

Power and sample-size calculations for trials that compare slopes over time: introducing the `slopepower` command

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Abstract

Trials of interventions that aim to slow disease progression may analyse a continuous outcome by comparing its change over time – its slope – between the treated and the untreated group using a linear mixed model. In order to perform a sample size calculation for such a trial, it is necessary to have estimates of the parameters that govern the between- and within-subject variability in the outcome, which are often unknown. The algebra needed for the sample size calculation can also be complex for such trial designs. We have written a new user-friendly Stata program, `slopepower`, that performs sample size or power calculations for trials that compare slope outcomes. The package is based on linear mixed model methodology, described for this setting by Frost, Kenward and Fox (“Optimizing the design of clinical trials where the outcome is a rate. Can estimating a baseline rate in a run-in period increase efficiency?”, *Statist Med* (2008) 27:3717–3731, DOI: 10.1002/sim.3280). In the first stage of this approach, `slopepower` obtains estimates of mean slopes, together with variances and covariances from a linear mixed model fitted to previously collected user-supplied data. In the second stage, these estimates are combined with user input about the target effectiveness of the treatment and design of the future trial in order to give an estimate of either a sample size or a statistical power. In this paper, we present the `slopepower` program, briefly explain the methodology behind it, and demonstrate how it can be used to help plan a trial and compare the sample sizes needed for different trial designs.

1. Introduction

Sample size is a critical design consideration when planning a randomised controlled trial (RCT). Given an estimate of the target treatment effect, a formula for the variance of the treatment effect (which will depend on the trial design and analysis model), and the acceptable type I and type II error rates, it is calculated with a simple algebraic formula [1]. However, for some designs and analysis models the algebra to obtain the formula for the treatment effect variance can be complex, and it can be difficult to derive reasonable guesses for the parameters that appear in that formula.

Consider a disease where progression can be measured by a continuous variable that is expected to deteriorate over time. Now consider an intervention whose aim is to slow that disease progression: we could use the continuous outcome as our trial outcome and see whether it responds to treatment over time. In such a trial, this outcome is typically recorded at participants’ baseline visits (prior to treatment allocation) and at least one follow-up visit with the aim of comparing randomised groups.

One way to analyse such an outcome is to use a linear mixed model (LMM) [2-5]. In the simple case of a single follow-up measure and no missing data, a properly specified LMM can also be expressed as a Generalised Least Squares model [6] and will give the same estimated treatment effect as ANCOVA, albeit with reported standard errors that are only asymptotically equal [6-8]. When there are multiple follow-up times, LMMs offer a flexible way of modelling the data which allows various assumptions to be made about the way the outcome changes over time. For example, it could be assumed that the outcome will change linearly over time in both groups and hence that the

treatment difference between the groups is proportional to time [6]. LMMs also provide a convenient way of handling missing data, provided that a missing at random assumption can be made [9].

Specifying the treatment effect variance formula from such a LMM for a sample size calculation requires knowledge of all of the parameters that govern between- and within-subject variability in outcomes, which are often unknown. In such situations, it is possible to use data from any relevant previously conducted longitudinal studies to estimate these parameters. We introduce a new package `slopepower` that translates a two-stage approach for estimating these parameters and performing sample size calculations [6, 10] into a user-friendly program, appropriate for planning two-arm parallel trials comparing slopes where the treatment is expected to slow disease progression by a constant amount throughout follow-up and where the outcome is expected to change linearly over time.

`slopepower` estimates sample size by first fitting a LMM to a user-supplied longitudinal dataset and extracting estimates of slopes and components of between- and within-person variability. It then combines these estimates with other user inputs, including the number and spacing of the visits planned, to calculate the required sample size for a proposed RCT.

In Section 2 we summarise existing methodology for estimating sample sizes for this design; in section 3 we describe the `slopepower` command; in section 4 we provide some examples of how to use `slopepower`; and in section 5 we give a short conclusion.

2. Methods

2.1. Future trial set-up and analysis method

It is important to base a sample size calculation on the model that will be used to analyse the trial. In this section, we therefore describe the sort of trial that `slopepower` could be applied to and the model that we assume will be used to analyse it. As described in Section 1, we consider a parallel-arm trial in which the outcome of interest is a continuous measurement of disease that is expected to change over time and to respond to treatment. We consider that the outcome will be measured at a baseline visit and at least one follow-up visit, which occur at fixed time points for all participants.

When analysing this outcome, we assume that it can be modelled as a linear change over time in the control group, with treatment acting to lessen that change proportionally over time. The analysis model can be written as follows:

$$y_{ij} = \beta_0 + \beta_1 t_j + \beta_2 g_i t_j + a_i + b_i t_j + \epsilon_{ij} \quad (1)$$

where y_{ij} is the outcome for person i at time point j , β_0 is the expected mean baseline measurement of the outcome in both arms, β_1 is the change in the outcome over time (slope) in the control group, t_j represents the times of the visits, β_2 is the treatment effect (i.e. the difference in slopes between the arms), g_i is an indicator which is 0 in the control group and 1 in the active group for the i^{th} person, a_i is a random person-level intercept, b_i is a random person-level slope and $\epsilon_{ij} \sim N[0, \sigma_\epsilon^2]$ is a normally distributed random error term. The person-level random effects are assumed to be distributed as follows:

$$\begin{pmatrix} a_i \\ b_i \end{pmatrix} \sim N \left[\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_a^2 & \sigma_{ab} \\ \sigma_{ab} & \sigma_b^2 \end{pmatrix} \right]$$

Note that in this model the baseline measure of the outcome, y_{i0} , is treated as a correlated outcome. We assume that randomisation is successful, so that there is no expectation of a difference between the two groups at baseline (i.e. at $t_0 = 0$), and estimate a single intercept for both arms. After baseline, it is assumed that the outcome changes linearly over time, and that the treatment effect is therefore also constant and linear over time. In this formulation, the treatment effect is defined as the difference between the slope in the treated arm compared to that in the untreated arm.

Once the analysis model is specified, the treatment effect and its variance and thus sample size requirements follow from the theory of linear mixed models [6]. A general formulation for a linear mixed model is

$$Y|u \sim N[X\beta + Zu; R] \text{ for } u \sim N[0; G] \quad (2)$$

where Y is the vector of outcome variables, X is the design matrix, β is the vector of fixed effects, Z is the design matrix for the random effects, u is the vector of random effects which are assumed to be distributed multivariate normally with mean 0 and covariance matrix G (note that this G is a matrix and shouldn't be confused with the group indicator g_i). Conditionally on the random effects, Y is assumed to have covariance matrix R .

