

Structure model index does not measure rods and plates in trabecular bone

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Conflict of interest statement

The authors declare a potential conflict of interest and state it below.

Dr Salmon is employed by Bruker micro-CT, which is a manufacturer of X-ray microtomography equipment and publisher of analytical software that was used in this work.

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25Abstract

Structure model index (SMI) is widely used to measure rods and plates in trabecular bone. It exploits the change in surface curvature that occurs as a structure varies from spherical (SMI = 4), to cylindrical (SMI = 3) to planar (SMI = 0). The most important assumption underlying SMI is that the entire bone surface is convex and that the curvature differential is positive at all points on the surface. 30 The intricate connections within the trabecular continuum suggest that a high proportion of the surface could be concave, violating the assumption of convexity and producing regions of negative differential. We implemented SMI in the BoneJ plugin and included the ability to measure the amounts of surface that increased or decreased in area after surface mesh dilation, and the ability to visualize concave and convex regions. We measured SMI and its positive (SMI⁺) and negative (SMI⁻) 35components, bone volume fraction (BV/TV), the fraction of the surface that is concave (CF), and mean ellipsoid factor (EF) in trabecular bone using 38 X-ray microtomography (XMT) images from a rat ovariectomy model of sex steroid rescue of bone loss, and 169 XMT images from a broad selection of 87 species' femora (mammals, birds, and a crocodile). We simulated bone resorption by eroding an image of elephant trabeculae and recording SMI and BV/TV at each erosion step. Up to 4070%, and rarely less than 20%, of the trabecular surface is concave (CF 0.155 - 0.700). SMI is unavoidably influenced by aberrations induced by SMI, which is strongly correlated with BV/TV

and CF. The plate-to-rod transition in bone loss is an erroneous observation resulting from the close and artefactual relationship between SMI and BV/TV. SMI cannot discern between the distinctive trabecular geometries typical of mammalian and avian bone, whereas EF clearly detects birds' more 45plate-like trabeculae. EF is free from confounding relationships with BV/TV and CF. SMI results reported in the literature should be treated with suspicion. We propose that EF should be used instead of SMI for measurements of rods and plates in trabecular bone.

1. Introduction

Since Hildebrand & Rüegsegger published their structure model index (SMI) method in 1997 (1) it sohas become the de facto standard for measuring the rod- and plate-like geometry in 3-dimensional trabecular bone images. 'Rods' are regions of trabecular bone characterized by being elongated and cylindrical, while 'plates' are extensive, flatter regions. The relative proportion of rods to plates in trabecular bone is thought to be important for bone's mechanical competence, with plates considered to be mechanically superior to rods. SMI is straightforward to implement and is built into X-ray 55microtomography analytical software, including that of commercial vendors (notably SkyScan and SCANCO) and the free BoneJ plugin for ImageJ (2). The principle of SMI is very simple: it compares the surface area of a structure before and after an infinitesimal dilation, to its volume. For primitive, convex geometries such as flat planes (SMI = 0), cylindrical rods (SMI = 3) and spheres (SMI = 4), SMI works well. Unfortunately, SMI does not account for concave surfaces, possibly 60making it unsuitable for use on bone geometries. For trabecular bone to form a network of two distinct and continuous phases, bone and marrow space, it must contain abundant concave surfaces joining the elements in addition to convex surfaces forming the elements themselves. Concave surfaces can exist as saddle curves (concave in one direction and convex in the other), troughs (concave in one direction and linear in the other) or bowls (concave in two orthogonal planes). To 65calculate SMI, a mesh of triangles is fitted to the bone surface and its area is calculated as the sum of the areas of all the triangles (S). The mesh is then dilated a short distance (r) away from the surface in the direction of the triangles' vertex normals and surface area measured again. An approximal surface area derivative is calculated by dividing the change in surface area (S') by r, and multiplied with bone volume (V) to give a final SMI value (Equation 1).

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$$SMI = 6 \cdot \frac{\frac{S'}{r} \cdot V}{S^2} \qquad (1)$$

Crucially, triangles on concave surfaces shrink in area when the volume is dilated, leading to a negative change in area and a negative contribution to *S'*. The negative contribution is an aberration from the mathematical and conceptual formulation of SMI, the presence of which contaminates the 75 final SMI determination.

