linear relation suggests different excitation mechanisms or misidentification. For the calculations, we have corrected the effect of beam dilution through  $T_s = T_R(\theta_b^2 + \theta_s^2)/\theta_s^2$ , where  $\theta_b$  ( $\sim 40''$  and  $30''$  for

the ARO 12 m and the SMT, respectively) is the antenna full beam at half-power, and  $\theta_s$  is the source diameter. Different transitions may have different  $\theta_s$  and it is hard to determine  $\theta_s$  for each molecule. According to the CO observations reported by Neri et al. (1998) and Teyssier et al. (2006), we assumed  $\theta_s = 22'' \pm 8''$ . The assumed  $\theta_s$  value is similar to that used by Fukasaku et al. (1994) and will introduce a  $\sim 70\%$  uncertainty in the derived column densities. Four molecular species, SiC<sub>2</sub>, SiS, HC<sub>3</sub>N, and C<sub>4</sub>H have adequate numbers of detected transitions covering a wide range of excitation energy and the rotational diagrams of these species are given in Figure 4. Although in general the transitions of these species are well fitted by straight lines, we note that the rotational diagram of SiC<sub>2</sub> indicates a higher  $T_{\text{ex}}$  for high- $J$  transitions compared to the low- $J$  ones. This is similar to what is found in IRC+10216 (Avery et al. 1992; He et al. 2008), suggesting that excitation by IR radiation may be important for this molecule in AGB envelopes. For the species for which the rotational diagrams are unavailable, an

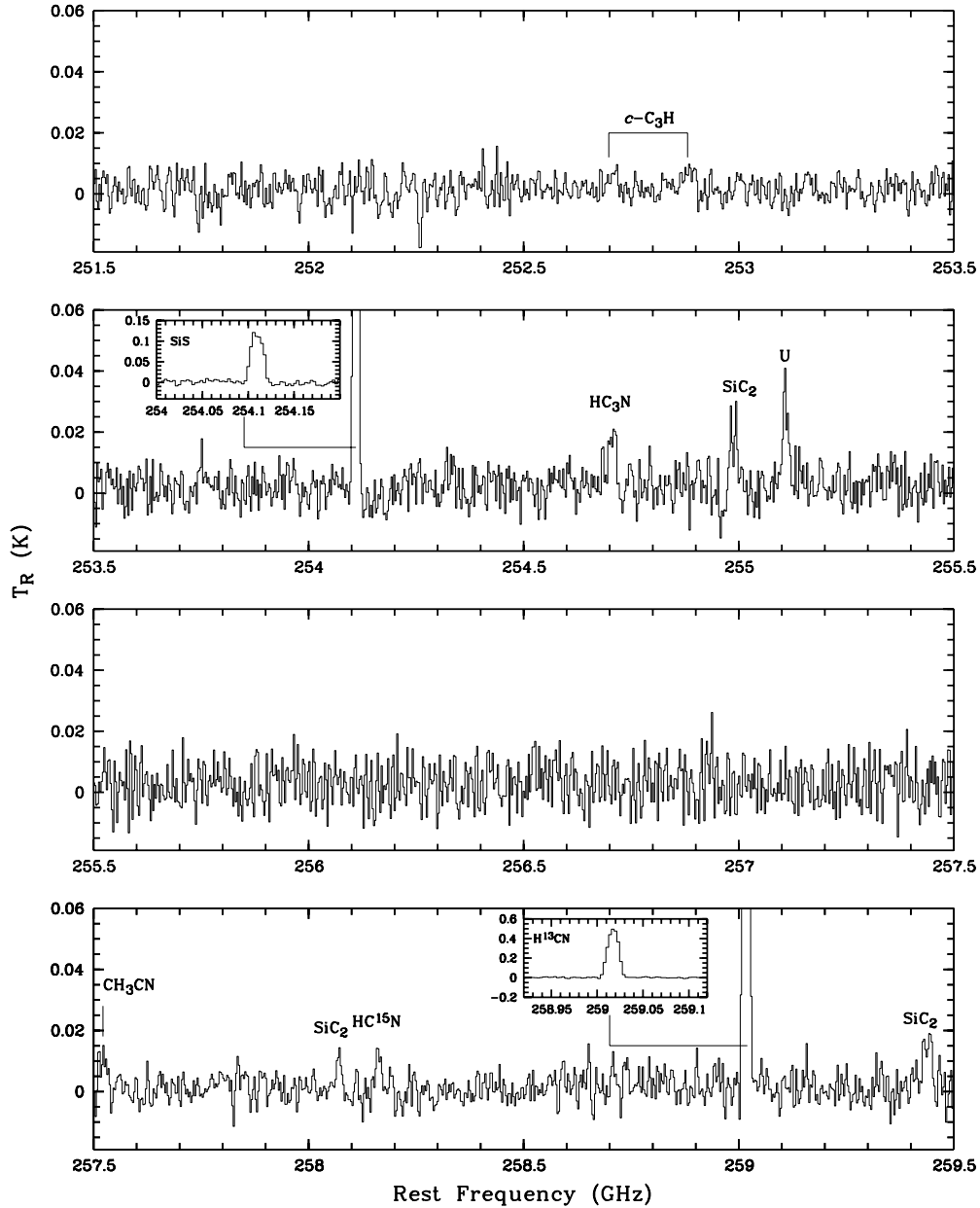


Figure 2. (Continued)

average  $T_{\text{ex}}$  ( $\sim 53$  K) was assumed to calculate their column densities.

The molecular abundances respect to molecular hydrogen ( $f_X$ ) were calculated using the expression by Olofsson (1996),

$$f_X = 1.7 \times 10^{-28} \frac{v_e \theta_b D}{M_{\text{H}_2}} \frac{Q(T_{\text{ex}}) v_{\text{ul}}^2}{g_u A_{\text{ul}}} \frac{e^{E_l/kT_{\text{ex}}}}{\int_{x_i}^{x_e} e^{-4x^2 \ln 2} dx} \int T_R dv, \quad (2)$$

where  $\int T_R dv$  is given in  $\text{K km s}^{-1}$ , the full HPBW  $\theta_b$  is in arc sec, the expansion velocity  $v_e$  is in  $\text{km s}^{-1}$ ,  $D$  is the distance in pc,  $M_{\text{H}_2}$  is the mass-loss rate in  $M_{\odot} \text{ yr}^{-1}$ ,  $v_{\text{ul}}$  the line frequency in GHz,  $g_u$  is the statistical weight of the upper level,  $A_{\text{ul}}$  is the Einstein coefficient for the transition,  $E_l$  is the energy of the lower level, and  $x_{i,e} = R_{i,e}/(\theta_b D)$  with  $R_i$  and  $R_e$  the inner and outer radii of the shell. To aid the reader, the Appendix provides full deduction of this formula. For the abundance calculation, we first determined the mass-loss rate using the CO (2–1) line. Using the formula of Winters et al. (2002) and assuming

$f_{\text{CO}} = 1 \times 10^{-3}$  and a distance of 1.05 kpc, we obtained  $M_{\text{H}_2} \approx 3 \times 10^{-5} M_{\odot} \text{ yr}^{-1}$ , in good agreement with the recent result of Schöier et al. (2002) and Woods et al. (2003) but a factor of 2 lower than that of Teyssier et al. (2006). Whenever available, the  $R_i$  and  $R_e$  values given by Woods et al. (2003) were used. The emission regions of isotopologues were assumed to have the same inner and outer radii with those of their main species. The  $T_{\text{ex}}$  values derived from rotation diagram analysis are adopted. For species where more than one line is detected, we find that the spreads of the abundances derived from different transitions are very small ( $< 10\%$ ), and determine the average values weighted by line intensity. Although the adopted  $T_{\text{ex}}$  value is significantly larger than the average excitation temperature derived by Woods et al. (2003) for a sample of carbon stars and the excitation temperature may not be homogeneous within the envelope, the abundances are essentially insensitive to  $T_{\text{ex}}$  in the case of  $E_l \ll kT_{\text{ex}}$ .

The derived values for  $T_{\text{ex}}$ ,  $N$ , and  $f_X$  are given in Table 2. Our calculations are based on an optically thin assumption.