Now let us rewrite our model in a form that is not conditional on the random effects u . Marginally, equation (2) implies that

$$Y \sim N[X\beta; \Sigma] \text{ where } \Sigma = R + ZGZ^T \quad (3)$$

Here Σ is the variance-covariance matrix for unconditional Y , and can be found from R , Z and G . Provided that there is a postulated fixed value for the variance-covariance matrix then

$$\hat{\beta} = (X^T \Sigma^{-1} X)^{-1} X^T \Sigma^{-1} Y \quad (4)$$

and

$$V(\hat{\beta}) = (X^T \Sigma^{-1} X)^{-1} \quad (5)$$

Equation (4) can be used to estimate the treatment effect, while equation (5) defines a variance-covariance matrix for the estimated fixed parameters that permits calculation of the standard error of the treatment effect.

In order to illustrate these equations, let us relate matrix equation (2) to our particular analysis model in equation (1) for the simple case of a two-person trial (one person per treatment group) with a baseline visit and two follow-up visits. In this case, we see that:

$$Y = \begin{pmatrix} y_{10} \\ y_{11} \\ y_{12} \\ y_{20} \\ y_{21} \\ y_{22} \end{pmatrix}; X = \begin{pmatrix} 1 & 0 & 0 \\ 1 & t_1 & 0 \\ 1 & t_2 & 0 \\ 1 & 0 & 0 \\ 1 & t_1 & t_1 \\ 1 & t_2 & t_2 \end{pmatrix}; \beta = \begin{pmatrix} \beta_0 \\ \beta_1 \\ \beta_2 \end{pmatrix}; Z = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 1 & t_1 & 0 & 0 \\ 1 & t_2 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & t_1 \\ 0 & 0 & 1 & t_2 \end{pmatrix}; u = \begin{pmatrix} a_1 \\ b_1 \\ a_2 \\ b_2 \end{pmatrix};$$

$$\mathbf{R} = \begin{pmatrix} \sigma_e^2 & 0 & 0 & 0 & 0 & 0 \\ 0 & \sigma_e^2 & 0 & 0 & 0 & 0 \\ 0 & 0 & \sigma_e^2 & 0 & 0 & 0 \\ 0 & 0 & 0 & \sigma_e^2 & 0 & 0 \\ 0 & 0 & 0 & 0 & \sigma_e^2 & 0 \\ 0 & 0 & 0 & 0 & 0 & \sigma_e^2 \end{pmatrix}; \mathbf{G} = \begin{pmatrix} \sigma_a^2 & \sigma_{ab} & 0 & 0 \\ \sigma_{ab} & \sigma_b^2 & 0 & 0 \\ 0 & 0 & \sigma_a^2 & \sigma_{ab} \\ 0 & 0 & \sigma_{ab} & \sigma_b^2 \end{pmatrix}$$

Σ from equation (3) therefore becomes a 6 x 6 matrix of form:

$$\begin{pmatrix} \Sigma^* & \mathbf{0} \\ \mathbf{0} & \Sigma^* \end{pmatrix};$$

where $\mathbf{0}$ is a 3 x 3 matrix of zeros and:

$$\Sigma^* = \begin{pmatrix} \sigma_a^2 + \sigma_e^2 & \sigma_a^2 + t_1\sigma_{ab} & \sigma_a^2 + t_2\sigma_{ab} \\ \sigma_a^2 + t_1\sigma_{ab} & \sigma_a^2 + 2t_1\sigma_{ab} + t_1^2\sigma_b^2 + \sigma_e^2 & \sigma_a^2 + (t_1 + t_2)\sigma_{ab} + t_1t_2\sigma_b^2 \\ \sigma_a^2 + t_2\sigma_{ab} & \sigma_a^2 + (t_1 + t_2)\sigma_{ab} + t_1t_2\sigma_b^2 & \sigma_a^2 + 2t_2\sigma_{ab} + t_2^2\sigma_b^2 + \sigma_e^2 \end{pmatrix}$$

and we can see that the algebra to obtain $V(\hat{\beta})$ from equation (5) is already fairly complex, even for this simple example. `slopepower` can perform the matrix calculations necessary to obtain $V(\hat{\beta})$ and hence the standard error for the estimated treatment effect, as we shall see in the next section.

2.2. Predicting a sample size for a future trial

Now that we have set up our trial design and analysis model, we can move on to how we would calculate a sample size for such a trial. For a sample size calculation, we need a formula for the variance of the treatment effect estimate, and we have shown how we can calculate this in the previous section. Since the matrices in equation (5) can get very large, we will use a simplifying trick – we shall first calculate the treatment effect standard error for a two-person trial s^* . Since the standard error for the treatment effect from a trial with N independent subjects in each arm is s^*/\sqrt{N} it follows from standard theory that the sample size required to identify a postulated treatment difference β_2 with statistical power $1 - \beta$ and two-sided significance level α is

$$N = \left[\frac{(z_{1-\alpha/2} + z_{1-\beta})s^*}{\beta_2} \right]^2 \quad (6)$$

Note that s^* will depend on the design matrix \mathbf{X} (which is itself dependent upon the number and spacing of the trial visits) and the variances and covariances from \mathbf{R} and \mathbf{G} ($\sigma_e^2, \sigma_a^2, \sigma_b^2$ and σ_{ab}). Generally, appropriate values for these variances and covariances will not be known a priori, but estimates for these quantities can be obtained by fitting an appropriate linear mixed model to a previously collected data set.

`slopepower` therefore estimates sample size in a two-stage process. In the first, it fits a linear mixed model to a user-supplied longitudinal dataset and extracts estimates of slopes and components of between- and within-person variability. In the second, it combines these estimates with other user inputs to calculate the required sample size for a proposed RCT, based on the analysis model given above in equation (1) and the sample size formula in equation (6).

2.3. Stage 1: slope and variance parameter estimation

`slopepower` uses Stata's `mixed` command with the restricted maximum likelihood (`reml`) option to fit a linear mixed model relating the outcome to time since study entry, using data supplied by the user. The data could be one of three different types:

1. Single group: dataset contains data from subjects with the disease of interest who are considered to be similar to the control group in the prospective trial. These may be subjects who are not receiving any treatment, for example, or are receiving standard of care. For simplicity, we shall refer to these subjects as untreated subjects. Such data could be from an observational study, or from the control arm of a previously conducted RCT.
2. Two group, observational: optionally, the data can also include subjects without the disease (healthy controls).
3. Two group, RCT: again optionally, the data can include subjects with the disease who are receiving an additional treatment, possibly the treatment of interest in the future RCT (treated subjects).

