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Tension capacity of staggered bolted connections in Cold-Reduced Steel **Sheets**

Lip H. Teh University of Wollongong, lteh@uow.edu.au

Drew D. A Clements University of Wollongong, ddac998@uow.edu.au

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Tension Capacity of Staggered Bolted Connections in Cold-Reduced Steel Sheets

Lip H. Teh¹ A.M.ASCE and Drew D. A. Clements²

Abstract:

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ula used in steel des This paper examines the assumption implicit in Cochrane's formula that stresses are uniformly distributed across the net section of a staggered bolted connection. The assumption was found to be overoptimistic for connections in steel having low ductility, leading to unconservative estimates for the tension capacity if the in-plane shear lag is not accounted for. The reduction factor of 0.9 specified in the North American specification for cold-formed steel structures partially but not wholly addresses the problems inherent in the code equations. This paper points out that the "simplification" of Cochrane's original formula into the standard formula used in steel design codes worldwide can lead to additional design capacity that may not be justified. It proposes an equation that accounts for the in-plane shear lag and incorporates Cochrane's original formula for determining the net section area. The proposed equation is demonstrated through laboratory tests on 74 staggered bolted connection specimens in 1.5 mm and 3.0 mm G450 sheet steel to be more accurate and consistent than the code equations in predicting the net section tension capacity.

Subject headings: bolted connections, cold-formed steel, steel plates, tensile strength

Author's keywords: cold-reduced steel sheet, net section tension strength, staggered bolts

¹Lecturer, School of Civil, Mining & Environmental Engineering, University Of Wollongong, Wollongong, NSW 2500, AUSTRALIA

²Honours Student, School of Civil, Mining & Environmental Engineering, University Of Wollongong, Wollongong, NSW 2500, AUSTRALIA

Introduction

mud Steel Structural Members 2007 (AISI 2010) and in AS/NZS 4600:2005 Cold-formed
eel Structures (SA/SNZ 2005). The two code equations have the same basic form but for the
efficients and in-plane shear lag factors. The co The net section tension capacity of a staggered bolted connection in cold-formed steel sheet is specified in Supplement No. 2 to the North American Specification for the Design of Coldformed Steel Structural Members 2007 (AISI 2010) and in AS/NZS 4600:2005 Cold-formed Steel Structures (SA/SNZ 2005). The two code equations have the same basic form but for the coefficients and in-plane shear lag factors. The common formula for determining the net area of a staggered bolted connection element is adopted from AISC specifications for structural steel members (AISC 1936, 2010), which was based on the theoretical work of Cochrane (1922) and which has remained the same over the past nine decades.

The North American cold-formed steel design code (AISI 2010) has a reduction factor of 0.9 applied to the net area computed using Cochrane's formula, pursuant to the recommendation of LaBoube & Yu (1996). More recently, Fox & Schuster (2010) argued that the reduction factor of 0.9 specified in the code was unnecessary based on their own laboratory test results.

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 $\&$ Yu (1996). More recently, The recommendation of LaBoube & Yu (1996) was based on the laboratory test results of six specimens only having a uniform gage of 41.3 mm and a uniform stagger of 12.7 mm (Holcomb et al. 1995), while the conclusion of Fox & Schuster (2010) was based on sixty eight specimens having a uniform gage of 35 mm. Each of the specimens tested by Fox & Schuster (2010) had a stagger that was equal to either the bolt diameter (12.7 mm) or twice the diameter (25.4 mm). Their experiment tests therefore involved two staggered configurations only, as the two variables of a staggered path are the gage and the stagger, as evident from Figure 1.

The steel materials used by Fox & Schuster (2010) appear to be more ductile than some coldreduced sheet steels used in the cold-formed steel construction industry (Hancock 2007), with

elongation at fracture of 41% (the base length was not reported) for some 1.6 mm sheet steel specimens and ratios of tensile strength to yield stress of 1.31 for 6.0 mm specimens. Material ductility is an important factor affecting the ability of a steel member to redistribute stresses away from stress concentration areas prior to reaching the ultimate limit state.