Because SMI is set up to report a single figure summarizing an entire bone surface, an SMI of 0 (ostensibly plate-like) can result from a surface that has an SMI of +1 on its convex portions and -1on its concave portions. Sometimes, the SMI sum is less than its defined minimum bound of 0(3-8015), which casts serious doubt upon the biological interpretation that is possible from any SMI result. The limitations in SMI have been known since its inception: Hildebrand and Rüegsegger (1997) wrote that "the intersections between structure elements, e.g. between rods and plates, are not accounted for", and their Figure 2 displays a consistent (but not discussed) negative relationship between SMI and bone volume fraction (BV/TV) (1). Despite these inherent shortcomings, SMI has steen used as core experimental evidence by the bone community, having been cited over 800 times to date according to Google Scholar¹. SMI data have been used in support of denosumab (16), bisphosphonates (3,17-21), teriparatide (21-24), strontium ranelate (25), rosiglitazone (26), propranolol (27), and newly discovered molecules (28,29) as treatments to improve bone architecture in human patients. It is well known that SMI is strongly confounded by BV/TV (1,30)(r = -0.80)90(31,32), r = -0.76, -0.93 (33), $R^2 = 0.86$ (34), $R^2 = 0.94$ (10), $R^2 = 0.80$ (4), $R^2 = 0.91$ (35)), so that comparisons of SMI values can be valid only if BV/TV is identical among specimens. This raises problems for studies where BV/TV variation is a prominent feature, for example those of mechanical (un)loading, osteoporosis or ovariectomy animal models. Our concern is that the pervasive use and misunderstanding of SMI has lead to many erroneous conclusions relating to plate-rod transitions in 95bone physiology and pathology. Until recently there has been no widely-available, validated and meaningful alternative to SMI, and so its use has continued despite its severe limitations.

Ellipsoid factor (EF) has been developed as a method for measuring rod- and plate-like geometry, independent of other geometric parameters, by fitting maximal inscribed ellipsoids inside 1003-dimensional continua (36). Early experience suggests that EF effectively identifies rods and plates directly by fitting elongated (prolate) or flattened (oblate) ellipsoids respectively, and identifies transitional regions with rounder, intermediate ellipsoids. EF at each point is calculated from the ellipsoid of greatest volume that encloses the point and that fits inside the structure. EF is calculated from the maximal ellipsoid's semi-axes a, b, c:

$$a \le b \le c, EF = \frac{a}{b} - \frac{b}{c}$$
 (2)

Bony plates are approximated by discus-shaped ellipsoids, where $a \ll b \le c$ and $EF \rightarrow -1$; rods are approximated by javelin-shaped ellipsoids where $a \le b \ll c$ and $EF \rightarrow 1$; while transitional regions have less extreme geometry and are rugby ball-shaped where $a \le b \le c$ and $EF \rightarrow 0$. A special class of ellipsoid exists for which a/b = b/c, where $a = qb = q^2c$; spheres have q = 1.

110We aim to investigate the source of the relationship between SMI and BV/TV, to determine whether SMI measures rods and plates in real trabecular bone geometries, and to quantify the amount of concave bone surface typically present in trabecular bone. Additionally, we use this opportunity to

⁵¹https://scholar.google.com/scholar?hl=en&cites=4353090427928514643

perform further testing of BoneJ's new Ellipsoid Factor feature to determine whether it is free of significant confounding effects and could be used in place of SMI when rod/plate geometry needs to 115be measured.

2. Materials and Methods

Two image data sets from the authors' previous work were analysed using SkyScan's CTAn (v1.4; Bruker, Kontich, Belgium) and BoneJ (v1.4.1²; bonej.org (2)) in ImageJ (v1.49q (37)). The data 120comprised X-ray microtomographic (XMT) images of trabecular bone in rat femoral condyles (n = 38) from a study investigating sex steroid rescue of ovariectomy-induced bone loss (38), and XMT images (n = 169) of trabecular bone in the femoral head and/or condyle from 87 species (69 mammals, 17 birds, and one crocodile), made for a study of trabecular bone scaling (39). The rat images were included to provide data from a large number of similar geometries formed under 125experimental conditions relevant to typical small animal studies on trabecular bone, which would test the response of SMI to generalized bone resorption and apposition. The taxonomically-broad images were included to provide a diverse range of naturally-occurring trabecular bone geometries, which would test the response of SMI to many different real trabeculae. Specimen data are provided as supplementary information. All procedures on the rats were approved by the ethics committee at the 130University of Gothenburg and conformed to the National Institutes of Health Guide for the Care and Use of Laboratory Animals.

