

# PyTorch-Hebbian: facilitating local learning in a deep learning framework

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## Unsupervised local learning in neural networks

Recently, unsupervised local learning, based on Hebb's idea that change in synaptic efficacy depends on the activity of the pre- and postsynaptic neuron only [1], has shown potential as an alternative training mechanism to backpropagation. Unfortunately, Hebbian learning remains experimental and rarely makes its way into standard deep learning frameworks. In this work, we:

- Propose a PyTorch framework for thorough and systematic evaluation of local learning rules.
- Investigate the potential of Hebbian learning in the context of standard deep learning workflows.
- Expand the Krotov-Hopfield learning rule to CNNs.
- Illustrate the potential of Hebbian learned feature extractors for image classification.

## The Krotov-Hopfield learning rule

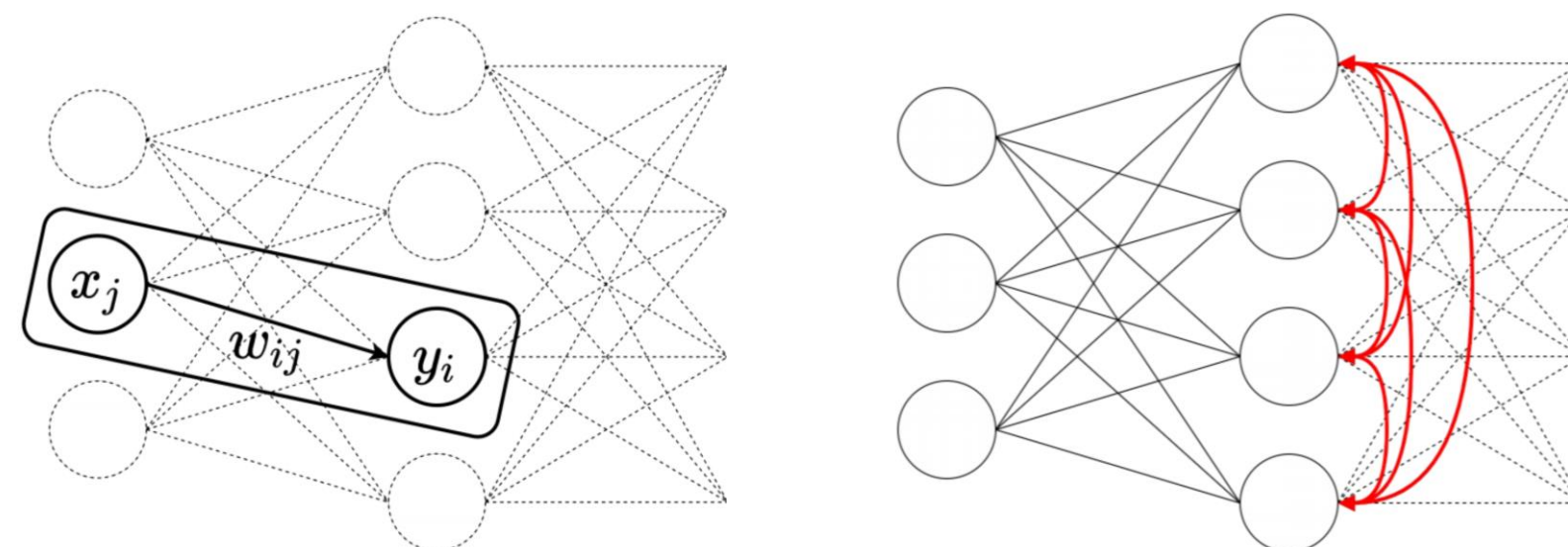
A computationally feasible Hebbian learning rule

