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### Effect of sample size on magnetic J<sub>c</sub> for MgB<sub>2</sub> superconductor

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#### Abstract

A strong effect of sample size on magnetic  $J_c(H)$  was observed for bulk MgB<sub>2</sub> when  $J_c$  is obtained directly from the critical state model. Thus obtained zero-field  $J_c$  ( $J_{c0}$ ) decreases strongly with the sample size, attaining a constant value for the samples larger than a few millimetres. On the other hand, the irreversibility field ( $H_{irr}$ ) defined at  $J_c = 100 \text{ A/cm}^2$ increases with the sample size. The decrease of  $J_{c0}$  is described in terms of voids in the bulk MgB<sub>2</sub> samples and magnetic screening around the cells of agglomerated crystals between these voids because of concentration of the current in the narrow bridges connecting the cells. For samples larger than a few millimetres, the value of magnetic  $J_c$  is in agreement with the transport  $J_c$  and it is restricted by the voids. The critical state model is not suitable for obtaining  $J_c$  for smaller bulk MgB<sub>2</sub>. The increase of  $H_{irr}$  with the sample size is an artefact of defining  $H_{irr}$  by the value of  $J_c$  at which magnetic decoupling occurs within the cells.

Superconducting wires based on MgB<sub>2</sub> superconductor are currently in the process of fast development, resulting in improved values of  $J_c$ ,  $J_c(H)$  and  $H_{irr}$ <sup>1,2,3</sup>. We will show that incorrect conclusions can be deduced when comparing these values for the samples of different size. The value of  $J_c$  obtained from the critical state model for the samples larger than a few millimetres corresponds to the overall screening current density of the whole sample. This is equivalent to the  $J_c$  obtained in transport measurements. A direct application of the critical state model to calculate  $J_c$  of smaller MgB<sub>2</sub> samples leads to erroneous results, as the measured magnetic moment is contributed to by magnetic screening at various length-scales.

The field dependence of  $J_c$  was obtained from measurements of magnetic hysteresis loops, using a critical state model for appropriate geometry and the dimensions of the whole sample. The value of  $H_{irr}$  was obtained as the field at which thus obtained  $J_c$  equals to 100  $A/cm^2$ . We will show that this model should not be used for small MgB<sub>2</sub> samples. Nevertheless, we use it to demonstrate its unsuitability for small MgB<sub>2</sub> samples and for large fields. The measurements were performed by a Quantum Design PPMS magnetometer, with the sweep rate of the field of 50 Oe/s. Two groups of samples were measured. An MgB<sub>2</sub> pellet was prepared by reacting magnesium and boron powders at 850°C under isostatic pressure of 150 MPa for 1 hour. The density of thus prepared pellet was 1.9 g/cm<sup>3</sup>. The  $T_c$  of 38.9K was obtained from measurements of ac susceptibility, with the transition width lower than 1K. The pellet was cut into a rectangular rod and measured. Subsequent measurements were performed after reducing all three dimensions of the same sample by 20%, with their proportions remaining the same. In this way, any geometrical effects on our results were eliminated. The sample dimensions are shown in Table 1. The field was applied along the longest dimension of the sample, x. The second group of samples were round iron sheathed  $MgB_2$  wires, prepared by powder in tube method, described elsewhere <sup>4</sup>. The iron sheath was removed before the measurements. Two groups of the wires were measured (Table 1). In the group D, the length of the wire was kept constant and its diameter was decreased for each of the measurements. In the group Z, the diameter was kept constant and its length was decreased. For each of the measurements, the field was applied along the cylindrical *z*-axis of the wire. Therefore, the dimension parallel to the field was varied in the group Z. On the other hand, the dimension perpendicular to the field was varied in the group D.

Figure 1 shows the field dependence of  $J_c$  at 5 and 20K, for a series of samples with subsequently decreasing volume. The  $J_c$  for low fields at 5K could not be calculated because of the flux jumps<sup>5</sup>. There was a strong influence of the sample size on  $J_c(H)$  as well as on the zero-field  $J_c$  ( $J_{c0}$ ). For example, the  $J_c$  dropped by more than two orders of magnitude at 7 T and 5K when the sample dimensions decreased from 25 to 0.26mm<sup>3</sup>. This was accompanied by an increase of  $J_{c0}$  as the sample size decreased.

The increase of  $H_{irr}$  with the volume (V) of the sample is shown in Figure 2 for T = 20K.  $H_{irr}$  increased very fast with V for V < 3.5mm<sup>3</sup>, followed by a much more gradual increase for V > 3.5mm<sup>3</sup>. The transition between these two regimes occurred at the same volume for all temperatures, however  $H_{irr}$  vs. V for different temperatures were not scaleable to a unique curve. Inset to Figure 2 shows the field dependence of  $J_c$  for two different MgB<sub>2</sub> samples at 5K, obtained from magnetic and transport measurements. The voltage contacts in transport measurements were at a distance of 1 cm, whereas the sample size for magnetic measurements was  $3.5 \times 3 \times 0.5 \text{ mm}^3$ . There is a good agreement between the two types of measurements.

