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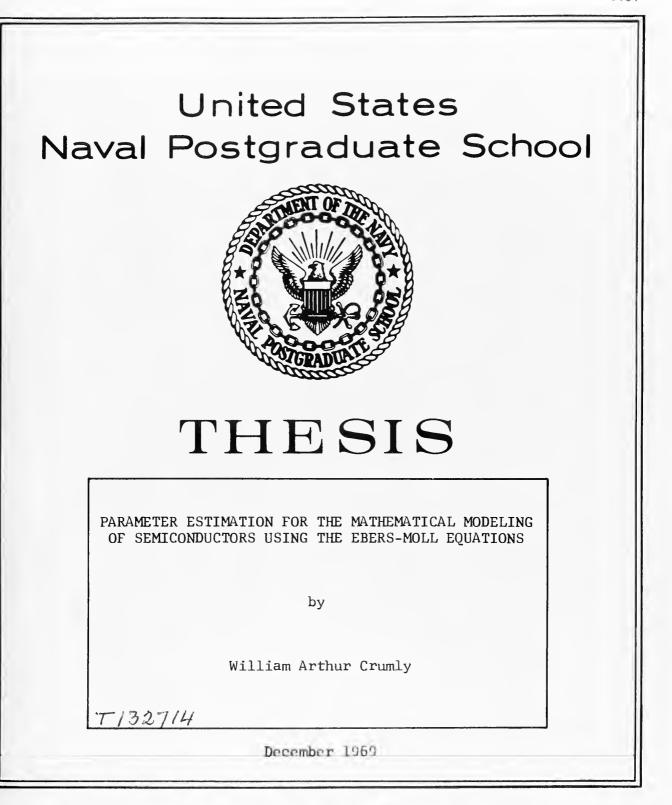
PARAMETER ESTIMATION FOR THE MATHEMATICAL MODELING OF SEMICONDUCTORS USING THE EBERS-MOLL EQUATIONS

by

William Arthur Crumly



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Parameter Estimation for the Mathematical Modeling of Semiconductors Using the Ebers-Moll Equations

by

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Submitted in partial fulfillment of the requirements for the degree of

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ABSTRACT

An accurate method of parameter estimation for the mathematical modeling of semiconductors using the Ebers-Moll equations is Its usefulness is apparent in estimating parameters presented. to be used in computer circuit-analysis programs that have been The Ebers-Moll models were modified to better developed. represent the actual characteristics. The least-square-error methods presented for estimating the parameters are easy to program to the digital computer and result in parameters that are quite accurate in describing the actual characteristics. This procedure yields solutions for parameters that are quite helpful to the engineer in solving electrical circuits involving p-n diodes and junction transistors.

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I. INTRODUCTION

In this age of computers, several excellent computer circuitanalysis programs have been developed which solve the equations describing electrical networks with remarkable accuracy. In order for the computed results to agree with actual circuit performance, the procedure of device modeling must furnish accurate models which are computationally efficient. As stated in a paper published by Design Automation, Inc. 1, "For all its advantages, the computer analysis of a circuit can be no better than the data that are fed into it. Poor models or improperly assigned values yield inaccurate results. In fact, once a circuit-analysis program is running on a computer and the designer has developed the skill to use it, the choice of semiconductor models and procedures for finding numerical values for the models' parameters are the main stumbling blocks to applying the program. The parameters of a real switching transistor or real diode vary as functions of voltage, current and temperature. Modeling is most accurate when the device characteristics are measured under conditions of voltage, current and junction temperature similar to those under which the device is expected to operate." After a model has been chosen, it is essential that the various parameters must be computed easily and accurately. With nonlinear devices, such as diodes and transistors, the model equations must give a mathematical description of the curve so that for a given voltage the current is known or vice versa. For this analysis, the

Ebers-Moll [2] models (modified slightly) for the diode and the transistor are usually employed. Using these models, methods are needed to determine the various parameters necessary for computation using any of the several computer circuit-analysis programs (TRAC, CIRCUS, NET I, NET II, and SCAN). These models cover both small-signal linear and large-signal nonlinear operation. The analysis in this thesis is limited to determining model parameters using steady-state characteristics.

In May, 1965, engineers at North American Aviation, Inc. completed analysis on the least-square-error curve fit for the semiconductor diode model parameters for the SCAN and TRAC computer circuit analysis programs. The modified Ebers-Moll model for the diode was presented and the necessary assumptions were included.

Design Automation, Inc., in June 1967, proposed a modeling procedure for transistors and diodes for computer-aided nonlinear circuit analysis [1]. The models presented were essentially the Ebers-Moll models with additions. The analysis by Design Automations, Inc. was developed for the NET I Network Analysis Program. Several improvements were made to the existing models.

In June 1968, the junction transistor model (modified Ebers-Moll model) was presented by E. Steele for the TRAC computer analysis program [3]. In March 1969 engineers at North American Rockwell Corporation presented, in an internal letter, a proposed method, using least-square estimation, of deriving the various parameters by analyzing the two junctions of the transistor separately.

In this thesis the problem of estimating the parameters of the Ebers-Moll models is considered. Questions investigated are: (1) determination of which regions of a semiconductor device are most useful for estimating each parameter of the model, (2) development of computer techniques of parameter estimation using least-square-error and normalized least square error solutions, and (3) estimation of the accuracy of the estimations. The ultimate question is whether the proposed models give an accurate representation of the actual performance of the semiconductor devices.

In Chapter II the modified Ebers-Moll models for the diode and the transistor are presented. These models allow accurate calculations to be made of the semiconductor device parameters necessary for the computer circuit-analysis programs.

In Chapter III the two methods of least-square-error solution are presented. One method is based upon the usual least-square-error solution and the other is based upon a normalized least-square-error solution as developed by Werther and Parker [4].

Procedures for calculating the semiconductor device parameters are presented for both the diode and the junction transistor. A discussion of the useful regions of parameter determination and the typical values expected from this analysis is included. A method of accumulating measured data and correcting estimated values accordingly in also discussed.

The parameters for typical diodes are calculated in the Appendix, using the two least-square-error methods. A comparison

of the results of these two methods is made and includes calculation of the error after the model parameters have been estimated.

The computer programs used for the solution of the model parameters are given following the Appendix. Recursive equations for both least-square-error methods are used. The FORTRAN IV programming language is used for the computer programs. Most of the subroutines were developed for this analysis, but several were existing subroutines in the Naval Postgraduate School Computer Facility subroutine library.

II. <u>EBERS-MOLL MODELS</u>

Ebers and Moll described the diode model and the junction transistor model, under DC conditions, using the small-signal parameters to relate to large-signal behavior [2]. These models described all regions of operation. Most of the other proposed models are mathematically equivalent and generally less accurate than the Ebers-Moll model [5]. Both the diode and the transistor models are considered below. The Ebers-Moll equations are modified by considering a term called the emission constant M for the diode and M_E and M_C for the transistor. Also linear resistances are added to account for the deviations from the ideal models. The Ebers-Moll models relate the semiconductor device characteristics in terms of several parameters, and generally provide very little insight to the actual physical processes within the devices represented by these models.

A. DIODE P-N JUNCTION MODEL

For an ideal p-n junction diode, the current and voltage have the following relationship

$$I = I_{s} \left[exp(W/kT) - 1 \right]$$
 (2.1)

where I_S is the reverse saturation current

V is the voltage across the terminals

q is the charge on an electron

k is the Boltzman constant

T is the absolute temperature (room temperature-298 $^{
m O}$ K)

kT/q equals 26mV at room temperature.

In practice very few p-n junctions can be described using the ideal diode relationship. In order to account for deviations between the theoretical and actual characteristics the ideal p-n junction diode needs to be modified by placing linear elements in parallel with or in series to the ideal diode. A large parallel resistance called the reverse diode leakage resistance is used to represent the slope of the reverse characteristics, and a small series resistance called the diode ohmic series resistance is used to represent part of the voltage drop across the p-n junction. Also, a modification to the Ebers-Moll model is the quantity M called the diode emission constant, with a value between 1 and 3, which changes the exponential dependence to more exactly describe the actual behavior, because of the non-ideal operation [3]. The modified ideal diode equation becomes

$$I = I_{s} \left[\exp\left(\frac{qV}{MkT}\right) - 1 \right].$$
 (2.2)

The DC diode circuit is given in Figure 1 using the above model. The various quantities included in Figure 1 are defined as

Vj, Ij - the measured diode terminal voltage and current R_s - the combined body, lead and contact resistance R_l - the reverse surface-leakage resistance across the junction D - the modified ideal diode

I - the ideal diode current given in equation 2.2. From the measured data of current and voltage, the parameters I_s , R_s , R_l and M are to be determined to describe a specific diode or p-n junction.