Rat condyles were imaged at 7.66 μm isotropic pixel spacing in a SkyScan 1072 XMT scanner (Bruker, Kontich, Belgium). The interspecies trabecular series was imaged at 3.4–15 μm isotropic pixel spacing (depending on specimen size) in an X-Tek HMX ST 225 XMT scanner (Nikon 135Metrology, Tring, UK). Full details of image acquisition can be found in the original manuscripts (38,39). The rat trabeculae were selected by manually drawing a conforming volume of interest distal to the growth plate that excluded cortical bone. The interspecies images were cropped down to cuboid stacks containing trabecular bone and marrow only. Binary images were produced by automatic thresholding with ImageJ's default IsoData algorithm (interspecies) or an adaptive local 140thresholding algorithm (rats) (40).

The rat image series was analysed using CTAn and again with BoneJ to generate a comparison of their SMI implementations. BV/TV was measured on the rat bones in CTAn. The interspecies series was analysed solely with BoneJ. BoneJ has the unique feature of calculating the positive (SMI⁺) and negative (SMI⁻) components of SMI by determining the triangles that increase or decrease in area, 145respectively, during surface mesh dilation. The SMI equation (1) can be expanded into each triangle's contribution (*s'*) to the overall change in surface area (*S'*)

$$SMI = 6 \cdot \frac{V}{r} \cdot \left(\frac{s'_1}{S^2} + \frac{s'_2}{S^2} + \frac{s'_3}{S^2} + \dots \frac{s'_n}{S^2}\right)$$
(3)

Grouping of the positive (t') and negative (u') values of s' allows calculation of SMI⁺ and SMI⁻ respectively

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$$SMI^{+} = 6 \cdot \frac{V}{r} \cdot \left(\frac{t'_{1}}{S^{2}} + \frac{t'_{2}}{S^{2}} + \frac{t'_{3}}{S^{2}} + \dots + \frac{t'_{p}}{S^{2}}\right) \quad , \quad SMI^{-} = 6 \cdot \frac{V}{r} \cdot \left(\frac{u'_{1}}{S^{2}} + \frac{u'_{2}}{S^{2}} + \frac{u'_{3}}{S^{2}} + \dots + \frac{u'_{q}}{S^{2}}\right) \quad (4)$$

And it follows that

$$SMI = SMI^{+} + SMI^{-}$$
(5)

BoneJ displays in 3D the surface mesh with triangles color-coded according to the sign and magnitude of s' relative to individual triangle area. The proportion of the surface area that is concave 155(the 'concave fraction', CF) can be calculated as the proportion of the total surface area (S) covered by triangles that decrease in area during mesh dilation (U)

$$CF = \frac{U}{S}$$
 (6)

Full details of BoneJ's SMI implementation can be read in the StructureModelIndex class in BoneJ's source code. Meshing was performed according to the standard marching cubes algorithm (41) as 160implemented in the ImageJ 3D Viewer (42) on binary images with a threshold of 128, voxel resampling of 3 and mesh smoothing of 0.5.

Ellipsoid factor was implemented in BoneJ with some minor performance enhancements on its initial release (36). Briefly, for each point of the structure's medial axis, a small ellipsoid is seeded and iteratively dilated, rotated and translated slightly until no further increase in volume is achieved. 165Then the largest ellipsoid containing each point in the structure is determined, and the EF calculated for that point. Mean EF values summarizing all the foreground pixels in each image were calculated and used for comparisons.

To simulate the changes in trabecular geometry during generalized bone resorption, a single binary stack of trabecular bone from an elephant's femoral head (chosen for having thick trabeculae and 170relatively high BV/TV) was repeatedly eroded by one pixel-width across the entire bone surface with BoneJ's Erode 3D, and SMI, SMI⁺, SMI⁻ and BV/TV measured at each step.

