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# Estimation of Multiple Inflows and Effective Channel by Assimilation of

<sup>2</sup> Multi-satellite Hydraulic Signatures: The Ungauged Anabranching Negro River

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# 21 Abstract

With the upcoming SWOT satellite mission, which should provide spatially dense river surface elevation, width 22 and slope observations globally, comes the opportunity to assimilate such data into hydrodynamic models, from the 23 reach scale to the hydrographic network scale. Based on the HiVDI (Hierarchical Variational Discharge Inversion) 24 modeling strategy (Larnier et al. [1]), this study tackles the forward and inverse modeling capabilities of distributed 25 channel parameters and multiple inflows (in the 1D Saint-Venant model) from multisatellite observations of river 26 surface. It is shown on synthetic cases that the estimation of both inflows and distributed channel parameters 27 (bathymetry-friction) is achievable with a minimum spatial observability between inflows as long as their hydraulic 28 signature is sampled. Next, a real case is studied: 871 km of the Negro river (Amazon basin) including complex 29 multichannel reaches, 21 tributaries and backwater controls from major confluences. An effective modeling approach 30 is proposed using (i) WS elevations from ENVISAT data and dense in situ GPS flow lines (Moreira [2]), (ii) average 31 river top widths from optical imagery (Pekel et al. [3]), (iii) upstream and lateral flows from the MGB large-scale 32 hydrological model (Paiva et al. [4]). The calibrated effective hydraulic model closely fits satellite altimetry obser-33 vations and presents real like spatial variabilities; flood wave propagation and water surface observation frequential 34 features are analyzed with identifiability maps following Brisset et al. [5]. Synthetic SWOT observations are generated from the simulated flowlines and allow to infer model parameters (436 effective bathymetry points, 17 friction 36

patches and 22 upstream and lateral hydrographs) given hydraulically coherent prior parameter values. Inferences 37 of channel parameters carried out on this fine hydraulic model applied at a large scale give satisfying results using 38 noisy SWOT-like data at reach scale. Inferences of spatially distributed temporal parameters (lateral inflows) give 39 satisfying results as well, with even relatively small scale hydrograph variations being inferred accurately on this 40 long reach. This study brings insights in: (i) the hydraulic visibility of multiple inflows hydrographs signature at 41 large scale with SWOT; (ii) the simultaneous identifiability of spatially distributed channel parameters and inflows 42 by assimilation of satellite altimetry data; (iii) the need for prior information; (iv) the need to further tailor and 43 scale network hydrodynamic models and assimilation methods to improve the fusion of multisource information and 44 potential information feedback to hydrological modules in integrated chains.

46 Keywords: 1D Saint-Venant Model, Hydrology couplings, Variational Assimilation, Satellite Altimetry, SWOT,

47 Hydraulic Visibility, Ungauged River

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#### 49 1. Introduction

Hydrographic networks represent major flowpaths for freshwater in the water cycle and an interface with the space of human societies. It is of prior importance in a context of climate change to improve the knowledge and representation of continental water fluxes, including river discharge, defined as an essential physical variable (see Global Climate Observing System [6, 7]). However, modeling flows structure in the different compartments of a catchment remains a hard task (see [8] and references therein) especially at poorly gauged locations. In complement of in situ sensors networks, which are declining in several regions (e.g. [9]), new generations of earth observation satellites and sensors provide increasingly accurate and dense measurements of water surface variabilities.

The Surface Water and Ocean Topography (SWOT) satellite, to be launched in 2021, will bring observations of water surface (WS) with an unprecedented spatio-temporal coverage [10, 11, 12, 13, 14]. This will yield greater hydraulic visibility (see definition in [15, 16, 17]) of hydrological responses through WS signatures from the local scale to the hydrographic network scale, hence an opportunity to better characterize hydrological fluxes and potentially constrain local to integrated hydrodynamic models and inverse problems. However, estimating river discharge Qfrom "geometric" observables of flow surface (elevation Z, width W and slope S) remains a difficult inverse problem particularly in case of poor knowledge on river bathymetry and friction (see [18, 1] and references therein).

Hydraulic inverse problems with various model complexities, data-unknowns types and amounts are investigated by recent studies in a satellite data context (see [13] for a review). A few studies started to test the benefit of assimilating (synthetic) SWOT WS observations with sequential methods in simplified hydraulic models, for estimating inflow discharge assuming known river friction and bathymetry [19, 20] or inferring bathymetry assuming known friction [21, 22]. Next, methods based on low-complexity models have been proposed for estimating river discharge from WS observables in case of unknown bathymetry b and friction K, based on the low Froude model [23, 18], hydraulic geometries [24] or empirical algebraic flow models [25]. The intercomparison of low complexity methods in [26] highlights the difficulty of estimating the so-called unknown triplet (Q, K, b) from WS observables as well as the importance of good prior guesses on the sought parameters.

The combined use of dynamic flow models of river systems and optimization methods enables to solve hydraulic 73 inverse problems, as shown for upstream flood hydrograph(s) estimation by [27] from WS width time series and a 74 1D Saint-Venant model or by [28, 29, 30] using variational assimilation of flow depth time series in a 2D shallow-75 water model. The variational data assimilation (VDA) approach (see e.g. [31] and references therein) is suitable to 76 address the present hydraulic inverse problem from WS observations (see [32, 5, 33, 34, 1] and references therein 77 single upstream hydrographs in all studies except multiple "stepwise" offtakes on synthetic and densely observed 78 irrigation-like cases in [32]). It consists in fitting the modeled flow features to observations through the optimization 79 of control parameters in a variational framework. To be solved efficiently, such an ill-posed inverse problem needs to 80 be regularized: see [35] for the theory of regularization of such inverse problems and [32, 1] for the present inverse 81 flow problem. 82

Crucial aspects of this difficult inverse problem are (i) the spatio-temporal sparsity of altimetric observations 83 regarding flow controls – as analyzed in [5] for inferable hydrographs frequencies with the introduction of the 84 *identifiability maps* and in [34] for inferable channel parameters patterns; (ii) the sensitivity of the triplet inference 85 to good prior guesses on the sought parameters as highlighted in a SWOT context by [18, 36, 1, 37, 34]. The latest is highlighted by recent discharge estimates (in a triplet setup) from synthetic SWOT data on the Pô, Garonne and 87 Sacramento Rivers in [1] (see also [38]), from AirSWOT airborne measurements on the Willamette River in [37] or 88 from ENVISAT altimetric data on an anabranching portion of the Xingu River [34]. Using a biased prior hydrograph 89 results in a biased estimate of inflow hydrograph despite a correct temporal variability at observation times - see 90 [1] for detailed analysis. A hierarchical modeling strategy HiVDI (Hierarchical Variational Discharge Inversion) is 91 proposed in [1] including low complexity flow relations (Low Froude and locally steady-state) for providing robust 92 prior guesses to the VDA process by taking advantage of databases or regional hydrological models. 93

Most studies mentioned above tackle the estimation of a single upstream inflow discharge hydrograph from WS observations on relatively short river reaches regarding the spatio-temporal sparsity of (satellite) observations sampling and without complex flow zones - confluences, multichannel portions (except [34]), floodplains. Moreover, few recent studies address the effective modeling of (ungauged) river channels using multisatellite data [15, 39, 34, 40].

The present study investigates the challenging inference of multiple inflows and channel parameters patterns from hydraulic signatures in a SWOT context. Particular attention is paid to the difficult inference of hydraulic controls (HC) with correlated effects on WS signatures including overlapping backwater effects. Moreover, we present an effective hydraulic modeling approach based on multi-satellite observations of WS and accounting for hydrological

model inputs. It is applied to a long river reach including confluences with tributaries and strong backwater effects 103 in the Amazon basin. The computational inverse method, based on the full 1D Saint-Venant equations, is that 104 presented in [5, 1] with a spatially distributed friction power law in water depth and a simple piecewise linear channel 105 bathymetry [34]. It is adapted here to account for lateral inflows/offtakes and is weakly coupled to the large scale 106 MGB hydrological model [41, 42, 43]. Numerical investigations of the resulting WS signatures and identifiability 107 tests are presented along with sensitivity analysis to the parameters of both the (forward) hydraulic model and the 108 inverse method. The challenging inference of multiple inflows and channel parameters patterns is investigated with 109 various observations densities including the assimilation of synthetic SWOT ones. 110

The paper is organized as follows. Section 2 presents the modeling approach with the 1D Saint-Venant flow model and the inverse computational method. Section 3 investigates the capabilities of the inverse method for identifying spatially distributed inflows with and without unknown channel parameters given observation patterns of WS signatures including overlapping backwater effects. Section 4 presents the effective modeling approach from multisatellite data applied to 871 km of the Negro river (Amazon basin) and the analysis of flow propagation features against SWOT observability. Section 5 proposes inference tests for spatially distributed inflows with and without unknown parameters on the Negro case in the presence of strong backwater effects.

## 118 2. Modeling Approach

#### 119 2.1. The flow model

The Saint-Venant equations ([44]) consist in the unidirectional form of the shallow water equations and are commonly used to describe open channel flows (see e.g. [45, 46, 47] for detailed assumptions including the long wave one). In what follows, x denotes the curvilinear abscissae from upstream to downstream along a reach of length  $\mathcal{L}$  (usual simplifying hypothesis are used) and  $t \in [0, T]$  denotes the time. In this representation, let A(x, t) be the flow cross sectional area [m<sup>2</sup>] and Q(x, t) the discharge [m<sup>3</sup>.s<sup>-1</sup>] such that U = Q/A represents the longitudinal cross-section averaged velocity [m.s<sup>-1</sup>]. The Saint-Venant equations in (A, Q) variables at a flow cross section read as follows:

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$$\begin{cases} \partial_t A + \partial_x Q = k_{lat} q_{lat} \\ \partial_t Q + \partial_x \left(\frac{Q^2}{A}\right) + g A \partial_x Z = -g A S_f + k_{lat} U q_{lat} \end{cases}$$
(1)

where Z(x,t) is the WS elevation [m] and Z = (b+h) with b(x) the river bed level [m] and h(x,t) the water depth [m],  $R_h(x,t) = A/P_h$  the hydraulic radius [m],  $P_h(x,t)$  the wetted perimeter [m], g is the gravity magnitude [m.s<sup>-2</sup>],  $q_{lat}(x,t)$  is the lineic lateral discharge [m<sup>2</sup>.s<sup>-1</sup>], and  $k_{lat}$  is a lateral discharge coefficient chosen equal to one here since we consider inflows only. In DassFlow, the friction term  $S_f$  is classically parameterized with the empirical Manning-Strickler law established for uniform flows:

$$S_f = \frac{|Q|Q}{K^2 S^2 R_b^{4/3}} \tag{2}$$

The Strickler friction coefficient  $K \left[ m^{1/3} \cdot s^{-1} \right]$  is defined as a power law in h:

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$$K(x, h(x, t)) = \alpha(x) h(x, t)^{\beta(x)}$$
(3)

where  $\alpha$  and  $\beta$  are spatially distributed parameters. This spatially distributed friction law enables a variation of friction effects in function of the flow state (see effective modeling of multichannel flows in [34]).