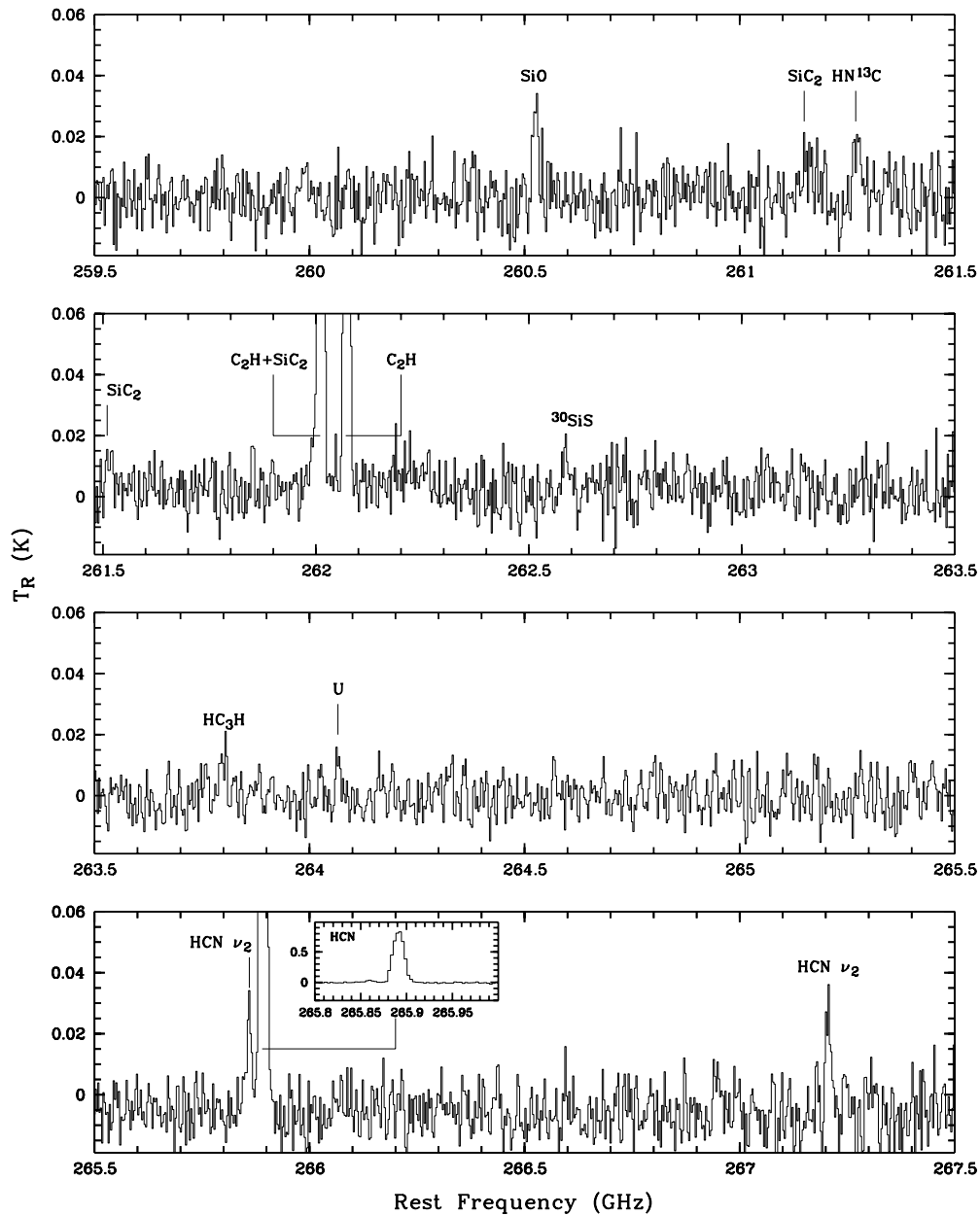


Figure 2. (Continued)

Therefore, for the optically thick emission, the  $N$  and  $f_X$  given in Table 2 should be treated as lower limits. Combining various error sources (uncertainties of line intensity, excitation temperature, distance, mass-loss rate, etc.), we crudely estimate that the errors of the absolute column densities and abundances amount to a factor of  $\sim 5$ . Note that the estimated errors are for the case that the basic assumptions of the method, i.e., optically thin emission, are met. If the extent of a given species is significantly different from that of CO, its column density may bear a larger error than estimated here. It is impossible to accurately determine the extent of each species without interferometric observations. In most of the cases, the self-shielding molecule CO is more extended than other molecules (see, e.g., Woods et al. 2003). If the source size is overestimated by a factor of 2, the resultant column density will be underestimated by a factor of 4. Accordingly, it is possible that the actual errors could rise above a factor of 10.

Nevertheless, the column density ratios and the abundance ratios should be much more reliable.

Table 2 also gives a comparison of our results with those derived by Fukasaku et al. (1994) and Woods et al. (2003). While more molecular species are detected in our survey, for the molecules that are commonly detected (but not necessarily from the same transitions), Table 2 shows that the  $N$  and  $f_X$  values are in agreement within 1 order of magnitude. Such discrepancies are understandable considering different instruments and methods used for the observations and abundance analysis.

## 5. DISCUSSION

### 5.1. Isotopic Species

Theory predicts that during the AGB phase the nucleosynthesized products in the inner shell are dredged up to the stellar surface, resulting in changing the isotopic ratios of circumstel-