Krotov and Hopfield propose a biologically inspired learning rule that combines both normalization and lateral inhibition [2]. They introduce their learning rule in the context of feedforward neural networks with a single hidden layer, consisting of  $M$  hidden neurons or units ( $m, p$  and  $\Delta$  are hyperparameters):

$$\Delta w_{ij} = g(\text{rank}(\langle \mathbf{w}_i, \mathbf{x} \rangle_i)) (x_j - \langle \mathbf{w}_i, \mathbf{x} \rangle_i w_{ij})$$

$$\langle \mathbf{w}_i, \mathbf{x} \rangle_i = \sum_j |w_{ij}|^{p-2} w_{ij} x_j$$

$$g(\mu) = \begin{cases} 1 & \mu = M \\ -\Delta & \mu = M - m \\ 0 & \text{otherwise} \end{cases}$$

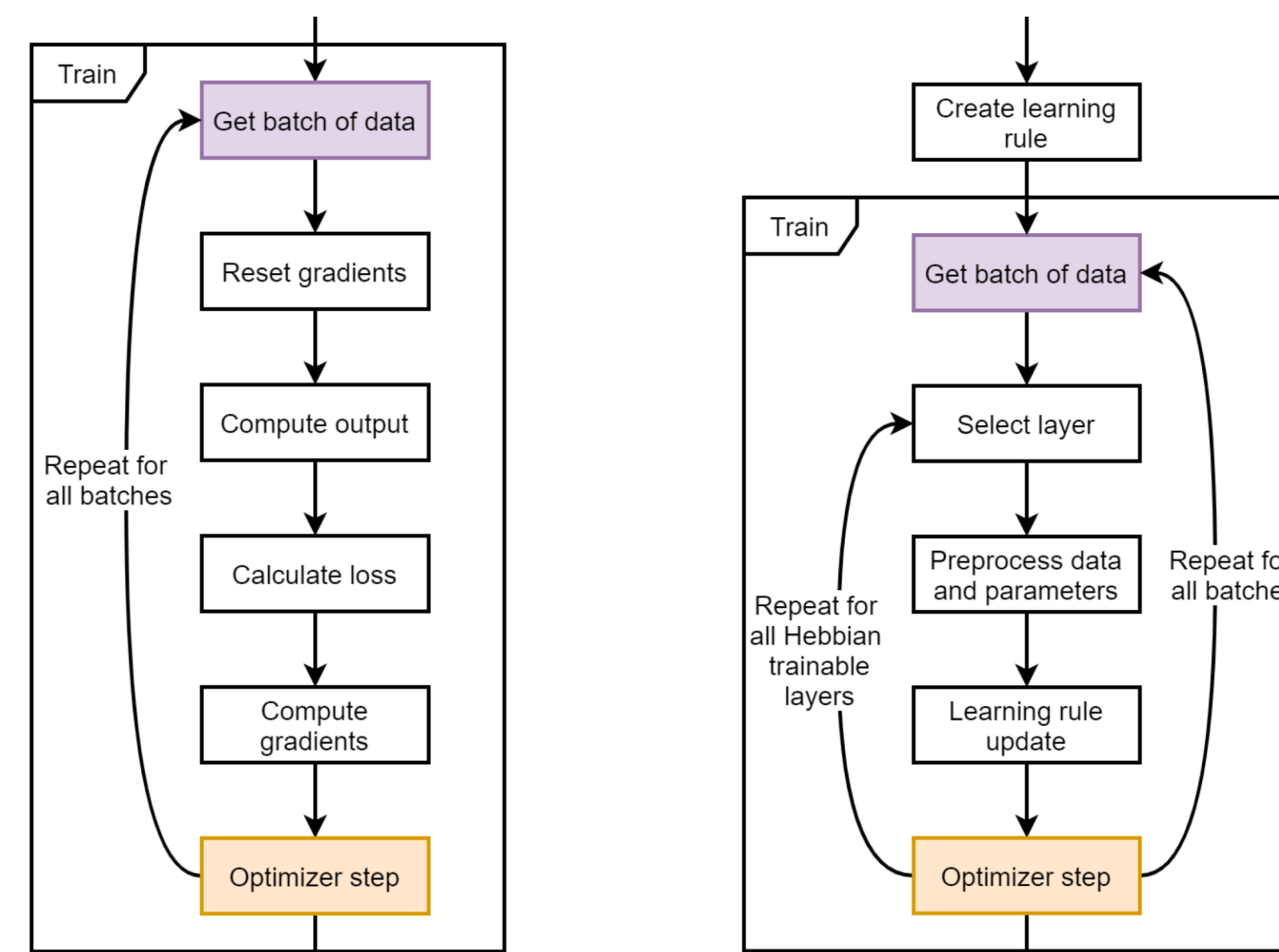


(a) A connection with weight  $w_{ij}$  between pre- and postsynaptic neuron,  $j$  and  $i$ . (b) Competition between neurons is introduced by adding inhibitory lateral connections (red arrows) between all neurons.