Inflow hydrographs  $Q_{in}(t)$  and  $q_{lat,l}(t)$  at  $l \in [1..L]$  are classically imposed respectively upstream of the river 137 domain and at known injection cells, that is inbetween two computational cross-sections along the river channel. 138 Let us recall the Froude number definition Fr = U/c comparing the average flow velocity U to pressure wave celerity 139  $c = \sqrt{\frac{gA}{W}}$  where W is the flow top width [m]. Considering subcritical flows (Fr < 1) in a satellite observability 140 context (see [18]), a boundary condition is imposed at the downstream end of the model using the Manning-Strickler 141 equation depending on the unknowns  $(A, Q, K)_{out}$ . The initial condition is set as the steady state backwater curve 142 profile  $Z_0(x) = Z(Q_{in}(t_0), q_{lat,1..L}(t_0))$  for hot-start. This 1D Saint-Venant model (eq. (1)) is discretized using 143 the classical implicit Preissmann scheme (see e.g. [48]) on a regular grid of spacing  $\Delta x$  using a double sweep 144 method enabling to deal with flow regimes changes,  $\Delta t$  is precised in numerical cases. This is implemented into the 145 computational software DassFlow [49]. 146

#### 147 2.2. The computational inverse method

The paper studies the estimation of spatially and temporally distributed flow controls from WS observables using the inverse method presented in [1] (see also [5]) with an augmented composite control vector c; the method is detailed in AppendixA. The principle of the inverse method is to estimate (discrete) flow controls by minimizing the discrepancy between observed and simulated flow lines,  $Z_{obs}$  and Z(c) respectively, the latter depending on the unknown parameters vector c through the hydrodynamic model (eq. (1)). This discrepancy is classically evaluated with the observation cost function term  $j_{obs}(c) = \frac{1}{2} ||(Z(c) - Z_{obs})||_{\mathcal{O}}^2$  computed on the observation spatial and temporal grids, see details in AppendixA.

The control vector c contains temporally and spatially distributed unknown "input parameters" of the 1D Saint-Venant model: a friction law ([34]) and lateral inflows, unlike in [1], where there is a spatially uniform friction law K(h) without lateral flows. It reads:

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$$c = \left(Q_{in}^{0}, ..., Q_{in}^{P}; Q_{lat,1}^{0}, ..., Q_{lat,1}^{P}, Q_{lat,2}^{0}, ..., Q_{lat,L}^{P}; b_{1}, ..., b_{I}; \alpha_{1}, ..., \alpha_{N}; \beta_{1}, ..., \beta_{N}\right)^{T}$$
(4)

where  $Q_{in}^p$  is the upstream discharge (the superscript  $p \in [0..P]$  denotes the observation time),  $Q_{lat,l}^p$  is the lateral discharges injected in the inflow cell  $l \in [1..L]$  (note that  $Q_{lat,l} = q_{lat,l}\Delta x$ ),  $b_i$  the river bed elevation ( $i \in [1..I]$ )

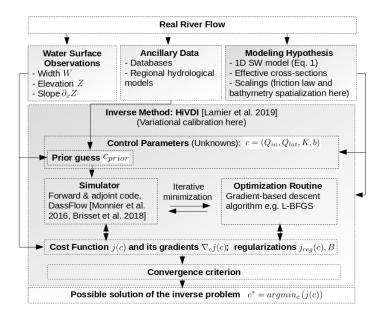


Figure 1: Flowchart of the method using the HiVDI inverse method [1] for variational calibration, adapted from [50, 51, 34].

denotes the computational cross section index in space) and, for each patch  $n \in [1..N]$  with  $N \leq I$ , the spatially distributed parameters  $\alpha_n$  and  $\beta_n$  of the friction law (eq. (3)) depending on the flow depth.

The inversion consists in solving the following minimization problem:  $c^* = \operatorname{argmin}_c j(c)$  starting from the socalled prior  $c_{prior}$  in the parameter space. This minimization problem is solved using a first order gradient-based algorithm, more precisely the classical L-BFGS quasi-Newton algorithm (see AppendixA). Note that the sought parameters have a correlated influence on the modeled flow lines, therefore leading to an ill-posed inverse problem. In order to be solved efficiently, the optimization problem is "regularized" as detailed in AppendixA. The main steps of the method are illustrated in Fig. 1.

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#### <sup>170</sup> 3. Inference capabilities from WS signatures: synthetic test cases

In order to calibrate the parameters of a hydraulic model (eq. (1)) from WS observables, one has to identify 171 and understand the influence of these parameters on the observable(s): in our case the WS profile. Fluvial flows 172 are studied here in the context of satellite altimetry (see [18]). Following [52], the influence of the parameters on 173 the modeled flow lines is referred to as their "hydraulic signature" (HC) and a reach is defined inbetween two fluvial 174 HCs. Fluvial HCs can be defined in steady state (see [52]) as "local maximal deviations of the flow depth from the 175 normal depth  $h_n$  (equilibrium), imposing the upstream variation of the water depth profile h(x) over the so-called 176 control length [53]". They can stem from a change in either the hydraulic resistance, cross-section shape, bottom 177 slope or total flow variation through lateral exchanges. 178

This section studies the influence of inflows on hydraulic signatures, the capabilities of the inverse method described above to infer multiple inflows and channel parameters (either spatially constant or not), with a focus on

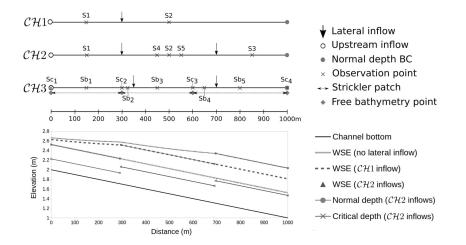


Figure 2: **TOP**: Academic test cases configurations. Rectangular channels of length  $\mathcal{L} = 1000 \text{ m}$  and constant cross section width W = 300 m, constant bottom slope of  $10^{-3} \text{ m/m}$  for Ch1, 2 and varying between  $10^{-4} and 10^{-2} \text{ m/m}$  for Ch3 - the bottom b(x) is defined by linear interpolation between the 4 bathymetry points (diamonds,  $b = \{2, 1.88, 1.28, 1.12\} \text{ m}$ ) - and friction defined by constant values on 3 patches ( $\alpha = \{30, 12.5, 30\} \text{ m}^{1/3} \text{ s}^{-1}$ ). Upstream inflow at x = 0; for Ch1, 2, 3 respectively lateral injections at abscissae (in m):  $x = 300, x = \{300, 700\}, x = \{350, 700\}$ , and observations at  $\{x_{S1}, ..., x_{S5}\} = \{150, 500, 850, 450, 550\}, \{x_{Sb1}, ..., x_{Sb5}\} = \{150, 325, 450, 600, 800\}, \{x_{Sc1}, ..., x_{Sc4}\} = \{0, 300, 600, 1000\}$ . **BOTTOM**: Sample waterlines with visible upstream and downstream controls and signatures. For the sake of clarity here, upstream and injected flow are set at  $100 \text{ m}^3 \text{ s}^{-1}$  (Fr ~ 0.12 - 0.3). Using the identifiability index  $I_{ident} = T_{wave}/\Delta t_{obs}$  introduced in [5] with  $T_{wave} = \mathcal{L}/c_k$  and the kinematic wave velocity for a rectangular channel  $c_k = 5/3U$  ( $c_k = 1.16 \text{ m.s}^{-1}$  considering average speed  $U = 0.69 \text{ m.s}^{-1}$ ) and a high observation frequency ( $\Delta t_{obs} = 20 \text{ s}$ ), gives a high identiability index  $I_{ident} = 43$  for the present flow observation configuration.

the influence of the spatial observability of those hydraulic signatures.

182 3.1. Test case design

Three test cases configurations representing typical hydraulic-observations setup of increasing complexities involving lateral inflows are presented (see Fig. 2). Cases Ch1 and Ch2 are designed to study the effect on the inference of the overlapping signatures triggered by the propagations of, respectively, one or two lateral hydrographs, concommitantly with the one of the upstream inflow hydrograph. Case Ch3 is a complexification of Ch2 through the introduction of a non-flat bottom and a variable friction pattern  $K = \alpha(x)$  as needed in a real river case in the next sections ( $\beta = 0$  in eq. (3) - see investigations on spatialized friction laws with multiscale bathymetry controls in [34]).

For all three channels the boundary conditions (fluvial) consist in: (i) a normal depth (equilibrium) imposed 190 downstream and (ii) sinusoidal hydrographs (see Tab. 1) imposed upstream and at lateral injection cells. The 191 simulation time step is set to  $\Delta t = 20$  s for all cases. They are set up as twin experiments, where a forward run 192 of the flow model (eq. (1)) is used to generate perfect WS elevation observations which are then used to infer 193 an unknown parameter vector c (eq. (4)) with the inverse method described in section 2.2 and AppendixA. The 194 inferences are started from erroneous prior guesses  $c^{(0)}$  that verify Manning-Strickler law for hydraulic consistency, 195 that is unbiased priors (see investigations in [1, 34]); hydrograph priors are constant values equal to the average 196 value of the target hydrographs. 197

Increasingly challenging inverse problems are considered, with increasing number of unknowns sought simultaneously and various observations densities. Cases Ch1 and Ch2 are used to infer temporal parameters only, given

Case	$Q_{in}$			$Q_{lat,1}$			$Q_{lat,2}$			Froude range								
Case	$Q_0$	$a_Q$	T	$Q_0$	$a_Q$	T	$Q_0$	$a_Q$	T	Floude range								
Ch1	100	0	6300	100	20	6300	-			0.13-0.29								
Ch2a				100	20	6300		100 20				100 20 6						0.12-0.3
Ch2b	1			400	80	6300					100 20			0.05-0.55				
Ch2c	100	20	6300	100	20	630			100 20	100 20			20 6300	20 6300	0.1-0.33			
Ch2d	1			100	20	6300				0.12-0.3								
Ch3	1			100	20	6300				0.09-0.53								

Table 1: Parameter values for sinusoidal hydrographs  $Q(x,t) = Q_0(x) + a_Q(x) \sin\left(\frac{2\pi}{T}t\right)$  used in synthetic channels; resulting modeled Froude ranges. Flows in m<sup>3</sup>s<sup>-1</sup>, time T in s.

a channel of constant slope and friction. Case Ch3 is the most challenging case with all inflows and non constant channel parameters sought simultaneously.

202 3.2. Informative content of hydraulic signatures: single/multiple inflows inferences

The fluvial signature from a single lateral inflow is divided in two parts (see Ch1 on Fig. 2, bottom): (i) in the 203 reach downstream of the injection point, the cumulative flow  $(Q = Q_{in} + Q_{lat,1})$  is uniform with a water depth 204 corresponding to the normal depth imposed downstream, (ii) in the reach upstream of the injection point an M1 205 backwater curve profile (see [54], [55, 52] in the present "altimetry context") is obtained given the upstream flow 206  $Q_{in}$  and the water depth imposed downstream of this reach as the normal depth corresponding to the cumulative 207 flow. In the case of two distinct lateral injections (Ch2), WS signatures overlap in the most upstream reach because 208 of the stronger backwater effect created by two downstream inflows, which represent a more challenging inference 209 problem. 210

Inference trials in case Ch1 with control vector  $c_1 = \left(Q_{lat,1}^0, ..., Q_{lat,1}^P\right)^T$ , assuming a known constant  $Q_{in}(x=0,t)$ , 211 show that a single observation point in space with a dense sampling in time, placed either upstream (S1, in Fig.212 2, top) or downstream (S2) from the lateral inflow, is sufficient to infer one lateral inflow hydrograph perfectly -213 noiseless twin experiments - (not presented). Indeed, the hydraulic signature of a lateral inflow is visible and fully 214 informative either upstream from it because of its downstream control on the upstream flow line or downstream 215 from it, in the signature of the cumulative flow. This means that as long the river is well temporally-observed 216 regarding its response time (see [5] without lateral inflows) and that the temporal variations of the observed system 217 stem from a single control, only one spatial point is needed to infer this parameter. 218

In the case of two distinct lateral injections (*Ch2*), WS signatures overlap in the most upstream reach because of the stronger backwater effect created downstream by the two inflows, which represents a more challenging inference problem considering the unknown control vector  $c_2 = \left(Q_{in}^0, ..., Q_{in}^P; Q_{lat,1}^0, ..., Q_{lat,1}^P, Q_{lat,2}^0, ..., Q_{lat,2}^P\right)^T$ . Several variants of *Ch2* are considered to study the possible misattibution of flow controls (locations, amplitudes and frequencies) in case of identical inflow hydrographs (*Ch2a*), the backwater influence of inflow hydrographs on  $Q_{in}$ downstream signature observed at *S*1 given 4 times larger inflow amplitude (*Ch2b*) or 10 times higher frequency (Ch2c), different observations samplings "mixed" inflows signatures (see Fig. 2 and Tab. 1).

