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ADAPTIVE BEAMFORMING USING UNIFORM CONCENTRIC CIRCULAR ARRAYS WITH FREQUENCY INVARIANT CHARACTERISTICS

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Abstract—This paper proposes a new method for adaptive beamforming using uniform concentric circular array (UCCA) that has nearly frequency invariant (FI) characteristics. The basic principle of FI UCCA is to transform the received signals to the phase mode and compensate for the frequency dependency of the individual phase mode through the use of a digital beamforming network. The far field pattern of the array is then determined by a set of weights and it is approximately invariant over a wide range of frequencies. Therefore, the minimum variance beamforming (MVB) approach can be used to adapt the small set of weights, as if it is a narrowband array. Design examples and simulation are given to demonstrate the usefulness of the proposed FI UCCA in broadband DOA estimation and beamforming.

I. INTRODUCTION

Wideband beamforming using sensor arrays is an effective method for suppressing interference whose angles of arrival are different from the desired looking direction. They find important applications in radio communications, sonar, radar, and acoustics [1-3]. Traditional adaptive wideband beamformers usually employ tapped-delay line with adaptive coefficients to generate appropriate beam patterns for interference suppression. This usually requires considerable number of adaptive coefficients resulting in rather long convergence time and high implementation complexity. This can be remedied by using subband decomposition technique, partial adaptation or using frequency invariant beamformers (FIB) [4-6,7,9]. In FIB, a beam-forming network is used to generate beam pattern with approximately frequency invariant (FI) characteristics over the frequency band of interest. They can attenuate broadband directional interference using an adaptive beamformer with very few number of adaptive filter coefficients [5]. One of the widely studied FIB is the uniform linear array (ULA) FIB [4-8]. The ULA has a linear geometry with equal inter-sensor spacing. Due to this geometry, its angular resolution at boresight is better than that at its end-fire. In addition, this simple array structure enables many efficient direction-of-arrival (DOA) detection algorithms to be obtained. For example, the MUSIC algorithm [10] provides a high resolution method for detecting the angle of arrival (AoA) of the signal sources based on the subspace approach. The MUSIC algorithm is also applicable to DOA estimation of wideband coherent sources by performing the algorithm in beamspace using ULA-FIB [9]. Besides AoA estimation of wideband sources, adaptive interference suppression using beamspace adaptive beamforming [5] is very attractive because of the small number of adaptive weights required and the possibility of employing partial adaptation, yielding faster convergence and fewer number of high speed variable multipliers.

Recently, electronic steerable uniform-circular arrays (UCAs) [1] with frequency invariant characteristics were studied in [14]. Beamforming networks are used to compensate for the frequency dependence of the array. Unfortunately, the passband of a UCA is closely related to its radius and exhibit a bandpass characteristic. To obtain a frequency invariant characteristic over a large bandwidth, the dynamic range of the

compensation filters will become very large and it leads to considerable noise amplification of the array. In this paper, we show that this problem can be overcome if uniform concentric circular arrays (UCCA) are employed and develop an adaptive beamformer using these FIB UCCAs. The sensors in a UCCA are placed on concentric circles with a uniform inter-sensor spacing and increasing radius. We find that UCAs with increasing radius will have their passbands moving towards the lower frequency bands. Hence, by using ring subarrays with progressively larger radius in a UCCA, one can achieve a frequency invariant characteristic over a much larger bandwidth than a single UCA. Thus, UCCA is able to form electronic steerable beam patterns that are relatively invariant with frequency over a wide bandwidth.

Similar to the FI UCAs in [14], the basic idea of the FI UCCA is to transform each snapshot sampled by the array to the phase modes via an Inverse Discrete Fourier Transform (IDFT). The transformed data is then filtered to compensate for the frequency dependence of the phase modes. Finally, these frequency invariant phase-modes are linear combined using a set of weights or coefficients to obtain the desired frequency invariant beam patterns. These weights, which govern the far field pattern of the UCCA, can be designed by conventional 1D digital filter design techniques such as the Parks-McClellan algorithm to form fix beam patterns. Alternatively, these coefficients can be varied by an adaptive algorithm to form an adaptive beamformer with approximately frequency invariant characteristics. The compensation filters proposed in this paper are designed using second order cone programming (SOCP). Design examples show that electronic steerable beam patterns with approximately frequency invariant over a fairly large bandwidth can be obtained. Simulation results on an adaptive beamformer and DOA estimation using the UCCA FIB are given to demonstrate its usefulness.

