

1 **Interpretation of Pressuremeter Test by Finite Element Method**

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27 **Abstract**

28 A pressuremeter test is a useful tool to explore geomechanical properties by comparing the in-situ  
29 measured stress-strain relationship with proposed soil behaviour. In this paper, a coupled hydro-  
30 mechanical finite element model is developed to interpret pressuremeter test data, considering  
31 nonlinear elasticity, tensile fracturing and consolidation of soil. The 1D finite element model reduced  
32 the total number of elements and hence saved computational time without losing accuracy. It is found  
33 that tensile fracturing plays an important role for the cohesive clay, which would lead to  
34 overestimation of the stiffness and strength if the tensile failure is not considered. In addition,  
35 consolidation needs to be considered when the permeability coefficient is between  $10^{-10}$ m/s and  
36  $10^{-8}$ m/s, and the errors of derived stiffness constant and friction angle can reach a maximum of 21%  
37 and 35.5% respectively if neglecting consolidation.

38

39 **Keywords**

40 Pressuremeter test, finite element, tensile fracturing, consolidation

41

42 **List of notation**

43  $\alpha$  stiffness constant

44  $\beta$  exponent of elasticity

45  $p$  pore pressure

46  $k$  permeability coefficient

47  $u$  displacement of soil

48  $\sigma'_t$  tensile strength

49  $\sigma'_3$  minor principal effective stress

50  $\sigma'_r$  radial effective stress

51  $\sigma'_\theta$  circumferential effective stress

52  $\gamma_w$  unit weight of water

53  $K_w$  bulk modulus of water

54  $\epsilon_{pt}$  tensile plastic strain

55

## 56 **1 Introduction**

57 The pressuremeter test is a widely used in-situ test to achieve quick and easy measurement of the  
58 stress-strain relationship of soil. By comparing this stress-strain relationship with proposed soil  
59 behaviour, some geomechanical parameters can be determined. It is common sense that the  
60 pressuremeter test can provide accurate estimates of soil properties due to its little soil disturbance in  
61 situ. However, in practice, it has been found that there are still some uncertainties about the  
62 interpretation of test data due to the complexity of soil physical properties.

63

64 In general, interpreting pressuremeter test involve fitting curves to the test data (Clarke 1995; Schnaid  
65 et al. 2000). This interpreting approach rely either on empirical correlations, or on solving the  
66 boundary problem. Due to the pressuremeter test normally being performed over a short period of  
67 time, a number of analytical models have been proposed to interpret the pressuremeter test in clay  
68 under undrained conditions (Gibson and Anderson, 1961; Wroth, 1982; Jefferies, 1988; Bolton and  
69 Whittle, 1999; Cunha 1994; Cunha 1996). All these studies simplified the pressuremeter test as an  
70 undrained cylindrical cavity expansion in elastic/perfectly plastic clay. Unlike in clay, interpreting the  
71 results of a pressuremeter test in sands or rocks with a high permeability coefficient, the approaches  
72 consider the volume change in drained conditions (Hughes et al., 1977; Housby and Withers, 1988;  
73 Withers et al., 1989; Yu and Housby, 1991; Yu, 2000; Mo et al., 2014). These analytical methods  
74 bring convenience in curve-fitting analysis when interpreting pressuremeter test data due to the  
75 explicit formulation and hence quick calculation. Numerical method has recently become an effective  
76 and widely-used mathematical tool for modeling more complicated soil behaviour in pressuremeter  
77 test (Yeung and Carter, 1990; Housby and Carter, 1993; Ajalloeian and Yu, 1998; Sánchez et al.,  
78 2014; Isik et al., 2015). It has been shown that numerical analysis can obtain more accurate results  
79 compared to the analytical method, due to its capacity and flexibility for implementing complex  
80 constitutive models and boundary conditions to simulate the complicated soil behaviours. However,  
81 the degree of complexity of these numerical models inhibits the curve-fitting analysis into general  
82 purpose numerical codes, thus restricting their usefulness in engineering practice. (Emami and  
83 Yasrobi, 2014). In addition, most of these studies neglect the effects of tensile fracturing and

84 consolidation on soil behaviour in this particular geotechnical problem. For some soils with medium  
85 permeability, the soil is partially drained, and hence lie somewhere between the perfectly drained and  
86 undrained conditions. For some cohesive materials, tensile failure may happen before friction failure  
87 during the pressurimeter test.

88

89 This paper depicts numerical modelling based on the 1D finite element (FE) method, purposely  
90 designed for pressuremeter test. This FE modelling allows for considering complex constitutive  
91 models and capturing complete soil response with different geomechanical parameters, including  
92 nonlinear elasticity, permeability coefficient and tensile strength. The comparison of test results with  
93 the numerical reference framework indicates a method to determine the geomechanical parameters of  
94 soil, which will help understand the mechanisms of pressuremeter test. Due to the simplified geometry,  
95 the curve-fitting analysis can be easily incorporated for industry application. Therefore, this 1D finite  
96 element modelling can be a framework for the interpretation of pressuremeter test.

## 97 **2 Finite Element for coupled hydro-mechanical process**

98 During the pressuremeter test, a rubber membrane of the pressuremeter is expanded to exert  
99 horizontal pressure on the wall of the test cavity. The membrane expands at the constant strain rate,  
100 generally from 0.1% to 1% per minute in typical tests. The successive variation of cavity pressure with  
101 cavity strain is monitored and then compared with those obtained from numerical analysis to  
102 determine the geomechanical parameters. To simulate such a geomechanical process, the  
103 pressuremeter test is simplified as a time-dependent cylindrical cavity expansion in an elastic/plastic  
104 porous medium (soil) coupled with the dissipation of excess pore pressure. Some assumptions have  
105 been adopted based on the theory of continuum mechanics to develop the coupled hydro-mechanical  
106 model for deformable porous geological media:

- 107 (1) The soil is treated as a fully saturated medium.
- 108 (2) The seepage flow of pore water follows Darcy's law, and the inertia is ignored.
- 109 (3) The membrane is assumed to be long enough to ensure that a cylindrical cavity is formed and  
110 this cavity expands and contracts in plain strain condition.
- 111 (4) Considering the axial symmetry of geometry, the plane strain model can be further simplified  
112 to a 1D problem, to reduce the computational load without losing accuracy.

113

114 A finite element model in 1D axisymmetric space is built as shown schematically in Figure 1. All the  
115 FE analysis discussed in this paper is based on this model. This soil layer is located at the centre of  
116 the pressuremeter membrane. The initial cavity radius is 0.045m, same with the radius of  
117 pressuremeter membrane, but this radius would increase with the cavity expansion. The right  
118 boundary lies in the far field, 10m away from cavity center, to avoid boundary effects. Vertical  
119 movement is restrained, and hence the 1D model has only two degrees of freedom: displacement in  
120 radial direction and pore water pressure. The assumed initial condition includes the hydrostatic state  
121 of the soil and pore pressure. There are 120 quadratic elements generated in total, and the mesh  
122 near the pressuremeter is relatively finer than that in the far field. In order to simulate the large soil  
123 deformation in this test, the calculation mesh is modified in each stage. At the end of each stage, the  
124 displacement increment of each node will be added to the coordinates, so that the new family of  
125 radius is updated based on the deformed meshes from the previous stage.

126

127 Figure 1. Sketch of the numerical model to simulate a pressuremeter test

128

129 In the context of the theory of mixtures, the saturated porous medium is viewed as a mixed continuum  
130 of two independent overlapping phases. Its conservation equation can be obtained according to the  
131 principles of continuum mechanics, as shown in Figure 2.

132

133 Figure 2. Soil stress and pore flow velocity in axisymmetric problem

134

135 (1) Axisymmetric elastic equations:

136 If momentum can be neglected, the stress equilibrium for axisymmetric problem can be written as  
137 follows:

$$138 \quad \frac{\partial \sigma'_r}{\partial r} + \frac{\sigma'_r - \sigma'_\theta}{r} + \frac{\partial p}{\partial r} = 0 \quad (1)$$

139 where  $\sigma'_r$  is the radial effective stress,  $\sigma'_\theta$  is the circumferential effective stress,  $p$  is the pore pressure,  
140  $r$  is the radial coordinate.

