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The H-ternary line code power spectral density modelling investigation

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Keywords

Ternary, Line, Code, Power, Spectral, Density, Modelling, Investigation

Disciplines

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The H-Ternary Line Code Power Spectral Density Modelling Investigation

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Abstract- *The power spectral density of the H-ternary line code is investigated in this paper. Accurate simulation results are extracted from a simulation model that generates and encodes very long P-N binary sequence. The simulation results are compared with that of the theoretical results obtained from the analytical model. Both results almost fit with each other except for very low frequency components where the simulation results drift slightly. This deviation is a result of the fact that the simulation model is able to generate more realistic data sequence that mimics real-world data.*

Keywords- Line codes Data transmission Power spectral density Telecommunication networks Simulation and Modelling

I INTRODUCTION

Coding is the technique that is used in many telecommunication applications for the purpose of data transmission and storage. The encoding principle is based on either adding or removing redundant bits to/from the original binary data. A variant form of coding to restructure the original binary pulse shape is also available. The latter is mainly used in applications where transmission or storage of data are required. The restructuring process is needed for the purpose of matching the encoded signal to the transmission storage media.

Line codes have many desirable properties that make them attractive for certain applications. These desirable features include small power spectral density bandwidth with no dc content frequent changes in signal level and hence adequate time information content for clock recovery and hence ease of transmitter receiver combination synchronisation error

detection and correction capability and finally easy encoding and decoding methods and hence simple hardware implementation and cost effectiveness.

Line coding has a generic form that is a multi level signal code. Special cases can be obtained for binary ternary and quaternary line codes. For binary ternary and quaternary codes; two three and four levels are used respectively to represent the code signal. Current applications of line codes are enormous in data transmission networks and in recording and storage of information systems. The applications include local and wide area networks both wireless and wire connected and the new technology of the digital subscriber loops networks. Further information about line codes classifications properties and their applications can be sought from [4].

In this paper a simulation model for the H ternary line is given and compared with the analytical model. The next section provides a description of the procedure for how a binary sequence is encoded to an H ternary line code and then decoded back to its original state. A review of the mathematical model of the power spectral density (PSD) of the new line code together with its counterparts is given in section three. Section four is devoted to a description of the simulation model and how it has been achieved. Section five gives a discussion of the results and a comparison between mathematical and simulation models. In the final section the conclusions are given.

II H TERNARY LINE CODE OPERATION

The H ternary line code operates on a hybrid principle that combines the binary NRZ L the ternary dicode and the polar RZ codes and thus it is called hybrid ternary. The H ternary code has three output

levels for signal representation; these are positive (1), zero (0) and negative (-1). The following subsections give a description of the procedures for the encoding and decoding principles.

A. Encoder Operation

The states shown in Table I depict the encoding procedure. The H ternary code has three output levels for signal representation; these are positive (1), zero (0) and negative (-1). These three levels are represented by three states. The state of the line code could be in any of these three states. A transition takes place to the next state as a result of a binary input (0 or 1) and the encoder output present state. The encoding procedure is as follows:

- (1) The encoder produces level 1 when the input is a binary 0 and whether the encoder output present state is at 0 or -1 level.
- (2) The encoder produces -1 level when the input is a binary 1 and whether the encoder output present state is at 0 or 1 level.
- (3) The encoder produces 0 level when the input is binary 0 and the encoder present state is 1 level or when the input is binary 1 and the encoder present state is -1 level.
- (4) Initially the encoder output present state is assumed at 0 level when the first binary bit arrives at the encoder input.

TABLE I
ENCODER OPERATION PRINCIPLES

Input Binary	Output Ternary	
	Present	Next
0	0	0
0	0	1
0	0	-1
1	1	0
1	1	1
1	1	-1
0	1	0
0	1	1
0	1	-1

The operation procedure gives the reader sufficient information about the operation of this new line code scheme. Further details and comparison together with design and modelling of the encoder can be sought from [4, 5, 7, 9]. The variation of this new line code is that it violates the encoding rule of NRZ-L and dicode when a sequence of 0s or 1s arrives. In the latter case it operates on the same encoding rule of polar RZ but with full period pulse occupancy.

B. Decoder Operation

Table II shows the input states of the H ternary decoder and its decoding procedure for an output binary. It is a reverse process of the encoding operation given in the previous subsection. The decoder has only two output states (binary) whereas the input is three

states (ternary). The decoding procedure is as follows [9].

