AN EXPERIMENTAL INVESTIGATION OF HYPERSONIC FLOW OVER BLUNT NOSED CONES AT A MACH NUMBER OF 5.8

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Thesis by

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ABSTRACT

Shock shapes were observed and static pressures were measured on spherically-blunted cones at a nominal Mach number of 5.8 over a range of Reynolds numbers per inch from 97,000 to 238,000 for angles of yaw from 0° to 8°. Six combinations of the bluntness ratios 0.4, 0.8, and 1.064 with the cone half angles 10°, 20°, and 40° were used in determining the significant parameters governing pressure distribution.

The pressure distribution on the spherical nose for both yawed and unyawed bodies is predicted quite accurately by the modified Newtonian theory given by $C_p = C_p \cos^2 \eta$, where η is the angle max between the normal to a surface element and the flow direction ahead of the bow shock. On the nose-cone junction and the conical afterbody, cone half angle was found to be the significant parameter in determining the length of the transition zone. For a cone half-angle of 40°, a pressure minimum exists on the skirt immediately downstream of the nose-cone junction, but this pressure minimum is located far downstream when the half-angle is 20°. The tangent cone concept at angles of yaw is useful in predicting the downstream movement of the pressure minimum. Shock cetachment distance between bow shock and body surface on the axis varies linearly with aoso radius. Drag coefficients for bodies at zero yaw compare very closely with those obtained by integrating the mocified Newtonian approximation, except at large half-angles and low blastnesses where drag approaches that given by the Taylor-Maccoll theory for sharp cones.



TABLE OF CONTENTS

PART	TITLE	PAGE
	Acknowledgments	
	Abstract	
	Table of Contents	
	Nomenclature	
I.	Introduction	1
II.	Equipment and Procedure	Q.
	A. Wind Tunnel	4
	B. Models	4
	C. Model Mounting	6
	D. Test Procedure	7
	1. Pressure Measurement	7
	2. Tests	8
III.	Results and Discussion	9
	A. Schlieren Observation	9
	B. Pressure Distribution	11
	C. Drag	18
IV.	Conclusions	19
	References	21
	Appendix	23
	List of Figures	30
	Figures	31



NOMENCLATURE

C	drag coefficient, dimensionless
C DF	foredrag pressure coefficient, dimensionless
C _p	pressure coefficient, $\frac{p - p_{\infty}}{\frac{1}{2} \rho_{\infty} U_{\infty}^2}$, dimensionless
Cpmax	pressure coefficient at the stagnation point, dimensionless
d	shock detachment distance, inches
1	unit vector in the n- direction, dimensionless
j	unit vector in the y- direction, dimensionless
in the second se	unit vector in the z- direction, dimensionless
a la	Mach number, dimensionless
n	unit vector normal to surface, dimensionless
Р	air pressure, 1b./sq. in.
q	dynamic pressure, 10./sq. in.
74 4	nose radius, inches
R	cone base radius, inches
2 e	Reynolds number, dimensionless
x/R	blantness ratio, dimensionless
61	distance measured on the surface from the intersection of model surface with its longitudinal axis, inches
S/r	non-dimensional orifice distance
U	steam velocity, ft./sec.
x, y, z	a right hand system of coordinate axes, fixed in the body
13	yaw angle
8	ratio of specific heats, dimensionless
∇	gradient

- η angle between free stream flow direction and the normal to the body surface
- 0 cone half angle
- ρ air density, lb. sec.²/ft.[±]
- σ polar angle of spherical nose
- φ meridian angle

Subscripts

() 7	static condition in front of bow shock wave
()	static condition behind bow shock wave
()	free stream conditions
(),	refers to stagnation, or reservoir condition
();	refers to nose-conc junction
<)p.m.	at minimum pressure point
() 3	static condition
() _{t1}	refers to total head in front of bow shock
().2	refers to total head behind bow shock

Superscripts

()' cone half angle of tangent cone

١.



I. INTRODUCTION

Current interest in hypersonic flow over blunt nosed bodies has been generated by the realization that the effects of high recovery temperatures on present day materials force the use of blunt nosed missiles, not only to reduce the heat transfer rates, but also to provide the nose volume required by internal conduction, and by cooling or guidance apparatus. In addition to these considerations is the heartening fact that for a fixed body length or body volume, the nose shape producing minimum pressure foredrag is blunt. Eggers, Resnikoff, and Dennis (Ref. 1) show, for example, that for equal fineness ratios the drag of the 3/4- power body is as much as 20 per cent less than that of the cone over a range of Mach numbers from 2.73 to 6.28. Sommer and Stark (Ref. 2) show that for equal fineness ratios the drag of spherically blunted cones is less than that for cones over a range of Mach numbers from 1.2 to 7.0. This condition was shown to exist for bluntness ratios up to 12 per cent.

