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Title
Confirmation of the $X(1835)$ and observation of the resonances $X(2120)$ and $X(2370)$ in $J / \Psi \rightarrow \gamma \pi+\pi-\eta$

## Confirmation of the $X(1835)$ and Observation of the Resonances $X(2120)$ and $X(2370)$ in $J / \psi \rightarrow \gamma \pi^{+} \boldsymbol{\pi}^{-} \boldsymbol{\eta}^{\prime}$

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With a sample of $(225.2 \pm 2.8) \times 10^{6} \mathrm{~J} / \psi$ events registered in the BESIII detector, $J / \psi \rightarrow \gamma \pi^{+} \pi^{-} \eta^{\prime}$ is studied using two $\eta^{\prime}$ decay modes: $\eta^{\prime} \rightarrow \pi^{+} \pi^{-} \eta$ and $\eta^{\prime} \rightarrow \gamma \rho^{0}$. The $X(1835)$, which was previously observed by BESII, is confirmed with a statistical significance that is larger than $20 \sigma$. In addition, in the $\pi^{+} \pi^{-} \eta^{\prime}$ invariant-mass spectrum, the $X(2120)$ and the $X(2370)$, are observed with statistical significances larger than $7.2 \sigma$ and $6.4 \sigma$, respectively. For the $X(1835)$, the angular distribution of the radiative photon is consistent with expectations for a pseudoscalar.

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A $\pi^{+} \pi^{-} \eta^{\prime}$ resonance, the $X(1835)$, was observed in $J / \psi \rightarrow \gamma \pi^{+} \pi^{-} \eta^{\prime}$ decays with a statistical significance of $7.7 \sigma$ by the BESII experiment [1]. A fit to a Breit-Wigner function yielded a mass $M=1833.7 \pm 6.1$ (stat) $\pm$ 2.7 (syst) $\mathrm{MeV} / c^{2}, \quad$ a width $\quad \Gamma=67.7 \pm 20.3$ (stat) $\pm$ 7.7(syst) $\mathrm{MeV} / c^{2}$, and a product branching fraction $B(J / \psi \rightarrow \gamma X) \cdot B\left(X \rightarrow \pi^{+} \pi^{-} \eta^{\prime}\right)=[2.2 \pm 0.4($ stat $) \pm$ 0.4 (syst) $] \times 10^{-4}$. The study was stimulated by the anomalous $p \bar{p}$ invariance mass threshold enhancement, that was reported in $J / \psi \rightarrow \gamma p \bar{p}$ decays by the BESII experiment [2] and was recently confirmed in an analysis of $\psi^{\prime} \rightarrow \pi^{+} \pi^{-} J / \psi, J / \psi \rightarrow \gamma p \bar{p}$ decays by the BESIII experiment [3]. The possible interpretations of the $X(1835)$ include a $p \bar{p}$ bound state [4-7], a glueball [8-10], a radial excitation of the $\eta^{\prime}$ meson [11], etc. A high statistics data sample collected with BESIII provides an opportunity to confirm the existence of the $X(1835)$ and look for possible related states that decay to $\pi^{+} \pi^{-} \eta^{\prime}$, and the study of such states may help us to understand the dynamics of QCD.

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Lattice QCD predicts that the lowest lying pseudoscalar glueball meson has a mass that is around $2.3 \mathrm{GeV} / c^{2}$ [12]. This pseudoscalar glueball may have properties in common with the $\eta_{c}$, due to its similar decay dynamics that favor decays into gluons. One of the strongest decay channels of the $\eta_{c}$ is $\pi^{+} \pi^{-} \eta^{\prime}$. Thus $J / \psi \rightarrow \gamma \pi^{+} \pi^{-} \eta^{\prime}$ decays may be a good channel for finding $0^{-+}$glueballs.