141

142 The strain components for axisymmetric deformation are defined as follows:

$$143 \quad \varepsilon_r = \frac{\partial u_r}{\partial r} \quad (2)$$

$$144 \quad \varepsilon_\theta = \frac{u_r}{r} \quad (3)$$

145 where  $u_r$  is the displacement in radial direction,  $\varepsilon_r$  is the radial strain and  $\varepsilon_\theta$  is the circumferential  
146 strain.

147

148 Hence, the volumetric strain can be written by:

$$149 \quad \varepsilon_{\text{vol}} = \varepsilon_r + \varepsilon_\theta = \frac{\partial u_r}{\partial r} + \frac{u_r}{r} \quad (4)$$

150

151 The porous medium is assumed to be isotropic. If the shear modulus is assumed, the elastic  
152 constitutive equation can be expressed in terms of stress and strain increments:

$$153 \quad d\sigma'_r = \frac{2G\nu}{1-2\nu} d\varepsilon_{\text{vol}} + 2\theta d\varepsilon_r \quad (5)$$

$$154 \quad d\sigma'_\theta = \frac{2G\nu}{1-2\nu} d\varepsilon_{\text{vol}} + 2G d\varepsilon_\theta \quad (6)$$

155 where  $G$  is shear modulus and  $\nu$  is Poisson's ratio.

156

157 (2) Axisymmetric seepage equations:

158 In this study, the flow of pore water obeys Darcy's law. Hence, the flow velocity  $q_r$  can be written as:

$$159 \quad q_r = \frac{k}{\gamma_w} \frac{\partial p}{\partial r} \quad (7)$$

160 where  $k$  is the permeability coefficient (m/s),  $\gamma_w$  is the unit weight of water.

161

162 The mass conservation between volumetric strain and water drainage leads to the storage  
163 equation:

$$164 \quad \frac{1}{r} \frac{\partial}{\partial r} (r q_r) + \frac{d}{dt} \varepsilon_{\text{vol}} - \frac{n}{K_w} \frac{dp}{dt} = 0 \quad (8)$$

165 where  $n$  is the porosity and  $K_w$  is the bulk modulus of pore water.

166

167 Taking Equations (4) and (7) into Equation (8):

$$168 \quad \frac{k}{\gamma_w} \frac{\partial^2 p}{\partial r^2} + \frac{k}{\gamma_w r} \frac{\partial p}{\partial r} + \frac{d}{dt} \left( \frac{\partial u_r}{\partial r} + \frac{u_r}{r} \right) - \frac{n}{K_w} \frac{dp}{dt} = 0 \quad (9)$$

169

170 The balance of relations, listed above, characterises the fundamental physical properties of matter

171 independently of its specific material properties. However, in the pressuremeter test, the response of

172 soil to similar interactions with cavity expansion differs for various geomaterials. Thus, constitutive

173 relations have to be defined to characterize specific mechanical behaviour. Bolton and Whittle (1999)

174 indicate that the application of linear elastic analysis to a non-linear elastic problem will give a wrong

175 interpretation of the distribution of stresses and strains in the pressuremeter test. Hence, a power law  
176 function is applied to simulate the stiffness degradation of the soil, which was first proposed by Gunn  
177 (1992) and Bolton et al. (1993). The stress-strain relationship is expressed as:

$$178 \quad \tau = \alpha\gamma^\beta \quad (10)$$

179 Where  $\tau$  is shear stress,  $\gamma$  is the shear strain,  $\alpha$  is the stiffness constant and  $\beta$  is the exponent of  
180 elasticity.

181

182 In this finite element model, soil is defined as a elastic/perfectly plastic material. The Mohr-Coulomb  
183 model is applied to define the shear strength of the soils at different effective stresses. Except for  
184 shear failure, tensile fracturing is one of the most important processes in the pressuremeter test. It is  
185 a process of initiation and propagation of a thin physical separation when the soil effective stress  
186 drops below the tensile strength. .

187

188 The tension yield function is used, and can be written in the form of the minor principal effective stress:

$$189 \quad f^t = \sigma'_t - \sigma'_3 \quad (11)$$

190 where  $\sigma'_t$  is the tensile strength and  $\sigma'_3$  is the minor principal effective stress. During the process of  
191 cavity expansion in clay, because of the increasing difference between the radial and circumferential  
192 stress imposed by the applied pressure, the soil is sheared. The circumferential stress becomes the  
193 minor principal effective stress. If equation (11) is satisfied, tensile fracturing occurs, as shown in  
194 Figure 3.

195

196 Figure 3. Mechanisms of tensile fracturing in undrained conditions (after Mitchell and Soga, 2005)

197

198 Tensile failure happens when the tensile failure criterion is violated. The material still behaves as a  
199 continuum after the occurrence of tensile failure. In addition, the tensile potential function is assumed  
200 to follow the associated flow rule. Under conditions of tensile failure, the tensile strength is assumed  
201 to soften gradually rather than diminishing immediately. The softening law is shown in Figure 4b,  
202 where the tensile strength decreases from  $\sigma'_t$  to zero when the tensile plastic strain  $\varepsilon_{pt}$  increases from  
203 0 to 0.01 (Ng 2009). The complete yield surface, incorporating shear and tension yield functions, is  
204 shown in Figure 4a.

205

206 Figure 4. (a) complete yield surface (b) softening law of tensile strength

207

### 208 **3 Drained and undrained analysis**

209 Based on the formulations discussed above, an in-house finite element program was written. This is a  
210 procedural finite-element code using generic programming. In order to validate the finite element  
211 model, two different series of case studies were conducted, including drained and undrained analysis.

212

213 To interpret the sand strength in the pressuremeter test, Yu and Houlsby (1991) derived a widely  
214 accepted analytical solution. This solution is based on Cavity Expansion Theory, using the logarithmic  
215 strain and Mohr-Coulomb model parameters. Figure 5 compares Yu and Houlsby's closed-form  
216 solution and data generated by linear elastic finite element drained analysis with different values of  
217 shear modulus. All parameters are as listed in Table 1 (drained analysis). In this analysis, the pore  
218 pressure on every nodes is fixed as 0, which eliminate the effect of pore pressure on effective stress.  
219 Displacement boundary conditions will be applied on the left boundary abutting the instrument to  
220 simulate the cavity expansion, as shown in Figure 1. The cavity strain increases from 0 to 5%. The  
221 initial effective stress is set as 100kPa. 3 case studies with shear modulus of 50 MPa, 100 MPa and  
222 200 MPa were performed respectively. Yu's solution matches the FE-generated curve outstandingly  
223 well, which implies that both the elastic/plastic deformation and the large strain formulation have been  
224 properly taken into account.

225

226 Table 1 Soil parameters for drained/undrained analysis

227

228 Figure 5. Cavity expansion curve from numerical drained analysis and analytical solution

229

230 Undrained analysis can be performed in terms of either effective or total stresses. During the loading  
231 and yielding process, a significant amount of excess pore pressure would be developed. This excess  
232 pore pressure would lead to a change of the effective stress and therefore influence the shear



233 strength of the soil. Hence, the success of such analysis relies on whether the adopted constitutive  
234 model can correctly predict the development of effective stress and pore water pressure. If elastic  
235 perfect plastic model used, the prediction of pore water pressure in the pre-failure regime may be  
236 away from the real situation. Bolton and Whittle (1999) derived the undrained shear strength of clay in  
237 the pressuremeter test, assuming that the ground response to loading/unloading is non-linear  
238 elastic/perfectly plastic. A non-linear elastic/perfectly plastic undrained analysis was carried out using  
239 the proposed model in this paper. The hydro-mechanical coupling model can be used to carry out an  
240 effective stress analysis of pressuremeter test when the permeability coefficient  $k$  is set as 0. Figure  
241 6 shows the comparison of Bolton and Whittle's analytical solution and the results of the finite element  
242 simulation with different stiffness constants. All parameters are as listed in Table 1 (undrained  
243 analysis). Three case studies with different stiffness constant were performed. The numerical result  
244 matches the analytical solution, which indicates that the nonlinear elasticity model has been correctly  
245 implemented, which provides some confidence in using the FE model.