The paper is organized as follows: Sections II and III are devoted to the principle and design of the proposed UCCA FIB. Design examples and simulation results of the broadband beamformer and DOA estimation using the proposed UCCA are given in Section IV. Conclusions are drawn in Section V.

II. UNIFORM CONCENTRIC CIRCULAR ARRAY (UCCA)

Figure 1 shows a UCCA with P rings and each ring has K_p omnidirectional sensors located at $\{r_p \cos \phi_{k_p}, r_p \sin \phi_{k_p}\}$ (represented as Cartesian Coordinate with the center as the origin) where r_p is the radius of the p^{th} ring, $p=1, \dots, P$, $\phi_{k_p} = 2\pi k_p / K_p$ and $k_p = 0, \dots, K_p - 1$ as shown in Figure 2. In UCCAs, the inter-sensor spacing in each ring is fixed at $\lambda/2$ where λ is the smallest wavelength of the array to be operated and is denoted by λ_s . The radius of the p^{th} ring of the UCCA is given by

$$r_p = \lambda_s / (4 \sin(\pi / K_p)). \quad (1)$$

For convenience, this radius is represented as its normalized version

$$\hat{r}_p = r_p / \lambda_s = 1 / (4 \sin(\pi / K_p)). \quad (1a)$$

Let α denote the ratio of the sampling frequency f_s to the maximum frequency f_{\max} ($\alpha = f_s / f_{\max}$), the phase difference between the k_p^{th} sensor and the center of the UCCA is

$\chi_{k_p} = 2\pi\hat{r}_p\alpha \sin\theta \cos(\phi - \phi_{k_p})$, and the corresponding phase

shift is $e^{j\omega\hat{r}_p\alpha \sin\theta \cos(\phi - \phi_{k_p})}$, where ϕ , and θ are the azimuth angle and the elevation angle respectively, as shown in figure 3. Hence, the steering vector [1] of the p^{th} ring of a UCCA is:

$$\mathbf{s} = [e^{j\omega\hat{r}_p\alpha \sin\theta \cos(\phi - \phi_0)} \ e^{j\omega\hat{r}_p\alpha \sin\theta \cos(\phi - \phi_1)} \ \dots \ e^{j\omega\hat{r}_p\alpha \sin\theta \cos(\phi - \phi_{K_p-1})}]^T. \quad (2)$$

The azimuth angle ϕ is on the horizontal plane where the sensors are situated. It measures from a reference imaginary axis on this horizontal plane, while the elevation angle θ is measured from a reference imaginary axis perpendicular to the horizontal plane. Without loss of generality, our design will be focused at an elevation angle of $\theta = \pi/2$, i.e. the horizontal plane.

III. DIGITAL BROADBAND UCCA FIB

Figure 4 shows the structure of the broadband FIB for the p^{th} ring of a UCCA. After appropriate down-converting, lowpass filtering and sampling, the sampled signals from the antennas are given by the vector $\mathbf{X}_p[n] = [x_0[n] \ x_1[n] \ \dots \ x_{K_p-1}[n]]^T$, which is called a snapshot

at sampling instance n . This snapshot is IDFT transformed to the phase-mode and the transformed snapshot is denoted by $\mathbf{V}_p[n] = \mathbf{W}_{M_p K_p} \cdot \mathbf{X}_p[n]$, where $\mathbf{W}_{M_p K_p}$ is an M_p by K_p IDFT matrix with $[\mathbf{W}_{M_p K_p}]_{m_p, k_p} = e^{j2\pi m_p k_p / K_p}$

and
$$[\mathbf{V}_p[n]]_{m_p} = v_{m_p}[n] = \sum_{k_p=0}^{K_p-1} x_{k_p}[n] e^{j\frac{2\pi m_p k_p}{K_p}}. \quad (3)$$

