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Techniques to Visualize Occluded Graph Elements for 2.5D Map Editing

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Abstract

We propose an interface with two novel techniques to visualize occluded graph nodes and edges that help the user edit map data with a 2.5D geographical structure (*e.g.*, multi-floor indoor maps). We first design a visualization technique —*Repel Signification*— that employs microanimation to signify the graph elements that are overlapping with each other (and potentially erroneous). We also design a technique that enables the user to edit the occluded components with *Expansion Interaction*, which simultaneously visualizes both in-floor and across-floor occluded connections between the map elements. The combination of the two methods would enable the map editors (non-experts) to effectively find and fix erroneous data in 2.5D maps without changing the operation manner from the existing 2D mapediting interface.

Author Keywords

Geovisualization; Graph visualization.

CCS Concepts

-Human-centered computing \rightarrow Interaction techniques; Geographic visualization;

Introduction

Location-based services utilize geographical data of the physical environment (*e.g.*, road networks, points-of-interest)

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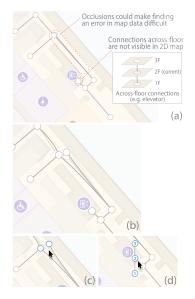


Figure 1: (a) Node/edge occlusions and across-floor connections make it difficult to find topological errors when a map for a multi-floor building was manually composed. (b) We design a technique that visualizes these occluded elements with micro-animation (repel) to support users to find them. We also design an interaction technique that visualizes (c) occlusions and (d) across-floor connection relationships related to the element near the cursor, which supports users acquire and edit the occluded elements.

to help users explore, navigate, and search for information about the physical world. Readily available map data (e.g., OpenStreetMap¹), represented as geographically and topologically constrained networks of nodes and edges (i.e., graphs), enables the development of such technologies. On OpenStreetMap, for instance, the data contributors use a map editing tool to draw nodes and edges to extend the graph that represents the geography and topology of the built environment in the given region. However, existing editing tools have limited capabilities in helping users explore and edit 2.5D geographical data that emerge as a result of representing the indoor environment of multi-floor buildings and dense, complex urban structures where layers of geographical data are placed on top of each other. One consequence of such inept interfaces is our inability to fix erroneous map elements that are unobservable due to occlusions (e.g., components that are incorrectly connected but hard to find; Figure 1a).

Considerable attention has been paid to addressing occlusions and consequent problems in network visualization, where researchers explored ways to visualize complex data like social networks, molecular maps, and transport networks [2, 12, 13]. For example, researchers have attempted to improve the visibility by rearranging the layout by using tree structures [21, 29], radial views [5], or fisheve distortions [24, 25], etc. However, much work has dealt with geographically unconstrained networks. A unique restriction of a map that requires nodes and edges to represent physical coordinates prevents us from optimizing the layout of graph elements (which mutates the elements' coordinates). Meanwhile, prior work has documented types of occlusions [4, 32] occurred in geographical data, and much also has been done on resolving the occlusions by bundling edges together [1, 14], applying a lens-metaphor visualization [33],

¹https://www.openstreetmap.org/

or directly interacting with them [16, 26, 32]. However, little has been done on exploring how to deal with erroneous elements in 2.5D maps.

In this paper, we propose novel methods to visualize occluded elements in the context of editing 2.5D map data. We design the methods with the intention to extend the existing 2D map interface. First, to support users find occluded elements, we design a visualization technique that uses micro-animation (*Repel Signification*) (Figure 1b) to signify the occluded elements. Second, to enable users to edit (acquire) map elements that are overlapping each other, we implement an *Expansion Interaction*—see Figure 1c and 1d—which visualizes the occlusions and acrossfloor connection relationships related to the element near the cursor. We believe the combination of the two methods will help non-expert users find and fix the map data errors in 2.5D maps with almost no change of operation manner from the existing 2D map interface.