226 3.2.1. Inference of multiple inflows

For all cases, using perfect and dense observations in space (1 every 10 m) and also in time leads to quasi perfect inferences. The influence of a sparser sampling and of the observability patterns of overlapping WS signatures on the identifiability of multiple inflows with the present inverse method is studied here - without a priori weighting of the parameters in the inverse method, that is equal and unadjusted  $\sigma_{\Box}$  values (see AppendixA). The inferred hydrographs are summed up in Fig. 3. Scores are given in Tab. 2, including cost function values and iterations number at convergence.

Variant Ch2a. Given only one observation station by reach (S1, S2, S3) very satisfying inferences of the 3 inflows are obtained (Fig. 3, red line). Hence sufficient information is provided by those three stations observing distinct signatures in each reach from upstream to downstream: (S1) propagation of the inflow  $Q_{in}(x = 0, t)$  in presence of the overlapping backwater effects due to  $Q_{lat,1}(x = 300, t)$  and  $Q_{lat,2}(x = 700, t)$ ; (S2) propagation of  $Q_{in}(x = 0, t) +$  $Q_{lat,1}(x = 300, t)$  in presence of the overlapping backwater effect due to  $Q_{lat,2}(x = 700, t)$ ; (S3) the propagation of the total discharge without downstream control.

Variant Ch2b. Assimilation is more difficult than in Ch2a but inferred hydrographs (Fig. 3, red line) are still accurate (Tab. 2). This testifies to the ability to discriminate multiple sources of various amplitudes given observations
of hydraulic signatures at higher frequency and at pertinent locations (S1, S2 and S3).

Interestingly, this case highlights the expected misattribution behaviour between inflow sources as shown by an intermediate iteration (Fig. 3, orange line) and remaining to a lesser extent at convergence (red line):  $Q_{in}$  and  $Q_{lat,1}$  are respectively over- and underestimated). This may be due to the relatively higher contribution of  $Q_{in}$  to the observed signature (it impacts WS elevation at S1, S2 and S3) and consequently its contribution in the cost function (observation part).

Note that the final overestimation of  $Q_{in}$  in Ch2b is slightly greater than in Ch2a. This is likely due to greater WS elevation variation at S1 caused by backwater from  $Q_{lat,1}$ , which is first attributed to  $Q_{in}$  since it has more impact on the cost function. Remember that, with perfect observations of WS signatures, at the end of the optimization process, nearly perfect hydrographs are inferred. However, the small flow misattributions during this optimization shows the difficulty of inferring multiple controls using an observation located in a strong backwater signal.

Variant Ch2c. Perfect inferences are obtained. An intermediate iteration (Fig. 3, orange line) shows that the expected misattribution of frequencies for all 3 inflows is present, though it disappears at convergence (Fig. 3, red line). This testifies to the ability to discriminate multiple sources of various frequencies given observations of hydraulic signatures at higher frequency and at pertinent locations (S1, S2 and S3).

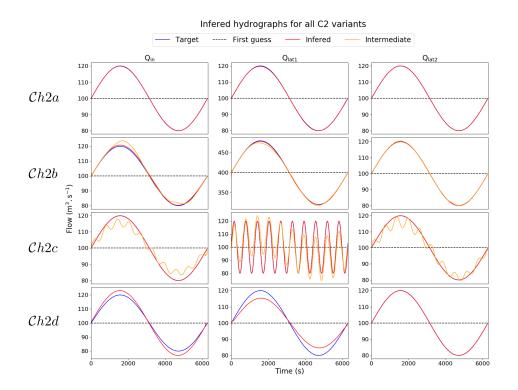


Figure 3: Inflows inferences from WS observations for all Ch2 variants. Intermediate iteration in the assimilation process are represented for Ch2b and Ch2c; they are hand-picked to illustrate "intermediate" behaviours before convergence ("inferred").

Variant Ch2d. Convergence is achieved but the flow upstream of S4 is misattributed between  $Q_{in}$  and  $Q_{lat,1}$ . Signatures of  $Q_{in}$  and  $Q_{lat,1}$  are only observed mixed, downstream of  $Q_{lat,1}$  (at S4 and S5) and downstream from both  $Q_{lat,1}$  and  $Q_{lat,2}$  (at S3). Given that all stations are located in the downstream infuence of both inflows, the distribution of flow between them makes little difference on the observed WS dynamics. This confirms the need to have at least one observation station between each sought inflow in order to be able to "separate" them.

Case		$Q_{in}$		$Q_{lat,1}$		$Q_{lat,2}$	Cost	N <sub>ite</sub>
Case	RMSE	rRMSE (×10 <sup>-6</sup> )	RMSE	rRMSE (×10 <sup>-6</sup> )	RMSE	rRMSE (×10 <sup>-6</sup> )	COSt	1 vite
Ch2a	0.08	2.5	0.15	4.7	0.05	1.6	$8.0 \times 10^{-6}$	54
Ch2b	0.72	22.9	1.34	10.6	0.08	2.7	$9.4 \times 10^{-6}$	261
Ch2c	0.06	1.9	0.27	8.7	0.04	1.3	$7.7 \times 10^{-6}$	78
Ch2d	2.21	70.0	3.31	105.0	0.03	0.9	$7.9 \times 10^{-6}$	24

Table 2: Inferred parameters misfits to the truth for Ch2 variants. The RMSE  $[m^3s^{-1}]$  and rRMSE represent the misfit of the inferred parameters, while the cost function used in the assimilation process represents the misfit of variables.

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} \left( Q_{target}^{i} - Q_{infered}^{i} \right)^{2}, rRMSE = RMSE / \sum_{i=1}^{n} Q_{target}^{i}}$$

#### 261 3.2.2. Synthesis

These first tests showed that for inferring multiple inflows, i.e. spatially distributed temporal controls, a minimal 262 spatial observability of their WS signature is required with one observation point between each inflow here. In case of 263 observation stations affected by backwater influence, the potential difficulty of separating multiple inflows from their 264 "mixed signature" is highlighted; using a higher spatial density of (simultaneous) observations leads to improved 265 inferences in the present configuration. Moreover, using observations with high temporal density (with regards to 266 the response time in the considered river system) and low spatial density, different frequencies can be correctly 267 attributed to multiple inflows (as highlighted for a single upstream inflow in [5]). Furthermore, note that if a 268 supercritical regime occurs in a reach between inflows, their hydraulic signatures are disconnected (not shown), 269 effectively reducing the assimilation problem to that of case Ch1. 270

## 271 3.3. Multiple and composite controls inference

In this section multiple inflows are sought simultaneously with channel parameters on case Ch3. Three friction 272 patches are consistently applied to sub-reaches inbetween the 4 sought bathymetry points. The control vector 273 is  $c_3 = \left(Q_{in}^0, ..., Q_{in}^P; Q_{lat,1}^0, ..., Q_{lat,1}^P, Q_{lat,2}^0, ..., Q_{lat,2}^P; b_1, b_2, b_2, b_4; \alpha_1, \alpha_2, \alpha_3\right)^T$ . Searching both inflows and 274 channel parameters creates a configuration (intendedly) prone to equifinality problems on the sought parameters 275 having correlated influence in the water surface signal. Three observation configurations (see Fig. 2) are studied: 276 one with a high station density (Ch3a: 100 stations, 1 every 10 m), another with fewer stations (Ch3b: 9 stations, 277  $Sb_{1..5}$  and  $Sc_{1..4}$ ) and a third one with even fewer stations (*Ch3c*: 4 stations,  $Sc_{1..4}$ ). Priors for inflows are those 278 defined for case  $Ch_2$  (subsection 3.2.1), priors for channel parameter are hydraulically consistent with flow priors and 279 initial flow line. For this equifinality prone configuration, the  $\sigma_{\Box}$  values used in the inverse problem regularization, 280 related to the sought parameters (see section AppendixA) and denoted as weights, are given in Tab. 3. 281

Inference results are presented in Fig. 4. In red, the final estimate of  $c_3$  for Ch3a with the "default" weights set 282 (see Tab. 3). In green, final inferences for variant-specific parameter weights adjusted through trial and error. In 283 orange, intermediate inferences with the "default" set of parameter weights. Equal values of 1, corresponding to "no weighting", were also tested: they lead to inaccurate inferences (not shown) and thus the "default" weights producing 285 more interpretable results are preferred. In further iterations, after the ones plotted in orange, behaviours similar 286 to the Ch3a "default" weights inferences (Fig. 4, in red) appear (not shown), i.e. a shift of inferred hydrographs 287 and Strickler coefficients away from the target. Also note that the inferred flow oscillation in the first time step 288 stems from the influence of the initialization scheme (see section 2.1) in the optimization on this quickly responding 289 channel. 290

 $Q_{in}$  is underestimated while the local friction is overestimated, denoting a local tendency to equifinality. This is linked to a strong backwater influence, created by both  $Q_{lat,1}$  and the increase in friction at x = 300 m. This

Case	Case		$\sigma_{Q_{lat,1}} \left( \mathrm{m}^{3} \mathrm{s}^{-1} \right)$	$\sigma_{Q_{lat,2}} \left( \mathrm{m}^{3} \mathrm{s}^{-1} \right)$	$\sigma_{\alpha} \left( \mathbf{m}^{1/3} \mathbf{s}^{-1} \right)$	$\sigma_{b}\left(\mathbf{m}\right)$	Cost	$N_{ite}$
	Ch3a					2	0.54	180
"Default"	Ch3b	- 50	50	50	600		0.54	97
	Ch3c						0.63	54
	Ch3a		30	30	400	2	0.23	156
"Adjusted"	Ch3b	1	0.9	1.2	300		0.25	108
	Ch3c	1	0.9	1.2	500		0.26	100

Table 3: Parameter weight sets in Ch3 variants.

local inflow error leads to compensation in downstream hydrographs. By adjusting parameter weights through trial and error, accurate inferences are obtained (Fig. 4, in green). This means that dense observations of the WS elevation are not sufficient for inferring all flow controls contained in  $c_3$  and that spatially distributed regularization parameters, acting as weights in the parameter search, are required.

297

Variant Ch3b and Ch3c. With sparses observations, the "default" weight set leads to worse inferences. However, 298 the existence of a set of adjusted weights that lead to good inferences (Fig. 4, in green) is enough to show that the 299 minimum observation spatial density of 1 station between each inflow can be sufficient to infer the extended control 300 vector  $c_3$ . Note that adjusted weight for Ch3b and Ch3c are different from adjusted weights for Ch3a (see Tab. 3). 301 Using less observation points in space, the influence of spatial parameters decreases without loss of meaningful 302 information and thus the relative influence of inflows increases. This simple test highlights the weighting influence 303 of the  $\sigma_{\Box}$  parameters in the regularization method in the present flow configuration. The spatial distribution and 304 density of WS observations along with the weights change the hydraulic representativity of spatially distributed 305 parameters in the optimization process. 306

The main difficulty uncovered with these academic cases is the challenge presented by simultaneous inferences of multiple inflows and channel parameters from their potentially overlapping hydraulic signatures. However, in the case of unbiased prior parameters and dense WS observation patterns relatively to those of spatio-temporal controls, satisfying inferences are obtained with the present inverse method. A real and complex river case is considered hereafter.

