



Experimental and finite element analysis of hybrid fiber reinforced concrete two-way slabs at ultimate limit state

Qaiser uz Zaman Khan¹ · Muhammad Ali² · Afaq Ahmad¹  · Ali Raza³ · Muhammad Iqbal⁴Received: 3 September 2020 / Accepted: 24 December 2020
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Abstract

Concrete is a brittle material that is weak in tension and is prone to internal microcracking. With the constant demand for improvement in concrete's durability and mechanical properties, the use of fiber reinforcements has shown promising results. The findings of this paper are based on test results on hybrid fiber reinforced concrete (HFRC) samples of simply supported two-way slabs, produced with a selected volumetric proportion of steel fiber (SF) and polypropylene fibers (PPF). A total of twenty-one specimens were fabricated. Concrete slab specimens were tested under flexural loading and their response in terms of strain, deflection, first crack, and ultimate failure loading was determined. The dosage of SF in concrete ranged from 0.7 to 1.0%, whereas 0.1–0.9% PPF was used by volume of concrete. It was found that a combination of 0.9% SF and 0.1% PPF gave favorable results for loading capacity, ductility, and cracks. A Finite Element Analysis (FEA) of the proposed HFRC two-way slabs was also performed via ABAQUS. The outputs from numerical modeling showed a close agreement with the experimental results. Using the selected FEA model, an extensive parametric study was also done to examine the effect of various parameters including longitudinal reinforcement ratio, compressive strength of concrete, and the concrete cover of specimens. The proposed FEA model presented a close agreement with the experimental outcomes.

Keywords Two-way slabs · Finite element analysis · Load-carrying capacity · Fiber reinforcement · Crack patterns

List of symbols

f'_c	Compressive strength of concrete
ϵ_c	Ultimate strain of plain concrete
f'_{cm}	Compressive strength of reinforced concrete
f'_t	Ultimate tensile stress of concrete
$\epsilon_{c,1}$	Strain of concrete at ultimate compressive strength
ρ_l	Main reinforcement ratio in slabs
$\epsilon_{c,u}$	Ultimate strain of concrete at failure
E_{cm}	Elastic modulus of reinforced concrete

1 Introduction

Concrete is a widely used construction material, but it carries some limitations in properties such as tensile strength, post-cracking, ductility, fatigue resistance and has brittle failure [1, 2]. The brittleness of concrete with its increased strength is the main concern of concrete. Therefore, increasing the strength of concrete leads to lower ductility which is a serious drawback of using concrete in construction works. This drawback between strength and ductility of concrete can be compensated by incorporating short fibers [3]. Micro-cracks produced in concrete cause the weakness in the resistive properties of concrete which can

✉ Afaq Ahmad, afaq.ahmad@uettaxila.edu.pk; Qaiser uz Zaman Khan, dr.qaiser@uettaxila.edu.pk; Muhammad Ali, muhammad.ali@port.ac.uk; Ali Raza, aliraza@piet.edu.pk; Muhammad Iqbal, afaq.ahmad@uettaxila.edu.pk | ¹Department of Civil Engineering, University of Engineering and Technology, Taxila 47080, Pakistan. ²School of Civil Engineering and Surveying, University of Portsmouth, Portsmouth 03801, UK. ³Department of Civil Engineering, Pakistan Institute of Engineering and Technology, Multan 66000, Pakistan. ⁴Creative Engineering and Management Solutions, Deans Centre Peshawar, Peshawar 25000, Pakistan.



be reduced by using different fibers [4]. Steel fibers (SF) are usually used to increase the ductility and crack resistance of concrete. In tunnel linings, slabs, and concrete pavements, it was examined that it is advantageous to use 0.5% SF by volume [5–8]. However, for controlling the shrinkage cracks, a low-volume fraction of 0.1% polypropylene fibers (PPF) and glass fibers (GF) by volume is suggested [9, 10].

The enhancement of the compressive strength of concrete occurs due to the addition of hybrid fibers. This enhancement has resulted from a good mechanical bond between the cement matrix and fibers causing the delay in micro-crack formation [11]. The addition of hybrid fibers bridges the cracks more effectively and enhances the flexural strength, splitting tensile strength, and flexural toughness of concrete. Moreover, the hybrid fibers are more effective in arresting the micro and macro cracks [12, 13]. The incorporation of single fibers has no significant effect on the compressive strength but improves the tensile and flexural performance of concrete [14, 15]. Steel fibers are efficient to increase the ductility and resistance to cracking in concrete. Moreover, the shrinkage cracks can be controlled by using a volumetric ratio of 0.1% of steel and glass fibers [16]. However, a combination of various fibers is found to be efficient for the improvement of different mechanical properties, impact, and blast resistance of concrete under normal and elevated temperatures [17–19].

In the literature, the researchers traditionally worked on the experimental performance of fiber-reinforced slabs. Labib [20] explored the structural performance of HFRC (steel and polypropylene fibers) slabs in terms of their punching failure mechanism and concluded that the punching shear behavior is significantly improved by adding the hybrid fibers instead of plain concrete or by using one type of fiber. Meng et al. [21] investigated the behavior of SF reinforced alkali-activated geopolymer concrete slabs that were exposed to the natural gas explosion and portrayed that these types of specimens can significantly withstand the methane gas explosion. After investigating the performance of steel fiber reinforced concrete slabs for the service loads, McMahon and Birely [22] concluded that the steel fibers can be used in a bridge deck to satisfy its service performance. The experimental study on the HFRC slabs depicted that the punching shear behavior of HFRC slabs performed in a good manner due to the addition of hybrid fibers [23]. The addition of hybrid fibers in the slabs and concrete bridge decks significantly improve the resistance against the punching failure and increase the ductility and load-carrying capacity of slabs [24, 25].

It consumes a lot of money and time to cast the large-scale specimens of structural members and analyze them. To overwhelm this problem, one can move towards the nonlinear finite element analysis (FEA). By comparing with experiments, finite element work saves time and cost by

simulating the models which can predict the structural performance and complexity of damage behavior of members accurately [26]. The numerical model should not be complex concerning mesh sizes and element types and there should be a balance among these parameters to reduce the analysis time and to increase the accuracy of the results. Therefore, finite element simulations with strong background knowledge are more economical and efficient methods and can be used as a convenient tool for engineering research [27]. Extensive research has been performed in the literature for finite element modeling of fiber-reinforced specimens [28, 29]. However, none of the researchers proposed the numerical model for predicting the structural performance of HFRC two-way slab specimens.

The purpose of this research is to examine the effects of hybrid fibers on the structural performance of two-way slabs. For this in the Sect. 2, there is detail discussion about the materials used for the casting of 21 two-way HFRC slab specimens reinforced with various ratios of SF and PPF, and tested under center-point loading to determine their load-deflection and cracking behavior. In the Sect. 3, a finite element model was proposed using the experimental results of load-deflection curves for predicting the performance of HFRC two-way slabs accurately and to perform an extensive parametric study for investigating the sensitivity of different parameters such as material properties and geometric configurations of two-way slabs. In the Sect. 4, the experimental results of 21 two-way HFRC slab are discussed in detail. In the Sect. 5, the comparative discussion about the experimental and numerical results are discussed. The significance of the present work is to implement the hybrid fibers in the construction industry after studying the different critical parameters such as ultimate capacity, deflection, and cracking behavior, and ductility of slabs due to the incorporation of hybrid fibers. In the last Sect. 6, by using the calibrated numerical models, 3D parametric investigation is conducted for the load carrying capacity of two-way HFRC slab.

2 Testing program

2.1 Materials

Ordinary Portland cement (OPC) according to ASTM Type-I, 43 Grade [30] was used to act as a binding material. Some physical properties of OPC are shown in Table 1. The coarse aggregate passing through sieve size of 25 mm and retained over sieve size of 4.75 mm arranged from Margalla Crush Plants have been used, whereas the fine aggregate passing through sieve 9.5 mm and retained over sieve size of 150 μm taken from Laurancepur was

Table 1 Physical properties of cement

Consistency	Initial setting time	Final setting time	Soundness	Fineness	Specific gravity	Compressive strength of mortar cubes (28 days)
28.75%	1 h and 31 min	3 h & 45 min	No expansion	3190 cm ² /g	3.03	41.1 MPa

Table 2 Properties of fine-aggregate sand coarse-aggregates used in testing

S. No	Description	Fine-aggregates	Coarse-aggregates
1	Specific gravity (SG)	2.67	2.71
2	Fineness modulus	2.40	–
3	Water absorption	1.21%	0.82%

Table 3 Physical properties of fibers

Sr. No	Description	Hooked end steel fiber	Fibrillated polypropylene fiber
1	Length (mm)	38	14
2	Diameter	0.5 mm	22 μm
3	Aspect ratio	76	–
4	Specific gravity	7.85	0.91
5	Tensile strength (MPa)	1100	400
6	Melting point	2530 °C	1700 °C
7	Young's modulus (kN/mm ²)	20	0.45
8	Elongation at failure	3.5%	15%
9	Thermal conductivity	Low	–

used as fine aggregate in the concrete mix according to [31]. Properties of fine and coarse aggregates based on laboratory testing are described in Table 2.

The fibers used in this research were steel fibers and polypropylene fibers. The physical properties of these fibers are given in Table 3. Dramix® 3D is a hooked ended cold drawn wire fiber. ASTM A-820 [32] specifies its classification as Type-I fiber. For even dispersion through the matrix, it is manufactured as glued in bundled. This type of fiber is mainly used in the mining industry. The construction industry is preferring the use of these fibers in tunneling and underground projects. In Pakistan, these fibers were used in the “Neelam Jhelum Project” for tunneling in Dam. Polypropylene fibers employed for this research work are known as Chemrite polypropylene fibers. These fibers help in reducing the plastic and drying cracks while improving the surface properties and durability of concrete. Both types of fibers were presented in Fig. 1.

The workability of the concrete mixture is decreased by the addition of different types of fibers [33].

**Fig. 1** PF and SF used in the present work**Table 4** Properties of superplasticizer used in concrete mixes

Sr. No	Description	Details
1	The density of admixture at 25 °C	Approximately 1.18 kg/lit
2	pH value of NN	Approximately 8
3	The chloride content of NN	Nil (EN 934–2)
4	Toxicity	Non-toxic
5	Transportation	Non-hazardous

Polynaphthalene based admixture namely Chemrite-NN was used as substantial water reducing agent at 0.6–2% by weight of cement complies with ASTM C494 [34] to increase the workability of freshly prepared FRC. Superplasticizers have many advantages such as increasing the workability and placing of concrete, early setting property, and minimum risk of segregation. Different properties of the superplasticizer used in the present study are listed in Table 4.

2.2 Fabrication and testing of samples

Twenty HFRC and one plain cement concrete (PCC) two-way slab specimens with dimensions of 900 × 900 × 100 mm were manufactured by using hybridization of four different volumetric fractions of SF (0.7%, 0.8%, 0.9%, 1%) and five that of PPF (0.1%, 0.3%, 0.5%, 0.7%, 0.9%) to produce different combinations of fibers for each specimen. The ratios of fibers were selected to avoid the cracks and shrinks during the early stages [22]. The mix design of concrete was kept the same for all the specimens with ratios of 1:1.4:2.8:0.48 representing the

ratios of cement, fine aggregates, coarse aggregates, and water to cement content, respectively (see Table 5).