At hypersonic speeds the component of flight Mach number normal to the surface of a blunt body is much larger than unity, and the inertia forces predominate over the elastic forces in the disturbed air. But this condition is precisely that postulated by Newton in his original treatment of fluid motion, as pointed out in Reference 1. In Newton's theory the fluid is regarded as a collection of discrete particles with no interaction between particles. It admits no shock wave and hence fluid particles are unperturbed before striking the surface of a body moving through them. As each particle strikes the surface, it



loses the component of its momentum normal to the body surface, while its tangential component is unchanged. The loss in normal momentum appears as an increase in pressure at the surface compared with the free stream pressure. The Newtonian pressure coefficient is

$$C_p = 2 \cos^2 \eta$$

where η is the angle between the free stream flow direction and the normal to the body surface. In the language of modern gas dynamics Newton's analysis applies strictly in the limiting case: $M \longrightarrow \infty$ and $V \longrightarrow 1$.

Newtonian theory predicts a pressure coefficient at the stagnation point, $C_{p_{max}}$, equal to 2, but in a real gas the how shock wave produces a finite volume compression and the rest of the deceleration to the stagnation point occurs isontropically. Therefore the actual value of $C_{p_{max}}$ is somewhat less than 2, being about 1.82 for $M_{p} = 5.8$ and $\gamma = 1.4$, and 1.66 at $M_{p} = 2$. As discussed by Lees (Ref. 3), Oliver (Ref. 4), and Penland (Lef. 5), the pressure distribution over a blunt body is predicted quite accurately if the Newtonian theor, is modified by introducing the normalized pressure distribution

$$c_p/c_{p_{max}} = \cos^2 \eta$$

This result agrees exactly with the recent stagnation point theories of Ting-Yi Li (Ref. 6) and Hayes (Ref. 7).

Now the Newtonian approximation also predicts quite closely the value of the pressure on the surface of a semi-infinite unyawed circular cone, provided λ_{c} state is sufficiently large. The object of the present investigation is to investigate experimentally the

surface pressure distribution and shock wave shape in the intermediate region extending from the stagnation-point zone on a blunt nose to the end of a conical afterbody. Oliver (kef. 4), in a recent study of a spherically-blunted 40° cone, observed an over-expansion below the final Taylor-Maccoll pressure value on the conical skirt, followed by a recompression to the proper asymptotic level. The present study seeks to determine what parameters are significant in determining the length of this transition zone, as well as other main features of the flow. It also extends the comparison with the Newtonian approximation and inviscid cone theories to the case of a yawed body.

Cix models in the form of truncated circular cones with tangentially connected spherical nose segments were used to obtain static pressure measurements at angles of yaw of 0°, 4°, and 3°. The parameters which were varied were cone half angle, $\theta_c = 40^\circ$, 20° , and 10°; and bluntness ratio, or ratio of nose radius to cone base radius, r/h = 0.4, 0.8, and 1.364.

The tests were conducted at a nominal Mach number of 5.8 in the GALCIT 5 x 5 inch hypersonic wind tunnel. The experimental results presented in this report were obtained jointly with LT R. M. Machell, U.S. Navy.



II. EQUIPMENT AND PROCEDURE

A. Wind Tunnel

The tests were conducted in the GALCIT 5 x 5 inch hypersonic wind tunnel (leg no. 1), which is of the continuous-flow, closed-return type and can be operated with supply pressures between 1 and 6.7 atmospheres absolute. The Mach number was nominally 5.8. All tests were made at a fixed reservoir temperature of 225°F, over a range of reservoir pressures from 37 to 95 lbs. per sq. in. absolute. This temperature was selected to yield maximum Reynolds numbers per inch while insuring the absence of air condensation in the test section. A schematic diagram of the wind tunnel installation is shown in Figure 1. The test section, with one side plate removed, and two methods of model mounting are shown in Figure 2. An extensive description of the experimental facilities is given in Reference 8.

B. Models

The six truncated circular cones with tangentially connected spherical nose segments shown in Figure 3 were used in the investigation. They were constructed of bra.s and each had a base diameter of 1.75 inches. The parameters which were varied were the bluntness ratio, defined as the ratio of the nose to the base radius, r/K, and the cone half angle. The bluntness ratios used were 0.4, 0.3, and 1.064. The cone half angles used were 10, 20, and 40 degrees. Variation in these parameters caused and 1 length to vary from .613 to 1.734 inches.



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A COLO SPECIMANEON						
Model Number	4	2.	3	4	5	E.
Cone Half Angle, C, (degrees)	40	40	23	20	20	10
Nose Hadius (inches)	0.35	0.70	0.35	J.70	0.931	0.70
Bluntness Latio, r/2.	0.4	0.3	0.4	0.8	1.064	0.8
Lodel Length (inches)	0.049	0.654	1.731	1.057	0.613	1.631
Number Frescure Orifices	16	13	13	· · · · · · · · · · · · · · · · · · ·	S	10
Note: Model number 5 var the limiting case where the spherical						
nose was the las	nose was the largest which could be inscribed within a 20 ⁰					
half-angle cone,	half-angle cone, and hence was merely a segment of a sphere.					

The models varias individually as follows:

Static pressure orifices on the front surfaces were .014 to .020 inches in diameter and the e small enough to insure a pressure variation across the orifice diameter of less than five per cent of the stagnation pressure. (See Appendix for a discussion of accuracy.) Figure 4 shows the method of construction of a typical model. The axial orifice intersected a shaft which was drilled from the after end of the model sting. This shaft was subsequently plugged so that pressure would be transmitted through the metal tube inserted in the side of the sting. The number of philices drilled in each obtained from eight to sizteen as shown in . igure, 5 to 7, which also give orifice locations. The orifices were located on from four to eight rays depending on the particular model shape.