## 312 4. Effective hydraulic model of the Negro river

After addressing increasingly challenging hydraulic inverse problems on synthetic test cases in the previous section, a real complex river flow case is now considered. It consists in 871 km of the Negro river, including several confluences with tributaries and anabranching flow zones. The reach is located upstream of the Solimoes-Negro

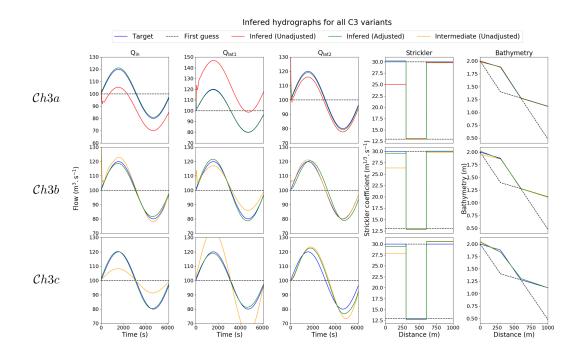


Figure 4: Inflow, bathymetry and friction patch inferences from WS observations for all Ch3 variants. In red, final inference with "default" parameter weights (see Tab. 3). In green, final inference with adjusted parameter weights. In orange, intermediate inferences with "default" parameter weights.

confluence which is responsible for significant backwater effects (see e.g. [52]). This section presents the elaboration
of effective flow models in view of performing forward and inverse flow modeling from WS observations of varying
sparsity in the next section.

The modeling approach consists in (i) a 1D hydraulic model (full Saint-Venant equations, see subsection 2.1) (ii) based on effective cross sections defined from multisatellite and in situ data and (iii) weakly coupled to the large scale hydrological model MGB [41, 42, 43]. The idea is to build an effective river flow model both in coherence with the main hydrological signals (inflows) propagations along with observable flow surface signatures and hydraulic controls (see [52]). As shown in what follows, this 1D approach allows for a fair representation of flow propagation and longitudinal signatures, which are the core focus of this paper.

325 4.1. Study zone

The study domain corresponds to the main stream of the Negro River, a major "left-bank" Amazon tributary 326 draining the north part of the basin, with an average discharge of  $28400 \,\mathrm{m^3.s^{-1}}$  [56]. The reach covers the 871 km 327 upstream of its confluence with the Solimoes and presents singular channel morphologies such as multichannel flow 328 zones mainly located in two large grabens ([57]). Part of the reach is strongly influenced by the control imposed 329 by the Solimoes river at its confluence (average discharge of  $100\,819\,\mathrm{m}^3.\mathrm{s}^{-1}$  according to ORE HYBAM gauge data 330 [58], their confluence gives birth to the Amazon river). This hydraulic control is due to higher discharge and a 331 consequently lower slope of the Negro River in its lower reach when compared to the Solimões River near to the 332 confluence [59, 60]. The reach of interest has been crosscut by 18 ENVISAT ground tracks every 35 days from 2003 333

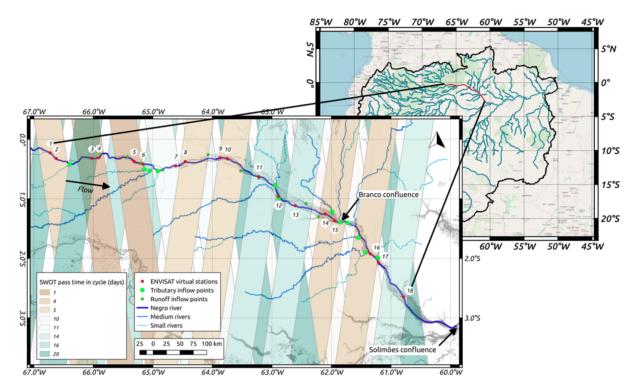


Figure 5: Study zone on the Negro river. ENVISAT Virtual Stations are numbered from 1 to 18 starting from upstream. The boundaries of the studied reach are defined by stations 1 and 18. The 21 tributaries are divided between actual rivers and inflow points from the hydrological model. SWOT swaths give an almost full spatial coverage of the reach. In gray is the average water extent map used to extract width values, from [3].

to 2010 (see [61]), representing 68 to 79 measurements of WS elevations at each of the 18 Virtual Stations (VS).

<sup>335</sup> Note that the measurements are not simultaneous for each station.

336 4.2. Effective models construction

This section presents the elaboration of effective flow models from multisatellite data. First, a  $\mathcal{G}1$  "sparse" channel geometry is built from effective bottom elevations at ENVISAT VS resolution. Next, in view to test the additional constraints brought by spatially dense satellite data (synthetic SWOT), a more spatially detailled effective channel geometry  $\mathcal{G}2$  is built using a high resolution water mask and an in situ flow line as explained below.

341 4.2.1. Effective geometry G1 from altimetry and optical data

An effective 1D channel with effective rectangular cross sections is set up from available multisatellite data (altimetry, optical) and a large scale hydrological model following [15, 34]. According to [57], high width to depth ratios make the rectangular channel a pertinent effective modeling approach of the true geometry, even in highly anastomosed reaches - where an error on the actual hydraulic perimeter  $P_h$  hence  $R_h$  (see subsection 2.1) is expected. This is supported by a qualitative analysis of some additional ADCP measurements of river flow and cross-sectional bathymetry.

• The river centerline from [62], formed by 30×30 m pixels, is used to calculate the river length and to project all spatial objects, such as VS, widths and inflow points, on a single one-dimensional reference. • A longitudinal profile of cross sectional WS width W is calculated from the average river extent map derived from 31 years (1984-2015) of optic landsat imagery by [3]. A single width value per centerline point is extracted in order to build a 1D rectangular geometry. For multi-channel reaches, the effective width is the sum of the widths of all channels. This underestimates the actual hydraulic perimeter. Specific hand-filtering based on hydraulical expertise was necessary in some anabranching parts of the model where the water extent may include inactive flow zones not accounted for in the present 1D effective model. Note that [63] concurs to the necessity of reach-scale flow zone evaluation in the Amazon river catchment.

• An effective channel bottom elevation  $b_{env}$  is obtained at each VS (Fig. 6, in red) from altimetric rating curves (RC) from [64]. Its slopes range from  $-7.1 \times 10^{-5}$  to  $2.0 \times 10^{-4}$  m/m with an average of  $7.0 \times 10^{-5}$  m/m. RCs were obtained by adjusting the parameters  $(\gamma, \delta)$  of a stage discharge relationship  $Q = \gamma (Z_{sat} - b)^{\delta} S_{sat}^{0.5}$ using WS elevations  $Z_{sat}$  and slopes  $S_{sat}$  gained by satellite altimetry and discharge Q simulated with the large scale hydrological model MGB ([41, 42, 43]) on the temporal window of interest.

Effective rectangular cross sections geometries are defined at the R = 18 VS using the above defined effective bottom elevations  $\{b_{env}\}_{r \in [1..R]}$  and river widths  $\{W_1\}_{r \in [1..R]}$ . The final model geometry  $(\mathcal{G}1 = \{b_{env}, W_1\}_{r \in [1..R]})$ is obtained by linear interpolation between those 18 effective cross sections on the model grid with  $\Delta x = 200$  m.

#### 365 4.2.2. Effective geometry G2 at increased spatial resolution

Spatially dense WS elevation data is introduced in the form of an in situ GPS flow line with G = 579 spatial points. It was collected by survey ship along the whole studied reach over 7 days during the low-flow period in december 2010 ([2]); it provides local WS elevations Z every 1.4 km on average and WS slopes S for every 25 km reach (ranging between  $2.0 \times 10^{-5}$  and  $8.11 \times 10^{-5}$  m/m, averaging at  $3.4 \times 10^{-5}$  m/m). Under the hypothesis of a wide rectangular cross section and a steady uniform flow, the Manning equation writes:

$$Q = K \left(Wh\right)^{5/3} \left(W + 2h\right)^{-2/3} \sqrt{S} \tag{5}$$

The water depth writes h = (Z - b) and the bottom elevation is sought using (i) the fixed WS width pattern 371  $W_2$  from imagery, (ii) the WS elevation  $Z_{GPS}$  and slope  $S_{GPS}$  given by the GPS profile and (iii) the discharge Q 372 from the hydrological model (see subsection 4.1) on the river domain at the corresponding time  $t_*$ . We invert an 373 effective bathymetry  $b_{GPS}$  using equation 5 by minimizing the square sum of misfits to  $b_{env}$  at ENVISAT stations 374 through the modification of M = 14 friction values  $((\alpha_m, \beta_m = 0), m \in [1..M],$  friction law eq. (3)). They are 375 simply spatialized into M "hydraulic" patches consistent with large scale morphological features classified as follows: 376 single channels, multiple channels (from 2 to 3), lightly anastomosed and heavily anastomosed (Fig. 6, in purple). 377 The friction coefficient values are coherent with the physical properties of the classified reaches. 378

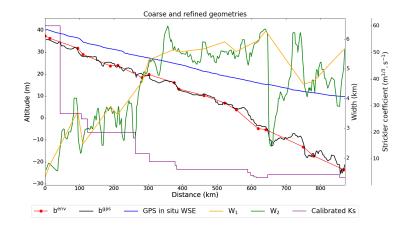


Figure 6: Effective river channel bottom and width for spatially sparse,  $\mathcal{G}1 = \{b_{env}, W_1\}_{r \in [1..R]}$ , and spatially dense,  $\mathcal{G}2 = \{b_{GPS}, W_2\}_{G \in [1..G]}$ , model geometries along with a low-flow GPS waterline from [2].

The new bathymetry  $b_{GPS}$  is coherent with the best available reference data and its corresponding set of physically distributed Strickler patches. The final model geometry is  $\mathcal{G}2 = \{b_{GPS}, W_2\}_{G \in [1,.G]}$ .

In the following, using either geometry  $\mathcal{G}1$  or  $\mathcal{G}2$ , the hydraulic model is inflowed with time series at a daily time step upstream of the river domain and at 21 tributaries (both river tributaries and runoff inflows) corresponding to the 21 catchment cells feeding into the Negro river cells in the large scale hydrological model MGB ([42, 41]). The largest of these tributaries is the Branco river at 657 km.

#### 385 4.3. Effective Models calibration against altimetry

The friction of the hydraulic model (eq. (1)) is calibrated against altimetric WS elevation time series following 386 [34], i.e.  $\{Z_{s,p}^{obs}\}_{S=16,P\in[68..79]}^{env}$  at ENVISAT VS, the most downstream VS being used as BC (see subsection 2.1). 387 The friction law is distributed using N = 17 "ENVISAT" patches with constant  $(\alpha_n, \beta_n = 0), n \in [1..N]$  values for 388 each reach between two successive VS. This choice is made to avoid spatial "overparameterization" in the calibration 389 process regarding the spatial sparsity of ENVISAT observations of WS signatures. The aim of parameter calibration 390 is to obtain a "real-like" model as close as possible of the sparse observation set. Three models are considered, to 391 assess the impact of the bathymetry refinement and of the downstream BC on the modeled hydraulic signatures and 392 on inverse problems: a "sparse" model (M1) using channel geometry  $\mathcal{G}1$  and the WS elevation time series from VS 393 18 as BC, a refined model (M2a) with channel geometry  $\mathcal{G}^2$  including all the spatial variability from multisource 394 data described above while keeping the same BC and a further changed refined model (M2b) where the BC is 395 changed to an altimetric RC which is of interest for "operational-like" applications in other rivers and basins. 396

The inverse method presented in [1] and described in subsection 2.2 and AppendixA is used here, without regularization terms, for friction calibration. Effective Strickler patches, starting from priors corresponding to average values of the "hydraulic" patches used above (Fig. 6, in purple), are calibrated following [34] who use observations of the same nature. Friction patterns  $c_{g1}^*$ ,  $c_{g2a}^*$  and  $c_{g2b}^*$  found with the inverse method are shown in Fig. 7. Most differences in calibrated friction from M1 (Fig. 7, in red) to M2a (Fig. 7, in blue) correspond to their

#### Strickler coefficient inferences with ENVISAT observations

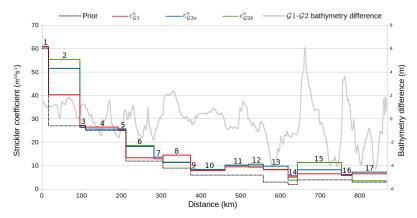


Figure 7: Friction patches after calibration against ENVISAT WS elevation observations. Inferred Strickler coefficient values are very close for all configurations for patches 1, 3 to 5, 9 to 14 and 16. Patches 2, 6 and 15 are especially sensitive to model variations.

difference in bathymetry at the virtual station point (Fig. 7, gray line), i.e. a lower slope in M2a leads to a higher inferred Strickler parameter in order to match WS observations (e.g. in patch 2 and 6. Inferred parameters for M2b roughly match those of M2a, with some discrepancies in patch 2, 15 and 17. Using a different BC influences WS sensitivity to parameters and the relative contribution to the cost function of local WS misfits, which explains differences in patch 15 and 17; the one in patch 2 stems for the high friction values, hence lower WS sensitivity as analyzed after.

