

4
NAVAL POSTGRADUATE SCHOOL
Monterey, California



PODEMS - A POINT DEFENSE MISSILE
SIMULATION

by

Michael H. Redlin

March 1973

Approved for Public Release; Distribution Unlimited

FEDDOCS
D 208.14/2
NPS-57RP73031A

F204001

L 202 1412. NPS-STRP73031A 02

NAVAL POSTGRADUATE SCHOOL
Monterey, California

Rear Admiral Mason Freeman, USN
Superintendent

Milton U. Clauser
Provost

ABSTRACT

A Point Defense Missile Simulation has been developed. This report describes the concept of such a missile, the basic features of the simulation program including the integration routine and the jet reaction controllers, and provides a FORTRAN coded source program.

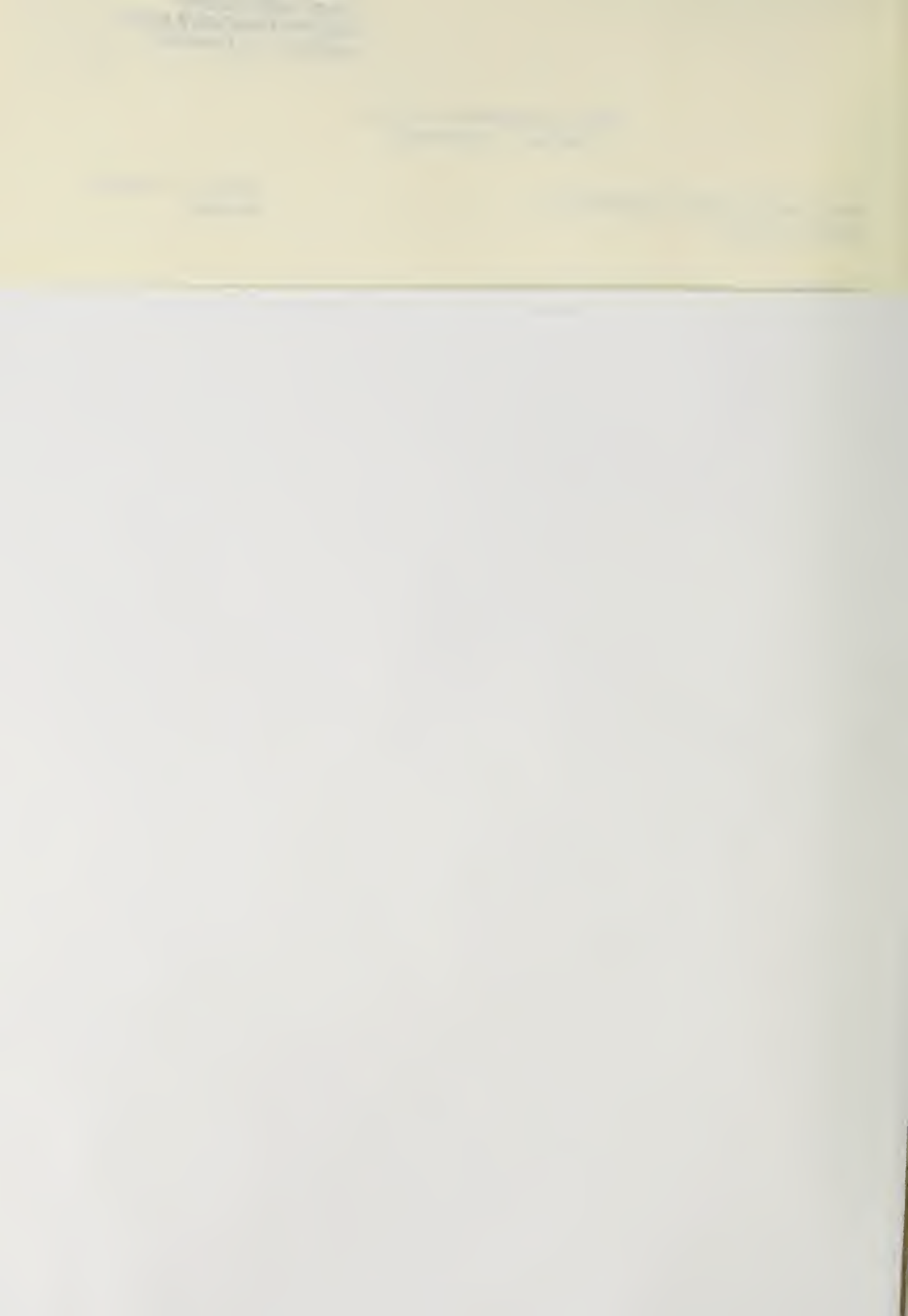


TABLE OF CONTENTS

	PAGE
I. INTRODUCTION	1
II. COMPUTER PROGRAM EXPLANATIONS	3
A. Definitions of Coordinate Systems	3
B. Missile Position and Orientation	3
C. Quaternions	5
D. Differential Equations for Rigid Body	7
E. Definition of Relative Wind Orientation	8
F. Aerodynamic Data	8
G. Integration Routine	9
H. Other Subroutines	10
REFERENCES	24
APPENDIX A - Computer Program Listing	25
APPENDIX B - Listing of Program Variables	57
INITIAL DISTRIBUTION LIST	64
FORM DD 1473	65

LIST OF SYMBOLS

c_i	Corrector for state variables at time step i
$C_{l'}$ $C_{m'}$ $C_{n'}$	Moment coefficients of baseline missile expressed in pitch axes
$C_{x'}$ $C_{y'}$ $C_{z'}$	Force coefficients of baseline missile expressed in pitch axes
d	Missile diameter, ft
e_0-e_3	Quaternion parameters
h	Step size for fast integration speed, secs
h_s	Step size for slow integration speed, secs
I_x, I_y	Longitudinal and transverse moments of inertia, slugs-ft ²
K_m, K_n	Moment amplification factors due to JRC's
K_y, K_z	Force amplification factors due to JRC's
m	Missile mass, slugs
m_i	Modified value of state variables at time step i
m'_i	Derivatives of state variables evaluated with m_i
p, q, r	Missile angular rates about body axes, rad/sec
p_i	Predicted value of state variables at time step i
r_{mT}	Range from target to missile, ft
S	Reference area, ft ²
T11-T33	Elements of transformation matrix from inertial axes to body axes
T_r	Thrust of rocket, lbs
T_{JRC}	Thrust of JRC's, lbs
u, v, w	Components of missile's inertial velocity in body axes, ft/sec

u_T, v_T, w_T	Components of total relative wind velocity in body axes, ft/sec
u_W, v_W, w_W	Components of true wind velocity in body axes, ft/sec
V	Magnitude of relative wind velocity, ft/sec
x, y, z	Body axes coordinate system
x_{mT}, y_{mT}, z_{mT}	Target position relative to missile in body axes, ft
x', y', z'	Pitch axes coordinate system
X, Y, Z	Inertial axes coordinate system
X_I, Y_I, H_I	North-south, east-west, and height inertial position of missile, ft
X_F, Y_F, Z_F	Total forces along missile body axes, lbs
X_M, Y_M, Z_M	Total moments along missile body axes, lbs-ft
X_{IT}, Y_{IT}, H_{IT}	North-south, east-west, and height inertial position of target, ft
x_{cg}	Position of missile center of gravity, ft
x_{JRC}	Position of missile JRC thrusters, ft
\tilde{y}_i, \tilde{z}_i	Predicted values of state variables at time step i
α	Missile angle of attack, degrees
ϵ	Quaternion orthogonality error
ϵ_B	Angular error between gyro spin axis and target line of sight, rad
ϵ_C	Angular error between coil housing axis and target line of sight, rad
θ, ϕ, ψ	Standard missile Euler angles, deg
θ_4	Angular error associated with seeker gimbal ring, rad
σ_A, σ_B	Target elevation and azimuth angles relative to missile axes
ϕ_1	Seeker roll angle, rad
ϕ_J	Orientation of relative wind with respect to thruster axes, deg
ϕ_W	Orientation of relative wind with respect to missile axes, deg
ψ_2	Seeker coil housing look angle, rad

ψ_3	Angular error associated with seeker gimbal ring, rad
Ω_C	Angular rotation rate of coil housing, rad/sec
Ω_{G_y}	Angular rotation rate of gyro spin axis about its y axis, rad/sec
Ω_{G_z}	Angular rotation rate of gyro spin axis about its z axis,
Ω_Y	Angular rotation rate of seeker yoke, rad/sec

LIST OF FIGURES

	PAGE
1. Definition of Missile Fixed Coordinate System	14
2. Definition of Pitch Axes Coordinate System	14
3. Relative Wind Orientation	15
4. Relative Wind Orientation With Respect to JRC Thruster Axis	16
5. C_z , vs α for $\Phi_w = 0, \pi/4, \pi/2$	17
6. C_m , vs α for $\Phi_w = 0, \pi/4, \pi/2$	18
7. K_z vs α for $\Phi_J = 0, \pi/2, \pi$	19
8. K_m vs α for $\Phi_J = 0, \pi/2, \pi$	19
9. Dual Speed Integration for One Large Step h_s .	20
10. Definitions of JRC Orientations	21
11. Definition of Target Azimuth and Elevation Angles	22
12. Definition of Missile Parameters	23

INTRODUCTION

A Point Defense Missile Simulation (PODEMS) program has been developed and this report offers a description of its basic features, structure, and requirements. Although rather straight forward in nature, this program provides the basic framework from which further simulations of increased complexity and sophistication can be easily implemented.

The concept of a point defense missile as defined by this effort can be best understood by analyzing a typical flight. The seeker of the missile initially acquires a low-altitude, high speed, incoming target. The surface-to-air missile launches vertically, and then immediately performs a rapid pitch-over maneuver toward the target with a consequent altitude gain of less than 500 feet. The primary controllers for this phase of the flight are two pairs of diametrically opposed jets (jet reaction controllers-JRC) aligned perpendicular to both one another and the missile axis of symmetry. Upon attainment of an approximately horizontal flight path, the primary controller of the missile transfers to typical aerodynamic surfaces (CANARDS) which then guide the missile to intercept. The maneuvers of lift-off and pitch-over, for which the time frame is 1. - 1.5 secs, are of primary interest and therefore are the object of this simulation.

The important features of the simulation are: acceptance of a vertical launch configuration, implementation of JRC controlled maneuvers, a detailed simulation of a large-look angle seeker, and a dual speed integration routine.

The basis of the simulation is a dual speed integration routine using Hamming's predictor-modifier-corrector formulation for the recursion equations. The user has the option of specifying which state variables are integrated with the two different steps size h and h_s . Additionally, because of the singularities evident in the Euler angles, four quaterion parameters are

employed to uniquely represent the missile attitude for all possible orientations.

All of the missile parameters, including the aerodynamic data for both the baseline missile and the JRC's, are listed within the report. However, the reader is cautioned against the assumption that a particular missile is being simulated for the data are only representative of this type of missile.

The intention of this effort was to provide a general basic structural program capable of simulating a missile as a rigid body with the specific subroutines for the aerodynamic data, rigid body parameters, etc. to be supplied by the user as required.

COMPUTER PROGRAM EXPLANATIONS

A. Definitions of Coordinate Systems

1. Inertial Coordinate System

An inertially fixed coordinate system (X,Y,Z) is attached to the earth with the origin at ground zero, the X axis indicating north, the Y axis indicating east and the Z axis indicating the local vertical (positive downward).

2. Missile Fixed Coordinate System

A body fixed coordinate system (x,y,z) is located with its origin at the missile center of gravity, the x axis as the missile's axis of symmetry (positive pointing forward), the y axis rotated negative 45° from the right-hand pitch canard, and the z axis rotated accordingly. See Figure 1.

3. Pitch Axis Coordinate System

The origin and the x' axis of the pitch axes coordinate system (x',y',z') are coincident with their counterparts in the missile fixed axes system, while the z' axis always coincides with the projection of the relative wind vector onto the y , z plane. The angle ϕ_w indicates the relative rotation of (x',y',z') with respect to (x,y,z). See Figure 2.

B. Missile Position and Orientation

The coordinates X , Y , HT locate the missile center of gravity with respect to the inertial coordinate system in the north-south, east-west, and height above ground zero directions respectively.

The orientation of the missile axes with respect to the inertial system is monitored using the standard Euler angles¹ ψ , θ , ϕ (yaw, pitch, roll) with the order of rotation as given. The resulting transformation matrix from inertial coordinates to missile coordinates is

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} T11 & T12 & T13 \\ T21 & T22 & T23 \\ T31 & T32 & T33 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

where

$$T11 = \cos \psi \cos \theta$$

$$T12 = \sin \psi \cos \theta$$

$$T13 = -\sin \theta$$

$$T21 = \cos \psi \sin \theta \sin \phi - \sin \psi \cos \phi$$

$$T22 = \sin \psi \sin \theta \sin \phi + \cos \psi \cos \phi$$

$$T23 = \cos \theta \sin \phi$$

$$T31 = \cos \psi \sin \theta \cos \phi + \sin \psi \sin \phi$$

$$T32 = \sin \psi \sin \theta \cos \phi - \cos \psi \sin \phi$$

$$T33 = \cos \theta \cos \phi$$

In the actual simulation, the Euler angles are not employed because of their singularity at $\theta = \pm 90.$; however they are calculated and outputted to aid the program user in visualization of the missile orientation. The following equalities define the Euler angles when $\theta \neq \pm 90.$:

$$\theta = \sin^{-1} (-T13)$$

$$\psi = \tan^{-1} (T12/T11) \quad (4 \text{ quadrant } \tan^{-1})$$

$$\phi = \tan^{-1} (T23/T33) \quad (4 \text{ quadrant } \tan^{-1})$$

However, when $\theta = \pm 90.$, ψ and ϕ are undefined and the following convention is adopted

$$\psi = 0$$

$$\phi = \tan^{-1} (T21, T31) \quad (4 \text{ quadrant } \tan^{-1})$$

C. Quaternions²

To avoid the singularity of the Euler angles at $\theta = \pm 90$. the quaternion system of four coordinates is adopted. The introduction of an extra coordinate into the system removes the singularity but requires the addition of a constraint equation on the four parameters.