First let us consider a single group data set that contains only untreated subjects with the disease (situation 1 above). The outcomes y_{ij} for person i at occasion j are modelled as a linear function of time elapsed since baseline t_{ij} with random intercepts a_i , slopes b_i , and residual errors ϵ_{ij} :

$$y_{ij} = \beta'_0 + \beta'_1 t_{ij} + a_i + b_i t_{ij} + \epsilon_{ij} \quad (7)$$

$$\begin{pmatrix} a_i \\ b_i \end{pmatrix} \sim N \left(\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_a^2 & \sigma_{ab} \\ \sigma_{ab} & \sigma_b^2 \end{pmatrix} \right), \epsilon_{ij} \sim N(0, \sigma_\epsilon^2)$$

Note that we have marked the coefficients from the model in equation (7) with primes to distinguish them from the coefficients in the proposed analysis model for the future RCT from equation (1).

Note also that time is now indexed by i and j , since if the data are from an observational study then visit times might vary by participant. For each person, the baseline visit is at time zero: $t_{i0} = 0$, and `slopepower` will rescale the times in the data set if this is not the case.

The expected slope from the user-supplied data in equation (7) is β'_1 . This describes the expected change in the outcome per unit of time that would be seen without treatment in a person who has the disease under study. In this first stage, `slopepower` simply collects and stores the parameters from the model: β'_1 , σ_a^2 , σ_b^2 , σ_{ab} and σ_ϵ^2 , which will be used in stage 2 calculations.

If the supplied dataset also includes healthy controls (two group, observational data, situation 2) then parameters are estimated separately in each group, such that the healthy controls have their own intercept, slope over time, and variances and covariances. It is possible to have `slopepower` run this model leaving out the random slopes over time for healthy controls (i.e. neglecting σ_b^2 and σ_{ab} for healthy controls), since the variability over time in healthy controls can sometimes be very small, leading to convergence issues in a model that tries to estimate these parameters.

Under this scenario, `slopepower` will store the slope ($\beta'_{1,us}$), variances and covariances ($\sigma_a^2, \sigma_b^2, \sigma_{ab}, \sigma_\epsilon^2$) from the untreated subjects. It will also store the slope ($\beta'_{1,hc}$), only, from the healthy control group.

Finally, if the data set is from a previous RCT and includes treated subjects (two group, RCT data, situation 3), then the model in equation (1) is used. In this model both groups have the same intercept, since we expect the two groups to have the same mean at baseline under randomisation, but the slopes over time are allowed to differ. The variance parameters are constrained to be the same in the two groups.

In this final scenario, `slopepower` will store the difference between the slopes in the treated and untreated groups (β'_2) and the joint variances and covariances ($\sigma_a^2, \sigma_b^2, \sigma_{ab}, \sigma_\epsilon^2$).

2.4. Stage 2: treatment effect variance estimation, sample size calculation

In the second stage, `slopepower` assumes the trial under consideration will be analysed using the model in equation (1). `slopepower` builds Σ for a two-person trial using equation (3) and the estimated variance and covariance parameters obtained from the first stage ($\sigma_a^2, \sigma_b^2, \sigma_{ab}, \sigma_\epsilon^2$). It then calculates the standard error of the treatment effect for this two-person trial, s^* , by using equation (5). s^* depends on the design matrix X , which is specified by the user, who tells `slopepower` the number and spacing of the visits for the future trial. Once s^* is obtained, equation (6) is used to calculate the sample size.

In addition to s^* , equation (6) depends on the target treatment effect. The program allows three scenarios regarding the effectiveness of the treatment under study. In these scenarios, the treatment effect is defined as being:

1. towards no annual change, i.e. it will reduce the rate of (future) change by a certain proportion of the way to zero. Under this scenario, a 100% effective treatment is defined as one that would halt change, but not reverse it. Using single group data without healthy controls or trial data from unrelated interventions implies this scenario. In this situation, the target treatment effect used in the sample size calculation, β_2 , is calculated from the slope obtained from the user supplied data (β_1') and the user-supplied effectiveness, which we shall denote as e and which takes a value between 0 and 1:

$$\beta_2 = e \times \beta_1'$$

2. towards the slope observed in healthy controls, i.e. it will reduce the rate of change over-and-above that seen in a disease-free population (the 'excess' rate of change) by a certain proportion. Under this scenario, a 100% effective treatment would slow the change in subjects with the disease to the change observed in healthy controls, but would not halt or reverse it. Using two group observational data that includes healthy controls implies this scenario, and the target treatment effect in this case is calculated as:

$$\beta_2 = e \times (\beta_{1,us}' - \beta_{1,hc}')$$

where $\beta_{1,us}'$ is the slope of the untreated subjects and $\beta_{1,hc}'$ is the slope of the healthy controls obtained from the user specified data.

Note that the slope in the healthy controls could be interpreted as an upper limit on what is achievable with treatment, particularly when the outcome is expected to change over time even in healthy people. For example, say the outcome is a measure of cognitive decline in patients with Huntington's disease, and we know that even healthy people experience cognitive decline due to aging effects. Then even a very effective treatment for patients with Huntington's disease is unlikely to eliminate or reduce cognitive decline to a level below that of the aging effects.

3. equal to a previously observed treatment effect. For example, if a data set from a previously conducted trial of the same or a similar treatment is available (perhaps a phase II trial that is being used to plan a phase III trial), the treatment effect observed in the previous trial can be used. Using such trial data, along with the appropriate `usetrt` option (described in Section 3.2.2), implies this scenario. In this case, the target treatment effect is calculated as:

$$\beta_2 = \beta_2'$$

where β_2' is the difference in slopes between the treatment and control arms from the model fitted to the user supplied RCT data set.

Note that it is also possible to use a treatment effect that is proportional to the previously observed treatment effect in the previously conducted trial. This can be done by running the model under treatment effectiveness scenario 3 in order to obtain the sample size when

targeting the previously observed treatment effect, and then multiplying by the appropriate inflation factor (see example in Section 4.1.3).

`slopepower` will use the user-supplied effectiveness (or the previously observed treatment effect, if specified) to calculate the target treatment effect for the future trial. It will then combine this with s^* to calculate either the sample size or the power using equation (6).

The sample size calculated by `slopepower` thus depends upon the design matrix X (which is itself dependent upon the number and spacing of the trial visits) as well as the various components of variance and covariance that were estimated from the user-supplied data. These are assumed to be equal to what would be seen in a future trial setting.

Note that by fitting a model to data observed at discrete time points, `slopepower` can estimate the variance of the treatment effect for designs incorporating visits at any time points, including ones not in the original study. Trialists can use this flexibility to explore the sample size implications for a range of designs that differ in length, number and timing of interim visits and/or dropout patterns. We illustrate this in Section 4.2.

