# Optimisation and Simulation of RC Time Constants 

 in Snubber CircuitsSat Mohanram<br>Brunel University London<br>Electronic and Computer Engineering London, U.K.<br>SatyanandVidyaSagar@Brunel.ac.uk

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#### Abstract

Semiconductor devices are subjected to elevated levels of stresses when used at high voltage high current and temperature applications. This stress is mainly due to hard switching which is proportional to the switching frequency. This paper presents methods used to remove this energy to prevent expensive switch damage due to overheating and high dv/dt oscillations. In confirmation of the research title, the process in the determination of ' $R C$ ' in snubber circuits has been proven by OrCAD optimisation and presented.


Keywords- Hard Switching, Input-Output Parameters, Simulation, Snubber Circuit (RC), Switching Frequency, Losses, TC Optimizations.

## I. INTRODUCTION

In the design of converters, power supplies etc., it is necessary to select components with optimum characteristics to ensure switching devices function within their Safe Operating Area (SOA). Failing such selection, there are indirect losses to consider due to manufacturing down time [1] and cost [10] of equipment replacement.

In practice the RC time constant can be a fraction of the switching cycle period T , or related to the transient period ( $t_{\text {off }}$ ) of the switch at turn-off, which will allow the capacitor to charge (diverting the switch current) and discharge completely at turn-on [14] [15]. This energy if completely diverted to the capacitor will be equal to $1 / 2$ $\mathrm{CV}^{2}$ joules. Further analysis will be carried out to optimise the RC values for maximum transfer of the capacitor energy as heat dissipated in the resistor or transferred to the input for efficiency enhancement [3].

Methods to determine Time Constants are complex. Most articles recommend values based on experimental results (Rule of Thumb Method), by selecting the values of $R$ and $C$ that removes most of the switch energy at switch-off transition [4]. Other methods, employ simulation, algorithm tools and programs that require input parameters before the simulation begins[5].

Example of inputs are, initial values of $R$ and $C$, voltage across the switch, load current, switching frequency and switching losses. These inputs are fed into a "simulation black-box" with a choice of output target conditions, i.e. minimum switch loss, optimum values for $R$ and $C$ and ideal switching frequency. The initial values of $R$ and $C$ will be determined by using the basic Rule of Thumb method, which will test various RC time constants until a minimum switch loss is obtained. The output of this process will provide the optimum design parameters for the protection circuit (see Fig.1) [1][2][3][4][5]. The methods to determine RC time constants are posted in the block diagram of Fig. 2.

Determination of RC time constants at low frequency and high frequency applications will also be determined by simulation process. These results will enable correct design of over voltage protection circuits depending on the switching device selected and its operating frequency.

The RC time constants for the Turn-Off snubber circuits has been suggested to be a fraction of the switching device on/off period, i.e. T/2, T/3, T/5, T/10 and $\mathrm{T} / 13$, [6] [7] [8]. The requirement is that the capacitor must be charged during the switch off period and be discharged sufficiently during the switch on period, to be ready for the next off/on switching cycle. Other methods involve several simulations of the schematic circuit, with different values of $R$ and $C$ in the snubber circuit, until an optimum RC time constant is found. Fig. 2 provides some methods available involving critical circuit analysis [9]. In most Power Electronics research, the popular methods used are PSpice [11] and MATLAB. Due to the limited size of the paper set by UPEC, the description will focus on PSpice simulations.

## II. SWITCHING WAVEFORMS

Fig. 3, shows a standard voltage pulse switching waveform, which will be used to drive the MOSFET device in the test circuits to follow.

Fig. 4, shows a complete RC turn-off snubber circuit connected across the switching device. ESR (r1), is the capacitor Equivalent Series Resistance normally selected from the manufacturer's capacitor data sheet. During the turn-off transition, the capacitor via D2 and $\mathrm{r}_{1}$ is required to divert the switch current and reduce the switch terminal voltage, ideally to zero volts. At turn-on, $C, r_{1}$ and $R$ in the discharge circuit, dissipates the capacitor stored energy into R. It takes approximately five-time constants to fully charge a capacitor. However, the charge time of the capacitor will be determined by a fraction of the turn-off transition period (toff) as suggested above and is discussed in the next section.

## III. DETERMINATION OF SWITCHING DEVICE TURN-OFF PERIOD

## A. Manual determination of RC time constant for Snubber circuit using PSpice

Fig. 5, shows two Buck converter circuits. Circuit A with a MOSFET switch without a snubber circuit. Circuit $B$ with a MOSFET switch with a snubber circuit.

The first step in finding the RC time constant is to determine the transient switch off period (toff) of the switching device. A PSpice simulation of circuit A was therefore carried out and (toff) was measured in Fig. 6 to be $0.09 \mu \mathrm{~s}$. It was decided to choose a time constant of 20 ns to be within the (toff) period (i.e. $<0.09 \mu \mathrm{~s}$ ) [13].