The four coordinates are e_0, e_1, e_2, e_3 with the constraint of $e_0^2 + e_1^2 + e_2^2 + e_3^2 = 1$ (orthogonality). The elements of the previously mentioned transformation matrix are functions of these coordinates.

$$T_{11} = e_0^2 + e_1^2 - e_2^2 - e_3^2$$

$$T_{12} = 2(e_1 e_2 + e_0 e_3)$$

$$T_{13} = 2(e_1 e_3 - e_0 e_2)$$

$$T_{21} = 2(e_1 e_2 - e_0 e_3)$$

$$T_{22} = e_0^2 + e_2^2 - e_1^2 - e_3^2$$

$$T_{23} = 2(e_2 e_3 + e_0 e_1)$$

$$T_{31} = 2(e_1 e_3 + e_0 e_2)$$

$$T_{32} = 2(e_2 e_3 - e_0 e_1)$$

$$T_{33} = e_0^2 + e_3^2 - e_1^2 - e_2^2$$

The differential equations for the quaternion parameters as functions of the missile angular rates (p,q,r) are:

$$\dot{e}_0 = -\frac{1}{2} (e_1 p + e_2 q + e_3 r)$$

$$\dot{e}_1 = \frac{1}{2} (e_0 p - e_3 q + e_2 r)$$

$$\dot{e}_2 = \frac{1}{2} (e_3 p + e_0 q - e_1 r)$$

$$\dot{e}_3 = \frac{1}{2} (-e_2 p + e_1 q + e_0 r)$$

Mechanization of the constraint equation is achieved by defining an error

$$\epsilon = 1 - (e_0^2 + e_1^2 + e_2^2 + e_3^2)$$

which is a measure of the violation of the constraint and applying a correction factor to each differential equation which reduces the error. With a value of $K = 1$ the equations remain correctly constrained within $|\epsilon| \leq 10^{-6}$.

$$\dot{e}_0 = -\frac{1}{2} (e_1 p + e_2 q + e_3 r) + Ke_0 \epsilon$$

$$\dot{e}_1 = \frac{1}{2} (e_0 p - e_3 q + e_2 r) + Ke_1 \epsilon$$

$$\dot{e}_2 = \frac{1}{2} (e_3 p + e_0 q - e_1 r) + Ke_2 \epsilon$$

$$\dot{e}_3 = \frac{1}{2} (-e_2 p + e_1 q + e_0 r) + Ke_3 \epsilon$$

The required initial conditions on e_0 , e_1 , e_2 , e_3 are given as functions of the initial Ψ , θ , Φ by

$$e_0 = \cos(\Psi/2) \cos(\theta/2) \cos(\Phi/2) + \sin(\Psi/2) \sin(\theta/2) \sin(\Phi/2)$$

$$e_1 = \cos(\Psi/2) \cos(\theta/2) \sin(\Phi/2) - \sin(\Psi/2) \sin(\theta/2) \cos(\Phi/2)$$

$$e_2 = \cos(\Psi/2) \sin(\theta/2) \cos(\Phi/2) + \sin(\Psi/2) \cos(\theta/2) \sin(\Phi/2)$$

$$e_3 = -\cos(\Psi/2) \sin(\theta/2) \sin(\Phi/2) + \sin(\Psi/2) \cos(\theta/2) \cos(\Phi/2)$$

D. Differential Equations for Rigid Body

With X_F , Y_F , Z_F defined as the total forces on the missile expressed in missile axes x, y, z respectively and X_M , Y_M , Z_M defined as the total moments about the missile center of gravity expressed in the same axis system, the differential equations of motion are:

$$\dot{u} = rv - qw + X_F/m$$

$$\dot{v} = pw - ru + Y_F/m$$

$$\dot{w} = qu - pv + Z_F/m$$

$$\dot{p} = \frac{X_M}{I_x}$$

$$\dot{q} = - \frac{pr (I_x - I_y) + Y_M}{I_y}$$

$$\dot{r} = + \frac{pq (I_x - I_y) + Z_M}{I_y}$$

$$\begin{bmatrix} \dot{x}_I \\ \dot{y}_I \\ \dot{HT} \end{bmatrix} = \begin{bmatrix} \\ T^{-1} \\ \end{bmatrix} \begin{bmatrix} u \\ v \\ -w \end{bmatrix}$$

$$\dot{e}_0 = - \frac{1}{2} (e_1 p + e_2 q + e_3 r) + Ke_0 \epsilon$$

$$\dot{e}_2 = \frac{1}{2} (e_0 p - e_3 q + e_2 r) + Ke_1 \epsilon$$

$$\dot{e}_3 = \frac{1}{2} (e_3 p + e_0 q - e_1 r) + Ke_2 \epsilon$$

$$\dot{e}_4 = \frac{1}{2} (- e_2 p + e_1 q + e_0 r) + Ke_3 \epsilon$$

It is assumed that the missile is symmetric about the x axis, no cross products of inertia exist and $I_y = I_z$. $T^{-1} = T^T$ where T is the transformation matrix from (X, Y, Z) to (x, y, z) .

E. Definition of the Relative Wind Orientation

Two angles α and ϕ_w define the orientation of the relative wind vector with respect to the missile axis system as shown in Figure 3, where u_T , v_T , w_T are the x,y,z components of the resultant wind and $V = (u_T^2 + v_T^2 + w_T^2)^{\frac{1}{2}}$. Along each axis the resultant wind component is the difference of the missile inertial velocity and the true wind for that axis.

$$u_T = u - u_w$$

$$v_T = v - v_w$$

$$w_T = w - w_w$$

Additionally, ϕ_J defines the orientation of the resultant wind with respect to each individual JRC (Jet Reaction Controller). Positive ϕ_J is defined as shown in Figure 4.

F. Aerodynamic Data

The missile aerodynamics are divided into two distinct categories: (1) aerodynamic coefficients for the baseline missile (no JRC) and (2) amplification factors which represent the effect of the JRC thrusters. Both sets of data are functionally dependent on α and either ϕ_w or ϕ_J but not on Mach number.

The baseline aerodynamic coefficients $C_{x'}$, $C_{y'}$, $C_{z'}$, $C_{\ell'}$, $C_{m'}$, $C_{n'}$ are given as shown in Figures 5-6. For the present simulation $C_{x'} = C_{y'} = C_{\ell'} = C_{n'} = 0$.

The effects of the JRC thrusters are summarized by amplification factors as follows (y force and moment amplification factors are used as examples)

$$K_y = \frac{Y_F |_{\text{JRC on}} - Y_F |_{\text{JRC off}}}{T_{\text{JRC}}}$$

$$K_m = \frac{Y_M |_{\text{JRC on}} - Y_M |_{\text{JRC off}}}{T_{\text{JRC}} (x_{\text{JRC}})}$$

The specific values of K_y , K_z , K_m , K_n as programmed are shown in Figures 7-8. For this simulation $K_y = K_n = 0$. Additionally, the effects of the JRC jets are assumed to be independent.

G. Integration Routine³

Hamming's predictor, modifier, corrector set of recursion equations are used for the dual speed numerical integration of the problem state variables. The following is a brief explanation of the equations.

For a system of n ordinary differential equations

$$y' = f(x,y)$$

where

$$y' = dy/dx ,$$

a sequence of the solution variables

$$y_i = y(x_i) \quad i = 1, 2, \dots$$

can be expressed as a function of previous y_i and y_{i-1} . With

$h = x_{i+1} - x_i$ Hammings method is:

$$\text{PREDICT:} \quad p_{i+1} = y_{i-3} + \frac{4h}{3} (2y'_i - y'_{i-1} + 2y'_{i-2})$$

$$\text{MODIFY:} \quad m_{i+1} = p_{i+1} - \frac{112}{121} (p_i - c_i)$$

$$m'_{i+1} = f(x_{i+1}, m_{i+1})$$

$$\text{CORRECT:} \quad c_{i+1} = \frac{1}{8} [9y_i - y_{i-2} + 3h (m'_{i+1} + 2y'_i - y'_{i-1})]$$

$$\text{FINAL VALUE:} \quad y_{i+1} = c_{i+1} + \frac{9}{121} (p_{i+1} - c_{i+1})$$

Each advance of h in the independent variable x requires two evaluations of y' , once for the predictor and once for the corrector. The method is numerically stable with truncation errors to the order of h^5 .

The values of y and y' from the past three intervals are necessary, thus a starting technique is required. The conventional application of a 4th order Runge-Kutta integration method on the first three steps was discarded in favor of calculating the required state variables by a Euler backstep. Specifically, for $i = 0$,

$$y_{-3} = y_0 - 3hy'_0$$

$$y_{-2} = y_0 - 2hy'_0$$

$$y_{-1} = y_0 - h y'_0$$

$$y'_{-2} = y'_{-1} = y'_0$$

This method suffers from inaccuracy when y'_{-2} and y'_{-1} differ appreciably from y'_0 . However, in this simulation, no variation in the solution was detected from the application of the less accurate Euler backstep when compared with a Runge-Kutta starter.

An additional complexity was introduced by the requirement of a dual speed integration algorithm because of computational time considerations. Now there are two systems of differential equations:

$$y' = f(x, y, z)$$

$$z' = f(x, y, z)$$

with the z equations requiring smaller time steps than the y equations for the same accuracy criteria. With h and h_s defined as the smaller

and larger step sizes respectively, figure 9 depicts the sequencing of the algorithm for one step of h_s . A ratio of $h_s/h = 5$ is chosen for illustration although this is variable at the operator's option.

H. Other Subroutines

CONTROL SYSTEM

The JRC's were assumed to be the primary controlling elements for the initial missile trajectory and, therefore, the canard deflection are identically zero for this phase of the flight.

Two control equations govern the action of the JRC's, one for each pair of opposing jets. Figure 10 defines the jet numbers and orientations. For illustration the control of jets 1 and 3 is presented. A variable PRMTZ is defined as a function of missile-target relative position and rates. The exact specification for this equation is the operators responsibility. When $PRMTZ > 0$ jet 3 is on while jet 1 is off. If $PRMTZ < 0$ the reverse is true, and when $PRMTZ = 0$ both jets are off.

As an example of a possible control equation consider

$$PRMTZ = \sigma_A + K \dot{\sigma}_A$$

where σ_A is defined in Figure 11.

SEEKER

This program incorporates a simulation of a large look angle version of a present day seeker. The simulation was supplied by the manufacturer and was only slightly modified to interface correctly. The system description will not be discussed here, only the inputs and outputs of the subroutine.

The following information is required by subroutine SEEKER: $X_I, Y_I, HT, XT_I, YT_I, HTT, [T], p, q, r, \dot{p}, \dot{q}, \dot{r}$. The subroutine returns: $\phi_1, \psi_2, \psi_3, \theta_4, \epsilon_B, \epsilon_C, \dot{\phi}_1, \dot{\psi}_2, \Omega_y, \Omega_C, \Omega_{G_y}, \Omega_{G_z}$ for outputting if desired.

RIGID BODY PARAMETERS

All rigid body parameters (mass , I_x , I_y , C.G. position) are linearly interpolated between the initial values at lift-off and the final values when the missile thrust motor is expended. The instantaneous position of the center of gravity x_{cg} is defined relative to the reference point for the aerodynamic data as in Figure 12. The following table indicates the parameters as used in the program.

<u>PARAMETER</u>	<u>LIFT OFF</u>	<u>BURN OUT</u>	
m	6.742	4.710	slug
I_y	65.1	48.1	slug-ft ²
I_x	.420	.245	slug-ft ²
x_{cg}	-.321	.406	ft

$$s = .13635 \text{ ft}^2$$

$$d = .4167 \text{ ft}$$

$$x_{JRC} = 2.434 \text{ ft}$$

$$T_{JRC} = 400. \text{ lbs}$$

$$T_r = 3000. \text{ lbs}$$

ATMOSPHERE⁴

Both the density and acoustical velocity of air as functions of height are generated within ATMOS. A linear interpolation of these parameters is based on data from an ICAO Standard Atmosphere Table at heights of 0. and 1000. ft.

Additionally values for the X and Y components of surface winds maybe entered as constant or functions of altitude depending on the operator's preference.

TARGET

Subroutine target calculates the time history trajectory of the target as a function of its initial inertial position, constant inertial velocity components and time.

THRUST

Missile thrust is assumed to be a constant THR for a duration of burn TBURN, after which $THR = 0$. . .

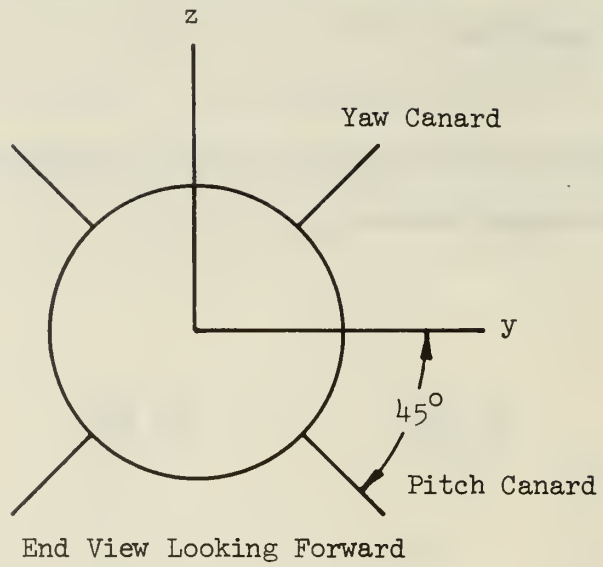


Figure 1. Definition of Missile Fixed Coordinate System

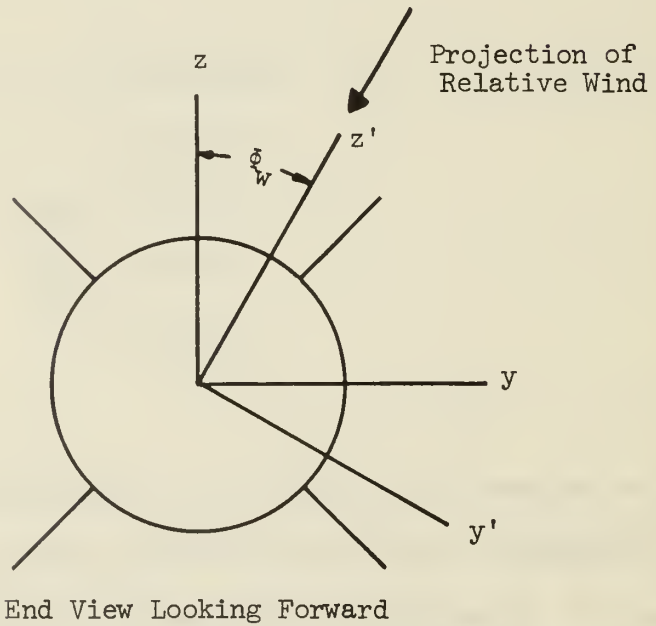
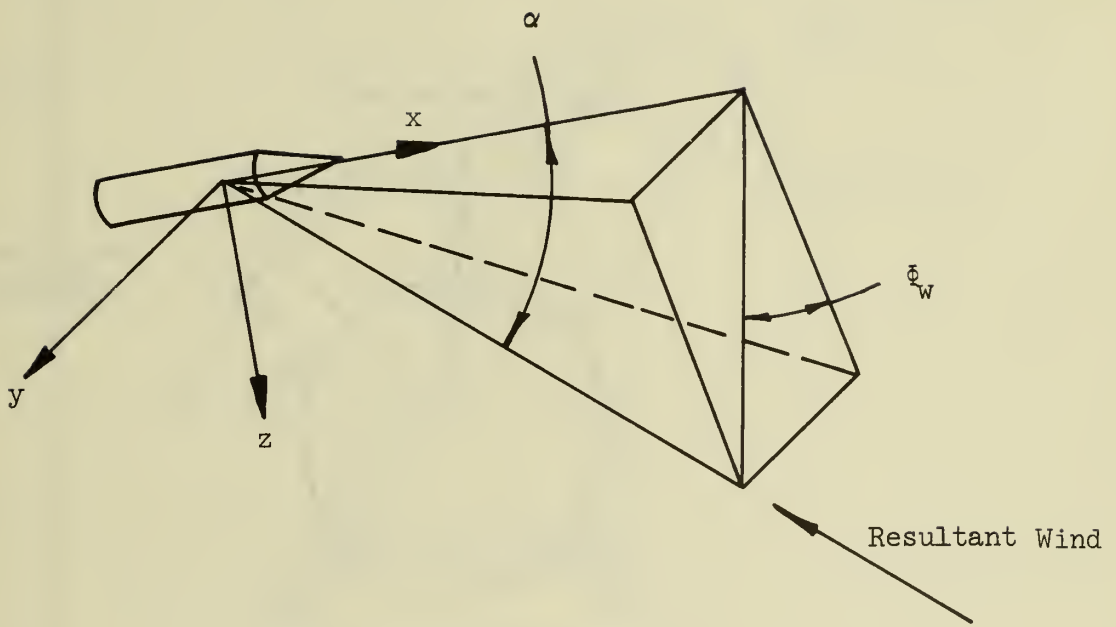


Figure 2. Definition of Pitch Axes Coordinate System



$$\alpha = \cos^{-1} (u_T/V)$$

$$\phi_w = \cos^{-1} (w_T / (v_T^2 + w_T^2)^{\frac{1}{2}})$$

If $\alpha = 0$, $\phi_w \equiv 0$

Figure 3. Relative Wind Orientation

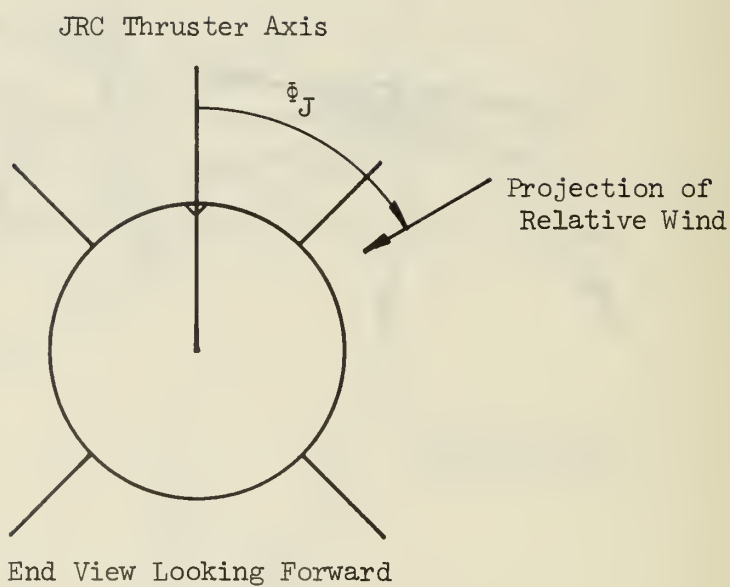


Figure 4. Relative Wind Orientation
With Respect to the JRC Thruster Axis.