## A PyTorch framework for local learning rules

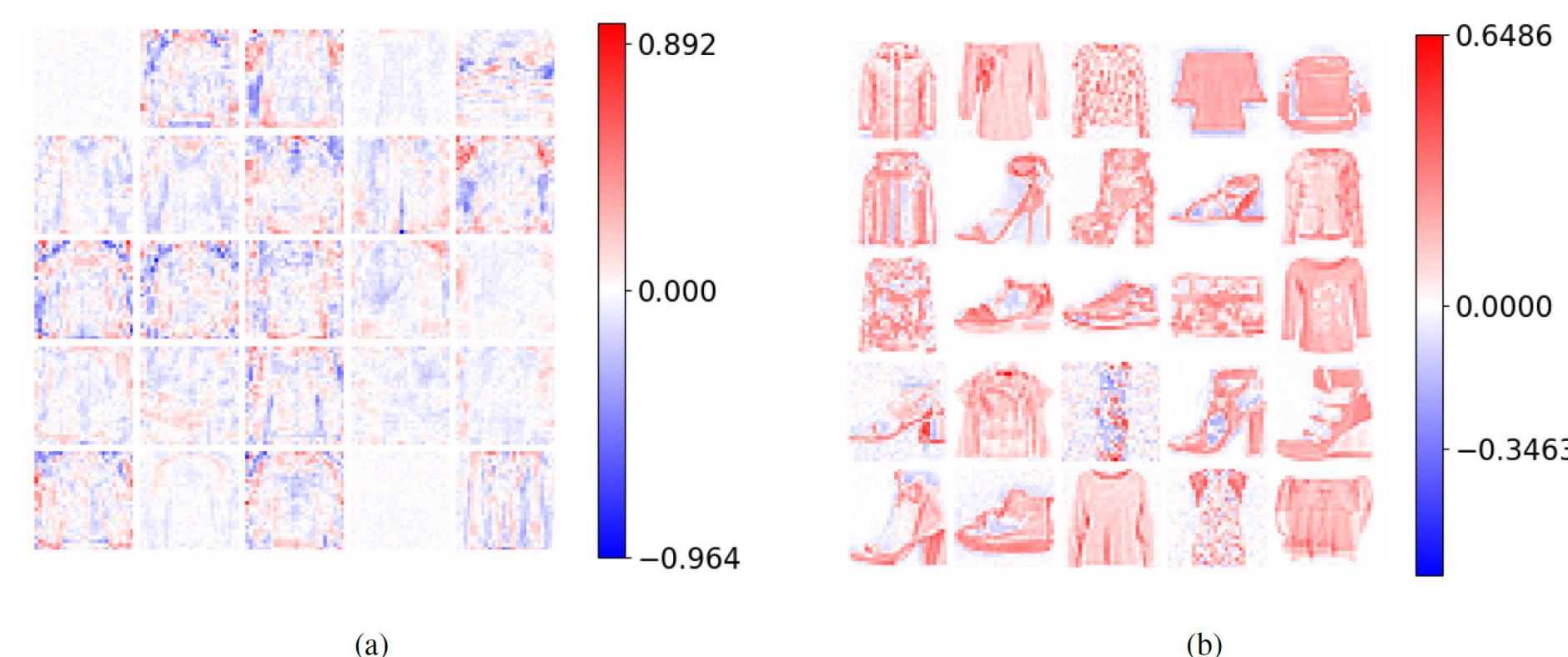
Introducing local learning into standard deep learning workflows

Hebbian learning introduces a new learning paradigm with an accompanying shift in execution flow. The flow for a single epoch, compared to the classical backpropagation execution flow, is illustrated below. For Hebbian learning, there is no single forward pass and the Hebbian trainable layers are trained separately. The Hebbian paradigm thus introduces a second loop.