There is an implicit assumption in Cochrane's formula for determining the net area, that stresses are uniformly distributed across the net section. For a bolted connection in steel sheet with low material ductility, such an assumption is difficult to justify in light of the laboratory test results obtained by Teh & Gilbert (2012). The finite element analysis results obtained by Epstein & Gulia (1993) suggest that the formula may be overoptimistic.

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execs are uniformly distributed across the net section. For a bolted connection in steel sheet
th low material ductility, such an assumptio Furthermore, Cochrane's formula as given in the steel design codes (termed "Cochrane's standard formula" in this paper) has been derived by neglecting a term in the original formula that Cochrane (1922) considered to be "comparatively small" and ignored for "practical purposes". However, the neglect can result in an additional design capacity of about 10%, as demonstrated through a heuristic example in this paper.

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ula" in this paper) has been derived by neglecting a term in the orige

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owever, the neglect ca This paper proposes an equation for predicting the net section tension capacity of a staggered bolted connection in cold-reduced steel sheet, based on Cochrane's original formula and the in-plane shear lag factor derived by Teh & Gilbert (2012). The equation is verified against the laboratory test results of staggered bolted connections in 1.5 mm and 3.0 mm G450 steel sheets, which had relatively low material ductility. A total of 78 specimens with 58 different configurations were tested. Most specimens were loaded concentrically (double shear), while some 3.0 mm specimens were loaded eccentrically (single shear).

Code equations for the tension capacity of a staggered bolted connection

Clause 5.3.3(5) of AS/NZS 4600:2005 (SA/SNZ 2005) specifies the nominal net section tension capacity of a member with staggered bolt holes to be

$$
P_p = F_u A_n \tag{1}
$$

in which F_u is the material tensile strength, and A_n is the net area of the considered section.

Clause 5.3.1 of AS/NZS 4600:2005 specifies that in determining the net area *A*n of a member with staggered bolt holes, the width to be deducted shall be the greater of the deduction for non-staggered holes and

$$
W_d = n_s d_h - \sum \frac{s^2}{4g} \tag{2}
$$

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nrane (1922) using the equal-stress method, and is termed Co in which n_s is the number of bolts in the considered section (equal to 2 in Figure 1), d_h is the bolt hole diameter, *s* is the stagger, and *g* is the gage. Equation (2) is based on the theoretical work of Cochrane (1922) using the equal-stress method, and is termed Cochrane's standard formula in this paper.

For the member with staggered bolt holes depicted in Figure 1, Equation (1) thus becomes

$$
P_p = F_u t \left[W - \max \left(d_h, 2d_h - s^2 / 4g \right) \right] \tag{3}
$$

in which *t* is the sheet thickness and *W* is the total width of the member.

The beneficial effect of stagger is fully exploited when the tension capacity of the member can be computed from

$$
P_p = F_u t (W - d_h) \tag{4}
$$

which implies failure across the unstaggered path.

It can be seen from Equations (3) and (4) that, for the member depicted in Figure 1 with the stagger *s* set to be three times the bolt hole diameter d_h , the beneficial effect of stagger is fully exploited when

$$
g \le 2.25d_h \tag{5}
$$

On the other hand, if the gage *g* is set to be three times the bolt hole diameter d_h , the beneficial effect of stagger is fully exploited when

$$
s \ge 3.464 d_h \tag{6}
$$

plotted when
 $g \le 2.25d_n$

(5)

the other hand, if the gage g is set to be three times the bolt hole diameter d_b, the

neficial effect of stagger is fully exploited when
 $s \ge 3.464d_n$

(6)

can be seen from Equations 64 d_h

In from Equations (5) and (6) that it is not difficult to fully exploit

ing to Cochrane's formula. However, there is an implicit assum

ensile stresses are uniformly distributed over the net section.

Section E5 It can be seen from Equations (5) and (6) that it is not difficult to fully exploit the stagger effect according to Cochrane's formula. However, there is an implicit assumption in the formula that tensile stresses are uniformly distributed over the net section.

