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1 **Optimisation study of a supersonic separator considering**
2 **nonequilibrium condensation behaviour**

3 Chuang Wen¹, Hongbing Ding², Yan Yang^{1,*}

4 ¹Faculty of Engineering, University of Nottingham, University Park, Nottingham

5 NG7 2RD, UK

6 ²Tianjin Key Laboratory of Process Measurement and Control, School of Electrical

7 and Information Engineering, Tianjin University, Tianjin 300072, China

8 *Corresponding author: Yan Yang, Email: yan.yang1@nottingham.ac.uk;

9 flyloveyang@gmail.com

10 **Abstract:** The supersonic separation offers an opportunity for natural gas processing.
11 The problem is that the phase change of water vapour in the supersonic flow is not fully
12 understood in the presence of shock waves in a supersonic separator. This study aims
13 to evaluate the performance of the supersonic separation with the phase change process
14 and shock waves. The condensing flow model is developed to accurately predict the
15 energy conversion within the supersonic separator. The computational results show that
16 the single-phase flow model over-estimates the vapour expansions by 12.43% higher
17 Mach number than the condensing flow model. The liquid fraction of 8.2% is predicted
18 by the condensing flow model during the phase change process in supersonic separators.
19 The supersonic separator is optimised via combining the diverging part of the
20 supersonic nozzle and constant cyclonic separation tube as a long diverging part of the
21 newly designed nozzle. The optimised supersonic separator reduces the energy loss by
22 eliminating the oblique and expansion waves in the newly designed nozzle, which

23 improves the energy efficiency for natural gas processing.

24 **Keywords:** supersonic separator, gas processing, supersonic flow, nonequilibrium
25 condensation, condensing flow, phase change

26 **1. Introduction**

27 Clean utilisation of natural gas provides an opportunity to mitigate environmental
28 pollutions [1]. A supersonic separator has been used for gas separation working on the
29 phase change in supersonic flows and the strong centrifugal force owing to a swirling
30 flow [2, 3]. The high-speed flow induces the low-pressure and low-temperature [4],
31 which results in the nonequilibrium condensation of water vapour [5, 6]. The
32 experiments have demonstrated that the hydrate does not form under low-pressure and
33 low-temperature conditions [7]. Thus, a supersonic separator does not need any
34 chemicals or inhibitors to prohibit hydration formation, which provides an
35 environment-friendly way for natural gas processing.

36 The computational fluid dynamics (CFD) modelling has been employed for
37 predicting the dehydration performance of the supersonic separator [8, 9], and most of
38 them did not consider the phase change behaviour. Yang & Wen [10] assumed the size
39 of the particles, which was released from the exit plane of the supersonic nozzle, to
40 track the particle trajectories in a supersonic separator. Majidi & Farhadi [11] used a
41 dry gas flow to study the influence of the drain structure on the position of the shock
42 wave for the supersonic separation. Hu et al. [12] numerically investigated the flow
43 structure in a supersonic separator with a reflow channel without considering
44 nonequilibrium condensations.

45 A few studies were performed to simulate the water vapour phase change process
 46 within a supersonic separator, as shown in Table 1. In these numerical studies,
 47 Shooshtari & Shahsavand [13], Ma et al. [14, 15], Bian et al. [16, 17], Sun et al. [18,
 48 19] developed a condensing flow model to investigate the phase change behaviour in a
 49 supersonic nozzle, but the shock wave was not involved in these simulations.
 50 Shooshtari & Shahsavand [20, 21] studied the phase change process in a supersonic
 51 separator using a mass transfer rate method for calculating the droplet growth with the
 52 one-dimensional model. Niknam et al. [22] investigated the phase change process of
 53 water vapour in a supersonic separator based on the evaporation-condensation model
 54 in ANSYS FLUENT. It can be seen that the phase change process is not fully
 55 understood in a supersonic separator.

56 Table 1 CFD studies on the supersonic separation with the phase change process

References	Models in the numerical study
Shooshtari & Shahsavand [13]	Condensing flow model, nozzle flow, no shock waves
Ma et al. [14, 15]	Condensing flow model, nozzle flow, no shock waves
Bian et al. [16, 17]	Condensing flow model, nozzle flow, no shock waves
Sun et al. [18, 19]	Condensing flow model, nozzle flow, no shock waves
Shooshtari & Shahsavand [20, 21]	Homogeneous nucleation and mass transfer rate calculations for liquid droplet growth
Niknam et al. [22]	Evaporation-condensation phase change model in ANSYS FLUENT

57 This study aims to assess the performance of the supersonic separation considering
 58 the phase change process and shock waves. A condensing flow model is developed for
 59 predicting the complicated fluid flow, heat and mass transfer of water vapour in the

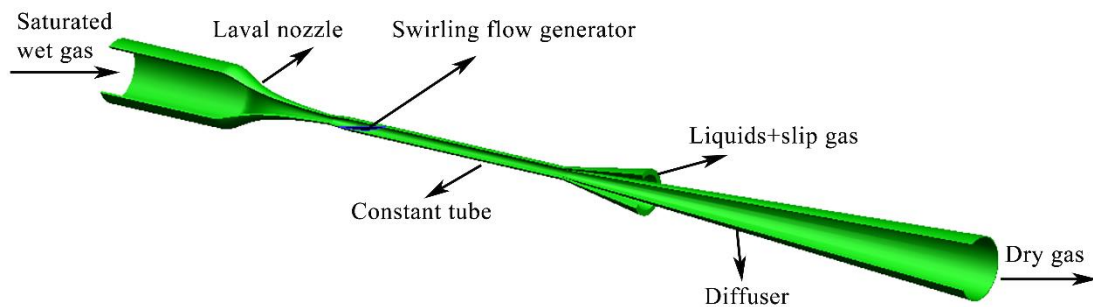
60 supersonic separator. The detailed analysis is performed to figure out the impact of
61 nonequilibrium condensation behaviour on the supersonic separation using the single-
62 phase flow and condensing flow models. The condensation parameters are described in
63 detail within the supersonic separator including the nucleation rate, droplet radius and
64 liquid fraction. The supersonic separator is optimised based on the condensing flow
65 model to improve the separation performance and energy efficiency.

66 2. Mathematical modelling

67 2.1. Physical model

68 A typical supersonic separator is described in Fig. 1. The swirling flow generator
69 is not involved in the present simulation to simplify the physical model by focusing on
70 the condensation process in a supersonic separator. The Laval nozzle has a throat
71 diameter of 14.70 mm, while the nozzle inlet and outlet diameters are 35.10 mm and
72 18.30 mm, respectively. The constant tube is installed to the exit plane of the Laval
73 nozzle for the cyclonic separation. The outlet diameter of the diffuser is fixed at 40.00
74 mm. The dimension of the supersonic separator is shown in Table 2 [23].

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Fig. 1 Schematic of a supersonic separator

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Table 2. The dimensions of a supersonic separator [23]

Dimensions	Value (mm)
Nozzle inlet diameter	35.10
Nozzle throat diameter	14.70
Nozzle outlet diameter	18.30
Length of nozzle converging part	33.39
Length of nozzle diverging part	73.50
Length of the constant tube	220.50
Outlet diameter of the diffuser	40.00
Length of the diffuser	206.85

81

82 **2.2. Numerical model**

83 The Eulerian approach is used for the flow prediction inside a supersonic separator
84 involving the condensation process [24]. The liquid fraction (y) and droplet number (n)
85 equations are employed to solve the phase change process in supersonic flows [25, 26]:

$$86 \quad \frac{\partial(\rho y)}{\partial t} + \frac{\partial(\rho y u_j)}{\partial x_j} = \Gamma \quad (1)$$

$$87 \quad \frac{\partial(\rho n)}{\partial t} + \frac{\partial(\rho n u_j)}{\partial x_j} = \rho J \quad (2)$$

88 where ρ is the mixture density, kg m^{-3} ; u is the mixture velocity, m s^{-1} ; y is the liquid
89 fraction, dimensionless; n is the droplet number, m^{-3} ; t is the time, s ; J is the nucleation
90 rate, $\text{m}^{-3} \text{s}^{-1}$; Γ is the mass generation rate due to the nonequilibrium condensation, kg
91 $\text{m}^{-3} \text{s}^{-1}$, which is given [27, 28]:

92
$$\Gamma = \frac{4}{3} \pi r_c^3 \rho_l J + 4 \pi r^2 \rho_l n \frac{dr}{dt} \quad (3)$$

93 where r_c is the critical droplet radius, m; r is the droplet radius, m; ρ_l is the liquid density,
 94 kg m⁻³; dr/dt is the growth rate of the condensed droplet, m s⁻¹.

95 The classical nucleation theory is used to calculate the nucleation rate [29]:

96
$$J = \frac{q_c}{1+\phi} \frac{\rho_v^2}{\rho_l} \sqrt{\frac{2\sigma}{\pi m_v^3}} \exp\left(-\frac{4\pi\sigma}{3k_B T_v} r_c^2\right) \quad (4)$$

97 where ρ_v is the vapour density, kg m⁻³; m_v is the mass of a vapour molecule, kg; T_v is the
 98 vapour temperature, K; σ is the surface tension, N m⁻¹; k_B is the Boltzmann's constant, J
 99 K⁻¹. q_c and ϕ are the model parameters, dimensionless.

100 The Young's model is used to calculate the droplet growth rate [30, 31]:

101
$$\frac{dr}{dt} = \frac{\lambda_v \Delta T}{\rho_l h r} \frac{(1 - r_c/r)}{\left(\frac{1}{1+2\beta \text{Kn}} + 3.78(1-\nu) \frac{\text{Kn}}{\text{Pr}}\right)} \quad (5)$$

102
$$\Delta T = T_s - T_v \quad (6)$$

103 where λ_v is the vapour conductivity, W m⁻¹ K⁻¹; T_s is the saturation temperature, K; ΔT
 104 is the degree of supercooling, K; h is the enthalpy, J kg⁻¹; β and ν are the model
 105 parameters, dimensionless; Pr is the Prandtl number, dimensionless; Kn is the Knudsen
 106 number, dimensionless.