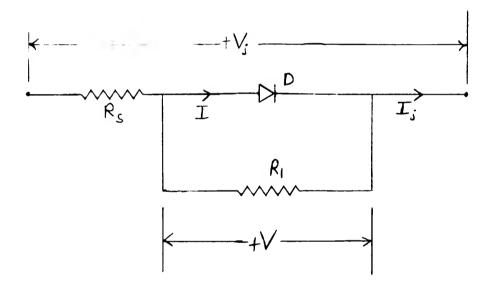
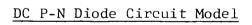


FIGURE 1



B. JUNCTION TRANSISTOR MODEL

For the ideal junction transistor, Ebers and Moll proposed the following current-voltage relationship assuming a pnp transistor [2].

$$\mathbf{I}_{E} = \frac{\mathbf{I}_{EO}}{1 - \boldsymbol{\alpha}_{N} \boldsymbol{\alpha}_{I}} \left[\exp\left(q \boldsymbol{V}_{E} / \boldsymbol{k} T\right) - 1 \right] - \frac{\boldsymbol{\alpha}_{I} \mathbf{I}_{CO}}{1 - \boldsymbol{\alpha}_{N} \boldsymbol{\alpha}_{I}} \left[\exp\left(q \boldsymbol{V}_{C} / \boldsymbol{k} T\right) - 1 \right] \quad (2.3)$$

$$\mathbf{I}_{C} = \frac{\boldsymbol{\alpha}_{N} \mathbf{I}_{EO}}{1 - \boldsymbol{\alpha}_{N} \boldsymbol{\alpha}_{I}} \left[\exp\left(q \mathbf{V}_{E} / \mathbf{k}_{T}\right) - 1 \right] + \frac{\mathbf{I}_{CO}}{1 - \boldsymbol{\alpha}_{N} \boldsymbol{\alpha}_{I}} \left[\exp\left(q \mathbf{V}_{C} / \mathbf{k}_{T}\right) - 1 \right]$$
(2.4)

$$\boldsymbol{\alpha}_{\mathrm{I}}^{\mathrm{I}}_{\mathrm{CO}} = \boldsymbol{\alpha}_{\mathrm{N}}^{\mathrm{I}}_{\mathrm{EO}} \tag{2.5}$$

where $I_F =$ the emitter current

- I_{C} = the collector current
- V_E = the emitter-to-base voltage
- V_{C} = the collector-to-base voltage
 - N = the common-base normal-mode DC current gain
 - I = the common-base inverted-mode DC current gain
- ${\rm I}_{\rm EO}$ = the saturation current of the emitter junction with zero collector current.
- I_{CO} = the saturation current of the collector junction with zero emitter current.

From this the following is true $\boxed{3}$

$$I_{ES} = I_{E0} / (1 - \boldsymbol{\alpha}_{N} \boldsymbol{\alpha}_{I})$$
 (2.6)

$$I_{\rm CS} = I_{\rm CO} / (1 - \alpha_{\rm N} \alpha_{\rm I})$$
(2.7)

where I_{ES} = the emitter-to-base p-n junction saturation current I_{CS} = the collector-to-base p-n junction saturation current.

In order to make the exponential dependence more exact, two quantities M_E and M_C are needed similar to the diode exponential emission constant. The quantity M_E is the emission constant for the emitter-base p-n junction and the quantity M_C is the emission constant for the collector-base p-n junction. The ideal transistor equations then become

$$I_{E} = I_{ES} \left[\exp\left(qV_{E}/M_{E}kT\right) - 1 \right] - \alpha_{I}I_{CS} \left[\exp\left(qV_{C}/M_{C}kT\right) - 1 \right]$$
(2.8)

and

$$I_{C} = I_{CS} \left[e \times p \left(q V_{C} / M_{C} k T \right) - 1 \right] - \alpha_{N} I_{ES} \left[e \times p \left(q V_{E} / M_{E} k T \right) - 1 \right].$$
(2.9)

Linear circuit elements are then added to modify the ideal transistor to an equivalent element to describe the actual relationship, similar to the diode formulation. The transistor equivalent circuit is presented in Figure 2 [1]. The elements of Figure 2 are defined below:

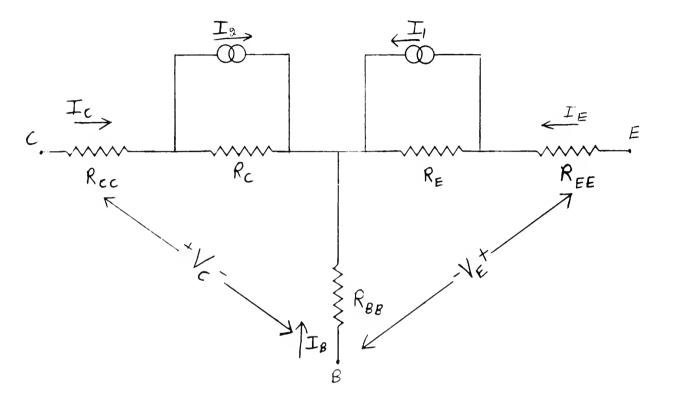
$$I_B = I_E + I_C$$
 the base current

$$I_{2} = \text{the current generator across the collector-base junction}$$
$$= I_{CS} \left[exp(qV_{C}/M_{C}kT) - 1 \right] - \alpha_{N}I_{ES} \left[exp(qV_{E}/M_{E}kT) - 1 \right]$$

 I_1 = the current generator across the emitter-base junction

=
$$I_{ES}\left[\exp\left(qV_{E}/M_{E}kT\right) - 1\right] - \mathcal{A}_{I}I_{CS}\left[\exp\left(qV_{C}/M_{C}kT\right) - 1\right]$$

 R_{BB} = the base spreading, bulk and contact resistance R_{EE} = the emitter bulk and contact resistance R_{CC} = the collector bulk and contact resistance R_E = the emitter-base junction ohmic leakage resistance R_C = the collector-base junction ohmic leakage resistance





DC Junction Transistor Circuit Model

The equivalent circuit for a pnp junction transistor may be used for a npn transistor by changing the polarities of V_C and V_E and the directions of I_1 and I_2 .

The specification sheets for transistors usually specify common-emitter DC current gains H_{FE_n} and H_{FE_i} rather than the common-base DC current gains $\boldsymbol{\prec}_N$ and $\boldsymbol{\boldsymbol{\prec}_I}$. The relationship between these $\boldsymbol{\boldsymbol{\checkmark}}$'s and H_{FE} 's are

$$\alpha_{\rm N} = {\rm H_{\rm FE}}_{\rm n} / ({\rm H_{\rm FE}}_{\rm n}^{+1})$$
 (2.10)

and

$$\alpha_{I} = H_{FE_{i}} / (H_{FE_{i}} + 1) .$$
 (2.11)

A simplified ideal model of the junction transistor is given in Figure 3, where I_1 and I_2 are replaced with diodes and dependent current sources. The resistances R_E and R_C are assumed to be very large and R_{BB} , R_{CC} , and R_{EE} are assumed to be small. For Figure 3 the elements are defined below

$$I_{EF} = I_{ES} \left[exp \left(q V_E / M_E k T \right) - 1 \right]$$
(2.12)

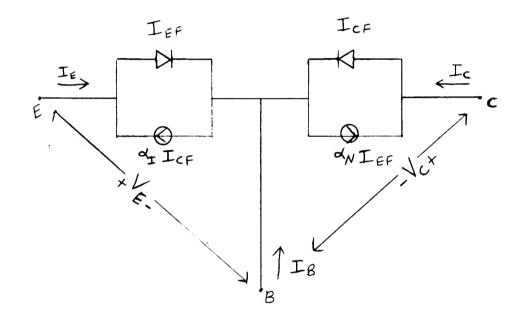
and

$$I_{CF} = I_{CS} \left[e_{xp} (qV_C / M_C kT) - 1 \right].$$
 (2.13)

From measured data, the parameters R_{CC} , R_{EE} , R_{BB} , M_E , M_C , I_{ES} , I_{CS} , H_{FE} , and H_{FE} are to be determined to describe a specific transistor.