**Table 1**  
Molecular Transitions Detected in CRL 3068

Species (MHz)	Transition	Frequency <sup>a</sup> (Upper-Lower)	rms (mK)	$T_R$ (K)	$\int T_R dv^b$ (K km s <sup>-1</sup> )	$\Delta V_{FWHM}$ (km s <sup>-1</sup> )
CO	$J = 2-1$	230538.0	4	1.893	35.942	17.7
<sup>13</sup> CO	$J = 2-1$	220398.7	4	0.221	5.149	21.2
C <sup>17</sup> O	$J = 2-1$	224714.4	4	0.009	0.23:	...
C <sup>18</sup> O	$J = 2-1$	219560.4	4	0.016	0.313	25.0
CS	$J = 3-2$	146969.0	11	0.143	2.658	18.4
	$J = 5-4$	244935.6	4	0.201	3.821	17.3
C <sup>33</sup> S	$J = 5-4$	242913.6	3	0.010	0.17:	...
C <sup>34</sup> S	$J = 5-4$	241016.1	3	0.025	0.485	21.2
<sup>13</sup> CS	$J = 5-4$	231221.0	4	0.013	0.325	33.5
C <sub>2</sub> H	$N = 3-2 J = 7/2-5/2$	262005.35	7	0.130	3.233	22.3
	$N = 3-2 J = 5/2-3/2$	262066.1	7	0.079	1.950	31.6
C <sub>4</sub> H	$N = 14-13 a$	133213.7	14	0.052	1.274	...
	$N = 14-13 b$	133252.1	14	0.035	1.100	...
	$N = 15-14 a$	142728.8	11	0.030	0.452	27.2
	$N = 15-14 b$	142767.3	11	0.029	0.553	27.3
	$N = 16-15 a$	152243.6	9	0.026	0.459	23.3
	$N = 16-15 b$	152282.1	9	0.029	0.508	27.7
	$N = 17-16 a$	161758.1	8	0.036	0.715	20.8
	$N = 17-16 b$	161796.6	8	0.041	0.716	22.2
	$N = 24-23 a$	228348.6	4	0.010	0.26:	...
	$N = 24-23 b$	228387.0	4	0.009	0.32:	...
c-C <sub>3</sub> H	$5(1,4)-4(1,3) 11/2-9/2$	252697.3	4	0.010	0.23:	...
	$5(1,4)-4(1,3) 9/2-8/2$	252881.0	4	0.010	0.31:	...
CH <sub>3</sub> CN	$J_K = 12_1-11_1$	220743.0*	4	0.014	0.291	13.2
	$J_K = 12_0-11_0$	220747.2*	4	...	...	...
	$J_K = 14_2-13_2$	257507.6*	4	0.015	0.264	26.0
	$J_K = 14_1-13_1$	257522.4*	4	...	...	...
	$J_K = 14_0-13_0$	257527.4*	4	...	...	...
CN	$N(J, F) = 2(3/2, 1/2)-1(3/2, 1/2)$	226287.4*	4	0.010	0.20:	...
	$N(J, F) = 2(3/2, 1/2)-1(3/2, 3/2)$	226298.9*	4	...	...	...
	$N(J, F) = 2(3/2, 3/2)-1(3/2, 1/2)$	226303.0*	4	...	...	...
	$N(J, F) = 2(3/2, 3/2)-1(3/2, 3/2)$	226314.5*	4	...	...	...
	$N(J, F) = 2(3/2, 3/2)-1(3/2, 5/2)$	226332.5*	4	0.015	0.594	22.5
	$N(J, F) = 2(3/2, 5/2)-1(3/2, 3/2)$	226341.9*	4	...	...	...
	$N(J, F) = 2(3/2, 5/2)-1(3/2, 5/2)$	226359.9*	4	...	...	...
	$N(J, F) = 2(3/2, 1/2)-1(1/2, 3/2)$	226616.6*	4	0.016	0.405	23.8
	$N(J, F) = 2(3/2, 3/2)-1(1/2, 3/2)$	226632.2*	4	...	...	...
	$N(J, F) = 2(3/2, 5/2)-1(1/2, 3/2)$	226659.6*	4	0.036	1.049	21.8
	$N(J, F) = 2(3/2, 1/2)-1(1/2, 1/2)$	226663.7*	4	...	...	...
	$N(J, F) = 2(3/2, 3/2)-1(1/2, 1/2)$	226679.3*	4	...	...	...
	$N(J, F) = 2(5/2, 5/2)-1(3/2, 3/2)$	226874.2*	4	0.088	2.399	21.9
	$N(J, F) = 2(5/2, 7/2)-1(3/2, 5/2)$	226874.8*	4	...	...	...
	$N(J, F) = 2(5/2, 3/2)-1(3/2, 1/2)$	226875.9*	4	...	...	...
	$N(J, F) = 2(5/2, 3/2)-1(3/2, 3/2)$	226887.4*	4	...	...	...
	$N(J, F) = 2(5/2, 5/2)-1(3/2, 5/2)$	226892.1*	4	...	...	...
	$N(J, F) = 2(5/2, 3/2)-1(3/2, 5/2)$	226905.4*	4	...	...	...
HCN	$J = 3-2$	265886.4	7	0.831	14.315	15.8
	$\nu_2=1^1e J = 3-2$	265852.8	7	0.034	0.401	11.5
	$\nu_2=2^0 J = 3-2$	267243.2	7	0.036	0.231	14.5
HC <sup>15</sup> N	$J = 3-2$	258154.7	4	0.014	0.233	22.3
H <sup>13</sup> CN	$J = 3-2$	259011.8	5	0.495	8.582	15.8
HN <sup>13</sup> C	$J = 3-2$	261263.4	7	0.021	0.445	23.7
HC <sub>3</sub> N	$J = 15-14$	136464.4	11	0.082	1.787	21.4
	$J = 16-15$	145560.9	10	0.053	0.953	21.4
	$J = 17-16$	154657.3	9	0.020	0.45:	...
	$J = 18-17$	163753.4	10	0.075	1.611	21.8
	$J = 25-24$	227418.9	4	0.027	0.530	20.5
	$J = 26-25$	236512.8	6	0.031	0.672	25.3
	$J = 27-26$	245606.3	4	0.031	0.541	21.3
	$J = 28-27$	254699.5	5	0.021	0.485	19.3
	$J = 29-28$	263792.3	6	0.021	0.310	26:
SiC <sub>2</sub>	$6_{0,6}-5_{0,5}$	137180.8	10	0.022	0.424	21:
	$6_{2,5}-5_{2,4}$	140920.1	9	0.025	0.483	20:
	$6_{2,4}-5_{2,3}$	145325.8	9	0.029	0.560	20.6
	$7_{0,7}-6_{0,6}$	158499.2	7	0.033	0.617	25.0

**Table 1**  
(Continued)

Species (MHz)	Transition	Frequency <sup>a</sup> (Upper–Lower)	rms (mK)	$T_R$ (K)	$\int T_R dv^b$ (K km s <sup>-1</sup> )	$\Delta V_{FWHM}$ (km s <sup>-1</sup> )
	10 <sub>0,10</sub> –9 <sub>0,9</sub>	220773.7	4	0.019	0.380	18.3
	9 <sub>2,7</sub> –8 <sub>2,6</sub>	222009.4	5	0.022	0.400	29.0
	10 <sub>2,9</sub> –9 <sub>2,8</sub>	232534.1	4	0.018	0.411	29.7
	10 <sub>8,2</sub> –9 <sub>8,1</sub>	234534.0*	6	0.012	0.222	29.3
	10 <sub>8,3</sub> –9 <sub>8,2</sub>	234534.0*	6	...	...	...
	10 <sub>6,5</sub> –9 <sub>6,4</sub>	235713.0*	5	0.024	0.415	15:
	10 <sub>6,4</sub> –9 <sub>6,3</sub>	235713.1*	5	...	...	...
	10 <sub>4,7</sub> –9 <sub>4,6</sub>	237150.0	5	0.019	0.417	30:
	10 <sub>4,6</sub> –9 <sub>4,5</sub>	237331.3	5	0.024	0.35:	15:
	11 <sub>0,11</sub> –10 <sub>0,10</sub>	241367.7	3	0.020	0.439	18.6
	10 <sub>2,8</sub> –9 <sub>2,7</sub>	247529.1	5	0.022	0.544	22.8
	11 <sub>2,10</sub> –10 <sub>2,9</sub>	254981.5	5	0.030	0.466	28:
	11 <sub>8,3</sub> –10 <sub>8,2</sub>	258065.0*	4	0.014	0.189	16.2
	11 <sub>8,4</sub> –10 <sub>8,3</sub>	258065.0*	4	...	...	...
	11 <sub>6,6</sub> –10 <sub>6,5</sub>	259433.3*	5	0.019	0.502	23.0
	11 <sub>6,5</sub> –10 <sub>6,4</sub>	259433.3*	5	...	...	...
	11 <sub>4,8</sub> –10 <sub>4,7</sub>	261150.7	7	0.016	0.33:	...
	11 <sub>4,7</sub> –10 <sub>4,6</sub>	261509.3	7	0.015	0.28:	22.4
	12 <sub>0,12</sub> –11 <sub>0,11</sub>	261990.7\$	7	0.130	3.233	22.3
SiO	$J = 3-2$	130268.6	12	0.026	0.976	22.1
	$J = 6-5$	260518.0	7	0.034	0.537	15.7
SiS	$J = 8-7$	145227.0	9	0.078	1.517	20.3
	$J = 9-8$	163376.7	10	0.119	2.127	19.5
	$J = 13-12$	235961.1	6	0.101	2.188	18.8
	$J = 14-13$	254102.9	5	0.121	2.265	18.4
<sup>29</sup> SiS	$J = 13-12$	231626.7	4	0.013	0.243	30:
<sup>30</sup> SiS	$J = 9-8$	157579.7	9	0.025	0.44:	...
	$J = 15-14$	262585.0	7	0.021	0.101	19.4
U		245982.0	5	0.017	0.605	14.7
		255108.0	5	0.041	0.817	16.0
		264067.0	5	0.016	0.175	13.9

**Notes.**

<sup>a</sup> (\*) Unsolved hyperfine-structure lines; (\$) blended with other species.

<sup>b</sup> The colon indicates uncertain detections. The pointing uncertainties induced errors are up to 20%–30%.

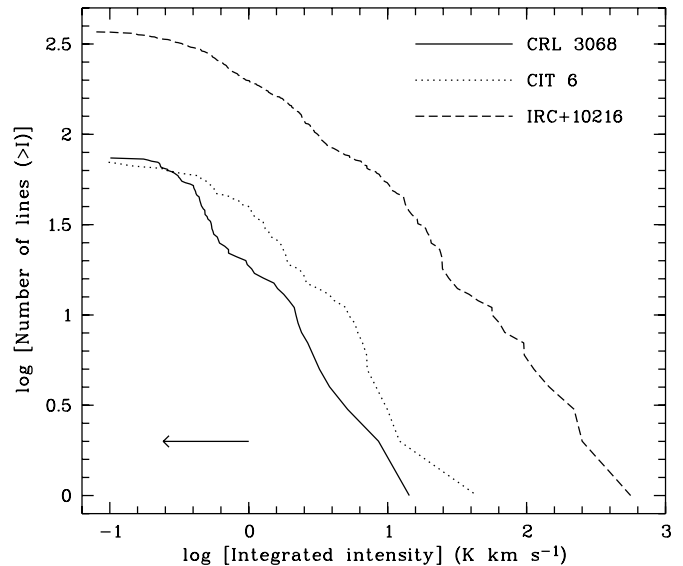
lar envelopes (see Busso 2006, for a recent review). Extensive observations have shown that the isotopic composition in carbon-rich stars is remarkably nonsolar (e.g., Cernicharo et al. 2000), providing substantial tests for nucleosynthesis theory of AGB stars. Such nonsolar isotopic ratios also make possible the identification of stellar solid-state materials in the solar system (Zinner 1998).