Pairwise comparisons were performed in R (v3.0.2 (43)) using its lm() function for linear regression. Where curved relationships were apparent in the scatter plots, quadratic curves were fitted. Quadratic fits for SMI⁻ were forced to intercept 0, because when CF is 0, SMI⁻ must be 0. No adjustment was 175made for multiple comparisons because we wished to test specific pairwise hypotheses, rather than gather significant results from a table of post-hoc comparisons, or to develop a model with multiple variables and a single outcome. We also expect a degree of multicollinearity (e.g. between SMI, BV/TV and concave fraction) and are seeking to define it rather than to avoid or correct for it.

To determine whether SMI and EF can discriminate between birds' and mammals' distinctive 180trabecular geometries, we applied a Wilcoxon-Mann-Whitney test (R's wilcoxon.test() method) to SMI, BV/TV, CF and EF results, with data categorised as 'Mammalian' or 'Avian'.

3. Results

Color-coded surface images (Figure 1) show that SMI⁺ regions (yellow) localize to rod-like features, 185ridges and saddle curves with a strong convex component. SMI⁻ regions (blue) localize to depressions and junction regions.

SMI values are highly correlated between CTAn and BoneJ implementations (Figure 2), so BoneJ's results can be placed in the context of those published using commercial software with reasonable confidence.

190Strong, significant correlations implying confounded relationships, and weak correlations implying no relationship between variables, were detected in both rat (Figure 3) and interspecies (Figure 4) bone image data (Table 1). Measurements from interspecies data were substantially more dispersed than those from the rat data, evidenced by much broader spread of points on scatter plots, lower correlation coefficients and higher *p*-values. SMI was strongly negatively correlated with BV/TV

195(Figure 3A, 4A) and CF (Figure 3B, 4B), and CF was strongly positively correlated with BV/TV (Figure 3E, 4E), indicating that high BV/TV structures tend to have high CF and consequently low SMI, due to an increased contribution from SMI⁻. SMI⁺ is independent of BV/TV in the interspecies data (*R*² < 0.001). EF is nearly independent of concave fraction, BV/TV and SMI, with very low correlations for rat and interspecies data (Table 1). EF is weakly correlated with SMI⁺ in the rat data, 200however the distribution of the data points (Figure 3F) and lack of relationship between EF and SMI⁺ in the interspecies data cast doubt on the ability to interpret this any further.

There was no significant difference in SMI between mammal and bird trabecular bone (p = 0.65), whereas EF and BV/TV were significantly different (p < 0.001) between mammals and birds (Figure 4C, D). Concave fraction is not significantly different between birds and mammals (p = 0.09) (Figure 2054D,E), perhaps in part explaining the lack of discriminating ability of SMI.

Response variable	Explanatory variable	a , for $f(x^a)$	<i>R</i> ²	р
Rat image data				
SMI	BV/TV	1	0.985	< 0.001
	CF	1	0.978	< 0.001
	EF	1	0.088	0.039
SMI ⁺	BV/TV	2	0.943	< 0.001
	CF	2	0.968	< 0.001
	EF	1	0.268	0.001
SMI	BV/TV	2	0.995	< 0.001
	CF	2	0.989	< 0.001
	EF	1	0.003	0.300
EF	BV/TV	1	0.093	0.035
	CF	1	0.147	0.010
CF	BV/TV	1	0.974	< 0.001
Interspecies image d	ata			
SMI	BV/TV	1	0.249	< 0.001
	CF	1	0.555	< 0.001
	EF	1	0.096	< 0.001
SMI ⁺	BV/TV	1	< 0.001	0.889
	CF	2	0.941	< 0.001
	EF	1	0.060	0.001
SMI ⁻	BV/TV	2	0.793	< 0.001
	CF	2	0.761	< 0.001
	EF	1	0.043	0.004
EF (mammal)	BV/TV	1	< 0.001	0.821
	CF	1	0.144	< 0.001
EF (bird)	BV/TV	1	< 0.001	0.537
	CF	1	0.070	0.074
CF (mammal)	BV/TV	1	0.262	< 0.001
CF (bird)	BV/TV	1	0.288	0.001

Table 1. Regression coefficients of determination (R^2) and significance levels p of the regressions for linear (a = 1) and quadratic (a = 2) fits to data plotted in Figure 3 and 4.