Here, $[\mathbf{A}]_{m,n}$ denotes the (mxn) entry of matrix \mathbf{A} . We assume that M_p is an odd number and define $L_p = (M_p - 1)/2$. Each branch of the IDFT output is then filtered by $H_{m_p}(\omega)$ (to compensate for the frequency dependency as we shall see later in this section), multiplied with g_{m_p} before combining to give the beamformer output $y_p[n]$:

$$y_p[n] = \sum_{m_p=-L_p}^{L_p} (v_{m_p}[n] * h_{m_p}[n]) \cdot g_{m_p}, \quad (4)$$

where $*$ denotes discrete-time convolution. To obtain the spatial-temporal transfer function of the beamformer, let us assume that there is only one source signal $s(n)$ with spectrum $S(\omega)$. Taking the Discrete Time Fourier Transform (DTFT) of equation (3), one gets

$$V_{m_p}(\omega) = \sum_{k_p=0}^{K_p-1} X_{k_p}(\omega) e^{j\frac{2\pi m_p k_p}{K_p}} = S(\omega) \sum_{k_p=0}^{K_p-1} e^{j\omega\hat{r}_p\alpha \cos(\phi - \phi_{k_p})} e^{j\frac{2\pi m_p k_p}{K_p}}. \quad (5a)$$

Taking DTFT on both size of equation (4) and using (5a), we have

$$\begin{aligned} Y_p(\omega) &= \sum_{m_p=-L_p}^{L_p} g_{m_p} V_{m_p}(\omega) H_{m_p}(\omega) \\ &= S(\omega) \sum_{m_p=-L_p}^{L_p} g_{m_p} \left(\sum_{k_p=0}^{K_p-1} e^{j\omega\hat{r}_p\alpha \cos(\phi - \phi_{k_p})} e^{j\frac{2\pi m_p k_p}{K_p}} \right) H_{m_p}(\omega) \end{aligned} \quad (5b)$$

Hence, the spatial-temporal response of the p^{th} ring is

$$G_p(\omega, \phi) = \sum_{m_p=-L_p}^{L_p} g_{m_p} \left[\sum_{k_p=0}^{K_p-1} e^{j\omega\hat{r}_p\alpha \cos(\phi - \phi_{k_p})} e^{j\frac{2\pi m_p k_p}{K_p}} H_{m_p}(\omega) \right]. \quad (6)$$

To obtain a frequency invariant response, the term inside the bracket should be independent of the frequency variable ω . First of all, using the expansion [13],

$$e^{j\beta \cos \gamma} = \sum_{n=-\infty}^{+\infty} j^n J_n(\beta) e^{jn\gamma}, \quad (7)$$

where $J_n(\beta)$ is the Bessel function of the first kind, (6) can be rewritten as

$$\begin{aligned} G_p(\omega, \phi) &= \sum_{m_p=-L_p}^{L_p} g_{m_p} \sum_{k_p=0}^{K_p-1} \sum_{n=-\infty}^{+\infty} j^n J_n(\omega\hat{r}_p\alpha) e^{jn(\phi - 2\pi k_p / K_p)} e^{j\frac{2\pi m_p k_p}{K_p}} H_{m_p}(\omega) \\ &= \sum_{m_p=-L_p}^{L_p} g_{m_p} H_{m_p}(\omega) \sum_{n=-\infty}^{+\infty} j^n J_n(\omega\hat{r}_p\alpha) e^{jn\phi} \left(\sum_{k_p=0}^{K_p-1} e^{j2\pi k_p (\frac{m_p - n}{K_p})} \right). \end{aligned} \quad (8)$$

Further, the term inside the bracket is evaluated to be

$$\sum_{k_p=0}^{K_p-1} e^{j2\pi k_p (\frac{m_p - n}{K_p})} = \begin{cases} K_p & m_p - n = Kq \\ 0 & \text{otherwise} \end{cases}, \quad \text{where } q \in \mathbb{Z}. \quad (9)$$

Substituting (9) into (8) gives

$$G_p(\omega, \phi) = K_p \sum_{m_p=-L_p}^{L_p} g_{m_p} \left[\sum_{n=m_p+Kq} j^n J_n(\omega\hat{r}_p\alpha) e^{jn\phi} \right] H_{m_p}(\omega). \quad (10)$$

From [13], the Bessel function has the following property

$$|J_{|n|}(\omega\hat{r}_p\alpha)| \leq \left(\frac{\omega\hat{r}_p\alpha}{2|n|} \right)^{|n|}. \quad (11)$$