The complete model including the AC components for the diode is given in Figure 4. The AC components added to the diode model are

C_t - the junction transition capacitance and





Simplified Transistor Model

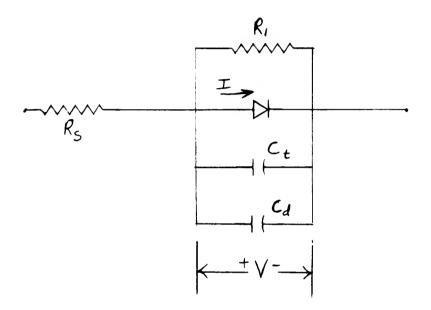


FIGURE 4

Complete Diode Model

 $\ensuremath{\mathtt{C}}_d$ - the junction diffusion capacitance.

In Figure 5 the AC components have been added to the transistor model so all operating conditions except the breakdown regions for the junctions can be accounted in the model. The added components are

 $\ensuremath{\mathtt{C}_{\mathsf{tE}}}\xspace$ - the emitter-base transition capacitance,

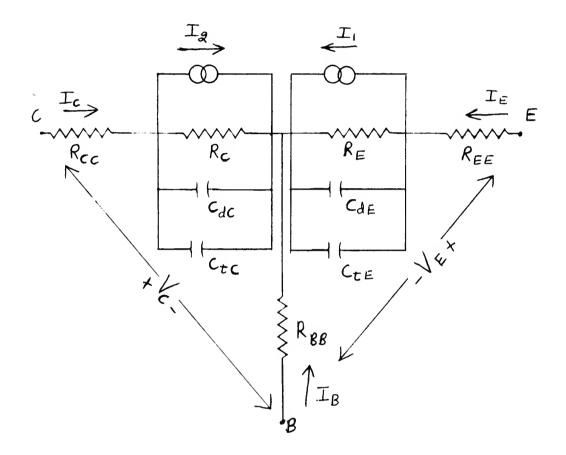
 C_{tC} - the collector-base transition capacitance,

C_{dE} - the emitter-base diffusion capacitance,

and

 $\ensuremath{\mathtt{C}_{\mathrm{dC}}}\xspace$ - the collector-base diffusion capacitance.

The transition capacitances are functions of the junction voltages and the diffusion capacitances are functions of the emitted currents from the emitter and from the collector [1].





Complete Transistor Model

III. LEAST-SQUARE-ERROR SOLUTIONS

The method chosen to compute the various parameters of the models presented is the least-square-error estimation. This solution is for a set of overdetermined simultaneous linear equations. There are two least-square-error methods presented. The first method is the usual least-square-error solution utilizing the concepts of the pseudo inverse as developed by Penrose [6] and presented by Werther [4]. The second method is the normalized least-square-error solution as developed by Werther and Parker [4]. A recursive equation is presented for each method to facilitate the use of additional data points in the calculation. These two methods and the estimations are compared with measurements to determine the usefulness of each method.

The material for the least-square-error estimation and the normalized least-square-error estimation was obtained from Werther 4.

A. LEAST-SQUARE-ERROR SOLUTION

The least-square-error solution is a very common method of solving a set of m simultaneous linear equations in n unknown, m being greater than n. This is the overdetermined case for linear equations which is common when measurements are made to find a small number of unknowns. The least-square-error solution

solves the relationship¹

$$A\underline{x} = \underline{b} \tag{3.1}$$

where A is the m by n matrix of coefficients,

 \underline{b} is the m by 1 vector of constants,

and

x is the n by 1 vector of unknowns.

A unique solution for \underline{x} is obtained by using the concept of the Penrose pseudo inverse. This yields the exact solution if it exists, or the least-square-error approximation if the exact solution does not exist. The Penrose pseudo inverse is a n by n matrix and is identified as A^+ . The least-square-error solution is

$$\widehat{\underline{\mathbf{x}}} = \mathbf{A}^{+}\underline{\mathbf{b}}.$$
 (3.2)

If the matrix A has rank n the least-square-error solution is

$$\underline{\hat{x}} = \left[\underline{A}^{T}\underline{A}\right]^{-1}\underline{A}^{T}\underline{b}$$
(3.3)

where A^{T} is the matrix transpose of the matrix A and $[A^{T}A]^{-1}$ is the matrix inverse of the product of A^{T} and A. In order for the rank of A to be n, the rows of A must be independent. This solution is easily obtained on the digital computer with available matrix operation subroutines.

For the recursive relationship, the least-square-error solution for the first k points is

$$\mathbf{\hat{x}}_{k} = P_{k} A_{k}^{T} \underline{z}_{k}$$
(3.4)

where \underline{z}_k is equal to \underline{b}_k which is the vector of k points,

¹The bar under a lower-case letter represents a column matrix or vector.

 A_k is the k by n coefficient matrix,

$$P_k$$
 is the inverse of the matrix $A_k A_k$,

and

\dot{x}_k is the least-square-error solution.

Now to consider the k+l equation, \underline{a}^{T} is a row of new coefficients to the A matrix and \underline{z}_{k+1} is the new data for the vector \underline{b}_{k+1} . Therefore

$$A_{k+1} = \begin{bmatrix} A_k \\ -\frac{a}{a} \end{bmatrix}$$
(3.5)

ጥ

and

$$\underline{b}_{k+1} = \begin{bmatrix} \underline{z}_k \\ - - - \\ \underline{z}_{k+1} \end{bmatrix}, \qquad (3.6)$$

The k+l least-square-error solution is

$$\hat{x}_{k+1} = P_{k+1} A_{k+1} T_{\underline{z}_{k+1}}$$
(3.7)

where P_{k+1} is the inverse of the matrix $\begin{bmatrix} A_{k+1}^T A_{k+1} \end{bmatrix}$. The resultant recursive equations are

$$\bigwedge_{\underline{X}_{k+1}} = \bigwedge_{\underline{X}_{k}} + \frac{P_{k\underline{a}}}{1 + \underline{a}^{T}P_{k\underline{a}}} (\underline{z}_{k+1} - \underline{a}^{T}\underline{X}_{k})$$
(3.8)

and

$$P_{k+1} = P_k - \frac{P_{ka} \underline{a}^T P_k}{1 + \underline{a}^T P_{ka}}$$
 (3.9)

B. NORMALIZED LEAST-SQUARE-ERROR SOLUTION

The normalized least-square-error solution is a weighted least-square-error solution with weighting factors chosen such that the solution lies as close as possible to all geometric loci described by equation 3.1.

The matrix of weighting or normalizing factors is a diagonal m by m matrix called W. The factors w_{ij} are given by

$$w_{ii} = \left(\sum_{j=1}^{n} a_{ij}^{2}\right)^{-\frac{1}{2}}, i=1,2,\dots,m$$
(3.10)

This weighting matrix is multiplied times the matrix A and vector <u>b</u> resulting in two new quantities

$$A^* = WA \tag{3.11}$$

and

$$\underline{\mathbf{b}}^* = \mathbf{W}\underline{\mathbf{b}}.\tag{3.12}$$

The normalized least-square-error solution is then

$$\underbrace{\mathbf{A}}_{\mathbf{X}}^{*} = \left[\underline{\mathbf{A}}_{\mathbf{X}}^{*} \mathbf{T}_{\mathbf{A}}^{*} \right]^{-1} \underline{\mathbf{A}}_{\mathbf{X}}^{*} \underline{\mathbf{b}}_{\mathbf{X}}^{*}.$$
 (3.13)

The recursive relationships for the normalized least-squareerror solution are

$$\overset{\wedge}{\underline{x}}_{k} = \overset{\wedge}{\underline{x}}_{k+1} + \frac{P_{k}^{*} \underline{a}^{*}}{1 + a^{*}P_{k}^{*} \underline{a}^{*}} (\underline{z}^{*}_{k+1} - \underline{a}^{*}\underline{x}^{*}_{k})$$
(3.14)

and

$$P_{k+1}^{*} = P_{k}^{*} - \frac{P_{k}^{*} \underline{a}^{*} \underline{a}^{*} P_{k}^{*}}{1 + \underline{a}^{*} P_{k}^{*} \underline{a}^{*}}$$
(3.15)