Each mix design of samples is differentiated by using different volumetric ratios of hybrid fibers. Six steel bars of 10 mm diameter having a yield strength of 420 MPa were used at equal spacing in both directions with a concrete cover of 20 mm on sides and 15 mm on top and bottom surfaces. In sample labeling, 'S' represents the slab specimen, the first numeric word after 'S' represents the ratio of SF, and the second numeric word represents the ratio of PPF. During the casting of slab specimens, concrete cylinders for each mix design were also cast to determine the compressive strength of concrete with different fiber ratios. The average compressive strength values for each mix design are presented in Table 6.

The sketch of the plan view and cross-sectional view of two-way slabs after preparing the sample for the experimental testing were shown in Fig. 2. The loading was applied to the center point of the slab using a load cell of 2000 kN capacity. The specimens were 900 × 900 mm in plan-view and their thickness was 100 mm. Three strain gauges (at the shown locations) and one Linear Variable Differential Transformer (LVDT) at the center of the specimen were attached to measure the required parameters including vertical deflections and the strains in concrete and reinforcement. The load was applied at the central region of the two-way slabs using a load cell. The ends of the slabs were adjusted in such a way that one end performed as a roller support and the other end performed as a hinge support.

Table 5 Quantities of concrete constituents

Material	Density (Kg/m ³)
Cement	468.26
Coarse aggregates	1310.86
Fine aggregates	655.43
Superplasticizer	0.5% by volume
Water	220.08
Steel fiber	0–1.0% by volume
PP fiber	0–0.9% by volume

3 Finite element modelling

In the current research, the numerical work was performed using a general-purpose commercial program ABAQUS 6.14 [35]. The FEA model saves the cost and time required for experimentation. The concrete material and reinforcing bars were modeled as 3D stress and truss elements, respectively. A control numerical model was simulated using the experimental results of the load-deflection performance of control two-way slab specimen (S0.7–0.1).

Table 6 Test matrix of specimens and ratios of fibers

Sr. No	Mix design	Sample Label	SF (%)	PPF (%)	Total volumetric ratio of fibers (%)	Compressive strength (MPa)
1	S2M-1	S0.0–0.0	0.0	0.0	0.0	23.51
2	S2M-2	S0.7–0.1	0.7	0.1	0.8	28.34
3	S2M-3	S0.7–0.3	0.7	0.3	1.0	31.91
4	S2M-4	S0.7–0.5	0.7	0.5	1.2	31.59
5	S2M-5	S0.7–0.7	0.7	0.7	1.4	25.08
6	S2M-6	S0.7–0.9	0.7	0.9	1.6	24.14
7	S2M-7	S0.8–0.1	0.8	0.1	0.9	29.3
8	S2M-8	S0.8–0.3	0.8	0.3	1.1	28.96
9	S2M-9	S0.8–0.5	0.8	0.5	1.3	20.55
10	S2M-10	S0.8–0.7	0.8	0.7	1.5	20.66
11	S2M-11	S0.8–0.9	0.8	0.9	1.7	17.32
12	S2M-12	S0.9–0.1	0.9	0.1	1.0	30.44
13	S2M-13	S0.9–0.3	0.9	0.3	1.2	26.35
14	S2M-14	S0.9–0.5	0.9	0.5	1.4	24.26
15	S2M-15	S0.9–0.7	0.9	0.7	1.6	29.62
16	S2M-16	S0.9–0.9	0.9	0.9	1.8	22.61
17	S2M-17	S1.0–0.1	1.0	0.1	1.1	28.87
18	S2M-18	S1.0–0.3	1.0	0.3	1.3	20.71
19	S2M-19	S1.0–0.5	1.0	0.5	1.5	24.68
20	S2M-20	S1.0–0.7	1.0	0.7	1.7	26.9
21	S2M-21	S1.0–0.9	1.0	0.9	1.9	18.32

Fig. 2 Schematic plan view and the cross-sectional view of testing of two-way slab

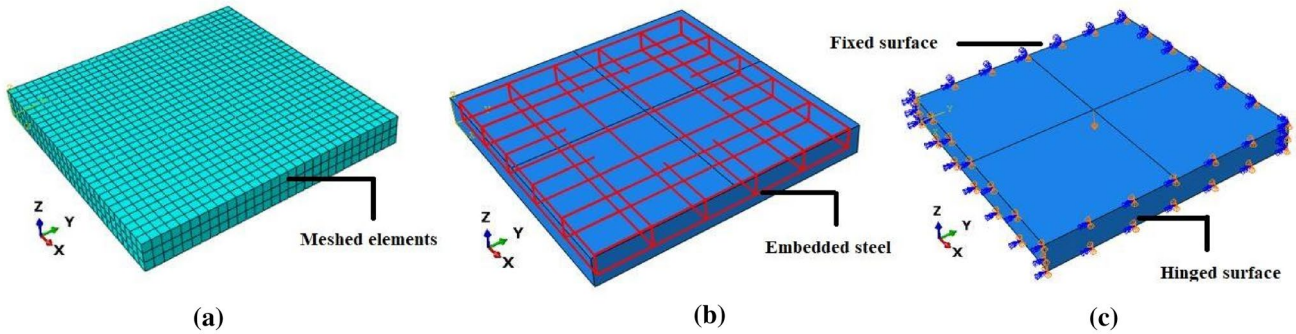
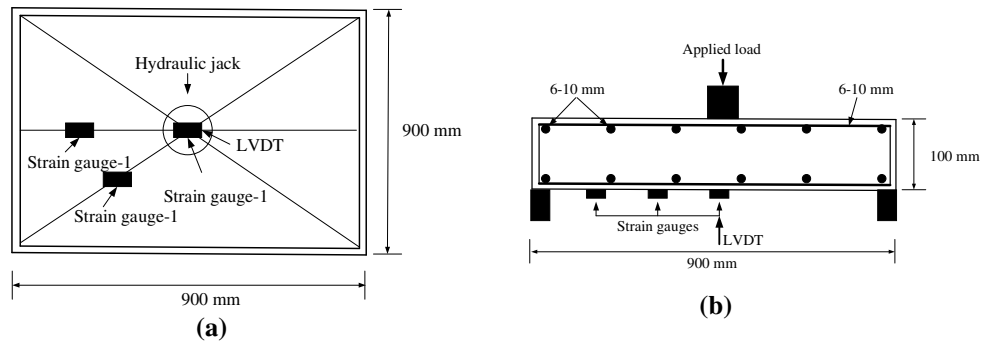


Fig. 3 Geometry and boundary conditions of the finite element model of the two-way slab (a) meshing (b) embedded region constraint (c) boundary conditions

Two sides of specimens were kept fixed in all directions and the other two were kept hinged to resist reactions and deflections in vertical and lateral directions. A point load was applied to the center of the two-way slab specimens using the displacement control method as represented in Fig. 3. The behavior of concrete and steel bars were simulated using the concrete damaged plasticity (CDP) model and bilinear elastoplastic model, respectively. For the validation of the control numerical model, an extensive calibration work was performed by considering the sensitivity of different material and geometric parameters of the specimen.

3.1 Materials simulations

The accuracy of the constitutive FEA model will be more if the boundary conditions and materials properties are defined accurately which is a complex task. The accurate simulation of the complex nonlinear behavior of concrete material under triaxial loading is a challenging task. The experimental stress–strain curves of each specimen with different quantities of SF and PPF were used for the definition of concrete behavior taken from [19]. For the definition of elastic behavior of concrete, two parameters are required in ABAQUS; one is elastic modulus and the second is the Poison’s ratio. Elastic modulus of concrete was

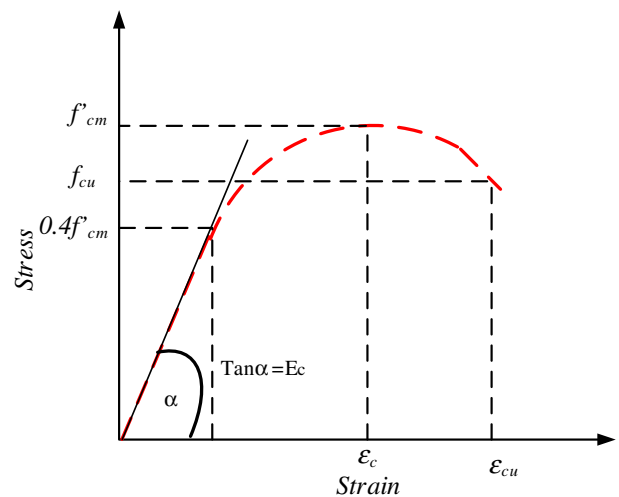


Fig. 4 Stress–strain performance of RC structures according to Euro code 2

taken as $4700\sqrt{f'_c}$ and the Poison’s ratio was taken as 0.2 up to $0.4f'_c$ [36] (see Fig. 4). The CDP model in ABAQUS can accurately predict the nonlinearity and complexity of plain and reinforced concrete [37, 38] and therefore, this model was used in the current work for the simulations of the

inelastic behavior of reinforced concrete (RC). The parameters for plastic behavior were calibrated using different values to achieve the results closer to experimental predictions. For the simulations of compressive damaging behavior of concrete, Eq. (1) and Eq. (2) were utilized for the calculations of compressive strains ($\epsilon_{c,1}$ and $\epsilon_{cu,1}$) and Eq. (3) was used for the calculations of compressive stress (f'_c) of RC [39].

$$\epsilon_{c,1} = 0.0014[2 - e^{-0.024f_{cm}} - e^{-0.140f_{cm}}] \tag{1}$$

$$\epsilon_{cu,1} = 0.004 - 0.0011[1 - e^{-0.0215f_{cm}}] \tag{2}$$

$$f'_c = f_{cm} \frac{k\eta - \eta^2}{1 + (k - 2)\eta} \tag{3}$$

where $k = 1.05E_{cm} \frac{\epsilon_{c,1}}{f_{cm}}$ and $\eta = \frac{\epsilon_c}{\epsilon_{c,1}}$ where f_{cm} is the maximum compressive strength of reinforced concrete. To define the tensile behavior of concrete is essential for the flexural members because of the tensile stresses on the bottom side of the slabs. The stress–strain model of concrete under tension should include the strain hardening and softening behavior and interaction between steel bars and concrete material. The tension stiffening model used in the present research has been represented in Fig. 5. The ultimate tensile stress (f'_t) was calculated using Eq. (4) as proposed by [39].

$$f'_t = 0.33\sqrt{f'_c} \text{ (MPa)} \tag{4}$$

The steel reinforcement having 420 MPa yield strength was used in the present research. The steel reinforcement was simulated as truss elements available in ABAQUS. The elastic behavior was defined by Young’s modulus of

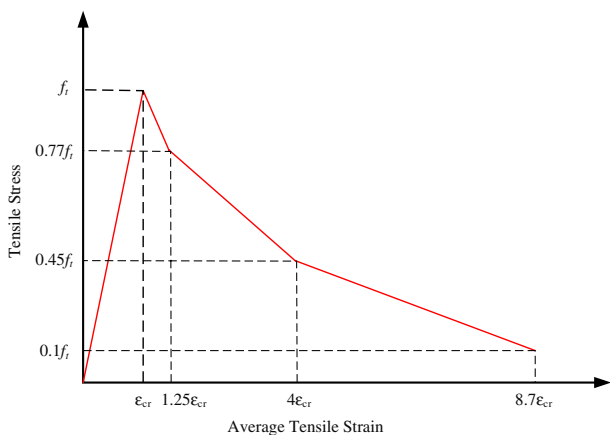


Fig. 5 Tensile model of concrete

200 GPa and Poison’s ratio of 0.3. The simulation of plastic behavior of steel bars was performed by considering elastoplastic material with the bilinear performance of the stress–strain model having a strain hardening ratio of 0.01% for the second linear line [40] as shown in Fig. 6.

