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A roadblock-and-kill mechanism of action model for the DNA-targeting antibiotic ciprofloxacin

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Abstract

Fluoroquinolones - antibiotics that cause DNA damage by inhibiting DNA topoisomerases - are clinically important, but their mechanism of action is not yet fully understood. In particular, the dynamical response of bacterial cells to fluoroquinolone exposure has hardly been investigated, although the SOS response, triggered by DNA damage, is often thought to play a key role. Here we investigate growth inhibition of the bacterium *Escherichia coli* by the fluoroquinolone ciprofloxacin at low concentrations. We measure the long-term and short-term dynamical response of the growth rate and DNA production rate to ciprofloxacin, at both population- and single-cell level. We show that despite the molecular complexity of DNA metabolism, a simple `roadblock-and-kill' model focusing on replication fork blockage and DNA damage by ciprofloxacin-poisoned DNA topoisomerase II (gyrase) quantitatively reproduces long-term growth rates in the presence of ciprofloxacin. The model also predicts dynamical changes in DNA production rate in wild type *E. coli* and in a recombination deficient mutant, following a step-up of ciprofloxacin. Our work highlights that bacterial cells show a delayed growth rate response following fluoroquinolone exposure. Most importantly, our model explains why the response is delayed: it takes many doubling times to fragment the DNA sufficiently to inhibit gene expression. We also show that the dynamical response is controlled by the timescale of DNA replication and gyrase binding/unbinding to the DNA, rather than by the SOS response, challenging the accepted view. Our work highlights the importance of including detailed biophysical processes in biochemical-systems models to quantitatively predict the bacterial response to antibiotics.

1

Introduction

It is difficult to exaggerate the impact antibiotics have had on modern medicine, yet how exactly they inhibit bacterial growth and proliferation remains controversial (1,2). Understanding mechanisms of antibiotic-induced growth inhibition is not only interesting from a basic science point of view, but also has the potential to contribute to rational drug design and optimization of treatment strategies that reduce the chance of resistance evolution (3–9). To this end, quantitative models for antibiotic action that can be integrated into models for resistance evolution are much needed.

Even though many antibiotics have well-defined molecular targets (10), the transition from a healthy bacterial cell to a dead, or non-growing, cell upon exposure to an antibiotic can be a complex and slow process. A prominent example is the bacterial response to fluoroquinolones – a class of DNA-targeting antibiotics that are used to treat a wide range of bacterial infections (11). Fluoroquinolone antibiotics typically produce a delayed response: bacteria initially continue to elongate after exposure (12), and a significant fraction of cells are still viable after 2-3h (13), even at concentrations where the antibiotic eventually kills almost all cells. Such a delayed response may play a role in the evolution of resistance, because elongating cells can continue to mutate and produce resistant offspring (14). However, no model has yet been proposed that explains the delayed response, and the delay also has not been accounted for in models of resistance evolution.

Fluoroquinolones target bacterial topoisomerases II (gyrase) and IV: enzymes that cut and re-seal the DNA, releasing the mechanical stresses accumulated during transcription and DNA replication, and helping to separate replicated chromosomes (15). Different fluoroquinolones have different binding affinities to topoisomerases II and IV. For example, ciprofloxacin – one of the most used antibiotics worldwide – binds predominantly to DNA gyrase in wild-type *E. coli* and only much more weakly to topoisomerase IV (16).

Ciprofloxacin traps the gyrase on the DNA as a DNA-protein complex and prevents it from dissociating (17). This has two main effects. Firstly, the poisoned (ciprofloxacin-bound) gyrases act as roadblocks for DNA replication forks (18), blocking DNA synthesis (19) and causing double-strand DNA breaks (DSBs) via a "chicken-foot" mechanism (20). Secondly, the poisoned gyrases also cause double-strand DNA breaks independently of replication fork activity (19,21). A single unrepaired DSB can be lethal in *E. coli* (22), but cells have mechanisms to repair DSBs. One of these is SOS-mediated repair via the RecBCD machinery (23). A side effect of the activation of SOS is the suppression of cell division. The resulting filament formation and a change of the typical aspect ratio from ≈ 4 (24) to > 10 is a characteristic signature of exposure to fluoroquinolones (14). For this reason, it is often thought that the SOS response is central in understanding the action of fluoroquinolones. Despite much work on the molecular mechanism of fluoroquinolone action, very little work has been done on the dynamics of growth inhibition when antibiotic-naïve cells are exposed to a fluoroquinolone, and as yet no models

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101 have been proposed to predict this dynamical response, despite its relevance
102 for resistance evolution. Moreover, some molecular aspects of the response
103 also remain unclear; in particular the relative importance of DNA replication,
104 replication-dependent and replication-independent DSBs, and SOS-mediated
105 DSB repair (19).
106
107 Here we use a combination of experiments and computer simulations to better
108 understand these processes. The objectives of our study are: (i) to determine
109 the short- and long-term response to ciprofloxacin through precise
110 measurements of cell growth rate and the amount of DNA, (ii) to create a
111 mathematical model consistent with the molecular mechanism described
112 above and with our experimental results, (iii) to understand whether the
113 delayed growth response can be explained by the altered DNA production
114 rate predicted by our model.
115
116 Our main result is that key features of the action of ciprofloxacin on growing *E.*
117 *coli* bacteria can be explained using a relatively simple model that accounts
118 for DNA replication fork stalling and both replication-dependent and -
119 independent DSBs caused by ciprofloxacin-poisoned gyrase, but does not
120 include an explicit SOS response. The model successfully reproduces the
121 long-term response to ciprofloxacin (growth inhibition curve) and, crucially,
122 also predicts the short-term dynamics of *E. coli* in response to ciprofloxacin
123 upshift, on the population- and single-cell levels. This challenges the view that
124 the SOS response is central, suggesting instead that the SOS system, while
125 important in setting the model parameters, does not determine the time scale
126 of the response of *E. coli* to ciprofloxacin.
127
Results

128
129
1. Parabolic shape of the growth inhibition curve suggests a cooperative inhibition mechanism

130
131
132
133 To understand the response of *E. coli* to ciprofloxacin (CIP) we first measured
134 the long-term (steady-state) growth rate at different CIP concentrations: the
135 growth inhibition curve. Previous work (25) indicated that the inhibition curve
136 of *E. coli* could be modelled by a Hill function with a plateau at low
137 concentrations. However, these experiments might not have been in a state of
138 balanced growth as the bacteria were exposed to CIP for only one hour.
139
140 To determine the steady-state growth rate for different CIP concentrations, we
141 used two different methods (Figs. 1, S1). We first measured *E. coli* growth
142 curves for a series of CIP concentrations by incubating bacteria in microplates
143 (200 µl/well) in a plate reader, and sampling the optical density every few
144 minutes over 1-2 days (Methods). We used two strains: the K-12 strain
145 MG1655, and a mutant derivative AD30. AD30 does not produce functional
146 fimbriae and therefore sticks less to surfaces (Fig. 1B and Methods),
147 preventing biofilm growth during the experiment. To minimize potential
148 problems such as the dependence of optical density on cell shape (26), which
149 changes during CIP-induced filamentation (14,27), we extracted growth rates
150 from time shifts between growth curves for cultures with different initial cell

3

density (Methods). Both strains produced very similar growth inhibition curves with a characteristic inverted-parabola-like shape (Fig. 1A, B). This shape is consistent with previous results for ciprofloxacin (25) but differs from that produced by many other antibiotics (5,25).

In parallel, we measured exponential growth rates for a range of CIP concentrations using steady-state cells grown in a turbidostat – a continuous culture device that dilutes cells once they reach a threshold density, maintaining exponential growth over long times (Methods and Fig. S1C, D). This could only be done for strain AD30, because the wild-type strain MG1655 rapidly forms a biofilm in the turbidostat. The growth rates in the turbidostat agree with those obtained from plate reader growth curves (Figure 1B).

If a culture is in a state of balanced exponential growth, all components of the bacterial cell must replicate at the same rate (28). Therefore the measured exponential growth rate should be the same as the rate of DNA synthesis. To confirm this, we measured total DNA at multiple time points in an exponentially growing culture for different CIP concentrations, and extracted the DNA production rate (Methods). Figure 1C shows that indeed the rate of DNA production matches the exponential growth rate as measured in our plate reader and turbidostat experiments.

Taken together, these results show that the long-term, steady-state rate of DNA production is a non-linear, inverted parabola-like function of CIP concentration, with only a small slope at zero CIP. If each DSB caused by CIP contributed (with probability p) independently to the probability of cell death, and the number of DSBs was n, the per-cell death rate would be proportional to $1 - (1 - p)^n \approx 1 - e^{-pn}$. Assuming that n increases proportionally to the CIP concentration c, we would then expect a concave relationship between the net growth rate (birth minus death) and c, with a negative slope at low c. As this is not the case, a cooperative effect may be at play, which causes the number of DSBs to increase faster than linearly with c. Alternatively, one might imagine a mechanism in which the number of DSBs is proportional to c but must exceed a certain threshold before its effects on the growth rate become visible. We will show that the first hypothesis (non-linear increase of DSBs) is strongly supported by the data (Secs. 2-6), whereas the alternative hypothesis (threshold number of DSBs needed for growth inhibition) is not (Sec. 7).

2. A quantitative model for the action of ciprofloxacin

To understand how the rate of DNA synthesis is affected by ciprofloxacin, we developed a quantitative model (Fig. 2). The model includes reversible replication fork stalling by CIP-poisoned gyrases, and both replication-dependent and replication-independent double strand breakage.

In our model, a bacterial culture is represented by an ensemble of replicating circular chromosomes. New chromosomes are synthesized on the template of parent chromosomes and remain attached to them via replication forks. The forks start from the origin of replication (*oriC*) and end at the terminus (*ter*).

4

201   Initiation occurs at time intervals drawn from a normal distribution with mean
202   τ_{fork} =24 min chosen to reproduce the CIP-free growth rate from Fig. 1B, and
203   standard deviation $\sigma(\tau_{\text{fork}})$= 5 min (arbitrary value). Once initiated, replication
204   forks progress at a constant rate v_f = 30 kb/min (29). When a chromosome
205   successfully completes replication, it separates from the parent chromosome.
206
207   Poisoned gyrases can appear anywhere along the chromosome with rate
208   k_+L/L_0, where k_+ is the DNA-poisoned gyrase binding rate, L is the current
209   chromosome length, and L_0 is the birth length of a fully replicated
210   chromosome. We assume that the rate k_+ is proportional to the extracellular
211   CIP concentration c with an unknown proportionality constant q (units =
212   1/(time*concentration)): $k_+ = qc$. Poisoned gyrases can also dissociate from
213   the chromosome with rate $1/\tau_{\text{gyr}}$, where τ_{gyr} is the turnover time. The number
214   of poisoned gyrases on the chromosome fluctuates, with the average value
215   being determined by the balance between the binding and removal rates:
216   <$\underline{N}_{\text{gyr}}$> = k_+ τ_{gyr} L/L_0.
217
218   If a replication fork encounters a poisoned gyrase it stops and remains stalled
219   until the poisoned gyrase is removed. The poisoned gyrase can also damage
220   the entire chromosome irreversibly with rate p_{kill} (Fig. 2C). Damaged
221   chromosome "conglomerates" (i.e. chromosomes plus any connected DNA
222   loops) are removed from the simulation. The exact nature of the DNA damage
223   is not important for the model, but a biologically plausible mechanism would
224   be the creation of a DSB that does not get repaired (15). The process of
225   repair is not modelled explicitly, but its effectiveness is implicitly included in
226   the value of p_{kill} (e.g., a large value of p_{kill} corresponds to impaired DNA repair,
227   since a poisoned gyrase is more likely to cause irreversible damage).
228
229   Our model has three unknown parameters: $\tau_{\text{gyr}}, p_{\text{kill}}$, and the proportionality
230   constant q that relates the extracellular concentration of CIP to the rate k_+
231   with which poisoned gyrases appear on the chromosome.
232
233
234   **3. The model reproduces the growth inhibition curve**
235
236   We first checked if the model could reproduce the growth inhibition curve from
237   Fig. 1. To do this, we calculated the rate of exponential increase of total DNA
238   predicted by the model as a function of the CIP-proportional poisoned gyrase
239   binding rate k_+ (Fig. 3A, B). Figure 3B shows predicted growth inhibition
240   curves for fixed $\tau_{\text{gyr}} = 15$ min (arbitrary value) and a range of values of p_{kill}.
241   The simulated curves resemble the experimental curve (Fig. 1A). As
242   expected, the rate of DNA synthesis decreases as the parameter k_+
243   increases, mimicking increasing CIP concentration.
244
245   We next systematically explored the parameter space (p_{kill}, τ_{gyr}, q) to find a
246   range of parameter combinations that quantitatively reproduce our
247   experimental data. Figure 3C shows that such a range indeed exists (dark
248   blue region of Fig. 3C); the best-fit parameters are $p_{\text{kill}} = (7 +/- 2)\cdot 10^{-5}$ min^{-1}
249   and $\tau_{\text{gyr}} = (25 +/- 5)$ min, and $q = (0.030+/- 0.005)$ ml ng^{-1} min^{-1}. This

5

combination produces an excellent fit to the experimental data (Fig. 3D). Our fitted value for τ_{gyr} is about half the turnover time (~55 min) that has been estimated from *in vitro* reconstitution assays (30); this discrepancy is perhaps not surprising since the *in vitro* assay lacks DNA repair systems (23) that may actively remove poisoned gyrases.

One can also extract from the model the average number of poisoned gyrases per chromosome, N_{gyr}, for a given CIP concentration (Fig. S2). For a CIP concentration of 10 ng/ml, which corresponds to a two-fold reduction in the growth rate, we obtain $N_{gyr} \approx 4$. The model thus suggests that a small number of poisoned gyrases is enough to inhibit growth (a typical gyrase copy number in the absence of CIP is ~500).

Our model explains why the growth inhibition curve assumes a parabolic shape. At low concentrations of CIP there are very few poisoned gyrases present; DNA replication proceeds at almost normal speed and the chromosome topology is almost normal (since there are few blocked replication forks). Since the rate at which a chromosome conglomerate is damaged by CIP is proportional to the total DNA in the conglomerate, and p_{kill} is small, chromosome "death" is negligible at low CIP. However, as the CIP concentration c increases, replication forks become blocked more often. As a consequence, new replication forks are initiated before the parent and daughter chromosomes separate, producing large interconnected DNA conglomerates. Because the total DNA per conglomerate increases, the number of poisoned gyrases that are bound to the DNA also increases. This produces a faster-than linear increase in the degree of growth inhibition as c increases.

To confirm this interpretation of our model, we considered a modified model in which the damage caused by a poisoned gyrase does not "kill" the entire chromosome conglomerate but only the chromosome segment to which it is attached. There is some evidence that this might be the case for *E. coli* that is deficient in DSB repair (31). This modified model predicts a very different growth inhibition curve (Fig. S3) which lacks the plateau at low CIP concentration.

4. The model predicts the dynamical response of *E. coli* to ciprofloxacin

Our model has been parameterized to reproduce the inhibition curve for steady-state growth in the presence of ciprofloxacin. To check if the model is able to predict the <u>dynamical</u> response of *E. coli* to ciprofloxacin (for which it has not been parameterized), we exposed the *ΔfimA* strain AD30 to a step-up in ciprofloxacin concentration and measured dynamical changes in the growth rate over many generations in the turbidostat while maintaining cells in the exponential growth phase. Interestingly, we observed that for low concentrations of ciprofloxacin, the growth rate does not decrease immediately on antibiotic addition. The time until the growth rate begins to decrease, and the time to achieve a new steady-state growth rate, both depend on the CIP concentration (Fig. 4A).