Using the fact that

$$\underline{z}^{*}_{k+1} = (\underline{a}^{T}\underline{a})^{-\frac{1}{2}}\underline{z}_{k+1}$$
(3.16)

and

$$\underline{\mathbf{a}}^* = (\underline{\mathbf{a}}^{\mathrm{T}}\underline{\mathbf{a}})^{-\frac{1}{2}}\underline{\mathbf{a}}$$
(3.17)

the recursive relationships become

$$\underline{\hat{x}}_{k+1} = \underline{\hat{x}}_{k+1} + \frac{\underline{P}_{k}^{\star} \underline{a}}{\underline{a}^{T} \underline{a} + \underline{a}^{T} \underline{P}_{k}^{\star} \underline{a}} (\underline{z}_{k+1} - \underline{a}^{T} \underline{x}_{k}^{\star})$$
(3.18)

and

$$P_{k+1}^{*} = P_{k}^{*} - \frac{P_{k}^{*} \underline{a} \underline{a}^{T} P_{k}^{*}}{1 + \underline{a}^{T} P_{k}^{*} \underline{a}}$$
(3.19)

The recursive relationships for both the least-square-error solution and the normalized least-square-error solution are easily adapted to the digital computer and a sample computer program for each method is found after the Appendix.

IV. DETERMINATION OF SEMICONDUCTOR PARAMETERS

Using the models presented in Chapter II, the model parameters are calculated utilizing the least-square-error method. Parameter calculation is accomplished using the above equations and the equivalent circuits. In order to use the least-square-error methods, the nonlinear equations characteristic of these semiconductor devices must be converted to a set of linear equations, which involves several assumptions. The solution is made on the nonlinear equations where these equations can be assumed to be linear. The error associated with these assumptions is so small it is considered negligible.

These parameters enable the user to employ these models in existing computer circuit-analysis programs and obtain computed results that very accurately represent the actual performance. The data for parameter estimation may be obtained using the measured current and voltage values or values taken from device specification sheets. When specification sheets are used, the values of the voltage should be read to several millivolts in order to obtain accurate results.

Since the data involves experimental error and is statistical in nature, as many data points as possible should be used in the estimation of the semiconductor parameters. Since the measurements are independent, in general, the rank of the matrix A in equation 3.1 is equal to n, the number of parameters. Since the overdetermined case must have the matrix A with a rank of at least n, the solution presented in Chapter III may be used.

A. LINEAR EQUATION FOR DIODE PARAMETER ESTIMATION

The model for the semiconductor diode is presented in Figure 1. In order to determine the values of the parameters, the model equation has to be simplified and made linear to be compatible with the least-square-error methods. Using Figure 1, the following can be stated:

$$I_{1} = I + V/R_{1},$$
 (4.1)

or

$$I_{j} = I_{s} \left[exp(qV/MkT) - 1 \right] + V/R_{1}.$$
 (4.2)

The first restriction is that V_j (the measured terminal voltage) be positive $(V_j > 0)$. With this restriction, exp(qV/MkT) >> 1 because even with small positive measured voltages (for example 0.1 volt) and with q/MkT = 0.025, the term exp(qV/MkT)=54.99. This is much greater than 1. Since R1 is so very large compared to V, I \gg V/R₁, and equation 4.2 is simplified to

$$I_{j} = I_{s} \exp(qV/MkT)$$
(4.3)

which by rearranging becomes

$$V = MkT/q \ln(I_{i}/I_{s}). \qquad (4.4)$$

Referring back to the model

$$V_{j} = V + I_{j}R_{s}, \qquad (4.5)$$

and substituting 4.4 into 4.5 results in

$$V_j = MkT/q \ln(I_j/I_s) + I_jR_s.$$
 (4.6)

This equation is simplified by letting $A_0 = MkT/q$ and $A_1 = 1/I_s$, obtaining

$$V_{j} = A_{0} \ln(A_{1}I_{j}) + I_{j}R_{s}$$

$$(4.7)$$

$$V_{j} = A_{0} \ln(A_{1}) + A_{0} \ln(I_{j}) + I_{j}R_{s}$$
 (4.8)

$$V_{j} = A_{3} + A_{0} \ln(I_{j}) + I_{j}R_{s}, \qquad (4.9)$$

where $A_3 = A_0 \ln(A_1)$. This approach is currently used by North American Rockwell Corp., among others.

In the above equation, V_j and I_j are the measured forwardvoltage and current data points for the diode. The other three quantities are constants to be determined using the least-squareerror procedure. For the least-square-error method

$$A = \begin{bmatrix} 1 & \ln(I_{1}) & I_{1} \\ \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots \\ 1 & \ln(I_{m}) & I_{m} \end{bmatrix}$$
(4.10)
$$\underline{b} = \begin{bmatrix} V_{1} \\ \vdots \\ V_{m} \end{bmatrix}$$
(4.11)

and

where $\hat{\underline{X}}$ is the least-square-error solution. After A₃, A₀ and R_s are determined, the parameters of primary interest are calculated using the following relationships:

$$M = A_0 q / kT, \qquad (4.13)$$

$$A_1 = \exp(A_3/A_0),$$
 (4.14)

and

$$I_{s} = 1/A_{1}.$$
 (4.15)

The three parameters M, I_s and R_s are then calculated and can be used in the circuit-analysis computer programs.

For determination of R1, (the reverse diode leakage resistance due to the imperfections, surface effects, and thermally generated carriers in the depletion region) the same equation is used as the one for the determination of the other diode parameters. For this case, data points are used from the reverse characteristics of the diode; thus V_j and I_j are both negative. The basic equation is 4.2. By making an assumption that $exp(qV/MkT) \ll 1$ for V less than -0.2 volts,² equation 4.2 is reduced to

$$I_{j} = -I_{s} + V/R_{l}.$$
 (4.16)

Solving for V,

$$V = (I_{j} + I_{s})R_{l}$$
(4.17)

and substituting this into equation 4.5 results in

$$V_{j} = (I_{j} + I_{s})R_{l} + I_{j}R_{s}.$$
(4.18)

Rearranging,

$$V_{j} = I_{j}(R_{1} + R_{s}) + I_{s}R_{1}.$$
 (4.19)

 $^{^{2}}$ With V = -0.2 volts and MkT/q = 0.026, exp(qV/MkT) = 4.5x10⁻⁵ and most measured data is less than -0.2 volts.

Setting $(R_1 + R_s) = A_5$ and $I_s R_1 = A_6$ results in

$$V_{i} = I_{i}A_{5} + A_{6}.$$
(4.20)

This is solved using the least-square-error procedures with

$$A = \begin{bmatrix} I_{1} & I_{1} & I_{1} & I_{2} & I_{2}$$

In the above procedure V_j and I_j are the measured voltage and current in the reverse direction of the diode. From the results, R_1 is determined after an assumption is made. From the assumption that $R_1 \gg R_s$, R_1 is then equal to A5 since A5 = $R_1 + R_s$ and R_s is so small it can be neglected. A value of reverse saturation current, I_s , may be found from this data but this value is not a good value for this current, especially for silicon diodes. For a 1N540 diode, the reverse saturation current is determined from the reverse characteristics along with R_1 . The value obtained is then placedas a constant into the equation used to derive the forward parameters. The other two parameters are derived to see if this reverse saturation current resulted in parameters in the useable range. It is found that the value of R_s is -1.46 ohms and the value of M is 3.67. These values are not realistic numbers to be used in computer circuit-analysis programs. These values are determined in the Appendix. The reverse characteristics of silicon diodes tend to be more difficult to model, since the ideal diode law breaks down completely as a description for the reverse silicon-diode behavior [7]. In most p-n junctions the reverse current is not completely voltageindependent, due to the surface leakage. R_1 is the only reliable parameter derived from the reverse data.