246

247 Figure 6. Cavity expansion curve from numerical undrained analysis and analytical solution

248

#### 249 **4 Effects of tensile fracturing**

250 Ng (2009) conducted tests of cavity expansion to simulate a pressuremeter test and tensile fracturing  
251 in cement bentonite. The borehole was modelled by a cylindrical specimen with an inner central  
252 cylindrical cavity. A rubber membrane was inserted into the inner cylindrical cavity of the specimen so  
253 that the injected water could apply pressure to the specimen's cavity through membrane expansion.  
254 Tests were performed in undrained conditions as the permeability of cement bentonite is very low.  
255 One of the test data is used as reference for comparison with FE analysis in this paper. The purpose  
256 of this paper is to demonstrate the effects of tensile fracturing and consolidation. Only the loading  
257 stage of test is simulated.

258

259 Two series of FE analyses were performed. The first is shear analysis using the Mohr-Coulomb model,  
260 which only considers the shear failure. The second is tensile/shear analysis which considers both  
261 shear failure and tensile failure. All the parameters used in the FE analysis are listed in Table 2. The  
262 calculation was divided into 250 steps. In each step the cavity strain increased 0.02%, as a boundary

263 condition applied on the left boundary. Permeability coefficient was 0 m/s. The cohesion and the  
264 friction angle were 235 kPa and 20°, according to the undrained triaxial test results of bentonite  
265 material (Joshi et al., 2008). The dilation angle and tensile strength were 0° and 65 kPa, based on the  
266 results of the Brazilian tests (Ng, 2009). The test data from Ng (2009) was used to calibrate the  
267 stiffness constant and exponent of elasticity, as shown in Figure 7.

268

269 Table 2 Soil parameters for shear and tensile/shear analysis

270

271 The FE results are shown in Figure 7. With the same stiffness constant of 8 MPa, the cavity pressure  
272 is 10% larger for the tensile/shear analysis than for the shear analysis when the cavity strain is about  
273 5%. In order to fit the test data with the same degree of accuracy, the stiffness constant needs to be  
274 reduced to 6.5 MPa for the tensile/shear analysis. Hence, it is concluded that failing to consider  
275 tensile fracturing leads to an underestimate of the cavity pressure and hence overestimate of the  
276 stiffness.

277

278 Figure 7. Cavity expansion curve for shear and tensile/shear analysis

279

280 The effective stress paths are presented in Figure 8, in which the change of effective radial stress with  
281 effective circumferential stress at the cavity wall is plotted. For the shear analysis, the increase in  
282 radial stress has a linear relationship with the decrease in circumferential stress until the shear stress  
283 reaches the yield surface. However, in the tensile/shear analysis, this turning point happens much  
284 earlier, when the effective circumferential stress is reduced to the tensile strength of -65 kPa. Due to  
285 tensile strength would soften gradually, it is shown that the effective circumferential stress increases a  
286 little after tensile failure. Between the case of shear analysis with  $\alpha = 8$  MPa and the tensile/shear  
287 analysis with  $\alpha = 6.5$  MPa, there is a marked difference in effective radial stress and circumferential  
288 stress. However, the difference in the cavity pressure at 5% strain is negligible, as shown in Figure 7,  
289 which indicates that considering tensile fracturing produces a much lower estimate of excess pore  
290 pressure during the cavity expansion process. This is reasonable, because the tensile fracture can  
291 lead to relief of the excess pore pressure.

292

293 Figure 8. Stress path at the cavity wall

294

295 The above process can be plotted in the form of Mohr's circles, as shown in Figure 9. In the shear  
296 analysis, as shown in Figure 9(a), the diameter of the Mohr's circles continues to increase and the  
297 centre of the Mohr circle keeps constant, initially corresponding to the undrained condition. The  
298 Mohr's circles finally stop expanding when the Mohr-Coulomb shear failure criterion is violated, and  
299 the effective radial stress reaches 520 kPa. In the tensile/shear analysis, as shown in Figure 9(b) and  
300 9(c), the soil undergoes tensile failure before reaching shear failure. After tensile failure, the centres of  
301 the Mohr's circles begin to move. The Mohr's circles finally reach the Mohr-Coulomb shear failure  
302 criterion with a much larger effective radial and circumferential stress than when tensile failure is not  
303 considered.

304

305 Figure 9. Mohr's circles at the cavity wall: (a) shear analysis ( $\alpha = 8\text{Mpa}$ ); (b) tensile/shear analysis  
306 ( $\alpha = 6.5\text{Mpa}$ ); (c) tensile/shear analysis ( $\alpha = 8\text{Mpa}$ )

307

308 In practice, the pressuremeter tests on low permeability soils are usually interpreted using total stress  
309 analysis, the undrained shear strength and elastic modulus can be estimated separately when other  
310 parameters are assumed. In this effective stress analysis, the cohesion and other parameters are  
311 assumed, as shown in Table 2, so that the stiffness constant or friction angle can be determined in  
312 each case study with different value of tensile strength. Figure 10 shows the derived stiffness  
313 constant and friction angle by interpreting data from Ng (2009), assuming that a stiffness constant of  
314 6.5 MPa and a friction angle of  $20^\circ$  are the real values. It seems that a high tensile strength value  
315 used in the model leads to an overestimation of the stiffness constant and friction angle. When the  
316 tensile strength increases beyond 140 kPa, the estimated stiffness constant and friction angle  
317 reaches about 7.9 MPa and  $38^\circ$ , respectively. This case is close to the shear analysis, in which the  
318 stress reaches the shear failure criteria before tensile failure occurs. Therefore, it can be concluded  
319 that tensile fracturing plays an important role in the pressuremeter test, and choosing a suitable  
320 tensile strength is very important in interpreting test data.

321 The success of this tensile/shear analysis lies on the accurate prediction of tensile failure and  
322 subsequent shear failure. For non-cohesive soil, shear failure would happen before the effective  
323 circumferential stress drops below 0 kPa, and hence the tensile stress will no longer occur. Hence,  
324 the proposed effects of tensile fracturing on pressuremeter test data only applies for cohesive soil,  
325 especially with high cohesion and low tensile strength. This effects reduces with the decreases of soil  
326 cohesion, and tensile/shear analysis becomes completely unnecessary for non-cohesive soil.

327

328 Figure 10. Effect of tensile strength on soil stiffness and strength

329

### 330 **5 Effects of consolidation**

331 Normally, pressuremeter testing in clay is considered an undrained process, but in reality some  
332 consolidation occurs for soil with medium permeability. In this section, a series of finite element  
333 analyses were performed to assess the effects of consolidation on the derived parameters from the  
334 pressuremeter test. To avoid the coupled effects of tensile fracturing and consolidation, the  
335 parameters were based on the shear analysis, as listed in Table 2 (shear analysis). The calculation  
336 was also divided into 250 steps and the cavity strain increased 0.02% in each step. Duration of each  
337 step was 12 seconds, corresponding to a conventional cavity strain rate of 0.1%/min adopted in the  
338 self-boring pressuremeter test. Figure 11 shows the cavity pressure for different values of the  
339 permeability coefficient. Initially, the cavity pressure increases with increasing cavity strain, and all the  
340 cases coincide to a single curve. After the cavity strain increases over 1%, individual curves show  
341 different behaviour. With a permeability coefficient of  $10^{-8}$  m/s, the cavity pressure reaches about  
342 1610 kPa when the strain is about 5%. This is much higher than the case of  $k = 10^{-10}$  m/s, in which  
343 the highest cavity pressure is about 1450 kPa. In addition, the stress–strain curves for the cases of  
344 the undrained condition and  $k = 10^{-11}$  m/s are identical, and the stress–strain curves for the cases of  
345 the drained condition and  $k = 10^{-7}$  m/s are identical. This indicates that consolidation must be  
346 considered when the permeability coefficient is between  $10^{-10}$  m/s and  $10^{-8}$  m/s.