6

300
301 Our model cannot predict the bacterial growth rate directly as it focuses on the
302 rate of DNA synthesis, which does not have to be the same as the population-
303 level growth rate during periods of unbalanced growth. However, the model
304 can be used to predict the time to the new steady state (Fig. 4B; see
305 Methods). The predicted values agree well with the results of our
306 experiments.
307
308 We next checked if the model also correctly predicts the dynamical response
309 of DNA synthesis to ciprofloxacin exposure in single cells. We treated *E. coli*
310 cells (MG1655) with ciprofloxacin for 1 hour, stained with DAPI to visualize
311 DNA, and imaged in the bright field and fluorescent channels (Fig. 5). To
312 prevent cell division and thus enable a direct comparison with the model, we
313 used cephalexin (8 μg/ml), which inhibits PBP3, a component of the *E. coli*
314 septation machinery (32). As expected, all the cells grew as filaments, without
315 dividing (Fig. 5A).
316
317 The bacterial elongation rate is extracted from our measured filament length
318 distributions by assuming exponential elongation with constant rate α starting
319 from the initial length distribution of untreated cells (Methods). For cells
320 treated with cephalexin only, the experimental length distribution was best fit
321 by an elongation rate α =(1.85 +/- 0.28) h^{-1}, similar to the growth rate obtained
322 in plate reader experiments without any antibiotic (1.70 +/- 0.10 h^{-1}, Figs. 1B,
323 5B). Therefore, cephalexin prevented cell division without visibly decreasing
324 the biomass growth rate.
325
326 Remarkably, the cell length distribution (and hence the biomass growth rate)
327 remained unchanged when cells were exposed to both ciprofloxacin (up to
328 15ng/ml) and cephalexin (Fig. 5B). This observation is consistent with
329 previous microscopy data (14). Even at the highest CIP concentration used
330 (50ng/ml, ~2.5x MIC for this strain), the elongation rate was only slightly
331 reduced (Fig. 5B, right).
332
333 We next characterized the DNA organization in single cells following exposure
334 to CIP and cephalexin. Figure 5C shows that cells treated solely with
335 cephalexin have clearly defined, evenly spaced chromosomes. The overall
336 chromosome density is consistent with that of antibiotic-free growth; for
337 example, for a cephalexin-treated filament of length 24 μm we observe ~16
338 chromosomes, while *E. coli* of length 3 μm grown on LB antibiotic-free
339 medium typically has ~2 chromosomes (Fig. S6A). However, in the presence
340 of CIP, DNA become less ordered and, as the CIP concentration increases,
341 fewer distinct chromosomes can be identified. This suggests the presence of
342 large entangled DNA structures and the failure of chromosome separation.
343
344 Our model makes a very specific prediction for how the total DNA in a
345 filamentous cell should depend on CIP concentration after 1h of exposure
346 (Fig. 6A). To test this prediction, we quantified the total DNA per cell by
347 measuring DAPI fluorescence in microscopic images of cells for different
348 concentrations of CIP. We obtained excellent quantitative agreement between
349 our simulations and experiments (Fig. 6B), without any additional fitting. Thus

7

350 our model, once fitted to the steady-state data, correctly predicts the early-
351 time dynamical response to ciprofloxacin in single cells.
352

5. Replication-dependent and replication-independent DNA damage predict the same shape of growth-inhibition curve

356 Ciprofloxacin-bound DNA gyrase has been hypothesized to cause both
357 replication-dependent and replication-independent DNA double strand breaks
358 (18,19,21). To test the role of replication-dependent versus replication-
359 independent killing, we simulated a version of the model in which
360 chromosome damage only occurs via fork-associated poisoned gyrase
361 (Methods). This model turns out to reproduce the growth inhibition curve
362 equally well (Fig. S7). Thus, models with replication-dependent only or both
363 replication-dependent and replication-independent DNA breaks produce the
364 same growth inhibition dynamics.
365

6. Basal DNA damage is sufficient to model a DNA repair-deficient mutant

369 Our model does not explicitly include repair of DNA double strand breaks,
370 which happens in *E. coli* via the RecBCD machinery, triggered by the SOS
371 response (15,33). We tested the role of DNA repair using a *recA* deletion
372 mutant that cannot trigger the SOS response (Methods). We first investigated
373 the growth of the Δ*recA* strain in the absence of ciprofloxacin. Δ*recA* cells
374 were similar in length and width to WT cells, but had less organized
375 chromosomes (Fig. S6B). In microplate cultures, the Δ*recA* strain showed a
376 reduced growth rate compared to that of the WT MG1655 strain (~1 h^{-1} versus
377 1.7 h^{-1} for WT). However, upon treating Δ*recA* cells with cephalexin and
378 measuring the cell-length distribution after 1 h, we found that individual Δ*recA*
379 cells elongate at the same rate as WT, although in the majority of the cells,
380 the DNA looks less organized (Fig. 7A, B). To resolve this apparent
381 contradiction, we imaged microcolonies of the Δ*recA* and WT strains growing
382 on agar pads. Interestingly, the Δ*recA* colonies were significantly smaller and
383 many colonies (~30%) did not grow at all (Fig. S9). This suggests that the
384 reduced population-level growth rate of Δ*recA* cultures is due to an increased
385 fraction of non-growing cells, rather than a decreased single-cell growth rate.
386 This is consistent with previous observations that cultures of bacteria deleted
387 for *recA* can contain a significant sub-population of non-growing cells (34,35).
388

389 We also wondered if our model could predict the shape of the growth
390 inhibition curve for the Δ*recA* strain. We measured the Δ*recA* growth inhibition
391 curve in the plate reader (Fig. 7C). The MIC of this strain (~1.5ng/ml) was an
392 order of magnitude lower than that of the WT. Moreover, the shape of the
393 growth inhibition curve was significantly different compared to parabola-like
394 curve of the WT (Fig. 1): for Δ*recA* the growth rate decreased approximately
395 linearly with increasing CIP concentration, without a plateau at low CIP. We
396 hypothesized that these features could be reproduced in our model by an
397 elevated rate of DNA damage associated with CIP-poisoned gyrases,
398 combined with a basal DNA damage rate in the absence of CIP, both being

8

399 due to the lack of the DSB repair mechanism. A modified model, in which the
400 basal DNA damage rate p_{kill0} = 0.0033 +/- 0.0002 min^{-1} was fixed by fitting to
401 the population growth rate in the absence of CIP, reproduced the
402 experimental growth inhibition curve very well (Fig. 7C, p_{kill}, q were fitted to
403 the inhibition curve). The same model also reproduced the growth-inhibition
404 curve for the $\Delta recA\Delta fimA$ double mutant (Fig. S8). One can intuitively
405 understand the origin of the negative slope at zero drug: the basal damage
406 rate acts as if non-zero CIP was present even when the actual concentration
407 of the antibiotic is zero. This causes the parabolic curve of the WT to shift to
408 the left, leaving only the part that is almost linear in the CIP concentration.
409
410 To investigate if our model could also predict the dynamic response, we
411 repeated the turbidostat experiment from Fig. 4 for $\Delta recA\Delta fimA$. Figure 8
412 shows that the time to reach the new steady-state growth rate after a CIP
413 upshift (T_{ss}) is very well predicted by the model. All this shows that even
414 though our model does not explicitly include DNA repair, an implicit modelling
415 of DNA repair via the parameters p_{kill0} and p_{kill} is sufficient to reproduce our
416 experimental data.
417

418 ### 7. An alternative hypothesis based on saturation of repair
419 ### mechanisms does not explain the data
420
421 Our model reproduces all our experimental observations – but could an
422 alternative model based on a different microscopic mechanism explain them
423 equally well? To investigate this, we considered a biologically plausible model
424 in which the parabolic shape of the inhibition curve arises due to a non-linear
425 response of the DNA repair mechanism to CIP concentration, rather than from
426 a non-linearity in the amount of DNA damage as in the previous model.
427

428 In this alternative model, for CIP concentrations above the MIC, DSB repair
429 mechanisms become saturated, which causes the accumulation of DSBs.
430 Below the MIC, however, we assume that recBCD-mediated DSB repair (36)
431 is very effective. Specifically, we assume that the number $n(t)$ of DSBs
432 evolves as
433

$$\frac{dn}{dt} = b - \min(r_{max}, rn^{\gamma}).$$

434
435 Here, DSBs are created at a rate b that is proportional to CIP concentration,
436 and are removed via repair at a rate rn^{γ}, which cannot exceed the maximum
437 rate r_{max}. The exponent γ characterizes the strength of the feedback between
438 the number of DSBs and the rate of repair; $\gamma = 1$ corresponds to a linear
439 response, whereas $\gamma < 1$ means that repair mechanisms are strongly
440 triggered even by a small number of DSBs. We further assume that each DSB
441 has equal probability p of killing the cell, hence the net growth rate is
442 proportional to $\exp(-pn)$.
443

444 This model, which does not consider the dynamics of DNA replication,
445 reproduces the steady-state growth inhibition curve quite well (Fig. S10) for
446 $\gamma \approx 0.5$. However, the model predicts that the time to reach a new steady-

9

447 state growth rate following an upshift of CIP should be proportional to

448 $b^{\frac{1}{\gamma}-1} \approx b$. The time to the new steady state is thus predicted to increase with
449 CIP concentration (since b increases with c) which disagrees with what we
450 observe experimentally (Fig. 4). Therefore, this model fails to reproduce the
451 dynamics of CIP inhibition.
452
453
454 **DISCUSSION**
455
456 Despite much work on the molecular mechanisms of fluoroquinolone action,
457 no models have yet been proposed that explain the delay in the bacterial
458 response to low concentration exposure, even though this may well have
459 important consequences for the chances of resistance evolution. We have
460 proposed a quantitative model for fluoroquinolone-induced growth inhibition of
461 the bacterium *E. coli* that for the first time explains the response delay. Our
462 model is based on the known molecular details of replication fork stalling and
463 DNA damage, and makes quantitative predictions for the long- and short-term
464 (dynamic) bacterial response to the fluoroquinolone ciprofloxacin. By fitting
465 the model's three parameters (Fig. 3) to the experimental steady-state
466 inhibition curve (long-term response), we not only reproduce the shape of the
467 curve very well but we also make correct predictions for the short-term
468 dynamics of bacterial growth following a step-up of ciprofloxacin. The
469 predictions are in agreement with our experimental data, without any further
470 parameter fitting (Fig. 4, 6). Importantly, our model also challenges the view
471 that the SOS DNA damage response plays a central role. Our model, with
472 altered parameters, also reproduces the behavior of a *recA* mutant that
473 cannot activate the DNA repair machinery and is significantly more sensitive
474 to ciprofloxacin. Thus the SOS system can significantly alter the parameters
475 of the model but, importantly, does not control the dynamics of the response.
476 Instead, the dynamics is controlled by the DNA replication rate and
477 binding/unbinding rates of gyrase from the DNA.
478
479 We have also considered modifications of the model in which DNA damage
480 occurs due to replication fork-associated gyrases only, and in which DNA
481 damage "kills" only the local DNA strand rather than the entire chromosome
482 conglomerate. It turns out that our model cannot distinguish between fork-
483 related and replication-independent killing, but is sensitive to whether
484 poisoned gyrases kill the whole cluster of interconnected DNA, or only the
485 local branch that is affected by a poisoned gyrase. The latter predicts a non-
486 parabolic inhibition curve that is at odds with the experimental data. An
487 alternative model based on the saturation of the repair mechanism as an
488 explanation of the growth inhibition curve fails to predict the dynamic
489 response to CIP.
490
491 Our work demonstrates that, despite the molecular complexity of
492 fluoroquinolone action, a simple physiological model can explain the behavior
493 of bacteria exposed to this class of antibiotics, leading to new insights that can
494 be used to make quantitative predictions. Below we discuss in more detail
495 some of the implications of our work.
496

10

497 *Shape of the growth inhibition curve.*
498 The growth-inhibition curve for CIP is parabolic-like (Fig. 1). Inhibition curves
499 for many antibiotics including CIP have been traditionally approximated using
500 the Hill function (25). This choice is often based on a qualitative description of
501 the shape rather than on mechanistic insight. The Hill function is also a
502 popular choice in population-level models of antibiotic treatment (37–39).
503 However, some antibiotics can have very different inhibition curves, that are
504 not well approximated by a Hill function (5). This is potentially important for
505 modelling the evolution of resistance to antibiotics, because differently shaped
506 inhibition curves are expected to produce different fitness landscapes (40,41),
507 leading to different levels of selection for resistant mutants, and hence
508 different trajectories to resistance.
509 We checked how well our measured growth inhibition curve can be
510 reproduced using a Hill function (Fig. S11). The fit is slightly less good than
511 that produced by our model. The Hill exponent ($\kappa = 4.4 \pm 0.5$) also differs
512 significantly from the value of $\kappa = 1.1 \pm 0.1$ that has been reported before
513 (25). We conclude that careful measurements of the steady-state growth
514 inhibition curve, combined with physiological models of antibiotic response,
515 can not only shed light on the mechanism of inhibition but are also required
516 for quantitative models of the evolution of antibiotic resistance.
517
518 *The role of the SOS response.*
519 The cellular response to DNA damage is not explicitly included in our model,
520 but rather enters through the parameter values. In others' work, the SOS
521 response has been modelled in the context of UV response (42–45). To check
522 how realistic it was to omit details of the SOS response in our model, we
523 adapted the model from Ref. (42) to our scenario. We set the initial number of
524 DSBs (parameter N_G from (42)) to zero, and added a term proportional to the
525 CIP concentration to the equation dN_G/dt which describes the rate of change
526 of the number of DSBs. We calculated the time it takes for LexA (the protein
527 whose inactivation triggers the response) to reach a new steady state after a
528 step-up in stimulus (10% above the infinite-time limit concentration). Figure
529 S12 shows that this time is less than 10 min for a broad range of DSB
530 creation rates, indicating that the SOS response occurs much faster than the
531 growth rate response we report in Fig. 4. When we fit this alternative model to
532 the data from Fig. 4B (the fitting parameter is the proportionality factor
533 between the CIP concentration and the production rate of DSBs), the reduced
534 $\chi^2 \approx 200$ for the best-fit curve is many times larger than the value reported in
535 the caption of Fig. 4B for our main model. Based on this and the excellent
536 agreement between our main model and experiments, we conclude that key
537 features of the growth inhibition in response to sub-MIC ciprofloxacin (the
538 shape of the inhibition curve and the dynamics of inhibition) can be
539 understood without modelling the SOS response explicitly. This does not
540 mean that the SOS response is not important; on the contrary, SOS-induced
541 changes in bacterial physiology (e.g., expression of low-fidelity polymerases)
542 are very important for the evolution of resistance (14,46), and the role of SOS
543 in mediating growth inhibition is also implicit in our model through the
544 parameters p_{kill} and p_{kill0}.
545
546 *The importance of chromosome segregation.*

11

547 In this work, we do not model individual cells; rather, we consider a collection
548 of replicating chromosomes. While this seems to be enough to reproduce the
549 population-level growth-rate response to ciprofloxacin, and the DNA dynamics
550 in single cells, it cannot account for some aspects of behavior at the cellular
551 level, such as the cell length distribution (in our experiments, we avoid this
552 issue by treating cells with cephalexin). More work will be required to create a
553 model that is able to, for example, predict the cell length distribution (Fig. 5),
554 cell division and budding (14), or antibiotic-induced fluctuations in the number
555 of cells in small populations (47).
556
557 *Other fluoroquinolones and bacterial species.* Based on the proposed
558 mechanism, we expect the results to be generalizable to other
559 fluoroquinolones, as long as gyrase is the primary target. This seems to be
560 the case for *E. coli* (48–50). Topoisomerase IV – the other potential target -
561 becomes important only in combination with resistant mutations in *gyrA* (51).
562 Topoisomerase IV has a stronger affinity to fluoroquinolones in other bacterial
563 species (50); we do not expect the model to quantitatively reproduce the
564 short- and long-time response for such cases. We note, however, that
565 parabolic inhibition curves have been reported for the Gram-positive
566 bacterium *Mycobacterium smegmatis* treated with nalidixic acid and
567 novobiocin (Fig. S2 in (52)). This may suggest that the long-term response
568 (and perhaps also the mechanism behind it) may be similar in other bacterial
569 species.
570
571 *Relevance for bacterial infections*
572 Predictive understanding of how antibiotics inhibit bacteria could help in the
573 design of better treatment strategies. Traditionally, models for antibiotic
574 treatment have assumed an instantaneous response of bacteria to the
575 antibiotic (53,54); models that take intracellular dynamics into account are still
576 rare (55,56). Our research shows that ignoring the transient behavior (here
577 the short-term bacterial response delay) can be problematic because these
578 transients can last for many generations at sub-MIC concentrations of the
579 antibiotic, for which the probability of developing resistance is the highest
580 (55,57,58). Our physiological model could be integrated into population-level
581 evolutionary models, allowing better prediction of the chances of resistance
582 emergence by taking account of the cell-level dynamical response. Such
583 effects are almost universally neglected in current evolutionary models. We
584 postulate that, rather than using ODE-based models (38) or stochastic models
585 such as birth-death processes (47,59), one could use individual-based
586 simulations with bacterial physiology modelled explicitly, similarly to what has
587 been done in biofilm modelling (60). In such a model, individual
588 chromosomes, simulated according to our (or a similar) model, would also
589 mutate; this would be represented by changing the model parameters to
590 account for e.g., an increased MIC for resistant mutants (decreased number
591 of poisoned gyrases). Since our model is computationally expensive, it can be
592 used only for small populations of cells (up to a few million). This may be still
593 very useful for modelling laboratory evolution of resistance in microfluidic
594 devices, which is gaining popularity (61,62). For large population sizes such
595 as those required to model human infections (tens- or hundreds of millions of
596 cells), a hybrid model could be used in which only a small number of cells