In Table 3, we give the isotopic ratios (or their lower limits) of carbon, oxygen, nitrogen, sulfur, and silicon in the extreme carbon star, CRL 3068. This table also lists the isotopic ratios for CIT 6, IRC+10216, and the Sun. A comparison of isotopic ratios in these objects allows us to study the nucleosynthesis and dredge-up processes in diverse physical conditions.

5.1.1. Carbon

The <sup>12</sup>C/<sup>13</sup>C isotopic ratio is a good indicator of interior nucleosynthesis processing. The dredge-up processes can greatly enhance <sup>13</sup>C in the surface. Moreover, the cool bottom processing and hot bottom burning can further decrease the <sup>12</sup>C/<sup>13</sup>C ratio (e.g., Boothroyd & Sackmann 1999; Frost et al. 1998).

We detected three <sup>13</sup>C-bearing species, <sup>13</sup>CO, <sup>13</sup>CS, and H<sup>13</sup>CN. However, the CO/<sup>13</sup>CO, CS/<sup>13</sup>CS, and HCN/H<sup>13</sup>CN ratios only give lower limits of the <sup>12</sup>C/<sup>13</sup>C because the main lines appear to be optically thick. On the other hand, if the <sup>32</sup>S/



**Figure 3.** Cumulative number of observed lines exceeding a given value. The spectra of IRC+10216 and CIT 6 are from He et al. (2008) and Zhang et al. (2009), respectively. All the spectra were obtained using the same telescope settings in the same frequency ranges. If the distance to an object is increased by a factor of 2, the curve would move toward left by a length denoted by the shaft of the arrow in the lower left-hand corner.



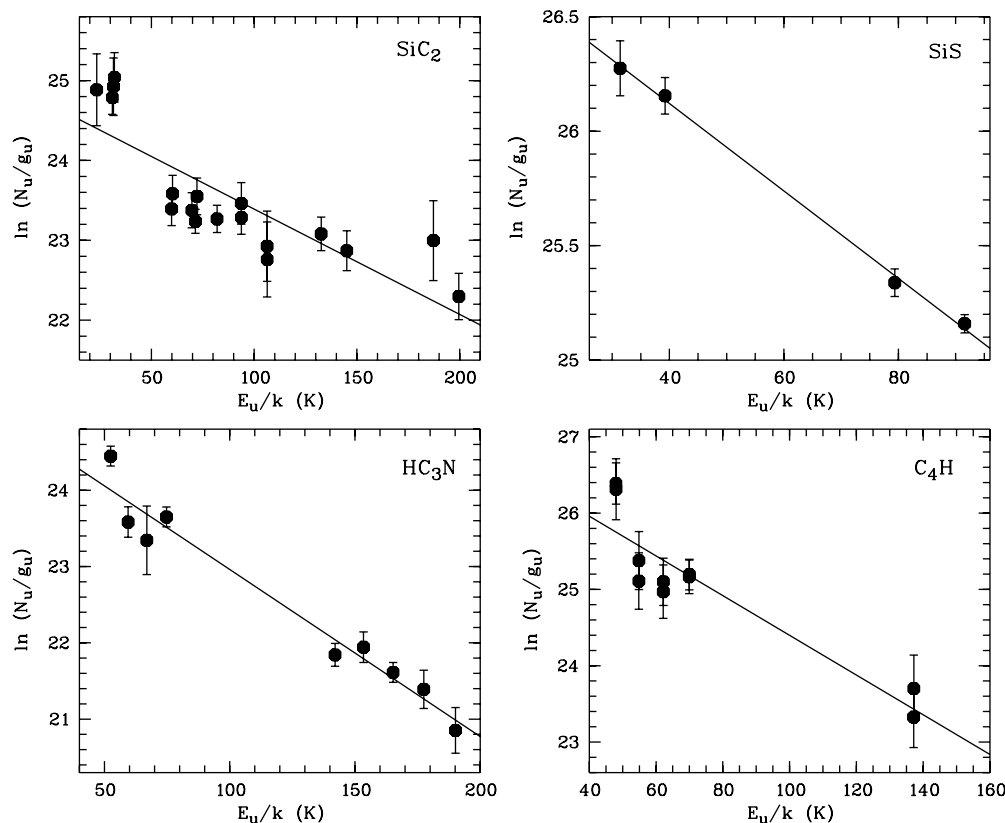


Figure 4. Rotational diagrams for the detected species in CRL 3068.

$^{34}\text{S}$  isotopic ratio were known, we could use the optically thin  $^{13}\text{CS}$  and  $\text{C}^{34}\text{S}$  lines to obtain the  $^{12}\text{C}/^{13}\text{C}$  ratio. Based on the fact that the nucleosynthesis in AGB stars is expected not to affect the abundances of sulfur isotopologues and that Cernicharo et al. (2000) have found the sulfur isotopic ratio in IRC+10216 to be close to solar, we can reasonably assume that the  $^{32}\text{S}/^{34}\text{S}$  ratio in CRL 3068 is solar (22.5). From this assumption, we obtained a  $^{12}\text{C}/^{13}\text{C}$  ratio of 29.7. Using a full radiative transfer analysis of  $^{12}\text{CO}$  and  $^{13}\text{CO}$  line emission, Woods et al. (2003) derived the  $^{12}\text{C}/^{13}\text{C}$  ratio of 30, lending strong support to our result. The  $^{12}\text{C}/^{13}\text{C}$  ratio in CRL 3068 is significantly lower than the solar value, suggesting the presence of extra mixing processes.

As a consequence of dredge-up processes, the C/O abundance ratio in circumstellar envelopes decreases along with the  $^{12}\text{C}/^{13}\text{C}$  ratio. As shown in Table 3, the  $^{12}\text{C}/^{13}\text{C}$  ratio in CRL 3068 is about a factor of 1.5 lower than those found in CIT 6 and IRC+10216, suggesting that CRL 3068 has a higher C/O ratio. Our observations, therefore, provide an opportunity to study circumstellar chemistry in an extremely carbon-rich environment.

### 5.1.2. Nitrogen

As a star ascends the AGB, the  $^{14}\text{N}$ -rich and  $^{15}\text{N}$ -poor material processed by the CNO cycle in the intershell is dredged up to the stellar surface, resulting in a high  $^{14}\text{N}/^{15}\text{N}$  abundance ratio in the envelope. Wannier et al. (1991) determined the lower limits of  $^{14}\text{N}/^{15}\text{N}$  in a sample of carbon stars and found that in most of the cases they were larger than the terrestrial ratio.

The nitrogen isotopologue,  $^{15}\text{N}$ , has been detected through a faint emission line from  $\text{HC}^{15}\text{N}$ . As its main line is optically thick, the  $\text{HC}^{14}\text{N}/\text{HC}^{15}\text{N}$  abundance ratio gives a lower limit of the isotopic ratio of 45. The optically thin species  $\text{H}^{13}\text{C}^{14}\text{N}$  and  $\text{H}^{12}\text{C}^{15}\text{N}$  may also be applied to derive the  $^{14}\text{N}/^{15}\text{N}$  ratio.

Assuming a  $^{12}\text{C}/^{13}\text{C}$  ratio of 29.7 (see above), we obtained the  $^{14}\text{N}/^{15}\text{N}$  ratio of 1099, a factor of 4 higher than the solar value. Wannier et al. (1991) obtained a lower limit of  $^{14}\text{N}/^{15}\text{N} > 500$  for CRL 3068, in good agreement with our result. The deduced nitrogen isotopic ratio is in accord with the predictions of stellar models.

### 5.1.3. Oxygen

Nucleosynthesis models predict enhancement of  $^{17}\text{O}$  in the circumstellar envelopes around carbon stars (Busso 2006). Previous observations have shown that the  $\text{C}^{17}\text{O}/\text{C}^{18}\text{O}$  ratios in carbon-rich envelopes are significantly higher than the terrestrial and interstellar values (Wannier & Sahai 1987; Kahane et al. 1992).