In this Letter, we report a study of $J / \psi \rightarrow \gamma \pi^{+} \pi^{-} \eta^{\prime}$ that uses two $\eta^{\prime}$ decay modes, $\eta^{\prime} \rightarrow \gamma \rho$ and $\eta^{\prime} \rightarrow$ $\pi^{+} \pi^{-} \eta$. The analysis uses a sample of $(225.2 \pm 2.8) \times$ $10^{6} \mathrm{~J} / \psi$ events [13] accumulated in the new Beijing Spectrometer (BESIII) [14] located at the Beijing Electron-Positron Collider (BEPCII) [15] at the Beijing Institute of High Energy Physics.

BEPCII is a two-ring $e^{+} e^{-}$collider designed for a peak luminosity of $10^{33} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$ at a beam current of 0.93 A . The cylindrical core of the BESIII detector consists of a helium-gas-based drift chamber, a plastic scintillator time-of-flight system (TOF), and a $\mathrm{CsI}(\mathrm{Tl})$ electromagnetic
calorimeter, all enclosed in a superconducting solenoidal magnet providing a $1.0-\mathrm{T}$ magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muon identifier modules interleaved with steel. The charged particle and photon acceptance is $93 \%$ of $4 \pi$, and the charged particle momentum and photon energy resolutions at 1 GeV are $0.5 \%$ and $2.5 \%$, respectively. The time resolution of TOF is 80 ps in the barrel and 110 ps in the endcaps, and the $d E / d x$ resolution is $6 \%$.

Charged-particle tracks in the polar angle range $|\cos \theta|<0.93$ are reconstructed from hits in the helium-gas-based drift chamber. Tracks that extrapolate to be within 20 cm of the interaction point in the beam direction and 2 cm in the plane perpendicular to the beam are selected. The TOF and $d E / d x$ information are combined to form particle identification confidence levels for the $\pi$, $K$, and $p$ hypotheses; each track is assigned to the particle type that corresponds to the hypothesis with the highest confidence level. Photon candidates are required to have at least 100 MeV of energy in the electromagnetic calorimeter regions $|\cos \theta|<0.8$ and $0.86<|\cos \theta|<0.92$ and be isolated from all charged tracks by more than $5^{\circ}$. In this analysis, candidate events are required to have four charged tracks (zero net charge) with at least three of the charged tracks identified as pions. At least two photons (three photons) are required for the $\eta^{\prime} \rightarrow \gamma \rho\left(\eta^{\prime} \rightarrow\right.$ $\pi^{+} \pi^{-} \eta$ ) channel.

For $J / \psi \rightarrow \gamma \pi^{+} \pi^{-} \eta^{\prime}\left(\eta^{\prime} \rightarrow \gamma \rho\right)$, a four-constraint (4C) energy-momentum conservation kinematic fit is performed to the $\gamma \gamma \pi^{+} \pi^{-} \pi^{+} \pi^{-}$hypothesis. For events with more than two photon candidates, the combination with the minimum $\chi^{2}$ is used, and $\chi_{4 C}^{2}<40$ is required. Events with $\left|M_{\gamma \gamma}-m_{\pi^{0}}\right|<0.04 \mathrm{GeV} / c^{2},\left|M_{\gamma \gamma}-m_{\eta}\right|<$ $0.03 \mathrm{GeV} / c^{2}, \quad 0.72 \mathrm{GeV} / c^{2}<M_{\gamma \gamma}<0.82 \mathrm{GeV} / c^{2}$, or $\left|M_{\gamma \pi^{+} \pi^{-}}-m_{\eta}\right|<0.007 \mathrm{GeV} / c^{2}$ are rejected to suppress the background from $\pi^{0} \pi^{+} \pi^{-} \pi^{+} \pi^{-}, \eta \pi^{+} \pi^{-} \pi^{+} \pi^{-}$, $\omega\left(\omega \rightarrow \gamma \pi^{0}\right) \pi^{+} \pi^{-} \pi^{+} \pi^{-}$, and $\gamma \pi^{+} \pi^{-} \eta\left(\eta \rightarrow \gamma \pi^{+} \pi^{-}\right)$, respectively. A clear $\eta^{\prime}$ signal with a $5 \mathrm{MeV} / c^{2}$ mass resolution is evident in the mass spectrum of all selected $\gamma \pi^{+} \pi^{-}$combinations shown in Fig. 1(a). Candidate $\rho$ and $\eta^{\prime}$ mesons are reconstructed from the $\pi^{+} \pi^{-}$and $\gamma \pi^{+} \pi^{-}$ pairs with $\left|M_{\pi^{+} \pi^{-}}-m_{\rho}\right|<0.2 \mathrm{GeV} / c^{2}$ and $\mid M_{\gamma \pi^{+} \pi^{-}}-$ $m_{\eta^{\prime}} \mid<0.015 \mathrm{GeV} / c^{2}$, respectively. If more than one combination passes these criteria, the combination with $M_{\gamma \pi^{+} \pi^{-}}$closest to $m_{\eta^{\prime}}$ is selected. After the above selection, the $X(1835)$ resonance is clearly visible in the $\pi^{+} \pi^{-} \eta^{\prime}$ invariant-mass spectrum of Fig. 1(b). Also, additional peaks are evident around 2.1 and $2.4 \mathrm{GeV} / c^{2}$ as well as a distinct signal for the $\eta_{c}$.