12

597 (e.g., new mutants) have explicit internal dynamics while the bulk of the
598 population is described using coarse-grained models. Such hybrid models are
599 used in cancer modelling (63,64) but have not yet been applied in
600 evolutionary microbiology.
601
602 In conclusion, we have proposed and tested a model that predicts bacterial
603 response to fluoroquinolone antibiotics. Our model complements those that
604 have recently been proposed for other classes of antibiotics; taken together,
605 such models may eventually be useful in understanding and predicting
606 bacterial response to clinically relevant treatment strategies, such as
607 the effect of combination therapies (65–67).
608
609
610 **Materials and Methods**
611
612 **Bacterial strains**
613 We used MG1655, a K12 strain of the bacterium *E. coli*, and two mutant
614 derivatives AD30 (*ΔfimA*), *ΔrecA,* and EEL01 *(ΔrecAΔfimA)*. Strain *ΔfimA* was
615 constructed by P1 transduction from JW4277 (the *fimA* deletion strain in
616 background BW25113 from the Keio collection) into MG1655 (68). The
617 kanamycin resistance cassette was removed using Flp recombinase
618 expressed in pCP20. Strain construction was confirmed by PCR using a
619 combination of kanamycin specific primers and gene specific primers.
620 The *ΔrecA* mutant was donated by M. El Karoui lab.This mutant is MG1655 in
621 which ΔrecA::CmR was introduced by P1 transduction from DL0654 (David
622 Leach, laboratory collection). Strain *ΔrecAΔfimA* was created by P1
623 transduction of the *recA* deletion with a chloramphenicol resistance selection
624 marker from the MG1655 *ΔrecA* strain. Briefly, the donor strain MG1655
625 *ΔrecA* was incubated overnight and inoculated at 37 ^{o}C for 25 minutes with
626 different dilutions of P1*vir* phage in the presence of $MgSO_4$ and $CaCl_2$ before
627 being mixed with molten top agar and spread onto an LB plate, left to set, and
628 incubated at 37°C overnight. Donor phage was harvested from the top agar
629 by mixing with phage buffer and a few drops of chloroform, the debris spun
630 down and the supernatant containing the donor phage used for transduction
631 into the recipient strain (*ΔfimA*). For the transduction, the recipient strain was
632 incubated overnight, harvested, and resuspended in LB with $MgSO_4$ and
633 $CaCl_2$, mixed with P1 donor phage, incubated at 37°C for 30 minutes before
634 the addition of sodium citrate. Cells were then incubated (37°C, 200 rpm) to
635 allow for expression of chloramphenicol resistance, and spun down and
636 plated onto LB plates with chloramphenicol for selection of the *ΔrecA::Cam^R*
637 construct. Following an overnight incubation at 37°C, colonies were purified
638 twice on chloramphenicol plates with sodium citrate.
639
640
641
642 **Growth media and antibiotics**
643 All our experiments were performed in LB medium at 37°C. LB liquid medium
644 was prepared according to Miller's formulation (10g tryptone, 5g yeast extract,
645 10g NaCl per litre). The pH was adjusted to 7.2 with NaOH before autoclaving

13

646 at 121°C for 20 min. To create LB in 1.5% agar, agar (Oxoid, Agar
647 Bacteriological, No. 1) was added before autoclaving.
648 Ciprofloxacin solutions were prepared from a frozen stock (10mg/ml CIP
649 hydrochloride in ddH2O) by diluting into LB to achieve desired concentrations.
650 Stock solution of cephalexin (10mg/ml) was prepared by dissolved 100mg of
651 cephalexin monohydrate in 10 mL of DMSO.
652
653 **Growth inhibition curves**
654 To determine the growth rate at a given concentration of CIP, we used two
655 different methods.
656
657 *Method 1.* We incubated bacteria in a micro-plate inside a plate reader (BMG
658 LABTECH FLUOstar Optima with a stacker) starting from two different initial
659 cell densities, and measured the optical density (OD) of each culture every 2-
660 5 min to obtain growth curves.
661 Plates were prepared automatically using a BMG LABTECH CLARIOstar
662 plate reader equipped with two injectors to create different concentrations of
663 CIP in each column of a 96 well plate (total injected volume 195µl per well).
664 Bacteria were diluted from a thawed frozen stock 10^3 and 10^4 times in PBS,
665 and 5µl of the suspension was added to each well (10^3 dilution to rows A-D,
666 10^4 dilution to rows E-H). After adding bacteria, plates were sealed with a
667 transparent film to prevent evaporation, and put into a stacker (temperature
668 37°C, no shaking), from which they would be periodically fed into the
669 FLUOstar Optima plate reader (37°C, orbital shaking at 200rpm for 10s prior
670 to OD measurement).
671 Assuming that all cultures grow at the same rate when cell density is low
672 (OD<0.1), the time shift (ΔT) between the curves from rows A-D and E-H (Fig.
673 S1A) is related to the exponential growth rate as follows:
674

$$a = \frac{\ln 10}{\mathrm{D}T}.$$

676 We used this relationship to calculate α from time shifts between 4 pairs of
677 replicate experiments (A-E, B-F, C-G, D-H) for 12 concentrations of
678 ciprofloxacin (range: 0—30 ng/ml). To validate the method we also calculated
679 growth rates by fitting an exponential curve $A + Be^{\alpha t}$ to the low-OD (OD<0.1)
680 part of the growth curve. The time-shift method gives more accurate but
681 overall similar results compared to the exponential curve fitting (Fig. S1B) or
682 maximum growth rate measurement methods (69). Our fitting method is not
683 sensitive to the relationship between the OD and the true cell density (which
684 depends on the cell shape and size) and it gives the average growth rate over
685 many more generations (growth from approx. 10^4 to 10^8 cells, ≈ 13
686 generations) than curve-fitting based methods (OD=0.01-0.1, 3 generations),
687 see Fig. S1B.
688
689 *Method 2.* To confirm that our measurements correspond to steady-state
690 growth, we also measured the growth rate in a turbidostat (Fig. S1C), in which
691 bacteria are kept at approximately constant optical density (OD=0.075-0.1) for
692 many generations by diluting the culture with fresh medium (and concomitant
693 removal of spent medium + bacteria) whenever the OD reaches a threshold

14

694 value. The growth rate is obtained by fitting an exponential function to the
695 background-corrected OD data between consecutive dilutions.
696
697 We found that strains MG1655 and AD30 have similar but not identical
698 susceptibility to ciprofloxacin: while the MG1655 wild type showed an MIC of
699 (19 +/- 3) ng/ml, in agreement with previous measurements (16), AD30 was
700 slightly less susceptible, with an MIC of (24+/- 3) ng/ml. The MIC values were
701 determined from the zero-growth point of the growth inhibition curves (3-6
702 replicate experiments).
703

Measurements of DNA production
705 To obtain the data in Fig. 1C, cells were grown in LB medium with or without
706 CIP in shaken flasks (3 replicates), and diluted periodically with fresh medium
707 to maintain steady-state exponential growth. Cells were sampled every ~20-
708 30 min, fixed (1ml of culture fixed with 250µL of 1.2% formaldehyde) and their
709 OD was measured using both a standalone spectrophotometer (Cary 100 UV-
710 Vis) and a plate reader (CLARIOstar) for cross-validation. DAPI was added to
711 the fixed samples to a concentration 2 µg/mL (27). After 30 min of incubation
712 with DAPI the cells were washed 3 times with PBS, and DAPI fluorescence
713 intensity was measured in the plate reader (CLARIOstar). Growth rates were
714 extracted from the fluorescence and OD versus time curves by least-squares
715 fitting of an exponential function.
716

Microscopy
718 To obtain the data from Figs. 5 and 7, exponentially growing cells (LB flasks)
719 were treated with ciprofloxacin and/or cephalexin. The samples were fixed
720 with formaldehyde and incubated for 30 min with DAPI (2 µg/mL(27)) and
721 0.1% TRITON to increase cell permeability. The fixed cells were put on
722 agarose pads (2 % agar in water) and imaged on a Nikon Eclipse Ti epi-
723 fluorescent microscope using a 100x oil objective (excitation 380-420 nm,
724 emission >430 nm, exposure time 100 ms). Cell lengths, widths, and
725 fluorescence intensity were extracted using the Fiji plug-in MicrobeJ (70). For
726 measuring the area of micro-colonies (Fig. S9) we used semi-automated
727 ImageJ plugin JFilament (71). After extracting the coordinates of the micro-
728 colony contours from phase-contrast images, colony area was calculated as
729 the area of the corresponding polygon (72,73).
730

Computer simulations of the DNA replication model
732 The computer code used to simulate our model was written in Java. Each
733 chromosome is represented as a one-dimensional lattice of $L_0 = 1000$ sites.
734 The ends of the lattice are either linked to each other (to represent a circular
735 chromosome) or to another chromosome lattice at points corresponding to the
736 current positions of the replication forks. Poisoned gyrases are identified by
737 the index of the chromosome on which they sit, and their position (lattice site)
738 within that chromosome. The simulation proceeds in discrete time steps (dt
739 $=N_{bp}/(L_0 v_f)$, where $N_{bp} =4,639,675$ is the number of base pairs in the *E. coli*
740 chromosome, and $v_f = 30,000$ bp/min is the fork speed. At each timestep, the
741 position of each fork that can move (i.e. that is not blocked by a gyrase) is
742 advanced by one lattice unit. Gyrases bind and detach with probabilities
743 proportional to the corresponding rate times dt. Chromosomes are killed with

15

744 probability $p_{\mathrm{kill}}\mathrm{d}t$ times the number of poisoned gyrases, and removed from
745 the simulation. Chromosomes are separated when two forks reach the
746 endpoints of the mother chromosome. A pair of new forks is added every τ_{fork}
747 time units, where τ_{fork} is drawn from a normal distribution with mean 24 min
748 and std. dev. 5 min. In simulations of the model with DNA damage occurring
749 only at the forks, only stalled forks kill chromosomes (probability $p_{\mathrm{kill}}\mathrm{d}t$ per
750 stalled fork).
751
752 All simulations were initiated with a single chromosome at $t = 0$ h, and
753 stopped at $t = 6$ h (Figs. 3, S5, 7) or $t = 5$ h (Fig. 6). Between 1000 and 5000
754 independent runs were performed to obtain averaged curves. The step of CIP
755 in Fig. 6 was simulated by running the simulation with $k_+ = 0$ for $t < 100$ min,
756 and switching to $k_+ > 0$ corresponding to the desired CIP concentration for $t >$
757 100 min.
758
759 To fit the model to the experimental growth inhibition curves we systematically
760 explored the space of parameters p_{kill} and τ_{gyr} (Fig. 3). The parameter p_{kill} was
761 varied in the range $5{\cdot}10^{-5}$-$10^{-3}\,\mathrm{min}^{-1}$ for 11 data points, and τ_{gyr} was varied in
762 the range 0 - 80 min in 5 min steps. For a given pair of values for p_{kill} and τ_{gyr}
763 we simulated the model with different values of k_+ and varied the scaling
764 factor q to fit the experimentally obtained growth-inhibition curve by
765 minimizing the sum of squares between the experimental and simulated
766 inhibition curves. The best fit was obtained for $p_{\mathrm{kill}} = (7 +/- 2){\cdot}10^{-5}\,\mathrm{min}^{-1}$ and τ_{gyr}
767 $= (25 +/- 5)$ min, $q = (0.030 +/- 0.005)$ ml ng^{-1} min^{-1} for the model with
768 replication-independent killing, and $p_{\mathrm{kill}} = (2 +/- 1.5){\cdot}10^{-5}\,\mathrm{min}^{-1}$ and $\tau_{\mathrm{gyr}} = (30 +/-$
769 5) min, $q = (0.040 +/- 0.005)$ ml ng^{-1} min^{-1} for the model with replication-
770 dependent killing (at the forks).
771
772 **Model for exponentially growing filaments (cephalexin)**
773 To extract growth rates from the filament length distributions in Figs. 5 and 7,
774 each cell was assigned an initial length l_0 from the experimentally observed
775 distribution (Fig. S5B), and a random growth rate a taken from a Gaussian
776 distribution characterized by its mean and standard deviation ($\alpha, \sigma(\alpha)$). The
777 new cell length after time $t = 1$h was calculated as $l = l_0 \exp(at)$. A histogram
778 of 642 000 predicted cell lengths was compared with the experimentally
779 obtained cell length distribution for cephalexin-treated cells. The best match
780 was obtained for $\alpha = 1.86$ h^{-1} and $\sigma(\alpha) = 0.22$ h^{-1} using the p-value from the
781 Kolmogorov-Smirnov test as the goodness-of-fit measure. The best-fit mean
782 growth rate was similar to the growth rate measured in the plate reader (1.7 h^{-}
783 ^{1}, Fig. 1A) indicating that cephalexin treated cells continued to elongate with
784 the same rate for at least one hour in the presence of CIP. The spread of
785 elongation rates given by $\sigma(\alpha)$ is similar to that observed for untreated cells
786 (74,75).
787
788 **Finding time to steady state (T_{ss})**
789
790 The time to new steady state (T_{ss}) was calculated from the experimental data
791 (growth rates versus time) as the time from the step-up of CIP to the point at
792 which the growth rate decreased to the threshold value $0.1k_0 + 0.9k_{\mathrm{ss}}$, where

16

793 k_0 is the growth rate before CIP and k_{ss} is the steady state growth rate (Figs.
794 4, 8). In the case of experiments with CIP > MIC, k_{ss} was assumed to be 0 h^{-1}.
795 To calculate T_{ss} in simulations, we used the same approach with the threshold
796 growth rate $0.01k_0 + 0.99k_{ss}$. Different thresholds for experimental/simulated
797 data were used to balance systematic errors: difficulty in detecting the true
798 steady-state in experiments, growth rates representing two different quantities
799 (OD-based growth rate in experiments, DNA-concentration based growth rate
800 in simulations).

Turbidostat

804 Our turbidostat device (Fig. S1C) encompasses 4 replicate cultures with a
805 culture volume of approx. 26 mL. The growth medium used in all experiments
806 was LB broth (Miller), and the *E. coli* strain used was AD30, to avoid biofilm
807 formation. In the turbidostat, all cultures are connected to a bottle of LB
808 medium and a bottle of LB + CIP (at 10x the desired CIP concentration in the
809 culture) through a system of computer-controlled syringe pumps and valves.
810 The optical density is measured every 20 s using custom-made photometers
811 (separate for each bottle) to which 3-4 ml of each culture is aspirated and
812 dispensed back into the culture using a syringe pump. When the optical
813 density reaches OD=0.1 or after 30 min since the last dilution (whichever
814 happens first), 25% of the culture is replaced with fresh medium to maintain
815 exponential growth. An appropriate volume of CIP-containing LB medium is
816 injected 2 hours after OD=0.1 is reached for the first time to achieve the
817 required concentration (5-100 ng/ml) in the culture. Smaller volumes are
818 injected in all subsequent dilution steps to maintain the prescribed
819 concentration of CIP for the rest of the experiment. All cultures are kept in an
820 incubator set to 37°C and are continuously stirred using magnetic stirrers and
821 aerated with an air pump to keep dissolved oxygen (measured using
822 Pyroscience FireStingO2) well above 50% of saturation concentration at 37°C
823 (aerobic conditions).