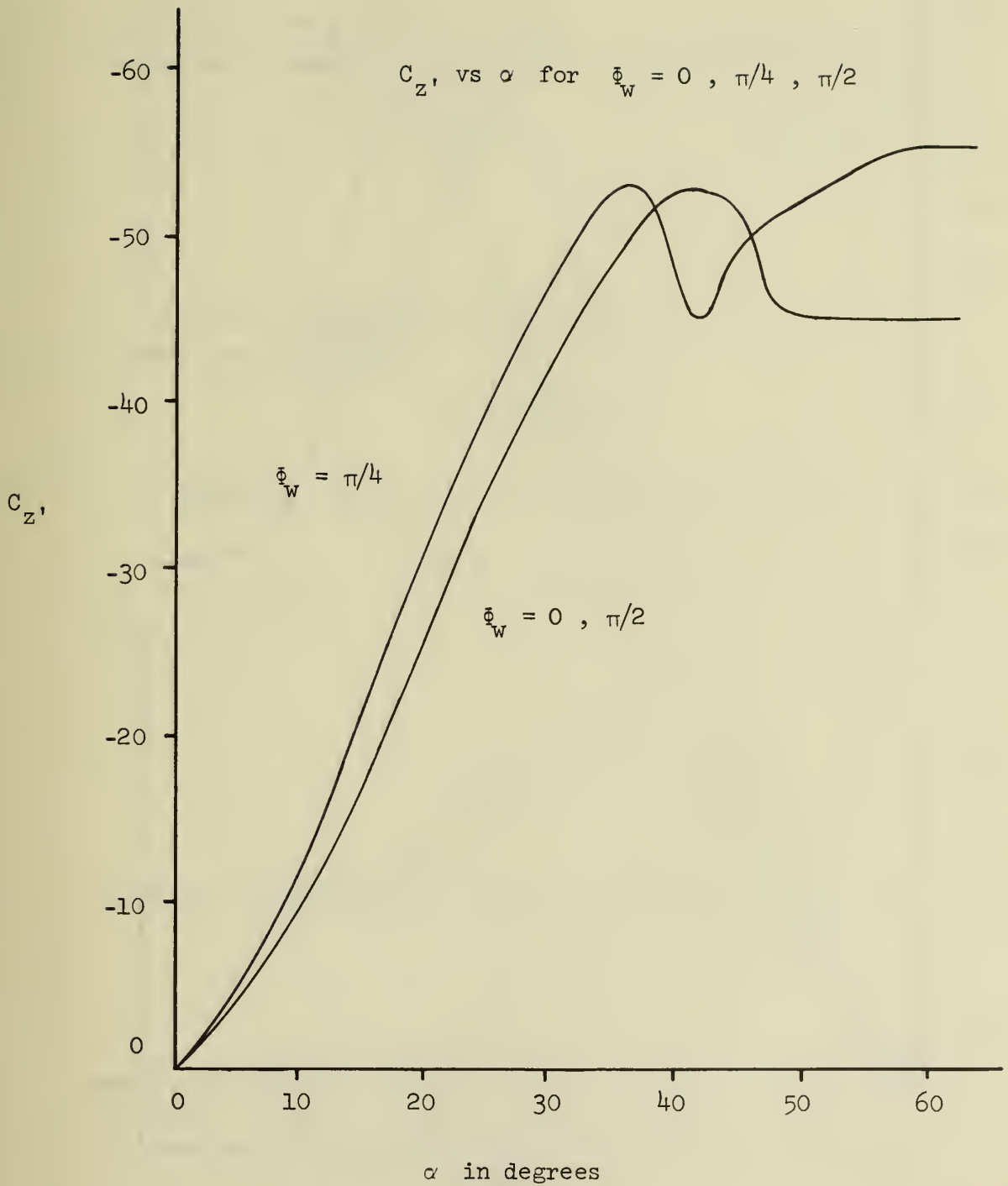


Figure 5. C_z , vs α for $\phi_w = 0, \pi/4, \pi/2$.

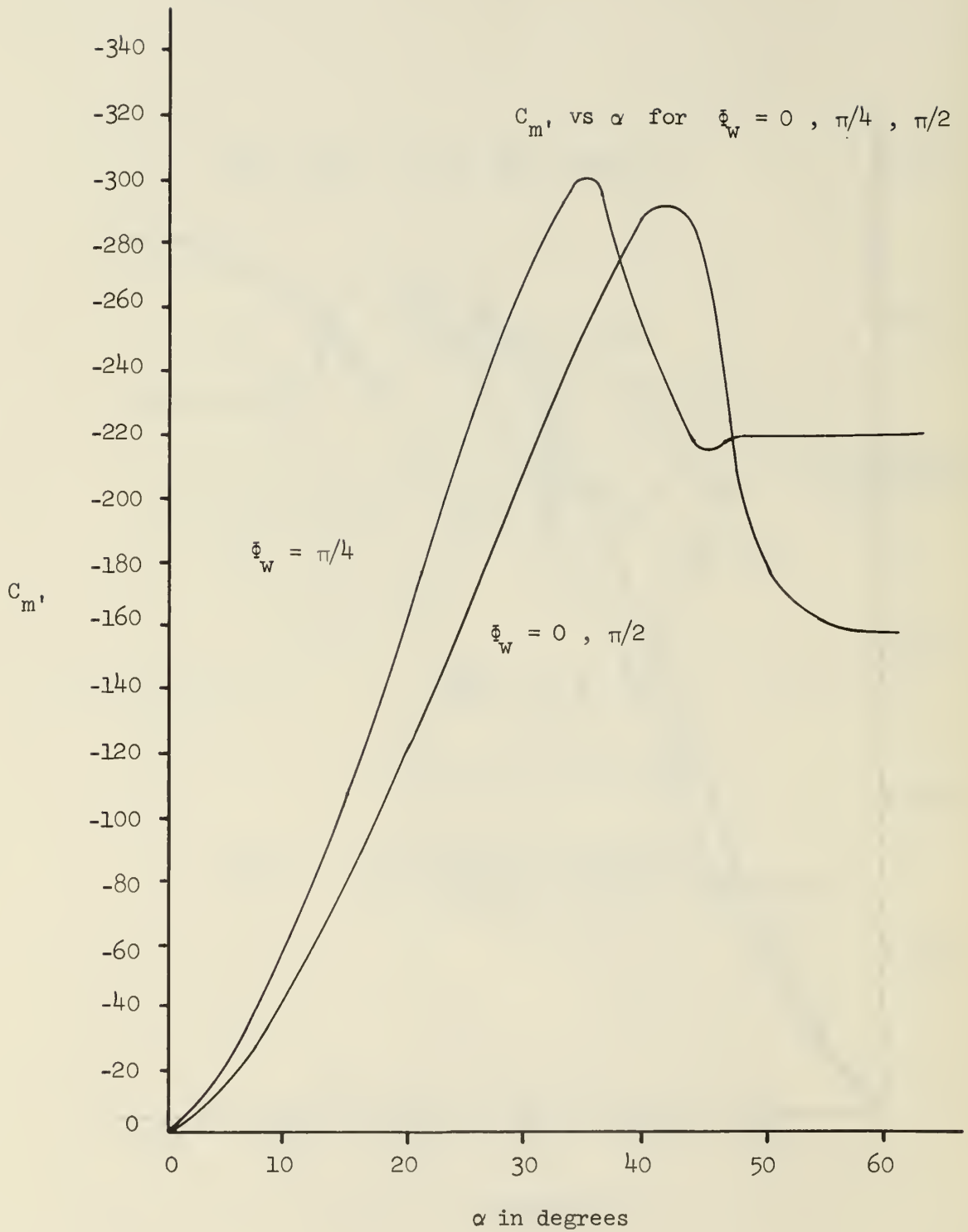


Figure 6. $C_{m'}$ vs α for $\phi_w = 0, \pi/4, \pi/2$.

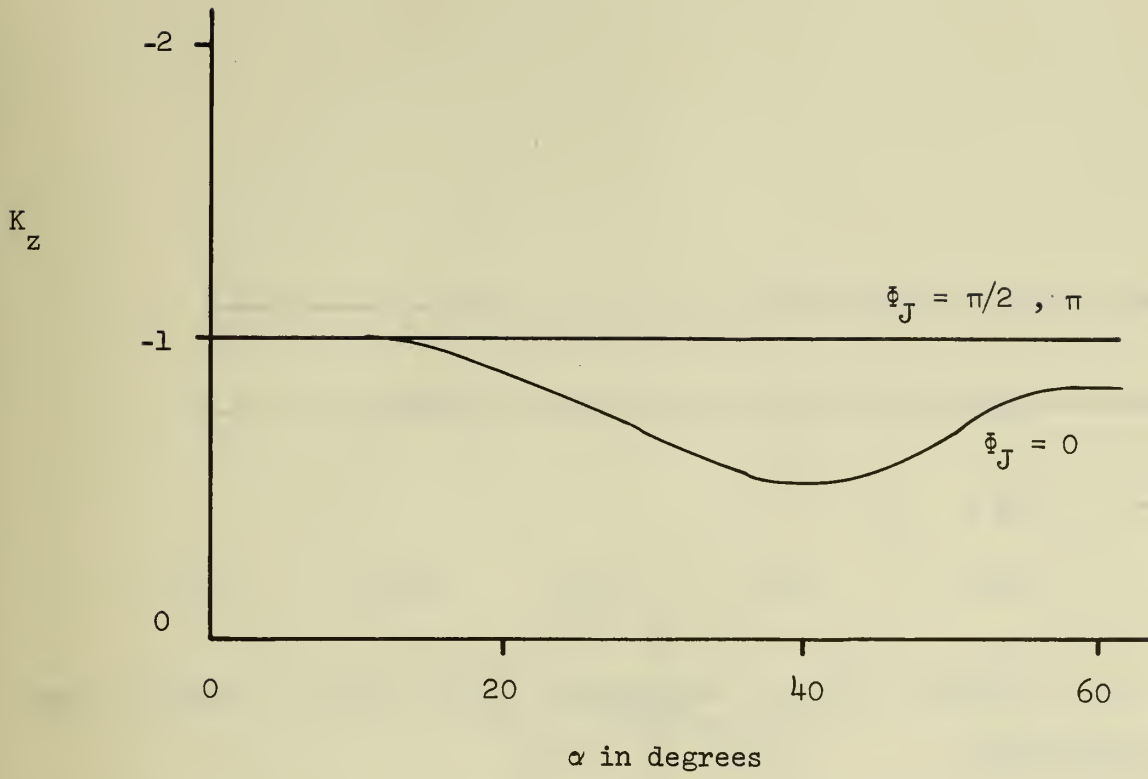


Figure 7. K_z vs α for $\phi_J = 0, \pi/2, \pi$.

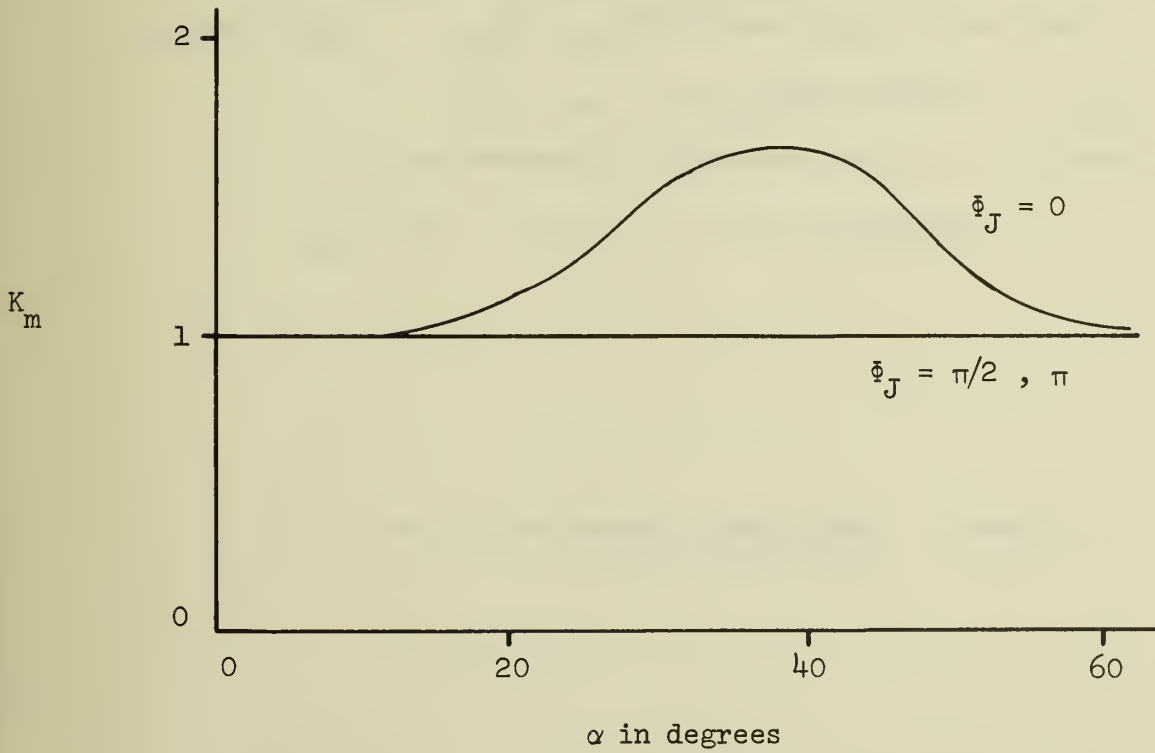
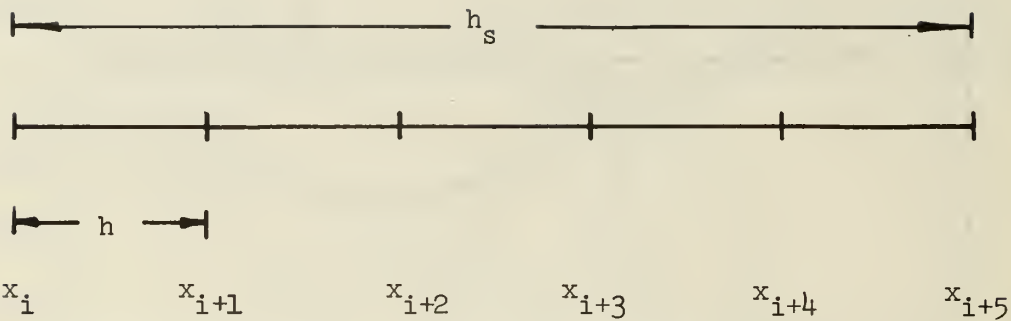
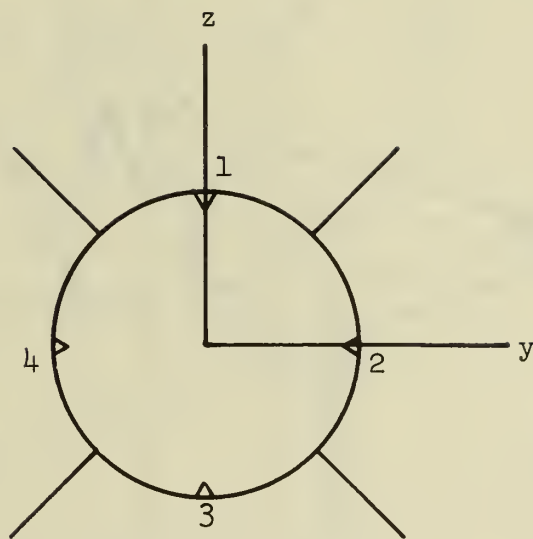


Figure 8. K_m vs α for $\phi_J = 0, \pi/2, \pi$.