#### 408 4.3.1. Water levels analysis

The following presents a detailed analysis of the effective hydraulic model for configuration M1, along with an analysis of changes obtained for configurations M2a and M2b.

The simulated WS elevation are compared to observed WS elevation at each ENVISAT virtual station in Fig. 411 8 - other time series are available in AppendixB. For the 3 models calibrated above, the modeled WS are fairly 412 close to observed WS given the limited modeling complexity and data uncertainties. More precisely, the fit to the 413 altimetric WS elevation time series is fairly good, as shown for M1 in Fig. 8, and nearly unbiased as shown in Fig. 414 9(left). The WS elevation global RMSE is at 0.936 m for M1; similar results are found with M2a (see Tab. 4). 415 Errors are greater in low and high flows, with consistent underestimations of flow amplitude upstream (VS 1-4) 416 which turns into overestimation downstream (VS 9 - 13), before disappearing closer to the BC (VS 14 - 18). VS 417 5 to 8 are particularly accurate. Error metrics are coherent with those from current state of the art models using 418 satellite data (see e.g. [40] on the Congo river). 419

The analysis of the time series for M1 gives insight on the 1D model behaviour regarding the real flow physics sampled with the sparse nadir altimetry data and dense in situ low flow line. Modeling errors can stem from either an (expected) improper representation of the channel and flow complexity or uncertain (ungauged) inflows and data.

424 Concerning the hydraulics, from downstream to upstream, relative errors are lower in anabranching reaches

outside of the backwater influence starting at the Branco tributary (x = 657 km up to around x = 350 km) and in the backwater influence of the (known "perfect") downstream BC. Overall, relative errors are higher upstream, in single channeled, low water height reaches and in the Branco backwater influences. Note that 2D complex lateral flows in floodplains or retention behaviours from "igarape" rivers may happen in high flow periods (see [65, 66]). These unaccounted phenomenons may decrease flood wave velocities and cause hydrograph skewness ([67, 68, 10]). The 1D modeling of water levels compared to altimetry observations (Fig. 8) can first be analyzed as follows:

Stations 14 to 18 are located in reaches with different morphological properties. Stations 14 and 15 are located
in a densely anastomosed reach upstream of the Branco river confluence, a major tributary. Stations 16 and
17 are in single channel reaches, upstream from the confluence with the Solimoes river. Station 18 is in a
densely anastomosed reach at the location of the BC forcing on WS elevation. Their low relative misfits do
not testify to the absence of complex hydraulic behaviours in this area but rather to the dominating influence
of the BC.

- Stations 5 to 13 are located in mostly homogeneous anastomosed reaches, with stations 5 to 8 in a less 437 densely anastomosed region than stations 9 to 13. This spatial division corresponds to two trends in relative 438 misfit, where lower misfit is seen in the less anastomosed reaches. This testifies to the difficulty of modeling 439 potentially 2D hydrodynamics using 1D approach. Indeed, the more channels there are, the further away 440 the simulated wetted perimeter is from the true wetted perimeter (and so the hydraulic radius). Note that 441 parameterizing the Strickler coefficient as described in eq.(3) and including  $\beta(x)$  in the control vector during 442 the calibration process, instead of the simpler  $\beta(x) = 0$  used here, does not yield a better fit in this complex 443 case modeled with a single rectangular channel. 444
- Stations 1 to 4 are located on single channel reaches. Although the area seems the most suitable to be modeled 445 in 1D, it still has the highest relative misfit to ENVISAT observations. For stations 1 and 2, this is partly 446 due to effective width estimation errors being more prevalent in the relatively narrow channel (around 2 km 447 in width). Furthermore, note that effective channel bottom elevation for these stations are respectively 37.3 m 448 and 36.3 m while the lowest ENVISAT WS elevation observation are respectively 36.6 m and 35.8 m. This 449 corresponds to low-flow water heights of 0.7 m and 0.5 m which do not fit field measurements. Consequently, 450 relatively high friction coefficients are inferred between station pairs 1-2 and 2-3 to fit low water depth. This 451 misfit might be due to data error, including effective width errors for stations 3 and 4 located in areas of sharp 452 width variations. Note that the higher the friction values, the less sensitivity of the modeled WS elevation, 453 which explains the highest spread of Strickler coefficient (K = 40 to  $55 \,\mathrm{m}^{1/3}\mathrm{s}^{-1}$ ) in reach 2 found during 454 calibration for the 3 models (Fig. 7). 455

	Global RMSE (m)	Global Average bias (m)	Upstream RMSE (m)	Upstream Average bias (m)
M1	0.94	-0.02	0.88	-0.08
M2a	0.94	-0.02	0.91	-0.01
M2b	1.72	0.23	0.90	-0.05

Table 4: RMSE and bias over 8 years for the M1, M2a and M2b models. Upstream metrics are calculated for stations 1 to 9 only, which are outside of the BC's backwater influence. The high global RMSE for M2b comes from the known dephasing of the Solimoes and Negro peak flow, which is not reproduced by the RC.

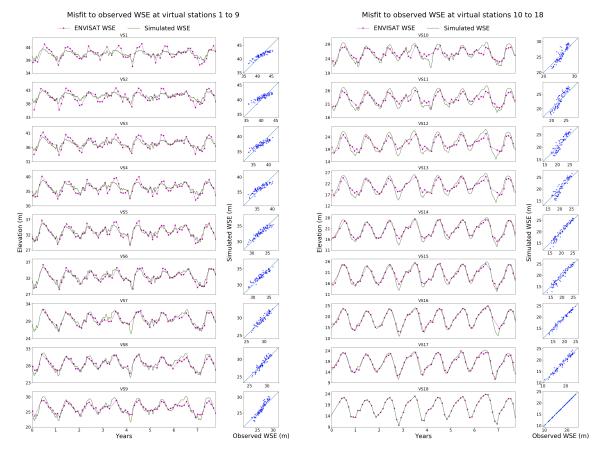


Figure 8: Modeled and observed WS elevation at ENVISAT VS after friction calibration at all stations for M1

The introduction of the refined geometry  $\mathcal{G}2$  in M2a, recall for generating spatially distributed SWOT data and to perform inference tests hereafter, has low impact on WS elevation bias and errors at ENVISAT VS (see Fig. 9), with only stations 1, 2 and 3 showing significant change. Using a rating curve as downstream BC in M2b mostly impacts the downstream part of the model where some misfit to altimetry data appears. Indeed, it is more difficult, using a simple power law depending on the local flow variables, to capture the influence of the confluence with the Solimoes River - not modeled. The latest having strong discharge variations out of phase with the one of the Negro River itself (e.g. [16]).

### 463 4.3.2. Effective model analysis

As a preliminary to hydraulic parameters inference from WS observables, this subsection studies the spatiotemporal features of the simulated hydraulic signatures, their sensitivity to model parameters and their observability

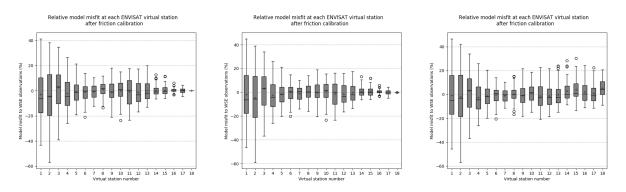


Figure 9: Relative misfit between modeled and observed WS elevation at ENVISAT for M1 (left, base model) M2a (middle, WS elevation at downstream BC) and M2b (right, rating curve at downstream BC). Crosses are average values, horizontal bars are median values.

given a SWOT sampling. First, an analysis of a flood wave propagation, resulting from multiple inflows, and its hydraulic signature visibility is performed using identifiability maps following [5]. The latter consist in a spacetime representation of the WS signal and flow propagation features against the observability pattern. These maps, inspired by the theory of characteristics (see [69, 47]), enable to read how the sought upstream discharge information is sampled in the downstream WS deformations and help to estimate inferable hydrograph frequencies. Next, a numerical sensitivity evaluation of the flow model is carried out.

In the context of regional hydrological modeling including river networks representation, the sensitivity of the present flow model is studied by using erroneous inputs. These inputs are also used in section 5 as erroneous priors for various assimilation setups.

- Inflow: two hydrograph sets (containing lateral inflows and the upstream BC inflow) corresponding respectively to 70% and 130% of the true hydrographs are used as erroneous values for sensitivity trials and are referred to as  $Q_{FG}^{-30}$  and  $Q_{FG}^{+30}$  respectively.
- Friction: two Strickler repartitions, with coefficient values worth respectively 70% and 130% of the truth are used as erroneous values for sensitivity and are referred to as  $K_{FG}^{-30}$  and  $K_{FG}^{+30}$  respectively.

• Bathymetry: the inflow sets  $Q_{FG}^{-30}$  and  $Q_{FG}^{+30}$  and the true Strickler values are used to dig two bathymetries as described in section 4.3. The bathymetry derived from underestimated flows is referred to as  $b_{FG}^{-30}$  (it overestimates the true bathymetry), and the other is referred to as  $b_{FG}^{+30}$ .

SWOT will provide spatially distributed observations with interesting revisit frequencies at the scales of the current river domain and hydrological signal propagations. Fig. 10 shows the evolution of the simulated WS elevation anomaly during the yearly peak flow (red-blue heatmap) as well as its multiple SWOT observability (in black). Based on the modeled flow, accounting for several inflows, the propagation of an intumescence corresponding to the annual flood wave signature is represented along the river through the maximum WS elevation in time

(following [55]) (Fig. 10, top, blue points). This intumescence propagation is visible on the upstream 400 km of the 488 river from day 164 to day 173. It is detected by a SWOT swath at t = 166 d and another one at t = 170 d. It is more 489 difficult to detect this signature in the downstream part of the river (x > 400 km) affected by the strong downstream 490 control imposed by high water depths at the Negro-Solimoes confluence; a downstream control due to the Branco 491 tributary also overlaps from  $x = 657 \,\mathrm{km}$  to around  $x = 400 \,\mathrm{km}$ . This control can be seen through the tracked WS 492 elevation maximum (Fig. 10, top, in gray), where an early rise in WS elevation originates from x = 657 km, and 493 through the extreme waterlines (Fig. 10, bottom, in blue), which highlights the change in length of this influence in 494 low and high flows. As a consequence, WS observations on the downstream part may contain combined information 495 due to the upstream hydrographs propagation but also to the expression of downstream controls. 496

The maximum WS elevation is tracked for simulations with erroneous parameters as defined above (Fig. 10, top, in red, green and cyan). They are not plotted where the flow displays "pool behaviour" (gray points). They highlight the sensitivity of propagation to model parameters which is also an important point when they are varied during an optimization process as featured in section 5. The propagation time from 0 to 400 km can be evaluated to around 10 days, and is estimated as follows for the rest of the river domain.