347

348 Figure 11. Cavity expansion curve using consolidation analysis

349

350 The above process was plotted in the form of Mohr's circles, as shown in Figure 12. For the case of  
351  $k = 10^{-7}$  m/s, the mean effective stress increases sharply after the Mohr circle violates the tensile  
352 failure criteria, and hence shows a rapid increase in shear strength. For this reason, the cavity  
353 pressure for higher permeability can reach a higher value.

354

355 Figure 12. Mohr circles at the cavity wall using consolidation analysis

356

357 Figure 13 shows the stiffness constant and friction angle derived by interpreting the data from Ng  
358 (2009) when considering consolidation. It seems that the undrained assumption leads to  
359 overestimation of the soil stiffness and strength. When the permeability increases to about  $10^{-7}$  m/s,  
360 the stiffness constant and friction angle reduce to about 6.3 MPa and  $12.9^\circ$ . The errors are about 21%  
361 and 35.5%, respectively. This study therefore concludes that consolidation is a crucial factor in the  
362 process of the pressuremeter test, especially for soils with medium permeability between  $10^{-10}$  m/s  
363 and  $10^{-8}$  m/s. Without considering soil consolidation, the derived geomechanical parameters in  
364 undrained condition may be much higher than the real values. It is unfortunate that making this error  
365 in data interpretation leads to a unsafe design in geotechnical engineering projects.

366

367 Figure 13. Effect of the permeability coefficient on soil stiffness and strength

368

## 369 **6 Conclusions**

370 In this paper, a 1D finite element model was presented as a tool to derive in situ soil parameters,  
371 based on comparing pressuremeter test results with the expected soil responses from FE analysis.  
372 The numerical results perfectly matched the analytical solutions under both drained and undrained  
373 condition, which indicates that FEM is a valid and flexible method for interpreting pressuremeter test  
374 data. The 1D model reduced the total number of elements and hence saved computational time  
375 without losing accuracy.

376

377 Tensile fracturing is one of the most important processes in the pressuremeter test. Good agreement  
378 between the in situ test results and the numerical simulations was obtained. Cavity pressure in the

379 tensile/shear analysis is lower than in conventional shear analysis, when equivalent stiffness and  
380 shear strengths are used. Hence, for cohesive soil, neglecting to consider tensile failure will lead to  
381 overestimation of the stiffness constant and friction angle.

382

383 Normally, pressuremeter testing in clay is considered as an undrained process, but in reality some  
384 consolidation occurs for the clay with medium permeability. When the permeability coefficient is lower  
385 than  $10^{-11}$  m/s, the pressuremeter test is assumed to be under undrained conditions. When the  
386 permeability coefficient is between  $10^{-8}$  m/s and  $10^{-10}$  m/s, consolidation has a large effect on the  
387 results. It seems that the undrained analysis leads to overestimation of the soil stiffness and strength.  
388 When the permeability increases to about  $10^{-7}$  m/s, the test process is close to a drained condition,  
389 and the errors in the derived stiffness constant and friction angle are about 21% and 35.5%,  
390 respectively.

391

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396

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#### 477 **Figure captions**

479 Figure 1. Sketch of the numerical model to simulate a pressuremeter test  
480 Figure 2. Soil stress and pore flow velocity in axisymmetric problem  
481 Figure 3. Mechanisms of tensile fracturing in undrained conditions (after Mitchell and Soga, 2005)  
482 Figure 4. (a) complete yield surface (b) softening law of tensile strength  
483 Figure 5. Cavity expansion curve from numerical drained analysis and analytical solution  
484 Figure 6. Cavity expansion curve from numerical undrained analysis and analytical solution  
485 Figure 7. Cavity expansion curve for shear and tensile/shear analysis  
486 Figure 8. Stress path at the cavity wall  
487 Figure 9. Mohr's circles at the cavity wall: (a) shear analysis ( $\alpha = 8\text{Mpa}$ ); (b) tensile/shear analysis  
488 ( $\alpha = 6.5\text{Mpa}$ ); (c) tensile/shear analysis ( $\alpha = 8\text{Mpa}$ )  
489 Figure 10. Effect of tensile strength on soil stiffness and strength  
490 Figure 11. Cavity expansion curve using consolidation analysis  
491 Figure 12. Mohr circles at the cavity wall using consolidation analysis



492 Figure 13. Effect of the permeability coefficient on soil stiffness and strength

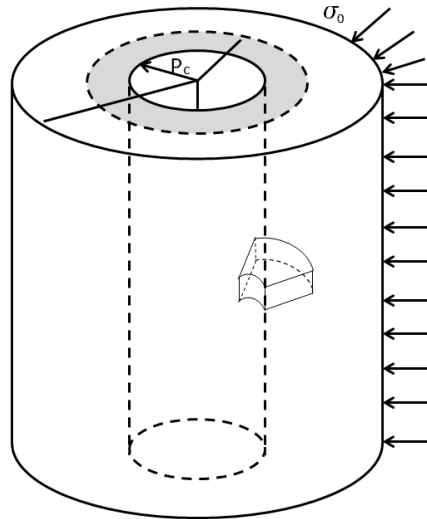
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494 **Table captions**

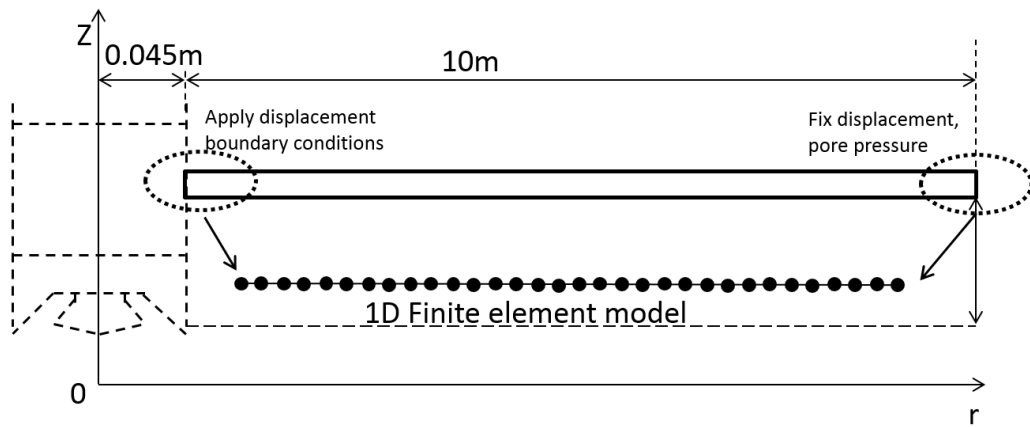
495 Table 1 Soil parameters for drained/undrained analysis

496 Table 2 Soil parameters for shear and tensile/shear analysis

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Figure 1. Sketch of the numerical model to simulate a pressuremeter test