4. Discussion

210SMI is very strongly confounded by BV/TV through the fraction of the surface that is concave, and the magnitude of the concavity. Results from our simulation and two large datasets raise the

possibility that SMI does not function as intended when applied to real bone structures, and that published SMI results should not be used for assessment of plate/rod geometry. A very common interpretation of SMI results is that decreasing BV/TV is accompanied by a trend toward rod-like

215trabeculae, but this 'trend' is merely an artefact of the design and implementation of SMI. Many studies show plots of SMI and BV/TV side by side indicating how the negative correlation can be missed and presented as though the variables are independent (9,14,19,26,27,44–53). If a real relationship exists between decreasing BV/TV and plate to rod transition, SMI is too biased by concave fraction and BV/TV to measure it. A shape measure that is independent of BV/TV, such as

220EF, should be used instead. Because SMI does not measure rod and plate geometry in real bone structures, prior conclusions based on SMI data are at best highly suspect. We propose that past studies in which SMI results were key data are reconsidered in the light of our new findings. New studies should not use SMI.

225SMI functions as intended only in a very small set of cases when SMI⁻ approaches 0. This occurs in artificial test images of spheres, rods and plates, such as used by BoneJ in its JUnit tests, and in bone structures with unusually low BV/TV and CF. When concave fraction approaches 0, SMI⁻ also approaches 0 and so the SMI sum nearly equals SMI⁺. The independence of SMI⁺ from BV/TV and the design of the SMI algorithm suggest that SMI⁺ could indeed measure rods and plates. 230Unfortunately, the original description of SMI (1) did not account for the very strong effect of SMIon the final SMI value. To be able to interpret SMI properly, it must be broken into its positive and negative components and read alongside concave fraction. This is the first study reporting the concave fraction of bone surface, however CF has little obvious use apart from explaining why SMI is so strongly related to BV/TV. As BV/TV decreases through thinning of trabeculae, concave 235 fraction tends to decrease in concert. SMI is strongly related to CF because as because as CF increases the contribution of SMI⁻ increases, and necessarily SMI⁺ decreases. This effect is clearer in the interspecies data than the rat data, because the interspecies data have a much weaker relation between CF and BV/TV than the rat data so their SMI versus BV/TV and SMI versus concave fraction relations are much less collinear. It also relates to geometry because it is possible to vary 240BV/TV without changing concave fraction, for example a bird to mammalian transition could be modeled by packing more parallel plates of the same thickness into the same volume, increasing BV/TV while concave fraction and SMI remain the same. Readers are invited to check their image data visually for contamination by concave surfaces using the 3D option in BoneJ's SMI implementation (Figure 1).

245The fits produced on the rat data are very much tighter than those on the interspecies data, perhaps reflecting a common underlying trabecular geometry that has varied only by thickening and thinning of elements after ovariectomy and sex steroid treatment. In contrast, trabecular bone geometry varies tremendously among species. Larger mammals, cheetah and primates tend to form extensive intra-trabecular osteonal systems (39) that create large areas of tightly concave surface, which can be 250associated with decreased SMI (22). Birds tend towards lower BV/TV (39) and more defined plates and fine rods than mammals (Figure 1A,B). The failure of SMI to detect a significant difference between these disparate classes of animals demonstrates that it cannot be relied upon to identify even

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SMI failure analysis

the most major differences in trabecular architecture. The interspecies data help to capture a broad parameter space within which the range of possible SMI, BV/TV, concave fraction and EF values ²⁵⁵may lie. The rat data illustrate the relationships between variables in a scenario with direct relevance to preclinical bone research.