After several simulation runs with combinations of C8 and R6, with fixed time constant of 20 ns , the final values of $\mathrm{C} 8=100 \mathrm{n}$ and $\mathrm{R} 6=0.2 \Omega$, were found. Voltage differential probes (green), current probe (red) and power probe (blue), required separate PSpice simulation runs. These simulations are shown in Fig. 6.

## B. Calculation of Switching Device Energy during toff

With no snubber circuit, switch energy during the switching period $t_{o f f}=\left(673 \mathrm{~W} \times 0.09 \times 10^{-6}\right) / 2$ Joules, (where VI = probe power value)

$$
=30.3 \mu \mathrm{~J}
$$

With snubber circuit, the switch energy is due to the
7.8 W during the period measured as 0.000025 ms

$$
\begin{aligned}
& =7.8 \mathrm{~W} \times 0.000025 \mathrm{~ms} / 2 \\
& =0.0975 \mu \mathrm{~J}
\end{aligned}
$$

Switch energy during $t_{\text {off }}=6 \mathrm{~W} \times 1.3 \mu \mathrm{~s} / 2$

$$
=3.9 \mu \mathrm{~J}
$$

The total energy, $\quad=0.0975 \mu \mathrm{~J}+3.9 \mu \mathrm{~J}=$ $3.9975 \mu \mathrm{~J}$
Reduction of switching energy,

$$
\begin{aligned}
& =(30.3-3.9975) / 30.3 \times 100 \\
& =86.8 \%
\end{aligned}
$$

The above PSpice simulation, has demonstrated that although time consuming due to running several simulations, can result in finding effective RC time constant for the Turn-Off snubber circuit, which in this case has reduced the MOSFET switching energy by 86.8\%

## C. Comparison of MOSFET Power level at turn-on and turn-off without protection

Fig. 7, shows, the voltage, current and power traces for two complete cycles of T $(100 \mu \mathrm{~s})$. The turn-on and turn-off periods, have equal mark/space ratio of $50 \mu \mathrm{~s}$. Due to load current, the MOSFET power at start of turnon, $(3.5 \mathrm{~kW})$ is much greater that the power at start of turn-off, ( 0.65 kW ) since the load current at turn-off is zero. The only power at turn-off is due to the di/dt decay and dv/dt rise across the switch (hard switching).

## D. Load Power to determine TURN-ON snubber time constant

i.e. Load power = turn-on power - turn-off power

$$
\begin{aligned}
& =(3.5-0.65) \mathrm{kW} \\
& =2.85 \mathrm{~kW}
\end{aligned}
$$

This load power will be useful when calculating the time constant for a Turn-On snubber circuit, whose function is to reduce the MOSFET in-rush current at turn-on. (Not included in this paper).

## E. Ratio of RC/Transient period toff

Determination of the above ratio, which was effective in the reduction of the switch energy to zero level.
The turn-off period, $\quad t_{\text {off }} \quad=0.09 \mu \mathrm{~s}$. In Figure 5 B, RC time constant, $\mathrm{T} \quad=0.2 \Omega \times 100 \mathrm{nF}$

$$
=20 \mathrm{~ns}
$$

The ratio of, $\quad \mathrm{T} / t_{\text {off }} \quad=\left(20 \times 10^{-9}\right) /\left(0.09 \times 10^{-6}\right)$

$$
=0.22
$$

Hence, RC time constant, $\quad=0.22 \times t_{\text {oft }} \approx$ $1 / 5 \times$ toff.
This result shows that by finding toff, without snubber protection, the value of the snubber circuit 'RC' time constant can be calculated as ( $1 / 5 \times t_{\text {off }}$ [12].
Ratio of RC/Turn-Off period T/2
In Figure 5 B, RC time constant, $\mathrm{T}=20 \mathrm{~ns}$
The turn-off period, $\quad \mathrm{T} / 2 \quad=50 \mu \mathrm{~s}$
The ratio of, T (Turn-off $)=\left(20 \times 10^{-9} \mathrm{~s}\right) /\left(50 \times 10^{-6} \mathrm{~s}\right)$

$$
\begin{aligned}
& =(1 / 2.5) \times 10^{-3} \mathrm{~s} \\
& =0.4 \times 10^{-3} \mathrm{~s}
\end{aligned}
$$

Hence, RC time constant, $\quad \mathrm{T}=0.4 \times 10^{-3} \times$ Turn-Off period
Knowing the device switching frequency (mark/space), the RC time constant t can be found from the above relationship.
Hence, the time constant of ( $C 8=100 \mathrm{n}$ \& R6 $=0.2 \Omega$ ) = 50 ns , can be determined by either the ratio of ( $1 / 5 \times t_{\text {off }}$ ) or
( $0.4 \times 10^{-3} \times$ Turn-Off period, $\mathrm{T} / 2$ ), which resulted in an effective reduction of the switch energy by the snubber circuit.