3.2 Calibration and validation of control model

The control FE model was calibrated and validated using the experimental results of the load–deflection behavior of S0.7–0.1. Different material parameters of concrete in the plastic region such as the angle of dilation stresses ratio, viscosity parameter, and shape factor parameter were calibrated using different values to achieve optimum accuracy as represented in Fig. 7. The different values of dilation angle used for the calibration were 45, 42, 39, 36, 33 and 30 degrees and that of viscosity parameter were 0.064, 0.053, 0.042, 0.031, 0.020 and 0.009. The governing parameter during the calibration process was found to be the viscosity parameter. An increase of 136% occurred in the loading capacity when this parameter increased from 0.009 to 0.64. Similarly, the different values were calibrated for stress ratio and shape factor of concrete yielding. A negligible effect was observed due to the variation of stress ratio and shape factor of concrete. However, the viscosity parameter of 0.02, dilation angle of 42 degrees, shape factor of 0.667, and a stress ratio of 1.16 gave the best results as compared with experimental predictions.

The sensitivity analysis due to variation of element types of concrete and reinforcement was also performed. All the types of 3D-stress elements of concrete material available in the ABAQUS library were examined and similarly, the effects of different truss elements of 3D-planer reinforcement bars were also observed, represented in Fig. 7. It was observed that 3-dimensional 8 node brick elements with reduced integration (C3D8R) for concrete as recommend by [40] and 3-dimensional 2 node truss

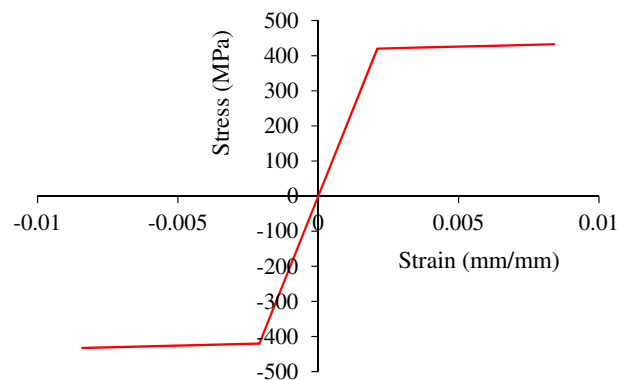


Fig. 6 Bilinear behavior of reinforcement

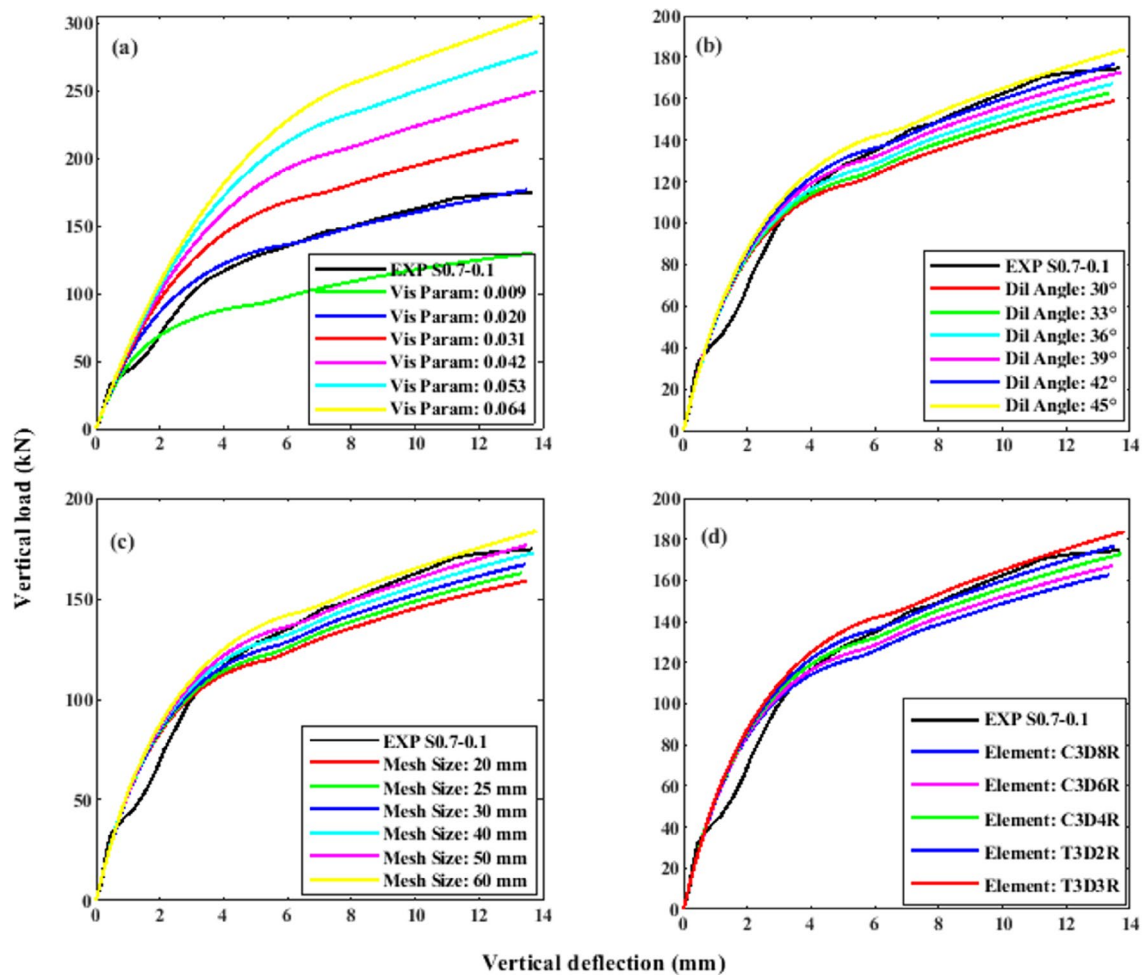


Fig. 7 Sensitivity analysis of load-deflection curve due to **a** Viscosity parameter **b** Dilation angle **c** Mesh size **d** element types of concrete and steel reinforcement

elements with reduced integration (T3D2R) for steel bars gave the close results in comparison with that of experiments.

The sensitivity analysis due to the size of elements of concrete and steel bars was observed by studying the mesh sizes of 60, 50, 40, 30, 25, and 20 mm, respectively. The effect of using different mesh sizes on the load–deflection behavior of a two-way slab control specimen was represented in Fig. 7. In linear FEA, the accuracy of outputs usually increases by decreasing the mesh size, but it does not hold for NLFEA [40]. The mesh size should not be small enough to increase the time of analysis for the computer. After an extensive calibration for various element sizes, it was observed that the mesh size of 30 mm gave close agreement with the experiments, and hence, this size was selected for the further analysis of remaining specimens and parametric study.

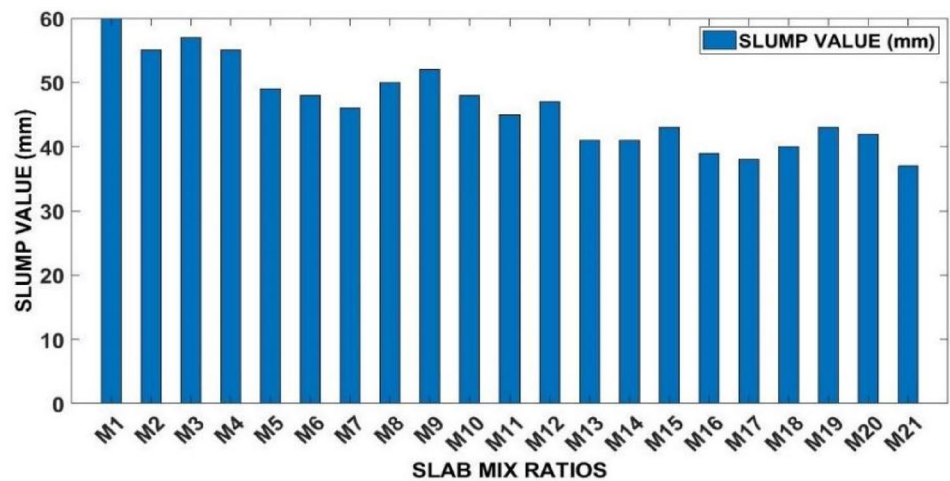
4 Experimental results and discussions

4.1 Workability of mixes

It is widely accepted that controlling the workability of fiber reinforced concrete is cumbersome due to the presence of fiber which decreases workability than ordinary mix. To increase the workability of the concrete mix, the superplasticizer named Chemrite NN was used. For measuring the workability of FRC, a slump cone test according to ASTM C143/C143M-15a [41] was performed for each batch of concrete. The workability of concrete was controlled in the range of 25–75 mm of slump cone as represented by Fig. 8.

It is obvious that the control mix has maximum workability and the minimum slump was noted for mix having

Fig. 8 Slump values of different concrete mixes



steel fibers with a volume fraction of 1% of concrete and 0.1% of polypropylene fiber. Mixes with steel fibers are much stiffer than mixes with polypropylene fibers due to the accumulation of water around steel fibers resulting in a reduction of free water in the mix. In the case of mix having only polypropylene fibers, workability was close to that of the control mix due to the softness of polypropylene fibers. Accumulation of water around fibers was quite less as seen in the case of steel fibers.

4.2 Flexural testing of slabs

The flexural behavior of two-way slabs was determined using different volumetric ratios of steel fibers and polypropylene fibers, a center point loading test was performed to check the first cracking load and the value of ultimate failure load. The deflection in slabs was measured using LVDT placed at the center of the slab, where maximum deflection was supposed to have occurred. Three strain gauges were also placed at different locations to measure strain response on the bottom fiber of the

specimens. Strain gauges were connected to a Whishay strain indicator and recorder P3 box. The deflection and three strains were recorded. The schematic diagram for the arrangement of measuring devices is given in Fig. 2 and the experimental testing was presented in Fig. 9. The complete structural and flexural analysis was performed using data recorded during testing. The experimental results in terms of initial and final cracks loads and corresponding deflections were presented in Table 7.