- (1) The decoder produces an output binary 0 when the input ternary is at 0 level and whether the decoder output present state is a binary 0 or 1.
- (2) The decoder also produces an output binary 1 when the input ternary is at 1 level and the decoder output present state is at a binary 0 or 1.
- (3) Similarly the decoder produces an output binary -1 when the input ternary is at -1 level and whether the decoder output present state is a binary 0 or 1.
- (4) Finally the decoder produces an output binary 0 when the input ternary is at 0 level and the decoder output present state is a binary 0 or 1.

It is clear that the decoding process at the receiver is quite similar to that of the NRZ-L code when the 0 and 1 levels are received. The difference arises when level -1 is received. In which case the decision is made depending on the decoder output present state.

TABLE II
DECODER OPERATION PRINCIPLES

Input Ternary	Output Binary	
	Present	Next
0	0	0
0	0	1
0	0	-1
1	1	0
1	1	1
1	1	-1
0	1	0
0	1	1
0	1	-1

III MATHEMATICAL MODELS

The power spectral density of a line code is a very crucial factor in determining the bandwidth needed for the transmission of the encoded signal. It also gives indication as how much the line code is able to compress the original binary code sequence bandwidth. The following two sub-sections give a brief analysis of the mathematical computation of H ternary line code and other peer codes and verification for the derived formula of the H ternary line code at zero frequency.

A. Review of Mathematical Analysis

The power spectral density (PSD) of a line code can be evaluated using either deterministic or stochastic analysis techniques. Since in our case the input data sequence is random, the second approach is therefore adopted.

The general expression of the PSD of a digital signal is given by [8]:

$$P_c(f) = \frac{|G(f)|^2}{T} \sum_{k=-\infty}^{\infty} R(k) e^{j\pi k T f} \quad (1)$$

where $G(f)$ is the Fourier transform of the line code pulse shape $s(t)$ of amplitude A and duration T and

$R(k)$ is its autocorrelation function. It is evident that the above equation shows that the spectrum of the digital signal depends on two things: the pulse shape used and the statistical properties of the encoded signal. Equation (3) can also be rewritten in a simpler series form as follows:

$$P_c(f) = \frac{|C|}{T} \left[R + \sum_{k=1}^{\infty} R(k) \cos(\pi k T f) \right] \quad (4)$$

The pulse shape of the H ternary line code is a pulse of unit amplitude with a duration T . The Fourier transform of the H ternary pulse is given by [8]:

$$C(f) = T \frac{\sin \pi f T}{T} = T \operatorname{sinc}(\pi f T) \quad (5)$$

The above sinc function has a spectrum that extends to infinity for both the positive and negative frequencies.

The statistical properties of the data are referenced to the autocorrelation function of the line code that is given by:

$$R(k) = \sum_{i=1}^N (A_i A_{i+k} P_i) \quad (6)$$

where A_i and A_{i+k} are the signal levels that correspond to the i th and $(i+k)$ th symbol positions that represent the H ternary line code respectively, and P_i is the probability of having the i th A_i and A_{i+k} product.

To calculate the autocorrelation function of the line code for a different combination of symbols, we first calculate the $R(0)$. This means the autocorrelation function of the line code pulse symbol with itself. From [7], the probability of occurrence of each symbol of the H ternary line code is equal. This means the probability of the three transmitted code levels are equal, i.e. $P_1 = P_2 = P_3 = 1/3$. Substituting these values together with their respected unit amplitude symbols into equation (6) for N signal symbols and averaging the same signal symbols results in:

$$R(0) = \frac{1}{N} \left[\frac{N}{3} (+1) + \frac{N}{3} (-1) + \frac{N}{3} (0) \right] = \frac{1}{3} \quad (7)$$

The calculation of $R(k)$ for all other values of k excluding $k=0$ can be determined using a tabulation method [8,9]. The values of $R(1)$, $R(2)$, $R(3)$, ..., $R(k)$ can be found using the probabilities of all possible states. The probabilities of each case also depend on the number of H ternary symbols that are considered. For example, the probabilities of each symbol are $P_1 = 1/4$, $P_2 = 1/8$, $P_3 = 1/6$, and so on. The autocorrelation function for each case using equation (6) is thus $R(1) = 1/2$, $R(2) = 1/4$, $R(3) = 1/8$, and so on for other values of R_k . The overall autocorrelation function for all values of k excluding $k=0$ is thus given as follows in a series form [8]:

$$R(k) = \left(\frac{-1}{k+1} \right) = \left(\frac{-1}{k} \right)^k \quad (8)$$

Substituting equations (5) and (7) together with (3) into (4) gives the PSD of the H ternary line code that is [8]:

$$P_c(f) = A T \operatorname{sinc}(\pi f T) \left[\frac{1}{3} + \sum_{k=1}^{\infty} \left(\frac{-1}{k} \right)^k \cos(\pi k T f) \right] \quad (9)$$

The PSD of the H ternary line code is a re-shaped form of the Fourier transform of a rectangular pulse having A amplitude and duration of T . The re-shaping function is the autocorrelation function of the H ternary line code.