## IV. CALCULATION OF R AND C FOR SNUBBER CIRCUIT BY "AREA" METHOD

The RC product is in units of time and can conveniently be represented by the area of a rectangle as in Fig. 8 . The object is to find the minimum values of $R$ and $C$ for a given area " $A$ " in units of time.

The Steps in the procedure are: -
STEP

1. Area $A=C \times R$
2. Perimeter $P=2 C+2 R$

Reduce $P$ for minimum $A$,
3. Minimum $A=X$
4. $C \times R=X$
5. Substitute for $C=X / R$
6. (2) in (1) $\quad P=2(X / R)+2 R$

$$
\begin{equation*}
P=2 R+2 X R^{-1} \tag{3}
\end{equation*}
$$

7. and

$$
\begin{align*}
P^{\prime} & =2-2 X R^{-2} \\
& =\left(2 R^{2}-2 X\right) / R^{2} \tag{4}
\end{align*}
$$

There are two roots in (4), $\left(2 R^{2}-2 X\right)$ and $R^{2}$. The root in
$R^{2}=0$, which is not practical and is ignored. The critical value for $R$ is found in,

$$
\begin{equation*}
\text { 8. i.e. }\left(2 R^{2}-2 X\right)=0 \text {, and } R=\sqrt{ } x \tag{5}
\end{equation*}
$$

9. since $C \times R=X$, then $C=\sqrt{ } x$

## A. Confirmation of the Area method

The PSpice simulation of the circuit in Fig.5A, gives the ( $t_{\text {off }}$ ) period to be $0.09 \mu \mathrm{~s}$ and will be used to calculate $R$ and $C$ using the result in above method.

## Example

Let, C R = X $=0.09 \mu \mathrm{~s}$, (switch-off transition period, $t_{\text {off }}$ )
And from (5) and (6), C \& R $=\sqrt{x}$
Hence, $\quad C=0.3 \mu \mathrm{f}$, and $\mathrm{R}=0.3 \Omega$
The R and C component values were entered in the test Buck converter PSpice schematic in Fig.5B and simulated.
Fig. 9 shows the result of the PSpice simulation.
Since the period for the 10 W is negligible, the energy will be ignored. The energy in the MOSFET during the measured turn-off transition of $4 \mu \mathrm{~s}$ is,

$$
\begin{aligned}
& =4 \mu \mathrm{~s} \times 1 / 2 \times 2 \mathrm{~W} \\
& =4 \mu \mathrm{~J}
\end{aligned}
$$

From section III B, the MOSFET switching energy without snubber circuit was $30.3 \mu \mathrm{~J}$.

From this simulation, reduction of switching energy is,

$$
\begin{aligned}
& =\{(30.3-4) / 30.3\} \times 100 \\
& =\underline{86.8 \%}
\end{aligned}
$$

This is reduction of the MOSFET switching energy, compares exactly to the $86.8 \%$ reduction figure in section III B above. This calculation Area method confirms the $R$ and $C$ values were equally effective in reducing the switch power loss. By changing the $R$ and C to PARAMETER values with min/max ranges using PSpice Advance Analysis, the switch loss energy may be further reduced to the ideal zero value.

## V. CALCULATION OF R AND C BY PARAMETRIC ANALYSIS IN PSPICE

This section will determine the optimum value of the RC time constant of the Snubber Circuit, based on changing a component to a global parameter with a minimum and maximum range. There will be several PSpice simulations, depending on the number of increments in the parameter range [16]. The capacitor value was parametised and the resistor value randomly adjusted to $0.288 \Omega$ (to be less than the $0.3 \Omega$ in the Area example). In Fig.10, C11 was renamed as a variable capacitor\{Cval\}. C11 was swept from $0.2 \mu \mathrm{f}$ to $0.3 \mu \mathrm{f}$, with $0.02 \mu \mathrm{f}$ increments, resulting in six iterations. Fig. 11 and Fig. 12 are the iteration results, with a final value for $\mathrm{C}=$ $0.3 \mu \mathrm{f}$ corresponding to the minimum power of 5 W . The time constant of $R=0.288 \Omega$ and $C=0.3 \mu f=0.0864 \mu \mathrm{~s}$, is less than $t_{\text {off }}=0.09 \mu \mathrm{~s}$ in section A. In Fig.11, examination of the peak of each power trace corresponds to a time value on the time axis. Hence, toff $=0.09 \mu$ s will correspond to a peak power value of 2 W . Comparing the two power levels (2W \& 5W and corresponding times), PSpice analysis would indicate that for a minimum switch loss, the RC time constant must not be less than a switch transition period ( $t_{\text {off }}$ ) (when measured without snubber circuit connected). Further benefits could be expected if both $R$ and $C$ were simultaneously Paramatised.

