



from short electron bunches has demonstrated its potential as a source of high power radiation in the sub-THz to THz range [11–14], and has also found applications for beam instrumentation purposes [15, 16] and spectroscopy. Observations of shadowing were performed by Naumenko [17],[18] measuring coherent radiation emitted at  $\lambda = 10 \text{ mm}$  by  $6.1 \text{ MeV}$  electron bunches. In that configuration, the predicted formation length was about  $0.45 \text{ m}$  long, and they observed a reduction of a factor 5 in radiation power for  $z$  ranging from  $22 \text{ cm}$  to  $2 \text{ cm}$ . This reduction was smaller than the value predicted by shadowing theory (i.e.  $> 10$ ) but still considered by the authors as an acceptable agreement, once taken into account experimental uncertainties.

In this letter we report on the study of shadowing effects occurring in the THz range between two sources of coherent radiation based on Coherent Diffraction Radiation (CDR) and Coherent Transition Radiation (CTR). The experiments were performed at the Cern Linear Electron Accelerator for Research (CLEAR) using relativistic short electron bunches. We then present a new general formalism that can model the interference mechanism between two consecutive coherent sources and accurately simulate shadowing effects in diffractive conditions. The CLEAR facility [19] delivers electron bunches

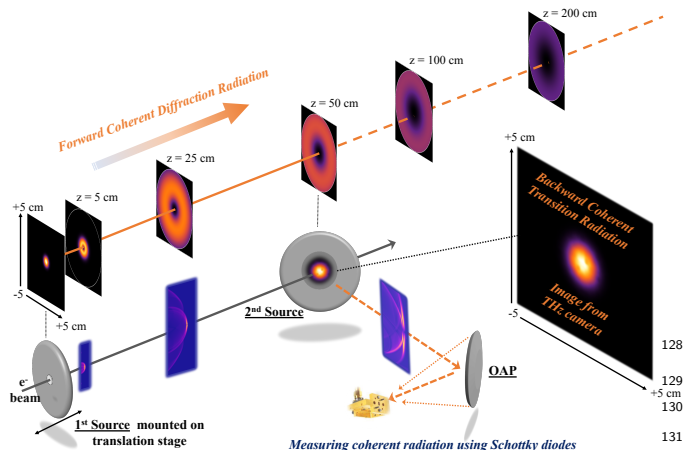


Figure 1. Experimental set-up at CLEAR : the electron beam  $e^-$  emits forward CTR/CDR from a first screen that interferes with backward CTR from a second screen. The resulting coherent radiation pulse is collected by an Off-Axis Parabolic (OAP) mirror that focuses it towards the detector.

with maximal beam energy of  $200 \text{ MeV}$ . A  $1 \text{ m}$ -long in-air testing area has been installed at the end of the beamline for the study of THz generation using coherent radiation mechanisms [16, 19]. The experimental set-up installed on CLEAR to study the shadowing effect of coherent radiation is composed of two consecutive sources emitting transition or diffraction radiation, as depicted in Fig. 1. A first screen placed perpendicular to the beam trajectory, produces forward coherent radiation. It is mounted on a remotely controlled translation stage allowing the precise adjustment of the distance be-

tween the two sources from  $5 \text{ cm}$  to  $45 \text{ cm}$ . Snapshots of the spatial distribution of the forward coherent radiation emitted from the first radiator are shown in Fig. 1 as an example. The resulting forward coherent radiation propagates co-linearly with the beam towards the second source. The latter is a screen tilted at  $45^\circ$  that emits backward CTR and reflects the forward radiation emitted from the first source. Both screens are made out of silicon,  $0.4 \text{ mm}$  thick, coated with a  $0.1 \text{ mm}$  thick aluminum layer and with an external radius of  $50 \text{ mm}$ . The corresponding radiation, whose front is figured as result of a 3D simulations using the VSim code [20], is collected by an Off-Axis Parabolic (OAP) mirror (focal length of  $15.4 \text{ cm}$ ), positioned  $20 \text{ cm}$  away from the second screen, focusing the radiation on the detection plane. The measurement system is based on waveguide band-pass-filtered Schottky diodes from Millitech. Two ini-