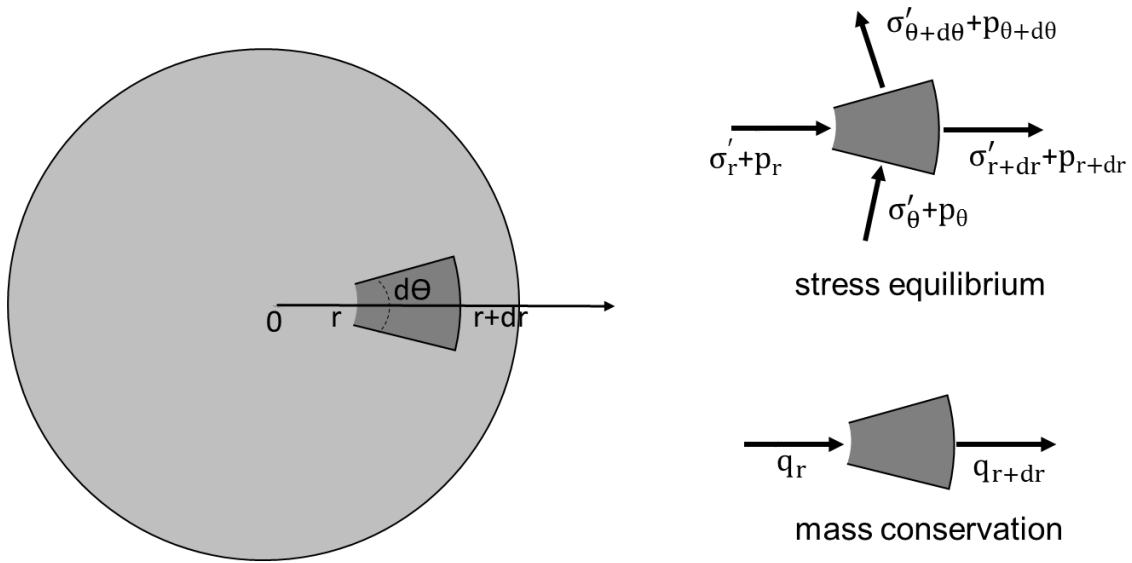


Figure 2. Soil stress and pore flow velocity in axisymmetric problem

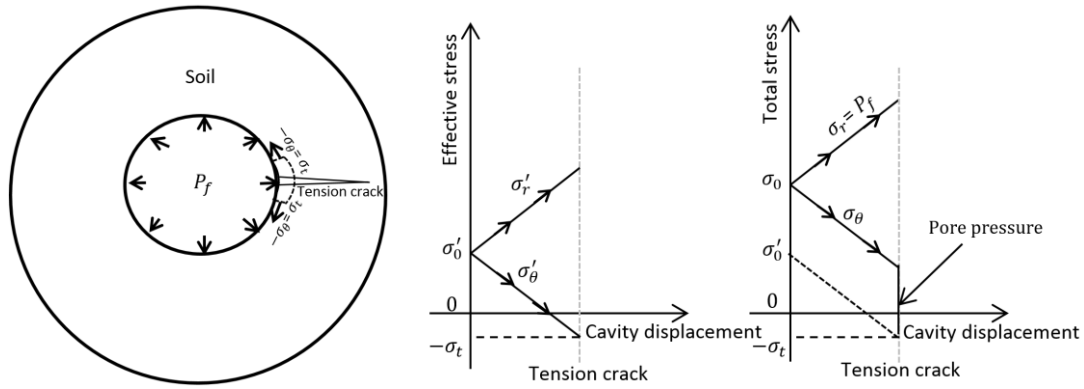


Figure 3. Mechanisms of tensile fracturing in undrained conditions (after Mitchell and Soga, 2005)

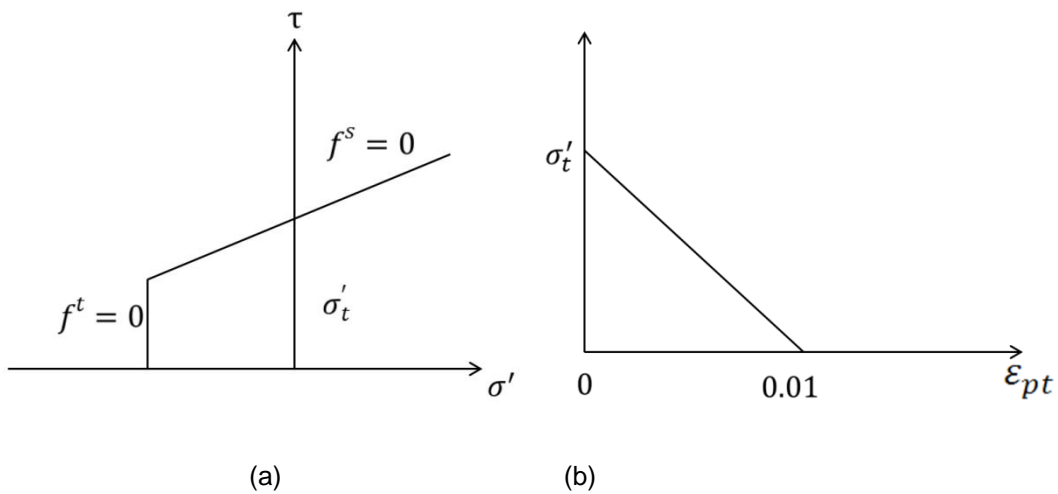
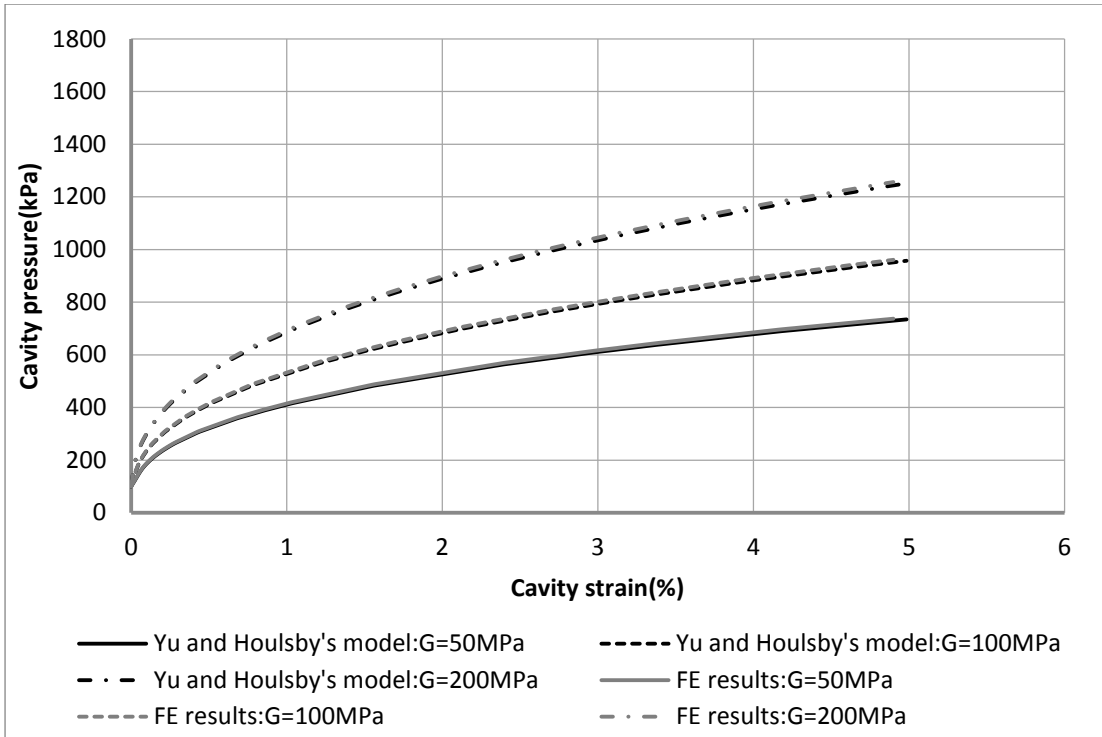