.

C. Model Mounting

The models were mounted in the test section in the region of most uniform flow conditions as determined by previously conducted static pressure calibration surveys. Distance from the nozzle throat was 24 inches when models were mounted on an axially driven support rod as shown in Figure 2A. The support rod itself was in turn supported at its upstream end by a vertically actuated strut which was at least 4.5 inches downstream of the model base. This method of mounting was used to test five models at zero angle of yaw. For yaw tests the models were mounted on two vertically actuated struts 3.375 inches apart as shown in Figure 2B. Distance from the nozzle throat was 22 inches and the most forward strut was 3.5 inches downstream of the model base. This method of mounting was used to test a sixth model at zero angle of yaw and two others at angles of yaw of 4 and 6 degrees as well as at zero yaw.

Model stings were designed to conform to the size least likely to affect static pressure readings according to Reference 7. For some models one or two pressure tubes on the base were positioned outside the circle of radius 0.7%, but these tubes had a negligible effect on the results.

Each model carries a close fitting collar-and-shaft type sting such that a collar screwed to the base of the model fitted over a chaft screwed to the model support, thus permitting rotation of the model about its longitudinal axis. A set-screw in the collar permitted the model to be locked in any desired rotational position. (Figure 4)

Saran tubing, a flexible plastic material, was attached to the steel tubes at the base of the model and was led to the outside of the tunnel through "o-ring" scale in a side port of the test section. Connections were there made to either silicone or mercury manometers, depending on expected pressures. The system was thoroughly leakchecked.

D. Test Frocedure

1. Pressure Measurement

Reference 4 indicates the time required for temperature stabilization of model and test section is approximately $1\frac{1}{2}$ hours. Accordingly, the tunnel was operated for this length of time at the stagnation pressure desired for pressure measurement before readings were taken.

In order to minimize the effects of irregularities in flow direction occurring across the test section, the model was rotated upon its axis to three different positions 90 degrees apart during zero yaw tests, and pressures were read at each position. A similar procedure for minimizing flow irregularities was used in angle of yaw tests, except that a complete survey of prossures along each of the eight rays of the model was desired in addition. To accomplish both aims, the model was rotated to each of four positions 45 degrees apart, beginning with a ray in a vertical position. In each position the model nose was moved successively to angles of yaw of $\pm 2^{\circ}$, $\pm 4^{\circ}$, 0° , $\pm 4^{\circ}$, and $\pm 8^{\circ}$ in the vertical plane, and pressures were taken at each angle. The use of minus angle of yaw positions reduced by half the number of times the model had to be rotated.

2. Tests

All six models were tested at zero angle of yaw at a stagnation pressure of 75 lbs. per sq. in. absolute. In order to ascortain Reynolds number effects, models 1 and 4 were tested at zero angle of yaw at varying stagnation pressures. Angle of yaw tests were also performed using models 1 and 4. These models were selected because they were completely dissimilar in the two geometrical parameters varied in this investigation. A summary of test conditions follows:

	Test Conditions				
Model No.	Vertical Yaw Angle (degrees)	P _o (psia)	Niach No.	Re/in. x 10 ⁻⁵	
1	0 0 4 2	29999 9999 9999	30 00 00 00 10 00 00 00 10 00 00	1.91 2.38 2.38 2.38	
2	0	75	5.8	1.91	
3	0	75	5.8	1.91	
4	0 0 0 .1 3	19 19 19 19 19 19 19 19 19 19 19 19 19 1	7 7 8 8 8 8 8 5 5 5 5 5 5	0.97 1.41 1.71 2.38 2.38 2.38	
5	0	75	5.8	1.91	
6	0	75	5.8	1.91	
III. RESULTS AND DISCUSSION

A. Schlieren Observations

Tigures 8 through 13 are schlieren photographe of the six models at zero angle of yaw, at a nominal Mach number of 5.8. Figures 14 through 17 are photographs of models 1 and 4 at vertical angles of yaw of 4 and 8 degrees.

As in most hypersonic flows, the shock wave is fairly close to the body surface. The outstanding feature of the schlieren observations is the variation of shock shape with cone half-angle. Cone half-angles of 40° show a characteristic inflection point in the shock wave some distance downstream of the spherical nose portion of the model, but prior to the intersection with the first Mach wave from the model base.* (Figures 8 and 9) For small bluntness ratios the shock shape is dominated by the cone skirt, as shown in Figures 8 and 10. For large bluntness ratios, shock shape is dominated by the spherical nose as shown by Figure 9 and by Figures 11 through 13. These observations are true for any angle of yaw from 0° to 5° . However, angle of yaw produces some dictortion in the curvature of the shock waves.

The ratio of measured detachment distance, d, between bow shock and body surface on the axis of revolution of the model at zero yaw, to model nose radius, r, is shown in the following table:

* See discussion of pressure distribution, page 12.