Background and Related Work

Modern location-based services and geographic information systems (GIS) demand high-quality spatial data for them to operate [20]. Mobile navigation tools like Google Maps², for example, combines a large and fine grained street network data with a routing algorithm to navigate a driver from one point to another. For such technologies to operate properly, data quality is paramount, and thus GIS and cartography researchers have studied spatial data quality for decades [3, 15, 27]. Van Oort offered a list of types of spatial data quality through a comprehensive survey [28].

Involvement of increasing number of non-experts without knowledge of geographical data emphasizes quality control

²https://maps.google.com/

of spatial data [28]. Involvement of paid or volunteer online workers to map geographical data (sometimes called volunteered geographical information or VGI) is common nowadays [6, 7, 8, 9, 10, 17, 18, 19, 23]. Notably, Open-StreetMap aims to create a set of public map data with edits of millions of volunteer workers [6, 7, 8]. Haklay *et al.* reported that the data provided by online workers is fairly accurate [7]. Recently, there are also attempts to apply Open-StreetMap to indoor route planning with 3D representation (*e.g.*, [30]). Priedhorsky *et al.* explored a technique to communicate potentially erroneous data in 2D maps of bicycle lanes. [18]. But we lack simple techniques to assess the quality of spatial data, particularly the geographical data that contains across-floor information and resides in 2.5D space.

Debiasi *et al.* have schematized visual clutter problems, which can occur when the components and geographic surfaces overlap with each other [4]. Wong *et al.* have also listed possible readability issues in edge congested graphs [32]. Although these visibility issues in 2D graph data are well investigated and summarized in detail, there are still few studies that consider geographic data with 2.5D structure. When dealing with 2.5D maps that consider multiple floor levels, across-floor connections (*e.g.*, stairs or elevators) can be utilized, but they cannot be essentially represented in most existing visualization techniques.

Communicating and visualizing complex graph data has been a research topic of information visualization. There are number of techniques to deal with the visual clutter problems by interacting with the graph data. Wong *et al.* have proposed techniques called EdgeLens [33], in which graph edges curve away from the user's point of focus allowing them to disambiguate the visual clutters without losing the nodes' spatial relationships. EdgePlucking offers the user to move edges with plucking action to reduce congestion [32]. Schmidt *et al.* have designed a group of techniques to solve visual clutter problems utilizing multitouch interaction [26]. Riche *et al.* tries to improve visibility by interactively controlling link curvature [22]. These techniques resolve graph occlusions in 2D maps well, but they are sometimes not effective for use in 2.5D map editing tasks. One reason is that they do not consider 2.5D map structure. Another reason is that the visualization in these techniques requires the user to perform additional operations which sometimes conflict with the operations used in the existing map editing tools.

Proposed Techniques

Design Considerations

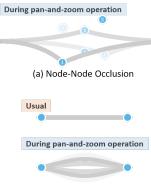
Supposing the task of data contributors co-editing 2.5D maps with multi-floor structure data, we design an interface to allow them to easily find and edit occluded components. Here we describe design considerations for the interface as follows.

Quick signification of the occluded elements. When a data contributor explores a map containing some occlusions (that are potentially topological errors), the interface should represent them to quickly notice to the user. One of the representative approaches is to change the visual properties (*e.g.*, color, shape, size, etc.) of the overlapping objects, which utilizes a human visual system called preattentive processing [11]. Our interface adopts a repelling micro-animation because many of visual properties such as color and shape are already used for representing other purposes in most commercial maps.

Detailed representation of the topology on the occluded elements. Existing tools like OpenStreetMap already offer map editing functionalities, but no way has been offered to

Usual

One node could occlude another, making it hard to find a potential error.



(b) Edge-Edge Occlusion

Figure 2: The behavior of *Repel Signification* for (a) node-node and (b) edge-edge occlusion. It uses shaking micro-animation to signify where an occlusion exists. Note: The translucent components represent animated time-lapse. The characters on the edges are not actually displayed. edit and fix the overlapped components or across-floor connections. Since finding erroneous elements is relatively a difficult task that requires the user to understand the structural relationship between components [4], our interface makes the components visually understandable and clickable to help the user correct the topology.