A comparison of the learning flow of backpropagation (left) and Hebbian learning (right).

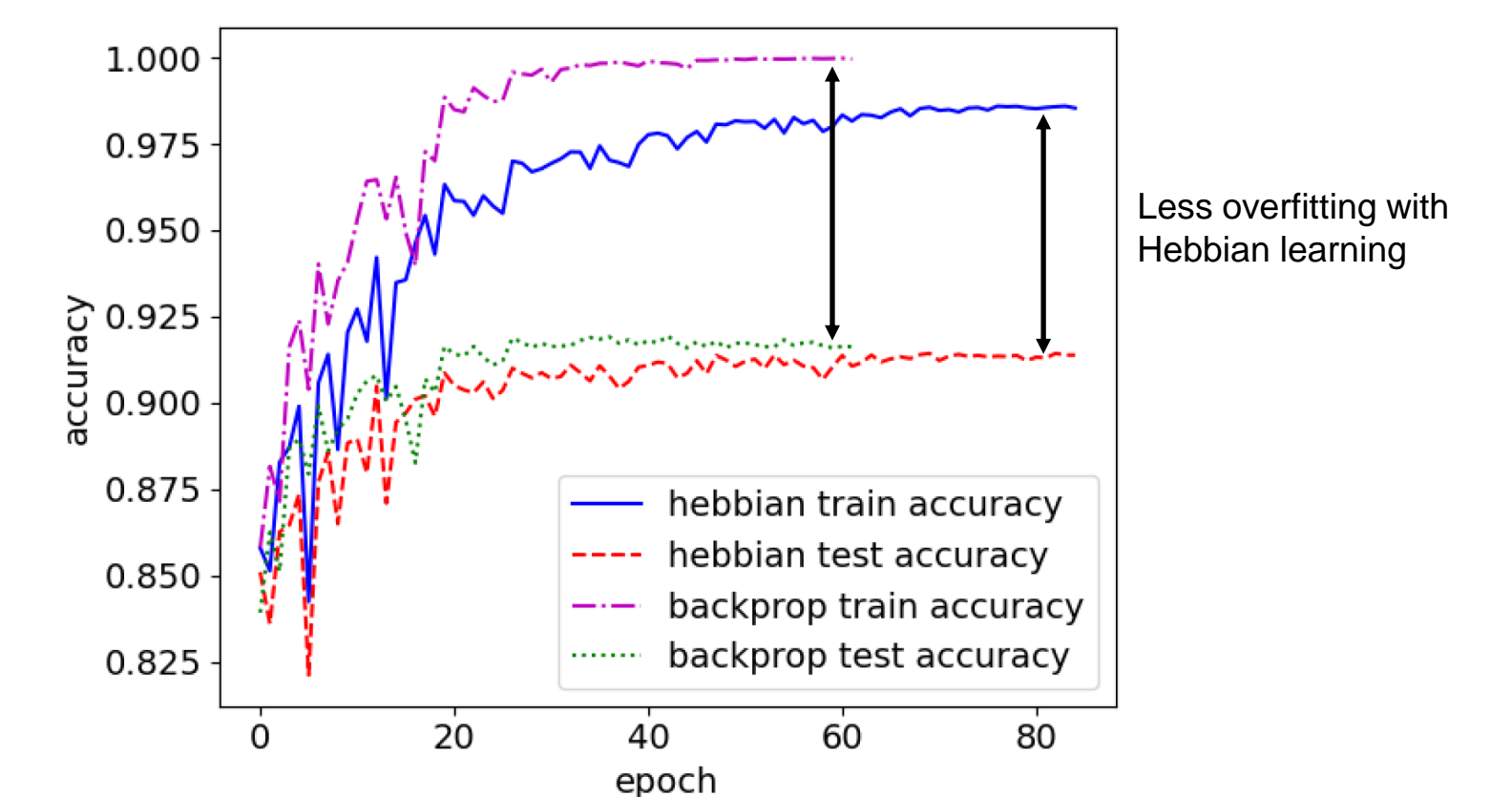
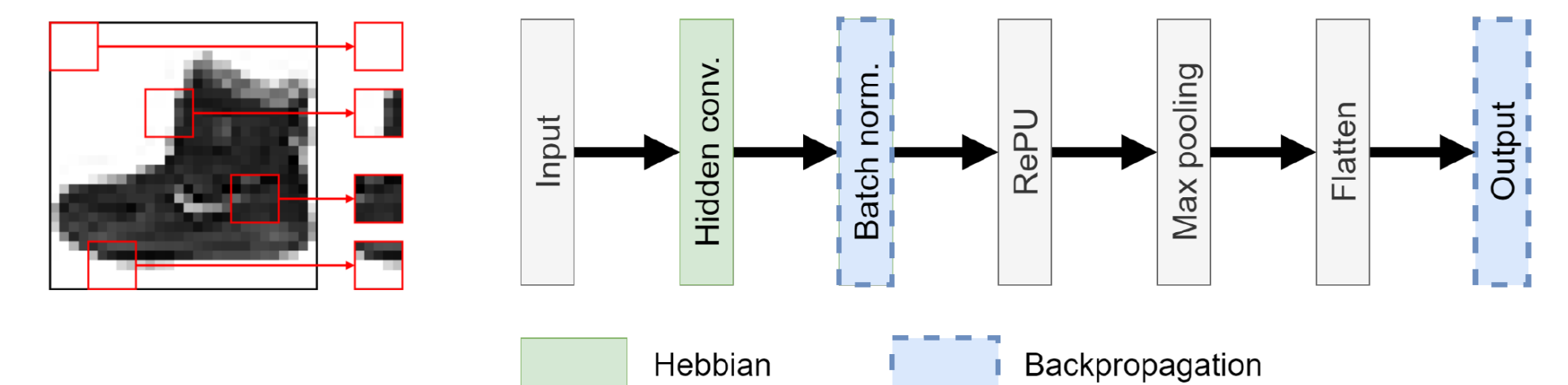
The proposed framework fully supports **CUDA** and offers more room for **parallelism** compared to backpropagation. For the Krotov-Hopfield learning rule on the MNIST digits dataset, our proposed framework is **14 times faster** with only 3 seconds per epoch compared to 44 seconds for the original numpy implementation [3].