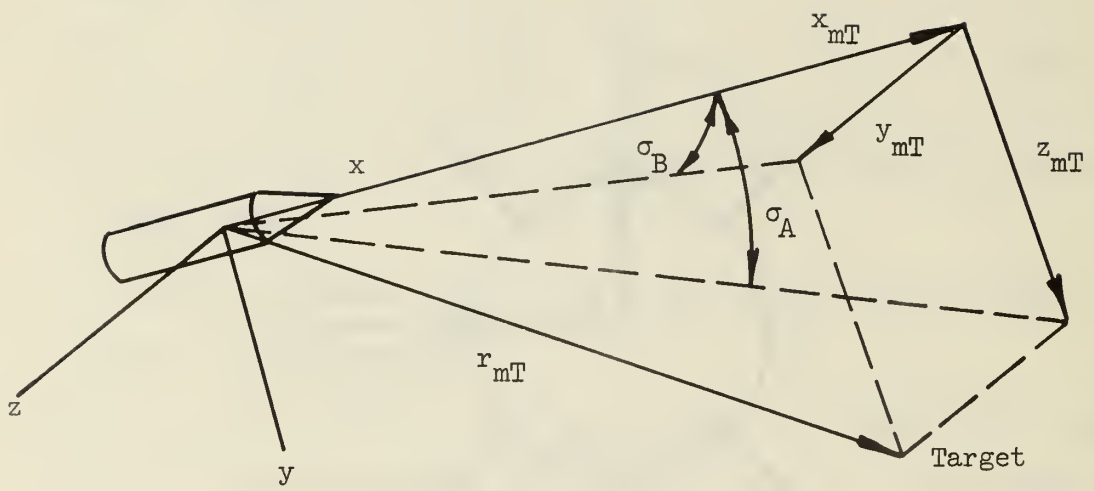
1. At $x = x_i$ evaluate z'_i, y'_i and predict \tilde{z}_{i+1} and \tilde{y}_{i+5} using h and h_s respectively.
2. At $x = x_{i+1}$ evaluate z'_{i+1}, y'_{i+1} and correct z_{i+1} and y_{i+5} using h and h_s respectively.
3. With y_{i+5} now fixed, at $x = x_{i+1}, x_{i+2}, \dots$ evaluate only $z'_{i+1}, z'_{i+2}, \dots$ and sequentially predict $\tilde{z}_{i+2}, \tilde{z}_{i+3}, \dots$ and correct z_{i+2}, z_{i+3}, \dots until $x = x_{i+5}$.
4. Repeat steps (1) - (3) for successive increments of h_s .

Figure 9. Dual Speed Integration for One Large Step h_s .



End View Looking Forward

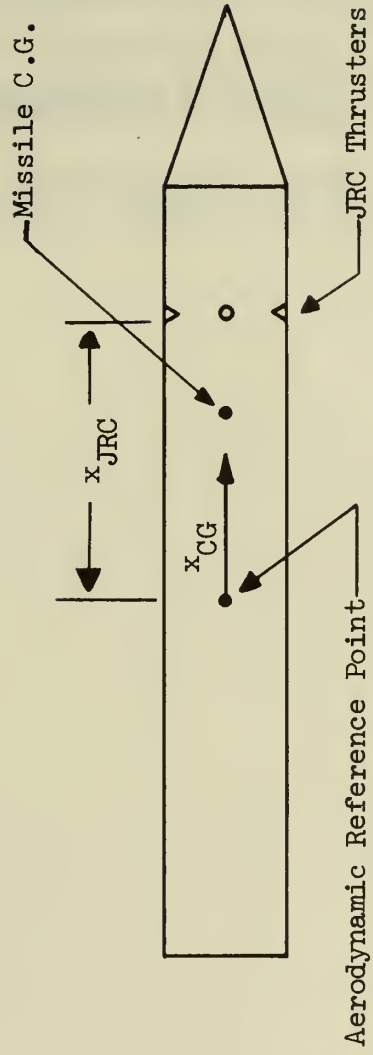
Figure 10. Definition of JRC Orientation.



$$\sigma_A = \tan^{-1} (z_{mT}/x_{mT})$$

$$\sigma_B = \tan^{-1} (y_{mT}/x_{mT})$$

Figure 11. Definition of Target Azimuth and Elevation Angles.



Note: x_{cg} is shown positive

Figure 12. Definition of Missile Parameters.

REFERENCES

1. Etkin, Bernard, Dynamics of Flight, John Wiley & Sons, Inc., 1959.
2. Mitchell, E. E. L., and Rogers, A. E., "Quaternion Parameters in the Simulation of a Spinning Rigid Body," Simulation, Vol. 4, No. 6, June, 1965.
3. Ralston, A., and Wilf, H. (Editors), Mathematical Methods for Digital Computers, Vol, I, John Wiley & Sons, Inc., New York, 1967.
4. Dommasch, Daniel O., and others, Airplane Aerodynamics, Pitman Publishing Corporation, New York, 1967.

APPENDIX A

PROGRAM LISTING

The following is a FORTRAN listing of the simulation program designed for compatibility with the United Computing Service, Inc. time sharing system. A typical input/output listing is also included.

```

00100 PROGRAM SXDF(INPUT,OUTPUT,TAPE1,TAPE2,TAPE3)
00110 COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
00120+ ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI

00130+ ,VSND,SPHIW,HTE,GUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
00140+ PHI,Z(14),DZ(14)
00150 COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
00160* COMMUNICATIONS BETWEEN SUBROUTINE CTLSYS,AROJRC
00170 COMMON/CTLSYJ/ IJET(4)
00180* COMMUNICATIONS BETWEEN SUBROUTINES TRNSMT,TARGET,SEEKER
00190 COMMON/TRANS/T11,T12,T13,T21,T22,T23,T31,T32,T33
00200* COMMUNICATIONS BETWEEN SUBROUTINES CTLSYS,SEEKER
00210 COMMON/SEEKR/ EPB,SPHI1,CPHI1,EPBC
00220* EQUIVALENCING COMMON MISSILE TERMINOLOGY TO THE STATE VARIABLES
00230* Y(I) AND Z(I) AND THEIR RESPECTIVE DERIVATIVES DY(I) AND DZ(I)
00240 EQUIVALENCE (U,Y(1)),(V,Y(2)),(W,Y(3)),(XI,Y(4)),(YI,Y(5)),

00250+ (HT,Y(6)),(P,Y(7)),(Q,Y(8)),(R,Y(9)),
00260+ (UD,DY(1)),(VD,DY(2)),(WD,DY(3)),
00270+ (XID,DY(4)),(YID,DY(5)),(HTD,DY(6)),(PD,DY(7)),(QD,DY(8)),
00280+ (RD,DY(9))
00290* EQUIVALENCING COMMON MISSILE TERMINOLOGY TO THE STATE VARIABLES
00300* Y(I) AND Z(I) AND THEIR RESPECTIVE DERIVATIVES DY(I) AND DZ(I).
00310 EQUIVALENCE (WYX,Z(3)),(PHI1,Z(4)),(WCZ,Z(5)),(PSI2,Z(6)),
00320+ (WGY,Z(7)),(WGZ,Z(8)),(PSI3,Z(9)),(THT4,Z(10)),
00330+ (E0,Z(11)),(E1,Z(12)),(E2,Z(13)),(E3,Z(14)),(PHI1D,DZ(4)),
00340+ (PSI2D,DZ(6)),(E0D,DZ(11)),(E1D,DZ(12)),(E2D,DZ(13)),
00350+ (E3D,DZ(14))
00360 DATA CON4/57.29577951/,GRAV/32.2/
00370 DATA CON1/1.0/
00380 RETRIEVE(CTLSYS)
00390 RETRIEVE(INIT)
00400 RETRIEVE(THRUST)
00410 RETRIEVE(AERO)
00420 RETRIEVE(TRNSMT)
00430 RETRIEVE(TARGET)
00440 RETRIEVE(RBFRMT)
00450 RETRIEVE(INTEG)
00460 RETRIEVE(AROBSE)
00470 RETRIEVE(SEEKER)
00480 RETRIEVE(ATMOS)
00490 RETRIEVE(AROJRC)
00500 RETRIEVE(INTER2)
00510 RETRIEVE(OUTPUT1)
00520 REWIND 2
00530* INITIALIZE ALL PROGRAM VARIABLES
00540 CALL INIT
00550* THE INTEGRATION ROUTINE REQUIRES TWO EVALUATIONS OF THE STATE
00560* VARIABLE DERIVATIVES FOR EACH TIME STEP. ADDITIONALLY,THE STATE
00570* VARIABLES ARE SEPARATED INTO TWO CATEGORIES; Z(I) FOR VARIABLES
00580* WHICH UPDATE AT EVERY TIME STEP H, AND Y(I) FOR VARIABLES WHICH
00590* UPDATE ONLY EVERY "IRATIO" TIME STEPS.
00600* CALCULATE THE NUMBER OF DERIVATIVE EVALUTIONS NECESSARY FOR
00610* "IRATIO" NUMBER OF TIME STEPS.
00620 IRT2=2*IRATIO
00630 3 DO 2 K=1,IRT2
00640* THE START OF THE DERIVATIVE EVALUATION LOOP.
00650* CALCULATE THE TRANSFORMATION MATRIX BETWEEN THE INERTIAL AXIS
00660* SYSTEM AND THE MISSILE BODY FIXED AXIS SYSTEM.
00670 CALL TRNSMT
00680* CALCULATE THE DERIVATIVES OF THE QUATERION VARIABLES.

```

```

00690      EFS=1.+T11+T22+T33-4.*E0*E0
00700      E0D=-.5*(E1*P+E2*Q+E3*R)+EPS*E0
00710      E1D= .5*(E0*P+E2*R-E3*Q)+EPS*E1
00720      E2D= .5*(E0*Q+E3*P-E1*R)+EPS*E2
00730      E3D= .5*(E0*R+E1*Q-E2*P)+EPS*E3
00740* IT IS NOT NECESSARY TO REEVALUATE ALL OF THE DERIVATIVES WHEN
00750* ONLY THE Z(I), AND NOT THE Y(I), VARIABLES ARE BEING UPDATED.
00760* "IRATE" EQUALS 1 IN THIS SITUATION, OTHERWISE IT EQUALS 0.
00770* WHEN "IRATE" EQUALS 1, PORTIONS OF THE LOOP ARE BYPASSED TO
00780* PREVENT RECOMPUTATION OF NON-UPDATED VARIABLES.
00790      IF (IRATE.EQ.1) GO TO 20
00800* COMPUTE TARGET POSITION.
00810      CALL TARGET
00820* COMPUTE MISSILE THRUST.
00830      CALL THRUST
00840* COMPUTE THE INSTANTANEOUS VALUES OF THE RIGID BODY PARAMETERS.
00850      CALL RBPRMT
00860* COMPUTE THE PERTINENT ATMOSPHERIC PARAMETERS.
00870      CALL ATMOS
00880      20 CONTINUE
00890* SIMULATE THE SEEKER DYNAMICS. THE SEEKER VARIABLES MUST BE
00900* INTEGRATED WITH THE SMALL TIME STEP TO AVOID COMPUTATIONAL
00910* INSTABILITIES, AND HENCE ARE EVALUATED DURING EACH PASS THROUGH
00920* THE LOOP.
00930      CALL SEEKER
00940* BYPASS PORTIONS OF THE LOOP BASED ON "IRATE".
00950      IF (IRATE.EQ.1) GO TO 30
00960* DETERMINE THE MISSILE CONTROL VARIABLES.
00970      CALL CTLSYS
00980* ADD THE EFFECTS OF ATMOSPHERIC WINDS.
00990      UT=U-WINDXB
01000      VT=V-WINDYB
01010      WT=W-WINDZB
01020* CALCULATE MISSILE VELOCITY, MACH NUMBER, AND DYNAMIC PRESSURE.
01030      VEL2=UT*UT+VT*VT+WT*WT
01040      VEL=SQRT(VEL2)
01050      VEL1=SQRT(VEL2-UT*UT)
01060      QUE=.5*RHO*VEL2
01070      RMACH=VEL/VSND
01080* DETERMINE ALPHA AND PHI OF THE WIND. AT THE SINGULARITY OF
01090* ALPHA=0, PHI IS DEFINED AS =0.
01100      PRMT=CON1
01110      IF (VEL.GT.0.) PRMT=UT/VEL
01120      IF (ABS(PRMT).GE.1.0) PRMT=SIGN(CON1,PRMT)
01130      ALPHA=CON4*ACOS(PRMT)
01140      PHIW=0.
01150      SPHIW=0.
01160      CPHIW=1.
01170      IF (VEL1.EQ.0.) GO TO 10
01180      SPHIW=VT/VEL1
01190      CPHIW=WT/VEL1
01200      IF (ABS(SPHIW).GE.1.0) SPHIW=SIGN(CON1,SPHIW)
01210      IF (ABS(CPHIW).GE.1.0) CPHIW=SIGN(CON1,CPHIW)
01220      PHIW=CON4*ACOS(CPHIW)
01230      IF (SPHIW.LT.0.) PHIW=-PHIW
01240* DETERMINE THE AERODYNAMIC FORCES AND MOMENTS.
01250      10 CALL AERO
01260* SUM THE AERO, THRUST, AND GRAVITY FORCES.
01270      XF=XFA+THR+T13*GRAV*RMAS

```

```

01280      YF=YFA+T23*GRAV*RMASS
01290      ZF=ZFA+T33*GRAV*RMASS
01300* EVALUATE THE MISSILE STATE VARIABLE DERIVATIVES.
01310      UD=R*V-Q*W+XF/RMASS
01320      VD=P*W-R*U+YF/RMASS
01330      WD=Q*U-P*V+ZF/RMASS
01340      PD=XM/XXI
01350      PRMT=F*(XXI-YYI)
01360      QD=(-R*PRMT+YM)/YYI
01370      RD=(Q*PRMT+ZM)/YYI
01380      XID=U*T11+V*T21+W*T31
01390      YID=U*T12+V*T22+W*T32
01400      HTD=-(U*T13+V*T23+W*T33)
01410      30 CONTINUE
01420* DETERMINE WHETHER OUTPUT IS DESIRED. "IPRINT"=0 INDICATES
01430* THAT THE INTEGRATION ROUTINE HAS ONLY PREDICTED AND HAS NOT
01440* CORRECTED, THEREFORE THE OUTPUT IS MEANINGLESS. "IPRINT"=1
01450* INDICATES THAT OUTPUTING IS POSSIBLE.
01460      IF (IPRINT.EC.0) GO TO 6
01470* DETERMINE IF THE DESIRED OUTPUT INTERVAL IS SATISFIED.
01480      IF (MOD(NSTEP,NPRINT).GT.0) GO TO 6
01490* CONVERT THE QUATERNIONS TO EULER ANGLES FOR OUTPUTING. AT THE
01500* SINGULARITY OF THETA=+90, PSI IS DEFINED AS =0 AND PHI
01510* IS CALCULATED.
01520      IF (ABS(T13).GE.1.0) T13=SIGN(CON1,T13)
01530      THT=CON4*ASIN(-T13)
01540      IF (ABS(THT).EC.90.) GO TO 4
01550      PSI=CON4*ATAN2(T12,T11)
01560      PHI=CON4*ATAN2(T23,T33)
01570      GO TO 5
01580      4 PSI=0.
01590      PHI=CON4*ATAN2(T21,T31)
01600      5 CONTINUE
01610* KEEP TRACK OF THE NUMBER OF TIMES OUTPUTING IS PERFORMED.
01620      ICOUNT=ICOUNT+1
01630* CONVERT RADIANS TO DEGREES FOR OUTPUTING.
01640      PSI20=PSI2*CON4
01650      THT40=THT4*CON4
01660      PHI10=PHI1*CON4
01670      EPB0=EPB*CON4
01680      PSI30=PSI3*CON4
01690      EPBC0=EPBC*CON4
01700* WRITE THE OUTPUT VARIABLES
01710      WRITE(2,) X,U,V,W,XI,YI,HT,P,Q,R,PSI,THT,PHI,
01720+      ALPHA,PHIW,PHI10,PSI20,PSI30,THT40,EPB0,EPBC0,
01730+      WYX,W CZ,WGY,WGZ,PHI1D,PSI2D,(IJET(I),I=1,4)
01740* DETERMINE WHETHER OR NOT ALL VARIABLES ARE TO BE UPDATED
01750* DURING THE NEXT PASS THROUGH THE LOOP. ALL VARIABLES ARE
01760* EVALUATED ON THE FIRST AND SECOND PASSES AND ONLY THE Z(I)
01770* VARIABLES ARE EVALUATED ON ALL SUBSEQUENT PASSES UNTIL AN
01780* "IRATIO" NUMBER OF STEPS HAVE BEEN TAKEN.
01790      6 IRATE=0
01800      IF (K.GT.2) IRATE=1
01810* CALL THE INTEGRATION ROUTINE.
01820      2 CALL INTEG
01830* STOP THE PROGRAM WHEN THE REQUIRED TIME HAS ELAPSED.
01840      IF (X.LT.(XMAX+H*IRATIO)) GO TO 3
01850* CALL THE PROGRAM TO SORT AND SEQUENCE THE OUTPUT VARIABLES FOR
01860* FOR TTY COMPATIBILITY.