Several regions of the forward characteristics were investigated to discover where the best parameter estimations can be The standard deviation was computed to determine the found. closeness of fit to the measured points of the various regions. The closeness of fit is an indication of the error involved. The least standard deviation was found to be when the data was utilized along as much of the forward curve as possible. A comparison using the standard deviation from data received in different regions along the curve reveals this fact. Using the points corresponding to the large values of the measured voltage, or far out on the curve, the standard deviation is three times greater than the standard deviation found using the complete The deviation found from the data of small values of curve. voltage, or closest to the origin, is also much larger than the least standard deviation. These calculations are included in the Appendix using the 1N540 diode.

The reverse saturation current determined from the forward characteristics was used to help find R_1 from the reverse characteristics by setting I_s a constant in the derivation. This

method reveals that this value of I_s has very little effect on the value of R_1 obtained. A simplified equation for determining R_1 can be made,

$$R_{l} = V_{j} / (I_{j} - I_{s}),$$
 (4.24)

where V_i and I_i are measurements from the reverse characteristics.

The parameters for two diodes, 1N540 and 1N277 are calculated in the Appendix. The standard deviation for each diode using the parameters determined is also given. The standard deviation was found using the measured voltage V_j and the calculated voltage VC_j from the measured current I_j . Equation 4.9 is solved placing the estimations of the parameters in the equation for the constants and using the various values of measured current. The value obtained is called VC_j . The standard deviation is found by the following relationship

standard deviation =
$$\sqrt{\frac{j = 1}{j = 1}} (VC_j - V_j)^2$$
 (4.25)

where N is the total number of data points used. This value of the standard deviation is used as an error indicator. The method with the largest standard deviation has the largest error using the same data points. For the two diodes used, it was found that the least-square-error method had a smaller standard deviation than the normalized least-square-error method, for both diodes. The difference is quite small and is not a good indicator of which method is best. From using these programs, it appears that the normalized least-square-error method has an

advantage in calculations when the measurements are at relatively great distances from the actual desired curve. Either method estimates parameters that give a curve that has less deviation than that expected due to variations from diode to diode due to manufacturing procedures and techniques.

B. DETERMINATION OF PARAMETERS FOR JUNCTION TRANSISTORS

The model for the junction transistor was presented in Figure 2. The parameters to be determined are I_{ES} , I_{CS} , M_E , M_C , R_{BB} , R_{CC} , R_{EE} , R_E and R_C . In this analysis, the emitter-base and the collector-base junctions are considered to be two separate diodes for these calculations. For the emitter-base p-n junction parameters, measured data are made with the collector terminal open circuited and for the collector-base p-n junction parameters, measured data are made with the emitter terminal open circuited.

Considering the emitter-base junction as a diode, calculations are made on the forward measured data to determine the quantities IES, ME, and RSE, the same as I_S, M and R_S were determined for the discrete diode above. The quantity R_{SE} is the combined emitterbase body, lead and contact resistance. The emitter reverse leakage resistance (R_E) is determined using the reverse characteristics, the same as for the diode.

For the collector-base junction considered as a diode, calculations are made on the forward characteristics to determine the quantities I_{CS} , M_C , and R_{SC} , the same as was computed for the diode. The quantity R_{SC} is the combined collector-base body,

lead and contact resistance. The collector reverse leakage resistance (R_{C}) is determined using the reverse characteristics, the same as for the diode.

To complete the model parameters for the junction transistor an assumption is made that the emitter bulk resistance is zero. The quantity R_{EE} is the emitter bulk resistance. Using this assumption, R_{BB} is calculated from

$$R_{BB} = (H_{FE_n} + 1)R_{SE}$$
 (4.26)

The collector bulk resistance is determined to be

$$R_{CC} = R_{SC} - R_{BB} / (H_{FE_{i}} + 1)$$
 (4.27)

The quantities H_{FE_n} and H_{FE_i} are the common-emitter DC normal and inverted current gains respectively.

The shift of H_{FE_n} can be evaluated from the specification sheets available on the individual transistors. Specification sheets normally give curves of H_{FE_n} versus I_C . An average value is obtained by taking n values of H_{FE_n} from the curve at equally spaced values of collector current over the range and then dividing by n. This average value of H_{FE_n} can then be used in further calculations of parameters. The parameter H_{FE_1} can be measured directly or assumed to be values as shown in Table I.

The common-base $\boldsymbol{\swarrow}$'s can be calculated using equations 2.10 and 2.11.

This procedure of determining the model parameters for the junction transistor are currently used by North American Rockwell Corp., among others.

TABLE I

Typical Values of H_{FE_1} (Reprinted from the Motorola Switching Transistor Handbook.)

Transistor Type	Typical H _{FEi}
Planar, silicon epitaxial	0.2
Alloy, uniform base	ц
Alloy, diffused base	1
Mesa, diffused base	0.4

C. TYPICAL VALUES FOR MODEL PARAMETERS

For the p-n junction diode the values of M, R_s and I_s are usually determined to be in the following ranges. The value of M is between 1.0 and 3.0. the value of R_s is between 10^{-5} and 10^{-1} kilohms, the value of I_s silicon is from 10^{-12} to 10^{-6} mA and for germanium is from 10^{-8} to 10^{-2} mA. The quantity R_1 has a value between one and ten megohms.

The junction transistor parameters are usually contained in the following ranges: The value of M_E and M_C is between 1.0 and 3.0, the value of R_{EE} and R_{CC} is between 10^{-5} and 10^{-2} kilohms, and R_{BB} is usually between 10^{-4} and 10^{-1} kilohms. R_{EE} has been assumed to be zero in this analysis. The usual range of I_{ES} is 10^{-14} to $10^{-6}mA$ for silicon and 10^{-8} to $10^{-2}mA$ for germanium. The value of I_{CS} is usually an order of magnitude larger than I_{ES} . The quantities R_C and R_E are usually larger than one megohm.

These are only typical values, but if a parameter is substantially outside the usual range, the input data and calculations should be checked for error. These values were presented by Design Automation, Inc. [1].

The parameter values for the two diodes calculated in the Appendix conform to the typical values for the model as is shown in Table II.

In Table III a comparison of the values calculated using the least-square-error methods to the values calculated following the procedures given by Design Automation, Inc. [1]. There is very little difference in the parameter values derived by either method. The standard deviation for the least-square-error methods

TABLE II

Calculated Parameters and Standard Deviations

	<u>1N540</u>		<u>lna</u>	277
	Usual	Normalized	Usual	Normalized
М	1.75	1.76	1.07	1.10
Is	1.65x10 ⁻¹⁰	1.86x10 ⁻¹⁰	2.65x10 ⁻¹⁰	3.72x10 ⁻¹⁰
R _s	0.13	0.126	82.83	67.9
SD	0.006	0.0062	0.0025	0.0027

TABLE III

A Comparison of Parameters Derived Using Two Methods

	Design Automation	Least Square	Normalized Least Square
М	1.75	1.75	1.76
I_s	1.5×10 ⁻¹⁰	1.65x10 ⁻¹⁰	1.86x10 ⁻¹⁰
R _s	0.132	0.131	0.126
SD	0.0076	0.006	0.0062

is a little less than that for the method of Design Automation, Inc. This indicates that the least-square-error methods are as well suited to these models as other procedures.

D. COLLECTION OF DATA POINTS

The measured values of current and voltage used in the A matrix and the b vector for the least-square-error methods need to be evenly distributed from the minimum value of voltage (at least 0.1 volt) to a value of voltage that corresponds to maximum If these values are too close together or on only one power. portion of the curve, the derived parameters turn out to be negative values or values that do not correspond to the usual range. Most of this type of error is due to the inaccuracy of the measurements of the voltage and current. A typical derivation is presented in the Appendix. After the parameters have been initially estimated, the additional points are utilized in the recursive relationships. The additional points may be taken anywhere between the minimum and the maximum values of voltage. The least standard deviation is found utilizing as much of the forward characteristics as possible.

For the reverse characteristics, fewer points are needed and they may be spread more than the forward characteristics. The reverse leakage resitance is a large value and if equation 4.24 is used only one set of points is needed in the calculation. This calculation need not be too accurate since the reverse leakage resitance is of little importance. Values of current and voltage between -0.2 volts and the breakdown voltage are acceptable.

V. CONCLUSION

1 . 2.