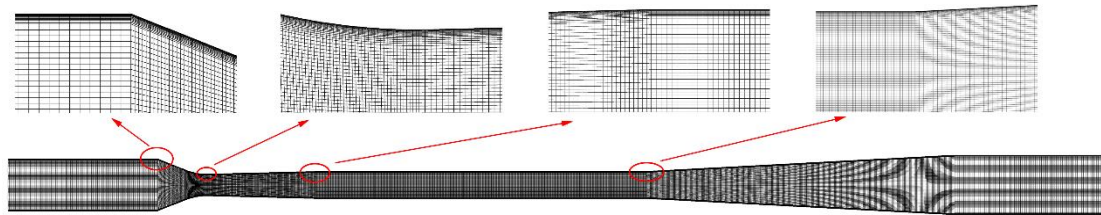
107 2.3. Model implementation

108 For the single-phase flow modelling, the continuity, mass and energy conservation
 109 equations are directly solved by ANSYS FLUENT 18 [32], and these well-known
 110 equations are not shown for simplicity. For the condensing flow modelling, the liquid
 111 fraction (y) and droplet number (n) equations, as well as the Eqs. (3) – (6) are solved

112 using C programming [33] to describe the nonequilibrium condensation process in a
113 supersonic separator. For the calculation of the phase change process, the nucleation
114 process starts to generate massive critical radius droplets when the vapour reaches the
115 nonequilibrium state. When the droplet radius is greater than the critical one, the droplet
116 growth process is initiated to form bigger droplets. The mass transfer between the
117 vapour and liquid phases comes from the nucleation and droplet growth processes. The
118 shear stress transport (SST) $k-\omega$ turbulence model [34, 35] is adopted considering the
119 supersonic flow [36] and nonequilibrium condensations [37]. The thermophysical
120 properties like the density [38], viscosity [39], specific heat capacity [40] and thermal
121 conductivity [41] are used from the Fluent library, while the saturation pressure,
122 saturation temperature, surface tension, and density of water liquid are developed by
123 the UDF during the numerical simulation.

124 The structured grid is employed for the designed supersonic separator, as shown
125 in Fig. 2. The boundary conditions for the supersonic separator are described in Table
126 3. The mesh independence is investigated based on 19500, 36000 and 66250 structured
127 cells for coarse, medium and fine meshes, respectively. Figure 3 describes the Mach
128 numbers and liquid fraction in the flow and longitudinal directions. The Mach number
129 is defined as the ratio of the flow velocity to the local speed of sound. Three different
130 grid resolutions represent almost the same flow behaviour both in the flow and
131 longitudinal directions upstream the shock wave. This indicates that these grids capture
132 the occurrence of the nonequilibrium condensation in the supersonic separator.
133 However, the difference is observed when the shock wave appears. The Mach number

134 and liquid fraction from the coarse mesh diverge from those of medium and fine meshes,
 135 which shows that the coarse mesh is not enough for predicting a shock wave. Therefore,
 136 the medium mesh is used for evaluating the dehydration performance of a supersonic
 137 separator considering the numerical cost and time.



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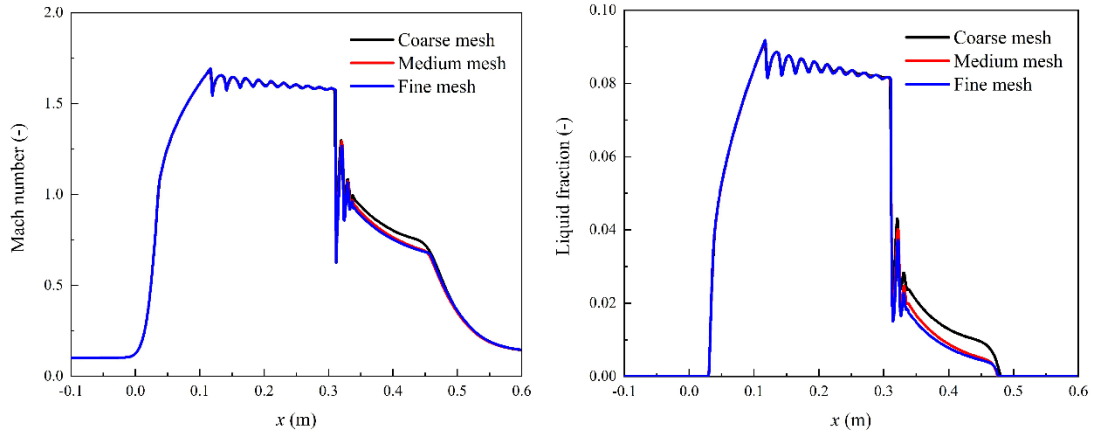
Fig. 2 Numerical grid for a supersonic separator

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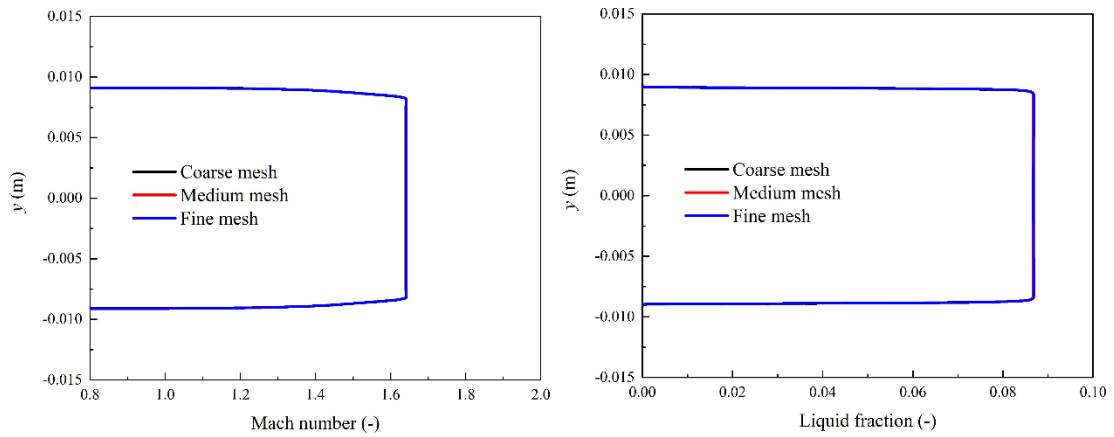
Table 3 Boundary conditions for the supersonic separator

Boundary conditions	Separator inlet	Separator outlet	Walls and fluids
Total pressure	40 bar	25 bar	Working fluids: water vapour
Total temperature	520 K	520 K	No-slip, adiabatic walls

141



(a) Mach number and liquid fraction along the flow direction



(b) Mach number and liquid fraction at the exit plane of the supersonic nozzle

142

143 Fig. 3 Impact of the grid resolution on the condensation flow in a supersonic separator

144 3. Results and discussion

145 3.1. Model validation

146 The developed condensing flow model is validated against experimental data [42].

147 The static pressure and droplet radius inside the Laval nozzle are shown in Fig. 4. The

148 results indicate that the developed CFD model predicts accurately the flow and

149 condensation behaviours in supersonic flows. The CFD model captures the onset of the

150 condensation shock due to the heat and mass transfer during the phase change process.

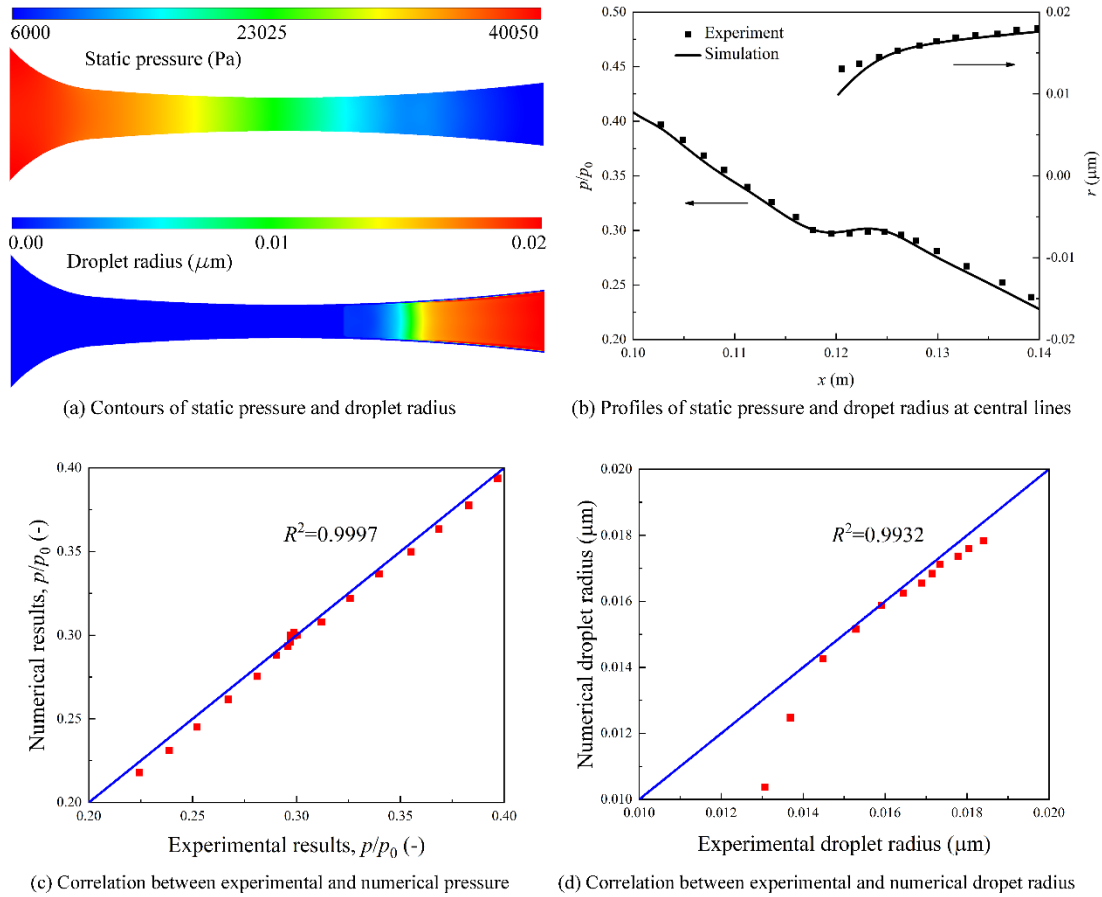
151 To compare the numerical and experimental results, the root-mean-square (R^2) is