Figure 4. (a) complete yield surface (b) softening law of tensile strength

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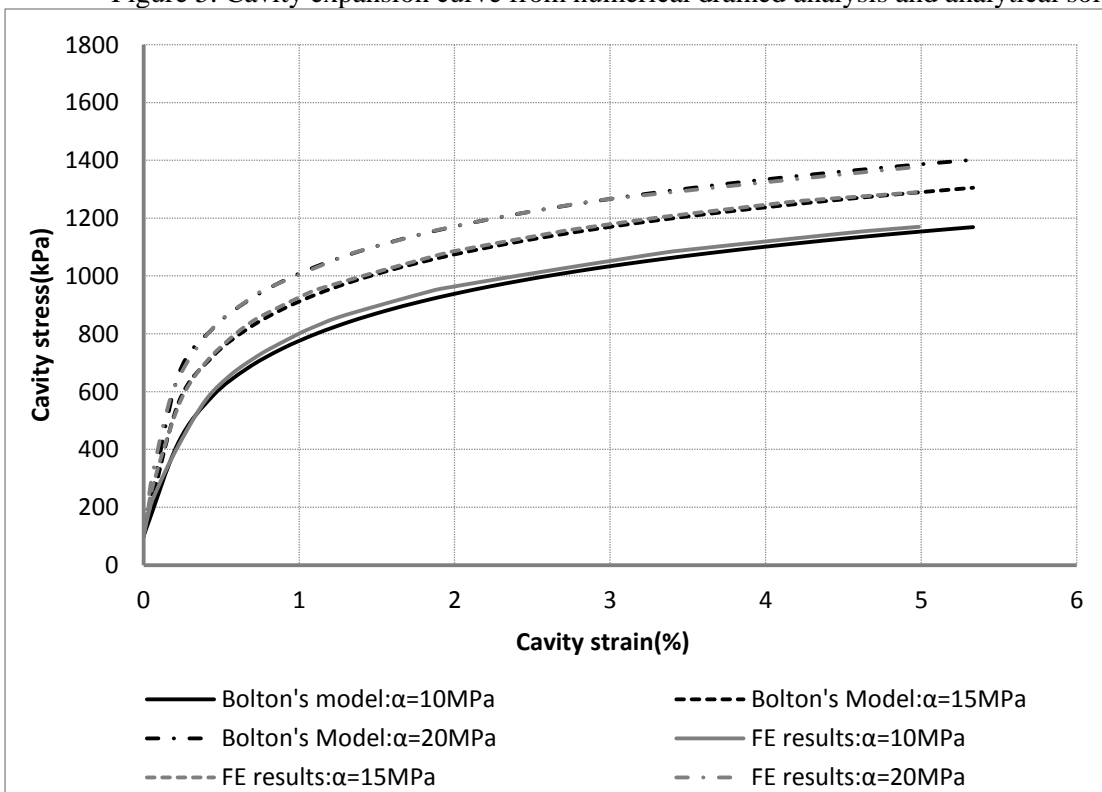
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Figure 5. Cavity expansion curve from numerical drained analysis and analytical solution

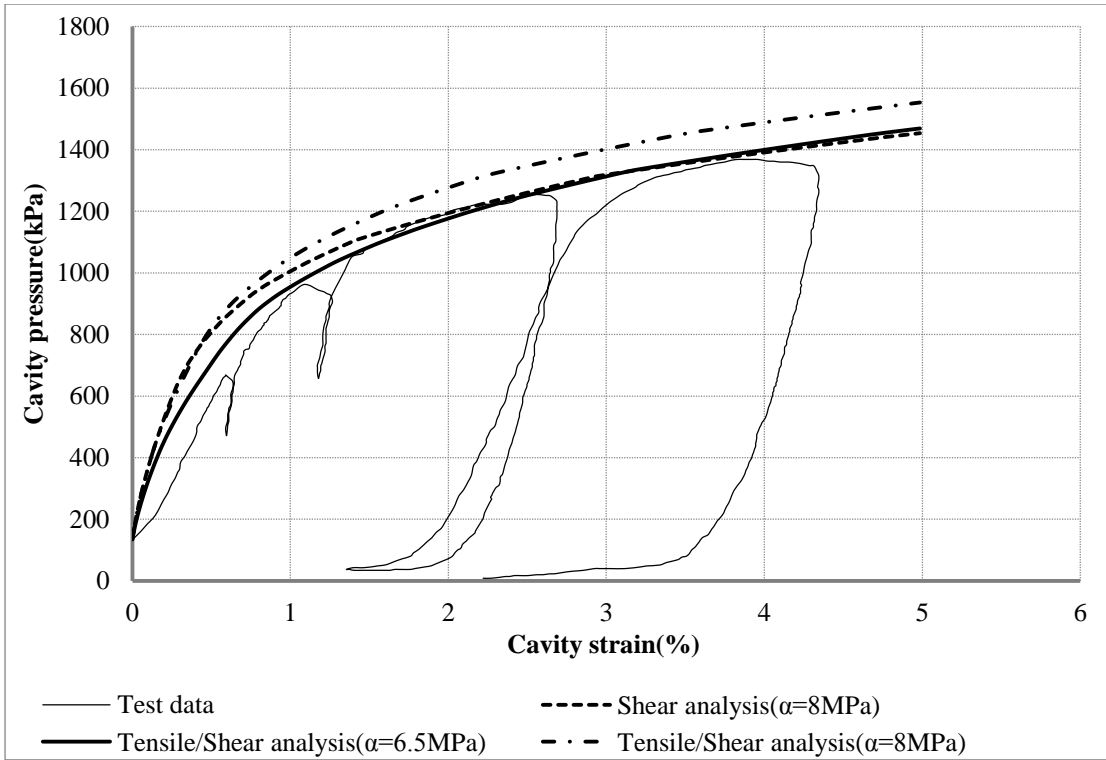


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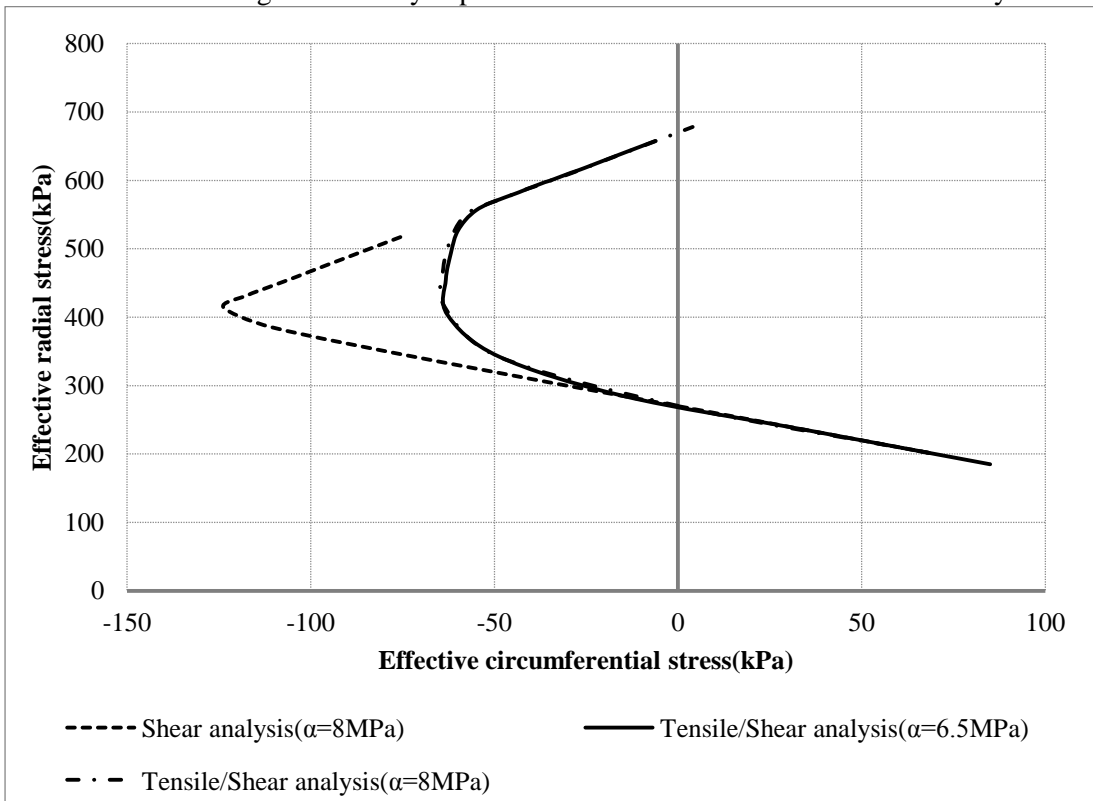
Figure 6. Cavity expansion curve from numerical undrained analysis and analytical solution



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Figure 7. Cavity expansion curve for shear and tensile/shear analysis