Figure captions

Figure 1. Growth-inhibition curve for ciprofloxacin and DNA production rates. (A)
841 Growth-inhibition curve for ciprofloxacin treated *E. coli* (MG1655) for different antibiotic
842 concentrations (plate reader data, green points). The orange line is a quadratic fit to the data.
843 The minimum inhibitory concentration (MIC) is ~20 ng/ml. Error bars represent SEM (4

17

844   replicates). (B) The growth-inhibition curve for the fimbrial knockout mutant (AD30). Growth
845   rates are normalized (divided) by the growth rate in the absence of CIP. Green points are
846   plate reader measurements, red points are measurements from turbidostat-incubated
847   exponential cultures, taken ~4 h after first exposure to ciprofloxacin. Both methods give
848   similar results. Error bars are SEM (4 replicates). The MIC of AD30 is ~25 ng/ml. (C) DNA
849   production rate (measured by DAPI staining) correlates well with biomass growth rate
850   (measured by OD). Error bars are SEM (3 replicates).

851

852   **Figure 2. Model of ciprofloxacin mechanism of action.** We model a collection of
853   replicating chromosomes. New DNA is synthesized at replication forks (black arrows).
854   Replication starts at the origin (*oriC*) and terminates at chromosome terminus (*ter*) (A). A
855   newly synthesized DNA strand remains connected with the parent chromosome until the forks
856   reach *ter* (B). Initiation of new forks at *oriC* occurs on average every τ_{fork} time units. The stars
857   represent gyrases poisoned by ciprofloxacin. Poisoned gyrases are obstacles for replication
858   forks, inducing fork stalling, and can also cause irreversible DNA damage with probability rate
859   p_{kill} (C). Once poisoned gyrase is removed from the chromosome (with turnover time τ_{gyr}),
860   stalled forks resume replication.

861

862   **Figure 3. Simulations reproduce the experimental growth inhibition curve.** (A) Total
863   amount of synthesized DNA predicted by the model as a function of time, for two different
864   DNA-poisoned gyrase binding rates ($k_+ = 0.1$ min^{-1}, green, and $k_+ = 0.6$ min^{-1}, red). These
865   rates correspond to two different ciprofloxacin concentrations below the MIC: low (growth rate
866   almost unchanged), and medium (growth rate visibly lowered). Where the curves become flat,
867   growth has been completely inhibited. Total DNA is calculated as the total length of all
868   chromosomes divided by L_0. (B) Growth rate vs DNA-poisoned gyrase binding rate (k_+)
869   obtained by fitting exponential curves to the last 30 min of the data from panel A, for different
870   values of killing rate p_{kill}. (C) Deviation between the experimental and simulated growth-
871   inhibition curves as a function of $p_{\text{kill}}, \tau_{\text{gyr}}$ (the third parameter, q, has also been fitted but is
872   not shown). A cross marks the best-fit parameters $p_{\text{kill}} = 7 \cdot 10^{-5}$ min^{-1}, $\tau_{\text{gyr}} = 25$ min and $q = 0.03$
873   ml ng^{-1} min^{-1}. (D) Experimentally measured growth inhibition curve (green), compared to the
874   simulated best-fit curve (orange). Errors are SEM (four replicates).

875

876   **Figure 4. Dynamic response to CIP in the turbidostat.** See Fig. S1C for a schematic
877   diagram of the turbidostat. (A) Growth rate as a function of time for the fimbrial knockout
878   strain AD30. Ciprofloxacin was added at 0 h. T_{ss} is the time to the new steady-state growth
879   rate ($c <$ MIC) or no growth ($c >$ MIC) following the addition of CIP (Methods). (B) The model
880   prediction for the time to new steady state is close to the experimental results. The reduced
881    $\chi^2 = 39.2$. Simulation parameters are same as in Fig. 3D. Other parameters close to the best
882   fit from Fig. 3D lead to an even better agreement (Fig. S4).

883

884   **Figure 5. Ciprofloxacin causes formation of entangled DNA structures.** (A) Phase
885   contrast microscopy images overlaid with fluorescent DAPI stained DNA images with
886   subtracted background intensity for clarity, after 1 h exposure to different concentrations of
887   ciprofloxacin. Cephalexin was added to prevent cell division (see Fig. S5 for CIP-only results).
888   (B) Distribution of cell lengths after 1 h of CIP exposure (green = experiment, red =
889   simulation). Cells shorter than 7 μm are excluded from the analysis. The best-fit for the cell
890   length distribution for a CIP concentration of 50 ng/ml has $\alpha = 1.62$ h^{-1}, $\sigma(\alpha) = 0.07$ h^{-1}. Only
891   the distribution for 50 ng/ml CIP differs from the CIP-free distribution (Kolmogorov-Smirnov *p*-
892   value = $2.5 \cdot 10^{-15} < 0.05$). (C) Distribution of DNA in cells of different lengths. Cells are
893   ordered by length from shortest to longest along the *x*-axis. Pseudo - colour is DAPI
894   fluorescence measured at different positions along cell midline (*y*-axis, scale bar on the right).
895   Separate chromosomes (lighter areas pointed by red arrows) are clearly visible in CIP-
896   untreated cells. The longest cells (~24 μm) have ~16 chromosomes. For 50 ng/ml CIP,
897   chromosomes fail to separate (a single fluorescent region at cell's midpoint).

898

899   **Figure 6. Simulations accurately predict the rate of DNA synthesis after ciprofloxacin**
900   **exposure.** (A) Simulated total DNA versus time (average of 1000 simulation runs). CIP is
901   added at time $t = 100$ min. Different colors correspond to different gyrase binding rates k_+
902   (different CIP concentrations). We used the best-fit parameters from Fig. 3. (B) Comparison

903 of the predicted (no additional fitting) and experimentally measured total DNA per cell (DAPI
904 staining) after 1 h of CIP exposure. Errors are SEM (350 cells on average per point).
905
906 **Figure 7. DNA-repair deficient cells ($\Delta recA$) fail to separate chromosomes and are**
907 **highly susceptible to ciprofloxacin.** (A) Phase contrast microscopy images overlaid with
908 fluorescent DAPI stained DNA images. All cells were treated with 8 μg/ml of cephalexin to
909 prevent cell division. Many $\Delta recA$ cells fail to form separate chromosomes. WT from Fig. 5A is
910 reproduced here for comparison. (B) The cell-length distributions for $\Delta recA$ and WT after 1h
911 of exposure to CIP do not differ even for a CIP concentration that inhibits the growth of $\Delta recA$
912 at the population level. (C) The model reproduces the experimental growth inhibition curve for
913 $\Delta recA$. Parameters $p_{kill0} = (0.0033$ +/- $0.0002)$ min^{-1}, $p_{kill} = (0.0042$ +/- $0.0001)$ min^{-1} and $q =$
914 0.03 ml ng^{-1} min^{-1}. Errors are SEM.
915
916 **Figure 8. Dynamic response of DNA-repair deficient cells ($\Delta recA\Delta fimA$) to a step-up of**
917 **CIP in the turbidostat.** (A) Growth rate vs time for $\Delta recA\Delta fimA$. Ciprofloxacin was added at 0
918 h. T_{ss} is the time to the new steady-state growth rate ($c <$ MIC) or no growth ($c >$ MIC)
919 following the addition of CIP. (B) Predicted T_{ss} closely matches the experimental results.
920
921
922 ## Supplementary figures captions
923
924 **Figure S1. Growth rate measurements.** (A) Background-corrected optical density OD$_{600nm}$
925 vs time, measured in a plate reader for two initial population sizes (inocula) of N_0 and $N_0/10$
926 cells. The time delay (ΔT, red double arrow) is related to the growth rate via Eq. (1). (Inset)
927 Microplate layout: columns = different concentrations, rows = different initial population sizes.
928 (B) Growth-inhibition curve for ciprofloxacin-treated cells (MG1655). The minimum inhibitory
929 concentration (MIC) is ~20 ng/ml. Our time-shift method gives similar results to that of the
930 standard exponential fitting method but it is more accurate (smaller error bars). Error bars are
931 SEM. (C) Schematic drawing of the turbidostat. While only one bacterial culture is shown, the
932 complete setup has four units that can be controlled independently. The pumps are syringe
933 pumps (shared between the units), and computer-controlled valves control the flow to/from a
934 particular unit. (D) Example data (OD versus time) from a single turbidostat experiment. The
935 red line marks the time at which CIP was first added to the culture.
936
937 **Figure S2. Number of poisoned gyrases predicted by the model.** (A) For the best-fit
938 parameters $p_{kill} = 7 \cdot 10^{-5}$ min^{-1} and $\tau_{gyr} = 25$ min (Fig. 4), we calculated the average number of
939 poisoned gyrases per chromosome length $\underline{N}_{gyr}$ (orange points, 1000 replicate simulations).
940 (B) Same as in (A) but using the best-fit parameters for $\Delta recA$ cells (Fig. 7). According to the
941 model, a single poisoned gyrase per chromosome is enough to cause complete DNA
942 inhibition in cells lacking the recombination repair mechanism.
943
944 **Figure S3**. **Simulation of the model when killing occurs only for the daughter**
945 **chromosomes leaving the mother chromosomes intact.** The predicted steep decrease in
946 growth rate with CIP concentration is in sharp contrast to the quadratic shape of the
947 experimental growth-inhibition curve from Fig. 1A. As in Fig. 2, we assume that the rate k_+ is
948 proportional to the extracellular CIP concentration c.
949
950 **Figure S4**. **Alternative predictions for the time to steady state (Fig. 4B) for model**
951 **parameters deviating slightly from the best-fit parameters from Fig. 3C.** The upper-left
952 panel shows the same goodness-of-fit plot as Fig. 3C. Best-fit parameters are marked "x".
953 Points marked -2,-1,…,5 correspond to different parameter sets selected from the blue-teal
954 area of the goodness-of-fit plot for which the fit to the long-term data (Fig. 3D) is only slightly
955 worse that for "x".
956
957 **Figure S5. Cell length distributions for ciprofloxacin- and cephalexin- treated cells.** The
958 histograms show the cell length distributions before (green) and after antibiotic treatment
959 (red). **(**A) When exposed to ciprofloxacin, cells form filaments that may bud from their end
960 (14). Ciprofloxacin decreases the frequency of cell division; almost no cells bud or divide
961 during first hour at the highest concentration used (15 ng/ml). (B) Cells exposed to 8 μg/ml ($\approx$

19

962　MIC) of cephalexin do not divide. The cell length distribution at t = 1 h is very similar to the
963　distribution for 15 ng/ml of ciprofloxacin from panel A.
964
965　**Figure S6. Chromosome organization in WT vs Δ*recA*.** (A) Cells are ordered by length
966　from shortest to longest along the *x*-axis, and fluorescence intensity (DAPI staining) is plotted
967　along the *y*-axis. Isolated chromosomes (up to 4 in longest cells) can be identified in WT cells
968　(red arrows), while Δ*recA* cells have much less organized chromosomes than WT cells. (B)
969　The cell-length and cell-width distributions are very similar for both strains.
970
971　**Figure S7. A model with DNA damage occurring at the stalled forks also reproduces**
972　**the experimental growth-inhibition curve.** (A) Schematic representation of the modified
973　model, (see Fig. 2). (B) Stalled replication forks cause irreversible DNA breaks with rate p_{fkill},
974　leading to "death" of the chromosome. (C) Goodness-of-fit for a range of model parameters.
975　The best-fit parameters p_{kill} = 2$\cdot$10^{-5} min^{-1}, τ_{gyr} = 30 min, and q = 0.04 ml ng^{-1} min^{-1} are marked
976　with a white cross. (D) Experimental growth-inhibition curve (green) agrees well with the
977　simulated curve (orange) for best-fit parameters. Errors are SEM (four replicates).
978
979　**Figure S8. Growth-inhibition curve for Δ*recA*Δ*fimA*.** The model reproduces the
980　experimental growth-inhibition curve for Δ*recA*Δ*fimA.* MIC for this strain is approximately 4
981　ng/ml. Parameters p_{kill0} = (0.0036 +/- 0.0002) min^{-1}, p_{kill} = (0.0011 +/- 0.0001) min^{-1} and q =
982　0.068 ml ng^{-1} min^{-1}. Errors are SEM.
983
984　**Figure S9. Colony size distribution for the WT (MG1655) and Δ*recA*.** (A) Example
985　colonies of WT and Δ*recA* cells imaged after 1 h and 2 h of growth starting from isolated cells
986　deposited on LB-agarose pads. Scale bar = 3 μm. (B) Distribution of colony sizes. Colonies of
987　Δ*recA* are smaller on average even though cells elongate with the same rate (Fig. 7B). By
988　comparing the same colony at t = 1 and 2 h we concluded that some cells did not grow.
989
990　**Figure S10. Alternative model (saturation of the repair mechanism).** Experimental growth
991　inhibition curve (green points) fitted with the model (orange line). Here b/b_0 is the ratio of the
992　growth rate at given CIP concentration c to the growth rate at $c = 0$. Although the inhibition
993　curve is correctly reproduced, the model fails to reproduce the dynamic response as
994　explained in the main text.
995
996　**Figure S11. A Hill curve fitted to the experimental growth inhibition curve.** The fitted Hill
997　exponent is 4.4 ± 0.5.
998
999　**Figure S12. The SOS response is much faster than the experimentally observed growth**
1000　**response to CIP.** The plot shows the time it takes the concentration of LexA (a protein
1001　involved in the SOS response) to reach its new steady state (less than 10% difference to the
1002　steady-state value) as a function of the rate with which DSBs are created. Based on model
1003　from (42) adapted as described in the main text.
1004
1005