152 employed to determine the error between them [43-45], which is defined in Eq. (7). The

153 root-mean-square (R^2) for the static pressure and droplet radius between the
154 experimental and numerical results can reach 0.99. The correlations (root-mean-square-
155 R^2) between the experimental and numerical static pressure and droplet radius are
156 shown in Fig. 4 (c) and (d), respectively. It can be seen that good compliance between
157 the experimental and numerical static pressure is obtained. For the droplet radius, the
158 upstream two numerical data deviate significantly from the experimental data, while
159 others agree well with each other. Generally, the numerical results can reflect the
160 experimental data very well. Thus, it can be concluded that the developed condensing
161 flow model can be used to evaluate the flow features in the supersonic separator.

$$162 \quad R^2 = 1 - \frac{\sum_{i=1}^n (a_i - p_i)^2}{\sum_{i=1}^n (p_i)^2} \quad (7)$$

163 where a_i is the experimental value, p_i is the numerical value, and n is the output data
164 number.



165

166 Fig. 4 CFD validation of the nonequilibrium condensation in supersonic flows: total
 167 pressure and temperature at nozzle inlet: 40.05 kPa and 374.3 K

168 **3.2. Flow features in supersonic separators by single-phase flow and condensing**
 169 **flow models**

170 The Mach number, static pressure and static temperature are described in Figs. 5-
 171 7 based on the single-phase flow and condensing flow models. The two models predict
 172 almost the same flow behaviour upstream the nozzle throat, where water vapour is
 173 accelerated with the increase of the Mach number. The choked flow is obtained at the
 174 nozzle throat and then the supersonic flow is achieved in the nozzle diverging part. The
 175 Mach number achieves the peak value at the nozzle exit plane. The supersonic flow is
 176 obtained in the constant tube both for the single-phase flow and condensing flow

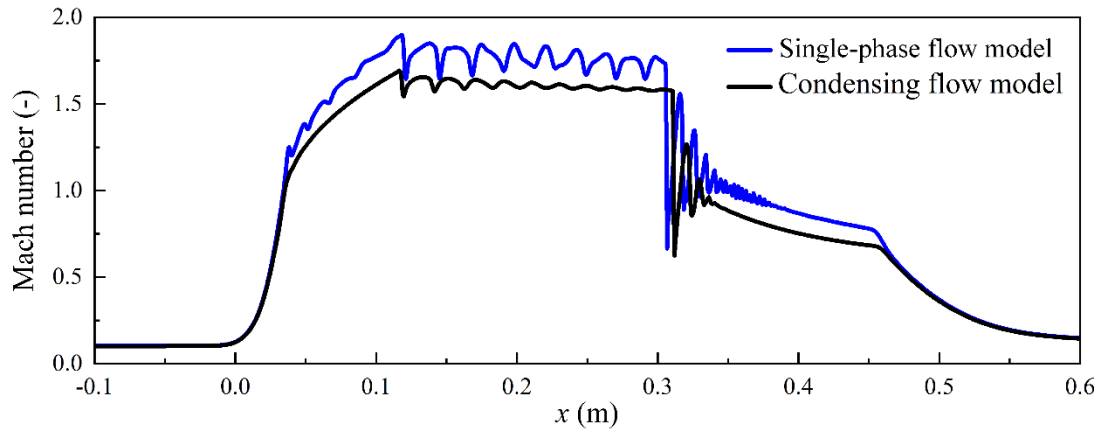
177 models, where the Mach number is greater than 1.5. The shock wave occurs in the
178 diffuser when the back pressure is fixed at 62.5% of inlet pressure. The static pressure
179 is recovered as the subsonic flow is achieved downstream the shock wave. This
180 improves the energy efficiency for the supersonic separation.

181 The different flow behaviours of the Mach number, static pressure and static
182 temperature, are observed downstream the nozzle throat between the single-phase flow
183 and condensing flow models. The Mach number predicted by the single-phase flow
184 model is greater than that of the condensing flow model. The maximum Mach number
185 at the nozzle exit plane is 1.90 for the single-phase flow assumption compared to 1.69
186 for the condensing flow model. This indicates that the single-phase flow model over-
187 estimates the expansion capacity of the Laval nozzle of 12.43% higher than the
188 condensing flow model.

189 For the single-phase flow model, the static temperature declines continuously in
190 the diverging part of the Laval nozzle without considering the supersaturation state of
191 water vapour. On the contrary, the condensing flow model causes a rise of the static
192 temperature downstream the nozzle throat. This indicates that the latent heat is released
193 to heat the vapour phase during the nonequilibrium condensation process in a
194 supersonic separator.

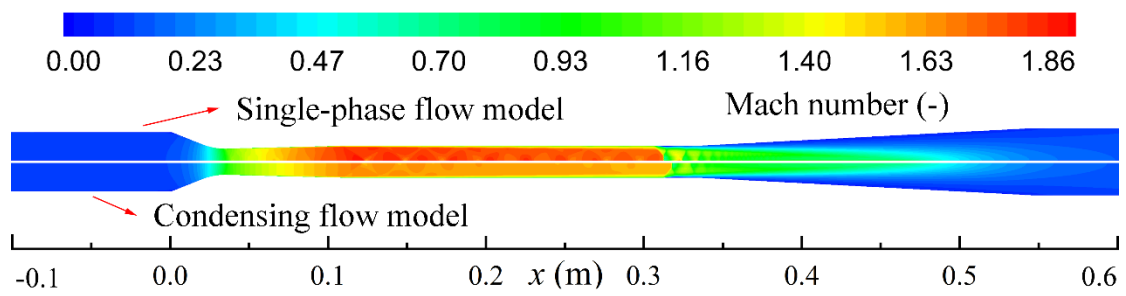
195 Furthermore, the single-phase flow and condensing flow models compute different
196 shock waves in the supersonic separator, such as the position and intensity of the shock
197 waves. On one hand, the single-phase flow model predicts an earlier shock position
198 compared to the condensing flow model, which shifts the shock position upward the

199 Laval nozzle. Under this operating condition, the single-phase flow model under-
200 predicts the dehydration performance of the supersonic separation. For instance, the
201 shock wave occurs in the diffusers for this design according to the condensing flow
202 model, which is a normal condition for water vapour separation in supersonic
203 separators. However, the single-phase flow model moves the shock position upward
204 and the shock wave occurs in the constant tube, where the supersonic separator does
205 not work as the abrupt rises of the static pressure and temperature because it can cause
206 the re-evaporation of the condensed droplets. On the other hand, the condensing flow
207 model weakens the intensity of the shock wave compared to the single-phase flow
208 assumption, which can be observed from the drops of the Mach number and rises of the
209 static pressure and temperature. This suggests that the condensing flow model improves
210 the prediction of the pressure recovery in a supersonic separator.



211

(a) Profiles of Mach number at the central line



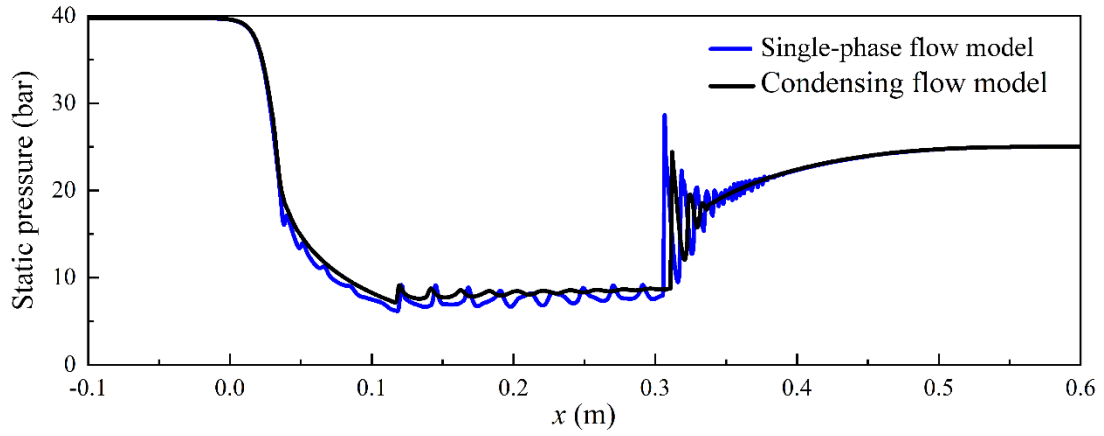
(b) Contours of Mach number in supersonic separators