```


01870 REWIND 2
01880 CALL OUTPUT1
01890 END

```

10      SUBROUTINE INIT
20      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
30+     ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI
40+     ,VSND,SPHIW,HTE,QUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
50+     PHI,Z(14),DZ(14)
60      COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
70*    COMMUNICATIONS WITH SUBROUTINE TARGET.
80      COMMON/INITL/XT0,YT0,HTT0,XTD,YTD,HTTD
90      EQUIVALENCE (E0,Z(11)),(E1,Z(12)),(E2,Z(13)),(E3,Z(14))
100     100 FORMAT(*INPUT H,XMAX,NPRINT,IRATIO*)
110     110 FORMAT(*INPUT XT0,YT0,HTT0,XTD,YTD,HTTD*)
120*   INITIALIZE INTEGRATION ROUTINE CONTROL VARIABLES.
130     IRATE=0
140     ICOUNT=0
150     IPRINT=1
160*   SET DIMENSIONS OF Y(I) AND Z(I) RESPECTIVELY. IF DIMENSIONS
170*   ARE INCREASED ALSO INCREASE THE STORAGE LOCATION DIMENSIONS
180*   SUBROUTINE INTEG.
190     NDIM=9
200     NDIMF=14
210     PRINT 100
220*   READ FROM TTY THE STEP SIZE, RUN TIME, OUTPUT INTERVAL,STEP SIZE
230*   RATIO.
240     READ      , H,XMAX,NPRINT,IRATIO
250*   READ FROM TTY THE TARGET POSITION AND VELOCITY.
260     PRINT 110
270     READ      ,XT0,YT0,HTT0,XTD,YTD,HTTD
280*   TIME=0.
290     NSTEP=0
300     X=0.
310*   INITIALIZE ALL STATE VARIABLES TO 0.
320     DO 1 I=1,NDIM
330     Y(I)=0.
340     1 DY(I)=0.
350     DO 2 I=1,NDIMF
360     Z(I)=0.
370     2 DZ(I)=0.
380     HTE=6.
390     TBURN=4.5
400*   INITIAL EULER ANGLES FOR VERTICAL ORIENTATION.
410     PSI=0.
420     THT=3.141592653/2.
430     PHI=0.
440*   COMPUTE INITIAL QUATERION VALUES FROM EULER ANGLES.
450     E0=+COS(PSI/2.)*COS(THT/2.)*COS(PHI/2.)+SIN(PSI/2.)*SIN
460+    (THT/2.)*SIN(PHI/2.)
470     E1=+COS(PSI/2.)*COS(THT/2.)*SIN(PHI/2.)-SIN(PSI/2.)*SIN
480+    (THT/2.)*COS(PHI/2.)
490     E2=+COS(PSI/2.)*SIN(THT/2.)*COS(PHI/2.)+SIN(PSI/2.)*COS
500+    (THT/2.)*SIN(PHI/2.)
510     E3=-COS(PSI/2.)*SIN(THT/2.)*SIN(PHI/2.)+SIN(PSI/2.)*COS
520+    (THT/2.)*COS(PHI/2.)
530     RETURN
540     END

```

```
10      SUBROUTINE TRNSMT
20      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
30+     ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI
40+     ,VSND,SPHIW,HTE,QUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
50+     PHI,Z(14),DZ(14)
60      COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
70      COMMON/TRANS/T11,T12,T13,T21,T22,T23,T31,T32,T33
80      EQUIVALENCE (E0,Z(11)),(E1,Z(12)),(E2,Z(13)),(E3,Z(14))
90*    CALCULATE THE ELEMENTS OF THE TRANSFORMATION MATRIX FROM THE
100*   QUATERNION VARIABLES.
110     T11=E0*E0+E1*E1-E2*E2-E3*E3
120     T12=2.*(E1*E2+E0*E3)
130     T13=2.*(E1*E3-E0*E2)
140     T21=T12-4.*E0*E3
150     T22=T11-2.*(E1*E1-E2*E2)
160     T23=2.*(E2*E3+E0*E1)
170     T31=T13+4.*E0*E2
180     T32=T23-4.*E0*E1
190     T33=T11-2.*(E1*E1-E3*E3)
200     RETURN
210     END
```

```
10      SUBROUTINE TARGET
20      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
30+     ,CFHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI
40+     ,VSND,SPHIW,HTE,QUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
50+     PHI,Z(14),DZ(14)
60      COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
70      COMMON/TARG/XTI,YTI,HTTI
80* COMMUNICATIONS WITH SUBROUTINE INIT
90      COMMON/INITL/XT0,YT0,HTT0,XTD,YTD,HTTD
100     COMMON/TRANS/T11,T12,T13,T21,T22,T23,T31,T32,T33
110     COMMON/SEEKR1/SIGA,SIGB,SIGAD,SIGBD
120     EQUIVALENCE (U,Y(1)),(V,Y(2)),(W,Y(3)),(XI,Y(4)),(YI,Y(5)),
130+    (HT,Y(6)),(F,Y(7)),(Q,Y(8)),(R,Y(9))
140     DATA CON1/57.29577951/
150* COMPUTE THE INERTIAL POSITION OF THE TARGET
160     XTI=XT0+X*XTD
170     YTI=YT0+X*YTD
180     HTTI=HTT0+X*HTTD
190* COMPUTE THE TARGET POSITION RELATIVE TO THE MISSILE IN THE
200* INERTIAL AXIS SYSTEM.
210     XIMT=XTI-XI
220     YIMT=YTI-YI
230     HTMT=HTTI-HT
240* TRANSFORM THIS INTO MISSILE BODY COORDINATES.
250     XMT=T11*XIMT+T12*YIMT-T13*HTMT
260     YMT=T21*XIMT+T22*YIMT-T23*HTMT
270     ZMT=T31*XIMT+T32*YIMT-T33*HTMT
280* COMPUTE THE MOTION OF THE TARGET AS VIEWED FROM THE MISSILE
290* AXES USING THE VELOCITIES OF THE TARGET AND THE MISSILE AND
300* THE ROTATIONAL RATES OF THE MISSILE.
310     XMTD=T11*XTD+T12*YTD-T13*HTTD-U-Q*ZMT+R*YMT
320     YMTD=T21*XTD+T22*YTD-T23*HTTD-V-R*XMT+P*ZMT
330     ZMTD=T31*XTD+T32*YTD-T33*HTTD-W-P*YMT+Q*XMT
340* COMPUTE THE AZIMUTH AND ELEVATION ANGLES OF THE TARGET AS
350* SEEN BY THE MISSILE AND THEIR RESPECTIVE RATES.
360     SIGA=ATAN2(ZMT,XMT)*CON1
370     SIGB=ATAN2(YMT,XMT)*CON1
380     SIGAD=CON1*(XMT*ZMTD-XMTD*ZMT)/(XMT*XMT+ZMT*ZMT)
390     SIGBD=CON1*(XMT*YMTD-XMTD*YMT)/(XMT*XMT+YMT*YMT)
400     RETURN
410     END
```

```
10 SUBROUTINE THRUST
20 COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
30+ ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI
40+ ,VSND,SPHIW,HTE,QUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
50+ PHI,Z(14),DZ(14)
60 COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
70 THR=3000.
80 IF (X.GT.TBURN) THR=0.
90 RETURN
100 END
```

```
10      SUBROUTINE RBFRMT
20      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
30+     ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI
40+     ,VSND,SPHIW,HTE,QUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,FSI,THT,
50+     PHI,Z(14),DZ(14)
60      COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
70      DATA RMASS0/6.742/,YYI0/65.1/,XXI0/.420/,XCG0/-.321/,
80+     RMASSD/-.4506/,YYID/-3.778/,XXID/-.03889/,XCGD/.16152/
90      IF (X.GT.TBURN) GO TO 1
100*   IF THE MAIN ROCKET IS STILL ON, THE MISSILE'S MASS,MOMENTS
110*   OF INERTIA AND CG POSITION ARE CALCULATED BASED ON THE INITIAL
120*   VALUE PLUS AN AVERAGE RATE OF CHANGE TIMES THE ELAPSED TIME.
130      RMASS=RMASS0+X*RMASSD
140      XXI=XXI0+X*XXID
150      YYI=YYI0+X*YYID
160      XCG=XCG0+X*XCGD
170      1 RETURN
180      END
```

```
10      SUBROUTINE ATMOS
20      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
30+     ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI
40+     ,VSND,SPHIW,HTE,QUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT
50+     PHI,Z(14),DZ(14)
60      COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
70      COMMON/TRANS/T11,T12,T13,T21,T22,T23,T31,T32,T33
80      EQUIVALENCE (HT,Y(6))
90      RHO=.0023769-HT*.0000000688
100     VSND=1116.89-HT*.00384
110*   SET THE INERTIAL COMPONENTS OF THE WIND.
120     WINDXI=0.
130     WINDYI=0.
140*   TRANSFORM INTO MISSILE AXES.
150     WINDXB=WINDXI*T11+WINDYI*T12
160     WINDYB=WINDXI*T21+WINDYI*T22
170     WINDZB=WINDXI*T31+WINDYI*T32
180     RETURN
190     END
```

```

10      SUBROUTINE SEEKER
20      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
30+     ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI
40+     ,VSND,SPHIW,HTE,QUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
50+     PHI,Z(14),DZ(14)
60      COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
70      COMMON/TRANS/T11,T12,T13,T21,T22,T23,T31,T32,T33
80      COMMON/TARG/XTI,YTI,HTTI
90      COMMON/SEEKR/EPB,SPHI1,CPHI1,EPBC
100     EQUIVALENCE (EL,Z(1)),(ER,Z(2)),(WYX,Z(3)),(PHI1,Z(4)),
110+    (WCZ,Z(5)),(PSI2,Z(6)),(WGY,Z(7)),(WGZ,Z(8)),(PSI3,Z(9)),
120+    (THT4,Z(10)),(ELD,DZ(1)),(ERD,DZ(2)),(WYXD,DZ(3)),(PHI1D,DZ
130+    (4)),(WCZD,DZ(5)),(PSI2D,DZ(6)),(WGYD,DZ(7)),(WGZD,DZ(8)),
140+    (PSI3D,DZ(9)),(THT4D,DZ(10)),(P,Y(7)),(Q,Y(8)),(R,Y(9)),
150+    (PD,DY(7)),(QD,DY(8)),(RD,DY(9))
160     EQUIVALENCE (XI,Y(4)),(YI,Y(5)),(HT,Y(6))
170     DATA INIT/0/,T1PSI/.0125/,T2PSI/.0033/,
180+    RKPSI/-960./,EPSIDB/25./,RKBPSI/.046/,RN2/-1./,RPSI/10.5/,
190+    RIPSIB/2.3/,RKTPSI/6.54/,T2PHI/.005/,T1PHI/.025/,RKPFI/300./
200+    ,EPHIDB/25./,RKBPHI/.199/,RPHI/8.8/,RKTPHI/28.1/,RIPHIB/2.84
210+    /,RKTT/350./,RKPTE/.2/,TGYEB/4./,TGZEB/4./,F1,F2,F3,F4/10.,2
220+    .,5.,5./,PSI2L,PSI3L,THT4L/2.35,.21,.21/,CKSTP2,CKSTP3,CKSTP
230+    4/800.,400.,400./,RIYX,RIYY,RIYZ/.25,.20,.10/,HS,RIGZ,RIGY,R
240+    KHG/3.5,.009,.009,.005/,RICX,RICY,RICZ/.04,.08,.08/,RIDPSI
250+    /.0007/,RKCUI2/.8/,TYX2,TYY2,TYZ2/3*0./,TCZ3,TCY3,TCX3/3*0./,
260+    TCXE,TCYE,TCZE/3*0./,TYXU,TYYU,TYZU,TCXU,TCYU,TCZU,TRXU,
270+    TRYU,TRZU,THXU,THYU,THZU,TGYU,TGZU,TGY5,TGZ5/16*0./
280     DATA CON1/3.141592654/,CON2/6.283185308/
290     XMTI=XTI-XI
300     YMTI=YTI-YI
310     ZMTI=-(HTTI-HT)
320     RMT=SQRT(XMTI*XMTI+YMTI*YMTI+ZMTI*ZMTI)
330     RNXI=XMTI/RMT
340     RNYI=YMTI/RMT
350     RNZI=ZMTI/RMT
360     RNMX=T11*RNXI+T12*RNYI+T13*RNZI
370     RNMZ=T21*RNXI+T22*RNYI+T23*RNZI
380     RNMZ=T31*RNXI+T32*RNYI+T33*RNZI
390     IF (INIT.EQ.1) GO TO 1
400     INIT=1
410     ISWSZ=0
420     SPSI2=SQRT(RNMZ*RNMZ+RNMZ*RNMZ)
430     PSI2=ATAN2(SPSI2,RNMZ)
440     PHI1=0.
450     IF (SPSI2.NE.0.) PHI1=ATAN2(RNMZ,RNMZ)
460     1 CONTINUE
470     SPHI1=SIN(PHI1)
480     CPHI1=COS(PHI1)
490     SPSI2=SIN(PSI2)
500     CPSI2=COS(PSI2)
510     SPSI3=SIN(PSI3)
520     CPSI3=COS(PSI3)
530     STHT4=SIN(THT4)
540     CTHT4=COS(THT4)
550     SPSIT=SPSI2*CPSI3+CPSI2*SPSI3
560     CPSIT=CPSI2*CPSI3-SPSI2*SPSI3
570     EPBPSI=-RNMZ*SPSIT+RNMZ*CPHI1*CPSIT+RNMZ*SPHI1*CPSIT
580     EPBTHT=-(RNMZ*CPSIT*STHT4+RNMZ*(CPHI1*STHT4*SPSIT-SPHI1*CTHT
590+    4)+RNMZ*(CPHI1*CTHT4+SPHI1*SPSIT*STHT4))