The weak  $\text{C}^{18}\text{O}$  and  $\text{C}^{17}\text{O}$  (2–1) transitions were detected in our survey, allowing us to determine the oxygen isotopic ratios in CRL 3068. The abundance ratios of CO and its isotopologues give lower limits of isotopic ratios, as can be seen in Table 3. Under the assumption of  $^{12}\text{C}/^{13}\text{C} = 29.7$ , we used the optically thin species  $^{13}\text{CO}$ ,  $\text{C}^{18}\text{O}$ , and  $\text{C}^{17}\text{O}$  to obtain the  $^{16}\text{O}/^{17}\text{O}$ ,  $^{16}\text{O}/^{18}\text{O}$ , and  $^{17}\text{O}/^{18}\text{O}$  ratios of 668, 472, and 0.7, respectively. The  $^{16}\text{O}/^{17}\text{O}$  and  $^{17}\text{O}/^{18}\text{O}$  ratios bear a large uncertainty, but clearly point to an enhancement of  $^{17}\text{O}$ . The  $^{16}\text{O}/^{18}\text{O}$  ratio is comparable with the solar value. These isotopic ratios are well within the ranges reported by Kahane et al. (1992) for a sample of carbon-rich envelopes.

### 5.1.4. Sulfur and Silicon

The isotopic compositions of sulfur and silicon are hardly affected by nucleosynthesis of AGB stars although they might be slightly changed by neutron capture. This is consistent with the observations that the S and Si isotopic ratios in IRC+10216

**Table 2**Excitation Temperatures, Column Densities, and Abundances Respect to H<sub>2</sub><sup>d</sup>

Species	$T_{\text{ex}}$ (K) <sup>b</sup>	$N$ (cm <sup>-2</sup> )		$f_X$	
		This Paper <sup>c</sup>	F94 <sup>d</sup>	This paper <sup>c</sup>	W03 <sup>d</sup>
CO	...	6.20(16)	...	1.5(-4)	...
<sup>13</sup> CO	...	1.17(16)	...	2.7(-5)	...
C <sup>17</sup> O	...	5.58(14):	...	1.2(-6):	...
C <sup>18</sup> O	...	7.66(14)	...	1.7(-6)	...
CS	...	3.24(13)	...	5.8(-8)	3.7(-7)
C <sup>33</sup> S	...	1.38(12):	...	2.7(-9):	...
C <sup>34</sup> S	...	3.95(12)	...	7.8(-9)	...
<sup>13</sup> CS	...	2.91(12)	...	5.9(-9)	...
C <sub>2</sub> H	...	1.82(14)	1.5 ± 1.1(14)	2.7(-7)	5.7(-6)
C <sub>4</sub> H	38 ± 18	3.52(14)	7.0(14)	6.5(-7)	...
<i>c</i> -C <sub>3</sub> H	...	1.78(13):	...	3.6(-8):	...
CH <sub>3</sub> CN	...	5.77(12)	...	8.1(-8)	< 1.2(-7)
CN	...	1.93(14)	...	3.9(-7)	4.6(-7)
HCN	...	4.17(13)	6.0(14)	4.5(-8)	6.3(-6)
HC <sup>15</sup> N	...	5.49(11)	...	1.0(-9)	...
H <sup>13</sup> CN	...	2.01(13)	...	3.7(-8)	3.0(-8)
HN <sup>13</sup> C	...	1.26(12)	...	2.3(-9)	< 1.4(-8)
HC <sub>3</sub> N	46 ± 15	1.78(13)	1.9 ± 1.7(14)	3.5(-8)	5.0(-7)
SiC <sub>2</sub>	76 ± 36	3.49(13)	...	3.8(-8)	< 7.5(8)
SiO	...	1.64(12)	...	3.0(-9)	...
SiS	52 ± 16	5.69(13)	5.4 ± 9.0(13)	1.5(-7)	6.7(-7)
<sup>29</sup> SiS	...	6.38(12)	...	1.3(-8)	...
<sup>30</sup> SiS	...	2.83(12)	...	5.2(-9)	...

**Notes.**<sup>a</sup>  $x(y)$  represents  $x \times 10^y$ .<sup>b</sup> A constant excitation temperature of 53 K was assumed for the species for which the rotation diagrams cannot be obtained.<sup>c</sup> For the species with optically thick emission (e.g., CO and HCN), this gives the lower limits.<sup>d</sup> F94: from Fukasaku et al. (1994); W03: from Woods et al. (2003).

and CIT 6 are close to the solar values (Cernicharo et al. 2000; Zhang et al. 2009).

We detected the S and Si isotopologues <sup>33</sup>S, <sup>34</sup>S, <sup>29</sup>SiS, and <sup>30</sup>SiS in CRL 3068. The main line CS (3–2) is optically thick, while the few SiS transitions are likely to be optically thin. Consequently, we derived the <sup>33</sup>S/<sup>34</sup>S, <sup>29</sup>Si/<sup>30</sup>Si, <sup>28</sup>Si/<sup>30</sup>Si, and <sup>28</sup>Si/<sup>29</sup>Si ratios, and the lower limit of the <sup>32</sup>S/<sup>34</sup>S ratio, as listed in Table 3. In IRC+10216 and CIT 6, the Si isotopic ratios were also obtained from the SiO and SiC<sub>2</sub> isotopologues (He et al. 2008; Zhang et al. 2009), which, however, were not detected in the spectra of CRL 3068. We found that these S and Si isotopic ratios are compatible with the solar values, and there is no significant deviation between the S and Si isotopic ratios in CRL 3068 and those in IRC+10216 and CIT 6.

### 5.2. Remarks on the Comparison between CRL 3068 and IRC+10216

CRL 3068 and IRC+10216 are the prototypes of extreme carbon stars, which are highly evolved heavily obscured by thick dust shells (Volk et al. 1992). Nevertheless, there exist some differences between the two objects. CRL 3068 has a colder IR color temperature than IRC+10216 (e.g., see Omont et al. 1993). Based on the *ISO* observations, Justtanont et al. (1998) have determined the color temperatures of CRL 3068 and IRC+10216 to be of 320 and 540 K, respectively. The *ISO* spectra show that the SiC 11.3 μm feature exhibits a weak flat-topped emission profile in IRC+10216 while in CRL 3068 it is in absorption. This suggests either that CRL 3068 has a thicker

**Table 3**

Isotopic Abundance Ratios

Isotopic Ratio	CRL 3068		CIT 6 <sup>a</sup>	IRC+10216 <sup>b</sup>	Solar <sup>c</sup>
	Species	Value			
<sup>12</sup> C/ <sup>13</sup> C	<sup>12</sup> C <sup>34</sup> S/ <sup>13</sup> C <sup>32</sup> S	29.7 <sup>d</sup>	45.4	45	89
	<sup>12</sup> CO/ <sup>13</sup> CO	5.6 <sup>e</sup>	...	...	...
	<sup>12</sup> CS/ <sup>13</sup> CS	9.8 <sup>e</sup>	...	...	...
<sup>14</sup> N/ <sup>15</sup> N	H <sup>12</sup> CN/H <sup>13</sup> CN	1.2 <sup>e</sup>	...	...	...
	H <sup>13</sup> C <sup>14</sup> N/H <sup>12</sup> C <sup>15</sup> N	1099 <sup>f</sup>	...	...	272
	HC <sup>14</sup> N/HC <sup>15</sup> N	45 <sup>e</sup>	...	...	...
<sup>16</sup> O/ <sup>17</sup> O	<sup>13</sup> C <sup>16</sup> O/ <sup>12</sup> C <sup>17</sup> O	668: <sup>f</sup>	890	967	2680
	C <sup>16</sup> O/C <sup>17</sup> O	125: <sup>e</sup>	...	...	...
<sup>16</sup> O/ <sup>18</sup> O	<sup>13</sup> C <sup>16</sup> O/ <sup>12</sup> C <sup>18</sup> O	472 <sup>f</sup>	...	1172	499
	C <sup>16</sup> O/C <sup>18</sup> O	88 <sup>e</sup>	...	...	...
<sup>17</sup> O/ <sup>18</sup> O	C <sup>17</sup> O/C <sup>18</sup> O	0.7:	...	1.14	0.2
<sup>32</sup> S/ <sup>34</sup> S	C <sup>32</sup> S/C <sup>34</sup> S	7.4 <sup>e</sup>	6.7 <sup>e</sup>	18.9	22.5
<sup>33</sup> S/ <sup>34</sup> S	C <sup>33</sup> S/C <sup>34</sup> S	0.3:	0.2:	0.19	0.18
<sup>29</sup> Si/ <sup>30</sup> Si	<sup>29</sup> SiS/ <sup>30</sup> SiS	2.5	1.0	1.46	1.52
<sup>28</sup> Si/ <sup>30</sup> Si	<sup>28</sup> SiS/ <sup>30</sup> SiS	28.8	8.8 <sup>e</sup>	24.7	29.9
<sup>28</sup> Si/ <sup>29</sup> Si	<sup>28</sup> SiS/ <sup>29</sup> SiS	11.5	8.9 <sup>e</sup>	17.2	19.6