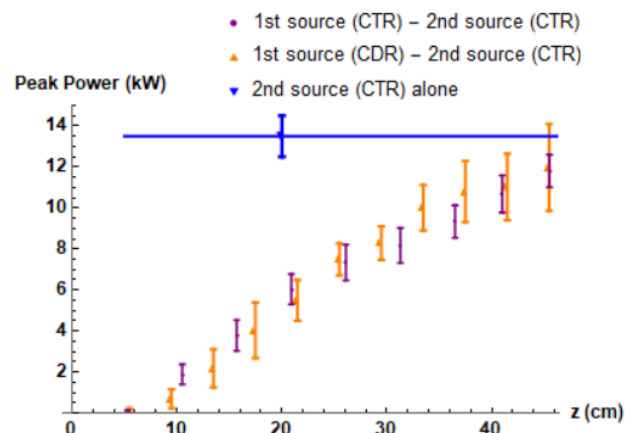
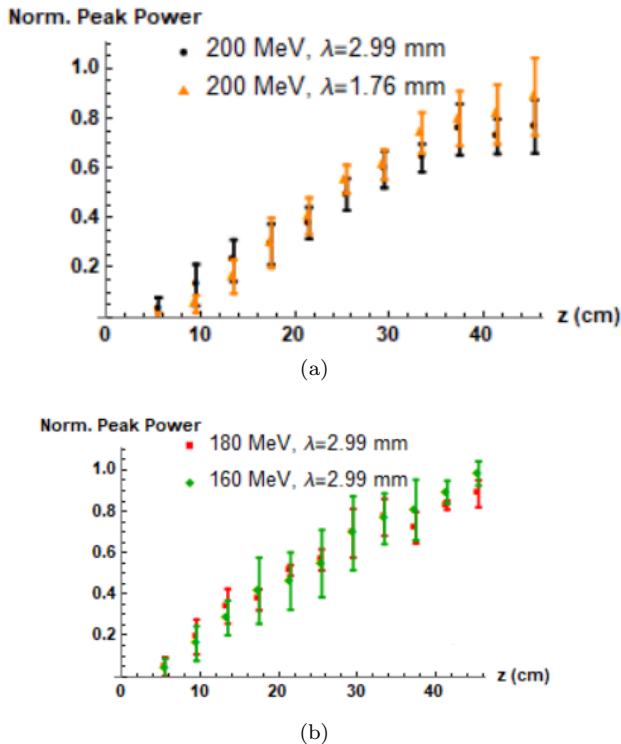


Figure 2. Measured radiation power at  $\lambda = 1.76 \text{ mm}$  as a function of the distance between the two sources. The blue line represents the measured power of backward CTR emitted by the second source.

tial tests have been carried out with electron bunches of  $200 \text{ MeV}$  and  $1.5 \text{ ps}$  rms long, using as first source of radiation either a solid screen or a hollow screen with  $5 \text{ mm}$  internal radius hole, emitting forward coherent transition or diffraction radiation respectively. In those first tests the radiation output power has been measured at a wavelength of  $\lambda = 1.76 \text{ mm}$ , and its evolution as a function of the distance between sources,  $z$ , is depicted in Fig. 2. The error has been evaluated as the rms fluctuation of the signal. In both cases a strong shadowing effect is observed for small values of  $z$  (i.e.  $5 \text{ cm}$ ) and the radiation power rapidly increases for larger distances between the sources. This observation is in direct contradiction with the model described by Eq. 1, which would predict a formation length in the  $\lesssim 100 \text{ m}$  range, suggesting a much stronger shadowing for  $z = 45 \text{ cm}$ . Whether the first source emits CTR or CDR has also a negligible impact on measured output powers and the corresponding shadowing effects. This suggests that the diffraction effect occurring at the central hole of the first screen is modi-