The conservative part of the Saint-Venant equations (i.e. without source terms) is hyperbolic: some quantities 502 depending on the water depth and velocity (known as the Riemann invariants) are transported by waves at speeds 503 different from the flow speed (see e.g. [69, 47]). The wave celerities are U + c and U - c with  $c = \sqrt{gh}$  for rectangular 504 cross sections (see analysis of propagation features in [5]). For the fluxial regime of interest here (Fr = U/c < 1), information propagates both downstream and upstream and the Riemann invariants are modified along the wave 506 due to the source term effects. The wave celerities obtained on the Negro River model are given by reach in Table 507 5, relatively high wave speeds are obtained hence propagation of information both upstream and downstream, 508 with spatio-temporal variability. The WS signature (and the discharge) thus reflects the nonlinear combination of 509 information coming from both upstream (due to inflows variations) and downstream (due to local hydraulic controls 510 or downstream BC - see the method of characteristic in [47]). This highlights the difficulty of inferring multiple 511 inflows from sparse observations of WS signature, especially given uncertain channel parameters and backwater 512 effects. 513

Nevertheless interesting frequential information can be gained from the identifiability map as introduced in 514 the case of a single inflow. Using the kinematic wave speed  $\frac{5}{2}U$  (Fig. 10, top, dashed blue line) which compares 515 fairly well to the intumescence speed on the upstream part of the reach (Fig. 10, top,  $x < 400 \,\mathrm{km}$ ). This gives 516 an approximate propagation time  $T_{wave} = 26 \,\mathrm{d}$  on the whole domain, greater than the SWOT observation cycle 517 period of 21 days. This brings the reach identifiability index to  $I_{ident} = 1.23$  (defined as  $I_{ident} = T_{wave}/\Delta t_{obs}$ , i.e. 518 the average number of time a wave is observed, see [5]). However, in the present case, the notion defined by [5]519 accounts for a single upstream inflow, not spatially distributed lateral inflows with potential upstream backwater 520 controls. Actual identifiability indices for reaches in between each lateral inflow would be much lower (estimated 521

x (km)	0 65	121	163	193	216	388	418	465	502	528	598	623	628	657	700	739	754	789	1000
$\frac{5}{3} \overline{u}_{HF}$	2.35	1.42	1.22	1.07	1.02	0.75	0.50	0.52	0.53	0.50	0.48	0.35	0.32	0.41	0.61	0.47	0.44	0.47	0.44
$^{c}HF$	8.32	9.23	9.71	10.31	10.36	11.19	12.52	12.61	12.62	13.49	13.95	15.90	16.28	16.82	17.93	17.26	17.56	19.37	19.69
$u_{HF} + c_{HF}$	9.74	10.08	10.44	10.95	10.97	11.64	12.82	12.92	12.93	13.79	14.23	16.11	16.47	17.06	18.29	17.54	17.82	19.65	19.95
$u_{HF} - c_{HF}$	-6.92	-8.38	-8.98	-9.67	-9.75	-10.73	-12.22	-12.29	-12.30	-13.19	-13.66	-15.68	-16.09	-16.57	-17.56	-16.99	-17.29	-19.09	-19.42
$I_{ident,HF}$	0.32	0.46	0.40	0.33	0.26	2.64	0.69	1.04	0.81	0.60	1.69	0.82	0.18	0.82	0.81	0.97	0.39	0.86	2.14
$\frac{5}{3} \bar{u}_{LF}$	1.40	0.96	0.83	0.70	0.69	0.52	0.34	0.37	0.45	0.40	0.41	0.25	0.22	0.26	0.31	0.26	0.24	0.24	0.23
$c_{LF}$	5.54	6.16	6.54	7.13	7.05	7.72	8.70	8.59	7.87	8.71	8.81	11.30	11.83	12.54	14.11	13.37	13.78	16.09	16.59
$u_{LF} + c_{LF}$	6.38	6.74	7.04	7.54	7.47	8.03	8.91	8.81	8.14	8.94	9.06	11.45	11.96	12.70	14.30	13.52	13.93	16.24	16.72
$u_{LF} - c_{LF}$	-4.70	-5.58	-6.04	-6.71	-6.64	-7.40	-8.50	-8.37	-7.60	-8.47	-8.56	-11.15	-11.70	-12.39	-13.93	-13.22	-13.64	-15.95	-16.45
$I_{ident,LF}$	0.54	0.67	0.58	0.50	0.39	3.80	1.03	1.47	0.95	0.76	1.97	1.16	0.26	1.29	1.61	1.76	0.73	1.71	4.21

Table 5: Identifiability indexes between each pair of inflow at low and high flow (see Fig. 10, bottom). Speeds are given in m.s<sup>-1</sup>.  $I_{ident}$  is given for a reach of length L and an observation time step  $\Delta t_{obs} = 1 \text{ d by } I_{ident} = \frac{L}{\frac{5}{3}\bar{u}\Delta t_{obs}}$ .

identifiabilities in between each inflow pair are given in Tab. 5 considering a fictious  $\Delta t_{obs} = 1 \,\mathrm{d}$  full domain observability). Furthermore, SWOT swaths observations consist in WS snapshots on different parts of the river domain at given times, hence containing various and mixed signatures (in the sense introduced in section 3) of both several inflows and channel parameters - the more downstream, the more aggregated is the inflow information. Inferences of multiple inflows and frequential analysis are presented in the next section given known or uncertain channel parameters, spatio-temporally dense or sparse (SWOT) observations.

528

#### 529 5. Inferences from satellite observables

This section studies the challenging inference of ungauged channel parameters and multiple inflows on the Negro 530 River case, which represents a real and complex large scale problem. Typical inverse problems in hydrological-531 hydraulic modeling are studied here considering SWOT WS observations. The inference of channel parameters 532 or/and inflows in the 1D Saint-Venant model is addressed using the inverse method presented in subsection 2.2 (see 533 also section AppendixA). The downstream BC is set as a known altimetric rating curve. Three observation sets 534 are generated: spatially and temporally dense ( $\Delta t = 600 \,\mathrm{s}$ ) observations (DenseSet), SWOT observations from the 535 hydraulic model outputs masked by SWOT swaths (SWOTSet) and noisy SWOT observations using the large scale 536 simulator [70] to add realistic measurement noise (SWOTNoiseSet). We first present inferences of inflows only, then 537 of channel parameters, and finally of all those spatio-temporal controls simultaneously. 538

539

#### 540 5.1. Multiple hydrographs inferences

Depicting flow structure within a river network and a catchment is a key issue in hydrological modeling, especially in ungauged basins. Seeking to infer, from distributed WS observations, flow controls that are both temporally and spatially distributed can represent a very challenging inverse problem, as previously highlighted on synthetic cases.

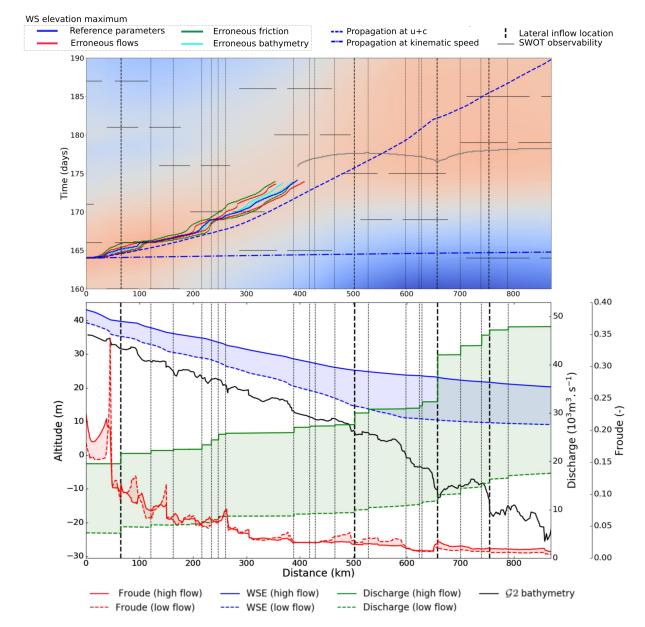


Figure 10: **TOP**: Identifiability maps and flood wave propagation during the yearly peak flow (may-june) in the Negro river model. The WS anomaly (heatmap) is given by  $Z_{ano}(x,t) = Z(x,t) - \overline{Z(x)}$ , where  $\overline{Z(x)}$  is the average local WS elevation from day 160 to 190. Blue points: tracking of maximum WS elevation value  $Z_m(x) = \max_{t \in [0,365]} Z(x,t), \forall x \in [0, L]$ . Gray points: tracking of maximum WSE in the downstream pool. Dashed blue lines: fictitious trajectory at kinematic speed (sparse dashes)  $c_k = 5/3U$  and at U + c (dotted dashes), starting at x = 0, at the time of the local WS elevation peak. The speeds are calculated from the simulated flow speed U and water height h and updated every  $\Delta x = 200 \text{ m}$ , such as  $t^{p+1} = t^p + \frac{\Delta x}{c_k^p}$ . **BOTTOM:** Extreme flow forcings and flow model variables over a 2 year period. Blue lines: Extreme simulated waterlines. Red lines: corresponding extreme Froude values. Green lines: corresponding cumulative injected flows.

Vertical black dashes are lateral inflow locations. Bold vertical dashes are inflows inferred in subsection 5.2.

Inferences of L = 21 inflow hydrographs from 2 years of SWOT synthetic observations are studied here. The channel geometry, friction and BCs are assumed to be known, hence the control vector reduced to  $c = (Q_{lat,1}^0, ..., Q_{lat,1}^P, Q_{lat,2}^0, ..., Q_{lat,L}^P)^T$ . The inferences are started from a prior guess  $c^{(0)}$  consisting in true hydrographs affected by uncertainties of  $\pm 30\%$ , that is  $Q_{FG}^{+30}$  and  $Q_{FG}^{-30}$  as defined above. Note that the inference is started from a hydraulically consistent initial state using an unbiased prior in the first time steps (see investigations in [1, 34]); the prior values of regularization parameters  $\sigma_{Qlat}$  correspond to inflows magnitudes.

The inferred hydrographs from inflow prior  $Q_{FG}^{-30}$  are presented in Fig. 11 for DenseSet (green lines) and 550 SWOTNoiseSet observations (orange lines). Results from prior  $Q_{FG}^{+30}$  are available in AppendixC. SWOTSet and 551 SWOTNoiseSet give almost identical inferences, therefore only the SWOTNoiseSet inferences are presented. For 552 under- and overestimated priors, the assimilation of dense and SWOT observations enables to infer the true hy-553 drographs fairly well. RMSE ranges from  $8.86 \,\mathrm{m^3 s^{-1}}$  at  $x = 465 \,\mathrm{km}$  up to  $578.31 \,\mathrm{m^3 s^{-1}}$  for the Branco tributary 554 at  $x = 657 \,\mathrm{km}$ . RMSE for all inferences presented in Fig. 11 can be found in section AppendixC. Some inferences 555 show global under- or overestimations (e.g.  $x = 216, 388, 789 \,\mathrm{km}$ ). These biases are linked to the prior bias. Strong 556 and numerous overlapping backwater signals may also influence flow misattribution, as discussed in the academic 557 cases (section 3) for a small scale model. As tested in numerical experiments (not shown), increasing a scalar value 558  $\sigma_{Q_{lat,l}}$  can give more effective weight to an hydrograph  $Q_{lat,l}$  in the inference and it can be found further away from 559 its prior guess, which highlights the role of the covariance matrix used for regularization. 560

Note that temporal oscillations appear on the inferred hydrographs when using SWOTNoiseSet which is "temporally sparse" observation patterns compared to flow propagation, which is not the case of DenseSet. These oscillations are especially present in downstream inflows, which may link them to particular hydraulic responses in the BC influence zone, although they can be seen in upstream inflows as well. They tend to be prevalent in declining limbs of hydrographs (e.g. in Fig. 11, at 789 km, from day 120 to 300).