Figure 3 shows the dependence of  $J_{c0}$  on the sample volume. Inset to Figure 3 shows the field dependence of  $J_c$ , detailing the increase of  $J_{c0}$  as the sample volume was decreased. Normalising  $J_{c0}$  to its value at  $V=12.8 \text{ mm}^3$ , the experimental points obtained at 10, 20 and 30 K overlapped. As the sample volume decreased from 25 to 6.9 mm<sup>3</sup>, the value of  $J_{c0}$  increased by only 10%. However, the increase of about 60 % of the initial  $J_{c0}$  was obtained as the volume decreased from 6.9 to 0.25 mm<sup>3</sup>. It was difficult to decrease the volume below this value, because of the sample fragility. However, the dependence of  $J_{c0}$  on V was progressively stronger as V decreased, and multiple increase of thus calculated  $J_{c0}$  can be expected for smaller volumes. This implies that the reported high values of  $J_{c0}$  for samples with V < 1mm<sup>3</sup> should not be directly compared with  $J_{c0}$  obtained for larger samples.

Figure 4 shows the dependence of  $J_{c0}$  on the length of the wire (samples Z), therefore on the dimension parallel to magnetic field.  $J_{c0}$  again decreases with the length of the sample. Inset to Figure 4 shows the dependence of  $J_{c0}$  on the diameter of the round wire (samples D), with the field along its z-axis.  $J_{c0}$  also decreases with the sample diameter. This excludes the change of the electrical field (*E*) as the origin for the sample size dependence of  $J_{c0}$ . Namely, for a cylindrical sample with magnetic field along its z-axis:  $E = D/2^* dB/dt$  on its surface, where *D* is the diameter of the sample. However, our measurements show that  $J_{c0}$  also changes with the length of the cylinder (Fig.4), where *E* remains constant.

The explanation for the sample size dependence of  $J_{c0}$  should instead be sought in the terms of sample homogeneity. The density of bulk MgB<sub>2</sub> is quite smaller than the density of MgB<sub>2</sub> crystal (about 70%). The bulk MgB<sub>2</sub> consists of a matrix of well-connected superconducting grains. Voids of the size of a few tens of micrometers are scattered through the matrix<sup>6</sup>, dividing it into cells of agglomerated grains between the voids connected by narrow bridges. The screening currents flowing around the sample are concentrated in these bridges, resulting in an increased current density in the bridges. The current transport through the bridges limits the overall screening of the whole sample. The cells and bridges consist of

the same material and have the same  $J_{c0}$ . However, the cross-sectional area for the current flow in the cells is larger than for the current in the narrow bridges. Because of this, extra screening is possible, with the current loops closing around the cells. This resembles the interand intra- grain current in high-temperature superconductors, with a significant difference that the bridges between the cells in high quality MgB<sub>2</sub> samples are not Josephson junctions. The sample size dependence of magnetically obtained  $J_c$  can be explained by a model devised for high-temperature superconductors <sup>7</sup>. Approximating the shape of the sample and cells by round cylinders, the reversible magnetic moment obtained from the hysteresis loop is <sup>7</sup>:

$$\Delta m = \left(afJ_{ca} + DJ_{cb}\right)2V/3,\tag{1}$$

where  $J_{ca}$  and  $J_{cb}$  are the current densities of the small loops around the cells and of the overall sample screening, respectively. D is the diameter of the sample, whereas a and f are the typical diameter of the cells and their filling factor, respectively.  $J_{ca}$  and  $J_{cb}$  are not critical current densities of the MgB<sub>2</sub> crystals.  $J_{ca}$  is restricted by the vortex pinning in the crystals and by the bottlenecks to the current flow between MgB<sub>2</sub> crystals inside the cells, whereas  $J_{cb}$ is additionally restricted by the bottlenecks created by the voids between the cells. This gives  $J_{ca} > J_{cb}$ . The contribution of  $J_{ca}$  to  $\Delta m$  is negligible for large samples (D >> a in Eq. (1)), resulting in a sample size independent  $J_c$  equal to  $J_{cb}$ . With lowering the sample size, the contribution of  $J_{ca}$  starts increasing. Further, the length scale used for calculating  $J_c$  in the critical state model (i.e. D) starts approaching the size of the cells. Because of this, and because  $J_{ca} > J_{cb}$ , thus calculated value of  $J_c$  increases with the decrease of the sample size. As the sample approaches the size of the cells,  $J_{cb}$  decreases because the bridges between the cells are broken up. Finally, for D = a, the calculated  $J_c$  equals  $J_{ca}$ . The simple critical state model cannot be used to calculate  $J_c$  when both  $J_{ca}$  and  $J_{cb}$  contribute significantly to  $\Delta m$ . The fit of normalised  $J_{c0}$  vs. V, using Eq. (1) for  $\Delta m$  in the critical state model with  $J_{cb}/J_{ca} = 1/3$ and  $af = 25 \mu m$ , is shown by solid line in Fig. 3. Microscopic examination of the samples shows that the average size of the cells is about 35  $\mu$ m and the density of the sample gives f =0.7, which results in  $af = 25 \,\mu\text{m}$ . The value of  $J_{cb}/J_{ca} = 1/3$  was obtained by the fitting. This is a sensible value, considering that the difference between  $J_{ca}$  and  $J_{cb}$  arises because of the bottlenecks to the current flow between the cells.