150 fying very weakly the properties of the emitted forward178  
 151 coherent radiation. For the maximum value  $z = 45$  cm179  
 152 the measured power reaches a level equivalent to the one180  
 153 corresponding to the emission of backward CTR from a181  
 154 single screen. This power is represented in Fig. 2 by the182  
 155 blue line. An image of the backward CTR radiation pat-183  
 156 tern acquired using a THz camera, is depicted in Fig 1184  
 157 and shows that the CTR source has a size of  $3$  mm rms.185  
 158 Complementary investigations have been performed to186



159 Figure 3. Top (a): Normalized radiation power as a function187  
 160 of the distance between the two sources of CDR and CTR,188  
 161 at different radiation wavelengths. Bottom (b): Normalized189  
 162 radiation power as a function of the distance between the two190  
 163 sources of CDR and CTR, at different beam energies.191  
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161 study the dependency of shadowing effects with respect211  
 162 to the beam energy and the observation wavelength. In212  
 163 those measurements the hollow screen emitting forward213  
 164 CDR has been kept as the first source of radiation. With214  
 165  $200$  MeV electrons the radiation power has been acquired  
 166 in two frequency bands, using band-pass-filtered Schot-  
 167 tky diodes at  $0.100 \pm 0.009$  THz and  $0.170 \pm 0.009$  THz  
 168 (i.e.  $\lambda = 2.99$  mm and  $\lambda = 1.76$  mm). The results pre-215  
 169 sented in Fig. 3(a) show a slightly stronger shadowing216  
 170 for longer wavelength, which is not in contradiction with217  
 171 the theory expressed by Eq. 1, that foresees a depen-218  
 172 dency proportional to  $\lambda$ . The additional experimental219  
 173 results obtained for different electron energies are pre-220  
 174 sented in Fig. 3(b). A small dependence on beam energy221  
 175 is measured, with shadowing effects slightly reducing for222  
 176 lower beam energies. This observation is in contradiction223  
 177 with the model described by Eq. 1 that predicts a much224

stronger dependency with beam energies, proportional to  
 $\gamma^2$ . In comparison, for shorter wavelength in the optical  
 range, the light emission from two consecutive transition  
 radiation screens is doubling for large distance between  
 sources [9]. Furthermore, the data in Fig. 3 has been  
 normalized to the reference level  $\sim 13.5$  kW, which was  
 comparable (within the error bars) to the one measured  
 in the experiment reported by Fig. 2 both for different  
 wavelengths and for different beam energies, due to the  
 experimental setup affected by diffraction losses domi-  
 nating both the radiation production and its detection.

All those observations indicate that the correct modelling  
 of shadowing effects in the sub-THz range requires a more  
 detailed treatment than the one developed initially for  
 short wavelengths. Theoretically, the electric field of for-  
 ward CTR or CDR radiated by ultra-relativistic electrons  
 can be calculated using the formalism developed in [21]  
 or [22]. For an azimuthally symmetric geometry and for  
 a gaussian electron bunch with rms time-duration  $\sigma_r$ , the  
 electric field radiated forward from a round and perfectly  
 conducting disk with an external radius  $b$  and a central  
 hole with radius  $a$  is described by the radial polarization  
 component

$$E_f(\vec{R}, \omega) = \frac{iQ\omega^2 e^{i\frac{\omega R}{c} - \frac{\omega^2 \sigma_r^2}{2}}}{4\pi\epsilon_0 \beta^2 \gamma c^2 R} \times \left[ \int_a^b d\varrho \varrho K_1\left(\frac{\omega \varrho}{\beta \gamma c}\right) J_1\left(\frac{\omega \varrho}{c} \sin \theta\right) e^{i\frac{\omega \varrho^2}{2cR}} \right] \quad (2)$$