Therefore, for sufficiently large value of n , the value of the Bessel function will be negligibly small. In other words, if the number of sensors is large enough, $G_p(\omega, \phi)$ can be approximated by

$$G_p(\omega, \phi) \approx K_p \sum_{m_p=-L_p}^{L_p} g_{m_p} \left[j^{m_p} J_{m_p}(\omega\hat{r}_p\alpha) H_{m_p}(\omega) \right] \cdot e^{jm_p\phi}. \quad (12)$$

It can be seen that for a given radius r_p , the bandwidth of the array, without compensation, is determined by the term $J_{m_p}(\omega\hat{r}_p\alpha)$. Rings with small radi usually have better high frequency response and vice versa. Therefore, to obtain a FI with large bandwidth, small responses of $J_{m_p}(\omega\hat{r}_p\alpha)$ at certain frequencies have to be compensated by $H_{m_p}(\omega)$. This is undesirable in general because it leads to considerable noise amplification. Fortunately, by employing more rings in a UCCA, a wider bandwidth can be obtained.

In a UCCA FIB, the outer rings have more phase modes than the inner ones. Let the weighting vectors of the rings be identical, i.e. $\mathbf{g}_1 = \mathbf{g}_2 = \dots = \mathbf{g}_p$, where $\mathbf{g}_p = [g_{-L_p} \ \dots \ g_{L_p}]^T$. The overall response of the beamformer can be written as:

$$\begin{aligned} G(\omega, \phi) &= \sum_{p=1}^P G_p(\omega, \phi) \\ &= \sum_{m=-L_p}^{L_p} g_m \cdot e^{jm\phi} \cdot \sum_{p=1}^P K_p \left[j^m J_m(\omega\hat{r}_p\alpha) H_m^p(\omega) \right] \end{aligned} \quad (13)$$

where for notation convenience, we write $H_m^p(\omega)$ as $H_{m_p}(\omega)$.

If the filters $H_m^p(\omega)$ are designed such that

$$\sum_{p=1}^P K_p \left[j^m J_m(\omega\hat{r}_p\alpha) H_m^p(\omega) \right] \approx 1 \text{ for } \omega \in [\omega_L, \omega_U], \quad (14)$$

where ω_L and ω_U are respectively the lower and upper frequencies of interest, then the beamformer in (13) will be approximately frequency invariant within $\omega \in [\omega_L, \omega_U]$ and

$$G(\phi) \approx \sum_{m=-L_p}^{L_p} g_m e^{jm\phi}. \quad (15)$$

Furthermore, its far field pattern is now governed by the spatial weighting $\{g_m\}$ alone. Since the right hand side of (14) is a linear function of the filter coefficients in $H_m^p(\omega)$'s, the design problem in (14) can be treated as a filter design problem

with all the filter outputs adding up to a desired response of value 1. If the minimax error criterion is used, the filter coefficients for $H_m^p(\omega)$ can be determined by second order programming (SOCP) [15]. It can also be seen from (15) that the far field spatial response is similar to that of a digital FIR filter with impulse response $\{g_m\}$. Therefore, $G(\phi)$ can be designed by conventional filter design algorithms such as the Parks-McClellan algorithm or SOCP if convex quadratic constraints are to be imposed. In addition, angular shifted versions of (15) can be derived by modulating $\{g_m\}$ with sinusoids at appropriate frequencies. For example, if the shift is $\pi/2$, then the modulation is $\{e^{j\frac{\pi}{2}m}\}$, $m = -L_p, \dots, L_p$. In example 1 to be described in Section IV, this property is used to generate a set of broadband beamformers uniformly spaced in the angular domain. Using a similar technique as in [9], DOA of broadband coherent signals can be estimated satisfactorily.