```



```

600      RNCY=-RNMX*SPSI2+RNMY*CPSI2*CPHI1+RNMZ*CPSI2*SPHI1
610      RNCZ=-RNMZ*SPHI1+RNMZ*CPHI1
620      EPBC=SQRT(RNCY*RNCY+RNCZ*RNCZ)
630      EPB=SQRT(EPBPSI*EPBPSI+EPBTHT*EPBTHT)
640      RLAMCG=SQRT(THT4*THT4+PSI3*PSI3)
650*    CALCULATION OF GAIN COMPENSATION IN ROLL AXIS DRIVE
660      IF (ABS(PSI2).LT..579) GO TO 10
670      VCCOMP=SIGN(1.0,PSI2)
680      GO TO 30
690      10 IF (ABS(PSI2).LT..174) GO TO 20
700      VCCOMP=SIGN(3.3,PSI2)
710      GO TO 30
720      20 VCCOMP=SIGN(10.5,PSI2)
730      30 CONTINUE
740      THRESH=.10
750      IF (ISWSZ.EQ.1) THRESH=.05
760      IF (RLAMCG.GT.THRESH) GO TO 40
770      IF (ABS(PSI2).GE.THRESH ) GO TO 40
780      EPSR=0.
790      ISWSZ=0
800      GO TO 50
810      40 EPSR=-THT4*VCCOMP
820      ISWSZ=1
830      50 CONTINUE
840*    ROLL AXIS DRIVE TORQUE MOTOR
850      ERD=(EPSR-ER)/T2PHI
860      EPHID=(T1PHI*ERD+ER)*RKPHI
870      EPHIDL=BOUND(EPHIDB,EPHID)
880      EPHNET=EPHIDL-PHI1D*RKBPFI
890      RIPHI=EPHNET/RPHI
900      TYXMOT=RKTPHI*BOUND(RIPHIB,RIPHI)
910*    OUTER LOOK AXIS DRIVE TORQUE MOTOR
920      EPSL=PSI3
930      ELD=(EPSL-EL)/T2PSI
940      EPSID=(T1PSI*ELD+EL)*RKPSI
950      EPSIDL=BOUND(EPSIDB,EPSID)
960      EPSNET=EPSIDL-RKBPSI*RN2*PSI2D
970      RIPSI=EPSNET/RPSI
980      TCZMOT=RKTPSI*BOUND(RIPSIB,RIPSI)
990*    GYRO TORQUE CONTROL EQUATIONS
1000     TGYENL=RKTT*EPBPSI-RKPTE*PSI3
1010     TGZENL=-RKTT*EPBTHT+RKPTE*THT4
1020     TGYE=BOUND(TGYEB,TGYENL)
1030     TGZE=BOUND(TGZEB,TGZENL)
1040*    SEEKER YOKE DYNAMICS
1050     WYY=Q*CPHI1+R*SPHI1
1060     WYZ=-Q*SPHI1+R*CPHI1
1070     WYYD=QD*CPHI1+RD*SPHI1-PHI1D*(Q*SPHI1-R*CPHI1)
1080     WYZD=-QD*SPHI1+RD*CPHI1-PHI1D*(Q*CPHI1+R*SPHI1)
1090     TYXF1=FRICT(F1,PHI1D)
1100     TYX1=TYXMOT+TYXF1
1110     TYX=TYX2+TYXU+TYX1
1120     TYY=RIYY*WYYD+WYZ*WYX*(RIYX-RIYZ)
1130     TYZ=RIYZ*WYZD+WYX*WYY*(RIYY-RIYX)
1140     TYY1=TYY-TYY2-TYYU
1150     TYZ1=TYZ-TYZ2-TYZU
1160     TMX1=-TYX1
1170     TMY1=-(TYY1*CPHI1-TYZ1*SPHI1)
1180     TMZ1=-(TYY1*SPHI1+TYZ1*CPHI1)

```

```

1190      RICC=RICX*CPHI1*CPHI1+RICY*SPHI1*SPHI1
1200      RIYXE=RIYX+RICC
1210      WYXD=(TYX-WYY*WYZ*(RIYZ-RIYY))/RIYXE
1220      PHI1D=WYX-F
1230* SEEKER COIL HOUSING DYNAMICS
1240      WCX=WYX*CPSI2+WYY*SPSI2
1250      WCY=-WYX*SPSI2+WYY*CPSI2
1260      TCZF2=FRICT(F2,PSI2D)
1270      TCZS2=STOPS(CKSTP2,PSI2L,PSI2)
1280      TCZ2=(TCZMOT-(RN2-1.)*RIDPSI*WYZD)*RN2+TCZF2+TCZS2-RKCU2*
1290+     PSI2
1300      TCZ=TCZ2+TCZU+TCZ3+TCZE
1310      WCZD=(TCZ-WCX*WCY*(RICY-RIX))/ (RICZ+RN2*RN2*RIDPSI)
1320      PSI2D=WCZ-WYZ
1330      TCXLI=RIX*(WYYD*SPSI2-PSI2D*(WYX*SPSI2-WYY*CPSI2))+WCY*WCZ
1340+     *(RICZ-RIY)
1350      TCYLI=RIY*(WYYD*CPSI2-PSI2D*(WYX*CPSI2+WYY*SPSI2))+WCZ*WCX
1360+     *(RIX-RIY)
1370      TCX2=TCXLI-TCX3-TCXE-TCXU
1380      TCY2=TCYLI-TCY3-TCYE-TCYU
1390      TYX2=- (TCX2*CPSI2-TCY2*SPSI2)
1400      TYY2=- (TCX2*SPSI2+TCY2*CPSI2)
1410      TYZ2=-TCZ2
1420* GYRO DYNAMICS
1430      TGY=TGY5+TGYE+TGYU
1440      TGZ=TGZ5+TGZE+TGZU
1450      TGYEFF=TGY-HS*WGZ-(RKHG/RIGZ)*(TGZ+HS*WGY)
1460      TGZEFF=TGZ+HS*WGY+(RKHG/RIGY)*(TGY-HS*WGZ)
1470      WGYD=TGYEFF/(RIGY+RKHG*RKHG/RIGZ)
1480      WGZD=TGZEFF/(RIGZ+RKHG*RKHG/RIGY)
1490* GYRO HOUSING DYNAMICS
1500      WHY=WGY
1510      WHZ=WGZ
1520      WRX=WCX*CPSI3+WCY*SPSI3
1530      WRY=-WCX*SPSI3+WCY*CPSI3
1540      WRZ=(WHZ-WRX*STHT4)/CTHT4
1550      PSI3D=WRZ-WCZ
1560      THT4D=WHY-WRY
1570      TRZF3=FRICT(F3,PSI3D)
1580      TRZS3=STOPS(CKSTP3,PSI3L,PSI3)
1590      TRZ3=TRZS3+TRZF3
1600      TRZ4=- (TRZ3+TRZU)
1610      THYF4=FRICT(F4,THT4D)
1620      THYS4=STOPS(CKSTP4,THT4L,THT4)
1630      THX4=-THXU
1640      THY4=THYF4+THYS4
1650      THZ4=- (TRZ4+THX4*STHT4)/CTHT4
1660      THY5=- (THYU+THY4)
1670      THZ5=- (THZ4+THZU)
1680      TGY5=-THY5
1690      TGZ5=-THZ5
1700      TRX4=- (THX4*CTHT4+THZ4*STHT4)
1710      TRY4=-THY4
1720      TRX3=- (TRX4+TRXU)
1730      TRY3=- (TRY4+TRYU)
1740      TCZ3=-TRZ3
1750      TCX3=- (TRX3*CPSI3-TRY3*SPSI3)
1760      TCY3=- (TRX3*SPSI3+TRY3*CPSI3)
1770      TCYE=-TGYE

```

PAGE 4

SEEKER

03/28/73. 16.33.16

1780
1790
1800

TCZE=-TGZE
RETURN
END

```
1810* FUNCTION ROUTINE FOR A LIMITER.  
1820     FUNCTION BOUND(XL,X)  
1830     BOUND=X  
1840     IF (ABS(X).GE.XL) BOUND=SIGN(XL,X)  
1850     RETURN  
1860     END
```

```
1870* FUNCTION ROUTINE FOR FRICTION.  
1880     FUNCTION FRICT(FL,X)  
1890     IF (X) 1,2,3  
1900     1 FRICT=FL  
1910     RETURN  
1920     2 FRICT=0.  
1930     RETURN  
1940     3 FRICT=-FL  
1950     RETURN  
1960     END
```

```
1970* FUNCTION ROUTINE FOR STOPS WITH COMPLIANCE.
1980     FUNCTION STOPS(SLOPE,XT,X)
1990     STOPS=0.
2000     DEL=ABS(X)-XT
2010     IF (DEL.GE.0.) STOPS=SLOPE*SIGN(DEL,X)
2020     RETURN
2030     END
```

10 SUBROUTINE SEEKER
1810* FUNCTION ROUTINE FOR A LIMITER.
1870* FUNCTION ROUTINE FOR FRICTION.
1970* FUNCTION ROUTINE FOR STOPS WITH COMPLIANCE.

```

10      SUBROUTINE CTLSYS
20      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
30+    ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI
40+    ,VSND,SPHIW,HTE,QUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
50+    PHI,Z(14),DZ(14)
60      COMMON NDIM,IPRINT,NSTEP,NFRINT,ICOUNT,IRATE,IRATIO,NDIMF
70      COMMON/CTLSYJ/ IJET(4)
80      COMMON/SEEKR/EPB,SPHI1,CPHI1,EPBC
90*    COMMUNICATIONS WITH SUBROUTINE TARGET
100     COMMON/SEEKR1/SIGA,SIGB,SIGAD,SIGBD
110     EQUIVALENCE (HT,Y(6)),(PSI2,Z(6)),(PSI2D,DZ(6))
115     EQUIVALENCE (PHI1D,DZ(4))
120     DATA TBJRC/1.2/
130     DATA CON1/.18/
140*   ENABLE THE CONTROL SYSTEM AT THE ENABLE HEIGHT.
150     IF (HT-HTE) 1,2,2
160     1 IJRC=0
170     TSJRC=X
180     GO TO 3
190     2 IJRC=1
200*   DETERMINE WHETHER THE JRC BURN TIME HAS BEEN EXCEEDED, AND IF
210*   SO, DISENABLE THE JRC'S.
220     IF ((X-TSJRC).GT.TBJRC) IJRC=0
230     3 IF (IJRC) 4,4,5
240     4 IJET(1)=0
250     IJET(2)=0
260     IJET(3)=0
270     IJET(4)=0
280     GO TO 6
290*   DETERMINE THE JRC STATES BASED ON THE CONTROL LAW.
300*   PRMTY CONTROLS THE JETS ON THE Y AXIS WHILE PRMTZ CONTROLS
310*   THE JETS ON THE Z AXIS. "IJET(1)"=1 SIGNIFIES THAT JET 1 IS ON.
320     5 PRMTY=SIGB+CON1*SIGBD
330     PRMTZ=SIGA+CON1*SIGAD
340     IF (PRMTZ) 7,8,9
350     7 IJET(1)=1
360     IJET(3)=0
370     GO TO 10
380     8 IJET(1)=0
390     IJET(3)=0
400     GO TO 10
410     9 IJET(1)=0
420     IJET(3)=1
430     10 IF (PRMTY) 11,12,13
440     11 IJET(2)=1
450     IJET(4)=0
460     GO TO 6
470     12 IJET(2)=0
480     IJET(4)=0
490     GO TO 6
500     13 IJET(2)=0
510     IJET(4)=1
520     6 CONTINUE
530*   THE CANARD DEFLECTIONS ARE SET TO ZERO
540     PCAN=0.
550     YCAN=0.
560     RETURN
570     END

```



```
10      SUBROUTINE AERO
20      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
30+     ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI
40+     ,VSND,SPHIW,HTE,QUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
50+     PHI,Z(14),DZ(14)
60      COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
70*     COMMUNICATION WITH AROBSE
80      COMMON/AROB/XFB,YFB,ZFB,XMB,YMB,ZMB
90*     COMMUNICATION WITH AROJRC
100     COMMON/AROJ/YFJ,ZFJ,YMJ,ZMJ
110*    DETERMINE BASELINE AERODYNAMIC FORCES AND MOMENTS.
120     CALL AROBSE
130*    DETERMINE FORCES AND MOMENTS DUE TO THE JRC.
140     CALL AROJRC
150*    SUM THE FORCES.
160     XFA=XFB
170     YFA=YFB+YFJ
180     ZFA=ZFB+ZFJ
190*    SUM THE MOMENTS AND TRANSFER REFERENCE POINT TO THE
200*    MISSILE CG.
210     XM=XMB
220     YM=YMB+YMJ+ZFA*XCG
230     ZM=ZMB+ZMJ-YFA*XCG
240     RETURN
250     END
```

```

10      SUBROUTINE AROBSE
20      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB, RMACH
30+    ,CPHIW,XFA,YFA,ZFA,THR,XCG, RMASS,PCAN,YCAN, XM, YM, ZM, XXI, YYI
40+    ,VSND,SPHIW,HTE,GUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
50+    FHI,Z(14),DZ(14)
60      COMMON NDIM,IFRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
70      COMMON/AERO1/DPHI,DALPHA
80      COMMON/AROB/XFB,YFB,ZFB,XMB,YMB,ZMB
90      DIMENSION CXB(25,3),CYPB(25,3),CZPB(25,3),CLB(25,3),
100+    CMPB(25,3),CNPB(25,3)
110     DATA CXB /75*0./
120     DATA CYPB/75*0./
130     DATA CZPB/
140+    0.,-2.,-4.0,-6.5,-10.0,-13.0,-17.0,-21.0,-25.0,-29.5,
150+    -34.0,-38.0,-42.0,-45.0,-48.0,-51.0,-52.5,-52.5,-51.0,
160+    -46.0,-45.0,-45.0,-45.0,-45.0,-45.0,
170+    0.,-2.,-4.5,-8.0,-12.0,-16.0,-20.5,-25.0,-29.5,-34.5,
180+    -39.0,-43.0,-47.0,-50.0,-52.5,-52.5,-48.0,-45.0,-49.0,
190+    -51.0,-52.0,-53.5,-54.5,-55.5,-55.5,
200+    0.,-2.,-4.0,-6.5,-10.0,-13.0,-17.0,-21.0,-25.0,-29.5,
210+    -34.0,-38.0,-42.0,-45.0,-48.0,-51.0,-52.5,-52.5,-51.0,
220+    -46.0,-45.0,-45.0,-45.0,-45.0,-45.0/
230     DATA CLB /75*0./
240     DATA CMPB/
250+    0.,-8.,-16.,-26.,-40.,-60.,-80.,-100.,-124.,-142.,
260+    -164.,-186.,-210.,-230.,-256.,-278.,-290.,-290.,-266.,
270+    -206.,-178.,-166.,-160.,-158.,-158.,
280+    0.,-8.,-20.,-36.,-56.,-76.,-100.,-128.,-158.,-184.,
290+    -214.,-238.,-264.,-282.,-300.,-286.,-250.,-200.,-214.,
300+    -218.,-218.,-218.,-218.,-220.,-220.,
310+    0.,-8.,-16.,-26.,-40.,-60.,-80.,-100.,-124.,-142.,
320+    -164.,-186.,-210.,-230.,-256.,-278.,-290.,-290.,-266.,
330+    -206.,-178.,-166.,-160.,-158.,-158./
340     DATA CNPB/75*0./
350     DATA CON1/45./,CON2/2.5/,CON3/90./
360     DATA DIA/.4166666667/,S/.1363538470/
370     PHIWT=AMOD(ABS(PHIW),CON3)
380     PHIWTE=PHIWT/CON1+1.0
390     IP=PHIWTE
400     DPHI=PHIWTE-IP
410     ALPHAE=ALPHA/CON2+1.0
420     IA=ALPHAE
430     IF (IA.GE.25) IA=24
440     DALPHA=ALPHAE-IA
450     CALL INTER2(CXB (IA,IP),CXB (IA+1,IP),CXB (IA,IP+1),
460+    CXB (IA+1,IP+1),CX )
470     CALL INTER2(CYPB(IA,IP),CYPB(IA+1,IP),CYPB(IA,IP+1),
480+    CYPB(IA+1,IP+1),CYP)
490     CALL INTER2(CZPB(IA,IP),CZPB(IA+1,IP),CZPB(IA,IP+1),
500+    CZPB(IA+1,IP+1),CZP)
510     CALL INTER2(CLB (IA,IP),CLB (IA+1,IP),CLB (IA,IP+1),
520+    CLB (IA+1,IP+1),CL )
530     CALL INTER2(CMPB(IA,IP),CMPB(IA+1,IP),CMPB(IA,IP+1),
540+    CMPB(IA+1,IP+1),CMP)
550     CALL INTER2(CNPB(IA,IP),CNPB(IA+1,IP),CNPB(IA,IP+1),
560+    CNPB(IA+1,IP+1),CNF)
570     CY=CYP*CPHIW+CZP*SPHIW
580     CZ=-CYP*SPHIW+CZP*CPHIW
590     CM=CMF*CPHIW+CNF*SPHIW