For $J / \psi \rightarrow \gamma \pi^{+} \pi^{-} \eta^{\prime}\left(\eta^{\prime} \rightarrow \pi^{+} \pi^{-} \eta\right)$, a 4C kinematic fit to the $\gamma \gamma \gamma \pi^{+} \pi^{-} \pi^{+} \pi^{-}$hypothesis is performed. If there are more than three photon candidates, the combination with the minimum $\chi_{4 C}^{2}$ is selected, and $\chi_{4 C}^{2}<40$ is required. In order to reduce the combinatorial background events from $\pi^{0} \rightarrow \gamma \gamma,\left|M_{\gamma \gamma}-m_{\pi^{0}}\right|>0.04 \mathrm{GeV} / c^{2}$ is required for all photon pairs. The $\eta$ candidates are selected


FIG. 1 (color online). Invariant-mass distributions for the selected candidate events. Panels (a) and (b) are the $\gamma \pi^{+} \pi^{-}$ invariant-mass spectrum and the $\pi^{+} \pi^{-} \eta^{\prime}$ invariant-mass spectrum for $\eta^{\prime} \rightarrow \gamma \rho$, respectively. Panels (c) and (d) are the $\pi^{+} \pi^{-} \eta$ invariant-mass spectrum and the $\pi^{+} \pi^{-} \eta^{\prime}$ invariantmass spectrum for $\eta^{\prime} \rightarrow \pi^{+} \pi^{-} \eta$, respectively. The histograms in (b) and (d) are from $J / \psi \rightarrow \gamma \pi^{+} \pi^{-} \eta^{\prime}$ phase-space MC events (with arbitrary normalization) for $\eta^{\prime} \rightarrow \gamma \rho$ and $\eta^{\prime} \rightarrow$ $\pi^{+} \pi^{-} \eta$, respectively.
by requiring $\left|M_{\gamma \gamma}-m_{\eta}\right|<0.03 \mathrm{GeV} / c^{2}$. A fiveconstraint fit with an $\eta$ mass constraint is used to improve the mass resolution from $8 \mathrm{MeV} / c^{2}(4 \mathrm{C})$ to $3 \mathrm{MeV} / c^{2}$, as shown in Fig. 1(c) where $\chi_{5 C}^{2}<40$ is required. To select $\eta^{\prime}$ mesons, $\left|M_{\pi^{+} \pi^{-} \eta}-m_{\eta^{\prime}}\right|<0.01 \mathrm{GeV} / c^{2}$ is required. If more than one combination passes the above selection, the combination with $M_{\pi^{+} \pi^{-} \eta}$ closest to $m_{\eta^{\prime}}$ is selected. After the above selection, structures similar to those seen for the $\eta^{\prime} \rightarrow \gamma \rho$ channel in the $\pi^{+} \pi^{-} \eta^{\prime}$ invariant-mass spectrum can be seen in Fig. 1(d), namely, peaks near 1.8, 2.1, and $2.4 \mathrm{GeV} / c^{2}$ as well as the $\eta_{c}$.