The normalised PSD results of the above derived formula for the H ternary code versus the normalised frequency is shown in figure 3. Figure 3 clearly shows that the bulk of the high weight frequency components of this line code are centred at $1/4$ of the normalised frequency (signalling rate). The spectrum also shows the line code has no dc component.

To compare the H ternary line code spectrum with other line codes spectra under consideration, the derived spectra formulae are given [8]:

$$P_c(f) = A T \operatorname{sinc}(\pi f T) \quad (10)$$

(Polar Non Return to Zero (NRZ-L))

$$P_c(f) = A T \operatorname{sinc}(\pi f T) \sin(\pi f T) \quad (11)$$

(Bipolar NRZ or Alternative Mark Inversion (AMI))

$$P_c(f) = A T \operatorname{sinc}(\pi f T) \sin(\pi f T) \quad (12)$$

(Manchester)

$$P_c(f) = A T \operatorname{sinc}(\pi f T) \sin(\pi f T) \quad (13)$$

Figure 3 also shows the PSD comparison between the different line codes. The figure clearly shows that the PSD of the H ternary line code overperforms NRZ-L and lies between AMI and Manchester line codes spectra.

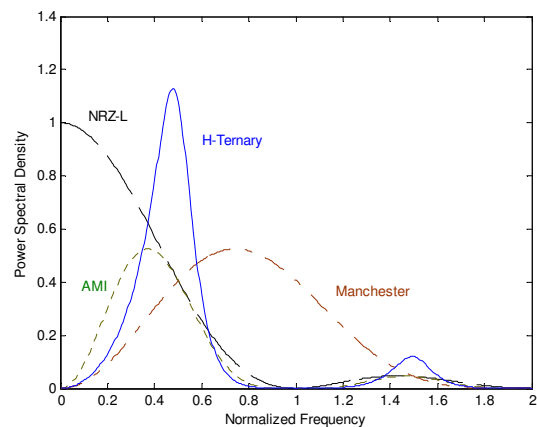


Fig. 3 Power spectra of different line codes

B. Investigation of the H Ternary Line Code Analytical Model

The mathematical PSD model derived in the previous sub-section for the H ternary line code will be further investigated analytically in this sub-section to validate its accuracy. The reason for doing this is to

check its validity with respect to the simulation results obtained from the simulation model

We need to prove that at zero frequency ($\omega = 0$) equation (7) produces a value of zero which means there is no dc component. This requires that the summation of the parameter which represents $R(k)$ for all values of k except for $k=0$ should converge to a value of $1/3$. The above parameter is the autocorrelation function of the line code that is derived in equation (6). The summation of $R(k)$ that appears in equation (7) can be rearranged in the form

$$R_k = \sum_{k=-\infty}^{\infty} r^k = \sum_{k=0}^{\infty} r^k - \sum_{k=1}^{\infty} r^k \quad (1)$$

where r is equal to $1/2$

The summation R_k of above geometric series is given by [3]

$$R_k = \frac{1-r^{k+1}}{1-r} - \frac{1-r^k}{1-r} \quad (2)$$

Substituting the value of $r=1/2$ into above equation yields

$$R_k = \frac{1-(1/2)^{k+1}}{1-1/2} - \frac{1-(1/2)^k}{1-1/2} \quad (3)$$

The above value of R_k represents the summation of $R(k)$ given in equation (7). This gives a very important conclusion that the summation of $R(k)$ tends to a value of $1/3$ for all values of k except for $k=0$. This in turn proves that the power spectral density given in the same equation has a zero value at zero frequency (dc)

IV SIMULATION MODEL

The results of simulation are collected from a model written in Matlab. The model generates $P \times N$ binary sequence of data which are then encoded into H ternary line code. The encoded three level signal is then transformed to the frequency domain for the determination of the line code power spectral density using Matlab FFT routine. The sampling frequency is chosen at four times the maximum rate of the H ternary encoded signal. This was made to ensure the accuracy of the results of the spectra that were obtained from the simulation model.

In the model the generated $P \times N$ binary sequence length is chosen to be 1000000 bits. These bits are encoded into three level H ternary symbols. Figures 2 and 3 show the simulation results for two different seeds. The PSD results show relatively high weights of low frequency components. This is slightly deviated from that of the analytical results.