2.5. Sample size adjustment for trial dropouts

To compensate for individuals who withdraw early from the trial, `slopepower` can optionally adjust the required sample size using a pattern-mixture approach as advocated by Dawson and Lagakos [11,12] and described by Frost and colleagues [6]. This approach is (appropriately) less conservative than up-scaling the estimated sample size according to the anticipated proportion of individuals who reach the final visit. This is appropriate when interim data will be used to estimate the treatment effect, as is the case when using a mixed model such as that in equation (1) to analyse the trial.

In brief, `slopepower` assumes that individuals will be separated into strata according to dropout patterns. The approach first estimates for each such stratum the necessary sample size in the hypothetical situation that all individuals are in that stratum. The overall sample size is computed as the reciprocal of the weighted mean of the reciprocals of these strata-specific sample sizes, with the weights equal to the proportions of individuals anticipated to have each missing data pattern. Note that `slopepower` allows for missing data due to trial dropout, but not for other patterns such as missed visits that result in intermittent missing values during follow-up.

2.6. Some notes of caution

It is important that the data set used for the first stage of model fitting is from a population that is sufficiently similar to that in the proposed trial that we can generalise the estimates of the variance parameters to the planned RCT. In practice, that might mean that similar inclusion criteria are used in the previous data set to those proposed in the future trial, and that the untreated subjects suffer from a similar severity of disease to that expected in the participants of the planned trial at baseline. It may be that no such data set exists, and in such a case it might be necessary to collect some data in a pilot study.

Note that, as always, variances and covariances will be estimated more precisely given more people and time points in the data set. Users should proceed with caution, especially if they have a small data set, and be aware that their sample size estimates will contain uncertainty due to the estimation of the variance parameters in the first stage. `slopepower` can be run with Stata's `bootstrap` prefix in order to obtain a 95% CI for a sample size estimate, although the user should be sure to take the structure of the data into account when doing so. Care should also be taken when bootstrapping small datasets, particularly those with outlying values, as the coverage of a

bootstrap confidence interval might then not be close to its nominal value. In addition, if the estimated slope in the user-supplied data set is not large relative to its standard error (as a rule of thumb we recommend that the ratio of the magnitude of the estimate to its slope should be greater than 2.5), it is possible that the bootstrap samples will yield estimates of the mean slope that are both negative and positive, meaning that some of the bootstrap samples will relate to trials that are trying to reduce a positive slope whilst others will relate to trials that are trying to reduce the magnitude of a negative slope, hence rendering the confidence interval meaningless. Such cases should, however, be unlikely, since if a trial is being contemplated to reduce a slope then there should be strong evidence of a trend over time such that the estimated slope is substantially larger than its standard error in the user-supplied data set. An example of how `bootstrap` can be used with `slopepower` is given in section 4.1.2.

As with any statistical model it is possible to make out-of-sample predictions. `slopepower` does not give a warning when estimating sample sizes for trials of duration longer than the maximum length of follow-up observed in the given data, so users should be aware of the assumptions that are made when doing this. Similarly, `slopepower` interpolates between time-points. This is a necessary assumption to make in order to be able to consider trial designs with visit spacing that differs from the original data set, but users should be aware that it is assumed that the model holds across the time scale of interest.

Also note that, other than subject-specific random effects, `slopepower` has no capability to model dependency between observations, such as centre- or visit-specific effects. This implies that, conditional on subject, observations are assumed to be independent.

3. The `slopepower` command

The syntax of `slopepower` is as follows:

```
slopepower depvar [if] [in] , subject(varname) time(varname)
schedule(numlist) [obs nocontrols rct casecon(varname)
treat(varname) dropouts(numlist) scale(#) alpha(#) power(#) n(#)
effectiveness(#) usetrtr iterate(#) nocontvar]
```

3.1. Description

`slopepower` will calculate sample size or power for trials where the outcome is a slope, using a two-stage approach. In the first stage, `slopepower` uses data in memory (provided by the user) to estimate the necessary slopes, variances and covariances. In the second stage it uses these estimates, along with user-specified information, to calculate a sample size or power.

The user-provided dataset can be of three basic types as described in Section 2.3: containing subjects with the disease who are untreated (or minimally treated, for example receiving standard of care) only, containing untreated subjects with the disease and healthy controls, or a previous RCT containing subjects who are untreated and subjects who are treated. In all cases, the data should contain repeated measurements of the outcome in long format (see `reshape` for more details). A linear mixed model is run (using `mixed`) on the data in memory to estimate the relevant parameters. The data in memory are not altered by `slopepower`.

3.2. Options

3.2.1. Options for data in memory

`subject (varname)` is the unique identifier for participants in the user-supplied data set

`time (varname)` is the time variable of visits in the dataset. This can be in any units (eg days, months, years). It is assumed to be time since start of observation for each individual. If it is not (for instance if it is an actual calendar date) `slopepower` will issue a warning and rescale it accordingly.

`obs` and `rct` tell Stata the nature of the data in memory. `obs` should generally be used for observational data, and `rct` for previously collected trial data (with an exception mentioned below). Exactly one of `obs` and `rct` must be specified.

`nocontrols` should be used with `obs` if all the subjects in your observational data have the condition of interest (i.e. if there are no healthy controls).

`casecon (varname)` specifies the variable used to identify cases in observational data; it can only be used with `obs`. It must be a binary 0/1 variable, with cases coded as 1.

`treat (varname)` specifies the treatment variable when you are using RCT data; it can only be specified with the `rct` option. It must be a binary 0/1 variable, with the experimental group coded as 1.

3.2.2. Options for planned trial

`schedule (numlist)` specifies the visit times for the proposed trial. A baseline visit at time 0 is assumed; this list should describe subsequent visits, in whole number units of time. The default is to use the same time unit as the time variable in the dataset. To use a different timescale, specify how many time units make one `schedule` unit in the `scale` option.

`dropouts (numlist)` specifies the estimated proportion of dropouts you expect at each study visit. It must correspond exactly to the schedule list. Each number in the list is a proportion between 0 and 1; this is the fraction of subjects (of those who start the trial) you estimate will fail to attend that visit. We follow the pattern mixture method of Dawson and Lagakos (see section 2.5).

`scale (#)` specifies the ratio between the time and visit timescales. For instance, if the `time` variable in your dataset is in days, and you wish to have visits annually for three years, you would specify `scale(365)` and `schedule(1 2 3)`.

`alpha (#)` sets the significance level (also known as Type I error rate) to be used in the planned study. The default is `alpha(0.05)`.

`power (#)` sets the power for the planned study. The default is `power(0.8)`. This option is required to compute the sample size.