Retention of spatial and topological relationships. Since geographical accuracy is essential in map data, so the interface should basically maintain the spatial and topological relationships between components. We minimize the effect of the micro-animation on the spatial/topological relationships by making it occur only during the user's pan-and-zoom operation, inspired by the interactive relief shearing technique proposed by Willett *et al.*[31].

Familiarity of the user interface. Editing map data requires more operation variations than just navigation, such as adding, moving, and deleting map elements, so no more operations should be added for visualizing occluded errors. Therefore, we apply a subtle add-on to familiar pan-andzoom interface, which basically follows the style of existing map editing tools like OpenStreetMap.

Compatibility with PC. Of course map navigation and editing are used on various types of devices. As an initial exploration, this study focuses on designing mouse-based user interface on a PC.

Based on these considerations, we design methods to visualize and edit occluded map data on top of a familiar node-edge graph visualization, which resembles existing geographical data editing tools. First, to help the user find occluded data, we introduce *Repel Signification*, which signifies these elements with micro-animation coupled with panning and zooming operation (Figure 1b). Second, to enable editing the occluded components, our *Expansion Inter*- *action* visualizes both in-floor and across-floor connections between the map elements near the cursor (Figure 1c). We implement these methods and the graph editing user interfaces using HTML, CSS, and JavaScript (D3.js). In this section, we suppose an specific environment to demonstrate our proof-of-concept prototype: interacting with a graph that has $3840 \times 2400 \ px$ size and is generated on a grid with interval of 160 px though a $1280 \times 800 \ px$ -size window on a PC.

Technique 1: Repel Signication

To notice the existence of occluded elements, this technique utilizes micro-animation to signify them; the occluded components are signified with an animation only when the user is performing pan-and-zoom operations (Figure 2). The basic idea of the algorithm is that the pairs of nodenode, node-edge, and edge-edge that have close proximity are repelled and shaken using a metaphor of elastic objects like a spring. The repel force exponentially increases based on the proximity between the pair of elements, but these components remain swinging around the original position because the moving direction of these components are randomly determined at every frame.

In our implementation, the overlapping pairs are identified (and their repel forces are also calculated) by calculating each distance between the pair components (*i.e.*, node-node, edge-edge, or node-edge). We set the average distance of the repelled node and edge from the original position to approximately 16 *px* and 25 *px* respectively when the pair components completely overlap (and repel force is maximum). The shaking micro-animation gradually stops once the user stops dragging or zooming. Figure 2 shows example appearances of the repel motion.

Original

Expanded

Original

Expanded

Original

Expanded

overlaps.

1

(a) Node-Node Occlusion

(b) Edge-Edge Occlusion

(c) Node-Edge Occlusion

Figure 3: Behavior patterns of

Expansion Interaction for in-floor

Technique 2: Expansion Interaction

When a data contributor finds an erroneous element using Repel signification, then it is expected for him/her to fix it to the correct state by deleting/moving the element or adding new component(s). To achieve this, we introduce Expansion Interaction, a technique to visualize a specific element in 2.5D map, which tries to address problems of both difficulties in interpretation and acquisition of the occluded elements. With this technique, as the user moves the cursor around a graph, the component closest to the cursor is highlighted and identified as a target component for the expansion. Then the system visualizes its related components (*i.e.* components that are directly connected to the target component and their overlapped components) by showing them around the target component with repel animation while resolving their overlaps. Both the target component and the visualized related components become clickable, indicating that they can be edited by existing operations like ordinary map editing tools. We individually design the expansion behavior between in-floor and across-floor graph connections, as follows.