```

```
600      CN=-CMP*SPHIW+CNP*CPHIW
610      XFB=QUE*S*CX
620      YFB=QUE*S*CY
630      ZFB=QUE*S*CZ
640      XMB=QUE*S*DIA*CL
650      YMB=QUE*S*DIA*CM
660      ZMB=QUE*S*DIA*CN
670      RETURN
680      END
```

```

10      SUBROUTINE AROJRC
20      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
30+     ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI
40+     ,VSND,SPHIW,HTE,CUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
50+     PHI,Z(14),DZ(14)
60      COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
70      COMMON/AEP01/DPHI,DALPHA
80      COMMON/CTLSYJ/ IJET(4)
90      COMMON/AROJ/YFJ,ZFJ,YMJ,ZMJ
100     DIMENSION RKYB(25,3),RKZB(25,3),RKMB(25,3),RKNB(25,3)
110     DIMENSION CPE(4),SPE(4)
120     DATA RKYB/75*0./
130     DATA RKZB/
140+    -1.0,-1.0,-1.0,-1.0,-1.0,-.99,-.97,-.92,
150+    -.88,-.86,-.81,-.76,-.70,-.62,-.58,-.53,
160+    -.52,-.53,-.58,-.66,-.72,-.78,-.80,-.82,-.82,
170+    50*-1.0/
180     DATA RKMB/
190+    1.0,1.0,1.0,1.0,1.0,1.03,1.06,1.10,
200+    1.16,1.22,1.29,1.38,1.47,1.54,1.60,1.63,
210+    1.65,1.60,1.48,1.30,1.18,1.08,1.04,1.04,1.04,
220+    50*1.0/
230     DATA RKNB/75*0./
240     DATA TJRC/450./,XJET/2.434/
250     DATA CON1/90./,CON2/2.5/,CON3/180./
260     DATA PHIE1/0./
270     DATA CPE/1.,0.,-1.,0./,SPE/0.,1.,0.,-1./
280     ALPHAE=ALPHA/CON2+1.0
290     IA=ALPHAE
300     IF (IA.GE.25) IA=24
310     DALPHA=ALPHAE-IA
320     RKY=0.
330     RKZ=0.
340     RKM=0.
350     RKN=0.
360     DO 1 I=1,4
370     IF (IJET(I).EQ.0) GO TO 1
380     PHIJ=PHIW-PHIE1-CON1*(I-1.)
390     CP=CPE(I)
400     SP=SPE(I)
410     IF (ABS(PHIJ).GT.180.) PHIJ=PHIJ-SIGN(360.,PHIJ)
420     PHIJT=ABS(PHIJ)
430     PHIJTE=PHIJT/CON1+1.0
440     IF=PHIJTE
450     IF (IF.GE.3) IP=2
460     DPHI=PHIJTE-IF
470     CALL INTER2(RKYB(IA,IP),RKYB(IA+1,IP),RKYB(IA,IP+1),
480+    RKYB(IA+1,IP+1),RKYJ)
490     CALL INTER2(RKZB(IA,IP),RKZB(IA+1,IP),RKZB(IA,IP+1),
500+    RKZB(IA+1,IP+1),RKZJ)
510     CALL INTER2(RKMB(IA,IP),RKMB(IA+1,IP),RKMB(IA,IP+1),
520+    RKMB(IA+1,IP+1),RKMJ)
530     CALL INTER2(RKNB(IA,IP),RKNB(IA+1,IP),RKNB(IA,IP+1),
540+    RKNB(IA+1,IP+1),RKNJ)
550     IF (PHIJ.GE.0.) GO TO 2
560     RKYJ=-RKYJ
565     RKNJ=-RKNJ
570     2 RKY=RKY+RKYJ*CP +RKZJ*SP
580     RKZ=RKZ-RKYJ*SP +RKZJ*CP

```

590 RKM=RKM+RKMJ*CP +RKNJ*SP
600 RKN=RKN-RKMJ*SP +RKNJ*CP
610 1 CONTINUE
620 YFJ=RKY*TJRC
630 ZFJ=RKZ*TJRC
640 YMJ=RKM*TJRC*XJET
650 ZMJ=RKN*TJRC*XJET
660 RETURN
670 END

```

00100      SUBROUTINE OUTPUT1
00110      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
00120+      ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI

00130+      ,VSND,SPHIW,HTE,GUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
00140+      PHI,Z(14),DZ(14)
00150      COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
00160      DIMENSION OUT(40,30),IOUT(40,4)
00170      100 FORMAT(F6.3,6F8.2)
00180      101 FORMAT(F6.3,3F8.2,3F7.2)
00190      102 FORMAT(F6.3,8F7.2)
00200      103 FORMAT(/,2X,*TIME*,5X,*U*,7X,*V*,7X,*W*,7X,*XI*,6X,
00210+      *YI*,6X,*HT*)
00220      104 FORMAT(/,2X,*TIME*,5X,*P*,7X,*Q*,7X,*R*,5X,*PSI*,4X,*THT*,
00230+      4X,*PHI*)
00240      105 FORMAT(/,2X,*TIME*,2X,*ALPHA*,3X,*PHIW*,3X,*PHI1*,
00250+      3X,*PSI2*,2X,*PSI3*,2X,*THT4*,4X,*EPB*,3X,*EPBC*)
00260      106 FORMAT(F6.3,4(5X,I1))
00270      107 FORMAT(/,*JET STATES. 1=ON, 0=OFF*,/)
00280      108 FORMAT(/,2X,*TIME*,2X,*WYOKE*,2X,*WCOIL*,4X,*WGY*,
00290+      4X,*WGZ*,2X,*PHI1D*,2X,*PSI2D*)
00300      200 FORMAT(/,*STEP SIZE=*,F6.4,2X,*IRATIO=*,I2)
00310      DO 10 I=1,ICOUNT
00320* READ ALL THE OUTPUTED VARIABLES.
00330      10 READ(2,)(OUT(I,J),J=1,27),(IOUT(I,J),J=1,4)
00340* OUTPUT THESE VARIABLES TO THE TTY IN APPROPRIATE COLUMNS WITH
00350* HEADINGS.
00360      PRINT 103
00370      DO 1 I=1,ICOUNT
00380      1 PRINT 100, (OUT(I,J),J=1,7)
00390      PRINT 104
00400      DO 2 I=1,ICOUNT
00410      2 PRINT 101, OUT(I,1),(OUT(I,J),J=8,13)
00420      PRINT 105
00430      DO 3 I=1,ICOUNT
00440      3 PRINT 102, OUT(I,1),(OUT(I,J),J=14,21)
00450      PRINT 108
00460      DO 5 I=1,ICOUNT
00470      5 PRINT 102, OUT(I,1),(OUT(I,J),J=22,27)
00480      PRINT 107
00490      DO 4 I=1,ICOUNT
00500      4 PRINT 106, OUT(I,1),(IOUT(I,J),J=1,4)
00510      PRINT 200, H,IRATIO
00520      STOP
00530      END

```

```

00010      SUBROUTINE INTEG
00020      COMMON Y( 9),DY( 9),X,H,WINDXB,WINDYB,WINDZB,RMACH
00030+      ,CPHIW,XFA,YFA,ZFA,THR,XCG,RMASS,PCAN,YCAN,XM,YM,ZM,XXI,YYI

00040+      ,VSND,SPHIW,HTE,GUE,ALPHA,PHIW,XMAX,TBURN,RHO,VEL,PSI,THT,
00050+      PHI,Z(14),DZ(14)
00060      COMMON NDIM,IPRINT,NSTEP,NPRINT,ICOUNT,IRATE,IRATIO,NDIMF
00070* STORAGE LOCATIONS FOR THE REQUIRED PAST STATE VARIABLES AND
00080* THEIR DERIVATIVES. "AUX" FOR Y(I) AND "BUX" FOR Z(I).
00090      DIMENSION AUX1( 9),AUX2( 9),AUX3( 9),AUX4( 9),AUX5( 9),
00100+      AUX6( 9),AUX7( 9),AUX8( 9),BUX1(14),BUX2(14),BUX3(14),
00110+      BUX4(14),BUX5(14),BUX6(14),BUX7(14),BUX8(14)
00120      DATA IENTR/1/,IENTRF/2/
00140      IF (IRATE.EQ.1) GO TO 100
00150* DECIDE WHETHER TO 1) PREDICT REQUIRED STARTING VALUES BY
00160* AN EULER BACKSTEP METHOD, 2) PERFORM PREDICTION OF THE Y(I)
00170* VARIABLES DURING INTEGRATION, OR 3) CORRECT THE Y(I) VARIABLES
00180* DURING INTEGRATION.
00190      IF (IENTR-2) 20,21,22
00200* DETERMINE REQUIRED STARTING VALUES USING AN EULER BACKSTEP, AND
00210* STORE INTO APPROPRIATE LOCATIONS.
00220      20 HS=IRATIO*H
00230      H1=3.*HS
00240      H3=4./3.*HS
00250      G1=3.*H
00260      G3=4./3.*H
00270      C1=112./121.
00280      C2=9./121.
00290      DO 16 I=1,NDIM
00300      AUX2(I)=Y(I)-HS*DY(I)
00310      AUX3(I)=Y(I)-2.*HS*DY(I)
00320      AUX4(I)=Y(I)-3.*HS*DY(I)
00330      AUX6(I)=DY(I)
00340      AUX7(I)=DY(I)
00350      16 AUX8(I)=0.
00360      DO 26 I=1,NDIMF
00370      BUX2(I)=Z(I)-H*DZ(I)
00380      BUX3(I)=Z(I)-2.*H*DZ(I)
00390      BUX4(I)=Z(I)-3.*H*DZ(I)
00400      BUX6(I)=DZ(I)
00410      BUX7(I)=DZ(I)
00420      26 BUX8(I)=0.
00430* PREDICT THE Y(I) VARIABLES.
00440      21 DO 17 I=1,NDIM
00450      AUX1(I)=Y(I)
00460      AUX5(I)=DY(I)
00470      DELT=AUX4(I)+H3*(AUX5(I)+AUX5(I)-AUX6(I)+AUX7(I)+AUX7(I))
00480      Y(I)=DELT-C1*AUX8(I)
00490      17 AUX8(I)=DELT
00500      IENTR=3
00510      GO TO 100
00520* CORRECT THE Y(I) VARIABLES.
00530      22 DO 18 I=1,NDIM
00540      DELT=.125*(9.*AUX1(I)-AUX3(I)+H1*(DY(I)+AUX5(I)+AUX5(I)
00550+      -AUX6(I)))
00560      AUX8(I)=AUX8(I)-DELT
00570      18 Y(I)=DELT+C2*AUX8(I)
00580      DO 19 I=1,NDIM
00590      AUX7(I)=AUX6(I)
00600      AUX6(I)=AUX5(I)

```

```
00610      AUX4(I)=AUX3(I)
00620      AUX3(I)=AUX2(I)
00630      19 AUX2(I)=AUX1(I)
00640      IENTR=2
00650* NOW TO REPEAT FOR THE Z(I) VARIABLES.
00660* DETERMINE WHETHER TO PREDICT OR CORRECT THE Z(I) VARIABLES.
00670      100 IF (IENTRF.EQ.3) GO TO 32
00680* PREDICT THE Z(I) VARIABLES.
00690      DO 27 I=1,NDIMF
00700          BUX1(I)=Z(I)
00710          BUX5(I)=DZ(I)
00720          DELT=BUX4(I)+G3*(BUX5(I)+BUX5(I)-BUX6(I)+BUX7(I)+BUX7(I))
00730          Z(I)=DELT-C1*BUX8(I)
00740      27 BUX8(I)=DELT
00750* UPDATE THE VARIABLE TIME BY "H" AFTER EACH PREDICTION.
00760      NSTEP=NSTEP+1
00770      X=NSTEP*H
00780      IPRINT=0
00790      IENTRF=3
00800      RETURN
00810* CORRECT THE Z(I) VARIABLES.
00820      32 DO 28 I=1,NDIMF
00830          DELT=.125*(9.*BUX1(I)-BUX3(I)+G1*(DZ(I)+BUX5(I)+BUX5(I)
00840+          -BUX6(I)))
00850          BUX8(I)=BUX8(I)-DELT
00860      28 Z(I)=DELT+C2*BUX8(I)
00870      DO 29 I=1,NDIMF
00880          BUX7(I)=BUX6(I)
00890          BUX6(I)=BUX5(I)
00900          BUX4(I)=BUX3(I)
00910          BUX3(I)=BUX2(I)
00920      29 BUX2(I)=BUX1(I)
00930          IENTRF=2
00940          IPRINT=1
00950          RETURN
00960          END
```



```
10      SUBROUTINE INTER2(C00,C10,C01,C11,CB)
20* PERFORMS A TWO DIMENSIONAL INTERPOLATION BETWEEN THE FOUR CORNERS
30* OF THE SQUARE C00-C11 AND RETURNS THE ANSWER BY CB.
40* COMMUNICATIONS WITH SUBROUTINE AERO WHICH CALLS INTER2.
50* DPFI AND DALPHA ARE THE INTERPOLATION INCREMENTS.
60      COMMON/AERO1/DPFI,DALPHA
70      C1=C00+DALPHA*(C10-C00)
80      C2=C01+DALPHA*(C11-C01)
90      CB=C1+DPFI*(C2-C1)
100     RETURN
110     END
```

READY.
FORTRAN, OLD, SXDF

READY.
RUN, M=11000

03/28/73. 17.05.04
PROGRAM SXDF

INPUT H, XMAX, NPRINT, IRATIO
? .0005, 2., 200, 10
INPUT XT0, YT0, HTT0, XTD, YTD, HTTD
? 9000, 3000, 100, 0, 0, 0

TIME	U	V	W	XI	YI	HT
0.	0.	0.	0.	0.	0.	0.
.100	41.41	0.	.00	.00	0.	2.07
.200	83.14	1.29	1.29	.02	.02	8.29
.300	124.61	-9.71	-7.74	.61	.55	18.68
.400	157.77	-18.84	-47.56	2.57	1.36	33.11
.500	166.45	-20.10	-114.34	7.15	2.96	50.89
.600	175.92	-36.26	-150.15	15.35	5.63	71.00
.700	196.31	-47.88	-166.24	27.98	9.39	91.98
.800	227.44	-52.29	-169.56	45.23	14.44	112.76
.900	266.06	-51.83	-162.85	67.10	20.97	132.50
1.000	308.77	-49.27	-150.62	93.59	29.04	150.66
1.100	353.54	-45.26	-136.15	124.68	38.69	166.91
1.200	400.89	-39.66	-118.95	160.36	49.92	181.18
1.300	449.40	-34.79	-100.35	200.65	62.74	193.53
1.400	498.01	-30.25	-86.66	245.59	77.18	204.17
1.500	552.44	-14.23	-36.64	295.19	93.24	213.61
1.600	601.57	11.12	37.54	349.48	110.87	222.88
1.700	645.79	27.02	80.41	408.31	129.98	233.29
1.800	698.37	16.60	45.12	471.48	150.43	245.71
1.900	749.20	-10.08	-34.29	539.20	172.30	259.58
2.000	796.43	-23.79	-70.56	611.76	195.74	273.45

TIME	P	Q	R	PSI	THT	PHI
0.	0.	0.	0.	0.	90.00	0.
.100	0.	0.	0.	0.	90.00	0.
.200	0.	-.52	.52	45.00	89.32	45.00
.300	0.	-2.43	1.31	41.34	77.76	41.40
.400	0.	-4.24	-.16	18.61	59.74	20.22
.500	0.	-3.25	1.12	11.62	35.64	14.61
.600	0.	-1.80	1.03	14.15	20.65	15.77
.700	0.	-1.00	.64	16.17	11.83	16.32
.800	0.	-.53	.19	17.03	6.90	16.46
.900	0.	-.25	.23	17.59	4.18	16.52
1.000	0.	-.23	.03	17.90	2.58	16.54
1.100	0.	-.15	.11	18.13	1.45	16.55
1.200	0.	.11	.09	18.23	1.12	16.55
1.300	0.	-.10	.07	18.40	1.03	16.55
1.400	0.	.26	-.06	18.39	.92	16.55
1.500	0.	1.16	-.39	18.30	5.77	16.54
1.600	0.	1.15	-.40	17.99	13.22	16.49
1.700	0.	.17	-.09	17.68	17.58	16.41
1.800	0.	-.98	.31	17.66	14.66	16.40
1.900	0.	-1.07	.37	17.90	7.83	16.45
2.000	0.	.02	.01	18.12	4.35	16.47