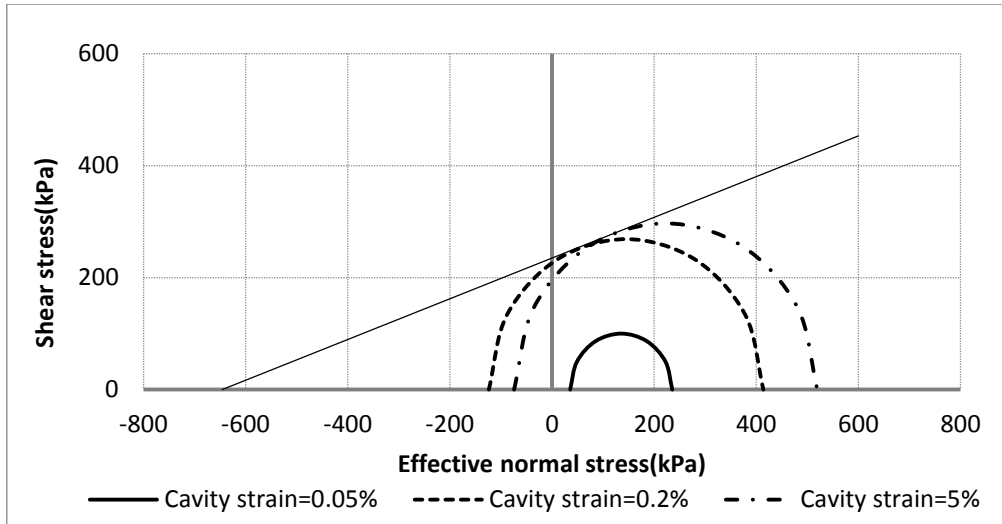
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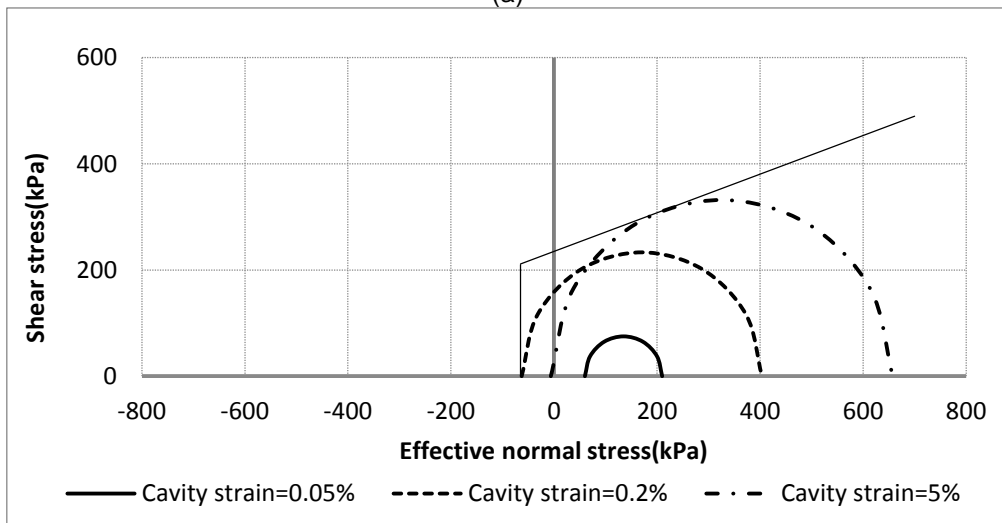
Figure 8. Stress path at the cavity wall

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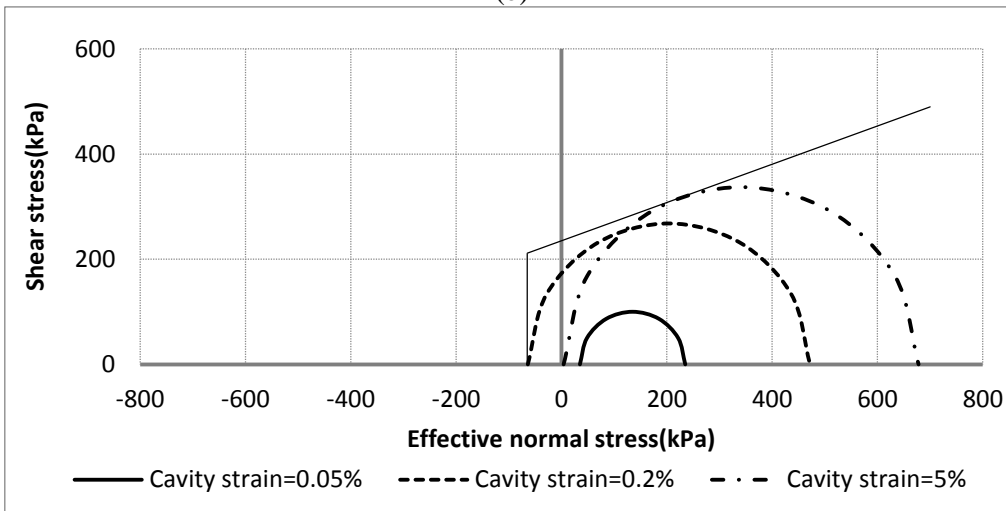
(a)

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(b)

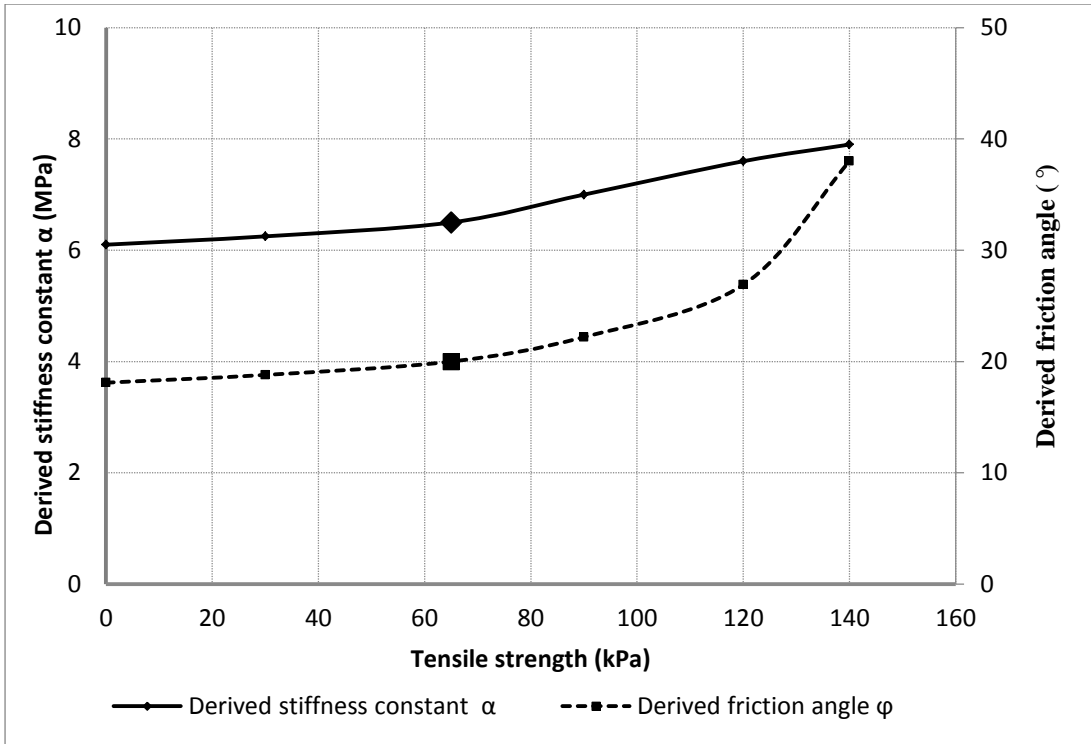
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(c)

528 Figure 9. Mohr's circles at the cavity wall: (a) shear analysis ( $\alpha = 8\text{MPa}$ ); (b) tensile/shear analysis  
529 ( $\alpha = 6.5\text{MPa}$ ); (c) tensile/shear analysis ( $\alpha = 8\text{MPa}$ )