The incoming weights for 25 (out of 2000) randomly sampled fully connected hidden units trained end-to-end with backpropagation (a) and the Krotov-Hopfield learning rule (b) on the MNIST fashion dataset.

## Experimental results and analysis

Using the novel framework, a convolutional layer was trained with the Krotov-Hopfield learning rule on the MNIST fashion dataset. The output layer was then trained with backpropagation. The resulting network achieves 91.44% test accuracy, which is **only 0.5% lower compared to the same network trained end-to-end with backpropagation**.



Train and test accuracy curves for the CNN trained on MNIST fashion with end-to-end backpropagation compared to backpropagation for the final layer only, with a Hebbian learned hidden layer.

	Hebb + backprop	End-to-end backprop
train accuracy (%)	98.64	99.98
test accuracy (%)	91.44	91.94

<https://github.com/Joxis/pytorch-hebbian> (available for your experiments)

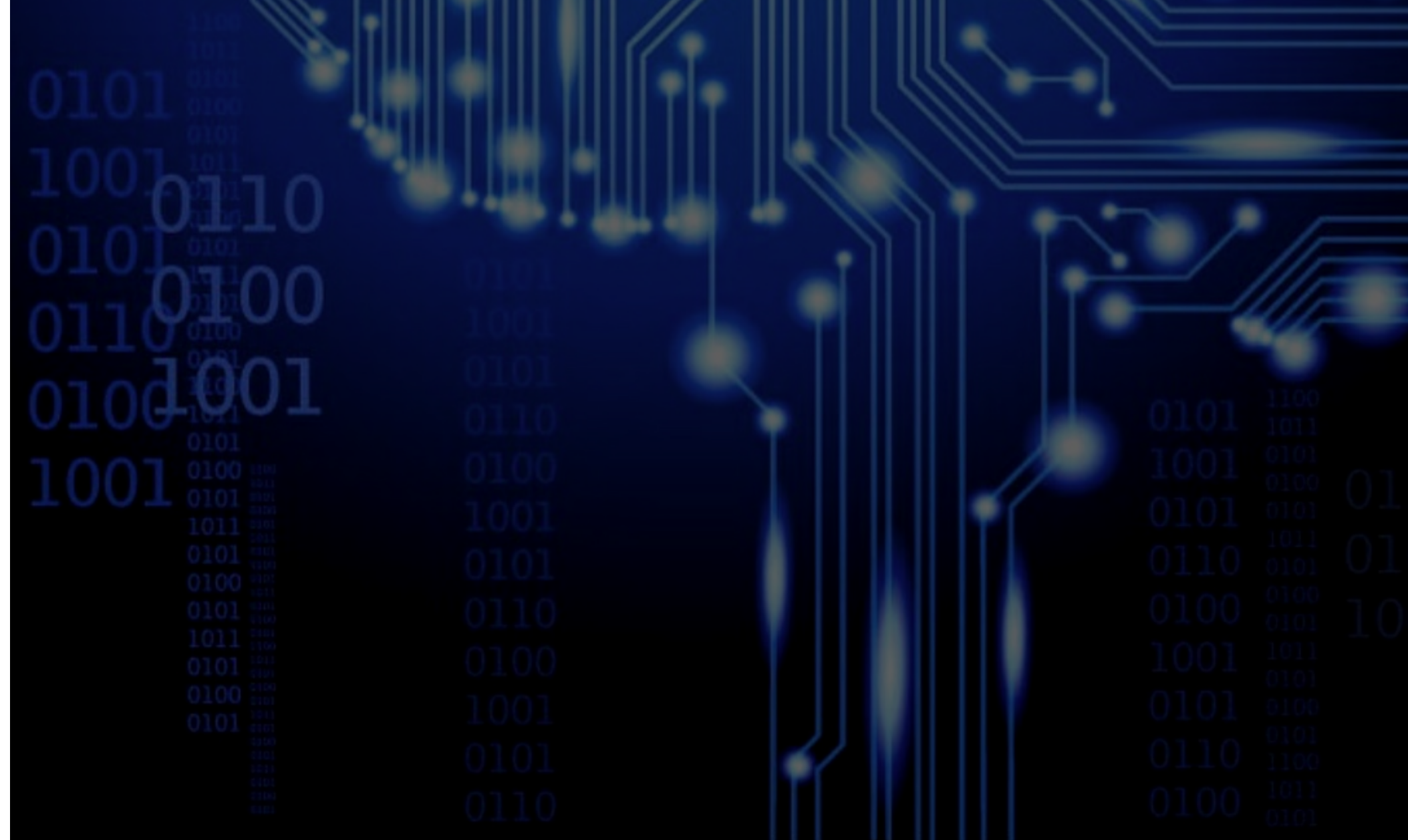
## References

- [1] D. O. Hebb, *The Organization of Behavior: A Neuropsychological Theory*. Psychology Press, 1949.
- [2] D. Krotov and J. J. Hopfield, "Unsupervised learning by competing hidden units," *Proceedings of the National Academy of Sciences*, vol. 116, pp. 7723–7731, Apr. 2019.
- [3] D. Krotov, "DimaKrotov/Biological\_learning." [https://github.com/DimaKrotov/Biological\\_Learning](https://github.com/DimaKrotov/Biological_Learning), Apr. 2020.

# BEYOND BACKPROPAGATION

Novel Ideas for Training Neural Architectures

Workshop at NeurIPS, 12th of December 2020



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## Overview

Is backpropagation the ultimate tool on the path to achieving artificial intelligence as its success and widespread adoption would suggest?