The very close correlation between BV/TV and SMI in our rat and simulation data could easily lead the naïve researcher to the common conclusion that decreases in BV/TV were accompanied by a 260dramatic shift from plate-like (SMI = 0) to rod-like (SMI > 2) trabeculae. However, it is clear when SMI is teased out into its positive and negative components, and after its relationship with concave fraction is exposed, that it is only the increasing contribution of SMI⁻ that is responsible for the apparent linkage between SMI and BV/TV, and not a plate-to-rod change in bone geometry. Mean EF does vary slightly as a function of BV/TV, but not consistently: the ovariectomized rats have a very 265slightly increased (more rod-like) EF, while all the other treatment groups have a very similar EF to the sham operated groups. The interspecies data show no relationship between EF and BV/TV and a much greater range of EF values than the rat data, reflective of the greater range of geometries present in the broad taxonomic sample. This is in clear contrast to the strong, negative, linear relationship between SMI and BV/TV, which does not relate to the real rod- or plate-like geometry of 270the bone structure. Increased apparent material properties associated with a rod-to-plate transition measured with SMI (10,13,17,18,26,34,53-56) can be explained by the close and artefactual relationship between SMI and BV/TV and the latter's strong effect on volumetric material properties (12,14,33,57,58).

EF lacks much bias or confounding relationship with BV/TV and concave fraction, but is 275computationally much more expensive than SMI, taking hours to days to process 1000 × 1000 × 1000 pixel images on a dual CPU, 24-core workstation (Dell T7600). Local identification of EF values allows determination of the structural source of EF summary values because individual strongly rod- or plate-like features can be visualized in the 2D stack slices or in a 3D rendering. Visualizing the spatial distribution of EF values increases confidence that the ellipsoid-fitting 280algorithm is correctly identifying geometries in the input image. The current implementation uses a field of 100 surface points that become relatively more sparse as the ellipsoid grows, which can mean that small features, particularly intratrabecular osteonal canals, can be ignored by the optimization algorithm. This has the effect of finding the dominant local structures but is not analytically correct. A version that uses scan-converted ellipses has shown in testing to be much more accurate but carries 285a significant processing time penalty in its current state and is not ready for release.

SMI relies upon generation of a surface mesh from 3D pixel data, which is a step that can vary by meshing algorithm implementation or by user-controlled aspects such as averaging compared to feature size. Mesh generation is a variable that is difficult to control because the smoothing and downsampling necessary to generate a smooth mesh might remove fine surface features. Even with 290downsampling and smoothing aliasing artefacts are visible as stripes in the surface. The relatively higher SMI values calculated by BoneJ than by CTAn may have resulted from a systematic difference in mesh creation. Mesh creation is a one-pass operation and so it should in principle scale linearly with increasing data size.

Alternative approaches to determining plate and rod architecture involve segmentation of the 295trabecular continuum into discrete elements, then determining the geometric qualities of each element separately (59,60). This approach leads to binary classification of pixels into 'rod' or 'plate' with no recognition of transitional or junction regions. Recent work by the inventors of ITS indicates the ability of individual trabecula segmentation (ITS)-based finite element models to predict the anisotropic mechanical properties of human trabecular bone (61). An independent group found no soosignificant contribution of ITS-based metrics to apparent material properties, which were explained almost entirely by BV/TV with a small (~10%) but significant contribution from fabric anisotropy measured by mean intercept length (MIL) (58). The ITS determination of the fraction of bone that is 'plate' (pBV/BV) is strongly negatively correlated with SMI (r = -0.81) (60). This is somewhat concerning because it means that high pBV/BV values (i.e. plate-dominated volumes according to 305ITS) relate to low and ostensibly plate-like SMI values, which our current analysis leads us to believe have little meaning. This relationship might occur due to an even stronger positive correlation between pBV/BV and BV/TV (r = 0.99), and the already established negative correlation between SMI and BV/TV. ITS-based finite elements analysis is able to predict the off-axis mechanical behavior more closely than predictions based on BV/TV alone (61), lending support to the concept 310that plate and rod geometry could have a real mechanical significance. To our knowledge the ITS software is restricted by patent and not readily available as binaries or source code for others to validate. In contrast, BoneJ is open source and free for anyone to download, use, modify and redistribute.

This study exposes a broader issue of misunderstanding analysis techniques and then presenting 315their results as meaningful when they have failed to measure what they are generally accepted to measure. Implementation of methods by major vendors and their widespread usage creates an environment where a consensus may form, in isolation from proper reference to the details of the algorithm's design. This style of practice creates a danger of making false conclusions with important ramifications such as the ability of pharmaceutical or exercise interventions to improve 'bone quality'.