Real-time adaptation of the beam pattern through the spatial weighting $\{g_m\}$ to suppress undesired interference is also feasible. Since only a small set of coefficients $\{g_m\}$ is involved, it has the potential to yield faster convergence speed than traditional broadband adaptive array using tapped delay lines. Here, we shall present a broadband adaptive UCCA FI beamformer using the minimum variance beamformer (MVB) concept [16]. Suppose that the DOA of the desired signal has been determined. The beamformer weight $\mathbf{w} = [g_{-L_p}, \dots, g_{L_p}]^T$ can be determined by minimizing the output energy of the beamformer output, subject to the constraints that the signal in the direction has a gain equal to one. This yields the following problem for the optimal weight vector:

$$\begin{aligned} & \text{minimize } \mathbf{w}^* \mathbf{R}_y \mathbf{w} \\ & \text{subject to } \mathbf{w}^* \mathbf{a}(\theta_d) = 1, \end{aligned} \quad (16)$$

where $\mathbf{R}_y = \sum_{n=1}^{n=N} \mathbf{y}(n) \mathbf{y}^*(n)$ is the estimation of the covariance matrix of the received signal vector $\mathbf{y}(n)$ and $\mathbf{a}(\theta_d) \in C^n$ is the array manifold on the desired angle. The analytical solution to this optimization problem is:

$$\mathbf{w}_{mv} = \mathbf{R}_y^{-1} \mathbf{a}(\theta_d) / (\mathbf{a}(\theta_d)^* \mathbf{R}_y^{-1} \mathbf{a}(\theta_d)). \quad (17)$$

This is possible because the frequency characteristics of the array has been compensated by the FIB. We now consider some design examples.

IV. DESIGN EXAMPLES

Example 1: DOA estimation using UCCA beamformers.

In this example, the UCCA beamformer is used to find the DOAs of two arriving signals at 35° and 45° . The first signal is composed of 33 sinusoidal signals with frequencies ranging from 0.8×10^8 to 4×10^8 at an interval of 0.1×10^8 Hz. The other signal is also a sequence of sinusoidal signals with frequencies ranging from 0.83×10^8 to 4.3×10^8 and the sampling rate α is set to 2. The ratio of the first signal to the second one is -21.16dB. The UCCA consists of two rings. The inner ring and the outer ring have 10 and 18 omni-directional sensors, respectively. The required bandwidth of the UCCA-FIB is $\omega \in [0.2\pi, 0.65\pi]$. The numbers of phase modes M are respectively 9 and 17. We choose the central 9 spatial filter coefficients (phase mode) out of the 17 to shape the spatial response of the UCCA FIB. The desired beam is targeted at 60° and the beamwidth is 10° . $\{g_m\}$ are obtained from the Parks-McClellan algorithm according to the given specification

with same passband and stopband ripples. The frequency responses are shown in figures 5 and 6. For convenience, the frequency responses of the UCCA-FIB for $\omega \in [0.2\pi, 0.65\pi]$ are overlapped together in figure 5 to illustrate the frequency invariant property of the beamformer. The frequency spectrum is approximately FI, with deep nulls formed at the desired position over the bandwidth of interest. Figure 6 shows the perspective view of the beamformer. Other beamformers are obtained by shifting the basic beamformer's response equally in the angular domain. The SNR of the first signal and the background noise is 29dB and the number of arrays used in the beamspace is 9. The DOA estimation method used is the beamspace MUSIC method in [9], which was originally designed for FIB ULA. Figure 8 shows the MUSIC spectrum obtained in dB and the estimated angles are found to be 35.01° and 45.22° , which are very close to the true values.

Example 2: Beamforming using UCCA beamformer.

An adaptive MVDR beamformer is obtained by the method in Section III using the same UCCA and signal model of example 1. The first signal is assumed to be the desired signal, while the second one is considered as the interference. The desired signal, interference signal and beamformer output in frequency domain are plotted in Figure 8 as real, dashed and dotted lines, respectively. From the figure, we can see that the interference signal is considerably suppressed and the desired signal is well preserved (The performance in the frequency range $[0.3\pi, 0.65\pi]$ is similar to the one in figure 8 and is omitted here for clarity).

V. CONCLUSION

A new broadband adaptive beamformer using a new uniform concentric circular array (UCCA) with frequency invariant characteristics is presented. By compensating the frequency dependency of individual phase modes of a UCCA using a digital beamforming network, an electronically steerable UCCA with nearly frequency invariant (FI) characteristics is obtained. The far field pattern of the array is determined by a set of weights and it is approximately invariant over a wide range of frequencies. The minimum variance beamforming (MVB) approach is used to adapt the small set of weights, as if it is a narrowband array. Design examples and simulation are given to demonstrate the usefulness of the proposed FI UCCA in broadband DOA estimation and beamforming.