Many have questioned the biological plausibility of backpropagation as a learning mechanism since its discovery. The weight transport and timing problems are the most disputable. The same properties of backpropagation training also have practical consequences. For instance, backpropagation training is a global and coupled procedure that limits the amount of possible parallelism and yields high latency.

These limitations have motivated us to discuss possible alternative directions. In this workshop, we want to promote such discussions by bringing together researchers from various but related disciplines, and to discuss possible solutions from engineering, machine learning and neuroscientific perspectives.

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## Accepted Papers

We will have two poster sessions in [\[Gather.Town\]](#). The numbers correspond to the papers' locations during these poster sessions. See map below.

### Papers accepted for oral presentations

- 19. Hardware Beyond Backpropagation: a Photonic Co-Processor for Direct Feedback Alignment - *Julien Launay, Iacopo Poli, Kilian Müller, Igor Carron, Laurent Daudet, Florent Krzakala, Sylvain Gigan* [\[Video\]](#)
- 36. Policy Manifold Search for Improving Diversity-based Neuroevolution - *Nemanja Rakicevic, Antoine Cully, Petar Kormushev* [\[Video\]](#)
- 39. Randomized Automatic Differentiation - *Deniz Oktay, Nick B McGreivy, Joshua Aduol, Alex Beatson, Ryan P Adams* [\[Video\]](#)  
ZORB: A Derivative-Free Backpropagation Algorithm for Neural Networks - *Varun Ranganathan, Alex Lewandowski* [\[Video\]](#)

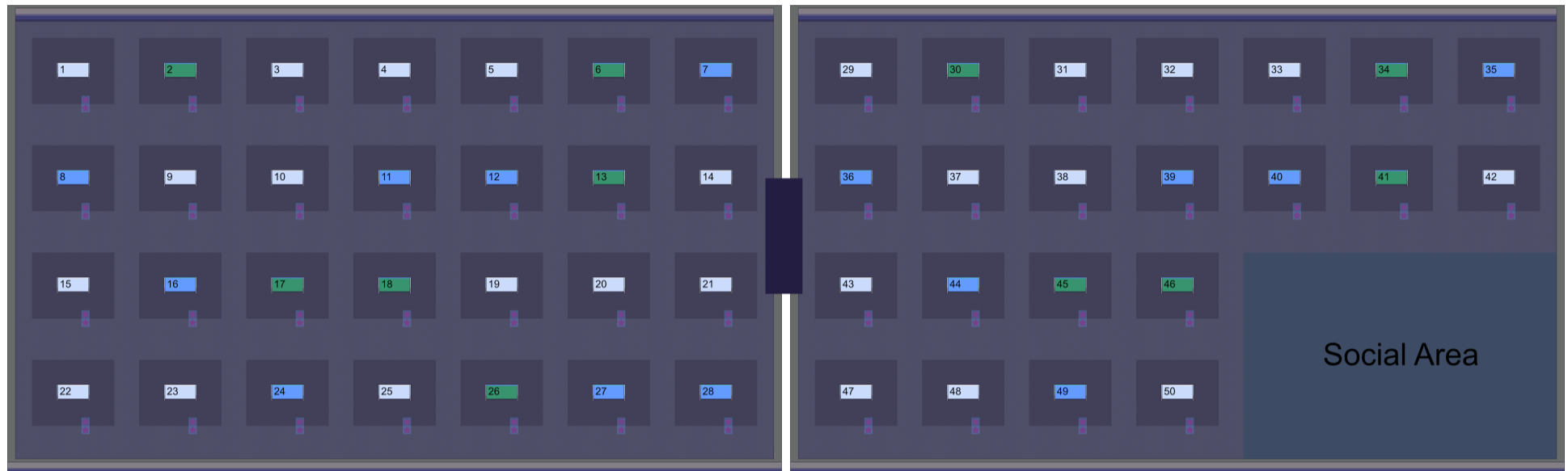
### Papers accepted for poster presentations