Potential background processes are studied with an inclusive sample of $2 \times 10^{8} \mathrm{~J} / \psi$ events generated according to the Lund-Charm model [16] and the Particle Data Group (PDG) decay tables [17]. There are no peaking backgrounds at the positions of the three resonances. To ensure further that the three peaks are not due to background, we have studied potential exclusive background processes using data. The main background channel is from $J / \psi \rightarrow$ $\pi^{0} \pi^{+} \pi^{-} \eta^{\prime}$. Non- $\eta^{\prime}$ processes are studied with $\eta^{\prime}$ masssideband events. Neither of these produce peaking structures.

The $\pi^{+} \pi^{-} \eta^{\prime}$ invariant-mass spectrum for the combined two $\eta^{\prime}$ decay modes is presented in Fig. 2. Here a small peak at the position of the $f_{1}(1510)$ signal is also present. Fits to the mass spectra have been made using four
efficiency-corrected Breit-Wigner functions convolved with a Gaussian mass resolution plus a nonresonant $\pi^{+} \pi^{-} \eta^{\prime}$ contribution and background representations, where the efficiency for the combined channels is obtained from the branching-ratio-weighted average of the efficiencies for the two $\eta^{\prime}$ modes. The contribution from nonresonant $\gamma \pi^{+} \pi^{-} \eta^{\prime}$ production is described by reconstructed Monte Carlo (MC)-generated $J / \psi \rightarrow$ $\gamma \pi^{+} \pi^{-} \eta^{\prime}$ phase space decays, and it is treated as an incoherent process. The background contribution can be divided into two different components: the contribution from non $-\eta^{\prime}$ events estimated from $\eta^{\prime}$ mass sideband, and the contribution from $J / \psi \rightarrow \pi^{0} \pi^{+} \pi^{-} \eta^{\prime}$. For the second background, we obtain the background $\pi^{+} \pi^{-} \eta^{\prime}$ mass spectrum from data by selecting $J / \psi \rightarrow \pi^{0} \pi^{+} \pi^{-} \eta^{\prime}$ events and reweighting their mass spectrum with a weight equal to the MC efficiency ratio of the $\gamma \pi^{+} \pi^{-} \eta^{\prime}$ and $\pi^{0} \pi^{+} \pi^{-} \eta^{\prime}$ selections for $J / \psi \rightarrow \pi^{0} \pi^{+} \pi^{-} \eta^{\prime}$. The masses, widths, and number of events of the $f_{1}(1510)$, the $X(1835)$ and the resonances near 2.1 and $2.4 \mathrm{GeV} / c^{2}$, the $X(2120)$ and $X(2370)$, are listed in Table I. The statistical significance is determined from the change in $-2 \ln L$ in the fits to mass spectra with and without signal assumption while considering the change of degree of freedom of the fits. With the systematic uncertainties in the fit taken into account, the statistical


FIG. 2 (color online). (a) The $\pi^{+} \pi^{-} \eta^{\prime}$ invariant-mass distribution for the selected events from the two $\eta^{\prime}$ decay modes. (b) Mass spectrum fitting with four resonances; here, the dashdotted line is contributions of non- $\eta^{\prime}$ events and the $\pi^{0} \pi^{+} \pi^{-} \eta^{\prime}$ background for two $\eta^{\prime}$ decay modes, and the dashed line is contributions of the total background and nonresonant $\pi^{+} \pi^{-} \eta^{\prime}$ process.