According to Section E5.2 of Supplement No. 2 to the North American Specification for the Design of Cold-formed Steel Structural Members 2007 (AISI 2010), the nominal net section tension capacity of the member depicted in Figure 1 is determined from

$$
P_p = F_u t \, 0.9 \left(W - 2d_h + s^2 / 4g \right) \tag{7}
$$

The reduction factor of 0.9 in Equation (7) was proposed by LaBoube & Yu (1996) to account for the test results of Holcomb et al. (1995), who found the ratios of ultimate test load to predicted failure load given by Equation (3) to range from 0.81 to 0.95, with a mean of 0.89. LaBoube & Yu (1996) suggested that the low ratios of ultimate test load to predicted failure load obtained in their laboratory tests could be attributed to the lack of plastic flow that was available in thin flat sheet, i.e. the lack of material ductility of the tested specimens.

In any case, it can be seen from Equation (7) that the North American specification (AISI 2010) does not appear to limit the net section tension capacity of the member to that given by Equation (4). For staggered bolted connections with narrow gages that satisfy the requirement that the bolt spacing be at least three times the bolt diameter (and hence the staggers are large), Equation (7) tends to overestimate of the tension capacity (see also Equations 5 and 6).

Cochrane's original formula and shear lag in cold-reduced steel sheets

Cochrane's standard formula shown in Equation (2) results from the simplification of the original formula

$$
W_d = n_s d_h - \sum \frac{s^2}{4g + 2d_h}
$$
 (8)

Although Cochrane's argument for the simplification of Equation (8) into Equation (2) was justified many decades ago (Cochrane 1922), in the present computer age there is little to be gained by neglecting the term " $2d_h$ " in Equation (8).

Figure 1.1 The solution of the term is the solution of the tension capacity (see also Equations 5 and 6).
 Solution 1.1 Solution (7) tends to overestimate of the tension capacity (see also Equations 5 and 6).
 Solution $d_h - \sum \frac{s^2}{4g + 2d_h}$

Shrane's argument for the simplification of Equation (8) into Equation

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glecting the term "2 d_h " in Equation (8).

ion meeting t For a connection meeting the requirement that the bolt spacing be at least three times the bolt diameter, the neglect of the term "2*d*h" in Equation (8) can result in overestimation of the net section area by up to 5%. For a connection subject to the requirement that the bolt spacing be at least two and a half times the bolt diameter, as specified in Appendix B of the North American Specification for the Design of Cold-formed Steel Structural Members 2007 (AISI 2007), the neglect can result in an overestimation by some 10%, as shown in the following.

If the member depicted in Figure 1 has $W = 55$ mm, $d_h = 13$ mm, $g = 15$ mm, and $s = 28$ mm, then the net section width (i.e. $W - W_d$) computed using Equation (2) will be 42.1 mm, which is 10.4% greater than the value of 38.1 mm given by Equation (8). With regard to the

Australasian code, the net width is limited by the relevant term in Equation (4) to 42.0 mm, which is still 10.2% greater than that given by Cochrane's original formula. The bolt spacing in this example satisfies the code requirement in Canada (Appendix B - AISI 2007) and Europe (ECS 2005) since it is 2.65 times the nominal bolt diameter of 12 mm.

Teh & Gilbert (2012) have demonstrated the effect of in-plane shear lag on the net section tension capacity of a bolted connection in cold-reduced steel sheets with low ductility. Based on the in-plane shear lag factor proposed by Teh & Gilbert (2012) and Cochrane's original formula shown in Equation (8), the tension capacity of the member depicted in Figure 1 should be computed from

$$
P_p = \left(0.9 + 0.1 \frac{d_h}{W}\right) F_u t \left[W - \max\left(d_h, 2d_h - \frac{s^2}{4g + 2d_h}\right) \right] \tag{9}
$$

Test materials

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Sion capacity of a botted connection in cold-reduced steel sheets with low duetility. Based

the in-plane shear lag factor proposed $0.9 + 0.1^{d_h}/W$ $F_u t \left[W - \max\left(d_h, 2d_h + \frac{d_s^2}{4g + 2d_h}\right)\right]$
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neet steel materials used in the laboratory tests, which have a

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neet steel materials u The G450 sheet steel materials used in the laboratory tests, which have a trade name GALVASPAN®, were manufactured and supplied by Bluescope Steel Port Kembla Steelworks, Australia. Two nominal thicknesses were used in the present work, being 1.5 mm and 3.0 mm. The average base metal thicknesses t_{base} , yield stresses F_y , tensile strengths F_u and elongations at fracture over 15 mm, 25 mm and 50 mm gauge lengths ε_{15} , ε_{25} and ε_{50} , and uniform elongation outside the fracture ε_{uo} of the steel materials as obtained from six 12.5 mm wide tension coupons are shown in Table 1. Tensile loading of all coupons and bolted connection specimens is in the direction transverse to the rolling direction of the G450 sheet steel. The tension coupon tests were conducted at a constant stroke rate of 1 mm/minute resulting in a strain rate of about 2×10^{-4} per second prior to necking.