201 where  $Q$  is the total charge of the electron bunch,  $c$  is  
 202 the speed of light in vacuum,  $\omega = 2\pi c/\lambda$  is the angular  
 203 frequency of radiation,  $\varphi$  is the azimuthal angle, and  $\epsilon_0$   
 204 is the vacuum dielectric constant. When  $a = 0$  and  $b \rightarrow \infty$ ,  
 205 Eq. 2 corresponds to the field radiated by ideal transition  
 206 radiation. In addition, the diffraction effect from the hole  
 207 is small, and the CDR field distributions become similar  
 208 to the ones of CTR as it is observed experimentally and  
 209 reported in Fig. 2. This concept is generally true in our  
 210 case because even the outer target dimensions are much  
 smaller than the field radius. We define the observation-  
 distance vector  $\vec{R} = R\{\cos \varphi \sin \theta, \sin \varphi \sin \theta, \cos \theta\}$ , with  
 $R = (x^2 + y^2 + z^2)^{1/2}$ . The spectral-angular distribution  
 of forward radiated energy is obtained from Eq. 2 using

$$\frac{d^2 I}{d\omega d\Omega} = \frac{\mu_0 c}{\pi} |E_f(\vec{R}, \omega)|^2 R^2 \quad (3)$$

Equations 2 and 3 show that the angular distribution of  
 the radiation changes as a function of the distance from  
 the source,  $z$ . Studied by Verzilov in [23], this feature  
 is due to the so-called pre-wave zone effect, and reflects  
 the fact that the radiated field is not a point source but  
 expands transversely similarly to the particle field. The  
 angular distribution of the radiation is thus affected by  
 the transverse distribution of the particle beam at least  
 for small distances  $z$  from the source, as was also shown  
 in simulations in [24]. Only in the far-field zone, for  $z \gg$

$\gamma^2 \lambda / 2\pi$ , such a dependence disappears. Using Eq. 2 the angular distribution of forward coherent radiation can be calculated as a function of  $z$ . Several examples of such distribution are depicted in Fig. 4 for the wavelengths  $\lambda = 1.76$  and  $2.99$  mm, assuming electrons with  $\gamma = 400$  and a screen with parameters  $a = 5$  mm and  $b = 50$  mm. The peak of the angular distribution of forward CDR, changes significantly as a function of the distance from the source as expected from both diffraction and pre-wave zone effects. For relatively short distances from the source, the emission cone of the radiation  $\theta_d$  is large and decreases asymptotically with  $z$  to reach a value of  $\theta_d \sim 0.38\lambda/b$  [25]. The shadowing effect between two

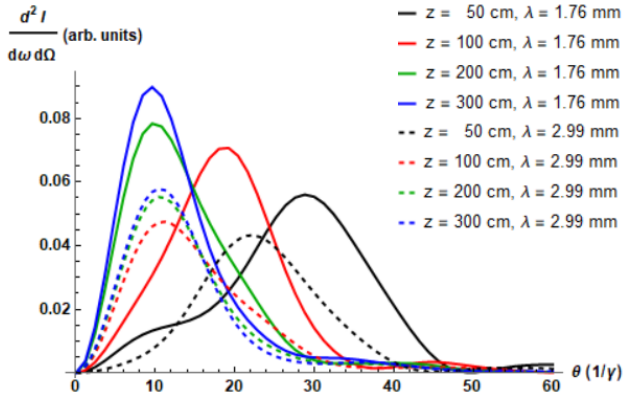


Figure 4. Angular distribution of forward CDR for different distances from the source and for two different wavelengths.