4.3 Load pattern in HFRC slab

During the application of load with the help of loading jack on slabs, the appearance of cracks in flexure was observed, which indicates the yielding zone. These values indicate that the specimen is starting to fail. The comparison of these cracks showed that each specimen has the separate cracking patterns with different combinations of hybrid fibers. This clearly shows that both fibers complement each other to produce the best results. These fibers need to be in perfect ratio to give maximum strength. Figure 10

Fig. 9 Flexural testing of specimen **a** Top view of the specimen **b** Bottom view with LVDT



(a)



(b)

Table 7 Experimental flexural testing results of HFRC two-way slabs

Mix ratio	Label	First crack load (kN)	Ultimate load (kN)	First crack deflection (mm)	Ultimate deflection (mm)
S2M-1	S0.0-0.0	35.84	159.53	2.832	11.03
S2M-2	S0.7-0.1	44.8	174.62	1.692	13.67
S2M-3	S0.7-0.3	67.2	192.43	1.118	9.31
S2M-4	S0.7-0.5	89.6	189.76	2.734	7.97
S2M-5	S0.7-0.7	53.76	201.53	1.481	10.91
S2M-6	S0.7-0.9	53.76	209.05	2.089	11.85
S2M-7	S0.8-0.1	53.76	171.31	1.285	9.55
S2M-8	S0.8-0.3	53.76	201.96	1.745	14.04
S2M-9	S0.8-0.5	67.2	221.21	2.768	15.12
S2M-10	S0.8-0.7	40.32	190.34	2.468	14.51
S2M-11	S0.8-0.9	67.2	154.76	1.694	8.98
S2M-12	S0.9-0.1	112	223.93	4.101	15.42
S2M-13	S0.9-0.3	67.2	176.52	1.952	10.56
S2M-14	S0.9-0.5	67.2	206.26	2.054	11.15
S2M-15	S0.9-0.7	89.6	179.91	2.624	13.2
S2M-16	S0.9-0.9	44.8	197.06	1.026	10.64
S2M-17	S1.0-0.1	89.6	211.7	2.824	12.53
S2M-18	S1.0-0.3	89.6	208.11	2.52	12.09
S2M-19	S1.0-0.5	80.64	150.93	2.77	8.22
S2M-20	S1.0-0.7	67.2	167.63	1.928	10.14
S2M-21	S1.0-0.9	67.2	111.18	1.527	6.67

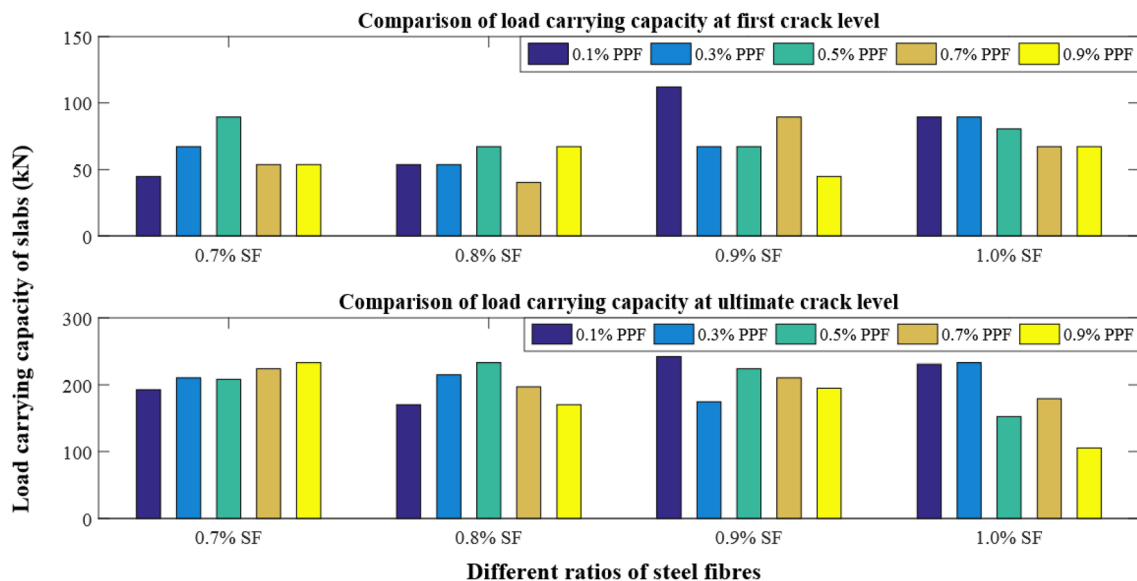


Fig. 10 First crack loads and ultimate loads of all slab specimens

shows the comparison of first crack loads for the different volumetric ratios of steel and polypropylene fibers.

A comparison of the values shows that using both fibers increases the strength of concrete concerning the control specimen. The maximum resistance against the

first crack was endured by the S0.9-0.1. It carried the load of 112 kN before the first crack appeared. The control specimen cracked at the loading of 35.84 kN. The first crack strength of specimen S0.9-0.1 has a 213% increase. The initial crack values of S0.7-0.5, S0.8-0.5, and S1.0-0.3

were 89.6 kN, 67.2 kN, and 89.6 kN, respectively which shows a 150%, 88%, and 150% increase, respectively. The combination of 0.9% SF and 0.1% PPF performed in a well manner showing the maximum loading capacity. This may be ascribed to a good bridging effect of fibers at this percentage. At the ultimate loading stage, the deflection was increased considerably but the load-carrying capacity was continuously decreasing. The ultimate capacity for each type of slab was observed as represented in Fig. 10.

Almost all the slabs were failed in flexure and the cracks also extended up to the outer edges of the slabs. The increase in loading was observed from 5.56 to 50.0% except for slabs S1.0-0.5 and S1.0-0.9. In these samples, the reduction in ultimate strength was observed to be 5.56 and 34.74%, respectively. This is because of the fluctuation of both the fibers, balling action, improper mixing, and thus resulting in bleeding of the concrete mix. The results are consistent with the first crack loading.

The values in the above graph clearly show that each group follows the same trend. The load-carrying capacity increasing up to a particular ratio and after that value starts to decrease. It follows the same trend in every group. The maximum resistance against the ultimate loading was ensured by S0.9-0.1. It carried the load of 223.93 kN before completely failing. The control specimen S0.0-0.0 was fully cracked at the loading of 159.53 kN. The ultimate strength of specimen S0.9-0.1 has a 40.36% increase. The values of S0.7-0.5, S0.8-0.5, and S1.0-0.3 were 189.76 kN, 221.21 kN, and 208.11 kN, respectively which shows 18.94%, 38.66%, and 30.45% increase, respectively. These combinations of the hybrid fibers portrayed a good performance in terms

of loading strength due to an efficient bridging effect of fibers.

4.4 Deflection pattern in HFRC slab

With the application of load, the deflection in the two-way slab was observed. The deflection in the slab was measured with the help of LVDT. One LVDT was placed at the bottom center of the slab. During testing of concrete slabs, the deflection was noted just after the appearance of the first crack for each type of slab and presented in Fig. 11. The slab was examined at each load increment to check the propagation of cracks and it was noted that the crack was initiated from the middle of the slab and then towards the outer periphery in a regular manner. Maximum deflection at first crack load was achieved by the specimen S0.9-0.1 which is 44.81% more than the control specimen S0.0-0.0. The deflection at first crack observed in the control specimen was 2.832 mm. With the addition of steel fibers, the stiffness of the section increased but with the addition of polypropylene fibers an increase in the slab deflection was observed as compared with the control model (S0.0-0.0). The increase in the deflection caused an increase in the strain absorption of each specimen which means an increase in the modulus of resilience and modulus of toughness which are the two basic flexural properties of concrete. Ultimate deflection is defined as the deflection at which the specimen reached its maximum load when there is no further load-carrying capacity in the slab. Ultimate deflections of all slabs were presented in Fig. 11.

The deflection at the first crack of the slab S0.9-0.1 was higher than that of all other slabs and also when specimens

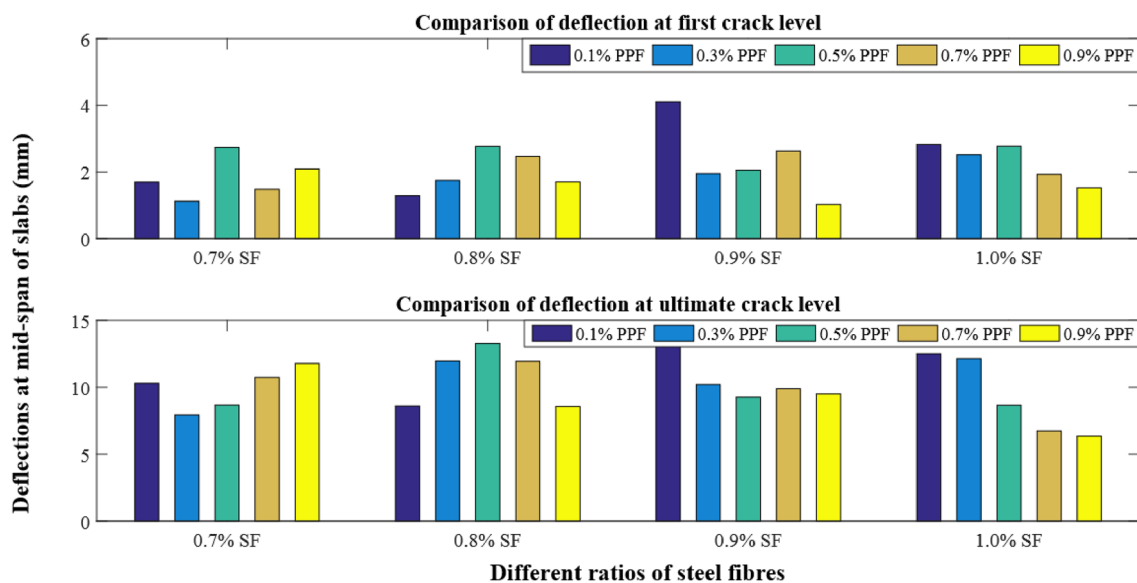


Fig. 11 Deflections at ultimate loads

reached their ultimate loading capacity, the specimen S0.9-0.1 having fibers contents of 0.9%SF + 0.1%PPF by volume of concrete showed maximum deflection with comparison to other specimens. This is because slab S0.9-0.1 has maximum loading capacity. Maximum deflection at ultimate load was achieved by S0.9-0.1 specimen which is 15.42 mm and is 39.80% more than the control specimen S0.0-0.0. The deflection observed in the control specimen was 11.03 mm. In conclusion, the application of flexural loading caused a significant amount of deflection which was measured using LVDT. The increase in deflection was 44.81% for S0.9-0.1 at first crack load whereas 39.80% for ultimate load in comparison with the control specimen. Load carrying capacity increased up to an optimum value of 213% for the first crack loading condition and 40.36% for the ultimate loading condition for S0.9-0.1 slab as compared to the control slab.