The G450 sheet steels used in the present work represent the grades of steel covered by AS/NZS 4600 (SA/SNZ 2005) which are among those having the lowest ductility and for which the nominal tensile strength and yield stress may be fully utilised in structural design calculations (Hancock 2007). The use of the present materials therefore represents a stringent verification of the design equations.

Specimen configurations and test arrangements

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infication of the design equations.

Declinent configurations and test arrangements

Le basic configuration of each specimen The basic configuration of each specimen is depicted in Figure 1. As shown in the figure, each specimen had three staggered bolts, arrayed along two gage lines. The presence of three bolts ensured that bearing failure did not occur. For each sheet thickness, the geometric variables are the sheet width *W*, the gage *g*, the stagger *s*, and the bolt hole diameter d_h . Their values for each bolted connection specimen are detailed in the next section, which ensured that block shear failure (Teh & Clements 2012) did not occur.

bearing failure did not occur. For each sheet thickness, the geomet
width *W*, the gage *g*, the stagger *s*, and the bolt hole diameter d_h . The
onnection specimen are detailed in the next section, which ensure
Teh & Cl There are groups of specimens in which the gage was kept constant while the staggers were varied, groups in which the stagger was kept constant while the gages were varied, groups in which the ratio of stagger to gage was uniform but the staggers (and the gages) were varied, and groups in which both the gage and the stagger were kept constant while the sheet widths were varied. There are however overlapping members between the groups, designed to minimise the total number of specimens.

Two nominal sizes of bolts, being 12 mm and 16 mm, were used for the connections. The bolt holes were 1 mm larger than the corresponding nominal bolt diameters. It may be noted that the maximum diameter of a bolt hole for a 12 mm or larger bolt is restricted to the bolt diameter plus 2 mm (SA/SNZ 2005) or 1.6 mm (AISI 2007). The bolts were only tightened by hand, and no washers were used unless indicated otherwise in the next section.

Most of the specimens were loaded concentrically as double shear connection specimens, as illustrated in Figure 2(a). For the purpose of investigating any noticeable differences in net section tension strength between double shear and single shear staggered bolted connections, some 3.0 mm specimens were loaded eccentrically, as illustrated in Figure 2(b).

In order to ensure the connected sheets remain vertical throughout the tensile test, a shim plate of the same thickness as the sheet was welded to one of the outer sheets of a double shear specimen at the grip end, as depicted in Figure 2(a). Shim plates were also welded to both sheets of a single shear specimen, as depicted in Figure 2(b). The bolted sheets were gripped in such a way that prevented them from rotating in-plane, as illustrated in Figure 3.

The 3.8 mm specifies were notated eccles are mass and the transient in Figure 2(b).

Order to ensure the connected sheets remain vertical throughout the tensile test, a shim plate

the same thickness as the sheet was weld nnection specimens were tested to failure using an Instron 8033 univ
stroke rate of 1 mm/minute, which coincides with that used for
on tests. In the vicinity of the ultimate load associated with net sect
of either a bolte The bolted connection specimens were tested to failure using an Instron 8033 universal testing machine at a stroke rate of 1 mm/minute, which coincides with that used for the present tension coupon tests. In the vicinity of the ultimate load associated with net section fracture, the elongation of either a bolted connection specimen or a tension coupon is concentrated in the yielded and/or necked region. Therefore, the stroke rate used in determining the ultimate test load P_t of a bolted connection specimen should ideally not be greater than that used in determining the material tensile strength *F*u, even though the overall length of the former is many times greater. A greater strain rate leads to a higher implied tensile strength (Kassar & Yu 1992).