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Acknowledgments

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Figure legends

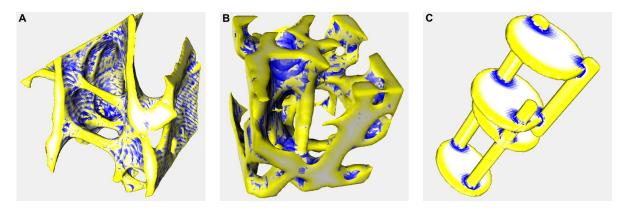


Figure 1: Surface meshes color-coded by curvature. Triangulated meshes used to calculate SMI color-coded according to whether each triangle's area enlarged (vellow), shrunk (blue) or remained 335constant (white) during mesh dilation. These images were created using the same settings as the other analyses in this manuscript (voxel averaging = 3, mesh smoothing = 0.5). Yellow and white regions correspond to convex and flat curvature respectively that contribute to SMI⁺; blue regions correspond to concave elements that contribute to SMI, artefactually decreasing SMI Image data are the same as in Doube (2015) (Figure 2) (36). (A) Trabecular bone from an emu, Dromaius novaehollandiae. 340Rods, ridges and cut edges of plates are identified in vellow indicating a positive contribution to SMI. Note the banding resulting from aliasing during mesh creation, despite pixel averaging and mesh smoothing (CF = 0.407, SMI⁺ = 1.707, SMI⁻ = -0.617, SMI = 1.090) (B) Trabecular bone from a lesser dwarf shrew. Suncus varilla. The large vertical rod in the center of the image is correctly identified in yellow, but merges into negatively curved blue regions (CF = 0.301, $SMI^+ = 2.462$, SMI^- 345= -0.493. SMI = 1.969) (C) Synthetic image of intersecting rods and plates. Rods and plate edges are correctly identified in yellow and plate surfaces are correctly identified in white. Junctions between rods and plates are identified in blue indicating negative contribution to SMI (CF = 0.152, $SMI^+=$ 2.249, SMI = -0.315, SMI = 1.933). Full details of the implementation are available in BoneJ's source code and input image stacks are available to download from http://bonei.org/ef.

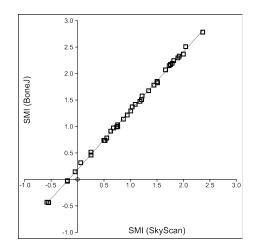


Figure 2: SMI calculation by BoneJ and SkyScan. A high level of agreement exists between BoneJ and CTAn implementations of SMI ($R^2 = 0.999$) when run on the same image data, although BoneJ 355consistently overestimates SMI relative to CTAn (SMI_{BoneJ} = $1.111 \times SMI_{SkyScan} + 0.192$).

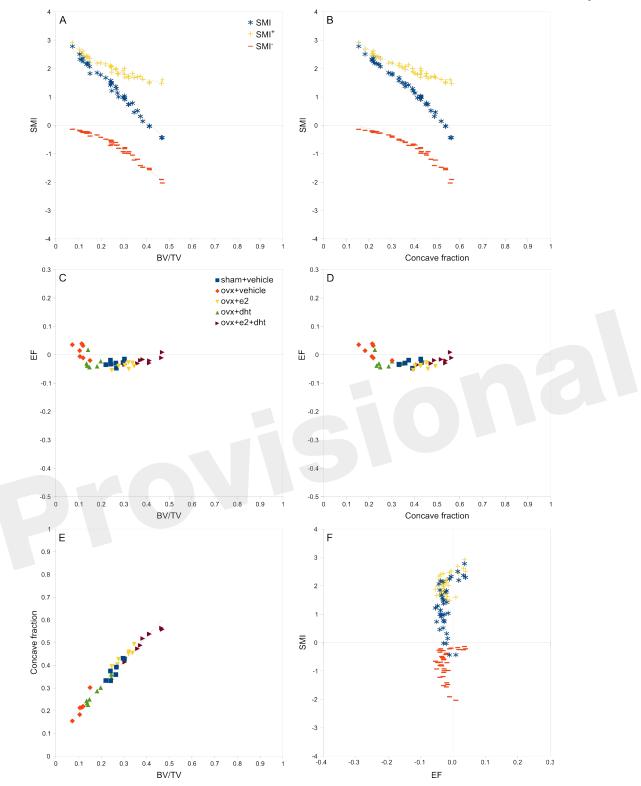


Figure 3: Correlations between parameters related to SMI – rat data. Scatterplots of pairs of parameters measured on trabeculae in rat femoral condyle images reveal strong and clear relationships between SMI, BV/TV and concave fraction (A, B, E), while EF is independent of 360BV/TV (C), concave fraction (D) and SMI (F). The linear correlation between SMI and BV/TV and between SMI and concave fraction results from the sum of SMI⁺ and SMI⁻, which have