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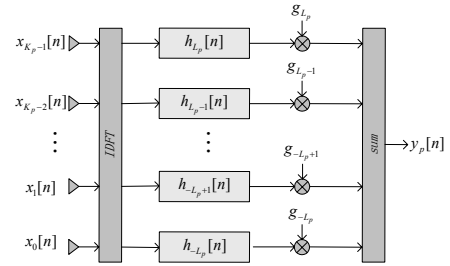


Figure 4. UCCA-FIB block diagram for the p^{th} ring.

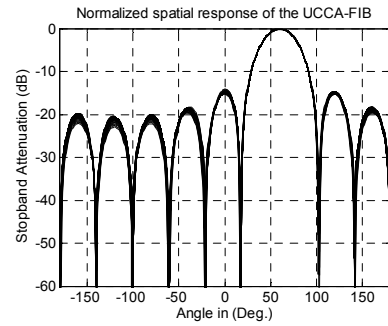


Figure 5. Spatial response of the UCCA-FIB.

FIGURES

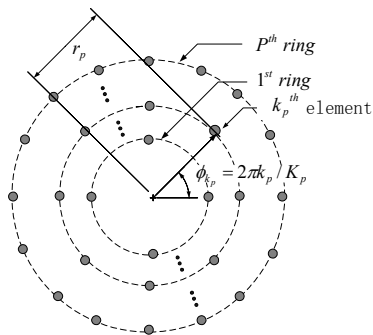


Figure 1. A UCCA with P rings and K_p -sensor at each ring.

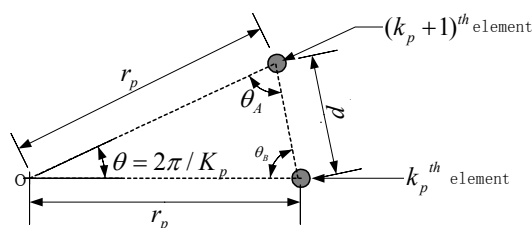


Figure 2. Relationship between inter-sensor spacing and the radius of the p^{th} ring of the UCCA.

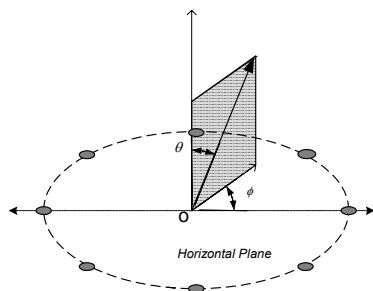


Figure 3. Geometry of the reference imaginary frame.

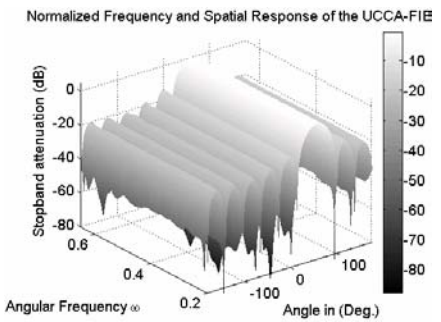


Figure 6. Spatial response and frequency response of the UCCA-FIB.

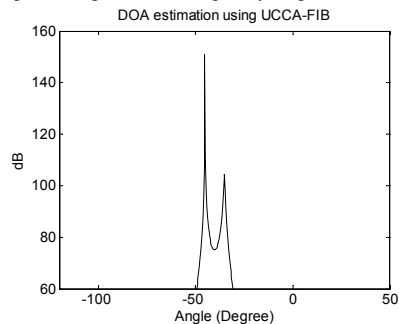


Figure 7. DOA estimation of two noncoherent sources based on the UCCA-FIB.

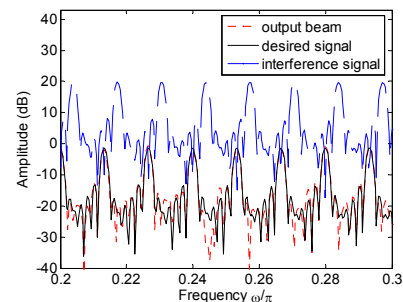


Figure 8. Adaptive beamforming using the UCCA-FIB: (red) beamformer output, (blue) interference signal, (black) desired signal in frequency domain.