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1238

A

oriC

ter

B DNA replication

oriC

oriC

ter

C

Death

p_{kill}

τ_{gyr}
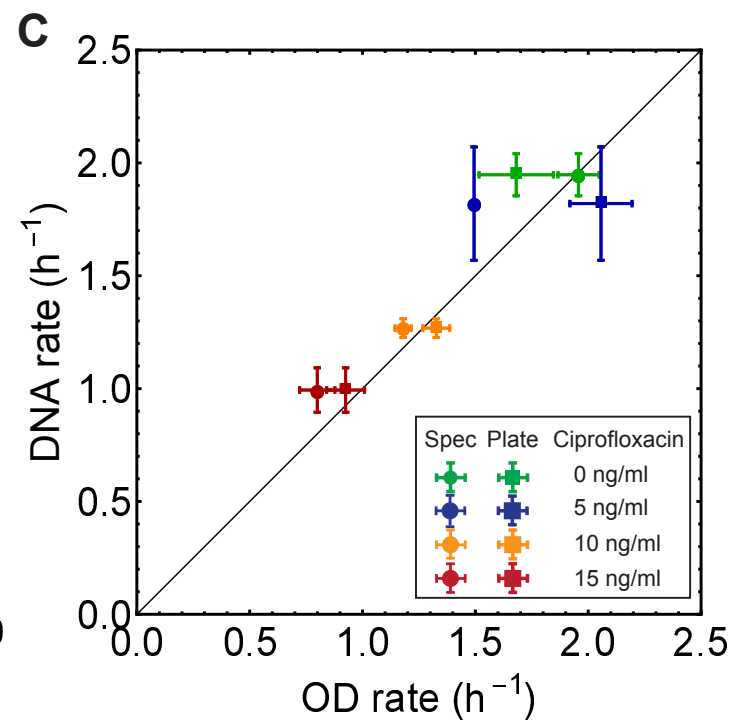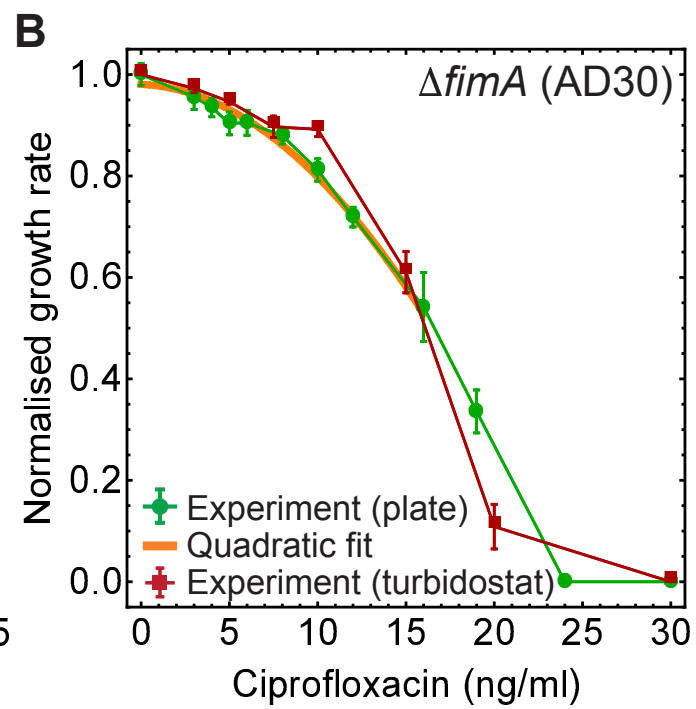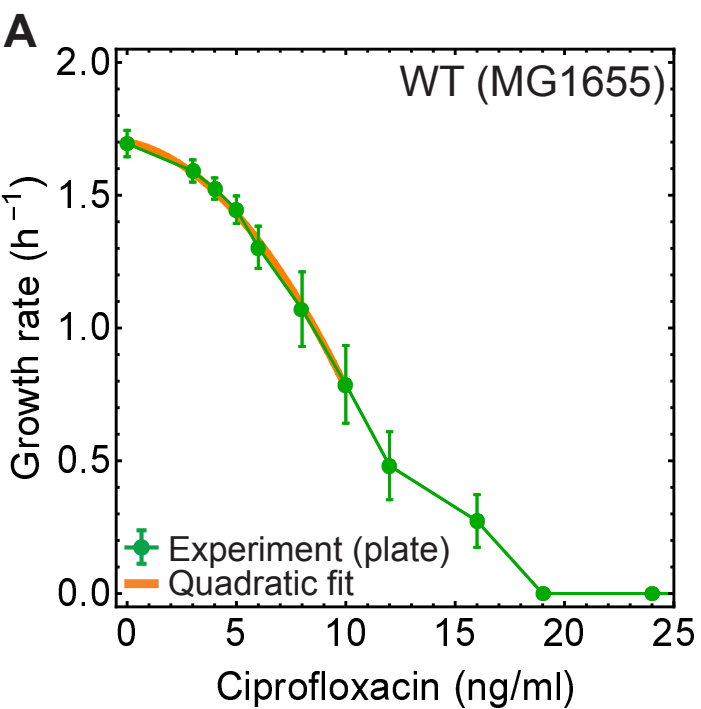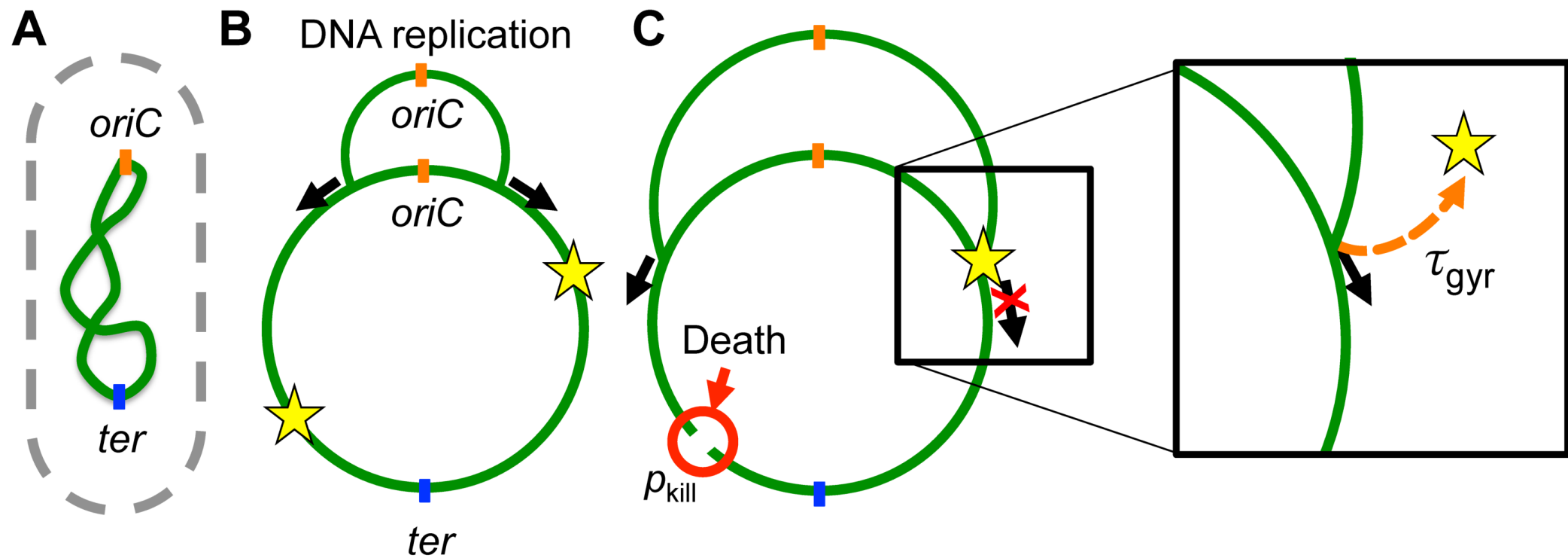
⭐ Gyrase bound ciprofloxacin (poisoned gyrase)

τ_{fork} - new fork initiation time

p_{kill} - probability rate for poisoned gyrase to irreversible break DNA

τ_{gyr} - poisoned gyrase turnover time

A

$p_{kill} = 5 \cdot 10^{-5}$ min^{-1}
$\tau_{gyr} = 15$ min, $\tau_{for} = (24.5 +/- 5)$ min

$k_+ = 0.1$ min^{-1}
$k_+ = 0.6$ min^{-1}

B

p_{kill} (min^{-1})

C

$$\text{Error} = \frac{1}{N}\sum_i^N \frac{(\text{GIC}^{exp}(i) - \text{GIC}^{sim}(i))^2}{\sigma^2(\text{GIC}^{exp}(i))}$$

D

Experiment
Simulation

A $\Delta fimA$

Ciprofloxacin (ng/ml)
5 10 15 20 30 40 50 100

T_{ss}

Growth rate (h^{-1})

Time (h)

B

● Experiment
— Simulation

T_{ss} (h)

Ciprofloxacin (ng/ml)

A   Cephalexin (8 μg/ml)

Ciprofloxacin (0 ng/ml)   Ciprofloxacin (5 ng/ml)   Ciprofloxacin (10 ng/ml)   Ciprofloxacin (15 ng/ml)   Ciprofloxacin (50 ng/ml)

DNA (DAPI)   10 μm

B

Experiment ($n = 437$)
Simulation ($n = 642 \cdot 10^3$)

($n = 245$)   ($n = 344$)   ($n = 400$)   ($n = 297$)

Probability — Cell length (μm)

C

DAPI

Distance from middle (μm)

Rank in cell length — 1 ... 313 | 1 ... 160 | 1 ... 226 | 1 ... 316 | 1 ... 262

A

k_+ (min^{-1})

Simulations

Total DNA

Time (min)

B

Experiment
Simulation

Relative DNA amount

Ciprofloxacin (ng/ml)

A

Cephalexin (8 µg/ml)

WT	ΔrecA
Ciprofloxacin (0 ng/ml)	Ciprofloxacin (0 ng/ml) Ciprofloxacin (5 ng/ml)