212

Fig. 5 Mach number in supersonic separators with and without the condensation

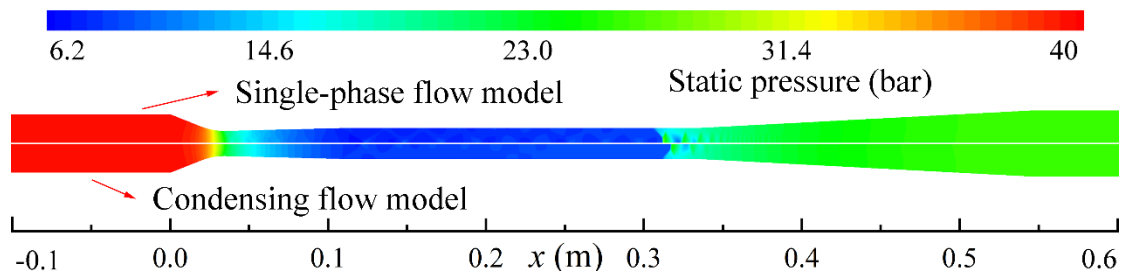
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process



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(a) Profiles of static pressure at the central line



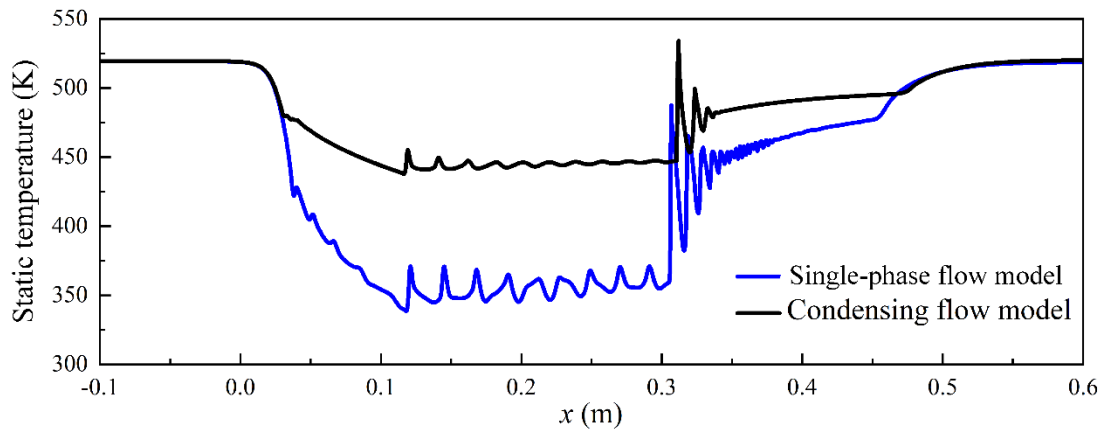
(b) Contours of static pressure in supersonic separators

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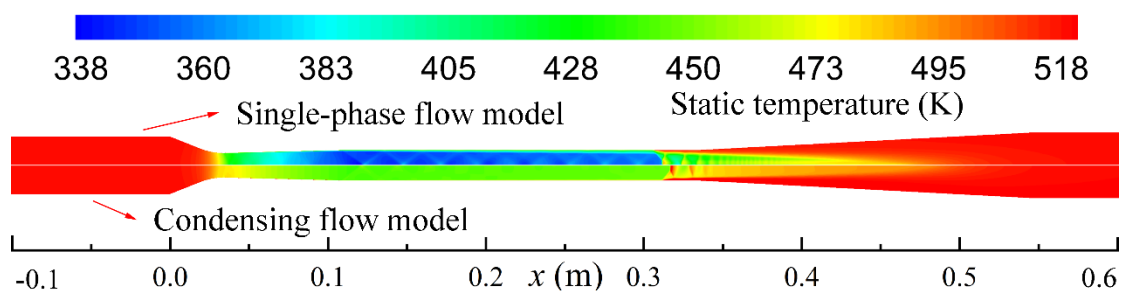
Fig. 6 Static pressure in supersonic separators with and without the condensation

216

process



(a) Profiles of static temperature at the central line



(b) Contours of static temperature in supersonic separators

217

218

Fig. 7 Static temperature in supersonic separators with and without the condensation

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process

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3.3. Condensation phenomenon in supersonic separators

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The condensation parameters during water vapour removal in the designed

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supersonic separators are shown in Figs. 8-11, including the degree of supercooling,

223

nucleation rate, droplet radius and liquid fraction, respectively. Fig. 8 implies that the

224

degree of supercooling increases with the vapour expansion in the Laval nozzle, which

225

can reach a peak value of approximately 23 K in the designed supersonic separator. The

226

extremely nonequilibrium state of water vapour induces the homogenous nucleation in

227

supersonic flows. The degree of supercooling fluctuating around zero in the constant

228

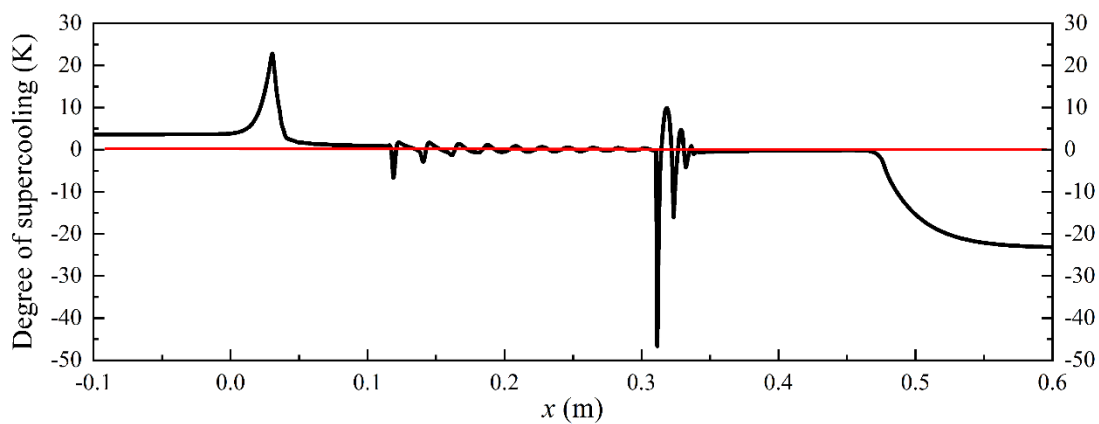
tube indicates that the latent heat is released to the vapour phase, which makes the

229 vapour return to the quasi-equilibrium state. The shock wave induces an overly
230 unsaturated state of water vapour with the degree of supercooling of -46 K, which will
231 cause the re-evaporation of the condensed droplets in the diffuser.

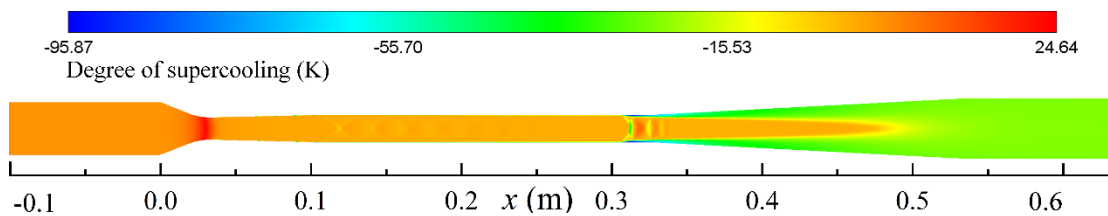
232 The maximum nucleation rate of $8.59 \times 10^{22} \text{ m}^{-3} \text{ s}^{-1}$ occurs in the nozzle diverging
233 part of the supersonic separator, as shown in Fig. 9. The nonequilibrium nucleation
234 induces the appearance of a great number of nuclei, which allows the vapour molecules
235 to condense on the nucleus surface. It, therefore, induces the growth of the size of the
236 condensed droplets, which can be observed from the distribution of the droplet radius
237 at $x = 0.028 \text{ mm} - 0.044 \text{ mm}$, as shown in Fig. 10. The maximum value of the droplet
238 radius is approximately $0.08 \text{ }\mu\text{m}$ in the designed supersonic separator. The liquid
239 fraction increases and achieves the maximum value of about 9.2% of the total mass,
240 which decreases downstream the exit plane of the Laval nozzle and stays at around 8.2%
241 in the constant tube, as shown in Fig. 11. As expected, the liquid fraction declines
242 suddenly as a result of the shock wave, which increases the static pressure and
243 temperature. This indicates that the condensed liquids re-evaporate completely at the
244 separator outlet if they enter into the diffuser, which should be removed by the strong
245 centrifugal force induced by the swirling flow generator (ignored in this study).

246 In addition, the fluctuation of the profiles both from the flow structure and the
247 condensation parameters, such as Mach number, static pressure and liquid fraction, was
248 not observed in the Moses and Stein experiments [42]. It shows that the oblique and
249 expansion waves occur in the supersonic separator, which are not expected for the
250 removal of water vapour. These shocks and waves generate the shock trains in the

251 constant tube, which increases the energy loss and leads to the decrease of the
 252 separation efficiency. The reasons are that the constant tube is placed to the nozzle exit
 253 without a smooth transition. An intersection angle forms between the straight profiles
 254 of diverging part of the Laval nozzle and the constant tube. This indicates that the
 255 connection of the Laval nozzle and constant tube needs to be designed specifically to
 256 avoid the shock trains for the removal of water vapour in supersonic separators.