TABLE I. Fit results with four resonances for the combined two $\eta^{\prime}$ decay modes

| Resonance | $M\left(\mathrm{MeV} / c^{2}\right)$ | $\Gamma\left(\mathrm{MeV} / c^{2}\right)$ | $N_{\text {event }}$ |
| :--- | :--- | :--- | :--- |
| $f_{1}(1510)$ | $1522.7 \pm 5.0$ | $48 \pm 11$ | $230 \pm 37$ |
| $X(1835)$ | $1836.5 \pm 3.0$ | $190.1 \pm 9.0$ | $4265 \pm 131$ |
| $X(2120)$ | $2122.4 \pm 6.7$ | $83 \pm 16$ | $647 \pm 103$ |
| $X(2370)$ | $2376.3 \pm 8.7$ | $83 \pm 17$ | $565 \pm 105$ |

significance of the $X(1835)$ is larger than $20 \sigma$, while those for the $f_{1}(1510)$, the $X(2120)$, and the $X(2370)$ are larger than $5.7 \sigma, 7.2 \sigma$, and $6.4 \sigma$, respectively. The mass and width from the fit of the $f_{1}(1510)$ are consistent with PDG values [17]. With MC-determined selection efficiencies of $16.0 \%$ and $11.3 \%$ for the $\eta^{\prime} \rightarrow \gamma \rho$ and $\eta^{\prime} \rightarrow$ $\pi^{+} \pi^{-} \eta$ decay modes, respectively, the branching fraction for the $X(1835)$ is measured to be $B(J / \psi \rightarrow \gamma X(1835))$ $B\left(X(1835) \rightarrow \pi^{+} \pi^{-} \eta^{\prime}\right)=(2.87 \pm 0.09) \times 10^{-4}$. The consistency between the two $\eta^{\prime}$ decay modes is checked by fitting their $\pi^{+} \pi^{-} \eta^{\prime}$ mass distribution separately with the procedure described above.

For radiative $J / \psi$ decays to a pseudoscalar meson, the polar angle of the photon in the $J / \psi$ center of mass system, $\theta_{\gamma}$, should be distributed according to $1+\cos ^{2} \theta_{\gamma}$. We divide the $\left|\cos \theta_{\gamma}\right|$ distribution into 10 bins in the region of $[0,1,0]$. With the same procedure as described above, the number of the $X(1835)$ events in each bin can be obtained by fitting the mass spectrum in this bin, and then the background-subtracted, acceptance-corrected $\left|\cos \theta_{\gamma}\right|$ distribution for the $X(1835)$ is obtained as shown in Fig. 3, where the errors are statistical only. It agrees with $1+\cos ^{2} \theta_{\gamma}$, which is expected for a pseudoscalar, with $\chi^{2} /$ d.o.f $=11.8 / 9$.

The systematic uncertainties on the mass and width are mainly from the uncertainty of background representation, the mass range included in the fit, different shapes for background contributions, and the nonresonant process and contributions of possible additional resonances in the $1.6 \mathrm{GeV} / c^{2}$ and $2.6 \mathrm{GeV} / c^{2}$ mass regions. The total systematic errors on the mass and width are ${ }_{-2.1}^{+5.6}$ and


FIG. 3. The background-subtracted, acceptance-corrected $\left|\cos \theta_{\gamma}\right|$ distribution of the $X(1835)$ for two $\eta^{\prime}$ decay modes for $J / \psi \rightarrow \gamma \pi^{+} \pi^{-} \eta^{\prime}$.
${ }_{-36}^{+38} \mathrm{MeV} / c^{2}$ for the $X(1835),{ }_{-2.7}^{+4.7}$ and ${ }_{-11}^{+31} \mathrm{MeV} / c^{2}$ for the $X(2120),{ }_{-4.3}^{+3.2}$ and ${ }_{-6}^{+44} \mathrm{MeV} / c^{2}$ for the $X(2370)$, respectively. For the systematic error of the branching fraction measurement, we additionally include the uncertainties of the MC generator, charged track detection efficiency, particle identification efficiency, photon detection efficiency, kinematic fit, the $\eta^{\prime}$ decay branching fractions to $\pi^{+} \pi^{-} \eta$ and $\gamma \rho$ [17], the requirement on the $\gamma \gamma$ invariant-mass distribution, signals selection of $\rho, \eta$, and $\eta^{\prime}$ and the total number of $J / \psi$ events [13]. The main contribution also comes from the uncertainty in the background estimation, and the total relative systematic error on the product branching fraction for the $X(1835)$ is ${ }_{-18 \%}^{+17 \%}$.