A good model has been chosen since it has been shown that these models accurately represent electrical performance of the device over a very wide range and the models are computationally efficient in regards to the computer circuit-analysis programs presently in use. It is found that the error by this method is considerably less than the variation in the characteristics due to manufacturing techniques. The region chosen to measure the data for the parameters for the forward characteristics is represented as the points lying between 0.1 volts and the maximum power rating of the device. The measured data best represents the device when the points cover as much of the curve between the above mentioned points as possible. Considering the two methods of parameter approximation, both methods give results that are well within the accuracy expected. The normalized least-squareerror solution does more to eliminate the influence of points located farthest from the desired curve.

The standard deviation, which is a measure of the error in parameter estimation, reflects that these models give an accurate representation of the actual performance of the semiconductor devices. The standard deviation from the least-square-error methods is a few millivolts and most measurements could be this inaccurate. As seen on the forward characteristics presented in Figures 6, 7 and 8, the difference between the actual measurements and computed values is almost indistinguishable.

Parameters were not estimated for a transistor, but the method of determining these parameters is straight-forward and should not present any serious difficulty. Semiconductor devices with more p-n junctions than the transistor can be modeled similarly by dealing with each junction separately as a diode.

A comparison of values of parameters from the least-square estimates with other methods of parameter estimation reveals that the least-square-error methods produce parameter values essentially the same as other procedures. The error for the least-squareerror methods is slightly less than other procedures.

APPENDIX

Examples of Parameter Estimation

This section is used to give two examples of the use of the procedures presented in this thesis. Two diodes, one the 1N540 and the other the 1N277, were used in this analysis as the two examples. Measured data of current and voltage were taken in the forward and reverse portions of the two devices to be used to determine the device parameters.

The following is the forward data collected for the two devices with the voltage given in volts and the current in milliamperes.

1N540

1N277

<u>Voltage</u>	Current	<u>Voltage</u>	Current
0.4 0.48 0.5 0.52 0.54 0.56 0.58 0.6 0.64 0.68 0.72	0.002 0.006 0.0092 0.014 0.021 0.033 0.0555 0.086 0.215 0.483 1.15	Voltage 0.25 0.27 0.28 0.285 0.29 0.3 0.31 0.32 0.34 0.36 0.38	Current 0.002 0.004 0.006 0.008 0.01 0.014 0.02 0.025 0.049 0.085 0.14
0.76 0.8	3.18 9.15	0.4 0.42	0.222 - 0.37
0.84 0.88	15.5 37.8		
0.92 0.96 1.0	76.0 155.0 270.0		

The reverse data for the devices are presented with both the current and the voltage as negative quantities and the current is in milliamperes and the voltage in volts.

1	N	5	4	0

1115110

1N277

1 NO 77

Voltage	Current	Voltage	Current
9.0 11.2 13.0 15.5 19.5 22.5	0.01 0.012 0.014 0.016 0.20 0.24	2.65 5.8 10.0 11.5 20.0 30.0	0.004 0.008 0.0125 0.014 0.024 0.0355
26.5	0.0265	36.0	0.0425

Using seven selected points, an A matrix is assembled to start the recursive operation with the forward characteristics. These seven selected points are spaced over as much of the curve as possible so as to take into consideration the influence of different parameters on various regions of the curve. Errors are sometimes encountered when two points are used that lie too close to each other.

The seven points chosen for the A matrix and <u>b</u> vector are

<u>1N340</u>			
Voltage	Current	Voltage	Current
0.58 0.6 0.68 0.72 0.88 0.96	0.0555 0.086 0.483 1.15 37.8 155.0	0.25 0.27 0.285 0.3 0.34 0.38	0.002 0.004 0.008 0.014 0.049 0.14
1.0	270.0	0.42	0.37

where the voltage is in volts and the current is in milliamperes. The natural logarithms of the currents were determined and the information was then run on the computer programs to start the recursive procedures. The solution of the parameters using only the first seven points for the lN540 are as follows for the least-square-error methods described above.

	Least Square	Normalized Least Square
A ₃ A ₀	1.0249 0,0453	1.0233 0.0451
Rs	0.1268	0.1324
A	6.656x10 ⁹	7.1373x10 ⁹
I	1.502x10-10	1.4019x10-10
I _s M	1.743	1.734

The solutions for the points for 1N277 are

	Least Square	Normalized Least Square
A3	0.6097	0.6162
A0	0.0275	0.0281
Rs	78.2493	71.3765
Al	4.1626x10 ⁹	3.3997×10^{9}
I _S M	2.4023x10 ⁻¹⁰	2.941×10-10
М	1.0587	1.0798

The rest of the measured points are used in the recursive equations and result in the final forward parameters as

1N540

	Least Square	Normalized Least Square
A3	1.0246	1.0261
Ao	0.0455	0.0458
Rs	0.1308	0.1257
Al	6.0536×10^{9}	5.3908×10^{9}
Is	1.6519×10^{-10}	1.855×10^{-10}
М	1.7495	1.7611

1N277

	Least Square	Normalized Least Square
A3 A0	0.6116 0.0277	0.6236 0.0287
Rs	82.8309	67.8968
Al Is	3.7768×10 ⁹ 2.6477×10 ⁻¹⁰	2.6885x10 ⁹ 3.7195x10-10
М	1.0666	1.1047

The seven points from the reverse characteristics were only evaluated using the normalized least-square-error method since the only parameter attained from the reverse characteristics is the reverse leakage resistance R_1 . The value of R_1 is of little importance and any value in the megohm range will be adequate. The calculated values of R_1 are

$$\frac{1N540}{R_1} = \frac{1N277}{8.69 \times 10^5}$$

Values of these parameters were calculated with the procedures of Design Automation, Inc., [1] using the data as listed above. The following values were obtained.

1N540

М	1.75
Rs	0.132
I_S	1.5×10^{-10}

It is evident that these values are quite similar to those of the least-square-error methods.

The standard deviation using equation 4.25 was calculated for the three sets of parameters calculated by the above methods. Each standard deviation calculated is listed below.

1 . . .

Standard Deviations

 \mathbb{N}_{0}^{2}

1N540

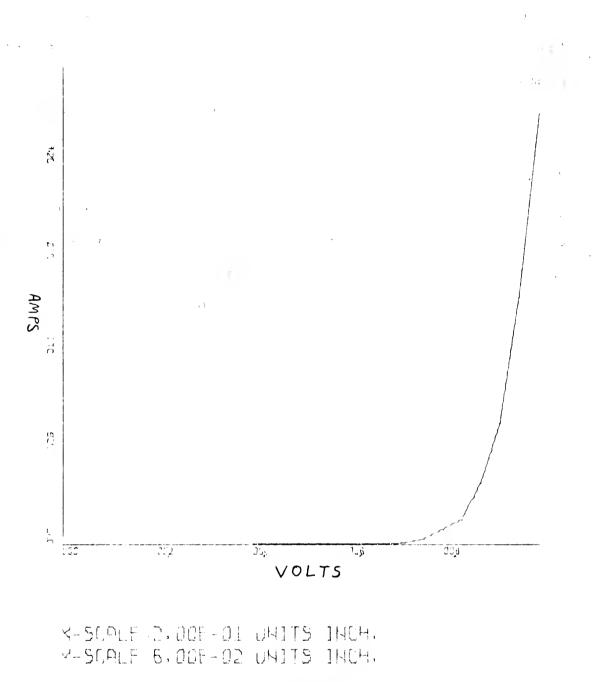
Design Automation	Least Square	Normalized Least Square
20.0076	0.006	0.0062
	1N277	
	0.0025	0.0027

In checking the various regions of the curve to be used the standard deviation was calculated for the parameters derived from data far out on the curve. The parameters calculated were M equals 1.872, I_S equals 5.686×10^{-10} and R_S equals 0.101. The

standard deviation for these parameters is 0.0184. This indicates that the best parameters are derived from data covering as much of the curve as possible.

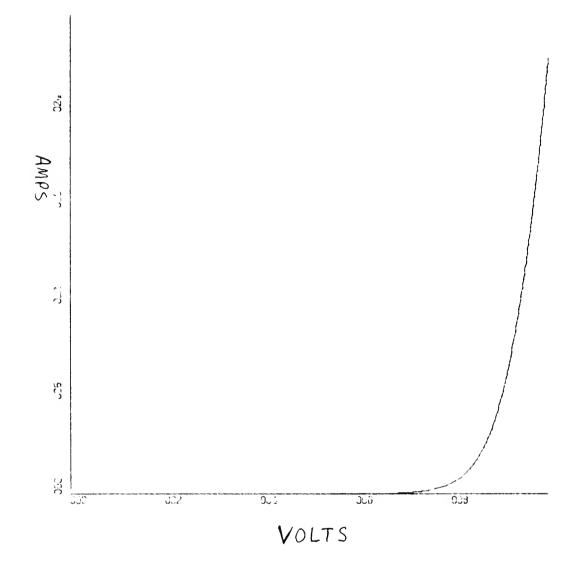
The standard deviation is a measure of the error between the calculated and the actual measurements. It is seen that the deviation is usually only a few milliamperes.