B

C
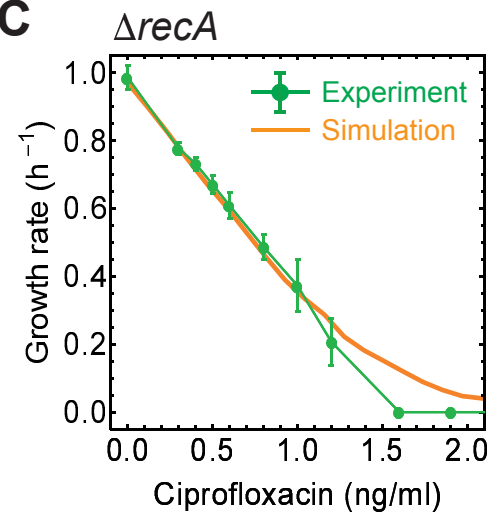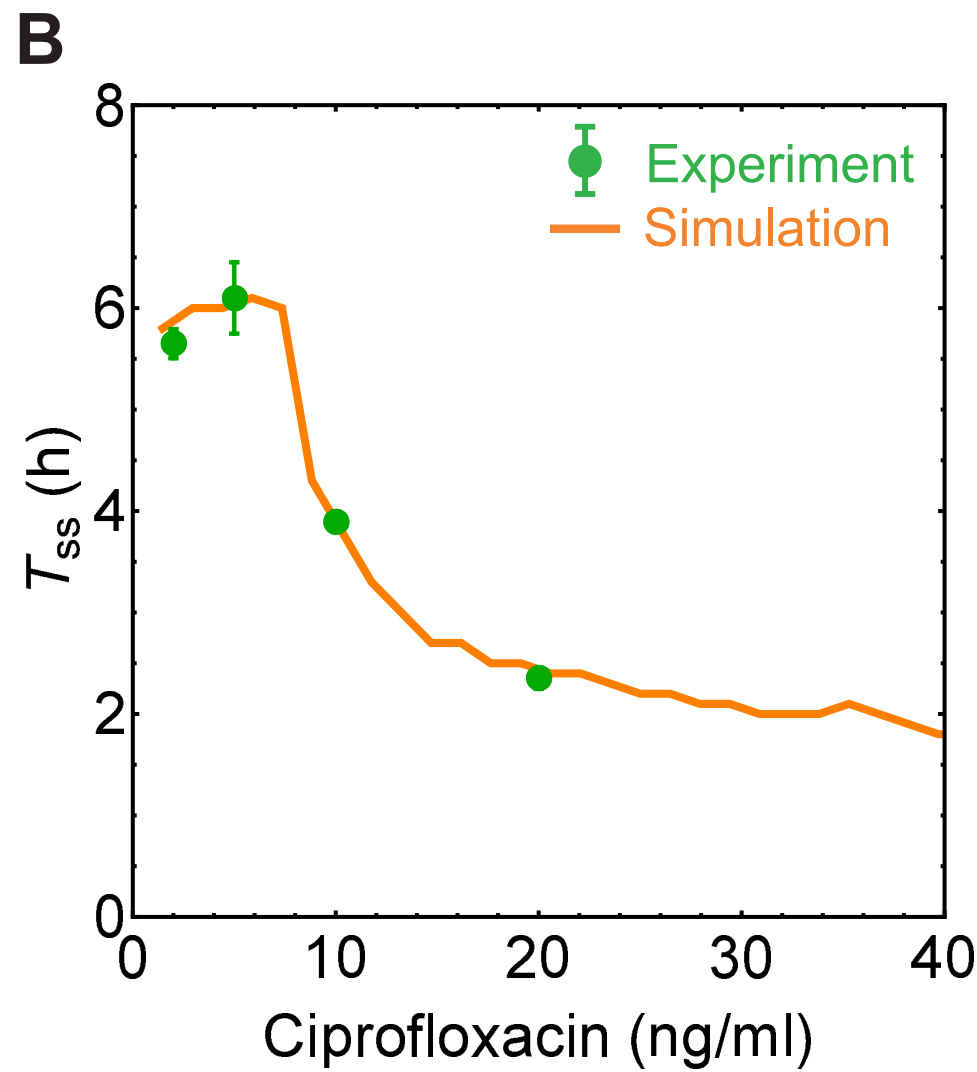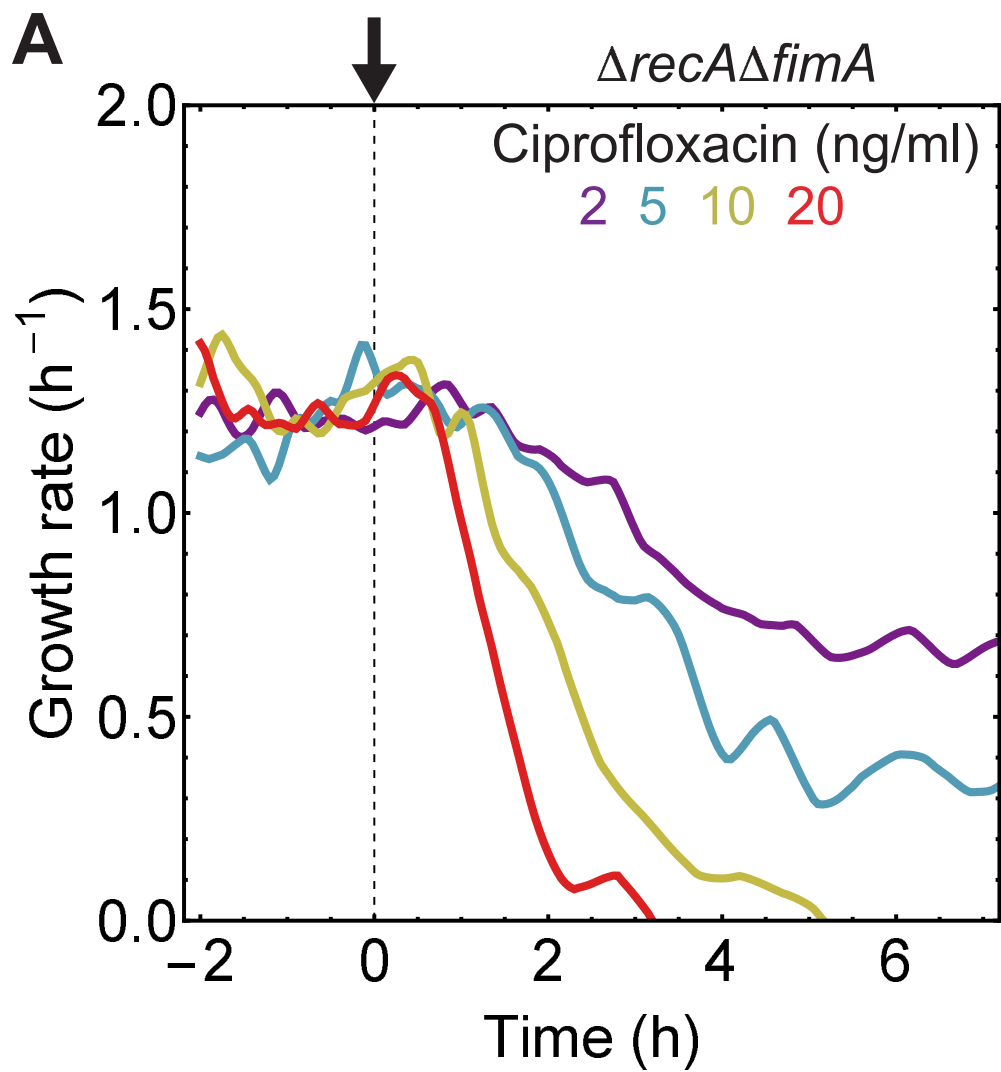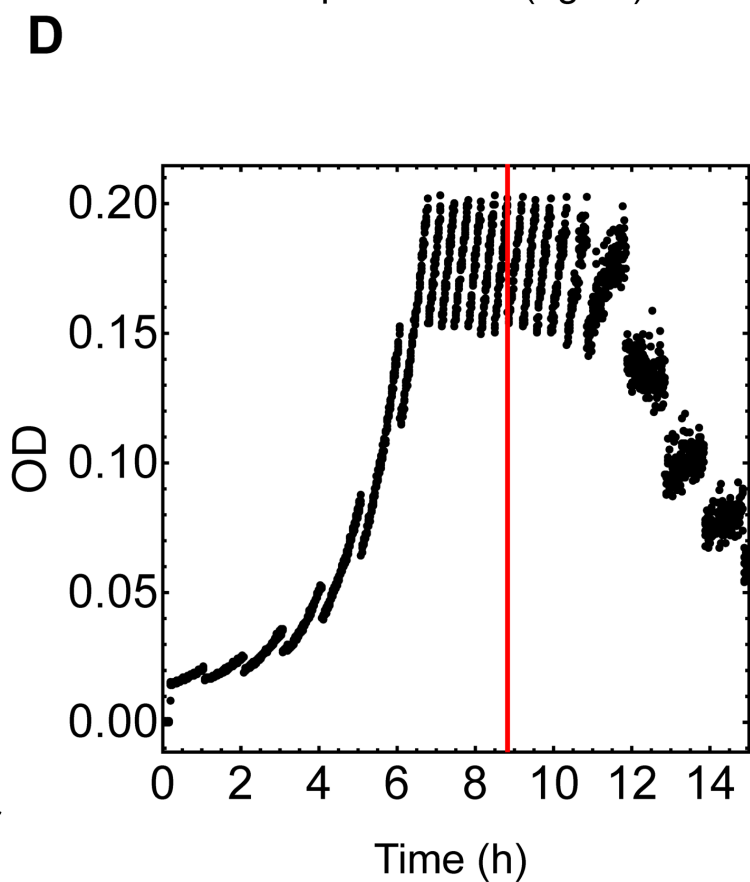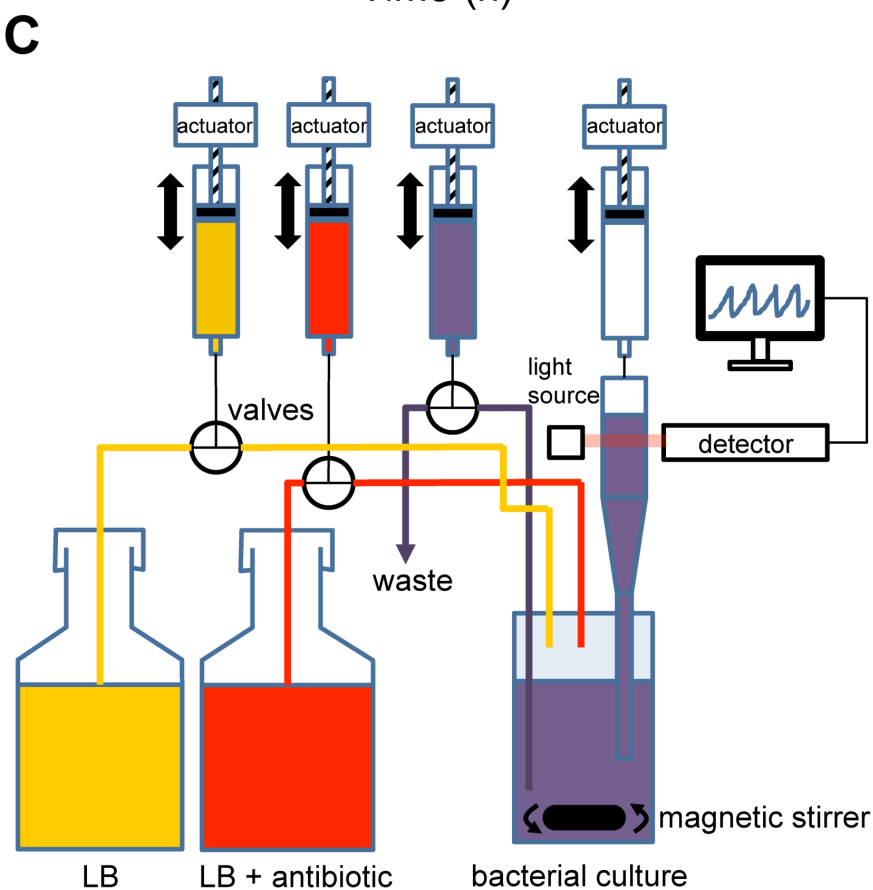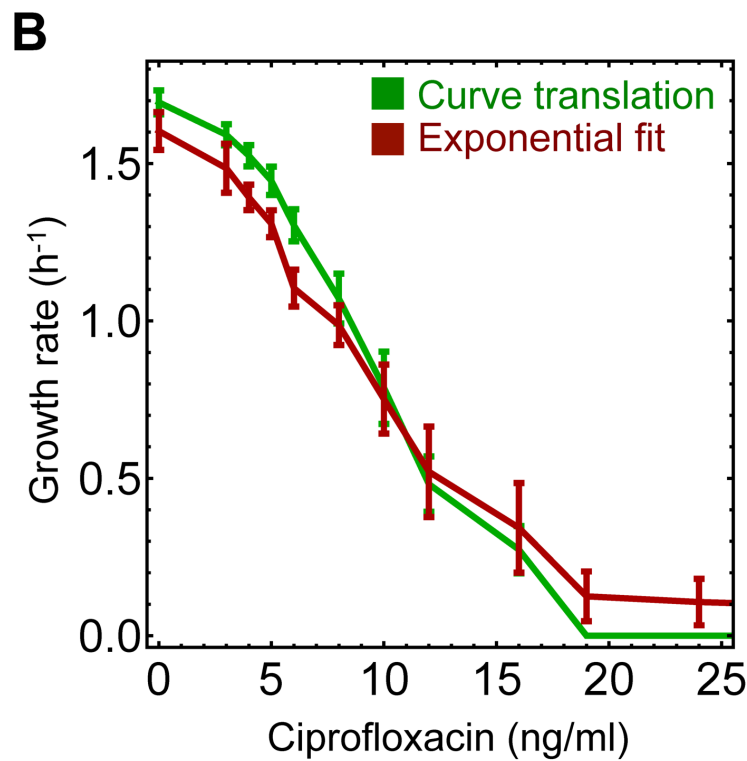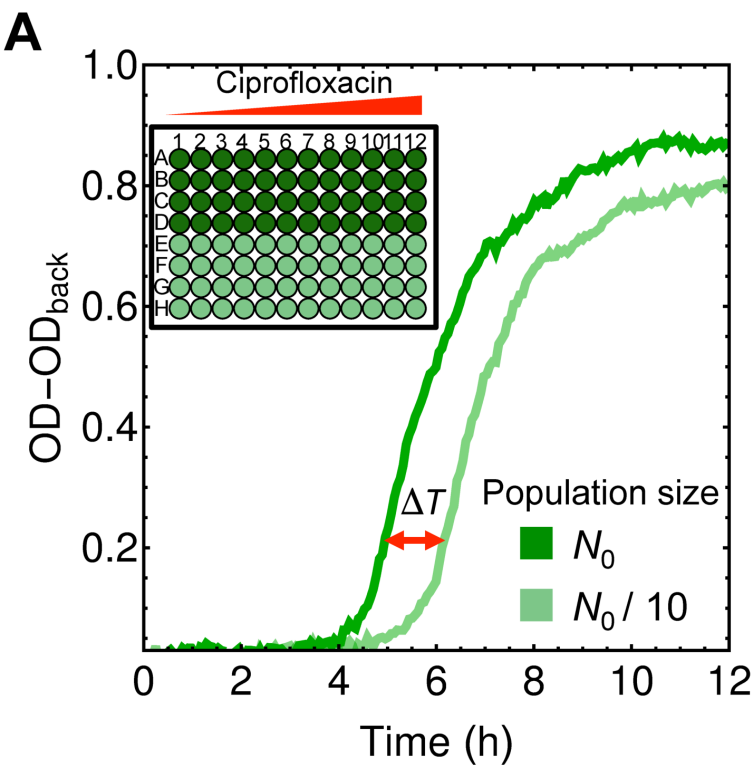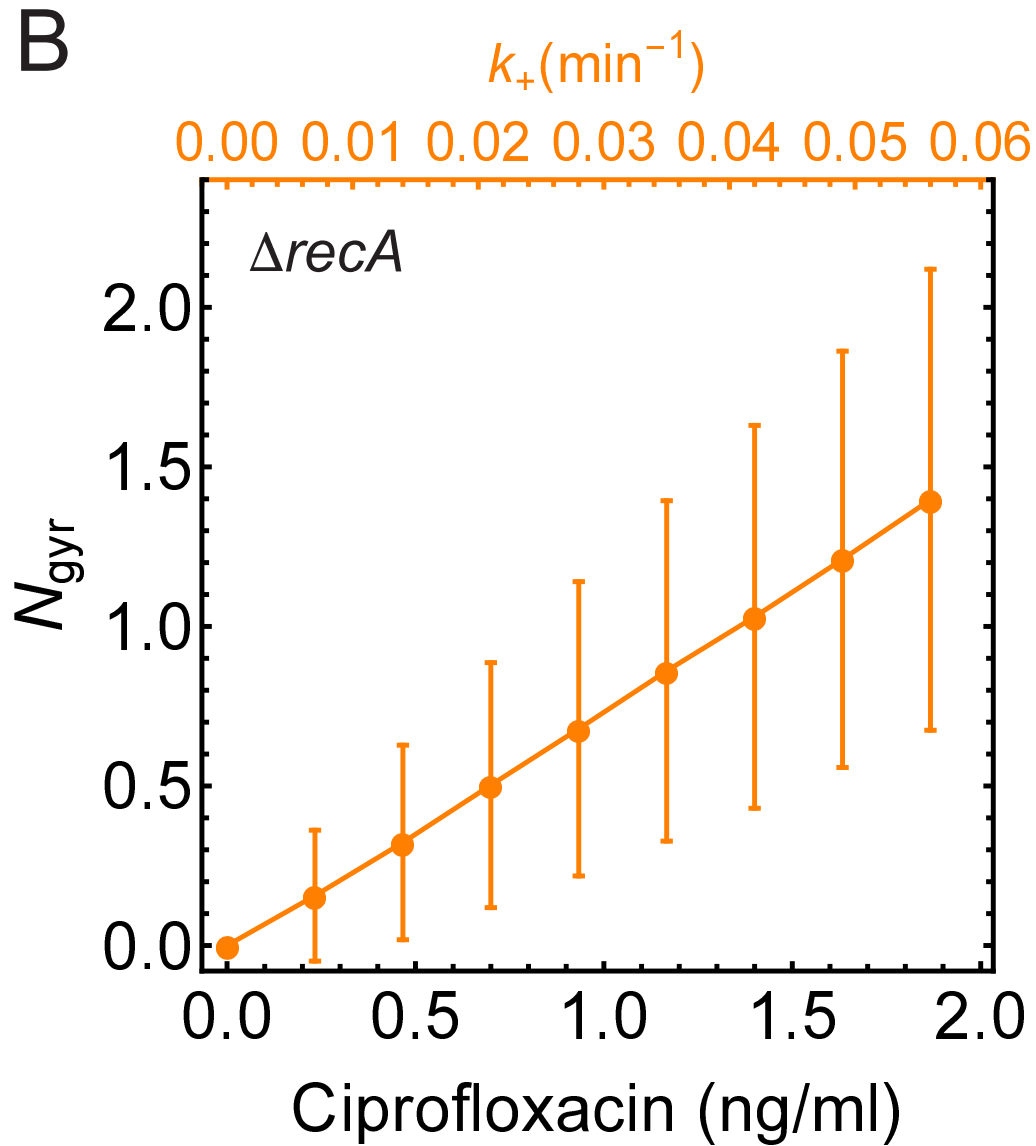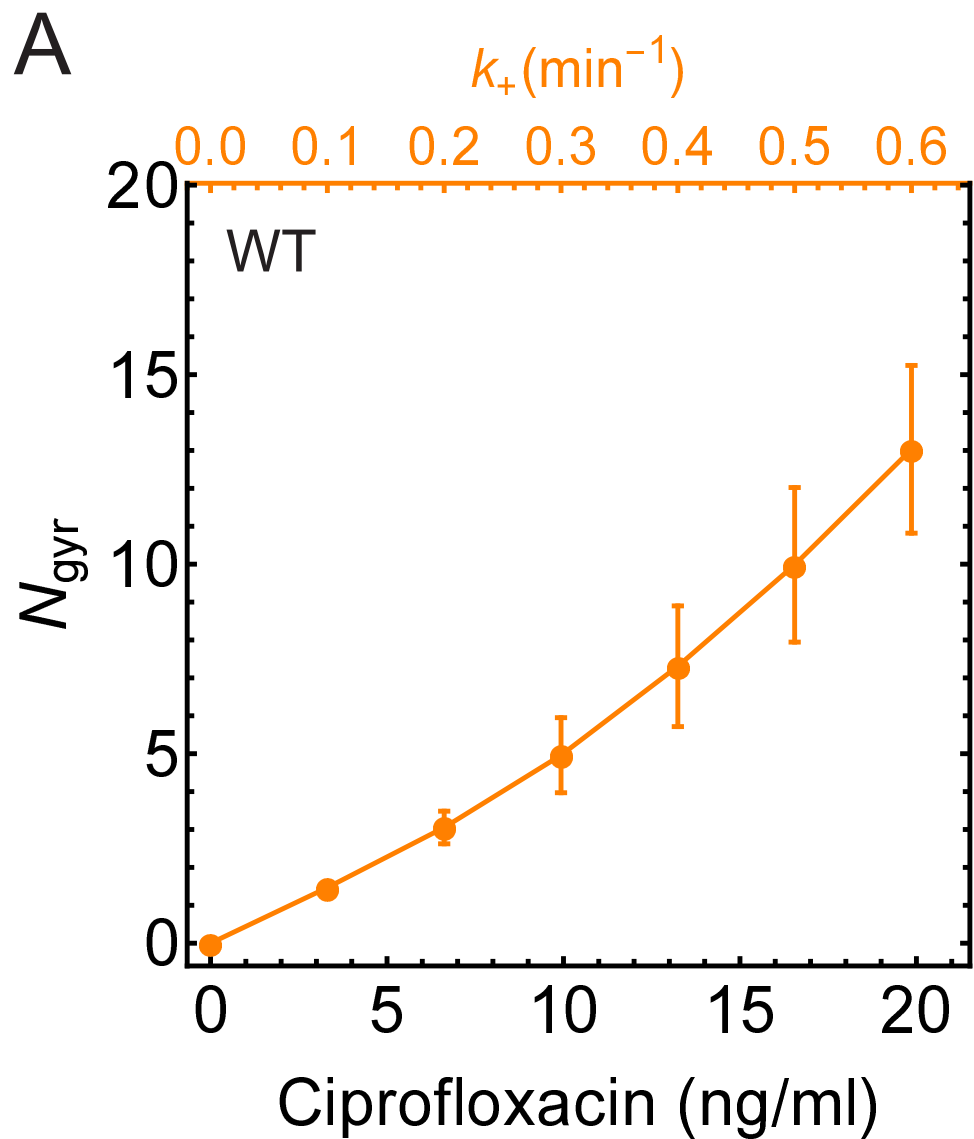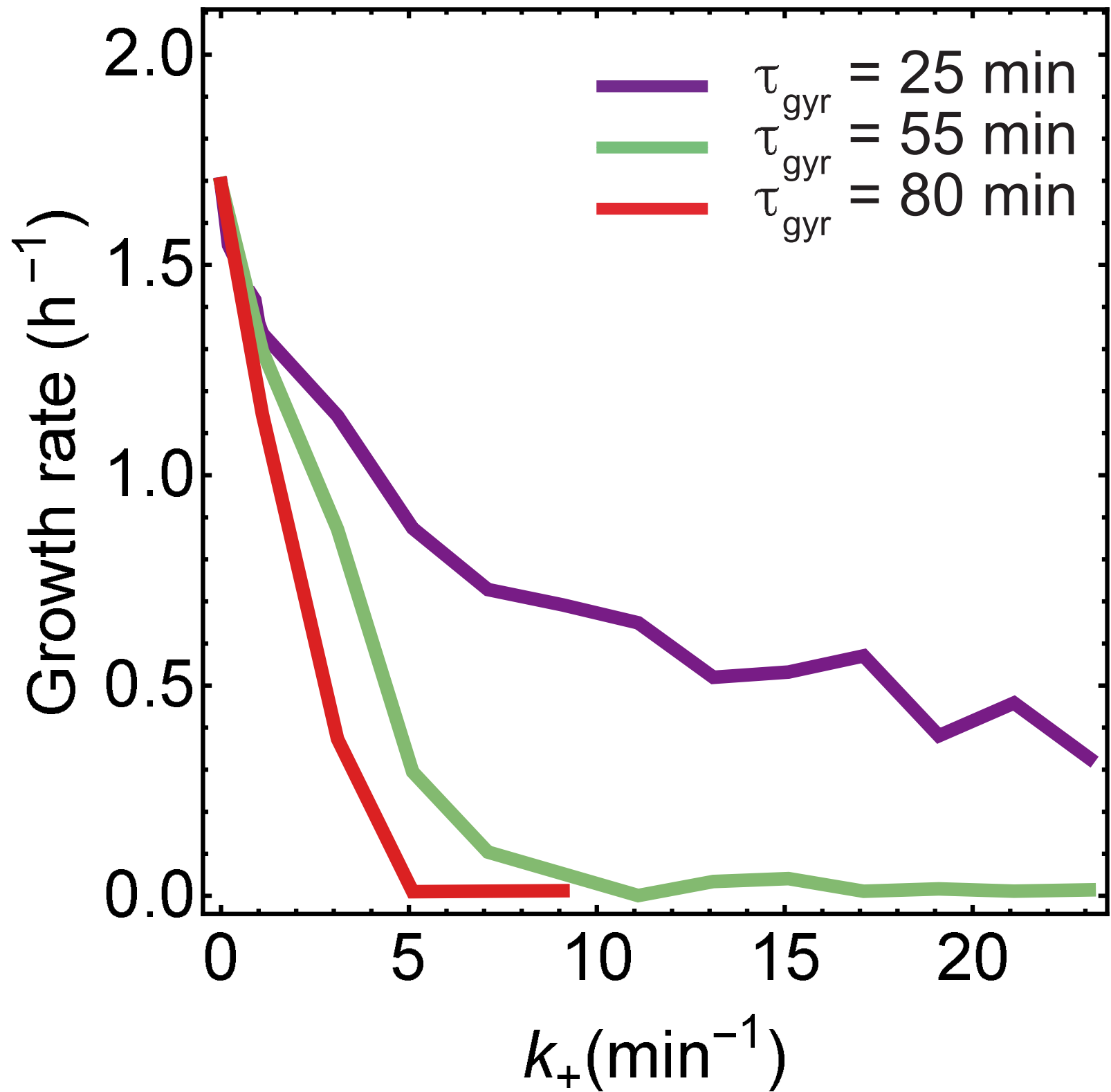
A
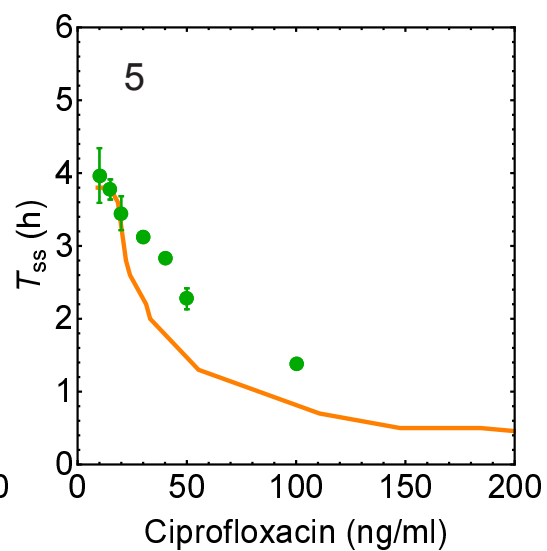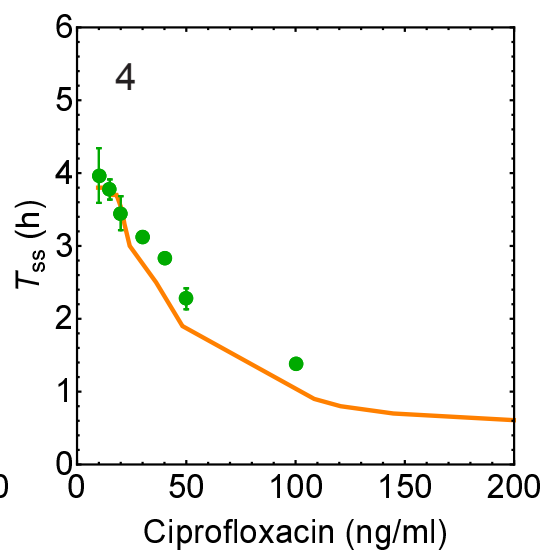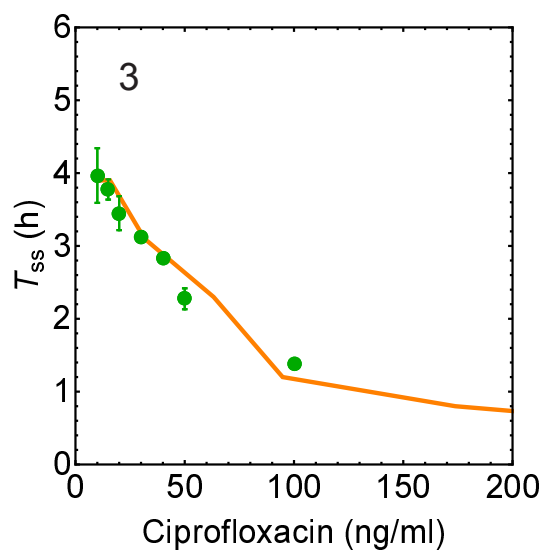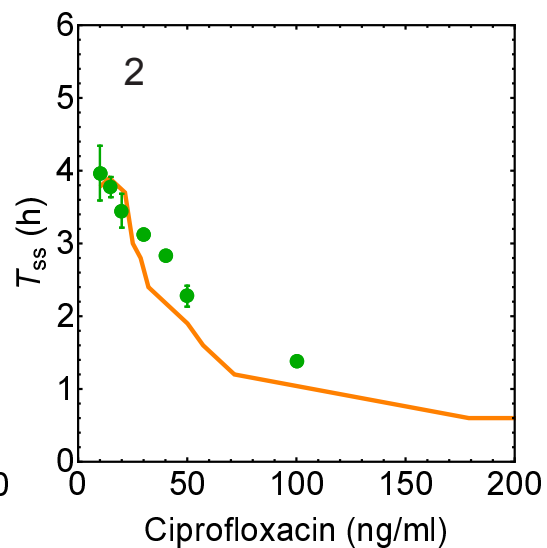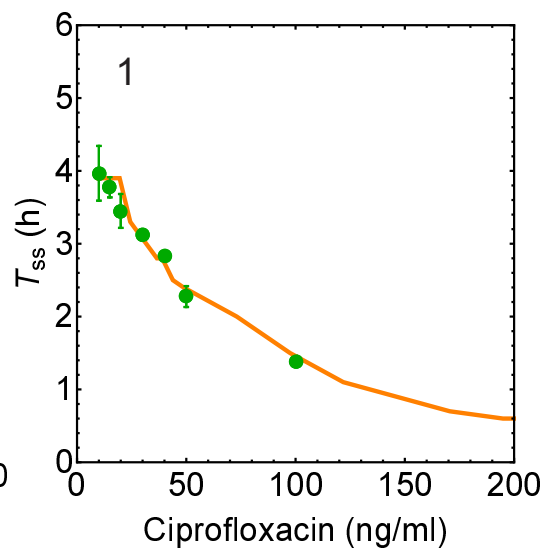