(a) Profile of degree of supercooling at the central line of the supersonic separator

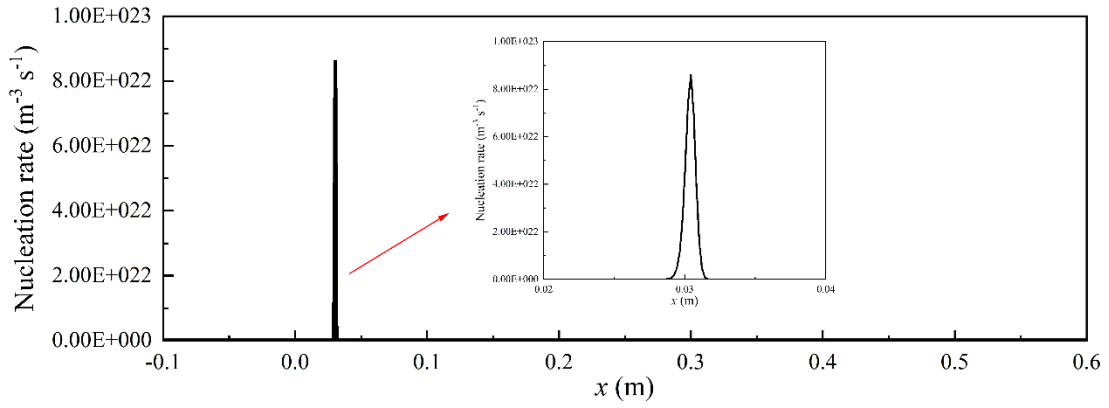


(b) Contour of degree of supercooling in the supersonic separator

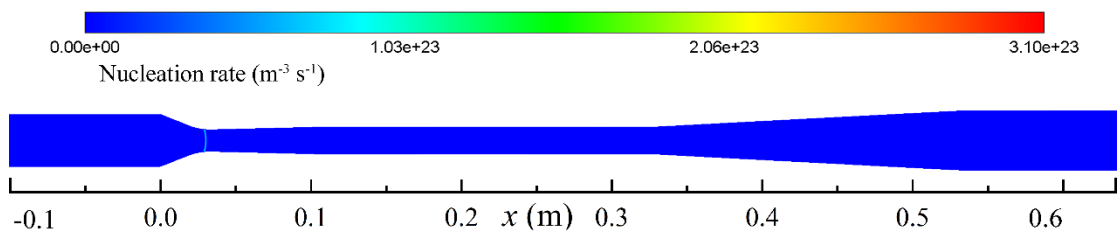
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Fig. 8 Degree of supercooling in the supersonic separator



(a) Profile of nucleation rate at the central line of the supersonic separator

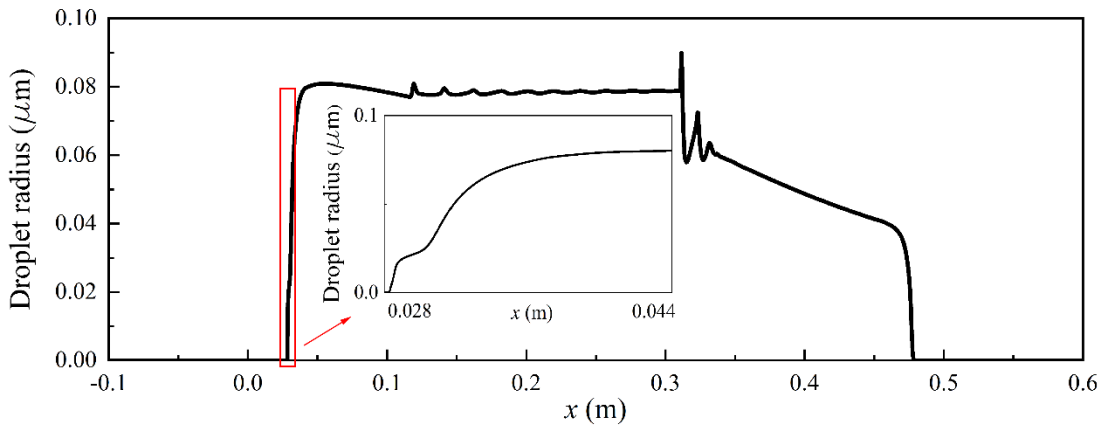


(b) Contour of nucleation rate in the supersonic separator

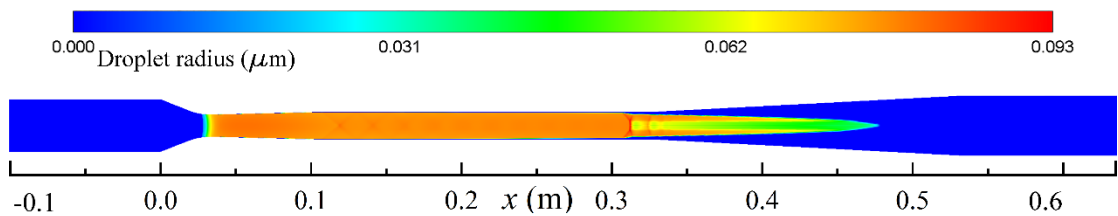
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Fig. 9 Nucleation rate in the supersonic separator



(a) Profile of droplet radius at the central line of the supersonic separator

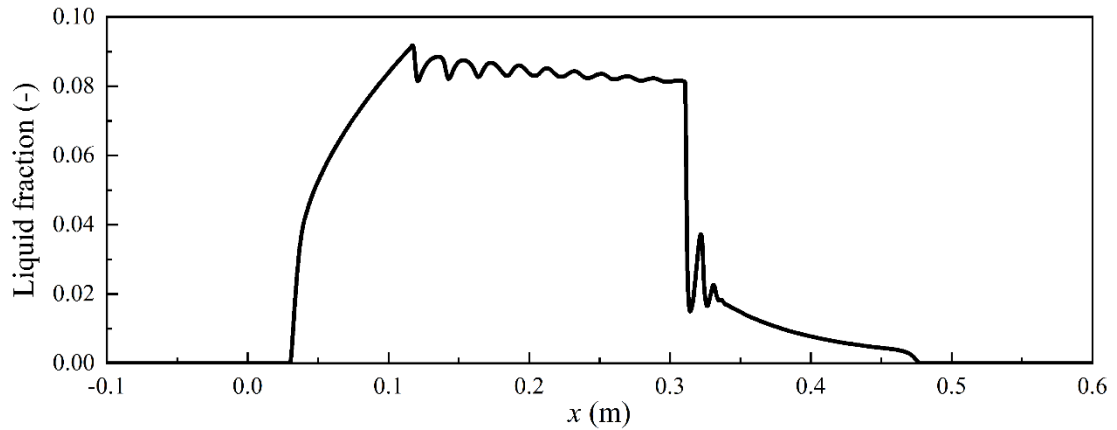


(b) Contour of droplet radius in the supersonic separator

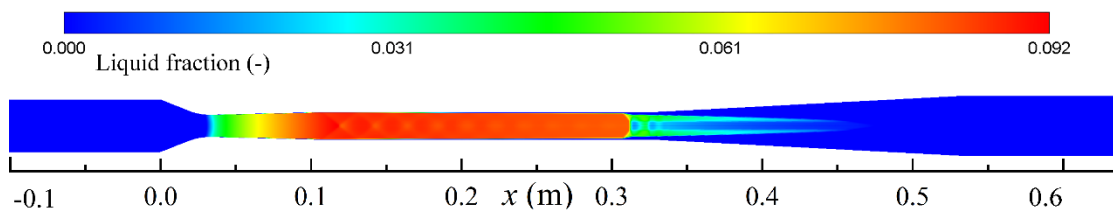
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Fig. 10 Droplet radius in the supersonic separator



(a) Profile of liquid fraction at the central line of the supersonic separator



(b) Contour of liquid fraction in the supersonic separator

Fig. 11 Liquid fraction in the supersonic separator

3.4. Optimisation of the supersonic separator

To mitigate the energy loss due to the oblique and expansion waves in the constant tube as mentioned above, the supersonic separator is optimised based on the idea of combining the diverging part of the Laval nozzle and the constant tube as a long diverging section of the new nozzle, which is expected to eliminate the flow fluctuation. The schematic diagrams of original and optimised geometries are illustrated in Fig. 12.