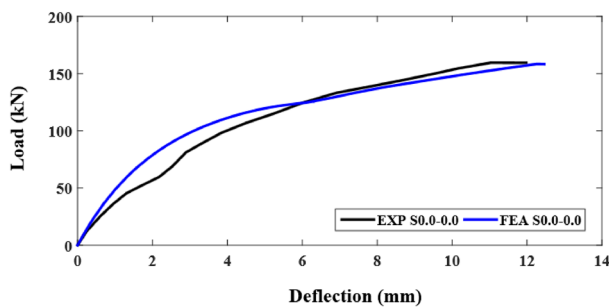


Fig. 12 Load-deflection performance of control model for experimental and numerical results

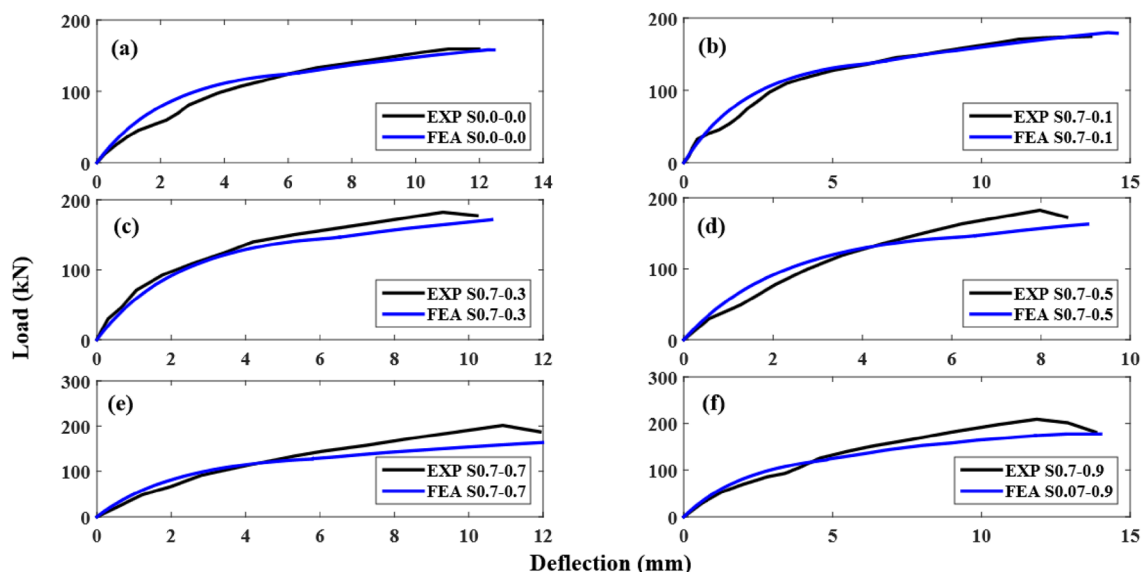


Fig. 13 Experimental and numerical load-deflection curves for two-way slabs with **a** plain concrete and 0.7% SF along with combination of **b** 0.1% PPF **c** 0.3% PPF **d** 0.5% PPF **e** 0.7% PPF **f** 0.9% PPF

5 Finite element results

5.1 Control specimen

The load-deflection curve for the control specimen was shown in Fig. 12. It can be observed that the discrepancy between experimental and numerical predictions is 2.89 and 4.24% for slab capacity and corresponding deflection, respectively. This discrepancy may be associated with the perfect bond assumed between reinforcement and concrete elements in the form of a 'tie' constraint in ABAQUS. Moreover, these minor discrepancies may be ascribed to the small imprecisions and imprecise results due to the differences between the actual testing experimental conditions such as initial geometric imperfections, different boundary conditions, varying strength of steel bars, the strength of concrete material, manufacturing faults of the specimens, the accuracy of the testing instruments and the conditions assumed in the FEA modeling. However, the proposed constitutive finite element model gives a close agreement between experiments and numerical results.

5.2 Load-deflection curves

To measure deflection at mid-span of the slab, one LVDT was placed below the center of the two-way slab. The deflection was noted for every increment of loading using a load cell positioned above the slabs. The load-deflection curves for all the slabs were shown in Figs. 13, 14, 15 and 16. It was observed that the initials,

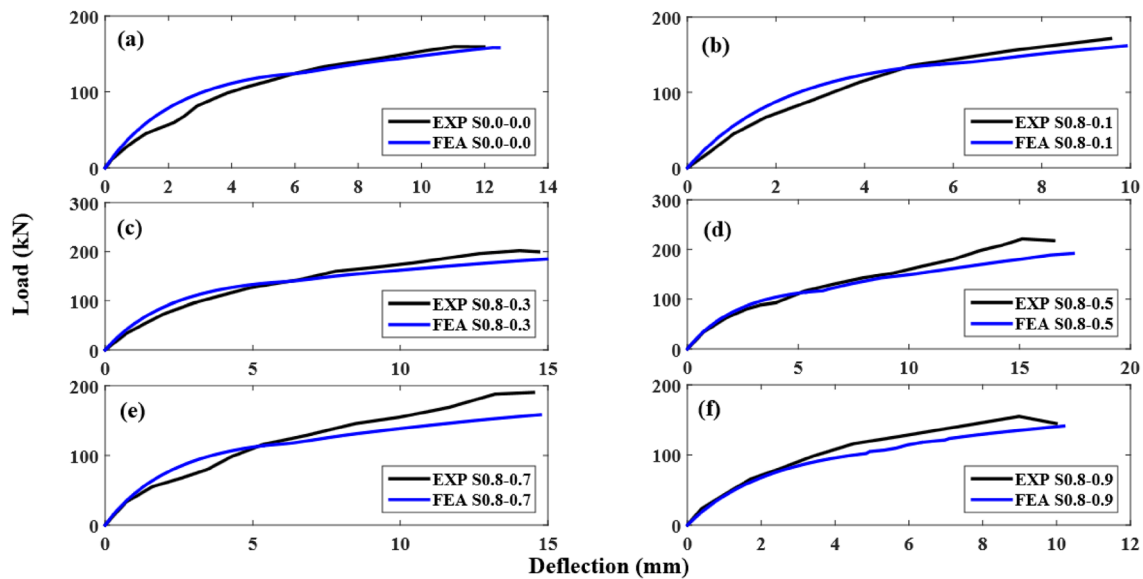


Fig. 14 Experimental and numerical load-deflection curves for two-way slabs with **a** plain concrete and 0.8% SF along with combination of **b** 0.1% PPF **c** 0.3% PPF **d** 0.5% PPF **e** 0.7% PPF **f** 0.9% PPF

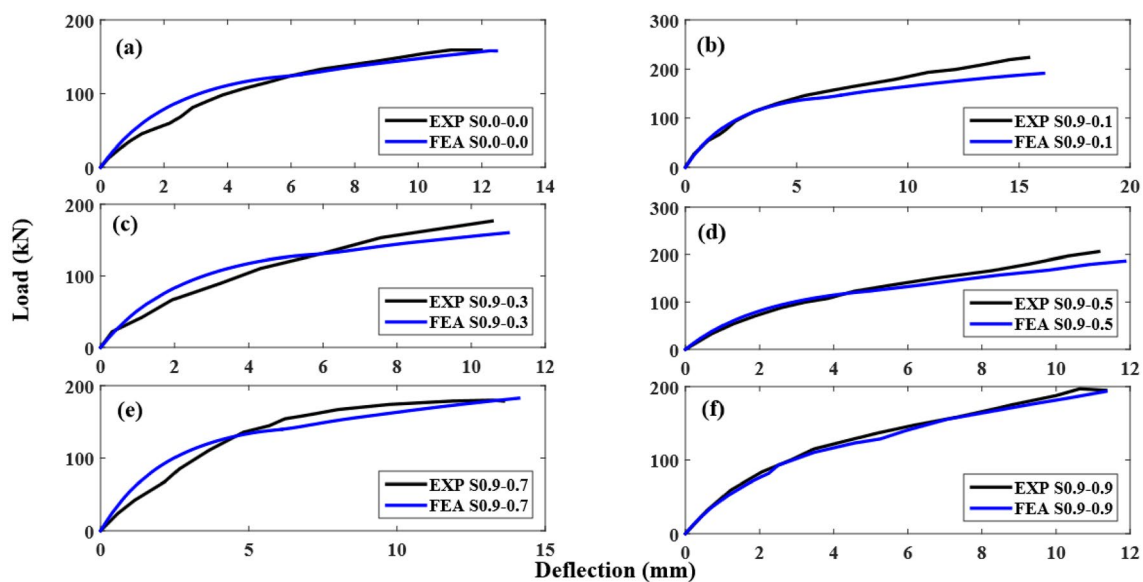


Fig. 15 Experimental and numerical load-deflection curves for two-way slabs with **a** Plain concrete and 0.9% SF along with combination of **b** 0.1% PPF **c** 0.3% PPF **d** 0.5% PPF **e** 0.7% PPF **f** 0.9% PPF

as well as the ultimate load-carrying capacity of slab S0.9-0.1, were quite high compared to control specimen S0.0-0.0. But it can also be observed that at initial stages both curves (experimental curve and FEA curve) are almost overlapping each other but after the elastic state, the loading capacity was changed abruptly. This is due to the reason that the fiber-reinforced concrete improved the post elastic properties of structural members [42]. It was worth mentioning that deflection at the ultimate

failure of the control specimen was low in comparison with that of S0.9-0.1.

Figure 13 reports the complete load-deflection curves for the specimens with 0.7% SF. The load-deflection curves of S1.0-0.5 and S1.0-0.9 were plotted with load at the vertical axis and deflection at the horizontal axis to compare behavior with that of the control specimen. The curves for S1.0-0.5 and S1.0-0.9 have a sudden failure at the ultimate load as there was a little gap between the elastic

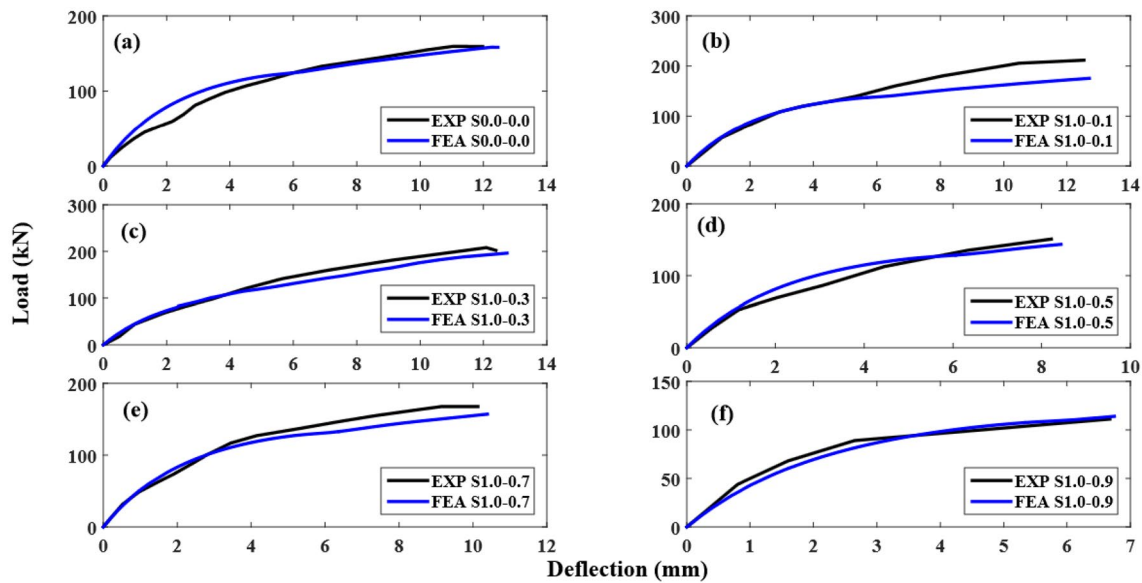


Fig. 16 Experimental and numerical load-deflection curves for two-way slabs with **a** Plain concrete and 1.0% SF along with combination of **b** 0.1% PPF **c** 0.3% PPF **d** 0.5% PPF **e** 0.7% PPF **f** 0.9% PPF

limit stage and the ultimate failure stage. Although slabs S1.0-0.5 and S1.0-0.9 showed a sufficient increase in load at the initial stage as it reached a final cracking load before the control sample. This was because of high steel & polypropylene fiber contents along with flocculation of both fibers, balling action, improper mixing, and thus resulting in bleeding of the concrete mix.