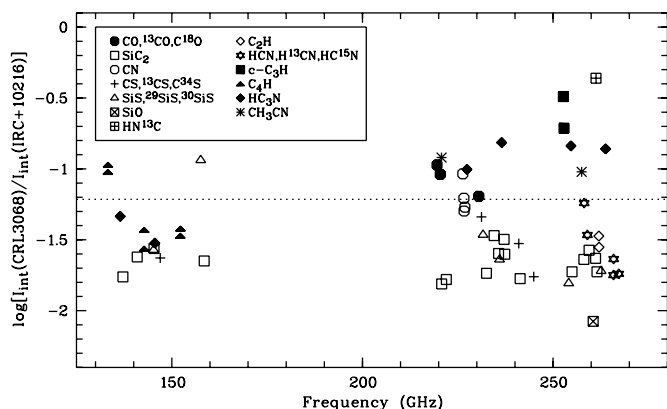
**Notes.**<sup>a</sup> From Zhang et al. (2009).<sup>b</sup> From He et al. (2008) except the <sup>12</sup>C/<sup>13</sup>C ratio which was taken from Cernicharo et al. (2000).<sup>c</sup> From Lodders (2003).<sup>d</sup> Assume that the <sup>34</sup>S/<sup>32</sup>S ratio is solar.<sup>e</sup> Should be treated as lower limits due to opacity effect.<sup>f</sup> Adopted: <sup>12</sup>C/<sup>13</sup>C = 29.7.

dust envelope, or the abundance of the SiC grains is higher. Both the color temperature comparison and the SiC feature are consistent with the suggestion that CRL 3068 is in an even more evolved state than IRC+10216.

In Figure 5, we compare the integrated-intensity ratios of the lines detected in CRL 3068 and IRC+10216. The average line ratio between the two objects is 0.06 with a standard deviation of 0.07. While there is a large scatter of ratios between species, for individual species the ratios are quite consistent. For example, the intensity ratios of SiC<sub>2</sub> lines have an average of 0.022 with a standard deviation of 0.005. Note that in this analysis, we have not taken into account the beam dilution effect. Using the same method in Zhang et al. (2009) and assuming that CRL 3068 and IRC+10216 have diameters of 22'' and 30'', respectively, we estimate that these intensity ratios would increase by a factor of 1.6 and 1.4 for the ARO 12 m and the SMT data, respectively, if the beam dilution effect is corrected for.<sup>5</sup> CRL 3068 is about 8–10 times more distant than IRC+10216, and thus might intrinsically have a stronger average line intensity when the distance factor is taken into account.

Referring to Figure 5, if taking the average line intensity ratio as a reference, one can find that the emission from SiO, SiC<sub>2</sub>, SiS, CS, HCN, and their isotopologues seems to be depleted in CRL 3068 compared to those in IRC+10216, while HN<sup>13</sup>C, *c*-C<sub>3</sub>H, HC<sub>3</sub>N, and CH<sub>3</sub>CN might be enhanced. The situation for other species is ambiguous. Although the classification is not very strict, it reflects that CRL 3068 has different chemical compositions, excitation conditions, and optical depths with IRC+10216. A detailed discussion of the implication for circumstellar chemistry will be given in the following section.

<sup>5</sup> According to the modeling by Woods et al. (2003), CRL 3068 has almost same CO envelope size as IRC+10216. If this is the case, the intensity ratios are not affected by the beam dilution effect.



**Figure 5.** Integrated-intensity ratios of the lines detected in CRL 3068 and those detected in IRC+10216. The dotted line represents the average value.

Our results are in contrast to that presented in Woods et al. (2003), who found that for a sample of carbon-rich circumstellar envelopes, the abundance discrepancies are typically less than a factor of 5 and the two objects, IRC+10216 and CRL 3068, are chemically similar. However, in CRL 3068, Woods et al. (2003) did not detect the species having the largest abundance discrepancies found here (e.g., SiO and *c*-C<sub>3</sub>H). Recent studies of SiO and SiS in samples of carbon stars have been presented by Schöier et al. (2006, 2007), who determined the molecular abundances through a detailed radiative transfer modeling of the SiO and SiS lines observed by them and some other authors. Their results suggest that the fractional abundances of SiO and SiS in carbon stars are in good agreement with each other. If the SiO and SiS abundances in CRL 3068 are similar to those in IRC+10216, our observations would suggest a significant enhancement of carbon chain molecules in CRL 3068, as shown in Figure 5. Nevertheless, we cannot completely rule out the possibility that the Si-bearing molecules in CRL 3068 are actually depleted.

### 5.3. Implication for Circumstellar Chemistry

The spectra of CRL 3068 are characterized by the wealth of C-bearing molecules. Among the newly detected species, only two are non-C-bearing molecules (SiO and SiS). From Figure 5, we can see that CRL 3068 has generally higher intensity ratios of C-bearing molecular lines to non-C-bearing ones compared to IRC+10216. This seems to lend support to the idea that CRL 3068 is more evolved and more carbon rich than IRC+10216.

It is intriguing that according to Figure 5 CRL 3068 shows enhancement of HN<sup>13</sup>C and depletion of H<sup>13</sup>CN compared to IRC+10216. Assuming that carbon isotope fractionation is insignificant for the two species and the HN<sup>13</sup>C/HNC abundance ratio is equal to the H<sup>13</sup>CN/HCN abundance ratio, we can infer that CRL 3068 has a higher HNC/HCN abundance ratio than IRC+10216. The HN<sup>13</sup>C (3–2)/H<sup>13</sup>CN (3–2) integrated-intensity ratio in CRL 3068 is 0.05, about an factor of 13 larger than the value in IRC+10216 (see He et al. 2008). HCN and HNC can be produced through a similar way, i.e., dissociative recombination of HCNH<sup>+</sup>, and can convert to each other at certain physical conditions. At high temperature, HNC can be reprocessed into HCN through hydrogen exchange reaction. Hence, the higher HNC abundance in CRL 3068 might be related to its extreme cold environment. Furthermore, HNC can

be destroyed by atomic oxygen through the reaction



Therefore, the higher HNC/HCN abundance ratio probably reflects the extremely carbon-rich nature of CRL 3068. Schilke et al. (1992) suggest that the HNC/HCN abundance increases with increasing dust depletion factor because reaction (1) can be suppressed as a result of freezeout of heavy elements onto dust grains. If this is the case, the extreme carbon star CRL 3068 may have a larger dust depletion factor than IRC+10216. Our observations also suggest that the column density ratio of HNC/HCN in CRL 3068 is about 1 order magnitude lower than that in PNe (Josselin & Bachiller 2003). This is consistent with the observations of Herpin et al. (2002) who found that HNC is enhanced with respect to HCN at post-AGB stage due to certain chemical processes in the photodissociation region.

The chemical processes of CN are interconnected with those of HCN and HNC. CN can be produced through photodissociation of HCN or HNC. On the other hand, CN can be reprocessed into HCN or HNC through reaction with molecular hydrogen. Very efficient photodissociation has been found in the highly evolved AGB envelope CIT 6 (Zhang et al. 2009). In CRL 3068, we do not find evidence showing enhancement of CN. C<sub>2</sub>H and HC<sub>3</sub>N can be reprocessed by the same chemical precursor, C<sub>2</sub>H<sub>2</sub><sup>+</sup>. The abundance ratio of the two species can provide a test for the chemical formation path (Wootten et al. 1980). We found that the abundance ratio  $f(\text{C}_2\text{H})/f(\text{HC}_3\text{N})$  in CRL 3068 is 7.7, lying within the range of 3–10 found by Wootten et al. (1980) in a wide variety of interstellar clouds and being consistent with gas-phase reaction scheme.