`n (#)` specifies the total number of participants who will be in the trial. If an odd number is given, $n - 1$ will be used to allow equal numbers per arm. This option is required to compute the power. Only one of `power` and `n` may be specified.

`effectiveness (#)` and `usetrt` specify the effect size you would like to be able to detect in the future trial. `effectiveness` specifies this effect size as a proportion of the difference between cases and healthy controls in the observational data in memory. If RCT data, or observational data with no healthy controls, are used `effectiveness` is a proportion of the difference towards a slope of 0. This must be a number between 0 and 1; the default value is 0.25.

`usetrt` specifies that, when RCT data is used, the planned study is targeting the same effect size as observed in the previous data set. You can only specify one of `effectiveness` and `usetrt`.

3.2.3. Model options

`iterate(#)` is used as an option in the `mixed` command, which specifies the maximum number of iterations allowed in the mixed model.

`nocontvar` specifies that the mixed model should not estimate a random slopes variance parameter or the covariance between random slopes and intercepts for healthy controls. This is only applicable when you are using observational data with healthy controls. Ignoring this variance and covariance may help the model to converge.

4. Examples

4.1. How to use the code

In this section, we use simulated data to illustrate the options described above. The three examples given cover the three types of data which can be used with `slopepower`: single group data (with only untreated subjects); two group, observational (with untreated subjects and healthy controls); and two group, RCT (treated and untreated subjects).

These example datasets together contain three groups of people:

- a. People with Huntington’s Disease (HD), who are receiving standard of care (untreated subjects)
- b. People without HD (or the genetic mutation which leads to it) (healthy controls)
- c. People with HD, who are being treated as part of a trial (treated subjects)

Section 4.1.1 describes the situation when you have a dataset containing only people from group (a). Section 4.1.2 describes a dataset consisting of people from groups (a) and (b), and Section 4.1.3 is for a dataset consisting of groups (a) and (c).

In all datasets, we have assumed that the “cases” (or untreated subjects) are people with HD, a neurodegenerative disorder in which cognitive functioning typically declines during disease progression. The outcome of interest is their score on the Symbol Digits Modalities Test [13], a measure of cognitive function taking integer values between 0 and 110 with higher scores indicating better function. We have not simulated any missing data. In all cases the data are in long format, ready for use with `slopepower`.

4.1.1. Single group data with untreated subjects only

We have simulated three years of data on 200 people with HD, with measurements recorded each year; the visit variable indicates the year of follow-up. Values for SDMT are simulated according to the model in equation (7) using parameter values of $\beta'_0 = 34$, $\beta'_1 = -1.8$, $\sigma_a^2 = 100$, $\sigma_b^2 = 2$, $\sigma_{ab} = 5$ and $\sigma_\epsilon^2 = 10$. Outcome values are then truncated at zero and rounded to the nearest integer. Code for generating the data is given in the appendix. Data for the first two participants are shown below:

```
+-----+
| id  visit  sdmt |
+-----+
|  1     0    41 |
|  1     1    33 |
|  1     2    25 |
|  1     3    30 |
```

2	0	16
2	1	14
2	2	13
2	3	6

We first show the syntax to plan an RCT with annual visits over two years, assuming no dropouts, with 80% power to detect a treatment effect that will eliminate one-third of the slope. Note that here the assumed effectiveness is towards “no annual change” or a slope of zero. The `obs` option identifies the data in memory as being observational (although note that it would be possible to use a data set containing only the untreated arm from an RCT with this option), and, with no healthy controls in the dataset, we use the `nocontrols` option. The default values of 5% Type I error and 80% power are used.

```
. slopepower sdmt , schedule(1 2) subject(id) time(visit) obs nocontrol
effectiveness(0.33)
```

Data characteristics:

```
Number of observations in model = 800
Participants in model = 200
Slope of cases = -1.672
```

Parameters for planned study:

```
alpha = 0.050
power = 0.800
effectiveness = 0.330
target treatment difference in slopes = 0.552
number of follow-up visits = 2
schedule (and dropouts) : 1, 2
scale = 1
```

Estimated sample size:

```
N = 712
N per arm = 356
```

This shows that that a total sample size of 712 will be required for the planned trial. The first section of the output shows three results from the linear model run on the data in memory: the number of observations and subjects that were included in the model, and the estimated slope from the data. The remaining output confirms the user-contributed parameters, or the defaults used if they were not specified, and gives the target treatment effect that `slopepower` calculates from the model slope estimates and the user-inputted effectiveness: this is β_2 in equation (6). Finally, `slopepower` gives the estimated sample size both as a total and per arm.

Visits do not have to be scheduled at regular intervals. If you wish to extend the above trial to five years, with no additional interim visits you would specify the command below. However, note that this is extending the estimates out of the initial sample duration. Here we have also assumed that 10% of participants would be lost to follow-up between the visit at year two and the final visit.

```
. slopepower sdmt , schedule(1 2 5) subject(id) time(visit) obs nocontrol
effectiveness(0.33) dropouts(0 0 0.1)
```

Data characteristics:

```
Number of observations in model = 800
Participants in model = 200
Slope of cases = -1.672
```

Parameters for planned study:

```
alpha = 0.050
power = 0.800
effectiveness = 0.330
target treatment difference in slopes = 0.552
number of follow-up visits = 3
schedule (and dropouts) : 1 (0), 2 (0), 5 (0.1)
scale = 1
```

Estimated sample size:

```
N = 328
N per arm = 164
```

Here the sample size is reduced due to the extended follow-up, despite the loss to follow-up, which is shown as a proportion in brackets after each visit in the schedule list.

If you wish to schedule visits every six months, you must use the scale option to indicate that half a unit in the observed timescale is equivalent to one unit in the RCT timescale. Hence the timescale specified in the command below is in increments of six months, and the trial is scheduled to last two years.

```
. slopepower sdmt , schedule(1 2 3 4) scale(0.5) subject(id) time(visit)
obs nocontrol effectiveness(0.33)
```

Data characteristics:

```
Number of observations in model = 800
Participants in model = 200
Slope of cases = -0.836
```

Parameters for planned study:

```
alpha = 0.050
power = 0.800
effectiveness = 0.330
target treatment difference in slopes = 0.276
number of follow-up visits = 4
schedule (and dropouts) : 1, 2, 3, 4
scale = .5
```

Estimated sample size:

```
N = 620
N per arm = 310
```

Again, the sample size is slightly reduced compared to the first example, due to an increase in efficiency gained from the interim visits. Also note that the slope observed in the data has halved; this is because it is reported in the units of the planned trial, so here it relates to a difference per six months (rather than per year as in the earlier examples).