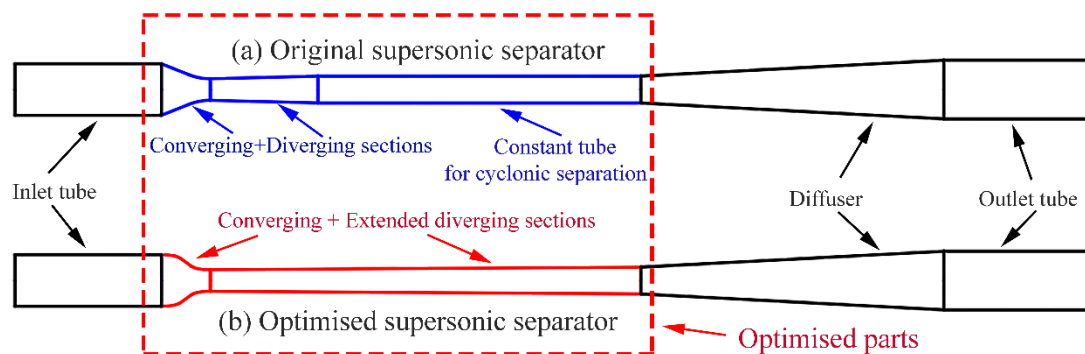


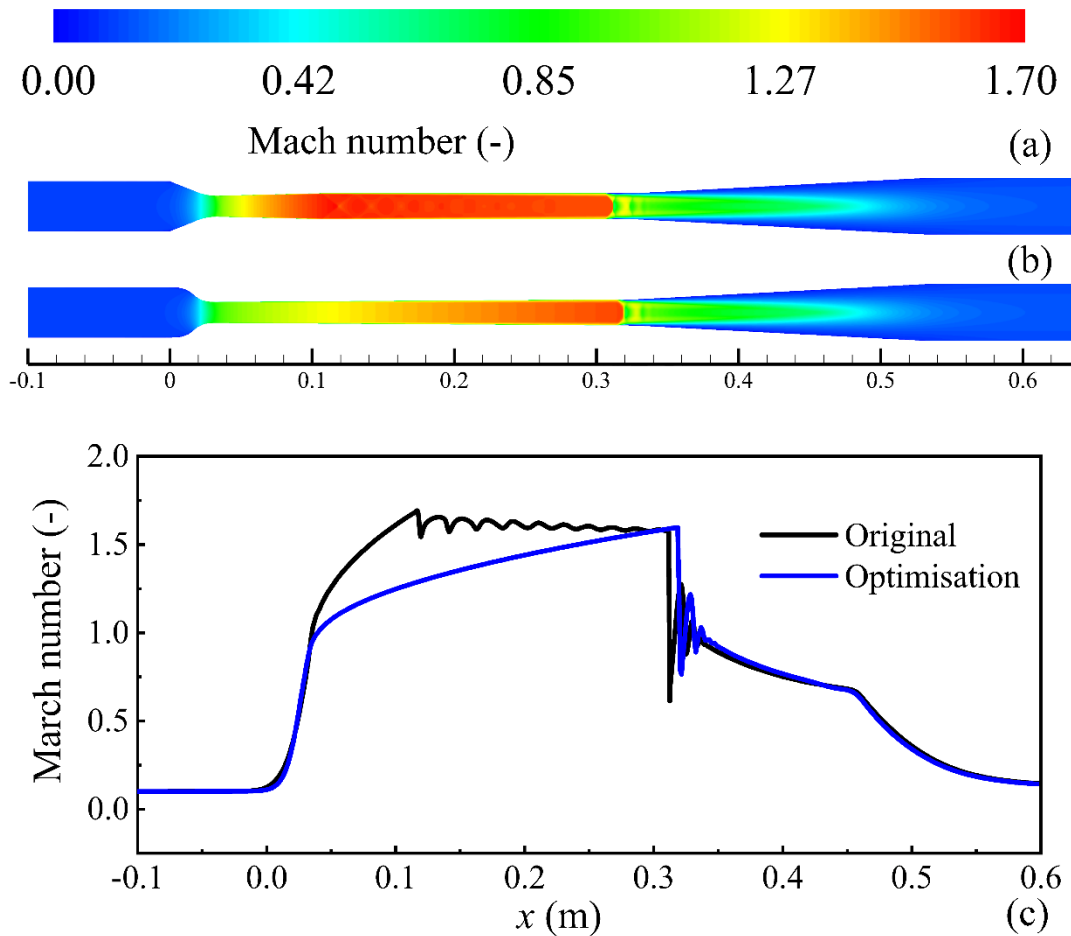
Fig. 12 Schematic diagram of the original and optimised supersonic separators

273 The detailed comparison of the flow and condensation parameters are described in
274 Figs. 13-17, including the Mach number, degree of supersaturation, nucleation rate,
275 droplet radius and liquid fraction. The Mach number in the original and optimised
276 supersonic separators presents that the vapour expands uniformly in the long diverging
277 part of the new nozzle compared to the original geometry which gives a faster
278 expansion and generates oblique and expansion waves. The fluctuation of the profiles
279 is not observed within the optimised supersonic separator, meaning that the oblique and
280 expansion waves disappear in the newly designed device.

281 The degree of supersaturation, which is defined as the ratio of the vapour pressure
282 to the saturation pressure, moves forwards the nozzle entrance in the optimised
283 supersonic separator compared to the one in the original geometry. This means that the
284 extremely nonequilibrium state occurs earlier in the optimised supersonic separator. It,
285 therefore, causes an earlier onset of the nucleation process as described in Fig. 15.
286 Accordingly, the optimised maximum value of the nucleation rate declines to $6.13 \times$
287 $10^{22} \text{ m}^{-3} \text{ s}^{-1}$ compared to $8.59 \times 10^{22} \text{ m}^{-3} \text{ s}^{-1}$ in the original geometry. When looking into
288 the details of the growth process of the condensed droplets, it can be seen that the
289 optimised geometry leads to an earlier onset of the formation of the liquid droplet. This
290 demonstrates that an earlier nucleation process induces an earlier formation of the
291 droplets. The optimized supersonic separator presents larger sizes of the condensed
292 droplet compared to the original one. Fig 17 reveals that the optimised geometry
293 induces an earlier onset of the liquid fraction compared to the original supersonic
294 separator. The liquid fraction then increases uniformly inside the long diverging section

295 of the newly designed nozzle in the optimised supersonic separator, which generates a
296 maximum liquid fraction of approximately 0.084 of the total mass.

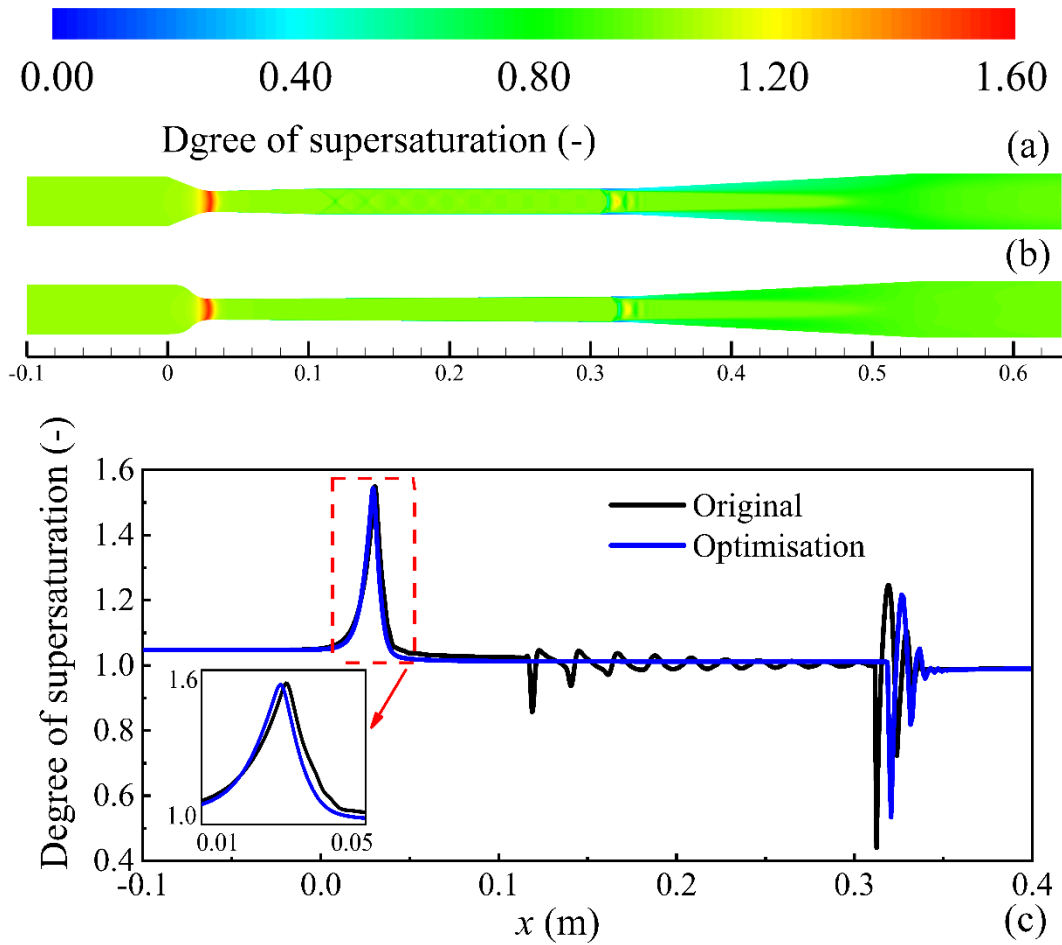
297 Furthermore, the profiles of the flow and condensation parameters depict that the
298 shock position inside the optimised separator moves downstream compared to the one
299 in the original geometry. The profiles of the Mach number and degree of supersaturation
300 illustrate that the optimised supersonic separator weakens the intensity of the shock
301 waves. The optimised idea of combining the nozzle diverging part and the constant tube
302 as a long diverging part of the newly designed nozzle reduces the energy loss due to the
303 oblique and expansion waves and improve the energy efficiency of the supersonic
304 separation.