In summary, the decay channel $J / \psi \rightarrow \pi^{+} \pi^{-} \eta^{\prime}$ is analyzed using two $\eta^{\prime}$ decay modes, $\eta^{\prime} \rightarrow \gamma \rho$ and $\eta^{\prime} \rightarrow$ $\pi^{+} \pi^{-} \eta$. The $X(1835)$, which was first observed at BESII, has been confirmed with a statistical significance larger than $20 \sigma$. Meanwhile, two resonances, the $X(2120)$ and the $X(2370)$ are observed with statistical significances larger than $7.2 \sigma$ and $6.4 \sigma$, respectively. The masses and widths are measured to be

$$
\begin{aligned}
& X(1835) \\
& M=1836.5 \pm 3.0(\text { stat })_{-2.1}^{+5.6}(\text { syst }) \mathrm{MeV} / c^{2} \\
& \Gamma=190 \pm 9(\text { stat })_{-36}^{+38}(\text { syst }) \mathrm{MeV} / c^{2} \\
& X(2120) \\
& M=2122.4 \pm 6.7(\text { stat })_{-2.7}^{+4.7}(\text { syst }) \mathrm{MeV} / c^{2} \\
& \Gamma=83 \pm 16(\text { stat })_{-11}^{+31}(\text { syst }) \mathrm{MeV} / c^{2} \\
& X(2370) \\
& M=2376.3 \pm 8.7(\text { stat })_{-4.3}^{+3.2}(\text { syst }) \mathrm{MeV} / c^{2} \\
& \Gamma=83 \pm 17(\text { stat })_{-6}^{+44}(\text { syst }) \mathrm{MeV} / c^{2}
\end{aligned}
$$

For the $X(1835)$, the product branching fraction is $B[J / \psi \rightarrow \gamma X(1835)] \cdot B\left(X(1835) \rightarrow \pi^{+} \pi^{-} \eta^{\prime}\right)=[2.87 \pm$ 0.09 (stat) ${ }_{-0.52}^{+0.49}($ syst $\left.)\right] \times 10^{-4}$, and the angular distribution of the radiative photon is consistent with a pseudoscalar assignment. The mass of the $X(1835)$ is consistent with the BESII result, but the width is significantly larger. If we fit the mass spectrum with one resonance as BESII, the mass and width of the $\mathrm{X}(1835)$ are $1841.2 \pm 2.9 \mathrm{MeV} / c^{2}$ and $109 \pm 11 \mathrm{MeV} / c^{2}$, where the errors are statistical only.

In the mass spectrum fitting in Fig. 2(b), possible interferences among different resonances and the nonresonant process are not taken into account which might be a source of the large $\chi^{2}$ value for the fit $\left(\chi^{2} /\right.$ d.o.f $\left.=144 / 62\right)$. The dips around $2.2 \mathrm{GeV} / c^{2}$ and $2.5 \mathrm{GeV} / c^{2}$ may not be fitted well due to the neglect of such interferences. In the absence of knowledge of the spin parities of the resonances and their decay intermediate states, reliable fits that include interference cannot be done.

It is intriguing that it is the first time resonant structures are observed in the $2.3 \mathrm{GeV} / c^{2}$ region in the $\pi^{+} \pi^{-} \eta^{\prime}$
mode and in $J / \psi$ radiative decays which a $0^{-+}$glueball may favor to decay to and to be produced from. To understand the nature of the $X(1835), X(2120)$, and $X(2370)$, it would be crucial to measure their spin parities and to search for them in more decay modes and in more production mechanisms. To determine their spin parities, and to measure their masses and widths more precisely, a partial wave analysis must be performed, which will be possible with the much higher statistics $J / \psi$ data samples planned for future runs of the BESIII experiment.

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