4.1.2. Observational data with cases and healthy controls

Here we have simulated 250 people with HD and 250 without, with dates of observation used rather than visit number. For cases (or untreated subjects), the SDMT score was generated as above. For controls, we assumed a mean at baseline of 53 and an increasing average annual change (due to a practice effect) of 0.9. Variance and covariance parameters of $\sigma_a^2 = 75$, $\sigma_b^2 = 1$, $\sigma_{ab} = 1$ and $\sigma_\epsilon^2 = 10$ were used for healthy controls. Data for the first control and the first case are shown below:

```
+-----+
| id           case           vdate    sdmt |
+-----+
```

```

| 1 Healthy control 11jul2009 40 |
| 1 Healthy control 21jun2010 46 |
| 1 Healthy control 06jul2011 41 |
| 1 Healthy control 06may2012 45 |
|-----|
| 251 Case 06jun2009 35 |
| 251 Case 13aug2010 34 |
| 251 Case 31aug2011 36 |
| 251 Case 05sep2012 39 |
+-----+

```

Note that `case` is a labelled numeric variable, and takes value 0 for healthy controls and 1 for cases.

Since we now have healthy controls in our data we drop the `nocontrols` option, and instead use `case` to tell `slopepower` which variable identifies the untreated subjects in our data set. Because the time variable is a date (recorded in days), and we wish to specify our RCT schedule in years, we use the `scale` option.

```

. slopepower sdmt , schedule(1 2) scale(365) subject(id) time(vdate) obs
case(case) effectiveness(0.33)
WARNING: time variable did not start at zero for all participants. Times
have been adjusted such that the first visit for each person is treated as
time zero.

```

Data characteristics:

```

number of observations in model = 2000
number of participants in model = 500
observed difference in slopes = -2.690
slope of cases = -1.715
slope of healthy controls = 0.975

```

Parameters for planned study:

```

alpha = 0.050
power = 0.800
effectiveness = 0.330
target treatment difference in slopes = 0.888
number of follow-up visits = 2
schedule (and dropouts) : 1, 2
scale = 365

```

Estimated sample size:

```

N = 296
N per arm = 148

```

The first thing to note is that because the time variable is a date, `slopepower` has issued a warning to let you know that it has been transformed in the model so that the earliest date for each individual is at time zero – this is necessary to ensure the intercept is estimated at baseline and that the covariance between the random slopes and intercepts is correctly estimated. Note that now there are two slopes reported in the output – one for the cases and one for the healthy controls. The effectiveness is now applied to the difference between these two slopes, which is also provided in the output.

The output shows that a total sample size of 296 will be required for the planned trial. The decreased sample size compared to that in the previous section is partly because here we have an estimate for the slope of healthy individuals, so instead of relating our effectiveness to no change over time (a slope of zero) we relate it to the difference between the slope in untreated subjects and

that in healthy controls. Hence the target treatment effect is larger here than above, even though an effectiveness of 0.33 was specified both times, since the healthy controls have a positive slope.

Let us suppose that we are interested in obtaining a bias-corrected and accelerated bootstrap confidence interval for this predicted sample size. We can do this by using the following command:

```
. bootstrap r(sampsize), cluster(id) idcluster(id2) strata(case) rep(2000)
seed(123) bca jack(n(r(obs_in_model))): slopepower sdmt, schedule(1 2) scale(365)
subject(id) time(vdate) obs case(case) effectiveness(0.33)
```

WARNING: time variable did not start at zero for all participants. Times have been adjusted such that the first visit for each person is treated as time zero.

Warning: Because slopepower is not an estimation command or does not set e(sample), bootstrap has no way to determine which observations are used in calculating the statistics and so assumes that all observations are used. This means that no observations will be excluded from the resampling because of missing values or other reasons.

If the assumption is not true, press Break, save the data, and drop the observations that are to be excluded. Be sure that the dataset in memory contains only the relevant data.

(running slopepower on estimation sample)

WARNING: time variable did not start at zero for all participants. Times have been adjusted such that the first visit for each person is treated as time zero.

```
Jackknife replications (500)
-----+--- 1 -----+--- 2 -----+--- 3 -----+--- 4 -----+--- 5
..... 50
[some output suppressed]
..... 500
```

```
Bootstrap replications (2000)
-----+--- 1 -----+--- 2 -----+--- 3 -----+--- 4 -----+--- 5
..... 50
[some output suppressed]
..... 2000
```

Bootstrap results

```
Number of strata = 2 Number of obs = 2,000
Replications = 2,000
```

```
command: slopepower sdmt, schedule(1 2) scale(365) subject(id) time(vdate)
obs case(case) effectiveness(0.33)
_bs_1: r(sampsize)
```

(Replications based on 500 clusters in id)

	Observed	Bootstrap			Normal-based	
	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
_bs_1	296	30.0739	9.84	0.000	237.0562	354.9438

```
. estat bootstrap, bca
```

Bootstrap results

```
Number of strata = 2 Number of obs = 2,000
Replications = 2000
```

```
command: slopepower sdmt, schedule(1 2) scale(365) subject(id) time(vdate)
obs case(case) effectiveness(0.33)
_bs_1: r(sampsize)
```

(Replications based on 500 clusters in id)

	Observed Coef.	Bias	Bootstrap Std. Err.	[95% Conf. Interval]
_bs_1	296	-17.738	30.073902	262 402 (BCa)

There are several important things to note about the bootstrap command. First, we have specified that we require bootstrapped confidence intervals for the sample size, which is saved by `slopepower` as `r(sampsize)`. Second, we need to use the `cluster` option so that people, rather than individual data points, are sampled from the data set. We also need to use the `idcluster` option, with a new identifier called `id2`, so that if one person appears twice in a bootstrapped sample they are treated as two separate people rather than as one person with twice as many data points than as in the data itself. Third, we need the option `strata` so that cases and healthy controls are sampled separately. Finally, because we want a bias-corrected and accelerated CI, we have to tell Stata where `slopepower` saves the number of observations in each model using the `jack(n(r(obs_in_model)))` option. Opting for a bias-corrected and accelerated confidence interval is recommended because the distribution of estimated sample sizes across the bootstrap samples is likely to be skewed. We can see in this example that the CI extends substantially further above the central value (up to a sample size of 402) than it does below it (down to a sample size of 262).