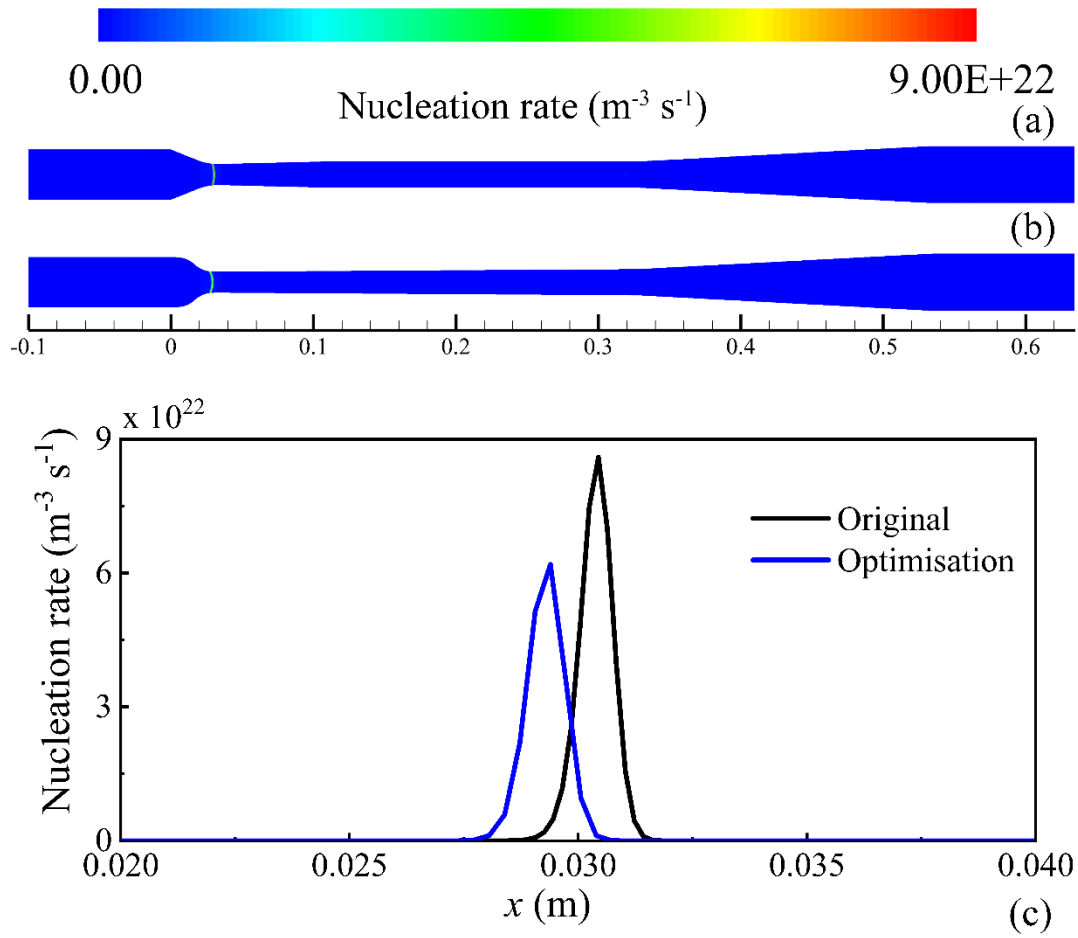
305

306 Fig. 13 Mach number in original and optimised supersonic separators: contours of the

307 original geometry (a), contours of the optimised geometry (b) and profiles of the
 308 original and optimised geometries (c)



309
 310 Fig. 14 Degree of supersaturation in original and optimised supersonic separators:
 311 contours of the original geometry (a), contours of the optimised geometry (b) and
 312 profiles of the original and optimised geometries (c)

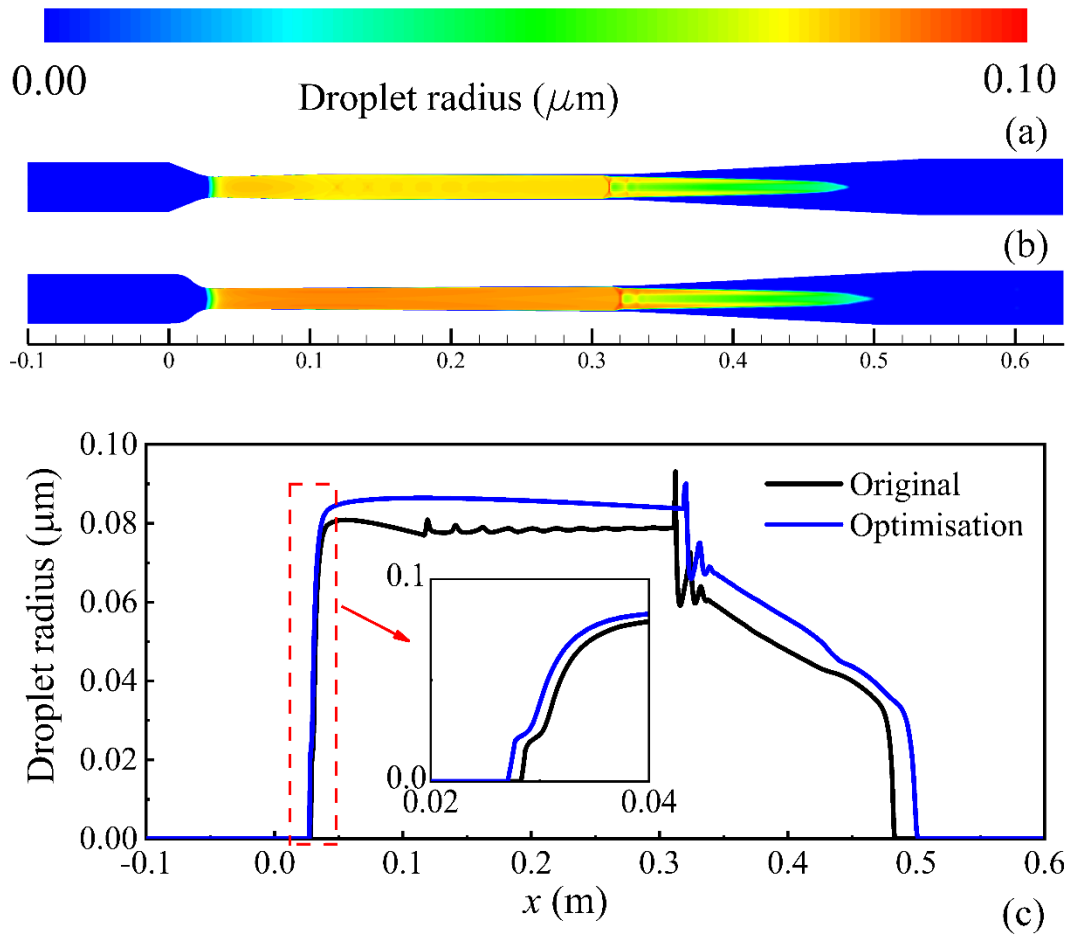


313

314 Fig. 15 Nucleation rate in original and optimised supersonic separators: contours of

315 the original geometry (a), contours of the optimised geometry (b) and profiles of the

316 original and optimised geometries (c)



317

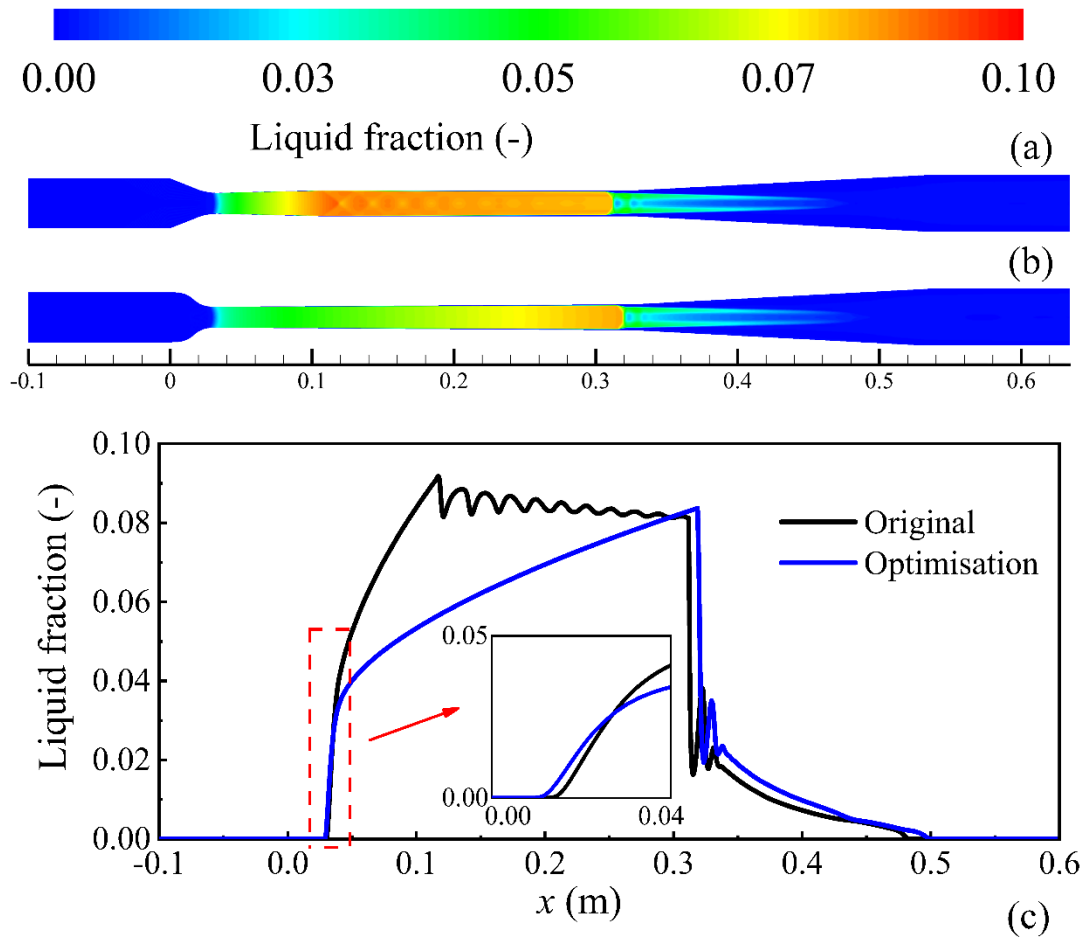
318 Fig. 16 Droplet radius in original and optimised supersonic separators: contours of the

319 original geometry (a), contours of the optimised geometry (b) and profiles of the

320 original and optimised geometries (c)

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323

324 Fig. 17 Liquid fraction in original and optimised supersonic separators: contours of
 325 the original geometry (a), contours of the optimised geometry (b) and profiles of the
 326 original and optimised geometries (c)

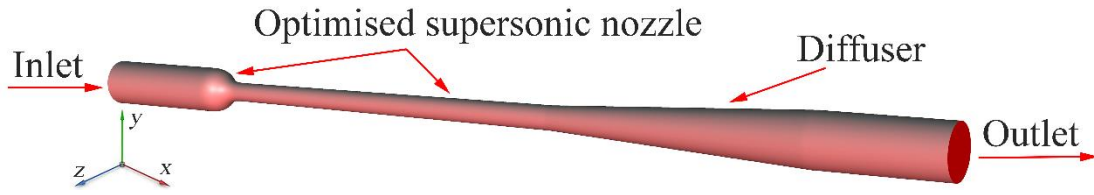
327 3.5. Two-dimensional axisymmetric and three-dimensional simulations

328 As there is a query that the supersonic separator is simplified to the two-
 329 dimensional simulation in this study, the two-dimensional (2D) axisymmetric and
 330 three-dimensional (3D) simulations are carried out for the optimised supersonic
 331 separator. The 3D geometry of the supersonic separator is shown in Fig. 18. The flow
 332 features, such as the contours and profiles of the Mach number and the liquid fraction
 333 are described in Figs. 19-20 based on the 2D axisymmetric and 3D simulations. It can
 334 be seen that similar results are obtained from the 2D and 3D simulations, while there

335 are some differences between them. The 3D simulation moves the position of the shock
336 wave tiny upstream compared to the 2D simulation. The position of the shock wave
337 locates at $x = 0.317$ m for the 3D case, while the shock wave occurs at $x = 0.320$ m for
338 the 2D simulation. Subsequently, the different expansion levels of the vapour in the
339 supersonic separator are observed that the vapour expands further for the 2D simulation
340 with the maximum Mach number of approximately 1.60, while the 3D simulation
341 predicts the maximum one of about 1.56.