TIME	ALPHA	PHIW	PHI1	PSI2	PSI3	THT4	EPB	EPBC
0.	0.	0.	71.57	89.40	0.	0.	.00	.00
.100	0.	0.	71.54	89.28	.13	.00	.03	.13
.200	1.25	45.00	71.57	88.88	-.02	-.04	.05	.04
.300	5.69-128.55		71.86	78.33	-.10	-.17	.03	.18
.400	17.96-158.39		70.92	59.40	-.10	.80	.03	.81
.500	34.90-170.03		64.24	36.08	-.16	.32	.02	.35
.600	41.28-166.42		62.46	21.07	-.18	.09	.02	.21
.700	41.39-163.93		62.35	12.18	-.19	-.10	.02	.20
.800	37.96-162.86		62.43	7.30	-.20	.02	.03	.19
.900	32.71-162.35		61.75	4.64	-.16	-.04	.03	.19
1.000	27.17-161.89		62.99	3.10	-.17	.02	.01	.16
1.100	22.09-161.61		62.93	2.03	-.16	-.02	.01	.15
1.200	17.37-161.56		62.97	1.59	.06	-.05	.04	.08
1.300	13.30-160.88		63.01	1.67	-.10	-.26	.03	.25
1.400	10.44-160.75		63.05	1.51	.06	-.19	.03	.22
1.500	4.07-158.77		63.43	6.23	.20	-.97	.02	.98
1.600	3.72	16.50	71.49	13.76	.23	.02	.03	.24
1.700	7.48	18.57	71.23	18.22	.21	.02	.02	.22
1.800	3.94	20.20	70.80	15.76	-.16	.09	.02	.17
1.900	2.73-163.62		69.92	9.06	-.17	.04	.03	.19
2.000	5.34-161.37		69.50	5.64	-.15	.00	.03	.15

TIME	WYOKE	WCOIL	WGY	WGZ	PHI1D	PSI2D
0.	0.	0.	0.	0.	0.	0.
.100	-.02	.03	.02	.03	-.02	.03
.200	.00	.19	-.06	-.01	.00	-.48
.300	.10	-.02	.01	-.02	.10	-2.73
.400	-.81	.06	-.03	.02	-.81	-3.90
.500	-.70	.02	.01	.04	-.70	-3.39
.600	-.03	.03	.01	.03	-.03	-2.04
.700	.20	-.01	.01	-.01	.20	-1.20
.800	-.03	-.01	-.04	-.02	-.03	-.57
.900	.21	.06	-.10	.04	.21	-.27
1.000	-.16	.03	-.09	.00	-.16	-.19
1.100	-.01	.00	.01	.01	-.01	-.18
1.200	-.01	-.04	-.04	-.01	-.01	.02
1.300	-.01	-.01	.02	.01	-.01	-.13
1.400	-.01	-.07	-.04	.03	-.01	.20
1.500	1.60	.00	-.01	-.03	1.60	1.22
1.600	-.08	-.02	-.03	.05	-.08	1.20
1.700	-.03	-.00	-.04	-.02	-.03	.19
1.800	-.07	.02	-.06	.01	-.07	-1.01
1.900	-.54	.05	-.03	.05	-.54	-1.08
2.000	-.14	-.07	-.03	.05	-.14	-.05

JET STATES. 1=ON, 0=OFF

0.	0	0	0	0
.100	0	0	0	0
.200	0	0	1	1
.300	0	1	1	0
.400	0	0	1	1
.500	1	0	0	1
.600	0	1	1	0
.700	0	1	1	0
.800	0	0	1	1
.900	0	1	1	0
1.000	0	0	1	1
1.100	0	1	1	0
1.200	0	1	1	0
1.300	0	1	1	0
1.400	0	0	0	0
1.500	0	0	0	0
1.600	0	0	0	0
1.700	0	0	0	0
1.800	0	0	0	0
1.900	0	0	0	0
2.000	0	0	0	0

STEP SIZE= .0005 IRATIO=10
STOP.

APPENDIX B
PROGRAM VARIABLES

The following is an alphabetical listing of the computer program variables except for the variables in subroutine SEEKER.

ALPHA	Missile angle of attack
ALPHAE	Angle of attack entry argument for coefficient table lookup
AUX 1	Storage locations for integration routine used for HS.
:	$Y_i, Y_{i-1}, Y_{i-2}, Y_{i-3}, DY_i, DY_{i-1}, DY_{i-2}$, truncation corrector
AUX 8	respectively
BUX 1	Storage locations for integration routine used for H.
:	$Z_i, Z_{i-1}, Z_{i-2}, Z_{i-3}, DZ_i, DZ_{i-1}, DZ_{i-2}$, truncation corrector
BUX 8	respectively
C1, C2	Intermediate answers for 2-D coefficient lookup
COO, C10	Entry points for 2-D coefficient lookup
CO1, C11	
CB	Coefficient value return by 2-D coefficient lookup
CL	Aerodynamic total rolling moment coefficient in body fixed axes
CM	Aerodynamic total pitching moment coefficient in body fixed axes
CMP	Aerodynamic total pitching moment coefficient in pitch axes
CMPB	Array of pitching moment coefficient for baseline missile (no JRC) vs α and ϕ_w
CN	Aerodynamic total yawing moment coefficient in body fixed axes
CNP	Aerodynamic total yawing moment coefficient in pitch axes
CNPB	Array of yawing moment coefficient for baseline missile (no JRC) vs α and ϕ_w
CON1	Program constants
:	
CON4	
CP	Dummy variable
CPE	Vector of cosines of ϕ_E for each engine
CPH11	$\text{Cos}(\phi_1)$
CPHIW	$\text{Cos}(\phi_w)$
CX	Aerodynamic total X force coefficient in body fixed axes
CXB	Array of X force coefficient for baseline missile (no JRC) vs α and ϕ_w
CY	Aerodynamic total Y force coefficient in pitch axes

CYP	Aerodynamic total Y force coefficient in body fixed axes
CYPB	Array of Y force coefficients for baseline missile (no JRC) vs α and ϕ_w
CZ	Aerodynamic total Z force coefficient in body fixed axes
CZP	Aerodynamic total Z force coefficient in pitch
CZPB	Array of Z force coefficients for baseline missile (no JRC) vs α and ϕ_w
DALPHA	The residule of α required for 2-D coefficient lookup
DELTA	Intermediate variable in integration routine
DIA	Missile diameter
DPHI	The residule of ϕ_w required for 2-D coefficient lookup
DY	Vector of derivatives of Y
DZ	Vector of derivatives of Z
EO	Quaterion variables
⋮	
E3	
EOD	Derivatives of EO-E3
⋮	
E3D	
EPB	Angular error between gyro spin axis and target line of sight in radians
EPBC	Angular error between coil housing axis and target line of sight in radians
EPBCO	EPBC in degrees for outputting
EPS	Error due to non-orthogonality of EO-E3
G1, G3	Internal constants for integration routine
GRAV	Gravity in ft/sec ²
H1, H3	Internal constants for integration routine
H	Step size for fast integration routine
HS	Step size for slow integration routine
HT	Altitude of missile
HTD	Derivative of HT
HTMT	Altitude difference between missile and target
HTTO	Initial height of target
HTTD	Target climb rate
HTTI	Altitude of target
IA	Entry location on α for 2-D coefficient lookup

ICOUNT	Number of times outputting is performed
IENTR	1--Calculate required starting values, 2--Predict Y(I) for integration, 3--Correct Y(I) for integration
IENTRF	2--Predict Z(1) for integration, 3--Correct Z(I) for integration
IJET	Array for each jet; 0--off, 1--on
IOUT	Array for outputting interger variables
IP	Entry location on $\bar{\phi}_w$ for 2-D coefficient lookup
IPRINT	0--No outputting permitted, 1--Outputting permitted
IRATE	Controls integration routine; 0--Integrate both Y and Z, 1--Integrate only Z
IRATIO	HS/H
IRT2	2* IRATIO
NDIM	Dimension of Y(I)
NDIMF	Dimension of Z(I)
NPRINT	Outputting interval = NPRINT*H
NSTEP	Counter for number of H integration steps
OUT	Array for outputting real variables
P	Missile roll rate in body axes in rad/sec
PCAN	Pitch canard deflection
PD	Derivative of P
PHI	$\bar{\phi}$ in degrees
PHI1	$\bar{\phi}_1$ in radians
PHI10	PHI1 in degrees for outputting
PHI1D	Derivative of PHI1
PHI1L	$\bar{\phi}_E$ for thruster number 1
PHIJ	$\bar{\phi}_J$ for thruster in degrees
PHIW	$\bar{\phi}_w$ in degrees
PHIWT	$\bar{\phi}_w$ reduced to a range of 0 - 90 degrees
PHIWTE	$\bar{\phi}_w$ entry argument for coefficient table lookup
PRMT	Dummy variable
PRMTY	Control function for JRC's aligned with missile Y axis
PRMTZ	Control function for JRC's aligned with missile Z axis
PSI	ψ in degrees
PSI2	ψ_2 in radians
PSI20	ψ_2 in degrees for outputting
PSI2D	Derivative of PSI2
PSI3	ψ_3 in radians

PSI30	Ψ_3 in degrees for outputting
PSI3D	Derivative of PSI3
Q	Missile pitch rate in body axes in rad/sec
QD	Derivative of Q
QUE	Dynamic pressure $\frac{1}{2}\rho V^2$ in lbs/ft ²
R	Missile yaw rate in body axes in rad/sec
RD	Derivative of R
RHO	ρ in slugs/ft ³
RKM	Total moment amplification factor along missile Y axis
RKMB	Array of moment amplification factor vs α and δ_J
RKN	Total moment amplification factor along missile Z axis
RKNB	Array of moment amplification factor vs α and δ_J
RKY	Total force amplification factor along missile Y axis
RKYB	Array of forces amplification factor vs α and δ_J
RKZ	Total force amplification factor along missile Z axis
RKZB	Array of forces amplification factor vs α and δ_J
RMACH	Mach number of missile
RMASS	Instantaneous missile mass
RMASSO	Initial missile mass
RMASSD	Derivative of RMASS
S	Missile reference area = $\frac{\pi d^2}{4}$
SIGA	σ_A in degrees
SIGAD	Derivative of SIGA
SIGB	σ_B in degrees
SIGBD	Derivative of SIGB
SP	Dummy variable
SPE	Vector of sines of δ_E for each engine
SPH1L	$\sin(\delta_1)$
SPH1W	$\sin(\delta_w)$
T11	Elements of matrix transformation from body to inertial axes
⋮	
T33	
TBJRC	Burn time of JRC's
TBURN	Burn time of missile main thruster
THT	θ in degrees
THT4	θ_4 in radians

THR	Main thruster thrust
THT ⁴ O	θ_4 in degrees for outputting
THT ⁴ D	Derivative of THT ⁴
TJRC	Thrust of one JRC
TSJRC	Enable time for JRC's
U	U velocity of missile
UD	Derivative of U
UT	U_T
V	V velocity of missile
VD	Derivative of V
VEL	Total missile velocity
VEL1	Dummy variable
VEL2	Dummy variable
VSND	Velocity of sound
VT	V_T
W	W velocity of missile
WCZ	Ω of seeker cage along Z axis
WGY	Ω of seeker gyro along Y axis
WGZ	Ω of seeker gyro along Z axis
WINDXB	Components of wind along missile body axes
⋮	
WINDZB	
WINDXI	Components of wind along inertial axes
⋮	
WINDZI	
WT	W_T
X	Time
XCG	Position of missile C.G. relative to aerodynamic reference point
XCGO	Initial XCG
XCGD	Derivative of XCG
XF	Total force along X axis
XFA	Total aerodynamic force along X axis
XFB	Total aerodynamic force along X axis for baseline missile (no JRC)
XI	Inertial X position of missile
XID	Derivative of XI
XIMT	Inertial X position of target relative to missile
XJET	Position of JRC's from aerodynamic reference point

XM	Total moment along X axis
XMAX	Total run time
XMB	Total moment along X axis for baseline missile (no JRC)
XMT	X position of target relative to missile in body axes
XMTD	Derivative of XMT
XTO	Initial XTI
XTD	Derivative of XTI
XTI	Inertial X position of target
XXI	I_{XX}
XXIO	Initial XXI
XXID	Derivative of XXI
Y	Vector of slow integration state variables
YCAN	Deflection of yaw canard
YF	Total along Y axis
YFA	Total aerodynamic force along Y axis
YFB	Total aerodynamic force along Y axis for baseline missile (no JRC)
YFJ	Total force along Y axis due to JRC's
YI	Inertial Y position of missile
YID	Derivative of YI
YIMT	Inertial Y position of target relative to missile
YM	Total moment along Y axis
YMB	Total moment along Y axis for baseline missile (no JRC)
YMJ	Total moment along Y axis due to JRC's
YMT	Y position of target relative to missile in body axes
YMTD	Derivative of YMT
YTO	Initial YTI
YTD	Derivative of YTI
YTI	Inertial Y position of target
YYI	I_{YY}
YYIO	Initial YYI
YYID	Derivative of YYI
Z	Vector of fast integration state variables
ZF	Total along Z axis
ZFA	Total aerodynamic force along Z axis

ZFB Total aerodynamic force along Z axis for baseline missile (no JRC)
ZFJ Total force along Z axis due to JRC's
ZM Total moment along Z axis
ZMB Total moment along Z axis for baseline missile (no JRC)
ZMJ Total moment along Z axis due to JRC's
ZMT Z position of target relative to missile in body axes
ZMTD Derivative of ZMT

DISTRIBUTION LIST

	No. of Copies
1. Defense Documentation Center Cameron Station Alexandria, Virginia 22314	20
2. Library Naval Postgraduate School Monterey, California 93940	2
3. Dean of Research Naval Postgraduate School Monterey, California 93940	2
4. Chairman, Department of Aeronautics Naval Postgraduate School Monterey, California 93940	1
5. Dr. W. H. Clark Code 30102 Naval Weapons Center China Lake, California 93555	10
6. Assistant Professor Michael H. Redlin Department of Aeronautics Naval Postgraduate School Monterey, California 93940	5

DOCUMENT CONTROL DATA - R & D

Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified

ORIGINATING ACTIVITY (Corporate author) Naval Postgraduate School Monterey, California 93940	2a. REPORT SECURITY CLASSIFICATION UNCLASSIFIED
	2b. GROUP

REPORT TITLE Modems - A Point Defense Missile Simulation

DESCRIPTIVE NOTES (Type of report and, inclusive dates) Technical Report, March 1973

AUTHOR(S) (First name, middle initial, last name) Michael H. Redlin

REPORT DATE March, 1973	7a. TOTAL NO. OF PAGES 66	7b. NO OF REFS 4
----------------------------	------------------------------	---------------------

CONTRACT OR GRANT NO. PROJECT NO.	9a. ORIGINATOR'S REPORT NUMBER(S) NFS-57RP73031A
	9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report)

DISTRIBUTION STATEMENT Approved for Public Release; Distribution Unlimited

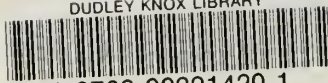
SUPPLEMENTARY NOTES	12. SPONSORING MILITARY ACTIVITY Naval Weapons Center China Lake, California 93555
---------------------	------------------------------------------------------------------------------------------

ABSTRACT A Point Defense Missile Simulation has been developed. This report describes the concept of such a missile, the basic features of the simulation program including the integration routine and the jet reaction controllers, and provides a FORTRAN coded source program.

14 KEY WORDS	LINK A		LINK B		LINK C	
	ROLE	WT	ROLE	WT	ROLE	WT
Point Defense Missile						
Missile Simulation						
Missile Guidance						
Advanced Seeker Simulation						



DUDLEY KNOX LIBRARY



3 2768 00391420 1