Figures 6, 7, 8, 9, 10 and 11 are plots of the forward characteristics from the measured data and also of the calculated parameters for diodes. From these curves it is clear that the solution obtained by the least-square-error methods is very accurate.





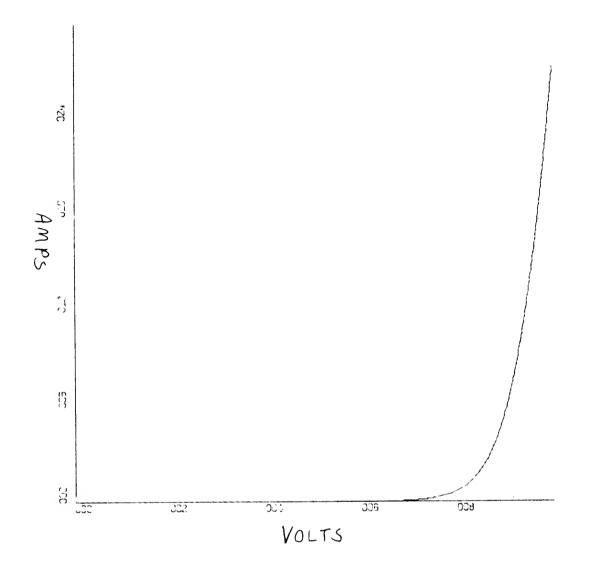
Plot of Measured Points for the 1N540 Diode



X-SCALE=2.00E-01 UNITS INCH. Y-SCALE=6.00E-02 UNITS INCH.

FIGURE 7

Plot of Calculated Points Using the Least-Square Parameters for the 1N540 Diode

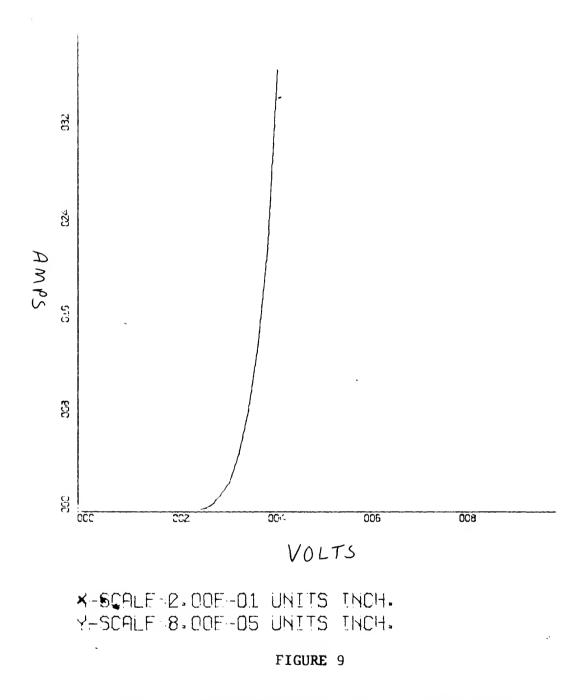


X-SCALF=2.00E-01 UNITS INCH. M-SCALF=5.00E-02 UNITS INCH.

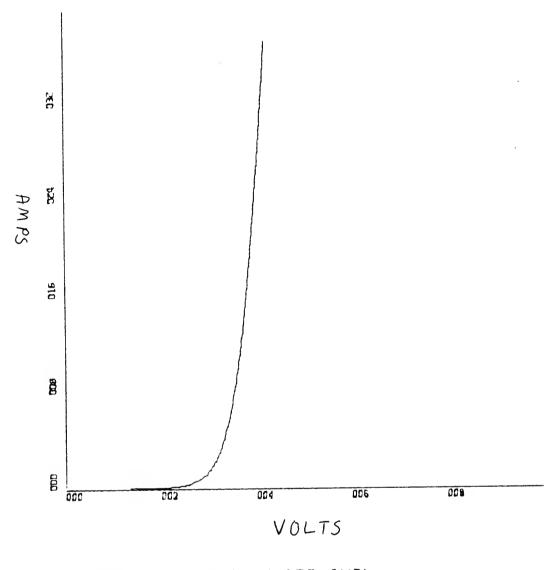
· · · · ·

FIGURE 8

Plot of Calculated Points Using the Normalized Least-Square Parameters for the 1N540 Diode



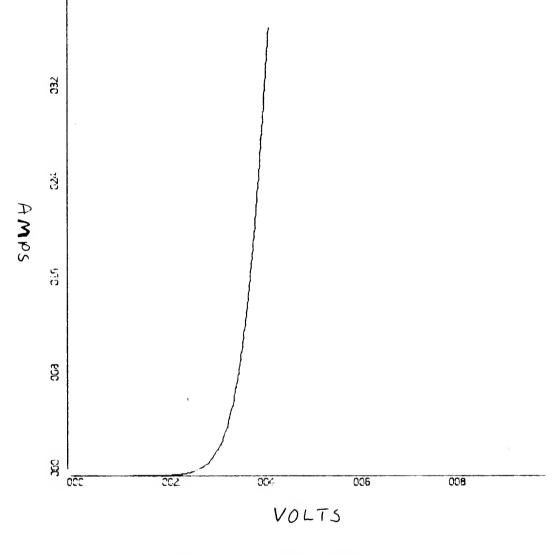
Plot of the Measured Points for the 1N277 Diode



K-SCALE=2.00E-01 UNITS INCH. Y-SCALE=8.00E-05 UNITS INCH.

FIGURE 10

Plot of Calculated Points Using the Least-Square Parameters for the 1N277 Diode



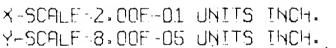


FIGURE 11

Plot of the Calculated Points Using the Normalized Least-Square Parameters for the 1N277 Diode