To improve the results and remove the discrepancy long $P \times N$ sequences are used. It is expected that the drift in the results of the simulation model will be eliminated when the simulation model is run for long sequences. Thus the simulation model has been modified to generate long $P \times N$ sequence of one million binary bits. As before the new sequence is encoded and transformed to the frequency domain and the results are collected. Although it took about 1000000 times the time needed for the previous 1000000 bit model to finish the run and gather the results, the results came almost similar to

that of the 1000000 bit model. Figure 4 shows the results for 1000000 H ternary code symbols.

It is also shown that different seeds give different weights for the different frequency components of the line code PSD as shown in figures 2 and 3. To reduce the difference the simulation model has been run for 1000000 times for different random $P \times N$ sequence seeds. The results from these runs are then added up and averaged over the number of runs and displayed in figure 5.

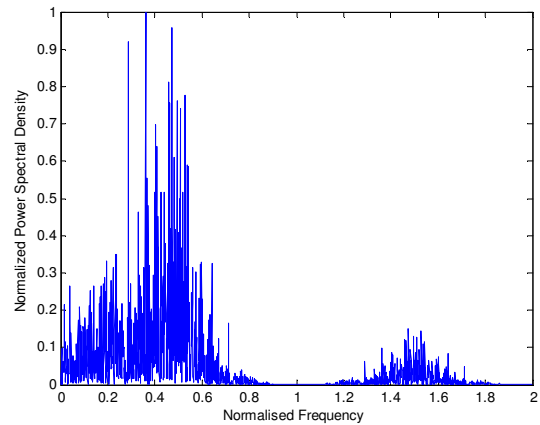


Fig 2 Normalised power spectral density of the simulation results for a 1000000 bit P N sequence (seed 345)

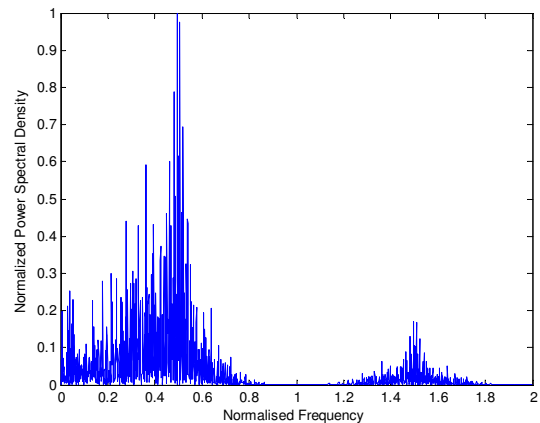


Fig 3 Normalised power spectral density of the simulation results for a 1000000 bit P N sequence (seed 543)

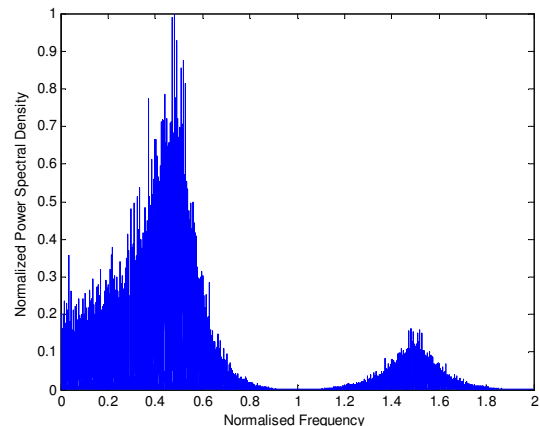


Fig 4 Normalised power spectral density of the simulation results for a 1000000 bit P N sequence (seed 345)

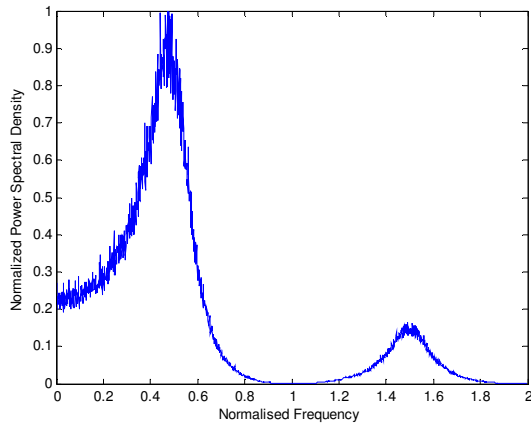


Fig 5 Normalised averaged power spectral density of the simulation results for different seeds

V RESULTS COMPARISON AND DISCUSSION

The mathematical model of the H ternary line code and its results have been thoroughly investigated and proved percent accurate. Comparing the simulation results obtained from the simulation model with that of the mathematical model can be seen in figure. In this figure the analytical results are compared with the simulation results for only a single seed. The results show a minor deviation from each other for both models at the low frequency components of the line code spectra. It also shows that the simulation discrete line spectra are fluctuating above and below the solid line of the mathematical model. Longer P N binary sequence is then suggested to improve the simulation results to match that of the analytical results at low frequency components. The latter encoded sequence spectra however show almost the same results of that of the shorter sequences as shown in figure 4.