Model No.	d(in.)	r(in.)	d/r
1 2 3 4 5 6	0.0594 0.1153 0.0592 0.1121 0.1496 0.1098	0.350 0.700 0.350 0.700 0.931 0.700	0.1695 0.1649 0.1692 0.1602 0.1607 0.1569
Average =			0.164

Thus, shock detachment varies nearly linearly with nose radius, as predicted theoretically. For instance, Ting-Yi Li (Ref. 6) predicts a value of c/r = 0.137 for $M_{co} = 5.8$ as given by

$$d/z = \frac{(1 - \rho_1/\rho_2)^2}{(1 - \rho_1/\rho_2)^2} - 1$$

$$\rho_1/\rho_2 (1 - \gamma_{1 - (1 - \rho_1/\rho_2)^2})$$

where ρ_1/ρ_2 is the ratio of the density before a strong shock to that behind it. Hayes (Ref. 7) predicts a value of d/r = 0.118 for $M_{_{(1)}} = 5.8$ as given by

$$d/r = \frac{p_1/p_2}{1 + \gamma 2 p_1/p_2}$$

Both theories assume that $\rho_1/\rho_2 < < 1$. Since $\rho_1/\rho_2 = 0.191$ for $M_{\infty} = 5.8$, and is not very small compared with unity, the agreement is considered to be good.

Heybey (Ref. 10) predicts a value of d/r = 0.140 for $M_{\odot} = 5.8$ which includes a correction for compressible flow behind the shock wave.



B. Surface Pressure Distribution

1. Unyawed Bodies

Surface pressure distributions for the six models at zero yaw are shown in Figures 18 through 23. Values of $C_p/C_{p_{max}}$ were obtained from observed data as explained in the Appendix. Both $C_p/C_{p_{max}}$ and the quantity $\cos^2 \eta$ appearing in the Lewtonian approximation are plotted vorsus the non-dimensional orifice distance, 2/r, where C is measured along the body surface from the intersection of the nose surface with the longitudinal axis. Taylor-Maccoll values of $C_p/C_{p_{max}}$ for a semi-infinite cone, as given by Kopal (Ref. 11), are also plotted over the conical portion of each model. In order to bring out the effect of bluntness ratio, r/C, with cone half angle held constant, the data of Figures 18 and 19 for $\theta_c = 40^\circ$ are replotted in Figure 24. Likewise the data of Figures 26 through 22 for $\theta_c = 20^\circ$ are replotted in Figure 25.

a. Spherical Nose

Close agreement between experimental pressures and Newtonian theory is evident on the opnerical nose of each model. In each case, however, the test data fall slightly below the theory in the region of most rapidly changing pressure. The deviation is usually only a few per cent, in some instances approaching a maximum of only 10 per cent. In the region approaching the junction between the spherical nose and conical afterbody come models show a marked deviation associated with local effects.



b. Nose-Cone Junction and Conical Lirt

Lumination of rigures de ana 25 shows that blunthese ratio itself has very little effect on the surface pressure distribution and that the half-angle of the conical shirt is the dominant geometric parameter. is pressure minimum downstream of the nose-cone junction is found on the 40° conical sairt, as in Miver's tests, but this minimum moves a considerable distance aft when the cone half angle is reduced to 20". This behavior a grees with qualitative predictions based on previous theoretical studies of blust boules at hypersonic species. For large cone half-angles the pressure on the spherical nose just apstream of the nose-cone junction should be given very closely by the modified Newtonian approximation, because $\lambda = \sin \theta_{\mu} >> 1$. For example, at $M_{p_1} = 5.6$ and $\delta = 1.4$, $C_{p_2} \approx 1.32 \sin^2 \theta_c$. But the Taylor-Maccoll value of the pressure on the coulcal shirt fat downstream is approximately 2.55 $\sin^2 \theta_e$ for $\Sigma_e \longrightarrow \infty$, * so that θ_p , should lie below this asymptotic value. Therefor a one would expect to find a pressure minimum on the skirt for large cone half-angles, followed by a recompression to the Taylor-1 accell value. This behavior should be accompanied by an inflection point in the bow shock wave as it adjusts itself to the Taylor-Maccoll conical shock angle far downstream. (Figure 2) Gince the drag/length of the skirt is high the pressure minintum occurs relatively close to the nose-cons junction.

the flow pattern, and the surface pressure is expected to approach the

* MOL, = L. the actual value is even if her.

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monotonically-decreasing pressure distribution typical of the limiting case of a hemisphere-cylinder ($\theta_c = 0$) for $\lambda_{-} > 3.50$ (air) as explained by Lees (lef. 12). That such behavior does eldst for helnisphere cylinders has been shown experimentally by many, see for example Oliver (Ref. 4). At M = 5.8 the pressures were shown to depart from Newtonian values on the spherical nose and consequently to be somewhat higher than Newtonian near the nose-cone junction. Figure 23 shows this behavior for $\theta_{1} = 10^{\circ}$. At the same time the skirt drag does not approach the nose drag until the skirt length is several nose diameters long. For both of these reasons the pressure minimum moves rapidly aft with decreasing 0 . A critical value of the halfangle exists below which the pressure minimum no longer occurs. In these tests this angle was approximately 20°. It should be pointed out that this critical angle decreases with decreasing Mach number below 5.8, and for M < 3.5 (air), over-expansion occurs even on the hemisphere-cylinder.