342 The significant differences are observed downstream the shock waves for the 2D
343 and 3D simulations of the optimised supersonic separators. It can be seen that both these
344 two cases achieve almost the same Mach number near the exit plane of the separator
345 although the Mach number predicted by 3D case declines more quickly than the 2D
346 axisymmetric case. Furthermore, the liquid fraction decreases to zero at $x = 0.406$ m for
347 the 3D simulation while it disappears at $x = 0.498$ m for the 2D simulation. This
348 indicates that both 2D and 3D simulations predict the re-evaporation of the condensed
349 droplets.

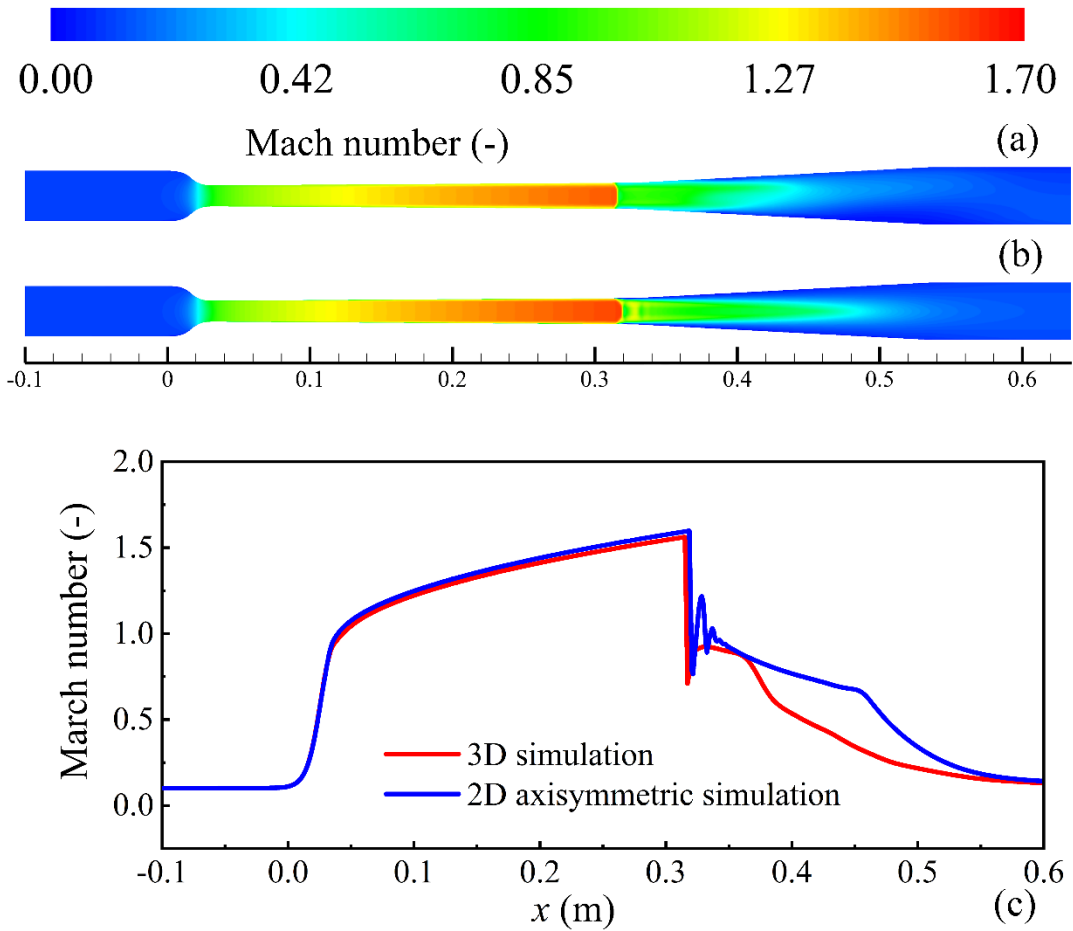
350 In general, both the 2D axisymmetry and 3D simulations predict very similar
351 results upstream the shock wave with tiny different shock positions. The differences
352 downstream shock waves do not affect the separation performance significantly for
353 these 2D and 3D cases. Therefore, the 3D simulation for the supersonic separator can
354 be reflected by the 2D axisymmetric modelling, which is acceptable considering the
355 computational cost and time.



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Fig. 18 Three-dimensional geometry of the optimised supersonic separator.



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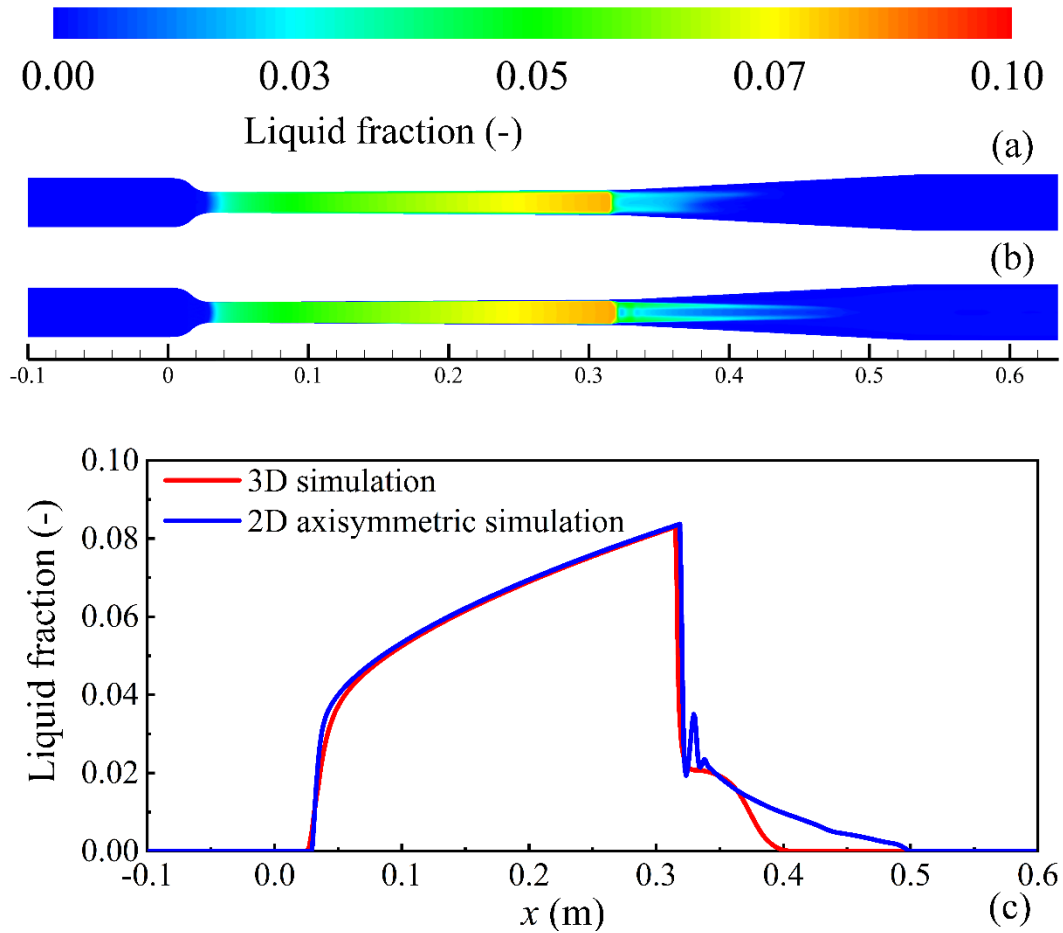
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Fig. 19 Mach numbers in two-dimensional axisymmetric and three-dimensional supersonic separators: contours of the three-dimensional simulation (a), contours of the two-dimensional axisymmetric simulation (b) and profiles of the two-dimensional axisymmetric and three-dimensional simulations (c)



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4. Conclusions

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The computational fluid dynamics modelling is developed for the performance evaluation of the supersonic separator. The single-phase flow model with an assumption of the dry gas stream causes unlimited decreases of the static pressure and temperature regardless of the saturation effect. The condensing flow model computes a liquid fraction of approximately 9.2% of the total mass, which influences the heat and mass transfer behaviour during the phase change process of water vapour in the supersonic

375 separator.

376 The supersonic separator is optimised based on the idea of combining the nozzle
377 diverging part and the constant tube as a long diverging part of the optimised nozzle.
378 The optimised supersonic separator can improve the separation performance by a)
379 eliminating oblique and expansion waves, b) inducing an earlier onset of the nucleation
380 rate and generating larger droplets, and c) moving downstream the shock position and
381 weakening the intensity of the shocks.

382 The present study ignores a swirling flow in a supersonic separator and a two-
383 dimensional axisymmetric model is employed to focus on the phase change of water
384 vapour. The impact of the swirling flow on the condensation process in a supersonic
385 separator based on the three-dimensional model will be carried out in future studies.

386 **Conflict of interest**

387 The authors declared that there is no conflict of interest.

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