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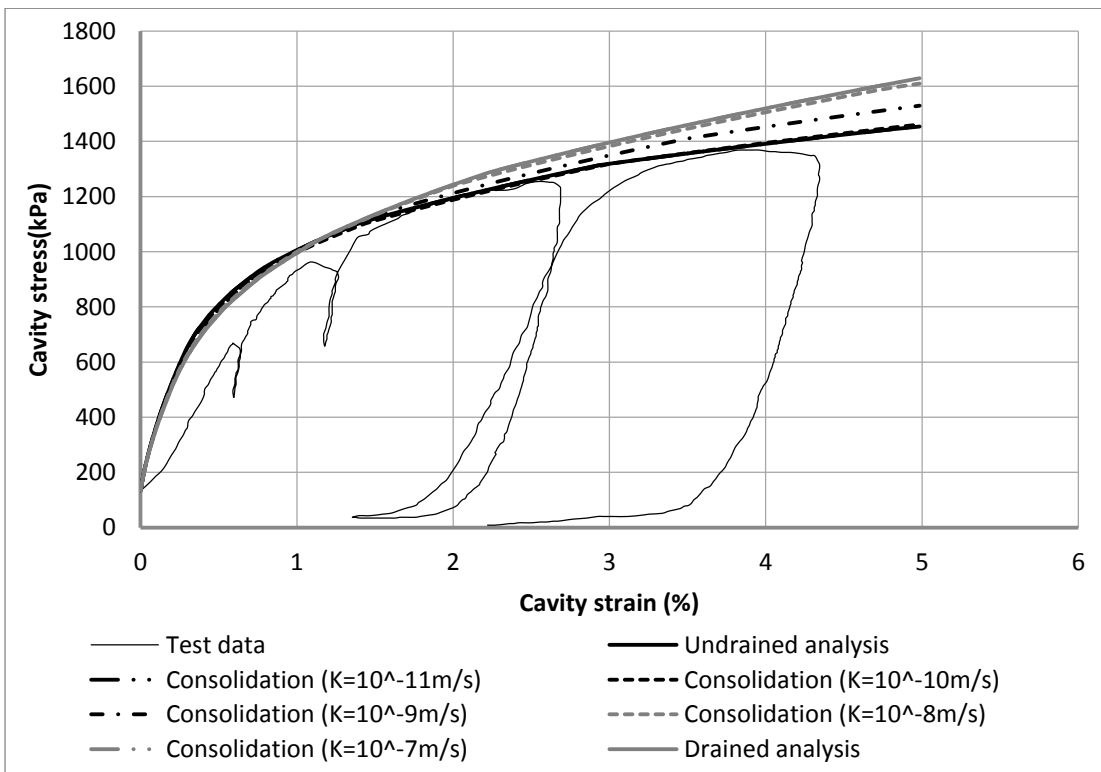


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Figure 10. Effect of tensile strength on soil stiffness and strength

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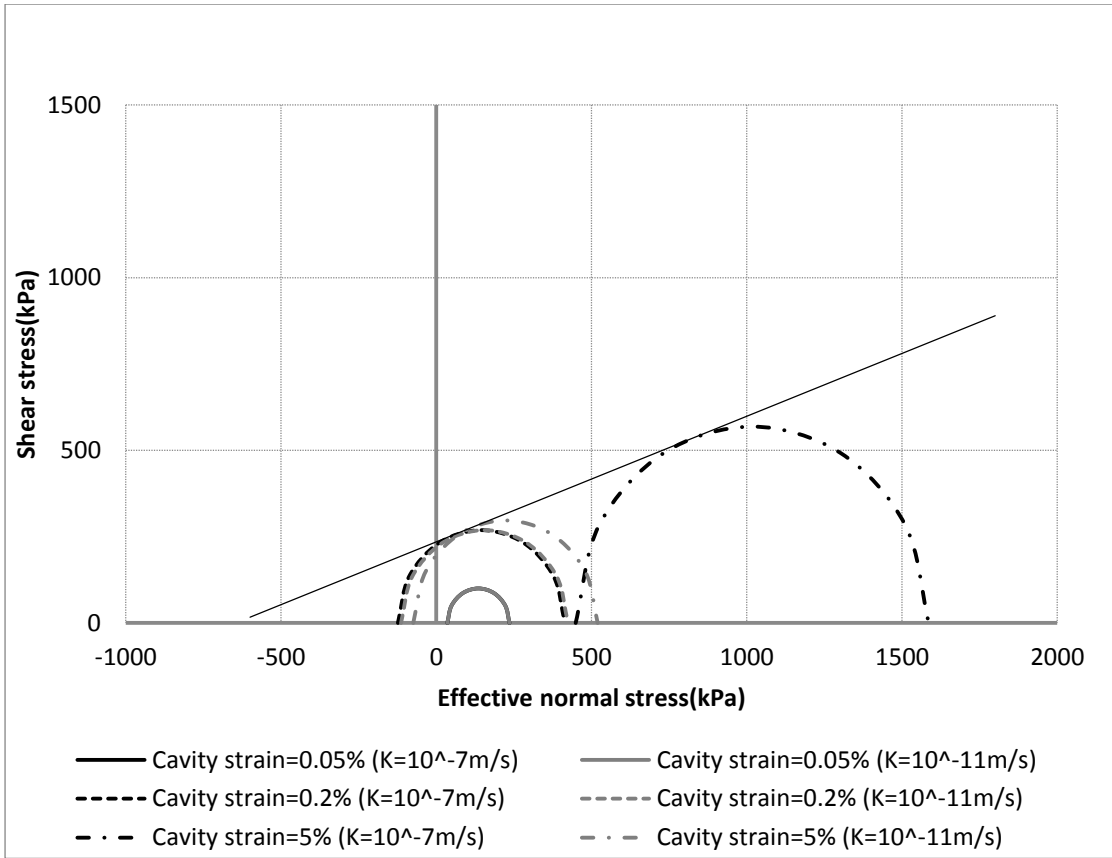
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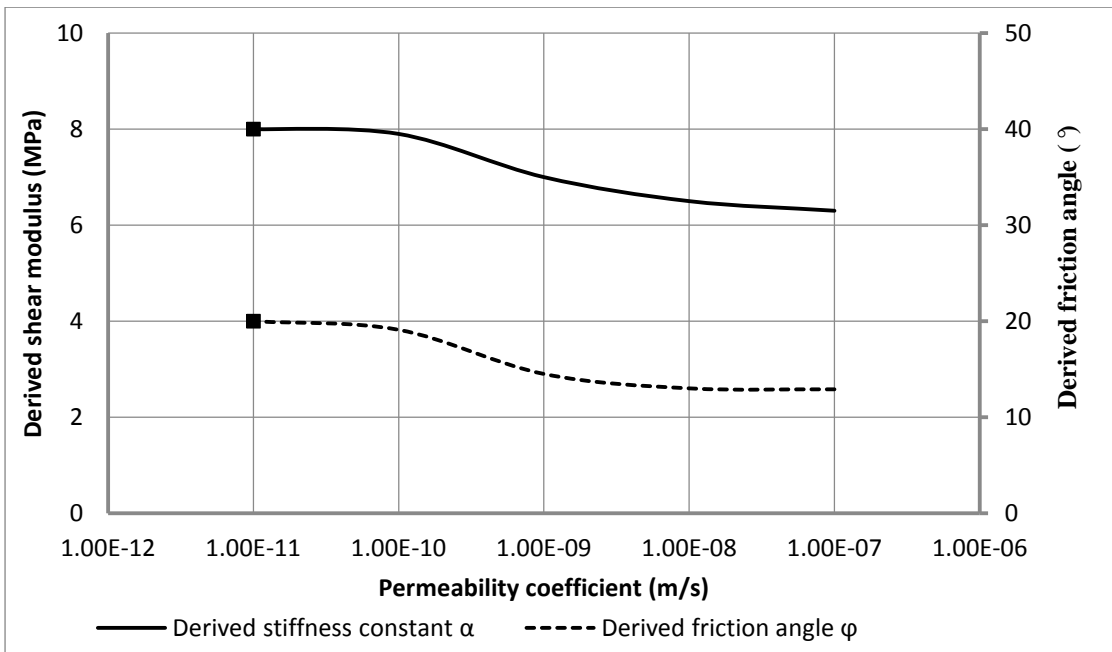
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Figure 11. Cavity expansion curve using consolidation analysis



537 Figure 12. Mohr circles at the cavity wall using consolidation analysis

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540 Figure 13. Effect of the permeability coefficient on soil stiffness and strength

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