Also, in the same trend load-deflection curves for peak values of S0.7-0.5, S0.8-0.5 and S1.0-0.3 were plotted with load at the vertical axis and deflection at the horizontal axis to compare behavior with that of the control specimen. It was observed that both the initial and ultimate load-carrying capacity of slabs S0.7-0.5, S0.8-0.5, and S1.0-0.3 was quiet high compare to the control specimen. But it can also be observed that at initial stages all curves are almost overlapping each other but after the elastic state load-carrying capacity was changed suddenly. Such behavior is due to the reason that the fiber-reinforced concrete improves the post elastic properties of structural members [42]. It was worth mentioning that deflection at the ultimate failure of the control specimen was low with comparison to that S0.7-0.5, S0.8-0.5, and S1.0-0.3.

For the finite element study of two-way slabs, the experimental load-deflection curves were converted to backbone curves to examine the peak loads and their corresponding vertical deflections. After validation of control FEM, it was used for the further analysis of remaining slab specimens to investigate the applicability and implementation of the structural response of two-way slabs systems. The comparison of experimental and FEA predicted load-deflection behaviors of specimens with 0.7% Sf were

presented in Fig. 13. It was observed that the discrepancies among experimental and FEA observations for the ultimate capacities of the RC slab systems with plain concrete and 0.7% SF were 0.75%, 2.89%, 10.84%, 10.44%, 18.79%, 15.05%, for S0.0-0.0, S0.7-0.1, S0.7-0.3, S0.7-0.5, S0.7-0.7 and S0.7-0.9, respectively. Similarly, the discrepancies for deflection at peak loads were 11.06%, 4.24%, 14.07%, 13.43%, 9.81% and 8.44%, respectively. The average percentage difference among the finite element predictions and experimental measurements of slabs with 0.7% SF was 9.79% and 10.17% for ultimate capacity and corresponding vertical deflection, respectively. The performance of the finite element load-deflection curve in the elastic region was relatively better but in the inelastic region, there were some discrepancies. These minor discrepancies may be ascribed to the reasons due to deviations between experimental and numerical boundary conditions, material properties variations, instrumentation and loading conditions, manufacturing faults, and assumptions made during finite element simulations.

Figure 14 represents the structural response of slab specimens with plain concrete and 0.8% steel fibers along with 0.1%, 0.3%, 0.5%, 0.7% and 0.9% PPF, respectively. The percentage deviations observed from the comparisons of numerical predictions and experiments were 5.60%, 8.48%, 14.75%, 16.81%, and 10.18% for specimens S0.8-0.1, S0.8-0.3, S0.8-0.5, S0.8-0.7, and S0.8-0.9, respectively. Similarly, the discrepancies for deflections were 3.66%, 6.48%, 8.40%, 1.52% and 8.80%, respectively. The average percentage difference was observed to be 11.16 and 577% for an ultimate capacity of two-way slabs and

their corresponding vertical deflections, respectively. This shows that the proposed constitutive FEA model gave better predictions for specimens with 0.8% SF as compared with that of 0.7% SF.

The FEA prediction for the ultimate loads was usually less than the experimental loads after approximately 100 kN. This may be due to the reason that the equations used for the prediction of the stress–strain behavior of HFRC material were initially developed for the plain concrete, but in the current research, they were used for the HFRC. As concerned with the predictions of the FEA model against experimental measurements for two-way slabs with 0.9% SF, they were represented in Fig. 15. The discrepancies of peak load results were 14.45%, 9.27%, 9.61%, 1.54% and 1.79% and that of deflections were 4.41%, 4.07%, 6.37%, 6.82% and 6.58% for the specimens S0.9-0.1, S0.9-0.3, S0.9-0.5, S0.9-0.7 and S0.9-0.9, respectively. On average, the percentage discrepancy for specimens with 0.9% SF was 7.33 and 5.65% for loading capacity and deflections, respectively.

The minimum error from numerical modeling was observed for the specimens reinforced with steel fibers of 1.0% quantity by the total volume of the specimen as shown in Fig. 16. The proposed model presented the discrepancies of 17.09%, 5.69%, 4.88%, 6.28% and 2.56% for peak capacities and 1.36%, 5.38%, 2.68%, 2.47% and 1.05% for deflections of slab specimens S1.0-0.1, S1.0-0.3, S1.0-0.5, S1.0-0.7 and S1.0-0.9, respectively. The average percentage error between the experiments and numerical work was 7.30% and 2.585 for load and deflection, respectively.

The numerical model predictions and experimental testing results for peak loads and corresponding vertical deflections at peak loads were represented in Figs. 17 and 18, respectively. It can be observed that the predictions of

the finite element were underestimated by 17.33% as compared with experimental measurements. This may be associated with the reason that the assumptions made in the FEA model for the bond-slip behavior between steel bars and concrete material were not perfect for the degrees of freedom (DOF) to be transferred from 3D truss elements to the 3D brick elements of concrete. Moreover, the definitions of compression and tension damage behaviors of concrete may also be ascribed to the reason of discrepancies because for flexural loading the accurate definition of these parameters is very important.

It can be observed from Fig. 18 that the predictions of the finite element were overestimated the vertical deflections by 19.5% as compared with experimental measurements. This discrepancy may be due to the assumptions of a perfect bond between steel bars and concrete material which made the slabs stiffer in numerical modeling. But in general, the proposed FE model showed consistent predictions in comparison with experimental measurements and can be used for the further analysis and parametric study of two-way RC slab.

5.3 Crack patterns

The crack patterns were studied during the testing of all specimens. With the use of polypropylene, there was a very large increase in the deflection obtained by specimens as compared to the control specimen. According to experimental results, it can be said that with the use of more polypropylene more elastic behavior of concrete is obtained. But the force of attraction between particles of concrete remains the same hence if larger deflection is obtained it will some time break the bond between particles of concrete hence producing a fissure plane that will cause the spalling of concrete. With

Fig. 17 Experimental and numerical peak loads for all specimens

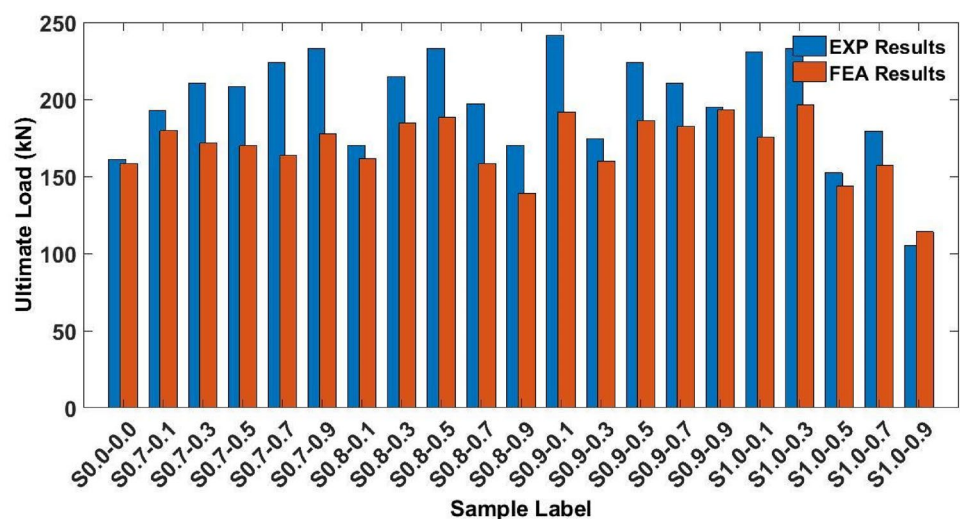
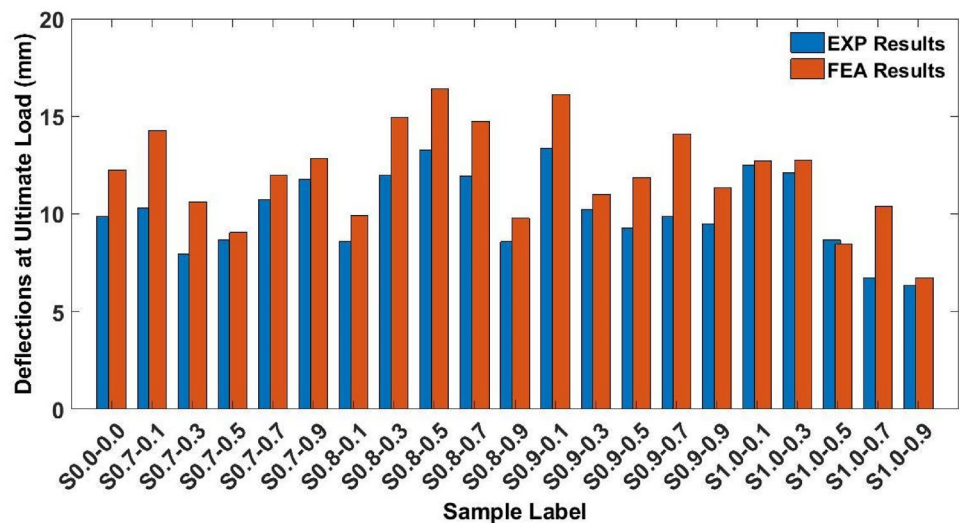


Fig. 18 Experimental and numerical deflections at peak loads



the use of steel fibers, it can be stopped up to some extent. The use of steel fibers helps in the transmission of the load over the fissure plane and which helps the specimen to transmit load over the entire span. But this can only be obtained with the use of a particular blend where both fibers complement each other and a greater loading, as well as deflection, is achieved.

Mostly, the cracks were developed on the tension side of the slabs in diagonal directions and the number of cracks increased slowly up to the collapse stages. The crack study was also performed using the FEA model as presented in Fig. 19, 20, 21, 22. The FEA crack patterns were represented using Max. Positive Principal plastic strains as reported in the previous studies [41, 42]. Moreover, FEA cracks patterns can also be represented using the stress limits of concrete material. When the stress of the compressive strength of concrete material increases from its limit, the cracking of concrete occurs at that location causing the yielding of steel reinforcement. It can be observed that the proposed FEA model accurately captured the crack patterns of the two-way slab specimens. The crack patterns obtained from FEA modeling represents that the proposed model predicted the concrete crushing accurately. In most of the slabs, the cracking was started at the yield line of the slab due to the center point loading flexural test and increased gradually up to the failure of the specimen. All the specimens presented the two peak behaviors; one from the start of loading up to the elastic limit of the curve for the first crack load; the second peak was

obtained at the ultimate load-carrying capacity of specimens with the rupture of concrete material on the bottom side of specimens.

6 Parametric study

The sensitivity of various parameters was examined using the proposed FEA model. Those parameters were main reinforcement ratio (ρ_l), concrete cover (cc) and concrete strength in compression (f'_c). The sensitivity of these parameters was studied in 3D plots as shown in Fig. 23.

6.1 Effect of main reinforcement (ρ_l)

The effect of main reinforcement (ρ_l) was presented in Fig. 23. It was observed that by increasing the ρ_l , there was an increase in the load-carrying capacity of the HFRC two-way slab. When the ρ_l was increased from 1.13 to 5.48%, an increase of 51.21% occurred in capacity with the increase of concrete strength (f'_c) from 10 to 50 N/mm². Similarly, by enhancing the same amount of reinforcement, the increase in vertical deflection of mid-span of the slab, a maximum increase of 45.29% occurred. When we increase the ρ_l along with the increase of concrete cover (cc), the capacity of the slab increases by 101.24%, and the vertical deflection increase by 37.47%.