Among the most interesting finding in this study is the discovery of the cyclic molecule *c*-C<sub>3</sub>H in CRL 3068. This follows the detection of another cyclic molecule C<sub>3</sub>H<sub>2</sub> in this source by Wannier et al. (1991). We further note that HC<sub>3</sub>N and CH<sub>3</sub>CN seem to be slightly enhanced in CRL 3068. In the protoplanetary nebula (PPN) CRL 618, cyanopolyynes chains are formed through the polymerization of HCN (Pardo et al. 2005). Our observations lead us to believe that CRL 3068 may be more evolved than IRC+10216 and cyclic and longer chain molecules are quickly being synthesized in its envelope. Since aromatic molecules emerge shortly after the end of the AGB (Kwok 2004), the possible role that ring and chain molecules play in the synthesis of aromatic compounds is an important question in the study of circumstellar chemistry.

The interaction between stellar winds from AGB stars usually forms shock waves. Woods et al. (2003) have found that shocks alter the chemical compositions (e.g., CS and SiO) in the inner regions of some AGB envelopes. According to a non-equilibrium chemical model presented by Willacy & Cherchneff (1998), shocks can also strongly enhance SiO, which is a commonly observed species in carbon-rich envelopes. However, we do not find enhancement of SiO in CRL 3068, probably suggesting that freezeout onto dust grains is significant in the extremely carbon-rich envelope.

## 6. SUMMARY AND CONCLUSIONS

In this molecular line survey toward the extreme carbon star CRL 3068 in the  $\lambda$  1.3 mm and  $\lambda$  2 mm windows, 72 molecular lines from 23 species were detected with three lines remain unidentified. The spectra are dominated by carbon-bearing molecules. The species *c*-C<sub>3</sub>H, CH<sub>3</sub>CN, SiC<sub>2</sub>, C<sup>17</sup>O, C<sup>18</sup>O, HC<sup>15</sup>N, HN<sup>13</sup>C, C<sup>33</sup>S, C<sup>34</sup>S, <sup>13</sup>CS, <sup>29</sup>SiS, and <sup>30</sup>SiS are de-

ected for the first time in this object. From these observations, we have derived the chemical abundances and isotopic ratios of the molecular species. A comparison between these observations with the spectra of other AGB envelopes obtained previously using the same observations settings allows us to rigorously investigate the chemical processes in circumstellar envelopes. Compared to the archetypal carbon star IRC+10216, CRL 3068 is more carbon rich and shows an enhancement of  $c\text{-C}_3\text{H}$  and  $\text{HN}^{13}\text{C}$ . The overall assessment is that CRL 3068 is a more evolved object on the AGB than IRC+10216. However, it should bear in mind that our conclusions are mainly based upon the comparison of relative line intensities which are assumed to directly correspond to the molecular abundances. To obtain more reliable absolute abundances and to make stronger statements about the chemical evolution in circumstellar envelopes, interferometric observations and sophisticated treatments of radiative transfer processes are required.

This study is a part of a long-term project of investigating the evolution of circumstellar chemistry in the late stages of stellar evolution using the  $\lambda$  2 mm and  $\lambda$  1.3 mm spectra of a sample of AGB stars, PPNe, and PNe. Such a systematic study of the gas-phase molecules presents an important step to understand the synthesis of more complex aromatic and aliphatic compounds in evolved stars, and their role in the distribution of organic compounds throughout the Galaxy (Kwok 2009). A detailed study of chemical processes in different physical conditions and evolutionary stages will be reported in the future.

The 12 m telescope and the SMT are operated by the Arizona Radio Observatory (ARO), Steward Observatory, University of Arizona. Y.Z. thanks the ARO staff for their hospitality during his stay at Kitt Peak and Mt. Graham. J.N. acknowledges financial support from Seed Funding Program for Basic Research in HKU (200802159006). The work was supported by the Research Grants Council of the Hong Kong under grants HKU7020/08P and HKU7033/08P. We also thank the anonymous referee for many helpful comments.

## APPENDIX

### OLOFSSON FORMULA FOR MOLECULAR ABUNDANCE

For the reader's convenience, we deduce the formula presented by Olofsson (1996) for the calculation of molecular abundances respect to  $\text{H}_2$ . The basic assumptions include: (1) all molecular emission originates from a spherical shell with inner radius  $r_i$  and outer radius  $r_e$ ; (2) the expansion velocity  $v_e$ , the mass-loss rate  $\dot{M}$ , and the excitation temperature  $T_{\text{ex}}$  are constant along the radius; and (3) the molecular abundance respect to  $\text{H}_2$  is homogeneous in the envelope.

For a Gaussian beam measuring a molecular line, the main beam temperature at a given velocity is obtained by

$$\begin{aligned} T_R(v) &= \frac{\int \exp\left(-\frac{4\ln 2}{\theta_b^2} p^2\right) T_s(v, p) d\Omega}{\int \exp\left(-\frac{4\ln 2}{\theta_b^2} p^2\right) d\Omega} \\ &= \frac{8\ln 2}{\theta_b^2} \int \exp\left(-\frac{4\ln 2}{\theta_b^2} p^2\right) T_s(v, p) p dp, \quad (\text{A1}) \end{aligned}$$

where  $p$  is the angular distance to the center,  $\theta_b$  is the HPBW, and  $T_s(v, p)$  is the source brightness temperature at  $v$  and  $p$ . For a given volume element at a distance to the center of the

envelope  $r$ , we have

$$p = \frac{r}{D} \sqrt{1 - (v/v_e)^2}, \quad (\text{A2})$$

where  $D$  is the distance between the antenna and the source and  $v$  is the velocity along the line of sight. From the radiative transfer equation, the source brightness temperature is given by

$$T_s(v, p) = T_{\text{ex}}[1 - e^{-\tau(v, p)}], \quad (\text{A3})$$

where  $\tau(v, p)$  is the optical depth. Substituting Equations (A2) and (A3) into Equation (A1), we have

$$\begin{aligned} T_R(v) &= 8\ln 2 T_{\text{ex}} \int_{x_i}^{x_e} e^{-4\ln 2[1-(v/v_e)^2]x^2} [1 - (v/v_e)^2] \\ &\quad \times [1 - e^{-\tau(v, x)}] x dx, \quad (\text{A4}) \end{aligned}$$

where we have defined  $x = r/(\theta_b D)$  and thus  $x_{i,e} = r_{i,e}/(\theta_b D)$ . According to radiative transfer equation,  $\tau(v, x)$  is given by

$$\tau(v, x) = \frac{c^3 g_u A_{ul} n(x)}{8\pi \delta v v^3 Q(T_{\text{ex}})} (1 - e^{-h\nu/kT_{\text{ex}}}) e^{-E_l/kT_{\text{ex}}} \delta z, \quad (\text{A5})$$

where  $g_u$  is the weight of the upper level,  $A_{ul}$  is the Einstein coefficient,  $h$  is the Planck constant,  $k$  the Boltzmann's constant,  $\nu$  is the line frequency,  $n(x)$  is the number density of the species,  $Q(T_{\text{ex}})$  is the partition function,  $E_l$  is the energy of lower level, and  $\delta z$  is the path length element along the line of sight. From the relation  $z = r(v/v_e) = Dp[1 - (v/v_e)^2]^{-0.5}(v/v_e)$ , we have

$$\delta z = \frac{Dp}{v_e} [1 - (v/v_e)^2]^{-1.5} \delta v = \frac{r}{v_e} [1 - (v/v_e)^2]^{-1} \delta v. \quad (\text{A6})$$

From Equations (A5) and (A6), we obtain

$$\tau(v, x) = \frac{n(x)x}{n(1)} [1 - (v/v_e)^2]^{-1} \tau(0, 1), \quad (\text{A7})$$

where

$$\tau(0, 1) \approx \frac{hc^3 g_u A_{ul} n(1) \theta_b D}{8\pi k v^2 v_e T_{\text{ex}} Q(T_{\text{ex}})} e^{-E_l/kT_{\text{ex}}}. \quad (\text{A8})$$