COMPUTER PROGRAMS

```
С
   THIS IS THE MAIN PROGRAM FOR THE NORMALIZED LEAST SQUARE
С
   ERROR SOLUTION.
С
   A IS THE M BY N INPUT MATRIX OF COEFFICIENTS.
   B IS THE M BY 1 INPUT VECTOR OF CONSTANTS.
С
С
   RS, SI, AND ETA ARE THE OUTPUT PARAMETERS WHERE RS
   IS BODY RESISTANCE, SI IS THE REVERSE SATURATION CURRENT
С
С
   AND ETA IS THE VALUE FOR THE EMISSION CONSTANT M.
       IMPLICIT REAL*8 (A-H, 0-Z)
       DIMENSION A(10, 10), B(10, 10), C(10, 10), D(10, 10)
       DIMENSION W(10,10), T(10), A2(10,10), E(10,10)
       DIMENSION A3(10,10), F(10,10), G(10,10), H(10)
       READ(5, 4) M,N
       READ (5,5) ((A (I,J), I=1,M), J=1, N)
       READ(5,5) (B(I,1), I=1, M)
     4 FORMAT(2110)
     5 FORMAT(7F10.0)
       DATA T/10*0.0/
       DO 118 I=1,M
       DO 118 J=1.N
       T(I) = T(I) + A(I, J) **2
   118 CONTINUE
       DO 122 I=1.M
       W(I,I) = 1.0 / DSQRT(T(I))
   122 CONTINUE
       DO 114 I=1,M
       B(I,1) = B(I,1) * W(I,I)
       DO 114 J=1,N
       A(I,J) = A(I,J) * W(I,I)
   114 CONTINUE
       DO 2-3 I=1,M
       DO 23 J=1,N
       A2(J,I) = A(I,J)
    23 CONTINUE
       CALL MATMUL (A2, N, M, A, M, N, C, M4, N4, L)
       CALL GAUSS3 (N, EPS, C, A3, KER, 10)
       IF (KER.EQ.2) GO TO 10
       CALL MATMUL (A3, M4, N4, A2, N, M, D, M5, N5, L2)
       CALL MATMUL(D, M5, N5, B, M, 1, G, M8, N8, L3)
       PRINT 8, (G(I,1), I=1, N)
     8 FORMAT(10X, 3D14.6)
       DO 303 J=1,10
       READ(5,30) (H(I), I=1, N)
       READ(5,32) Z
    30 FORMAT(3F10.0)
    32 FORMAT(1F10.0)
       CALL WRLSF (A3, H, G, Z, N)
       PRINT 8, (G(I, 1), I=1, N)
       A4=G(1,1)
```

```
A0=G(2,1)
       RS=G(3,1)
       Al=DEXP(A4/A0)
       PRINT 33, A4, A0, RS, Al
    33 FORMAT(10X, 4D14.6)
       SI=1.0/A1
       ETA=A0*38.46
        PRINT 8, SI, ETA
   303 CONTINUE
        GO TO 300
    10 \text{ WRITE}(6, 12)
    12 FORMAT(10X,8HSINGULAR)
   300 STOP
       END
С
   THIS IS THE MAIN PROGRAM FOR THE LEAST SQUARE ERROR
С
   SOLUTION.
С
   A IS THE M BY N INPUT MATRIX OF COEFFICIENTS.
С
   B IS THE M BY 1 INPUT VECTOR OF CONSTANTS.
С
   RS, SI, AND ETA ARE THE OUTPUT PARAMETERS WHERE RS
С
   IS BODY RESISTANCE, SI IS THE REVERSE SATURATION CURRENT
C
   AND ETA IS THE VALUE FOR THE EMISSION CONSTANT M.
        IMPLICIT REAL*8 (A-H,O-Z)
        DIMENSION A(10, 10), B(10, 10), C(10, 10), D(10, 10)
        DIMENSION A2(10,10), A3(10,10), G(10,10), H(10)
        READ(5, 4) M,N
        READ (5,5) ((A(I,J),I=1,M),J=1,N)
       READ(5,5) (B(I,1), I=1, M)
     4 FORMAT(2110)
     5 FORMAT(7F10.0)
       DO 23 I=1,M
        DO 23 J=1,N
       A2(J,I) = A(I,J)
    23 CONTINUE
        CALL MATMUL (A2, N, M, A, M, N, C, M4, N4, L)
        CALL GAUSS3 (N, EPS, C, A3, KER, 10)
        IF (KER.EQ.2) GO TO 10
        CALL MATMUL (A3, M4, N4, A2, N, M, D, M5, N5, L2)
        CALL MATMUL (D, M5, N5, B, M, 1, G, M8, N8, L3)
        PRINT 8, (G(I,1), I=1, N)
     8 FORMAT(10X, 3D14.6)
        DO 303 J=1,10
       READ(5,30) (H(I),I=1,N)
READ(5,32) Z
    30 FORMAT(3F10.0)
    32 FORMAT(1F10.0)
        CALL TRLSF (A3, H, G, Z, N)
        PRINT 8, (G(I,1), I=1, N)
        A4=G(1,1)
        A0=G(2,1)
        RS=G(3,1)
        A1=DEXP(A4/A0)
```

```
57
```

```
PRINT 33, A4,A0,RS,A1
33 FORMAT(10X,4D14.6)
SI=1.0/A1
ETA=A0*38.46
PRINT 8, SI,ETA
303 CONTINUE
GO TO 300
10 WRITE(6,12)
12 FORMAT(10X,8HSINGULAR)
```

```
300 STOP
END
```

```
SUBROUTINE WRLSF (A3, H, G, Z, M)
    IMPLICIT REAL*8 (A-H, 0-Z)
    DIMENSION A3(10,1), H(1), Q(10), V2(10), G(10,1)
    DIMENSION Q2(10, 10), Q3(10, 10), G1(10)
    CALL MATVEC (A3, M, M, H, Q)
    CALL VECMUL(H,H,M,S)
    CALL VECMUL(H, Q, M, V)
    V1=S+V
    DO 122 I=1,M
122 V2(I) = Q(I) / V1
    DO 132 I-1,M
    Gl(I) = G(I, 1)
132 CONTINUE
    CALL VECMUL(H,G1,M,Z2)
    Z3=Z-Z2
    DO 124 I=1,M
124 V2(I) = V2(I) * Z3
    DO 126 I=1,M
126 Gl(I) = Gl(I) + V2(I)
    DO 134 I=1.M
    G(I, 1) = G1(I)
134 CONTINUE
    CALL MULVEC (M, Q, H, Q2)
    CALL MATMUL(Q2, M, M, A3, M, M, Q3, M, M, L9)
    04=1.0D0+V
    DO 128 I=1,M
    DO 128 J=1,M
128 \ Q2(I,J) = Q3(I,J) / 04
    DO 130 I=1,M
    DO 130 J=1,M
    A3(I,J) = A3(I,J) - Q2(I,J)
130 CONTINUE
    RETURN
    END
```

```
SUBROUTINE TRLSF (A3, H, G, Z, M)
    IMPLICIT REAL*8 (A-H, Ó-Z)
    DIMENSION A3(10,1),H(1), Q(10), V2(10), G(10,1)
    DIMENSION Q2(10, 10), Q3(10, 10), G1(10)
    CALL MATVEC (A3, M, M, H, Q)
    CALL VECMUL(H, Q, M, V)
    V1=1.0+V
    DO 122 I=1,M
122 V2(I) = Q(I) / V1
    DO 132 I=1,M
    G1(I) = G(I, 1)
132 CONTINUE
    CALL VECMUL(H,G1,M,Z2)
    Z3=Z-Z2
    DO 124 I=1,M
124 V2(I) = V2(I) * Z3
    DO 126 I=1,M
126 Gl(I) = Gl(I) + V2(I)
    DO 134 I=1.M
    G(I, 1) = G1(I)
134 CONTINUE
    CALL MULVEC(M,Q,H,Q2)
    CALL MATMUL (Q2, M, M, A3, M, M, Q3, M, M, L9)
    DO 128 I=1,M
    DO 128 J=1,M
128 Q2(I,J)=Q3(I,J)/V1
    DO 130 I=1,M
    DO 130 J-1,M
    A3(I,J) = A3(I,J) - Q2(I,J)
130 CONTINUE
    RETURN
    END
    SUBROUTINE VECMUL(X,Y,M,SUM)
    IMPLICIT REAL*8 (A-H, 0-Z)
    DIMENSION X(1), Y(1)
```

```
SUM = SUM-SUM
DO 5 I=1,M
```

```
SUM=SUM+X(I)*Y(I)
5 CONTINUE
```

```
RETURN
END
```

```
SUBROUTINE MULVEC (M, X, Y, XY)
   IMPLICIT REAL*8 (A-H, 0-Z)
   DIMENSION X(1), Y(1), XY(10,1)
   DO 6 I=1,M
   DO 5 J=1,M
 5 XY(I,J) = X(I) * Y(J)
 6 CONTINUE
   RETURN
   END
   SUBROUTINE MATVEC(A,M,N,V,P)
   IMPLICIT REAL*8 (A-H, 0-Z)
   DIMENSION A(10,1), V(1), P(1)
   DO 6 I=1,M
   P(I) = P(I) - P(I)
   DO 6 J=1,N
   P(I) = P(I) + A(I, J) * V(J)
 6 CONTINUE
   RETURN
   END
   SUBROUTINE MATMUL (A, MA, NA, B, MB, NB, C, MC, NC, L)
   IMPLICIT REAL8* (A-H, 0-Z)
   DIMENSION A (10, 1), B(10, 1), C(10, 1)
   L=0
   IF (NA.NE.MB) RETURN
   L=1
   MC=MA
   NC=NB
   DO 12 J=1,NC
   DO 12 I=1,MC
   C(I,J) = 0.0
   DO 12 K=1,NA
12 C(I,J) = C(I,J) + A(I,K) * B(K,J)
   RETURN
   END
```

The other subroutine GAUSS3 is a subroutine in the Naval Postgraduate School Computer Facility subroutine library for calculating the inverse of a matrix if such an inverse exists.

These programs are not the most computationally efficient but are adequate for this calculation. There are several improvements that can be made to these programs expecially in regard to storage required.

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