Note that, regardless of oscillations, inferences tend to be further from the truth in decreasing hydrographs. These oscillations are not the effect of signal misattribution, as they are present with any number of inferred hydrographs (not shown), nor are they caused by the prior's shape, as filtered priors also lead to oscillations (not shown). Instead, the oscillations seems to stem from the combination of the low observation frequency compared to the spatially distributed inflow hydrographs and the nonlinear hydraulic response. Keep in mind that we track flow information through WS elevation deformations caused by the nonlinear propagation of parameter signatures (see subsection 4.3.2).

A sample illustration of those oscillations on the simulated WS elevation is presented in Fig. 12, at 870 km, downstream for three oscillating inferred hydrographs (at x = 738, 754 and 789 km). The inferred waterline from SWOTNoiseSet is compared to the truth at all simulated times and at SWOT pass times only. The misfit is logically lowest at SWOT pass times (goal of the optimization), while unobserved periods exhibit a slightly oscillating (unconstrained) misfit. Higher frequency observations, such as DenseSet, prevent this behaviours through a more

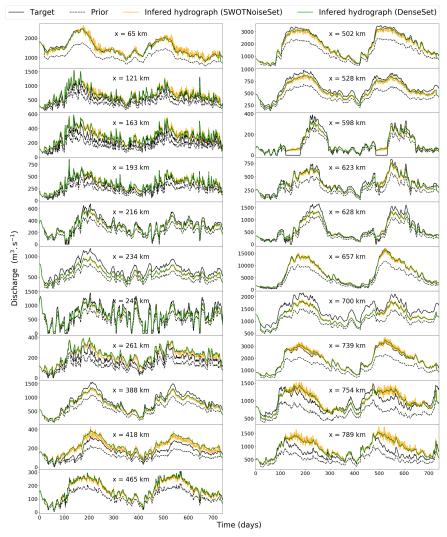
complete spatio-temporal observability of the WS signatures, hence constrain the spatio-temporal parameters in-578 ference further. Some model configurations where temporal parameters are discretized at a greater time step than 579 observation one do no exhibit such behaviours (e.g. results with DenseSet, [34]). As already shown in [5] for the 580 identification of a single hydrograph, the identification is possible only in time windows representing the wave prop-581 agation time  $T_{wave} \sim 26$  days in the present case, yet with multiple inflows and observation sample (see subsection 582 4.3.2). As a consequence, outside the "identifiable time windows", the infered values are not necessarily representing 583 reality (see related WS misfit in Fig. 12). They are the optimal solution corresponding to the considered priors 584 of the optimization problem. In practice, this means that introducing an additional regularization term  $j_{reg}$ , like 585  $\int_{0}^{t} \frac{\partial^{2} h}{\partial t^{2}} dt$  at observation points, would smooth (as following a spline curve) between the identifiable windows instead 586 of the obtained oscillations. This smooth discharge curve would not be more physical than the present oscillations 587 and we made the choice to not hide this well understood phenomena. It is a logical consequence of the disparity 588 between the samplings of observations and parameters and does not impede interpretations of hydraulic signatures 589 and identifiability. 590

Seeking to infer a control that is both temporally and spatially distributed represents a challenging assimilation 591 problem. In the present case: (i) the observation frequency now plays a role in identifying the hydraulic signa-592 ture, on top of its spatial density and resulting flow propagation: (ii) varying nonlinear flow propagation, and so 593 WS signatures, can result in different inferences depending whether they are performed from observations of ris-594 ing/declining hydrographs propagations (local Q(Z) hysteresis) and (iii) indirect contributions to parameter weight in the inverse method appear, as successive hydrographs influence the whole downstream water line (established in 596 subsection 3.2), which gives greater "effective weight" to upstream hydrographs as the cause of the misfit is observed 597 in more stations and thus accounted for multiple times in the cost function. The inferred flow variations may be 598 compensating for errors made at upstream stations with different SWOT pass times, impacting their WS elevation 599 either through backwater control or through the modification of the BC and its own backwater effect. 600

601

#### 5.1.1. Spatial parameters inference

The inference of effective channel parameters is studied here considering a control vector composed of all friction 603 coefficient values and bathymetry points. The bathymetry is composed of I = 436 free points (1 every 2000 m) 604 between each of which it is obtained by linear interpolation. SWOTSet is used, with a spatial observations sampling 605 (1 point every 200 m), i.e. 10 times greater than the sought bathymetry for observed reaches. Two inferences from 606 hydraulically consistent priors are presented, one with the refined bathymetry  $b_{FG}^{-30}$  introduced in subsection 4.3.2 607 (Fig. 13, in green) and another one with  $b_{env}^{+2.6m}$ , a shifted bathymetry from the M1 model in subsection 4.2.1, 608 in red. The 2.6 m correspond to the spatially averaged shift of  $b_{FG}^{-30}$  compared to  $b_{env}$ .  $b_{env}^{+2.6m}$  does not contain a 609 priori information on target bathymetry shape - such as a coarse DEM prior. The friction prior is  $K_{FG}^{-30}$  for both 610 inferences. 611



Infered lateral hydrographs (iteration 19)

Figure 11: Lateral hydrographs inferences from SWOTNoiseSet and DenseSet, using the  $Q_{FG}^{-30}$  inflow prior .

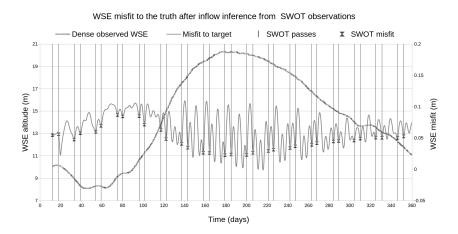


Figure 12: Difference between target and inferred WS elevation at 870 km, as observed by DenseSet and SWOTSet. The dotted line represents the inferred waterline inferred from SWOTSet (with  $Q_{FG}^{-30}$  as inflow prior), but observed by DenseSet. The difference between this waterline and the target waterline is the misfit to target. At SWOT pass times, the misfit is low as expected from an inference from SWOTSet. It only displays WS elevation oscillations at unobserved times.

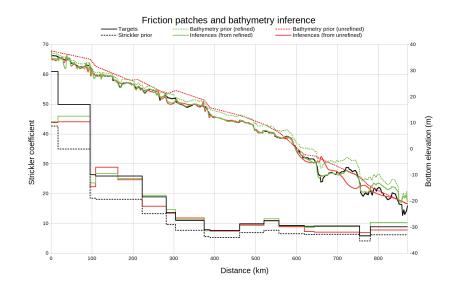


Figure 13: Bathymetry and friction pattern inferences from SWOTSet

Using  $b_{FG}^{-30}$  and  $b_{env}^{+2.6m}$  as priors, the inference of channel parameters (friction and bathymetry) respectively 612 reach a RMSE of  $(4.362 \text{ m}^{1/3} \text{s}^{-1}, 1.231 \text{ m})$  and  $(4.762 \text{ m}^{1/3} \text{s}^{-1}, 1.913 \text{ m})$ . Upstream (x = 0 - 110 km), irregularities 613 appear in both inferred bathymetries and correspond to underestimated Strickler coefficients. The high friction 614 partially hides the hydraulic signature of the bathymetry and enables inference error inconsequential to the cost 615 function. Downstream ( $x = 600 - 870 \,\mathrm{km}$ ), in the strong backwater control of the downstream BC, inferences tend 616 to stay close to their prior values. Furthermore, inferences from the unrefined prior  $b_{env}^{+2.6m}$  are smoother than those 617 from the refined prior  $b_{FG}^{-30}$ . This testifies to the role of the a priori bathymetry shape knowledge contained in the 618 prior when the WS elevation sensitivity to bathymetry is low. Strong backwater effects make the inference of channel 619 parameters more difficult and parameter compensation appears due to the lessened sensitivity of the simulated WS 620 (e.g. in green, at the last friction patch). The refined bathymetry prior  $b_{FG}^{-30}$  leads to inferred bathymetry and 621 friction that are closer to the truth. It will be used in the extended control vector inferences below. 622

623

## 624 5.2. Inference of channel parameters and inflows

This section investigates the simultaneous inference of both unknown inflows and channel parameters on the large scale Negro River case; it combines all previously mentioned difficulties and corresponds to an ungauged configuration. In the following, the aim is to determine: 1) if SWOT data are sufficient to infer the extended control vector given unbiased prior parameters; 2) how the added spatial complexity from lateral inflows impacts spatial parameter inference. In addition, further investigations on the impact of lateral inflow prior shape, representing for example hydrological modeling uncertainty in a simple manner, are presented. The considered extended control vector is the following:

$$c_{ext} = (Q_{lat,x=65}(t), Q_{lat,x=502}(t), Q_{lat,x=657}(t), Q_{lat,x=754}(t); b_1, ..., b_H; \alpha_1, ..., \alpha_N)$$
(6)

The inferences are performed from DenseSet and SWOTNoiseSet. The bathymetry and friction priors are  $b_{FG}^{-30}$ 632 and  $K_{FG}^{-30}$  respectively. Four major lateral inflows located at x = 65, 502, 657 and 754 km (Fig. 10, bold dashed 633 bars) are considered. Their reduced number facilitates the analysis of their spatial impacts. The other inflows are 634 set to their target values. Two inflows prior types are used:  $Q_{FG}^{flat}$ , that gives no a priori on hydrograph shapes 635 and  $Q_{FG}^{filter}$ , hydrographs obtained by applying a 80 days moving average filter to the true hydrographs. Prior 636 flow values in  $Q_{FG}^{flat}$  are set to the target flow values from the first time step up to 120 days for the sake of initial 637 hydraulic consistency. Inferences of all parameters for these inflow priors are presented in Fig. 14 and Fig. 15. The 638 inferred control vectors are referred to as  $c_{flat}^*$  and  $c_{filter}^*$ . Inferred parameter scores can be found in Tab. 6. 639

Inferred spatial parameters patterns are similar to those obtained previously without unknown inflows in subsection 5.1.1.  $c_{flat}^*$  features a fair bathymetry fit downstream ( $x = 600 - 870 \,\mathrm{km}$ ) while  $c_{filter}^*$  stays close to the prior value. This may be due to the different range of the simulated hydraulic responses in the first iterations: using  $Q_{FG}^{flat}$  leads to an increase in WS elevation sensibility to bathymetry. Upstream ( $x = 0 - 110 \,\mathrm{km}$ ), increased bathymetry irregularities in  $c_{flat}^*$  are linked to the erroneous prior  $Q_{FG}^{flat}$  leading to bathymetry errors in the first iterations, coupled with lower inferred Strickler coefficients, hence a lessened impact of bathymetry on the water surface and the inability to correct the "initial" errors.

In terms of temporal behaviours, both priors give fair estimates of hydraulic controls for DenseSet. Inferences 647 from SWOTNoiseSet are close to those from DenseSet with the presence of oscillations and the rising part of 648 hydrographs are better fitted than decreasing ones, as observed in subsection 5.1. In both  $c_{filter}^*$  and  $c_{flat}^*$  and for both observation sets, a correlation between sought inflows at x = 502; 657 and 754 km appears. The Branco 650 river flow, at x = 657 km, is better inferred and its well fitted peaks are also found in the two smaller rivers (e.g. 651 at 520 days), which are in its upstream and downstream influences zones (see Fig. 10, left). In all inferences, the 652 total flow at the downstream BC closely matches that of the truth, which means that only hydraulic signature is 653 misattributed across the 4 inferred temporal parameters, not on the total flow. In  $c_{filter}^*$ , more accurate inferences 654 are obtained, with a smaller influence of the Branco river on other influence in the influence zone and more accurate 655 inference of small scale behaviours. The filtered prior  $Q_{FG}^{filter}$  introduces information on low frequency behaviours 656 of the sought inflows, helping the assimilation process to converge to correct the target inflows. This configuration 657 allows for a better fit of small scale variation in the controls.