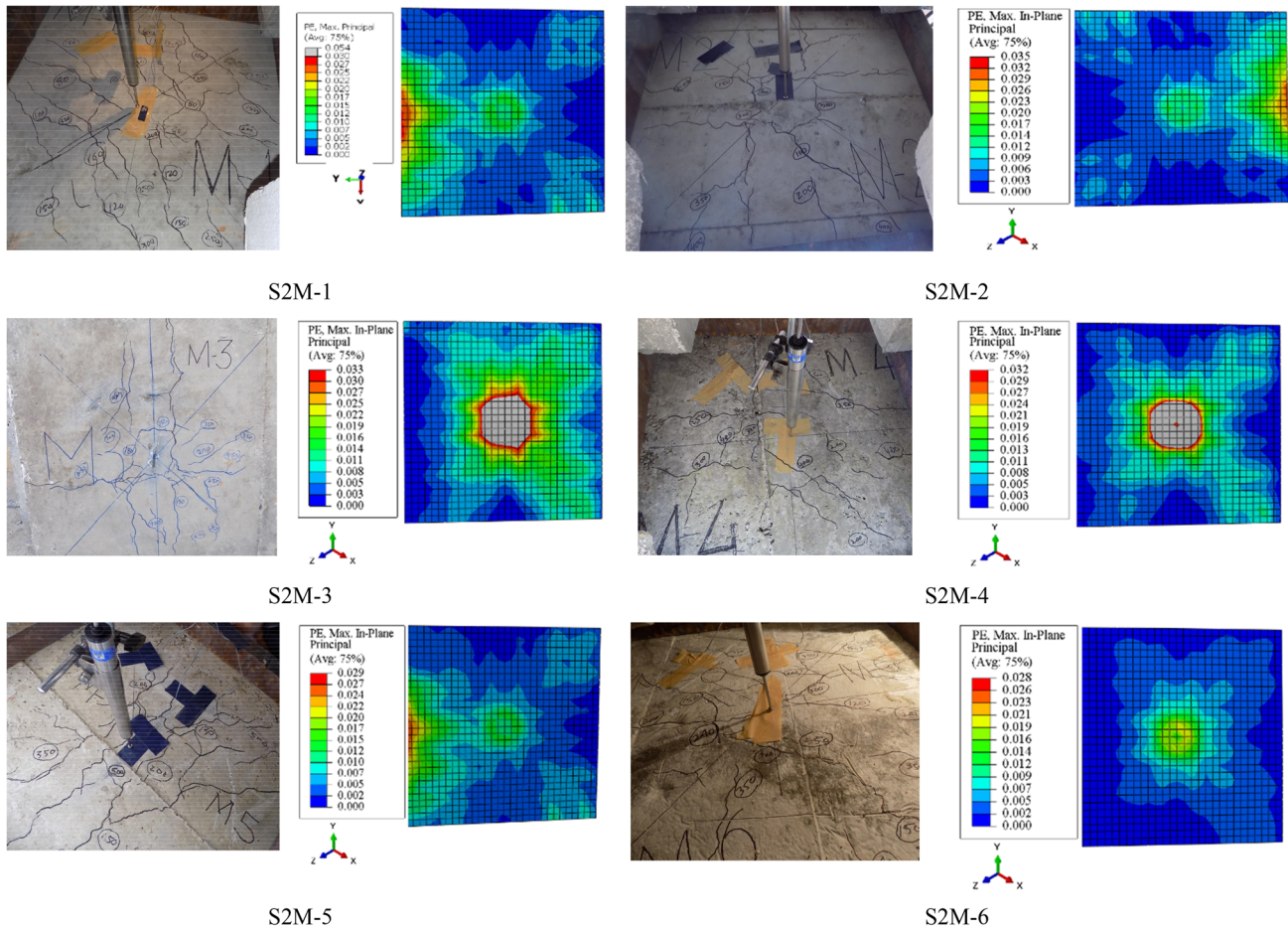


Fig. 19 Experimental and numerical crack patterns of two-way plain concrete and HFRC slabs with 0.7% steel fibers

6.2 Effect of concrete cover

The effect of the concrete cover was opposite to that of the main reinforcement. By increasing the concrete cover with the increase of ρ_l , there is a maximum decrease of 40.46 and 41.83% for loading capacity and corresponding vertical mid-span deflection, respectively as represented in Fig. 23. Similarly, by increasing the concrete cover with the increase of f'_c , there is a maximum decrease of 170.52 and 51.84% for loading capacity and corresponding vertical mid-span deflection, respectively.

6.3 Effect of concrete strength (f'_c)

The effect of concrete strength was dominant on the load-carrying capacity and vertical deflection of HFRC two-way slabs. When the f'_c was enhanced from 10 to 50 MPa, the increase of 145.73% was observed in loading capacity and the increase of 47.49% was observed in corresponding vertical deflection with the increase of ρ_l as presented in Fig. 23. Similarly, while increasing the 'cc', the optimum effect of f'_c increase f'_c was 170.92% for vertical capacity and 51.84% for deflection.

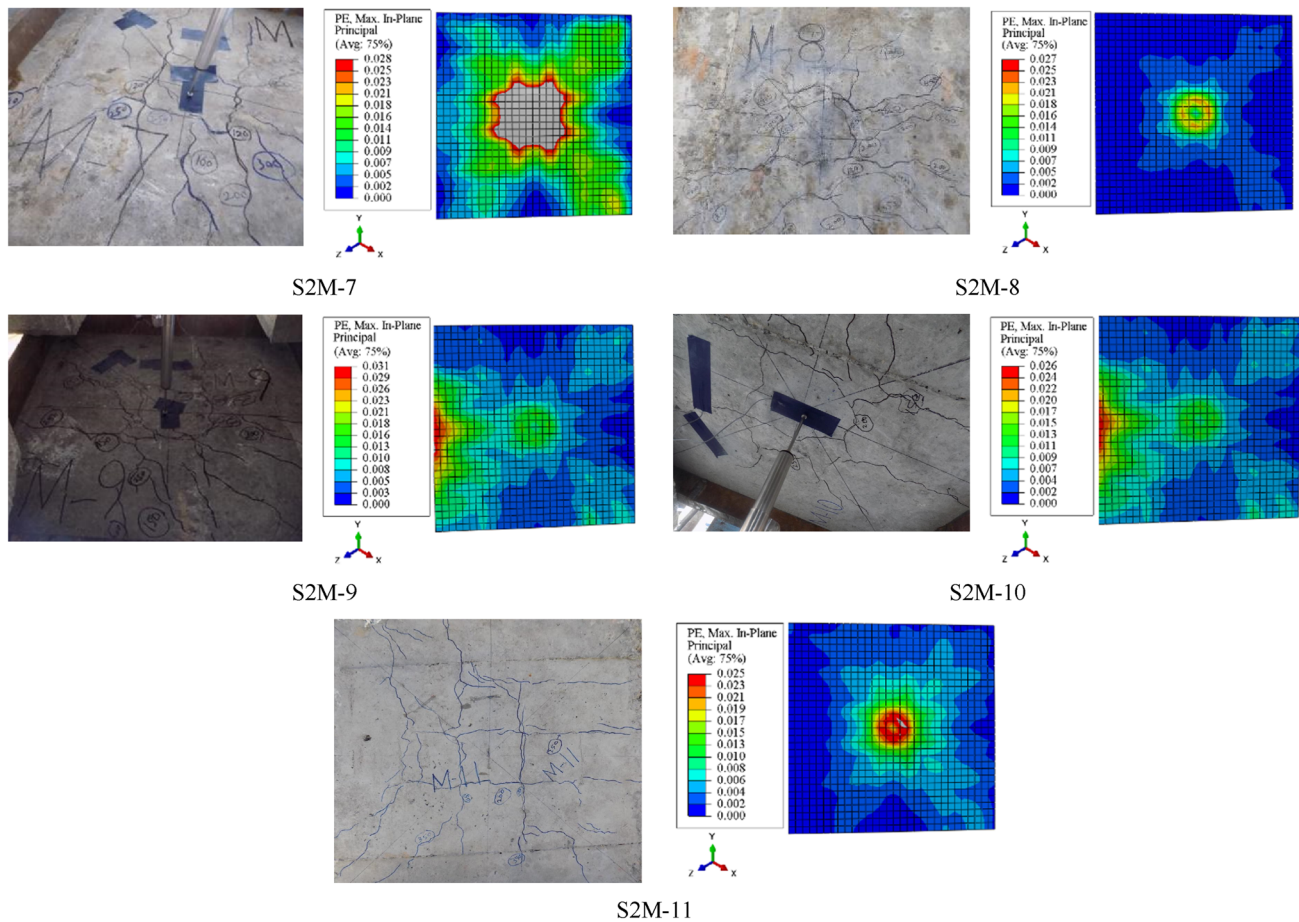


Fig. 20 Experimental and numerical crack patterns of two-way HFRC slabs with 0.8% steel fibers

7 Conclusions

This investigation aims to examine the load-deflection behavior of HFRC two-way slabs. A total of 21 specimens were fabricated and tested to failure under flexural loading. The following conclusions were drawn from the current research work:

1. The increase in the quantity of hybrid fibers in concrete reduces the workability of concrete and shows a stiffer nature of concrete in two-way slabs.
2. The load-carrying capacity of the HFRC two-way slab was increased up to a maximum percentage of 213% for the first crack loading condition and 40.36% for the ultimate loading condition for the S0.9-0.1 slab as compared to the control specimen having zero fibers.

3. The maximum increase in deflection was 44.81% at first crack load whereas 39.80% at the ultimate load for S0.9-0.1 in comparison with the control specimen.
3. The maximum load-carrying capacity of two-way slabs was achieved up to 213% for first crack loading and up to 45% for ultimate loading. In the case of slabs S1.0-0.5 and S1.0-0.9, the increase in first crack loading observed from 113 and 88%, respectively but in the case of ultimate loading, the load-carrying capacity of S1.0-0.5 and S1.0-0.9 decreased by 6 and 27.61%, respectively as compared to control specimen (S0.0-0.0). This decrease in ultimate load-carrying capacity is due to increased quantities of both types of fibers and improper mixing of fibers in concrete due to their large quantity.