Figures 2 and 3 show that  $J_{c0}$  and  $H_{irr}$  have the opposite dependence on the sample volume. This is seemingly contradicting, because larger  $H_{irr}$  signifies stronger vortex pinning and consequently, a larger  $J_{c0}$ . However, Figure 1 shows that the values of  $H_{irr}$  were obtained from the part of the  $J_c(H)$  curve exhibiting a steep decrease of  $J_c$ . This step in  $J_c(H)$  was explained by breaking down of the sample into separated screening islands<sup>5</sup>. These islands were agglomerates of crystals and their size in the first bulk MgB<sub>2</sub> was about 200µm<sup>5</sup>. TEM examination of the more advanced samples reveals smaller agglomerates, of about 200nm, consisting of sub-grains of the size of 10 nm<sup>8</sup>. Our preliminary measurements indicate the size of these screening islands for the samples reported here of about 100 nm. This indicates that the sample size dependence of  $H_{irr}$  in Fig.2 is an artefact of the magnetic breakdown into ~100 nm large agglomerates of grains inside the cells. Larger samples require a larger field in order to obtain full decoupling of the islands closer to the centre of the sample. This is manifested in an increase of the field at which the step in  $J_c(H)$  occurs, and thus of the apparent  $H_{irr}$ , with the sample size.

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Table 1: The dimensions of the samples measured. Samples a-h are rectangular pellets whose all three dimensions (x, y, z) were reduces by 20% before each subsequent measurement. The field was oriented along x. Samples Z are round wires whose length was reduced before each subsequent measurement. The field was along the length of the samples, i.e. along the cylindrical z-axis. Samples D were round wires with constant length, but the diameter was reduced before each subsequent measurement. The field was also along the cylindrical z-axis.

sample	x (mm)	y(mm)	z (mm)	$V (mm^3)$
a	7.15	3.27	1.07	25.01
b	5.72	2.62	0.86	12.87
c	4.65	2.12	0.7	6.90
d	3.64	1.68	0.57	3.49
e	2.92	1.34	0.46	1.78
f	2.29	1.08	0.36	0.89
g	1.87	0.85	0.29	0.46
1	1 40	0.0	0.04	0.02
h	1.42	0.68	0.24	0.23
h sample	1.42 Diamete	0.68 r (mm)	0.24 Ler	0.25 1gth (mm)
h sample D1	1.42 Diamete 1.54	0.68 r (mm)	0.24 Ler 3.9	0.25 ngth (mm) 1
h sample D1 D2	1.42 Diamete 1.54 1.23	0.68 r (mm)	0.24 Ler 3.9 3.9	0.25 ngth (mm) 1 1
h sample D1 D2 D3	1.42    Diamete    1.54    1.23    0.93	0.68 r (mm)	0.24 Ler 3.9 3.9 3.9	0.25 ngth (mm) 1 1 1
h sample D1 D2 D3 Z1	1.42 Diamete 1.54 1.23 0.93 1.54	0.68 r (mm)	0.24 Ler 3.9 3.9 3.9 6.2	0.25 ngth (mm) 1 1 1 3
n sample D1 D2 D3 Z1 Z2	1.42      Diamete      1.54      1.23      0.93      1.54      1.54	r (mm)	0.24 Ler 3.9 3.9 3.9 6.2 3.9	0.25 ngth (mm) 1 1 1 1 3 1 1 1 3 1
h sample D1 D2 D3 Z1 Z2 Z3	1.42      Diamete      1.54      1.23      0.93      1.54      1.54      1.54	r (mm)	0.24 Ler 3.9 3.9 6.2 3.9 6.2 3.9 1.9	0.25 ngth (mm) 1 1 1 3 1 5

Figure 1: Field dependence of  $J_c$  for samples of different size (Table 1).



Figure 2: Dependence of the irreversibility field on the sample volume for the rectangular samples a-h at T=20K. Inset: Field dependence of  $J_c$  for MgB<sub>2</sub> samples at 5K, obtained from magnetic (solid line) and transport (open symbols) measurements.



Figure 3: Dependence of the normalised  $J_{c0}$  on the sample volume for samples a-h (Table 1).  $J_{c0}$  for T = 10, 20 and 30 K was normalised to its value for  $V = 12.87 \text{ mm}^3$ . Solid line is fit with Eq.(1). Inset: Field dependence of  $J_c$  showing the increase of  $J_{c0}$  as the volume decreases.



Figure 4: Dependence of  $J_{c0}$  on the sample length of the MgB<sub>2</sub> wire, where the diameter of the wire did not change (samples Z in Table 1). Inset: Dependence of  $J_{c0}$  on the diameter of the MgB<sub>2</sub> wire, with fixed wire length (samples D in Table 1).



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