Experimental test results and discussions

In calculating the nominal tension capacity P_p of a specimen predicted by a design equation, the measured values of the geometric dimensions such as the base metal thickness, the overall sheet width, and the bolt hole diameter, are used. However, for ease of comparisons, only the nominal values are shown in the tables following.

Double shear 3.0 mm specimens

Table 2 lists the relevant geometric dimensions and the test results of the double shear connections in 3.0 mm G450 steel sheet. An empty cell in the table indicates that the data in the above cell applies. The table shows the ratios of the ultimate test load P_t to the tension capacity P_p predicted by Equations (3) and (7), which are specified in the current Australasian and North American cold-formed steel design codes, respectively. It also includes the ratios obtained using the proposed Equation (9).

Table 2 shows that Equation (3) consistently and significantly overestimates the net section tension capacity of the tested specimens. The major reason is the implicit assumption that stresses are uniformly distributed over the net section. The average ratio of the ultimate test load P_t to the net section tension capacity P_p predicted by the equation is 0.92.

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uation (7) yield Although Equation (7) yields reasonably accurate results for most specimens in Table 2, it overestimates the capacity of specimen CT22 (numbered 7) by more than 20% (1/0.81 = 1.23). The equation also significantly overestimates the capacity of specimens CT42 and CT43 (numbered 20 and 21), which had a gage of 15 mm but satisfied the requirement that the bolt spacing be at least three times the bolt diameter. These significant overestimations are despite the reduction factor of 0.9 embedded in the equation.

In contrast to Equations (3) and (7), Equation (9) consistently predicts the net section tension capacity of each specimen listed in Table 2 with excellent accuracy.

Figure 5(a) shows that the critical net section of specimen CT18 (numbered 1 in Table 2) cut across the unstaggered path, while Figure 5(b) shows that the critical net section of specimen CT11b (numbered 4) cut across the staggered path. Only the proposed Equation (9) yields accurate predictions for both specimens.

Single shear 3.0 mm specimens

Table 3 lists the relevant geometric dimensions and the test results of the single shear connections in 3.0 mm G450 steel sheet (see Figure 4b for an example). An empty cell in the table indicates that the data in the above cell applies. Specimens numbered 36 through 45 had washers under both the bolt head and the nut, while the rest did not. The table shows the ratios of the ultimate test load P_t to the tension capacity P_p predicted by Equations (3), (7) and (9).

ble indicates that the data in the above cell applies. Specimens numbered 36 through 45 had
shers under both the bolt head and the nut, while the rest did not. The table shows the ratios
the ultimate test load P_1 to th The bolt heads of specimens numbered 31 and 33 through 35 punched through the bolt holes, as shown Figure 6(a) for specimen numbered 33, resulting in low ratios of the ultimate test load to the predicted net section tension capacity, especially for specimen numbered 35. Figure 6(b) shows that the use of washers can prevent the bolt head from punching through the bolt hole to achieve the net section fracture mode.

prodicted net section tension capacity, especially for specimen nu
hows that the use of washers can prevent the bolt head from punct
o achieve the net section fracture mode.
So that, in cases where the specimen failed by Table 3 shows that, in cases where the specimen failed by pure net section fracture, Equation (9) predicts the net section tension capacity with reasonable accuracy. It is also evident from the range of P_t/P_p values shown in Tables 2 and 3 that separate resistance factors are not required for determining the design net section tension capacities of double and single shear staggered bolted connections in cold-reduced steel sheets.

The failure mode associated with the bolt head punching through the bolt hole should be treated as a distinct strength limit state, predicted using a separate equation.

Double shear 1.5 mm specimens

Table 4 lists the relevant geometric dimensions and the test results of the double shear connections in 1.5 mm G450 steel sheet. An empty cell in the table indicates that the data in

the above cell applies. The table shows the ratios of the ultimate test load P_t to the net section tension capacity P_p predicted by Equations (3), (7) and (9).