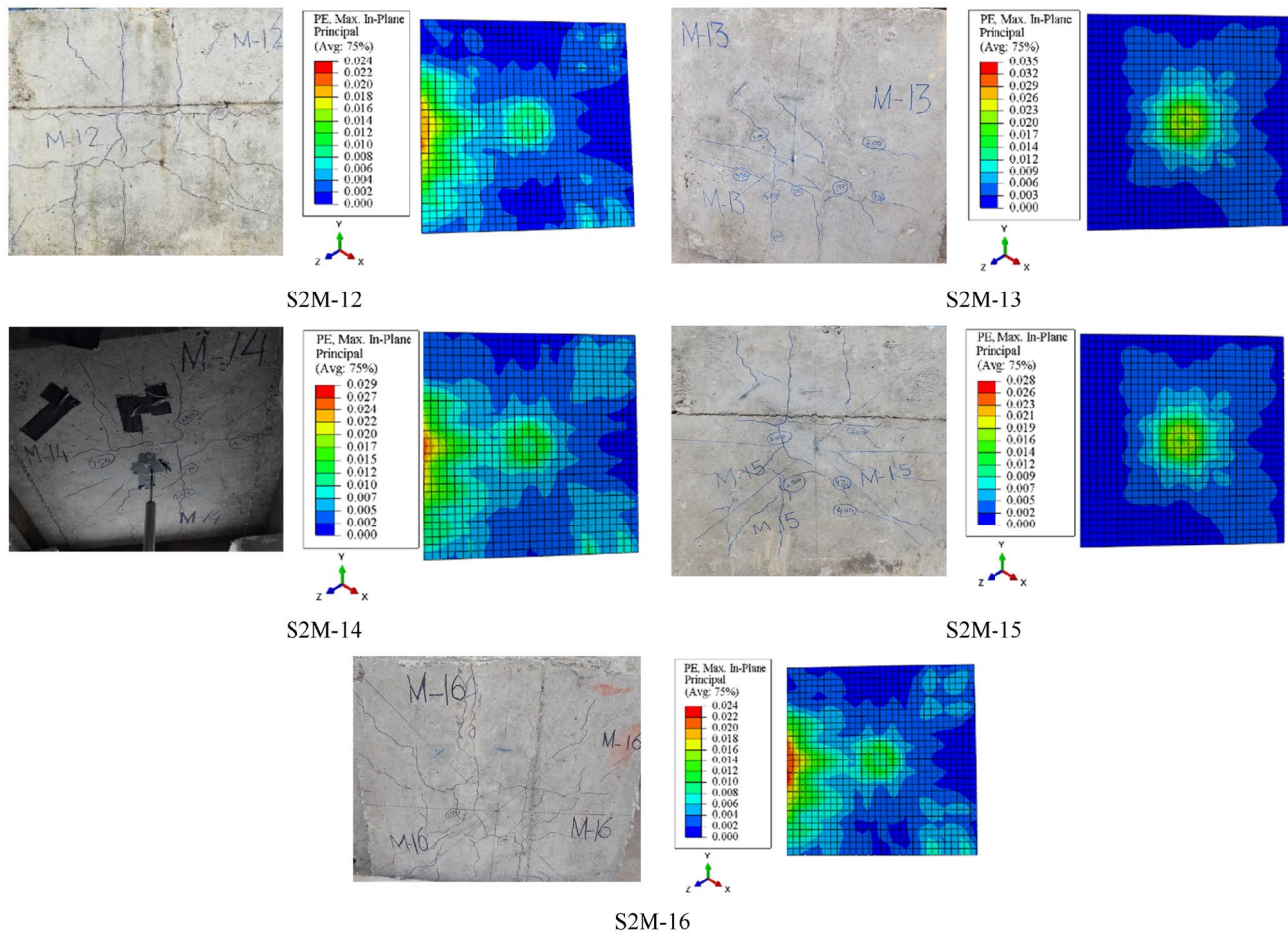


Fig. 21 Experimental and numerical crack patterns of two-way HFRC slabs with 0.9% steel fibers

4. The maximum loading capacity and corresponding vertical mid-span deflection of HFRC two-way slabs were achieved by using a volumetric combination of 0.9% SF and 0.1% PPF. The good results of the cracking patterns and failure process of slabs were obtained from the suggested FEA model.
5. The parametric study concludes that there is an increase in load-carrying capacity and ductility with the increase of concrete strength and the main reinforcement ratio, while the effect of concrete cover is the opposite.
6. The average percentage discrepancies among the experimental and FEA results were 8.94 and 6.24% for load and deflection, respectively. Therefore, it can be said that the proposed constitutive FEA model pre-

dicted the behavior of the HFRC two-way slab, accurately and it can be helpful for the structural engineers in the analysis and design of two-way slab systems with hybrid fibers reinforcement.

The authors recommend the further investigation of two-way slabs reinforced completely with either fiber reinforced polymers (FRPs) reinforcement or a combination of both steel and FRP reinforcement. Furthermore, the structural performance of two-way slab should be investigated by using recycled aggregates concrete because the recycled aggregates concrete has been proved to report higher ductility as compared with the natural coarse aggregate concrete.

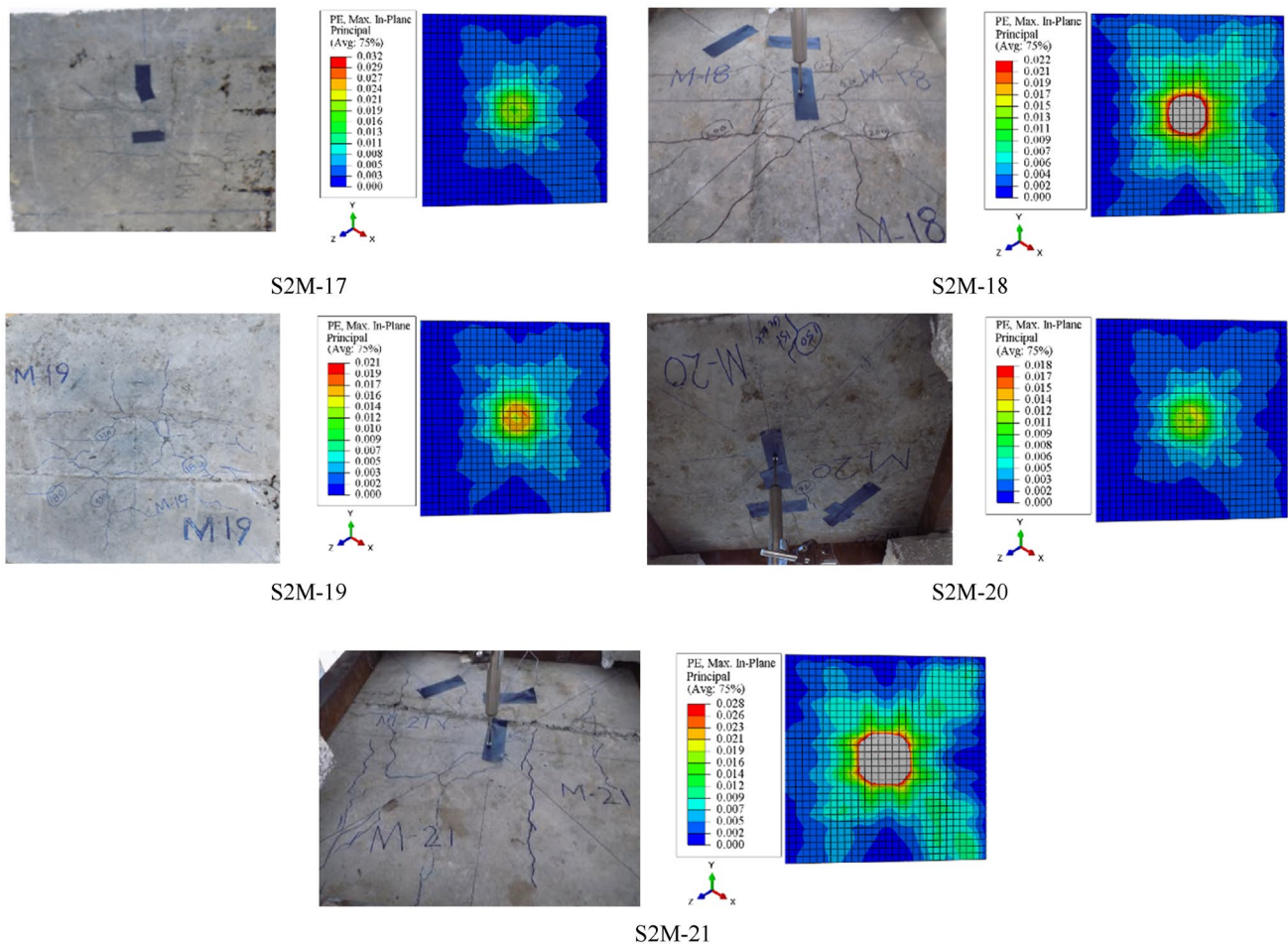


Fig. 22 Experimental and numerical crack patterns of two-way HFRC slabs with 1.0% steel fibers

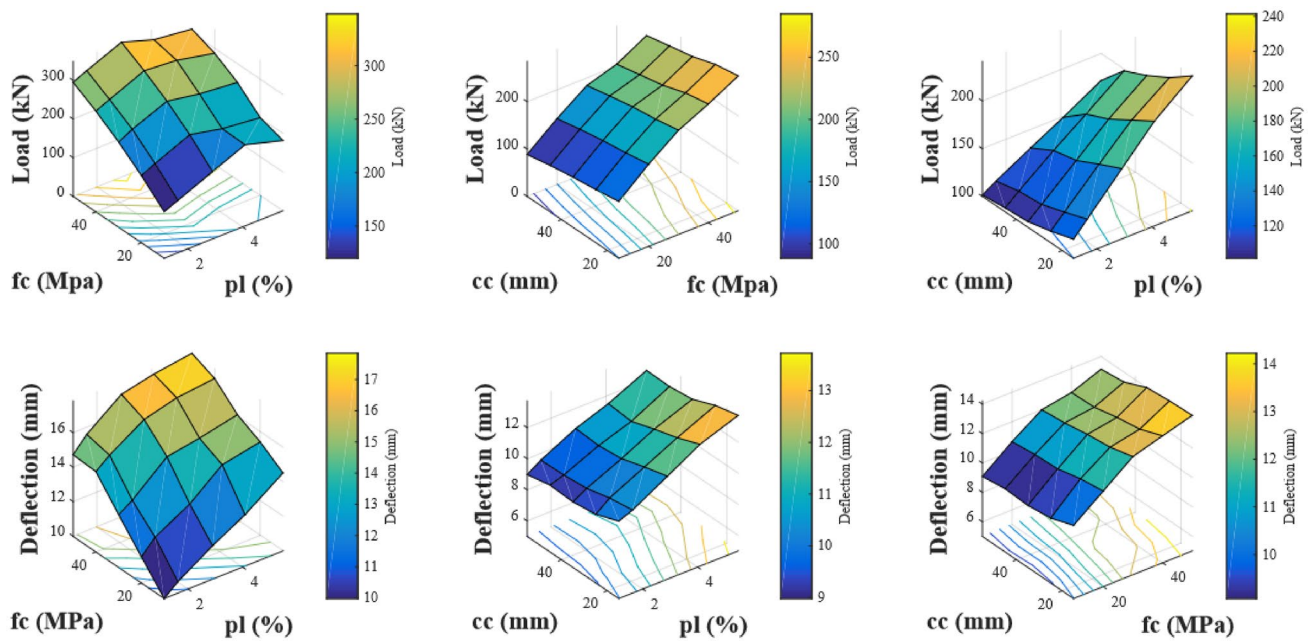


Fig. 23 Parametric study results for HFRC two-way slab specimens

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Compliance with ethical standards

Conflict of interest The authors whose names are listed in this paper certify that they have NO affiliations with or involvement in any organization or entity with any financial interest (such as honoraria; educational grants; participation in speakers' bureaus; membership, employment, consultancies, stock ownership, or other equity interest; and expert testimony or patent-licensing arrangements), or non-financial interest (such as personal or professional relationships, affiliations, knowledge or beliefs) in the subject matter or materials discussed in this manuscript.

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