Neglecting viscous effects, one would not expect the nose-shirt junction to influence the pressure upstream unless the Mach wave from the junction strikes the sonic line. At the junction the normal pressure gradient is discontinuous, and the corresponding discontinuity in pressure gradient along the surface is given by

$$\Delta\left(\frac{2C_{p}/C_{p}}{2S/r}\right) = + \frac{\chi \chi^{2}}{\gamma_{M^{2}-1}} \left(\frac{C_{p}}{C_{p}} + \frac{2}{\chi_{M}}\right) = \frac{1}{\gamma_{M^{2}-1}} \left(\frac{1}{\gamma_{M^{2}}}\right)$$

For all the conditions of the present series of experiments d C_p/C_{Pmax} this discontinuity in

would reduce the negative surface pressure gradient, but would not reverse its sign. Now, examination of Figures 23 through 25 shows that the nose-cone junction influences the surface pressure upstream to an extent that cannot be explained by deviations from the Newtonian distribution. For example, the pressure coefficient at the junction is only 5 per cent above Newtonian for 40° cones, but is 37 per cent higher for 20° cones, and 146 per cent higher for 10° cones. The deviation can be explained, at least in part, by model surface irregularities which naturally occur at the nose-cone junction because of the difficulty in fabricating the desired 'jump" in radius of curvature. Any gradual fairing in of the spherical nose with the conical skirt will reduce the negative surface pressure gradient on the nose and consequently raise the entire level of the cowastream pressure distribution.

The data of Figures 18 and 21 and also Figures 24 and 25 do not show any significant Reynolds number effects over the range tested.

2. Yawed Bodies

Surface pressure distributions for models 1 and 4 at a yaw angle of 3° are shown in Figures 26 through 31. Both $C_p/C_{p_{max}}$ and the quantity $\cos^2 \eta$ are again plotted versus the non-dimensional orifice distance, S/r. The angle, η , in the yaw tests is no longer a simple function of body geometry, but is a function of angle of yaw as well. The angle was computed by the procedure gives in the Appendix. To give adequate representation of the three-dimensional aspects introduced by yawed bodies, procedure distribution is plotted along four meridian planes. These planes are orientated up follows: [1] one plane is vertical; (d) to planes, reference to an diagonal meridian plane, lie in position, defined on the three of ϕ , and are d^2 and 315^2

from the vertical meridian plane; (3) one plane is horizontal. Because of symmetry, the data obtained on the two diagonal planes have been averaged and plotted as for one plane. Likewise, the data obtained on the two halves of the horizontal plane have also been averaged and plotted for one half of the plane. Values of C_p/C_p for a yawed cone, as given by the Stone-Lopal first order theory (Ref. 13), are also plotted over the conical portion of each model.

a. Spherical Nose

Yaw data show the same close agreement with the modified Newtonian approximation on the spherical nose as in the zero yaw case. In the region of most rapidly changing pressures, the experimental results again show slightly lower pressures than the theory. It is of importance to note at this point that in the yawed tests, except for the vertical meridian plane, the pressures obtained at orifices along a particular geometric ray are not pressure along one streamline, but are pressures obtained on many different streamlines. Hence, the Inodified Newtonian law holds over the entire surface in any direction for a spherical nose.

b. Nose-Cone Junction and Conical Scirt

In order to bring out the effects of yaw, the data of Figures 26 through 29 are replotted in Figure 32. Examination shows the downstream movement of the minimum pressure point as half angle is decreased. Here it is convenient to utilize a concept somewhat analogous to the tangent cone approximation. The upper and lower conical rays in

the volunal meridial plane may be regarded at the various angles of yaw tested as balla (11) to two other comes at zero yaw whose half angles are given by the relations,

$$\theta'_c = \theta_c + (Lower half plane)$$

 $\theta'_c = \theta_c - (Uppor half plane)$

For the two models, then, four conec may be considered whose half angles are 13° , 30° , 32° , and 33° . It may be presumed that the 28° cone, represented in the lower half meridian plane of model 4, would have a diminium pressure point were its shirt to be sufficiently increased in length, since its pressures lie below the Stone-Kopal values on the cone. On the other hand the pressure distribution over the 13° tangent cone, being above the Stone-Kopal values, behaves very similarly to that given by the 13° cone of Figure 23. The yaw data confirming to that given by the 13° cone of Figure 23. The yaw data confirming is not infinite pressure point, lies between a half angle of 10° and 10° .