consecutive sources can be calculated by summing up the spatial distribution of the forward CDR field, emitted from the first screen and propagating to the position of second screen, with the backward CTR field emitted by the latter. The total field is thus written as follows

$$\vec{E}(\vec{r}, \omega) = P(\vec{r}, \omega) \vec{E}_f(\vec{r}, \omega) e^{iz/L_f} + \vec{E}_b(\vec{r}, \omega) \quad (4)$$

where  $P$  is the pupil function taking into account the limited size of the second radiator with respect to the diverging front of forward radiation. The field  $\vec{E}_b$  is obtained from Eq. 2, sending  $\cos \theta \rightarrow -\cos \theta$  and  $a \rightarrow 0$ . Using this formalism, calculations have been performed to reproduce the experimental data. The results are presented in Fig. 5. The calculations have been carried out considering exactly the same parameters used for the experiment, both in terms of beam parameters and setup geometry. The data and the calculations have been consistent within the error bars associated to the experiment. More precise measurements could have matched even better the analytic model, nevertheless the electron charge fluctuations during the experiment have determined non-negligible fluctuations of the intensity of the coherent light and the goodness of the results has been slightly affected by this experimental limitation. The new model above presented is certainly an extension of the previous one used for example in [9], where incoherent radiation was considered and no diffraction effects were

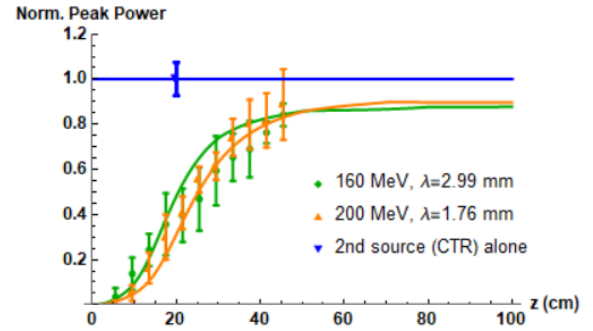


Figure 5. Comparison between data and analytic calculations for the shadowing of coherent radiation. Blue line corresponding to 13.5 kW.

taken into account. Indeed, Eq. 2 contains this new information, since the gaussian term in the radiation frequency is related to the bunch form factor (coherent radiation) and the expression under the integration sign is a Fresnel integral (diffraction effects). For sake of coherence and completeness we have also introduced the pupil function in Eq. 4 which takes into account the diffraction losses of the forward radiation front propagating onto the surface of the second radiator (where there was no need for this in previous works with incoherent radiation). It's important to state that, doing so, the analytic calculations only consider the diffraction losses but not the deformation of the reflected wavefronts due to the diffraction. Finally this aspect has not been so relevant for the presented experiment because the expected diffraction angle was low  $\lambda/b \ll 1$  and also because the detection has been performed by integrating over the radiation wavefronts, measuring only the total power. In the (sub-)THz range and for ultra relativistic electrons, several key parameters need to be considered to understand shadowing effects correctly and to estimate the output radiated power quantitatively. First, the interference becomes predominantly sensitive to the spatial overlap between the two radiation fields at the position of the second source. Secondly, the typical approximation of an infinitely wide radiator, used for short wavelengths, becomes invalid as the transverse dimension of the beam field is typically larger than the source size defined by the outer target dimensions, i.e.  $\gamma\lambda \gg b$  for longer wavelengths. This dependence of the spectral-angular distribution of the coherent radiation on the external radius of the radiator  $b$  has been experimentally studied in [26]. In order to estimate how important these two effects are on shadowing, further calculations have been made using infinitely large radii for the first and the second source,  $b_1$  and  $b_2$ , where we consider that the radius of the OAP mirror is infinite when the radius of the second source is also infinite. The results, plotted in Figs. 6(a) and 6(b), show a strong effect of the source radius on shadowing. When  $b_1$  is infinite while  $b_2 = 50$  mm shadowing effects increase and the output radiation levels decrease