It is also possible to calculate the power for a specified sample size by using the `n()` option instead of `power()`. Note that this `n` refers to the total sample size, and assumes a 1:1 ratio between the two treatment groups. Here we also assume a dropout rate of 5% per year of those who start the trial.

```
. slopepower sdmt , schedule(1 2) scale(365) subject(id) time(vdate) obs  
case(case) effectiveness(0.33) n(200) dropouts(0.05 0.05)  
WARNING: time variable did not start at zero for all participants. Times  
have been adjusted such that the first visit for each person is treated as  
time zero.
```

Data characteristics:

```
number of observations in model = 2000  
number of participants in model = 500  
observed difference in slopes = -2.690  
slope of cases = -1.715  
slope of healthy controls = 0.975
```

Parameters for planned study:

```
alpha = 0.050  
specified N = 200  
actual N = 200  
N per arm = 100  
effectiveness = 0.330  
target treatment difference in slopes = 0.888  
number of follow-up visits = 2  
schedule (and dropouts) = 1 (0.05), 2 (0.05)  
scale = 365
```

Estimated power:

```
power = 0.597
```

The estimated power is 60%. The other main difference in output here is that two values for the total N are given: the value specified by the user, and the value actually used in the power calculation, which is either n , or $n-1$ if the user specified an odd number.

4.1.3. RCT data with treated and untreated groups

The simulated RCT data contains 75 people who received treatment and 75 who did not receive active treatment. In this dataset, the outcome was generated from a model with an intercept of 34, a slope in the untreated arm of -1.8 units/year, a slope in the treated arm of -0.8 units/year, and variance and covariance parameters as in section 4.1.1.

Example data from one participant in each arm is shown here:

```
+-----+
| id      treat  visit  sdmt |
+-----+
|  1  Placebo    0     35 |
|  1  Placebo   .5     36 |
|  1  Placebo    2     34 |
+-----+
| 76    Treat    0     29 |
| 76    Treat   .5     33 |
| 76    Treat    2     35 |
+-----+
```

Again, note that `treat` is a labelled numeric variable, where “Placebo” (untreated arm) takes value 0 and “Treat” (treated arm) takes value 1.

If the aim of the planned study is to be able to detect the same effect size as in the previous RCT, then the `usetrt` option should be used. Here, we show the syntax to produce a sample size estimate for a three-year study with one interim visit at year two, and loss to follow-up of 10% per year of those who start the trial. Note that we now use the `rct` option instead of `obs`.

```
. slopepower sdmt , schedule(2 3) subject(id) time(visit) rct treat(treat)
usetrt dropout(0.2 0.1)
```

Data characteristics:

```
number of observations in model = 450
number of participants in model = 150
observed difference in slopes = -0.747
slope of control arm = -1.852
slope of experimental arm = -1.104
```

Parameters for planned study:

```
alpha = 0.050
power = 0.800
effectiveness = .
target treatment difference in slopes = 0.747
number of follow-up visits = 2
schedule (and dropouts) : 2 (0.2), 3 (0.1)
scale = 1
```

Estimated sample size:

```
N = 318
N per arm = 159
```

Here, we see that a sample size of 318 is required to be able to detect a 0.75 units per year change in annual decline that was seen in the previous RCT.

Suppose that the previous RCT is a pilot study or phase II trial, and that the investigators suspect that due to its small size the treatment effect might have been overestimated. They may wish to plan the future RCT such that it has power to detect a treatment effect that is 50% of that observed previously. To do this we can multiply the sample size above by 4 (i.e. one over 0.5 squared), so we

would need a sample size of 1272. More generally, note that if we want a sample size for a target treatment effect that is p times that observed in the previous trial, N_p , we need to multiply the N that uses the previously observed treatment effect (318 in this example) by p^{-2} . This follows from equation 6:

$$N_p = \left[\frac{(z_{1-\alpha/2} + z_{1-\beta})s^*}{p\beta_2} \right]^2 = \frac{1}{p^2} \left[\frac{(z_{1-\alpha/2} + z_{1-\beta})s^*}{\beta_2} \right]^2 = \frac{1}{p^2} N$$

Note that if we had data from a previous RCT that was trialling a completely different treatment to that under consideration in the future trial, we might have decided to use only the untreated arm as our dataset and used the options for a single group of untreated subjects as shown in section 4.1.1.

4.2. Exploring future trial designs with `slopepower`

`slopepower` can be used to explore sample sizes under a variety of scenarios, which may be of use when planning the future trial. Here we suppose we are planning a three-year study, using the observational dataset described in section 4.1.1, and targeting the same 33% effectiveness. We assume that we will be able to recruit a total of 450 participants, and report the estimated power for a number of different scenarios that explore different patterns of follow-up visits and dropouts. The code to obtain these results is given in the Appendix.

Planned trial design	Dropouts	Power
Baseline and final visit (three years) only	None	79.8%
Annual follow-up visits	None	81.7%
Six-monthly follow-up visits	None	86.5%
Baseline and final visit (three years) only	5% per year	73.2%
Annual follow-up visits	5% per year	77.1%
Six-monthly follow-up visits	5% per year	82.8%
Baseline and final visit (three years) only	10% per year	64.8%
Annual follow-up visits	10% per year	71.6%
Six-monthly follow-up visits	10% per year	78.3%

Table 1. Estimated power for different trial designs and dropout scenarios

As can be seen from Table 1, adding extra follow-up visits increases the power. For example, when there are no dropouts, the power increases from around 80% with a single follow-up visit to almost 87% with six-monthly follow-up visits. As the anticipated rate of dropouts increases, the trial designs that include extra follow-up visits become increasingly efficient, as they allow data collected at interim visits to be used in the analysis. Note that in this simulated example when 10% of participants are expected to be lost each year, adding six-monthly visits recovers information to the extent that it achieves nearly the same power as a trial with a single follow-up visit with no dropouts.

5. Conclusion

We have presented a new Stata program, `slopepower`, that can be used to perform sample size or power calculations for trials that compare rates of change in an outcome (the slope) over time.

`slopepower` can be used for any continuous clinical trial outcome that is expected to change at a constant rate over time and where a treatment is expected to slow that rate. This might include continuous outcomes such as log10-transformed total kidney volume [14], disease severity scores such as the Amyotrophic Lateral Sclerosis Functional Rating Scale-Revised [15], body mass index [16],

carotid intima-media thickness [17], biomarkers such as log₁₀-transformed C-reactive protein degraded by matrix metalloproteinases 1 and 8 [18], or variables measuring lung function such as forced expiratory volume [19] or forced vital capacity [20].

The package is based on linear mixed model methodology, described for this setting by Frost *et al.* [6], and requires a user-supplied data set containing longitudinal data on a similar population to that expected in the future trial. In the first stage of this approach, `slopepower` obtains estimates of the mean rate of change in the outcome, together with variances and covariances, from a linear mixed model fitted to user-supplied data. In the second stage, these estimates are combined with user input on the target effectiveness of the treatment and design of the future trial to give an estimate of either a sample size for, or the statistical power of, the future trial. This program provides, to our knowledge for the first time, a convenient way to calculate such estimates for trials with repeated measures that aim to alter rates of change in an outcome.