Further evidence of the downstream movement of the pressure $_{1}$ initial and θ_{c} is decreased to revealed by Figure 33 which shows data for the vertical meridian plane of model 1 at angles of yew of θ_{0}^{0} , 4^{0} , and θ_{0}^{0} . The tangent cones have values of $\theta_{c} = 32^{0}$, 36^{0} , 40^{0} , 44^{0} , and 4^{0} . The tangent cones have values of $\theta_{c} = 32^{0}$, 36^{0} , 40^{0} , 44^{0} , and 4^{0} . The tangent is the pressure minimum point downstream of the inter-down function is the pressure minimum point downstream of the inter-down function is the pressure at a scining or various cone half methods is concluded in the table following:



e or ec'	$(S/r)_{p.m.} - (S/r)_{j}$
48°	0.06
44°	0.09
40°	9.15
36°	0.25
32°	0.40
20°	2.28

Yaw tests show again that the nose-cone junction influences the surface pressure upstream to an unexplained but qualitatively predictable extent as half angle is varied. Per cent deviations of pressure coefficients from Newtonian values for actual and tangent cones as obtained from Figures 23 through 25 and from Figure 32 are summarized in the following table:

Model No.	e or e (degrees)	Deviation from Newtonian (per cent)
	10 12 20 23 32 40 48	146 133 37 17 10 5 10

When the cone skirt is sufficiently long the data show that the pressures approach the tangent cone values more closely than the values given by the stone-topal first-order theory. Also shown in Figure 33 is the fact that $\left(\frac{C\rho}{C_{P_{max}}}\right) - \left(\frac{C\rho}{C_{P_{max}}}\right)$ varies linearly over the range of yaw angles tested.

Variation of C_p/C_p with variation in meridian angle is shown in Figure 3. as replotted from Figures 26 through 23. .

C. Drag

By integrating the modified Newtonian approximation $C_p/C_p = \cos^2 \eta$ over the body surface, the following expression for drag coefficient at zero yaw is obtained for a spherically blunted

cone:

$$C_{\rm B} = C_{\rm P_{\rm max}} \left[\frac{1}{2} \cos^4 \theta_{\rm c} \left(\frac{r}{R} \right)^2 + \sin^2 \theta_{\rm c} \right]$$

In Figure 35 drag coefficients obtained by graphical integration of the experimental pressure distributions for the six models at zero yaw are compared with the theoretical value. The Taylor-Maccoll values for sharp cones are also shown.

Examination clearly shows the close agreement with the modified Newtonian approximation. However, at high half-angles and low bluntness ratios, the drag approaches that given by the Taylor-Maccoll theory.

IV. CONCLUSIONS

The results of this investigation provide the following conclusions regarding surface pressure distribution and shock wave shape for spherical nosed cones at a nominal Mach number of 5.8:

- (1) Static pressure distribution on the spherical nose agrees very closely with the modified Newtonian theory over the range of a from 0° to 8°, of 9 from 10° ro 40°, of r/R
 from 0.4 to 1.064, and of Reynolds number per inch from 97,000 to 238,900.
- (2) Under all conditions of the present investigation the half angle of the conical skirt is the dominant geometric parameter by which pressure distribution over the nosecone junction and the conical afterbody may be predicted, while bluntness ratio itself has very little effect.
- (3) There is a critical cone half angle, θ_c , above which there exists a pressure minimum on the conical skirt. This pressure minimum is far downstream for low θ_c and moves toward the nose cone junction as θ_c increases. The critical θ_c for $M_{\infty} = 5.3$ is about 20°, and the pressure minimum moves from a point 2.28 times the nose radius downstream of the nose-cone junction for $\theta_c = 20^\circ$ to a point only .06 times the nose radius downstream of the junction for $\theta_c = 48^\circ$.
- (4) At zero yaw the pressure on sufficiently long cone skirts approaches quite closely that given by the Taylor-Maccoll theory.

(5) At angles of yaw pressure distribution on sufficiently long cone skirts approaches quite closely that given by the Taylor-Maccoll theory as applied to tangent cones. The Stone-Kopal first order theory for yawed cones predicts the pressure behavior less accurately.

(6) $\binom{c_P}{c_{P_{max}}} - \binom{c_P}{c_{P_{max}}}$ varies linearly with variation in angle of yaw in the range from 0° to 8°.

- (7) There are no significant Reynolds number effects over the range of a, 9_c, r/R and R_e tested.
- (3) Bow shock detachment distance on the model longitudinal axis varies linearly with model nose radius. The ratio of detachment distance to nose radius is found to be 0.164 as compared with the predictions of Li, Hayes, and Heybey which are 0.137 0.118, and 0.140, respectively.
- (9) For 9_C sufficiently large, and hence for a minimum pressure point sufficiently near the nose cone junction, an inflection point in the bow shock wave occurs.
- (10) For low bluntness ratios shock shape is dominated by the conical afterbody, while for high bluntness ratios, shock shape is dominated by the spherical nose.