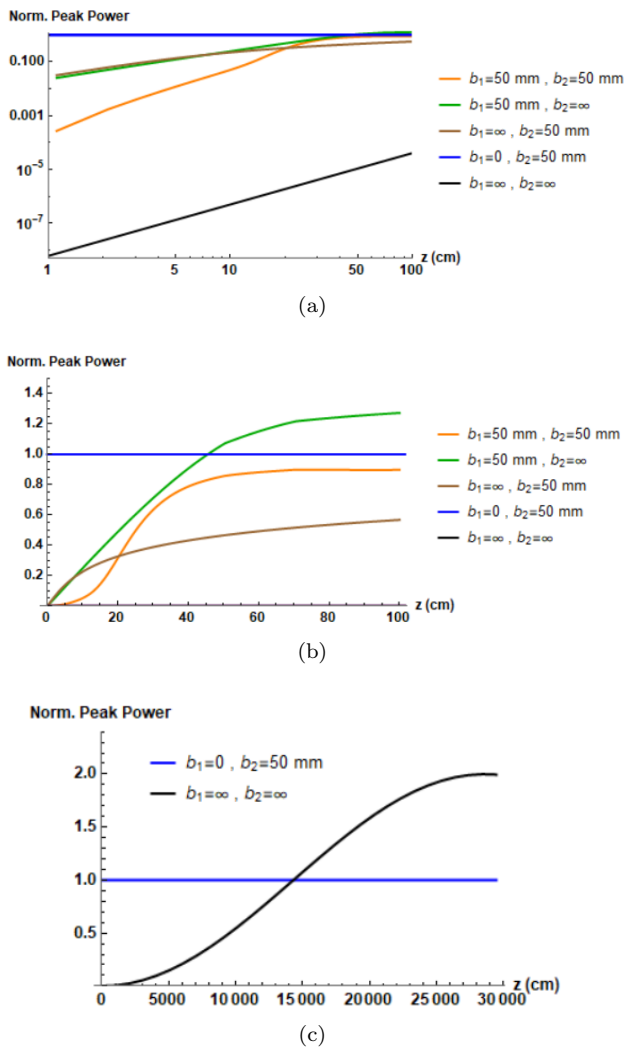


Figure 6. Top (a): Simulated shadowing effect with two sources of different size (peak power normalized to the case  $b_1 = 0, b_2 = 50\text{ mm}$ ). Center (b): Linear scale of the same plot in Fig. 6(a). Bottom (c): The limit case  $b_1 = \infty, b_2 = \infty$ , normally valid with incoherent radiation.

by roughly 40 % of the level of the backward CTR alone. In the opposite case, with  $b_1 = 50\text{ mm}$  and  $b_2$  infinite, the shadowing effect would decrease with the correspond-

ing output power higher by 30 %. One should also note that backward CTR power from an infinite large radiator is expected to be larger by a factor  $> 3$  compared to the value obtained in our test for a  $50\text{ mm}$  radius source. For completeness, the hypothetical case with all sources having an infinite radius is also presented in Fig. 6(c), where the shadowing effect would be much stronger. For a distance  $> 300\text{ m}$  the radiation would reach a level corresponding to twice the output power emitted as CTR from a single source, thus matching the observation done by [9] for shorter wavelengths with a formation length as long as one hundred meters. Fig. 6 demonstrates that even if the observations made with coherent radiation might seem in contradiction with past observations made with incoherent radiation, when properly considering the diffraction effects, one situation reduces to the other continuously, therefore the diffractive shadowing of coherent radiation is only a natural extension of the shadowing of incoherent radiation. The authors have found as well much instructive to represent examples of shadowing for limit situations as infinite radiators, finite radiators and mixed combinations.

In conclusion, we have been experimentally studying the shadowing effect between two sources of coherent radiation. We complemented our observations by the development of a generalized formalism that enables to accurately predict shadowing effects in diffractive conditions. For longer wavelength (i.e.  $\text{mm}$ ) and relativistic beam energies  $\gamma \gg 1$ , diffraction effects and pre-wave zone effects play a crucial role in the interference mechanism between two consecutive sources of radiation. The physical sizes of those sources are key parameters that influence the electromagnetic shadowing and limit its effect to a short distance. Our results will benefit any application of coherent radiation from multiple consecutive sources for intense THz beam generation [27–29] or for beam diagnostics’ purposes [30], where an upstream screen is used to shield from coherent radiation background such as synchrotron radiation or wakefields.

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