6. Acknowledgements

We acknowledge the contribution of Mike Kenward to developing the approach to sample size calculation that `slopepower` utilises.

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7. References

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8. Appendix

Here we provide the code used to simulate example data sets used in section 4. All data was generated using Stata 16.

```
* Data for example 4.1.1: single group data, untreated subjects only
set seed 5221

* create data set of 200 people
clear
set obs 200
gen id = _n

* draw random person intercepts and slopes
drawnorm a b, cov(100, 5 \ 5, 2)

* create more visits
```

```

expand 4
bys id: gen visit = _n - 1

* generate sdmt from model in equation (7)
gen sdmt = 34 -1.8 * visit + a + b * visit + rnormal(0, 10^0.5)
su sdmt

count if sdmt < 0

* truncate at zero and round to nearest integer to create a score like sdmt
replace sdmt = round(sdmt)
replace sdmt = 0 if sdmt < 0

* drop person intercept and slope which are no longer needed
drop a b

save slpower1, replace

* list of two ids from paper
list if id == 1 | id == 2, sep(4) noobs

* slopepower commands from paper
slopepower sdmt , schedule(1 2) subject(id) time(visit) obs nocontrol ///
    effectiveness(0.33)

slopepower sdmt , schedule(1 2 5) subject(id) time(visit) obs nocontrol ///
    effectiveness(0.33) dropouts(0 0 0.1)

slopepower sdmt , schedule(1 2 3 4) scale(0.5) subject(id) time(visit) ///
    obs nocontrol effectiveness(0.33)

* Data for example 4.1.2: two group data, observational, untreated subjects and
*healthy controls
set seed 1146

* create data set of 500 people, with 250 untreated subjects and 250 healthy
*controls
clear
set obs 500
gen id = _n
gen case = (_n > `=_N/2')

* draw two sets of random intercepts and slopes and use a, b for cases and c, d for
*controls
drawnorm a b, cov(100, 5 \ 5, 2)
drawnorm c d, cov(75, 1 \ 1, 1)

* create more visits
expand 4
bys id: gen visit = _n - 1

* generate sdmt from model in equation (7)
gen sdmt = 34 - 1.8 * visit + a + b * visit + rnormal(0, 10^0.5) if case == 1
replace sdmt = 53 + 0.9 * visit + c + d * visit + rnormal(0, 10^0.5) if case == 0
su sdmt

count if sdmt < 0

* truncate at zero and round to nearest integer to create a score like sdmt
replace sdmt = round(sdmt)
replace sdmt = 0 if sdmt < 0

* generate visit dates that vary for each individual
gen vdate = (visit * 365) + date("5 July 2009" , "DMY")
replace vdate = vdate + int(rnormal(0, 50))

```

```

format vdate %td

* drop visit, person intercept and slope which are no longer needed
drop visit a b c d

* label case variable
lab def case_lab 0 "Healthy control" 1 "Case"
lab val case case_lab

order id case vdate sdmt

save slpower2, replace

* list of two ids from paper
list if id == 1 | id == 251, sep(4) noobs

* slopepower commands from paper
slopepower sdmt , schedule(1 2) scale(365) subject(id) time(vdate) ///
    obs case(case) effectiveness(0.33)

bootstrap r(sampsize), cluster(id) idcluster(id2) strata(case) rep(2000) ///
    seed(123) bca jack(n(r(obs_in_model))): slopepower sdmt, schedule(1 2) ///
    scale(365) subject(id) time(vdate) obs case(case) effectiveness(0.33)
estat bootstrap, bca

slopepower sdmt , schedule(1 2) scale(365) subject(id) time(vdate) ///
    obs case(case) effectiveness(0.33) n(200) dropouts(0.05 0.05)

* Data for example 4.1.3: two group, rct, untreated subjects (cases) and treated
*subjects
set seed 1021

* create data set of 150 people, with 75 in each treatment arm
clear
set obs 150
gen id = _n
gen treat = (_n > `=_N/2')

* draw random person intercepts and slopes
drawnorm a b, cov(100, 5 \ 5, 2)

* create more visits
expand 3
bys id: gen visit = _n - 1
replace visit = 0.5 if visit == 1

* generate sdmt from model in equation (7)
gen sdmt = 34 - 1.8 * visit + 1 * treat * visit + a + b * visit + rnormal(0,
10^0.5)

replace sdmt = round(sdmt)

* label treatment variable
lab def treat_lab 0 "Placebo" 1 "Treat"
lab val treat treat_lab

* drop person intercept and slope which are no longer needed
drop a b

save slpower3, replace

```

```

* list of two ids from paper
list if id == 1 | id == 76, sep(3) noobs

* slopepower commands from paper
slopepower sdmt , schedule(2 3) subject(id) time(visit) rct treat(treat) ///
    usestrt dropout(0.2 0.1)

*****
* commands to produce Table 1
*

* use same dataset as first example
use slpower1, clear

* no dropout
slopepower sdmt , schedule(3) subject(id) time(visit) obs nocontrol ///
    effectiveness(0.33) n(450)
slopepower sdmt , schedule(1 2 3) subject(id) time(visit) obs nocontrol ///
    effectiveness(0.33) n(450)
slopepower sdmt , schedule(1 2 3 4 5 6) scale(0.5) subject(id) time(visit) ///
    obs nocontrol effectiveness(0.33) n(450)

* 5% dropout per year = 15% over 3 years
slopepower sdmt , schedule(3) subject(id) time(visit) obs nocontrol ///
    effectiveness(0.33) n(450) dropout(0.15)
slopepower sdmt , schedule(1 2 3) subject(id) time(visit) obs nocontrol ///
    effectiveness(0.33) n(450) dropout(0.05 0.05 0.05)
slopepower sdmt , schedule(1 2 3 4 5 6) scale(0.5) subject(id) time(visit) ///
    obs nocontrol effectiveness(0.33) n(450) ///
    dropout(0.025 0.025 0.025 0.025 0.025 0.025)

* 10% dropout
slopepower sdmt , schedule(3) subject(id) time(visit) obs nocontrol ///
    effectiveness(0.33) n(450) dropout(0.3)
slopepower sdmt , schedule(1 2 3) subject(id) time(visit) obs nocontrol ///
    effectiveness(0.33) n(450) dropout(0.1 0.1 0.1)
slopepower sdmt , schedule(1 2 3 4 5 6) scale(0.5) subject(id) time(visit) ///
    obs nocontrol effectiveness(0.33) n(450) ///
    dropout(0.05 0.05 0.05 0.05 0.05 0.05)

```