In-floor Expansion

Figure 3 overviews the basic behavior patterns of *expansion* interaction for in-floor overlaps which consist of nodenode, edge-edge, and node-edge expansions. The component that is closest to the cursor (and closer than a certain threshold distance) is determined the target component. Accordingly, the system identifies its related components as follows: (i) the edges that are directly connected to the target component, and (ii) the overlapping components with (i) and the target component. These related components are visualized with repel animation so that the overlaps are resolved; each pair of overlapping components move apart each other, and the displacements are determined by the close proximity between them before expansion; in our im-

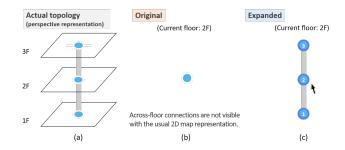


Figure 4: Behavior of *Expansion Interaction* for across-floor connections.

plementation, the displacement gets exponentially larger based on the proximity and we adjusted the maximum displacement (when two components overlap completely) as approximately 20 *px*. Once the *expansion* occurs, the expanded components remain visible unless the cursor moves away from either of them at the threshold distance.

Across-floor Expansion

Figure 4 shows the basic behavior of expansion interaction for across-floor connection. To represent the across-floor connection relationships in 2.5D maps, we introduce to simply illustrate them two-dimensionally while maintaining floorlevel relationships; upper-floor and lower-floor components are respectively drawn above and below the target component in a 2D map. In addition, a floor number is drawn on each of related nodes; we preliminary tested other representation patterns of the floor level such as change of the nodes' shapes or colors, but the method of describing floor numbers seemed to be the most easiest to understand the topology. In the example where the user is inspecting an error at an elevator node in the second floor as shown in Figure 4, only one node (second floor) is originally shown (Figure 4b), while the two other nodes with one level above and one level down become respectively shown at a distance

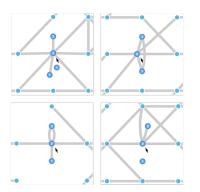


Figure 5: Example representations of simultaneous expansion for both in-floor and across-floor connections.

(40 px in our implementation) above and below the target component when the cursor is close (Figure 4c). Note that this expansion motion is not accompanied with repel animation in order to differentiate the visual effect between in-floor and across-floor representation.

In case there are both related components for in-floor and across-floor expansions in the graph, we simultaneously visualize them. When the user specifies a target component, the related components are determined as follows: (i) the edges that are directly connected to the target component in the floor. (ii) the nodes that are directly connected with the target component across different floors, (iii) the overlapping components with (i), (ii), and the target component, and (iv) the components that are prospectively overlapped with the newly displayed components of (ii) and (iii). The system then executes the expansion for all of these related components while resolving the overlaps and visualizing across-floor connection relationships at the same time. Figure 5 and video figure show several examples of simultaneous expansion for both in-floor and across-floor connections.

Early Results and Future Work

We conducted a preliminary test to get user feedback of the proposed techniques. Nine participants (6 males and 3 females) ranging from 20 to 27 ages participated. We first gave them an explanation of the purpose of the two techniques and how to use them, and then asked them to try the techniques in the context of correcting erroneous data in 2.5D maps. From the interviews after the test, we got many positive comments on the general user experience such as *easy to understand the topology on the occluded graph data.* The animation during *Repel Signification* was generally accepted, as some participants commented that it was *cute*, *friendly*, or *pleasant*, while one commented that it might be annoying that the animation always occurs. Expansion Interaction was also basically liked, as commented node selection was easy and smooth. Most of negative comments were about difficulties in selecting a edge error or its low visibility, even with the expansion. Some participants complained that the errors were hard to see when zoomed out.

In this study we presented novel techniques to visualize and edit occluded elements specified for 2.5D map data editing tasks. We designed *Repel Signification*, which signify and visualize the occluded components to support the user find them, and then we also designed *Expansion Interaction* to visualizes in-floor and across-floor connection relationships or overlaps relating to the occluded elements. Our future work includes investigating the fundamental performance through a target acquisition task, assessing the usability in more realistic tasks of correcting erroneous data in 2.5D indoor maps, and applying the techniques to touch-based devices.

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