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APPENDIX

A. Computation of
$$C_p/C_p$$
 at Zero Yaw

Manometer values of static pressure were subtracted from manometer reference pressures to give static pressure at each orifice in cm Si or cm Hg. Since both silicone and mercury manometers were vacuum-referenced, the pressures were then corrected by the amount the vacuum differed from zero pressure absolute. Then all silicone pressures were converted to cm of mercury at existing room temperatures, giving static pressure p_s . The pressure at the stagnation orifice is assumed to be the total pressure behind the bow shock wave, p_{t_2} . To get free stream total pressure, p_{t_1} , the static pressure one inch upstream of the threat was converted from lbs. per sq. in. gage to cm of mercury and the barometric pressure was applied. The ratio p_{t_2}/p_{t_1} was used to enter Reference 14 to obtain M_{∞} and p_1/p_{t_1} . The latter value, when multiplied by p_{t_1} , gave p_1 , the free stream static pressure. Thus the ratio $C_p/C_{p_{max}}$ was obtained as follows:

$$C_{p} = \frac{\Delta p}{q_{00}} = \frac{P_{s} - P_{1}}{q_{00}}$$
$$P_{t_{0}} - P_{1}$$

$$C_{p_{max}} = \frac{r_2}{q_{ro}}$$

and

$$C_p / C_{p_{\text{max}}} = \frac{P_s - P_1}{P_{r_2} - P_1}$$



B. Computation of $C_p/C_{p_{max}}$ at Angles of Yaw

At angles of yaw, no orifice was located at the stagnation point from which p_{t_2} could be found. p_{t_2} was obtained by using the pressure at the nose orifice with the model at zero angle of yaw and assuming that this value remained unchanged at angle of yaw. Since the model could be quickly altered in angle of yaw without changing tunnel conditions, the assumption is a valid one.

C. Computation of $\cos^2 \eta$ at Zero Yaw

The angle, η , is defined as the angle between the free stream flow direction and the normal to the surface at any point in question. Enowing the location of each orifice permits the determination of η and hence $\cos^2 \eta$.

D. Computation of $\cos^2 \eta$ at Angles of Yaw

The angle, η , is a function of the angle of yaw as well as of a function of surface geometry. The spherical nose and the cone skirt are treated separately.

The equation of a sphere in rectangular coordinates where the origin of the axes is at the center of the sphere is given by:

$$f = x^2 + y^2 + z^2 - r^2 = 0$$

The unit vector normal to the sphere is defined as the quotient of the gradient of the surface and the absolute value of the gradient. Hence,

$$\overline{L} = \frac{\nabla f}{|\nabla f|}$$

where $\nabla f = I 2x + J 2y + K 2z$



and

$$|\nabla f| = 2(z^2 \cdot y^2 + z^2)^{\frac{1}{2}}$$

Therefore,



From the sketch the following quantities are defined:

- a = angle of yaw in the z- plane
- $\sigma = \text{polar angle measured from the x-axis}$

Any point on the surface is defined by the coordinates where

 $x = r \cos \sigma$ $y = r \sin \sigma \sin \phi$ $z = r \sin \sigma \cos \phi$

The angle of yaw in the z- plane is given by



Then $\cos \eta$ is defined as

$$\cos \eta = -\pi \circ \overline{a}$$

where $-\overline{n}$ is the inner unit normal at any point, P.

Hence,

 $\cos \eta = -\pi \circ \overline{c} = -\sin \alpha \sin \sigma \cos \phi + \cos \alpha \cos \sigma$

The equation of the cone is

$$f_1 = x^2 \tan \theta_c - y^2 - z^2 = 0$$

where θ_c is the cone balf angle.



From the sketch, any point, I, while for and is defined by the coordinates where

$$r = -\pi \tan \theta_{c}$$
$$y = r \sin \phi$$


$$z = r \cos \phi$$

 $y/x = -\sin \phi \tan \theta_c$
 $z/x = -\cos \phi \tan \theta_c$

From which

$$\overline{n} = \frac{\nabla f_1}{|\nabla f_1|} = \frac{2(1 \pm \tan^2 \theta_c - \bar{j}y - \bar{k}z)}{2(x^2 \tan^4 \theta_c + y^2 + z^2)^2}$$

$$n = \frac{1 \times \tan^2 \theta_c - \frac{1}{y} - \frac{1}{z}}{x \tan \theta_c \sec \theta_c}$$

$$n = I \sin \theta_c + J \cos \theta_c \sin \phi + K \cos \theta_c \cos \phi$$

Hence,

$$\cos \eta = -\pi \circ a = -\cos \theta_c \cos \phi \sin a + \sin \theta_c \cos c$$

where

at the junction of the spherical segment and the cone.

E. Accuracy Considerations

1. Measured Quantities

The following is a list of possible sources of error in the measured static pressure, p_s , and reservoir pressure, p_{t_1} :

- (1) Reading errors
- (2) Orifice diameter
- (3) Orifice location errors



- (4) Angle of yaw errord
- (5) Meridian angle errors

The maximum random manometer reading error was estimated to be $\frac{1}{2}$ 0.3 per cent of the stagnation pressure for a reservoir pressure of 80 lbs. per sq. in. gage. Orifice diameter was designed to give a maximum pressure variation from the mean of $\frac{1}{2}$ 2.5 per cent of the stagnation pressure. However, it is assumed that pressure transmitted to the manometer varied by a negligible amount from the mean pressure across the orifice. Deviations from designed orifice positions were such as to produce errors no larger than $\frac{1}{2}$ 0.5 per cent of stagnation pressure. Errors caused by angle of yaw and meridian angle setting errors were negligible.

a. Static pressure, p_S

Total error in p_s is given as follows:

Reading error	100	0.3	ber.	cent
Orifice size	+	0.0	per	cent
Variation in orlfice position	1	0.5	per	cent
Total error in ps	÷ 9	0.3	per	cent

b. Reservoir pressure, p_t

The maximum error in reading the correct value of reservoir pressure was [±] 0.5 per cent of stagnation pressure.