In order to reduce the fluctuation in the simulation result spectra for the whole simulated spectrum several runs of the simulation model have been carried out for different P N sequence seeds. The results of these runs are then added up and averaged over the number of runs and are displayed in figure 7 together with that of the analytical model. Figure 7 show excellent agreement of both models at all frequency spectra except for that of the lower frequency region.

Figure 7 shows clearly that the analytical model starts from zero PSD value at zero frequency however this is not the case for the simulation results. The analytical results are accurate however they are unable to exactly reflect the practical case of the line code sequence. This does mean that the simulation model is able to generate binary sequence that is then encoded to a three level code signal which has higher weight of repeated patterns at low frequencies that are close to zero.

The H ternary line code considered here is a modification of other predecessor codes that are used for base band and pass band data transmission. The new code exploits the merits of these codes and

eliminates their deficiencies. The reshaping process of the H ternary pulses show preferred spectra with no dc component that enables better use of the allocated spectrum. It provides a signalling rate of around 44 percent of the original data bit rate provides better timing information for encoder decoder synchronisation and many other desirable features.

The H ternary line code has a noise performance which is superior to its predecessor line codes at low level signal to noise ratio [7]. This superiority enables the code to operate at lower power and perform better than the other line codes.

The code has also got the property of single error detection [5-9]. A property that is very much desirable in line codes. This came into effect due to the fact that encoding has a correlative relation between the adjacent line code symbols.

The new line code hardware is relatively more complex in implementation of the encoder and decoder. This complexity however meets a relative simplicity in the clock recovery circuit at the receiving end. This is due to the fact that for every transmitted H ternary symbol there is a change in signal level.

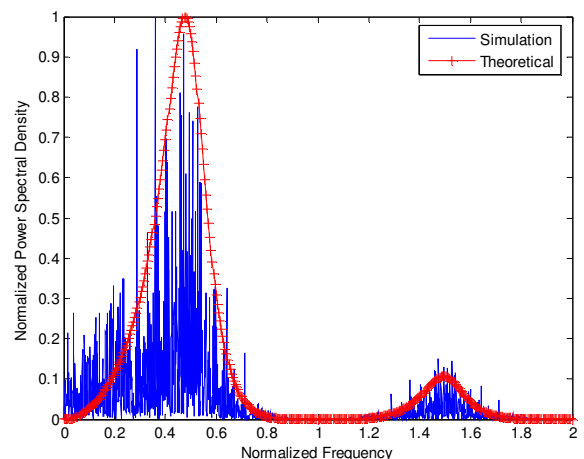


Fig Results comparison of the theoretical and the simulation models (single seed 345)

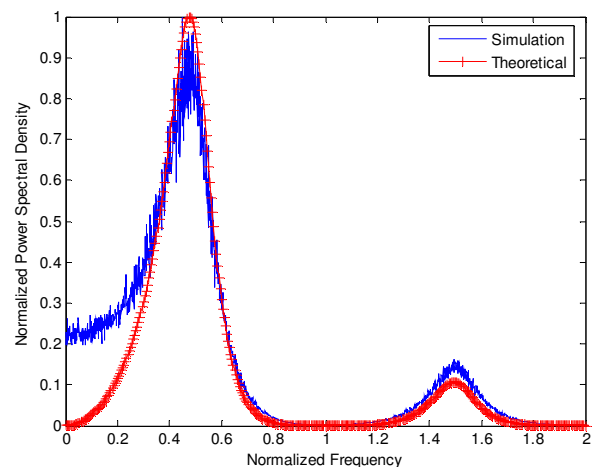


Fig 7 Results comparison of the theoretical and the simulation models (seeds)

VI CONCLUSIONS

A comparison between two models of the H ternary line code is presented. Investigation of the analytical model has been done together with the simulation model. The results obtained from both models are correct and accurate. The simulation results however reveal a fact that this model is able to generate sequence that are more realistic and closely resembles real world data. The overall results however revealed an important fact that the PSD of this new line code has very small bandwidth that is centred at about 44% of that of the normalised signalling rate of the binary sequence with no dc component. The code has many other desirable features such as timing information content and a single error detection capability.

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