## VI. CONCLUSIONS

In this paper, critical time constants were determined by three methods, calculations involving several iterations in PSpice simulation, minimisation of 'RC' time constant by an Area method and the 'Parameter' method of sweeping through a range of $C$ minimum to maximum values in PSpice analysis.
By limiting the value of the RC time constant within the transition switching period ( $t_{o f f}$ ), the switching device loss energy was reduced from a no protection level to 86.8\% with the snubber circuit connected. Further reduction of
the switch energy is possible by parametizing both R and C in the snubber circuit.

## References

[1] J. Hagerman, "Calculating Optimum Snubbers," Hagerman Technology, 24 July 1995. [Online].
[2] E. Lindell and L. Liljestrand, "Effect of Different Types of Overvoltage protection Devices Against Vacuum-Circuit-Breakers-Induced transients in Cable Systems," IEEE Transactions on Power Delivery, Vol.31, No.4. August 2016, vol. 31, no. 4, 2016.
[3] C. K. Huing, H. H. Nien, S. K. Changchien, C. H. Chan and C. K. Chen, "An Optimal Designed RCD Snubber For DC-DC Converters," in 10th International Conference on Control, Automation, Robotics and Vision, Hanoi, Vietnam, 2008.
[4] "Snubber Circuit Design Calculators," Daycounter, Inc. Engineering Services, 2016. [Online]. Available: Http://www.daycounter.com/Contact.phtml.
[5] Y. M. Chen, Thesis on RC Snubber design using Root-Loci Approach for Synchronous Buck SMPS, Ontario, Canada: University of Waterloo, 2005.
[6] L. Bartolomo, L. Abbatelli, M. Macauda, F. D. Giovanni, G. Catalisano, M. Ryzek and D. Kohout, "Wideband Gap Materials: Revolution in Automotive Power Electronics," in EVTeC and APE Japan on May 26, 2016 , Japan, 2016.
[7] A. Huang, "New cost-effective silicon carbide high voltage switch created," North Caroline State University, North Caroline , 2016.
[8] H. Dr. Stork, "ON Semiconductor - The Value and Supply Chain Impact of Wide BANdgap Substrate Materials," 13 July 2016. [Online].
[9] K. Bose, "Benefits in both Hard and Soft Switching Topologies," infineon, June 2016. [Online]. Available: http://www.infineon.com/coolmos.
[10] D. o. E. USA, "Wide Bandgap Power Electronics - Technology Assessment," USA, Department of Energy, 13 February 2015.

inPuT PARAMETERS

OUTPUT
[14] X.He, S. J. Finney, B. W. Williams and T. C. Green, "An Improved Passive Lossless Turn-On and Turn-Off Snubber," in IEEE, Edinburgh, 1993.
[15] R. T. Li, H. S.-H. Chung and A. K. Sung, "Passive Lossless Snubber For Boost PFC with Minimum Voltage and Current Stress," IEEE Transactions On Power Electronics, vol. 25, no. 3, pp. 602-613, March 2010.
[16] PSpice Advanced Analysis User Guide, Product Version 17.22016, San Jose, CA 15134, USA: Cadence Design Systems, Inc., 2016.
OUTPUT

Fig.1: Simplified RC Time Constant Simulation/Optimization process


Fig. 3: Switching Waveform


Fig. 4: Capacitor Charge and Discharge in RCD Snubber circuit



Figure 5-Buck Converter with a MOSFET switching device. Without snubber (top) and with snubber circuit connected (bottom)

Fig. 6-Waveforms for Buck Converter Top without snubber, bottom with snubber circuit


Fig. 7-Two cycles of V, I and P traces for Buck Converter without snubber circuit


Fig. 9-Simulation of Switch Energy reduction by AREA Method, showing the Voltage, Current and Power Traces


Fig. 10-Schematic to test the response of the snubber circuit on the MOSFET with a range of C11 from $0.2 \mu \mathrm{f}$ to $0.3 \mu \mathrm{f}$, with increments of $0.02 \mu$


Fig. $11-\mathrm{V}, \mathrm{I}$ and P traces (in groups of six) - Sweep
of the snubber capacitor, from $0.2 \mu \mathrm{f}$ to $0.3 \mu \mathrm{f}$ in steps of $0.02 \mu \mathrm{f}$, with R fixed at $0.288 \Omega$


Fig. 12-Magnified view of the Peak power area in the switch of Fig. 11