complementary curved relations with BV/TV and concave fraction. Points are labeled according to experimental treatment in (C, D, E; ovx, ovariectomized; e2, estradiol; dht, dihydrotestosterone) and according to SMI component in (A, B F). Regression lines are plotted where $R^2 > 0.20$, and listed in 365Table 1.



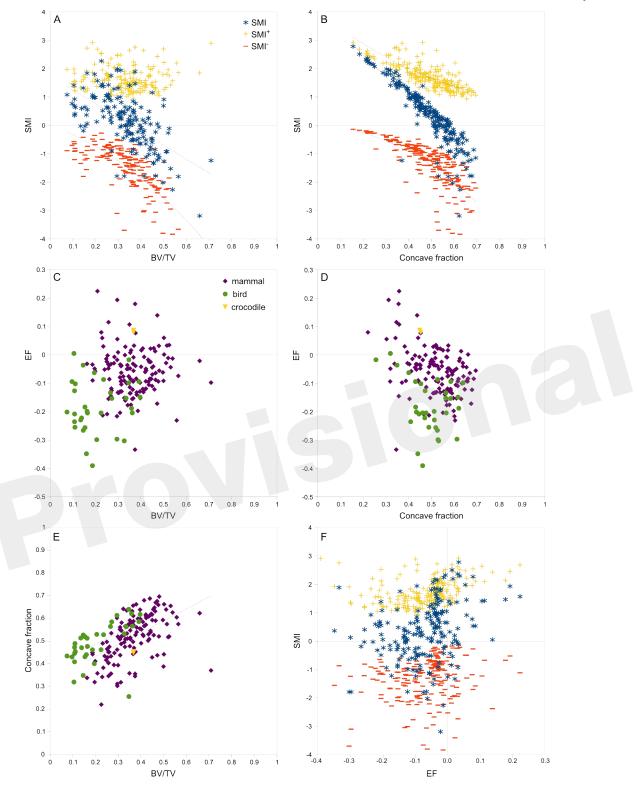


Figure 4: Correlations between parameters related to SMI – interspecies data Scatterplots of pairs of parameters measured on trabeculae in mammal, bird and crocodile femoral head and condyle 370images reveal strong and clear relationships between SMI, BV/TV and concave fraction (A, B, E). EF is nearly independent of BV/TV (C), concave fraction (D) and SMI (F) for both mammals and

birds. The linear correlation between SMI and BV/TV and between SMI and concave fraction results from the sum of SMI⁺ and SMI⁻, which have complementary curved relations with BV/TV and concave fraction. Note the much broader spread of data than in the rat data in Figure 3. Points are 375labeled according to phylogenetic taxon in (C, D, E) and according to SMI component in (A, B F). Regression lines are plotted where $R^2 > 0.20$, and listed in Table 1.

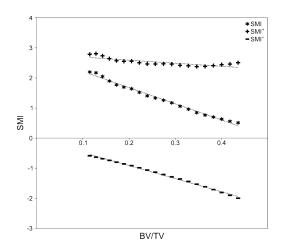


Figure 5: Simulated bone resorption of elephant trabeculae. Progressive erosion simulated bone 380resorption's effect on the SMI versus BV/TV relationship. Although there is no fundamental difference in bone architecture, SMI increases from 0.51 at BV/TV of 0.44, to 2.20 at BV/TV of 0.12 ($R^2 = 0.991$, p < 0.001). Note the strong negative correlation between SMI⁻ and BV/TV ($R^2 = 0.996$, p < 0.001), relatively stable SMI⁺ (2.38 – 2.81; $R^2 = 0.621$, p < 0.001), and the strong negative influence of SMI⁻ on SMI.

385Supplementary Material

S1 Specimen data tables containing species information and measurement results for interspecies and rat image data.

Figure 1.TIF