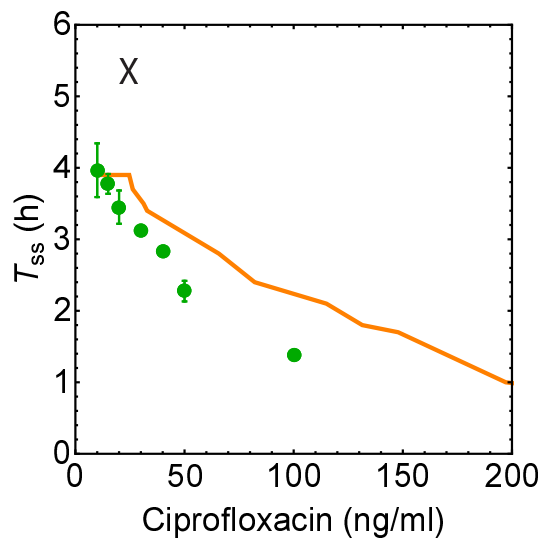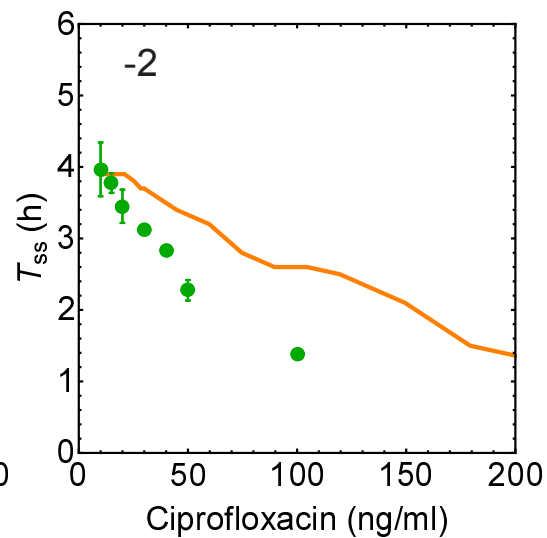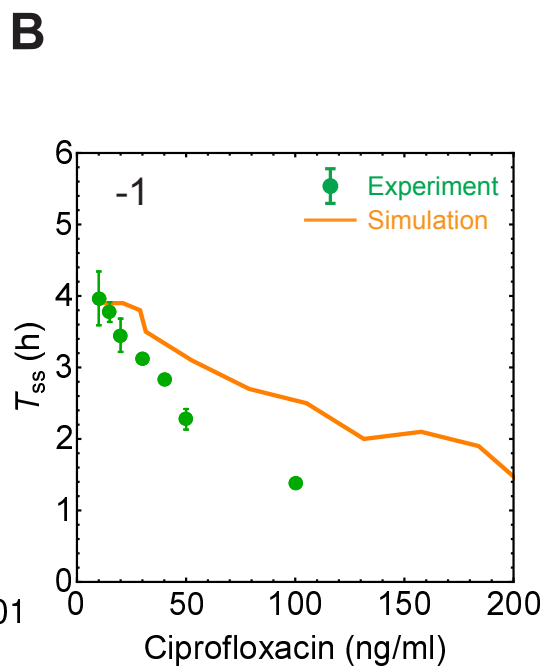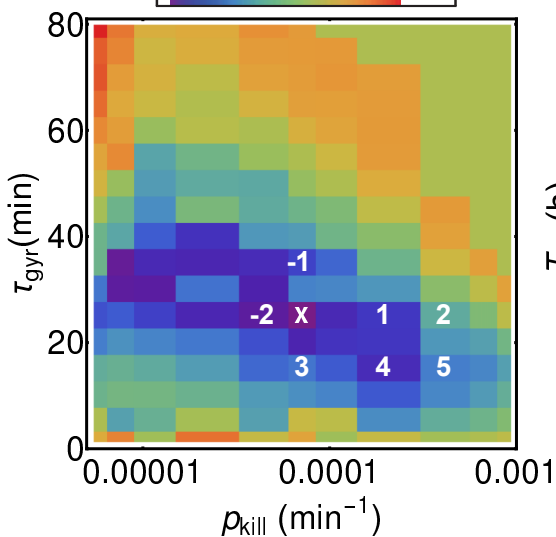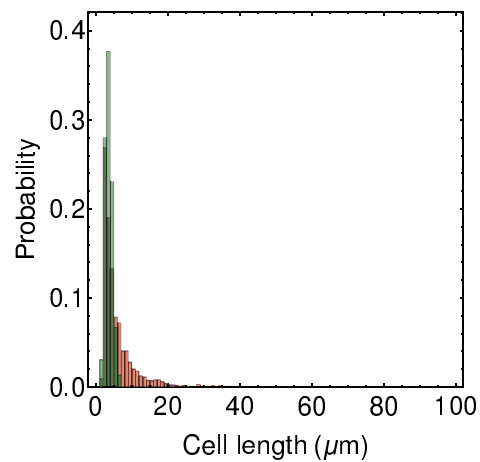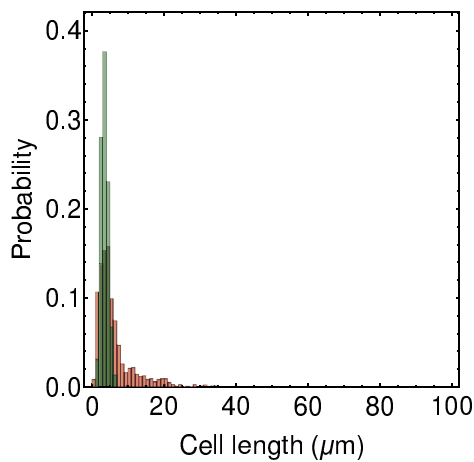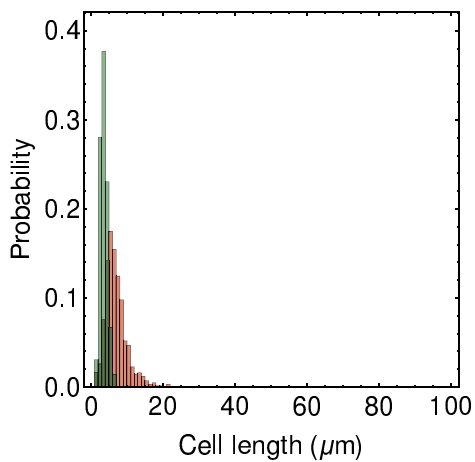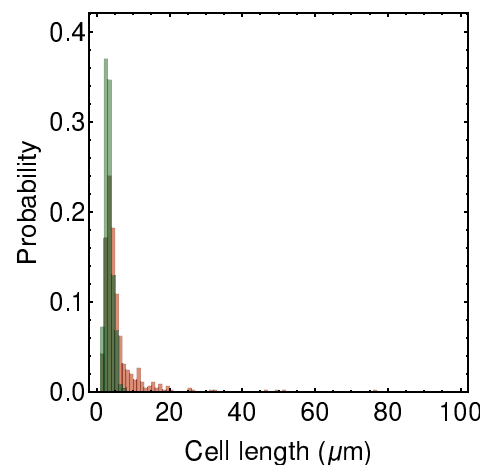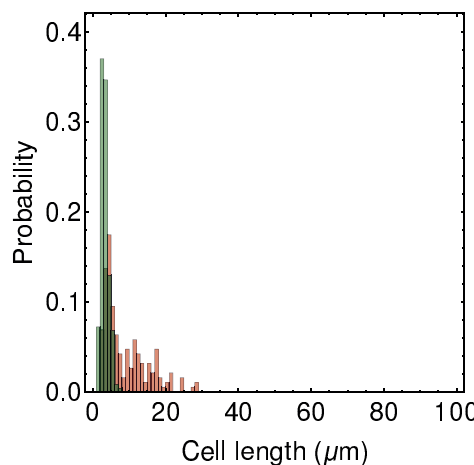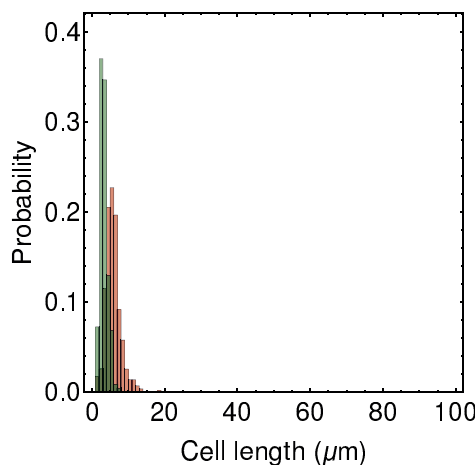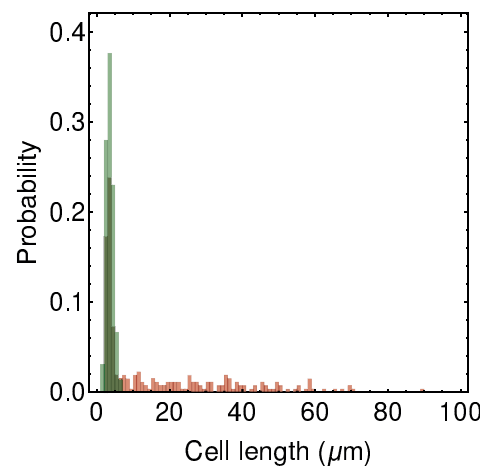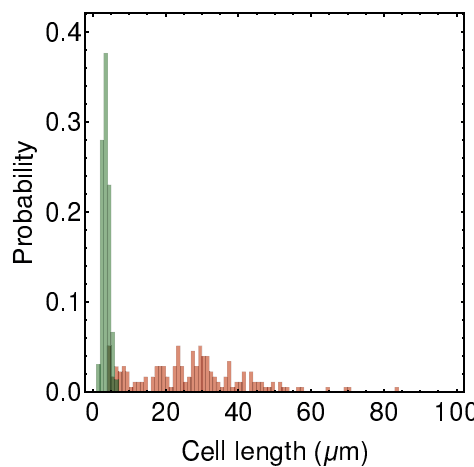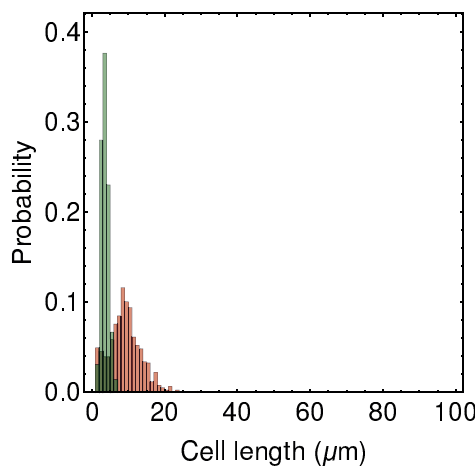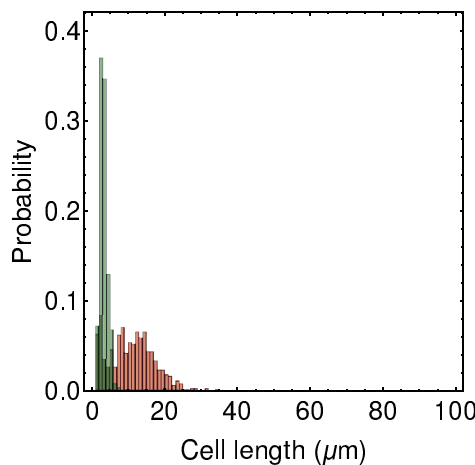
$\Delta recA\Delta fimA$