Table 4 shows that Equations (3) and (7) significantly overestimate the net section tension capacities of some 1.5 mm specimens. It can also be seen from Tables 4 and 2 that the effect of in-plane shear lag was more pronounced for the 1.5 mm specimens than for the 3.0 mm specimens, the latter having greater material ductility as evident from Table 1.

pacities of some 1.5 mm specimens. It can also be seen from Tables 4 and 2 that the effect
in-plane shear lag was more pronounced for the 1.5 mm specimens than for the 3.0 mm
ceimens, the latter having greater material du The average ratio of the ultimate test load P_t to the net section tension capacity P_p predicted by Equation (9) for the 1.5 mm specimens listed in Table 4 is 0.95, with a standard deviation of 0.033. These values compare unfavourably against the corresponding values of 1.01 and 0.025 for the double shear 3.0 mm specimens.

Figure 7(a) shows that the critical net section of specimen CT17a (numbered 46 in Table 4) cut across the unstaggered path, while Figure 7(b) shows that the critical net section of specimen CT29b (numbered 62) cut across the staggered path. Only the proposed Equation (9) yields reasonably accurate predictions for both specimens.

See values compare unfavourably against the corresponding values
double shear 3.0 mm specimens.
hows that the critical net seetion of specimen CT17a (numbered 46
e unstaggered path, while Figure 7(b) shows that the critic It is also evident from the mean values of P_t/P_p shown in Tables 2 and 4 that the reduction factor of 0.9 in Equation (7) proposed by LaBoube & Yu (1996) significantly improved the accuracy of the equation in predicting the net section tension capacities of the present specimens. However, Equation (7) results in substantially greater coefficients of variation compared to Equation (9).

Resistance factor (or capacity reduction factor)

The overall average ratio of the ultimate test load P_t to the net section tension capacity P_p predicted by Equation (9) for the 74 specimens that failed in net section fracture is 0.98, with a standard deviation of 0.041. It therefore seems reasonable to treat these specimens as one population for the purpose of determining a uniform resistance factor to be applied to the proposed equation.

Section F1.1 of the North American specification (AISI 2007) specifies that the resistance factor ϕ of a design equation is determined as follows

$$
\phi = C_{\phi} \left(M_m F_m P_m \right) e^p \tag{10}
$$

standard deviation of 0.041. It therefore seems reasonable to treat these specimens as one
pulation for the purpose of determining a uniform resistance factor to be applied to the
oposed equation.
Econ F1.1 of the North A $(M_m F_m P_m)e^p$
s the calibration coefficient equal to 1.52 in the case of the Load and
n (LRFD), M_m is the mean value of the fabrication factor equal to 0.99, and P_m
professional factor equal to 0.98 as stated in the fir in which C_{ϕ} is the calibration coefficient equal to 1.52 in the case of the Load and Resistance Factor Design (LRFD), M_m is the mean value of the material factor equal to 1.187 in the present case, F_m is the mean value of the fabrication factor equal to 0.99, and P_m is the mean value of the professional factor equal to 0.98 as stated in the first paragraph of this section. The statistical parameters of the material and fabrication factors of the (unwelded) 1.5 mm and 3.0 mm G450 sheet steels have been previously provided by Teh & Hancock (2005).

The power *p* of the natural logarithmic base *e* in Equation (10) is

$$
p = -\beta_0 \sqrt{V_M^2 + V_F^2 + C_p V_P^2 + V_Q^2}
$$
 (11)

in which the target reliability index β_0 is 3.5 (AISI 2007, SA/SNZ 1998), V_M is the coefficient of variation of the material factor equal to 0.03 in the present case, V_F is the coefficient of variation of the fabrication factor equal to 0.02 , V_P is the coefficient of variation of the professional factor equal to 0.065 being the minimum value specified in Section F1.1 of the

specification, C_p is the correction factor equal to 1.04 as computed from the relevant equation given in Section F1.1, and V_Q is the coefficient of variation of load effects equal to 0.21 as specified in Section F1.1.

It was found that in order to achieve the target reliability index β_0 of 3.5 in the LRFD, Equation (10) yields a resistance factor of 0.80. This value is higher than the current value of 0.65 specified in the cold-formed steel design codes (AISI 2007, SA/SNZ 2005), reflecting the greater reliability of the proposed Equation (9) compared to Equations (3) and (7).