The number density for a molecular species is given by

$$n(r) = \frac{f_X \dot{M}_{\text{H}_2}}{m_{\text{H}_2} v_e r^2},$$

or

$$n(x) = \frac{f_X \dot{M}_{\text{H}_2}}{m_{\text{H}_2} v_e} \frac{1}{(x\theta_b D)^2}, \quad (\text{A9})$$

where  $f_X$  is the abundance relative to  $\text{H}_2$ ,  $m_{\text{H}_2}$  is the mass of a hydrogen molecule, and  $\dot{M}_{\text{H}_2}$  is the mass-loss rate for  $\text{H}_2$ . Substituting Equations (A7)–(A10) into Equation (A4) and assuming  $\tau(v, x) \ll 1$ , we obtain the molecular abundance relative to  $\text{H}_2$

$$f_X \approx \frac{\pi}{2\ln 2} \frac{km_{\text{H}_2}}{hc^3} \frac{v_e \theta_b D}{\dot{M}_{\text{H}_2}} \frac{Q(T_{\text{ex}}) v_{\text{ul}}^2}{g_u A_{ul}} \frac{e^{E_l/kT_{\text{ex}}}}{\int_{x_i}^{x_e} e^{-4x^2 \ln 2} dx}. \quad (\text{A10})$$

## REFERENCES

- Avery, L. W., et al. 1992, *ApJS*, **83**, 363
- Bachiller, R., Fente, A., Bujarrabal, V., Colomer, F., Loup, C., Omont, A., & de Jong, T. 1997, *A&AS*, **319**, 235
- Boothroyd, A. I., & Sackmann, I.-J. 1999, *ApJ*, **510**, 232
- Bujarrabal, V., Fuente, A., & Omont, A. 1994, *A&A*, **285**, 247
- Busso, M. M. 2006, in IAU Symp. 234, Planetary Nebulae, ed. M. J. Barlow & R. H. Méndez (Cambridge: Cambridge Univ. Press), 91
- Cernicharo, J., Guélin, M., & Kahane, C. 2000, *A&AS*, **142**, 181
- Clément, D., Mutschke, H., Klein, R., & Henning, Th. 2003, *ApJ*, **594**, 642
- Frost, C. A., Cannon, R. C., Lattanzio, J. C., Wood, P. R., & Forestini, M. 1998, *A&A*, **332**, L17
- Fukasaku, S., et al. 1994, *ApJ*, **437**, 410
- Gérard, E., & Le Bertre, T. 2006, *AJ*, **132**, 2566
- Groenewegen, M. A. T., Baas, F., de Jong, T., & Loup, C. 1996, *A&A*, **306**, 241
- Habing, H. J., & Olofsson, H. (ed.), 2003, *Asymptotic Giant Branch Stars* (New York: Springer)
- He, J.-H., Dinh-V-Trung Kwok, S., Müller, H. S. P., Zhang, Y., Hasegawa, T., Peng, T. C., & Huang, Y. C. 2008, *ApJS*, **177**, 275
- Herpin, F., Goicoechea, J. R., & Cernicharo, J. 2002, *ApJ*, **577**, 961
- Jewell, P. R., & Snyder, L. E. 1984, *ApJ*, **278**, 176
- Jones, B., Merrill, K. M., Puetter, R. C., & Willner, S. P. 1978, *AJ*, **83**, 1437
- Josselin, E., & Bachiller, R. 2003, *A&A*, **397**, 659
- Justtanont, K., Cami, J., Yamamura, I., de Jong, T., & Waters, L. B. F. M. 1998, *Ap&SS*, **255**, 351
- Kahane, C., Cernicharo, J., Gómez-González, J., & Guélin, M. 1992, *A&A*, **256**, 235
- Knapp, G. R., & Morris, M. 1985, *ApJ*, **292**, 640
- Kwok, S. 2004, *Nature*, **430**, 985
- Kwok, S. 2006, *Physics and Chemistry of the Interstellar Medium* (Sausalito, CA: University Science Books)
- Kwok, S. 2009, *Ap&SS*, **319**, 5
- Le Bertre, T., Gougeon, S., & Le Sidaner, P. 1995, *A&A*, **299**, 791
- Lebofsky, M. J., & Rieke, G. H. 1977, *AJ*, **82**, 646
- Lodders, K. 2003, *ApJ*, **591**, 1220
- Mauron, N., & Huggins, P. J. 2006, *A&A*, **452**, 257
- Menzies, J. W., Feast, M. W., & Whitelock, P. A. 2006, *MNRAS*, **369**, 783
- Morris, M., Sahai, R., Matthews, K., Cheng, J., Lu, J., Claussen, M., & Sánchez-Contreras, C. 2006, in IAU Symp. 234, Planetary Nebulae, ed. M. J. Barlow & R. H. Méndez (Cambridge: Cambridge Univ. Press), 469
- Müller, H. S. P., Schlöder, F., Stutzki, J., & Winnewisser, G. 2005, *J. Mol. Struct.*, **742**, 215
- Müller, H. S. P., Thorwirth, S., Roth, D. A., & Winnewisser, G. 2001, *A&A*, **370**, L49
- Neri, R., Kahane, C., Lucas, R., Bujarrabal, V., & Loup, C. 1998, *A&AS*, **130**, 1
- Nguyen-Quang-Rieu, Deguchi, S., Izumiura, H., Kaifu, N., Ohishi, M., Suzuki, H., & Ukita, N. 1988, *ApJ*, **330**, 374
- Nummelin, A., et al. 1998, *ApJS*, **117**, 427
- Nyman, L.-Å., et al. 1992, *A&AS*, **93**, 121
- Olofsson, H. 1996, in IAU Symp. 178, *Molecules in Astrophysics: Probes & Processes*, ed. E. van Dishoeck (Dordrecht: Kluwer), 457
- Omont, A., Loup, C., Forveille, T., Te Lintel Hekkert, P., Habing, H., & Sivagnanam, P. 1993, *A&A*, **267**, 515
- Pardo, J. R., Cernicharo, J., & Goicoechea, J. R. 2005, *ApJ*, **628**, 275
- Pardo, J. R., Cernicharo, J., Goicoechea, J. R., Guélin, M., & Ramos, A. A. 2007, *ApJ*, **661**, 250
- Pickett, H. M., Poynter, R. L., Cohen, E. A., Delitsky, M. L., Pearson, J. C., & Muller, H. S. P. 1998, *J. Quant. Spectrosc. Radiat. Transfer*, **60**, 883
- Schilke, P., Walmsley, C. M., Pineau des Forêts, G., Roueff, E., Flower, D. R., & Guilloteau, S. 1992, *A&A*, **256**, 595
- Schöier, F. L., Bast, J., Olofsson, H., & Lindqvist, M. 2007, *A&A*, **473**, 871
- Schöier, F. L., Olofsson, H., & Lundgren, A. A. 2006, *A&A*, **247**, 255
- Schöier, F. L., Ryde, N., & Olofsson, H. 2002, *A&A*, **391**, 577
- Sopka, R. J., Olofsson, H. J., Johansson, L. E. B., Nguyen-Q-Rieu, & Zuckerman, B. 1989, *A&A*, **210**, 78
- Teyssier, D., Hernandez, R., Bujarrabal, V., Yoshida, H., & Phillips, T. G. 2006, *A&A*, **450**, 167
- Volk, K., Kwok, S., & Langill, P. P. 1992, *ApJ*, **391**, 285
- Volk, K., Kwok, S., & Woodsworth, A. W. 1993, *ApJ*, **402**, 292
- Wannier, P. G., Andersson, B.-G., Olofsson, H., Ukita, N., & Young, K. 1991, *ApJ*, **380**, 593
- Wannier, P. G., & Sahai, R. 1987, *ApJ*, **319**, 367
- Willacy, K., & Cherchneff, I. 1998, *A&A*, **330**, 676
- Winters, J. M., Fleischer, A. J., Le Bertre, T., & Sedlmayr, E. 1997, *A&A*, **326**, 305
- Winters, J. M., Le Bertre, T., Nyman, L.-Å., Omont, A., & Jeong, K. S. 2002, *A&A*, **388**, 609
- Woods, P. M., Schöier, F. L., Nyman, L.-Å., & Olofsson, H. 2003, *A&A*, **402**, 617
- Wootten, A., Bozayan, E. P., & Garrett, D. B. 1980, *ApJ*, **239**, 844
- Yuasa, M., Unno, W., & Magono, S. 1999, *PASJ*, **51**, 197
- Zhang, Y., Kwok, S., & Dinh-V-Trung 2008, *ApJ*, **678**, 328
- Zhang, Y., Kwok, S., & Dinh-V-Trung 2009, *ApJ*, **691**, 1660
- Zinner, E. 1998, *Ann. Rev. Earth Planet. Sci.*, **26**, 147
- Ziurys, L. M., Milam, S. N., Apponi, A. J., & Woolf, N. J. 2007, *Nature*, **447**, 1094