Ciprofloxacin (ng/ml)
2 5 10 20

Growth rate (h^{-1})

Time (h)

B

● Experiment
— Simulation

T_{ss} (h)

Ciprofloxacin (ng/ml)

A

Ciprofloxacin

ΔT

Population size
N_0
$N_0 / 10$

B

Curve translation
Exponential fit

C

actuator actuator actuator actuator

valves

light source

detector

waste

LB   LB + antibiotic   bacterial culture

magnetic stirrer

D

A

$$\text{Error} = \frac{1}{N} \sum_{i}^{N} \frac{(\text{GIC}^{\text{exp}}(i) - \text{GIC}^{\text{sim}}(i))^2}{\sigma^2(\text{GIC}^{\text{exp}}(i))}$$
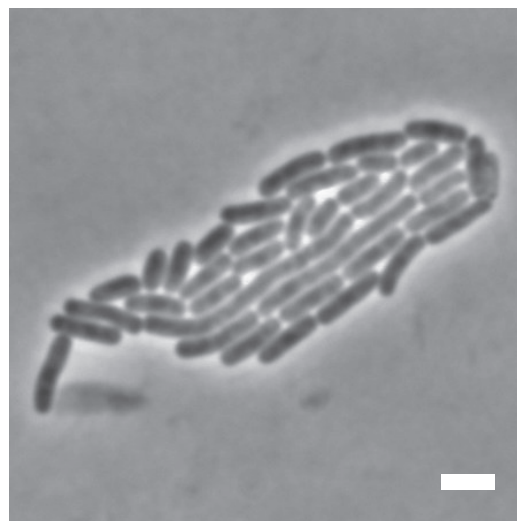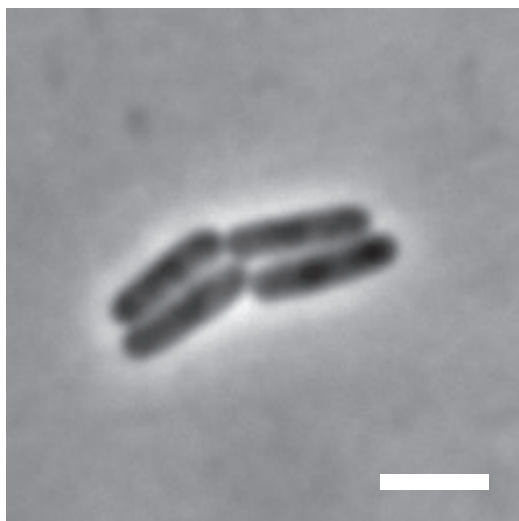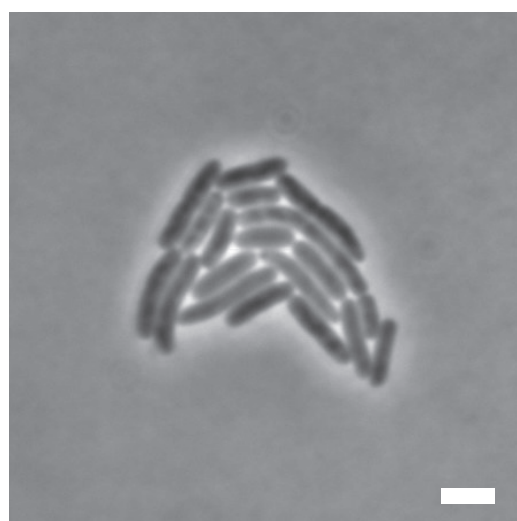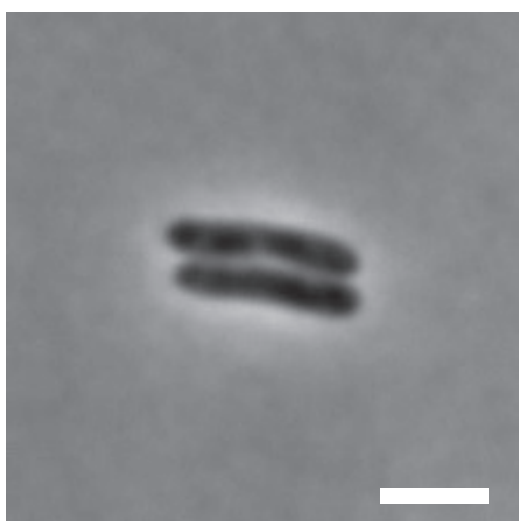
B

A

	1 h	2 h	3 h

Ciprofloxacin

5 ng/ml

10 ng/ml

15 ng/ml

B

Cephalexin

8 µg/ml

A

WT

$\Delta recA$

B

C Error = $\sum_i \frac{(GIC^{exp}(i) - GIC^{sim}(i))^2}{\sigma^2(GIC^{exp}(i))}$

A

Gyrase bound ciprofloxacin (poisoned gyrase)

τ_{gyr} - poisoned gyrase turnover time

B
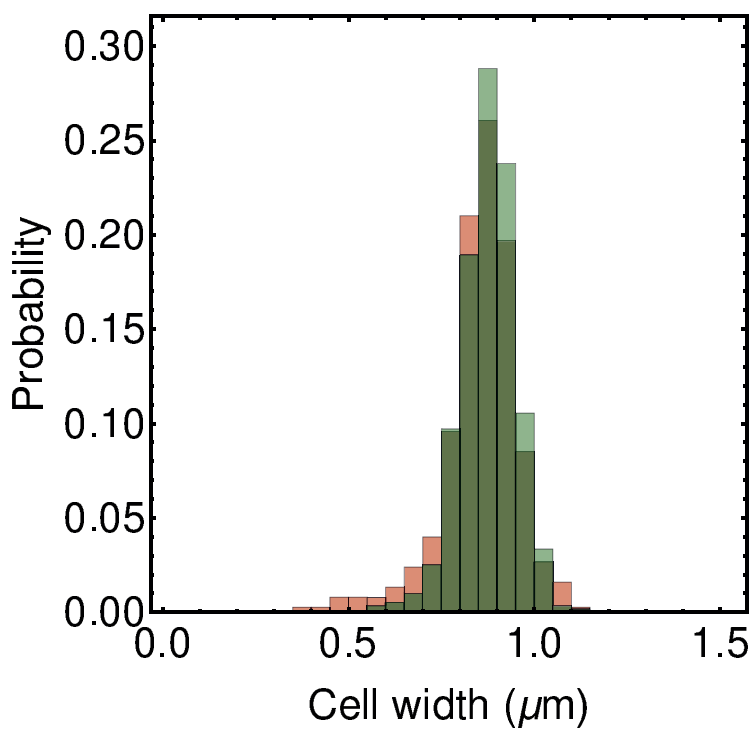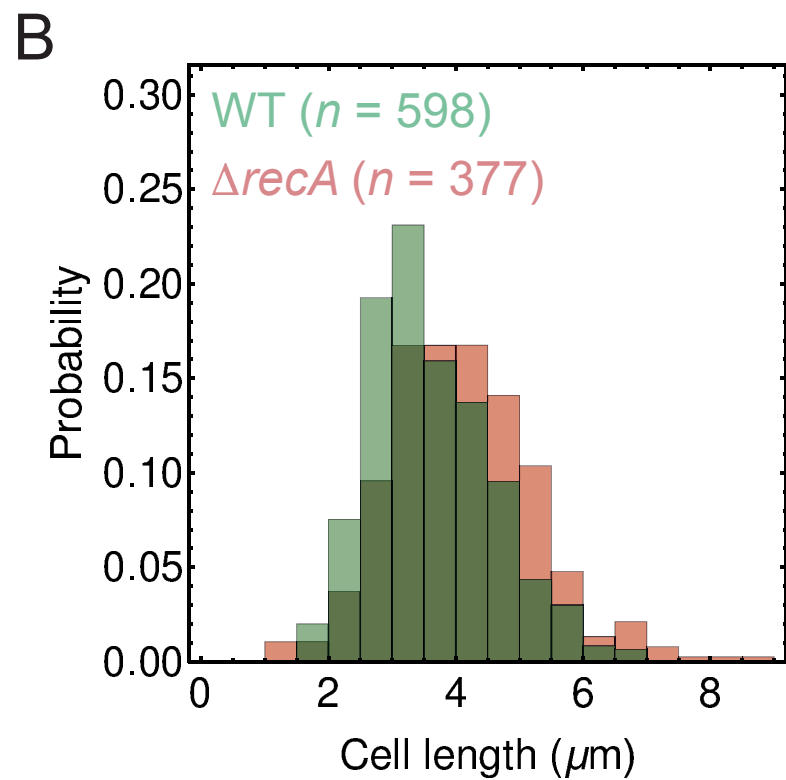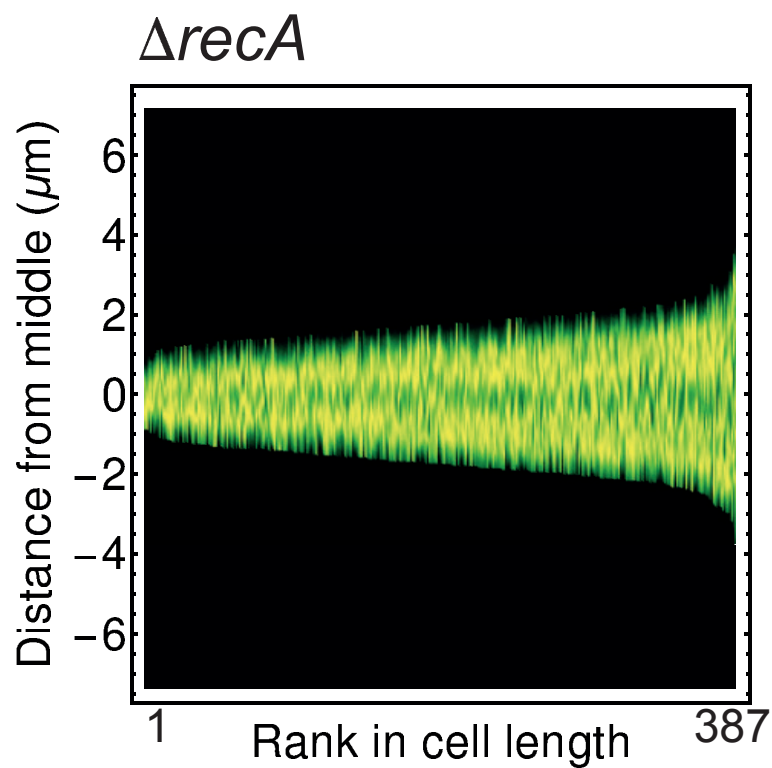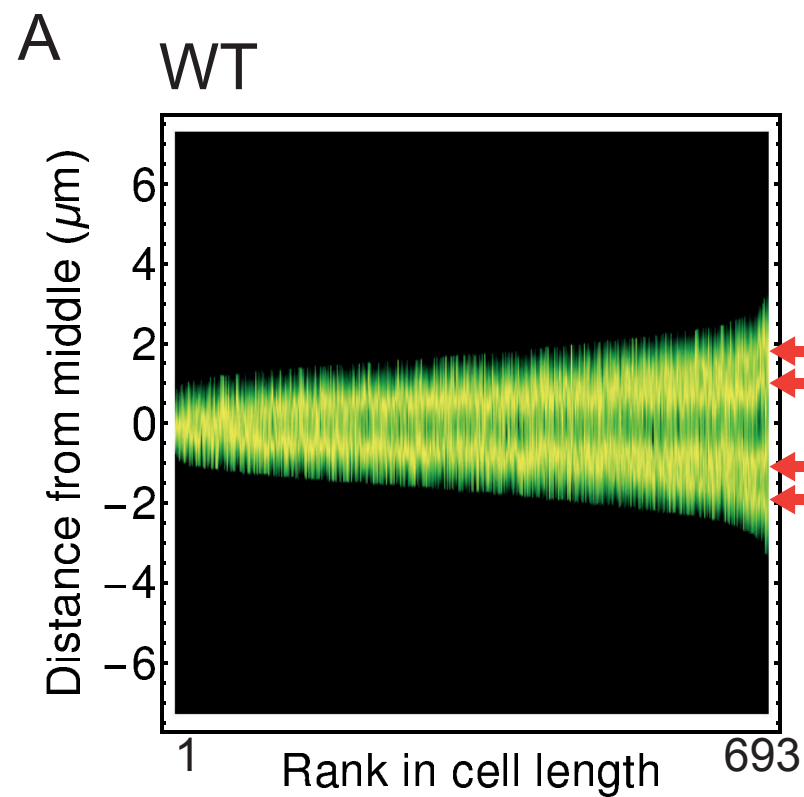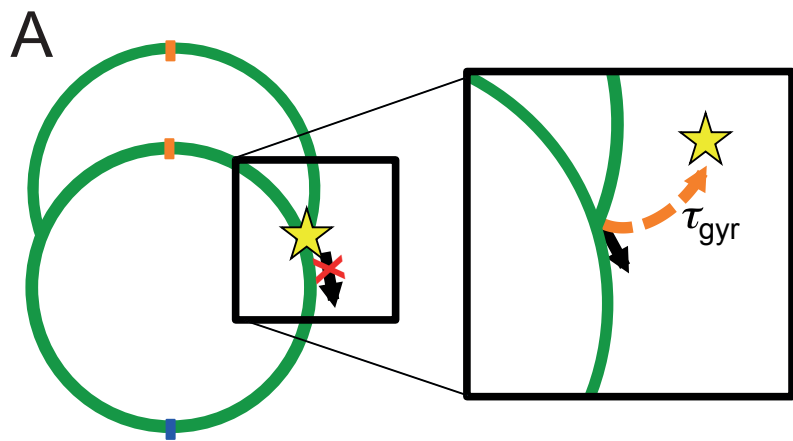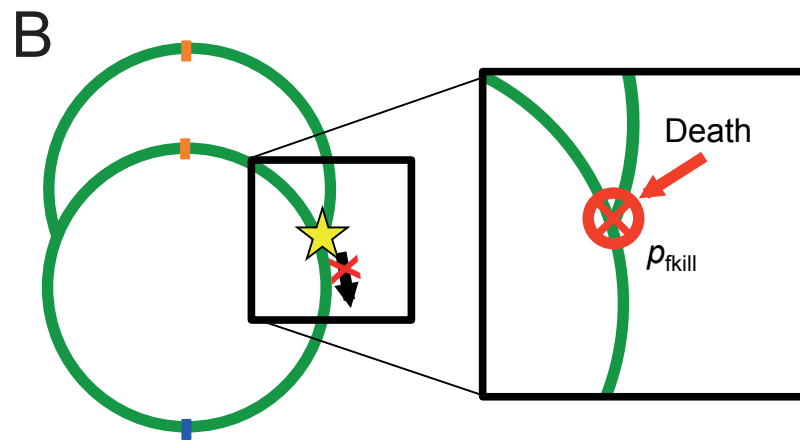
p_{fkill} - probability rate for replication fork to cause irreversible DNA break while stalling on poisoned gyrase

A

WT

$\Delta recA$

t = 1 h

t = 2 h

3 μm

B

t = 1 h

t = 2 h

WT (*n* = 45)
$\Delta recA$ (*n* = 55)

WT (*n* = 33)
$\Delta recA$ (*n* = 65)

Probability

Probability

Colony area (μm^2)

Colony area (μm^2)