- 1. A biologically plausible neural network for local supervision in cortical microcircuits - *Siavash Golkar, David Lipshutz, Yanis Bahroun, Anirvan Sengupta, Dmitri Chklovskii*
- 2. A More Biologically Plausible Local Learning Rule for ANNs - *Shashi Kant Gupta*
- 3. A Theoretical Framework for Target Propagation - *Alexander Meulemans, Francesco S Carzaniga, Johan Suykens, João Sacramento, Benjamin F. Grewe*
- 4. Align, then Select: Analysing the Learning Dynamics of Feedback Alignment - *Maria Refinetti, Stéphane d'Ascoli, Ruben Ohana, Sebastian Goldt*
- 5. Architecture Agnostic Neural Networks - *Sabera Talukder, Guruprasad Raghavan, Yisong Yue*
- 6. Backpropagation Free Transformers - *Dinko D Franceschi*
- 7. Biophysical Neural Networks Provide Robustness and Versatility over Artificial Neural Networks - *James Hazelden, Michael I Ivanitskiy, Daniel Forger*
- 8. BP2T2: Moving towards Biologically-Plausible BackPropagation Through Time - *Arna Ghosh, Jonathan Cornford, Blake Richards*
- 9. Convolutional Neural Networks from Image Markers - *Barbara C Benato, Italos Estilon de Souza, Felipe L Galvao, Alexandre X Falcão* [\[Video\]](#)

10. Deep Networks from the Principle of Rate Reduction - *Kwan Ho Ryan Chan, Yaodong Yu, Chong You, Haozhi Qi, John Wright, Yi Ma*
11. Deep Neural Network Training without Multiplications - *Tsuguo Mogami*
12. Deep Neural Networks Are Congestion Games - *Nina Vesseron, Ievgen Redko, Charlotte Laclau*
13. Deep Reservoir Networks with Learned Hidden Reservoir Weights using Direct Feedback Alignment - *Matthew S Evanusa, Aloimonos Yiannis, Cornelia Fermuller* [\[Video\]](#)
14. Direct Feedback Alignment Scales to Modern Deep Learning Tasks and Architectures - *Julien Launay, François Boniface, Iacopo Poli, Florent Krzakala*
15. Feature Whitening via Gradient Transformation for Improved Convergence - *Shmulik Markovich-Golan, Barak Battash, Amit Bleiweiss*
16. Front Contribution instead of Back Propagation - *Swaroop Ranjan Mishra, Anjana Arunkumar* [\[Video\]](#)
17. Gated Linear Networks and Extensions - *Eren Sezener, David Budden, Marcus Hutter, Christopher Mattern, Jianan Wang, Joel Veness*
18. Generalized Stochastic Backpropagation - *Amine Echraibi, Joachim Flocon-Cholet, Stéphane W Gosselin, Sandrine Vaton*
20. HebbNet: A Simplified Hebbian Learning Framework to do Biologically Plausible Learning - *Manas Gupta, ArulMurugan Ambikapathi, Ramasamy Savitha* [\[Video\]](#)
21. Hindsight Network Credit Assignment - *Kenny Young* [\[Video\]](#)
22. How and When does Feedback Alignment Work? - *Stéphane d'Ascoli, Maria Refinetti, Ruben Ohana, Sebastian Goldt*
23. Ignorance is Bliss: Adversarial Robustness by Design through Analog Computing and Synaptic Asymmetry - *Alessandro Cappelli, Ruben Ohana, Julien Launay, Iacopo Poli, Florent Krzakala*
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25. Investigating Coagent Networks for Supervised Learning - *Dhawal Gupta, Matthew Schlegel, James Kostas, Gabor Mihucz, Martha White*
26. Investigating the Scalability and Biological Plausibility of the Activation Relaxation Algorithm - *Beren Millidge, Alexander D Tschanz, Anil Seth, Christopher Buckley*
27. Layer-wise Learning of Kernel Dependence Networks - *Chieh Tzu Wu, Aria Masoomi, Arthur Gretton, Jennifer Dy* [\[Video\]](#)
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38. PyTorch-Hebbian: facilitating local learning in a deep learning framework - *Jules Talloen*
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## Reviewers

We would like to thank all of our reviewers for their great work:

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