2. Computed Quantities

As the result of errors in measurements, the computed quantities had errors as follows:

$$p_{co} = \frac{1}{2} 0.03$$
 per cent of stagnation pressure
M_ = $\frac{1}{2} 0.01$

3. Plotted Quantities

As the result of the errors noted above, the plotted values of $C_p/C_{p_{max}}$ contained maximum errors as follows:

Region of Model	Model No.	Fraction of Cp/Cpmax
Nose to S/R 2 0.2	211	< + 0.01
S/r ≅ 0.2 to nose-cone junction	a 1,3	+ 0.012
s/r = 0.2 to nose-cone junction	n 2, 4, 5, 6	± 0.01
Cone skirt	a11	< = 0.01

LIST OF FIGURES

NUMB	ER TITLE	PAGE
	Schematic Diagram of GALCIT 5 x 5 Inch Hypersonic Wind Tunnel Installation	31
2	Test Section of Hypersonic Tunnel Showing Methods of Mounting Models	32
3	Spherical Nosed Cone Static Pressure Models	33
4.	Details of Typical Model Construction	34
5(A)	40° Half Angle Cone, $r/R = 0.4$	35
5(B)	40° Half Angle Cone, $r/R = 0.8$	35
6(A)	20° Half Angle Cone, $r/R = 0.4$	36
6(B)	20° Half Angle Cone, $r/R = 0.8$	36
7(A)	20° Spherical Segment, $r/R = 1.064$	37
7(B)	10° Half Angle Cone, $r/R = 0.8$	37
8-13	Schlieren Photographs, All Models, $c = 0^{\circ}$	38 - 40
14, 15	Schlieren Photographs, $\theta_c = 40^\circ$, r/R = 0.4, a = 4°, 8°	41
16, 17	Schlieren Photographs, $\theta_c = 20^\circ$, r/R = 0.8, $a = 4^\circ$, 8°	42
18-23	Surface Pressure Distribution, All Models, $a = 0^{\circ}$	43 - 48
22	Surface Pressure Distribution, $\theta_c = 40^\circ$, $c = 0^\circ$	49
25	Surface Pressure Distribution, $\theta_c = 20^\circ$, $\eta = 0^\circ$	50
26-23	Surface Pressure, $\theta_c = 40^\circ$, $r/R = 0.4$, $\alpha = 8^\circ$	51 - 53
29-31	Surface Pressure, $\theta_c = 20^\circ$, $r/R = 0.8$, $a = 8^\circ$	54 - 56
32	Surface Pressure, $\theta_c = 20^\circ$; 40° , $\alpha = 8^\circ$	57
33	Surface Pressure, $\theta_c = 40^\circ$, $a = 0^\circ$, 4° , 8°	58
34	Surface Pressure, Four Meridian Planes, $\theta_c = 40^{\circ}$, $\alpha = 8^{\circ}$	59
35	Drag Coefficient Versus 1/R with Parameter 9	60





(A)



(B)

FIG. 2

TEST SECTION OF HYPERSONIC TUNNEL

SHOWING METHODS OF MOUNTING MODELS



SPHERICAL NOSED CONE STATIC PRESSURE MODELS

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(B) 20° HALF ANGLE CONE r/R = 0.8















SCHLIEREN PHOTOGRAPH OF 40° HALF ANGLE CONE

r/R = 0.4, $a = 0^{\circ}$



FIG. 9

SCHLIEREN PHOTOGRAPH OF 40[°] HALF ANGLE CONE

r/R = 0.8, $a = 0^{\circ}$





FIG. 10

SCHLIEREN PHOTOGRAPH OF 20° HALF ANGLE CONE r/R = 0.4, $a = 0^{\circ}$



FIG. 11 SCHLIEREN PHOTOGRAPH OF 20° HALF ANGLE CONE r/R = 0.8, $a = 0^{\circ}$

39



FIG. 12

SCHLIEREN PHOTOGRAPH OF 20⁰ SPHERICAL SECTION

 $r/R = 1.064, a = 0^{\circ}$



FIG. 13

SCHLIEREN PHOTOGRAPH OF 10° HALF ANGLE CONE

r/R = 0.8, $a = 0^{\circ}$



SCHLIEREN PHOTOGRAPH OF 40° HALF ANGLE CONE

r/R = 0.4, $a = 4^{\circ}$



FIG. 15 SCHLIEREN PHOTOGRAPH OF 40[°] HALF ANGLE CONE r/R = 0.4, a = 8[°]







SCHLIEREN PHOTOGRAPH OF 20⁰ HALF ANGLE CONE

r/R = 0.8, $a = 4^{\circ}$



FIG. 17

SCHLIEREN PHOTOGRAPH OF 20⁰ HALF ANGLE CONE

r/R = 0.8, $a = 8^{\circ}$


































SURFACE PRESSURE, HORIZONTAL MERIDIAN PLANE, a = 8° FIG. 28



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C'Bryant

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