Conclusions

Cochrane's formula for determining the net section area of a staggered bolted connection implicitly assumes that stresses are uniformly distributed over the net section. This assumption is not justified for connections in cold-reduced steel sheet with low ductility, in which the effect of in-plane shear lag on the net section tension capacity is significant.

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55 specified in the cold-formed st boromula for determining the net section area of a staggered bolted
sumes that stresses are uniformly distributed over the net so
not justified for connections in cold-reduced steel sheet with low
ect of in-plane shear lag The reduction factor of 0.9 specified in the current North American specification for coldformed steel structures goes a long way to account for the in-plane shear lag effect in staggered bolted connections. However, for the connections in which the gage is relatively narrow compared to the stagger, the code equation incorporating the reduction factor still leads to over-optimistic estimates for the net section tension capacity.

For certain configurations, the simplification of Cochrane's original formula into the standard formula used in the steel design codes worldwide leads to overestimations of the net section area by some 10%. There is little to be gained from the trivial simplification.

The new equation proposed in this paper incorporates the in-plane shear lag factor derived by Teh & Gilbert (2012) and Cochrane's original formula, leading to more accurate and more consistent results compared to the code equations.

It is proposed that a resistance factor of 0.80 be applied to the new equation in order to ensure a reliability index of not less than 3.5 in the LRFD approach of the North American specification for the design of cold-formed steel structures.

Acknowledgments

is proposed that a resistance factor of 0.80 be applied to the new equation in order to ensure
reliability index of not less than 3.5 in the LRFD approach of the North American
ceification for the design of cold-formed ste read Limited, for supplying the G450 sheet steel materials used in
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Notation

 A_n = net area of considered section

 C_p = correction factor

- C_{ϕ} = calibration coefficient
- $d =$ bolt diameter
- d_h = bolt hole diameter
- $g =$ bolt gauge spacing
- F_{m} = mean value of fabrication factor
- F_u = tensile strength of steel material
- F_y = yield stress of steel material
- $M_{\rm m}$ = mean value of material factor
- P_m = mean value of professional factor
- P_p = predicted failure load
- $s =$ bolt pitch spacing
- $t =$ nominal sheet thickness
- t_{base} = base metal thickness
- Franchise Contraction
 $\begin{aligned}\n &= \text{calibration coefficient} \\
 &= \text{bot diameter} \\
 &= \text{bot hole diameter} \\
 &= \text{bot square graph} \\
 &= \text{mean value of fabrication factor} \\
 &= \text{tensile strength of steel material} \\
 &= \text{mean value of material factor} \\
 &= \text{mean value of professional factor} \\
 &= \text{predicted failure load} \\
 &= \text{bot pitch spacing} \\
 &= \text{nomimal sheet thickness} \\
 &= \text{constant thickness} \\
 &= \text{coefficient of variation of fabrication factor} \\
 &= \text{coefficient of variation of material factor} \\
 &= \text$ V_F = coefficient of variation of fabrication factor
- V_M = coefficient of variation of material factor
- strength of steel material

ress of steel material

alue of material factor

ed failure load

ch spacing

al sheet thickness

lead thickness

etail thickness

etail thickness

etail thickness

etail thickness

etail thickn V_{P} = coefficient of variation of professional factor
- $V_{\rm Q}$ = coefficient of variation of load effects

 $W =$ sheet width

- β_0 = target reliability index
- ε_{15} = elongation at fracture over a gauge length of 15 mm
- ε_{25} = elongation at fracture over a gauge length of 25 mm

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- ε_{50} = elongation at fracture over a gauge length of 50 mm
- ε_{uo} = uniform elongation outside fracture zone
- ϕ = resistance factor (or capacity reduction factor)

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Figure 1 Staggered bolt configuration

Figure 2 Test arrangements of specimens

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Figure 3 Clamped end of specimen

(a) Double shear specimen (b) Single shear specimen

Figure 4 Some tested specimens

(a) Unstaggered path (b) Staggered path

Figure 5 Failure paths of double shear 3.0 mm specimens

(a) Punching failure (b) Effect of washer

Figure 6 Failure modes with and without washers

(a) Unstaggered path (b) Staggered path

Figure 7 Failure paths of double shear 1.5 mm specimens

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Table 1 Average material properties

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*The bolt heads punched through the bolt holes.