659

#### 660 6. Conclusion

This paper investigated the inference of river channel parameters and multiple inflows from water surface signatures in the context of satellite altimetry with the forthcoming SWOT mission and using water extents from optical data as well. The HiVDI inverse method presented in [1], based on the 1D Saint-Venant equations and a variational assimilation scheme adapted to account for lateral inflows (mass and momentum injections). Given hydraulically consistent prior guesses and regularization weights, it is successfully applied to synthetic test cases and a long reach

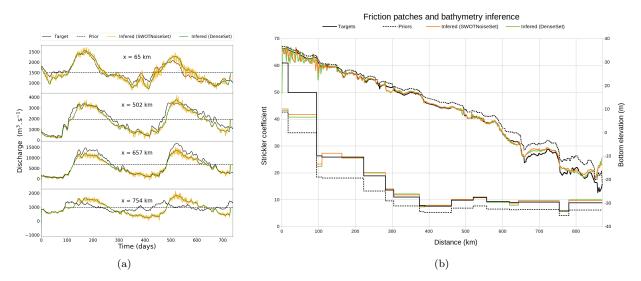


Figure 14: Inflow, bathymetry and friction patch inferences from SWOT synthetic data:  $c_{flat}^{*}$ , inferred control vector without a priori hydraulic behaviour.

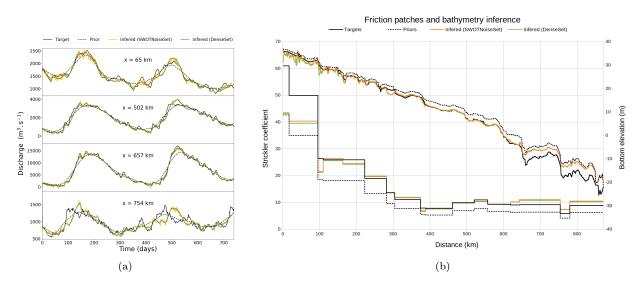


Figure 15: Inflow, bathymetry and friction patch inferences from SWOT synthetic data :  $c_{filter}^*$ , inferred control vector with a priori hydraulic behaviour.

Obs set	Prior		$RMSE \ [m^3s]$	$[r^{-1}] (rRMSE$	Nash-Sutcliffe				
Obs set		$65\mathrm{km}$	$502\mathrm{km}$	$657\mathrm{km}$	$754\mathrm{km}$	$65\mathrm{km}$	$502\mathrm{km}$	$657\mathrm{km}$	$754\mathrm{km}$
DenseSet	$Q_{FG}^{flat}$	189(0.12)	329(0.17)	1472 (0.22)	430(0.45)	0.84	0.90	0.87	0.10
NoiseSWOTSet	$Q_{FG}$	209 (0.14)	360(0.18)	1719(0.26)	421 (0.44)	0.81	0.88	0.82	0.10
DenseSet	$Q_{FG}^{filter}$	$101 \ (0.07)$	$195\ (0.10)$	412(0.06)	$158 \ (0.17)$	0.94	0.97	0.99	0.49
NoiseSWOTSet	$Q_{FG}$	102 (0.07)	208(0.11)	503~(0.07)	$154\ (0.16)$	0.94	0.96	0.99	0.51

(	a	) Hvd	lrograph	scores
١	a	) II y C	nograph	20100

Obs set	Prior	$\frac{RMSE_{\alpha}}{[m^{1/3}s^{-1}]}$	$RMSE_b$ [m]
DenseSet	$Q_{FG}^{flat}$	5.35	1.89
NoiseSWOTSet	$Q_{FG}$	5.12	1.64
DenseSet	$Q_{FG}^{filter}$	5.30	2.06
NoiseSWOTSet	$Q_{FG}$	5.13	1.99

(b) Channel parameters scores

Table 6: Inferred parameter scores for extended control inferences.

of the anabranching Negro River in the Amazon basin using multisatellite data.

Through low Froude synthetic cases, it is shown that the signature of a lateral inflow is visible downstream 667 from the inflow point through the total flow signature and can be visible upstream in case of downstream control 668 at the injection. Following this analysis and using the HiVDI variational assimilation method (global in time and 669 space), a study of the minimum spatial density of water surface observations necessary to infer lateral inflows from 670 their hydraulic signatures is carried out. Synthetic twin experiments yield the following results: (i) given high 671 observation temporal frequency relative to model hydraulic response, perfect inflows inferences can be obtained; (ii) 672 to correctly attribute signatures between multiple lateral inflows, a minimum of 1 observation point between each 673 injection cell is necessary; (iii) when simultaneously inferring inflows and/or channel parameters, a sensitivity to 674 parameter weights (see section AppendixA) appears; (iv) given a priori parameter weights, accurate inferences of 675 inflows and channel parameters is achievable even with the minimum spatial observability. 676

A method for building effective river models in coherence with multisatellite data and including realistic spatial variations is introduced based on multisource data of water surface elevation, width and slopes. This method makes use of (i) multimission altimetric rating curves (see [64]) or equivalently a distributed hydrological model and altimetry data and (ii) water surface width like those from current databases (see [71]); it should be applicable to rivers from the future SWOT database. It is applied here to build a simple effective 1D model of the Negro river upstream from its confluence with the Solimoes river. It fits currently available satellite water surfaces signatures and contains real-like spatial variabilities and flood wave propagation features.

The inference capabilities of spatially distributed channel parameters and inflows from synthetic SWOT observations are highlighted on the Negro River case given hydraulically coherent priors. The inference of temporal parameters in the form of 21 spatially distributed lateral inflow hydrographs leads to accurate estimates and low water surface misfit at observation times. High frequency observations give good inferences, with an expected sensitivity to both prior bias (see [1, 34]) and prior shape.

SWOT-like observations lead to comparable inferences, with slight oscillations due to the frequential disparity 680 between observations temporal controls combined to their spatial distribution and the resulting nonlinear flow prop-690 agation on the domain, as analyzed with identifiability maps. Those oscillations related to model-observations time 691 scales could be overcome by introducing additional regularizations - not done here for the sake of hydraulic analysis. 692 Inference of purely spatial parameters (bathymetry/friction) were carried out as well, leading to some complemen-693 tary remarks: (i) channel parameters equifinality is most present in the downstream part of the model, where the 694 waterline is influenced by the strong backwater effect of the boundary condition (Solimoes River) which diminishes water surface sensitivity to other parameters; (ii) bathymetry prior shape influences the inferred bathymetry. Fi-696 nally, simultaneous inference of channel parameters and spatially distributed inflows was achieved with satisfying 697 accuracy. We show that, with the present method, large scale temporal parameter variations can be found from 698 synthetic SWOT observations even without a priori knowledge of the shape of the hydrological response, but that 699 small scale variations can be better inferred with a priori hydrograph shape knowledge. 700

Recall that the estimation of discharges and channel parameters from (SWOT) WS observations is a difficult 701 inverse problem because of the correlated influence of flow controls on the observable water surface signatures -702 non uniqueness/equifinality issues. It is therefore necessary to use hydraulically consistent priors as investigated in 703 [1, 37, 34] with HiVDI method that contains low complexity flow relations for deriving robust prior guesses from 704 databases and hydrological models, or even in situ depth/discharge data when available (see [1]) - not the scope of 705 this paper. As already discussed in [1], the VDA solution depends on the priors which are the first guess value and 706 the covariances matrixes. Ongoing research efforts in the SWOT community, in view of global discharge estimates, 707 focus on the determination of priors through the construction of a SWOT a-priori database based on [72, 71] and 708 global/regional model outputs (see [26, 1]), constrained with available in situ gauge measurements. Note that 709 a-priori estimations/databases could be enriched or reprocessed during or after the SWOT mission lifetime and 710 HiVDI would enable to refining discharge estimates (see [1]). Moreover, as shown in [73], priors obtained by deep 711 learning can greatly improve global estimation. 712

More generally, reaching unbiased estimates of discharge, from downstream to upstream of river networks with varying densities of in situ discharge data hence ungauged river portions/basins, is a crucial challenge in hydrology that could benefit from the fusion of complementary in situ and remotely sensed data in integrated models. The present study brings insight in lateral inflows inference from hydraulic signatures and paves the way for further research on integrated hydrological-hydraulic assimilation chains for river networks and in coherence with multisatellites observables (of local hydrodynamic signatures) to benefit from them in a regionalization perspective.

Searching for distributed channel parameters and inflows given temporally sparse SWOT data and a global assimilation method brings the issue of signal attribution to the forefront, especially at the scale of a river network.

Further research should focus on tributaries that could be amenable to the use of SWOT and multisatellite obser-721 vations to better constrain estimates of lateral inflows and next distributed fluxes on network models considering 722 hydrological-hydraulic couplings. The introduction of pertinent signatures, scales and constrains in the forward-723 inverse models (e.g. forward operators, covariance matrices, cost function terms) should help maximizing the use 724 of various information sources and enable smooth discharge estimates and better signal attribution, given uneven 725 and heterogeneous satellite data in combination with other complementary databases/knowledge. This could help 726 leveraging better inferences of hydrological responses and flow structure within a river basin and eventually enable 727 information feedback to rainfall-runoff modules and ultimately regionalization issues. 728

729

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This work is a part of the PhD thesis work of LP.

Research plan: LP, PAG, JM, PFG; computational software DassFlow1D and satellite data curation toolbox
adapted from their previous versions by LP; Numerical investigations by LP with PAG, PFG, KL, JM for analysis.
JM is the principal designer of the inverse computational method and its analysis.

Data : The water surface widths were derived by SB and HY contributed to their analysis using satellite images. The SWOT synthetic observations were generated by KL. The multisatellite dataset was provided by SC and altimetric rating curves and MGB outputs by AP. The GPS flow lines were provided by DM and SC.

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- 974

## 975 AppendixA. The computational inverse method

The computational inverse method is based on Variational Data Assimilation (VDA) applied to the 1D Saint-976 Venant model (eq. (1)). The computational inverse method is the one presented in [5, 1] with an augmented 977 composite control vector c (eq. (4)): c contains a spatially distributed friction coefficient enabling to model complex 978 flow zones (while it is an uniform friction law K(h) in [1]). This definition of K(x,h) enables to consider more 979 heterogeneous bathymetry controls. c also contains lateral flow hydrographs  $Q_{lat,i}(t)$  to deal with in/offtakes due 980 to tributaries or underground flows. It is important to point out that the imposed downstream BC is an unknown 981 of the inverse problem. It is constrained with the observed water elevations and inferred river bottom slope using 982 a locally uniform flow hypothesis (i.e. Manning equation, see subsection 2.1) - except in the last real case above. 983 The cost function j(c) is defined as: 984

$$j(c) = j_{obs}(c) + \gamma j_{reg}(c) \tag{A.1}$$

where  $\gamma > 0$  is a weighting coefficient of the so-called "regularization term"  $j_{reg}(c)$ . The term  $j_{obs}(c)$  measures the misfit between observed and modeled WS elevations such that:

$$j_{obs}(c) = \frac{1}{2} \| (Z(c) - Z_{obs}) \|_{\mathcal{O}}^2$$
(A.2)

The norm  $\|\cdot\|_{\mathcal{O}} = \|\mathcal{O}^{1/2}\cdot\|_2$  is defined from an a priori positive definite covariance matrix  $\mathcal{O}$ . Assuming uncorrelated observations  $\mathcal{O} = diag(\sigma_Z)$ . The modeled WS elevations Z depend on c through the hydrodynamic model (eq. (1)) and the inverse problem reads as

$$c^* = \operatorname{argmin}_{c} j(c) \tag{A.3}$$

This optimal control problem is solved using a Quasi-Newton descent algorithm: the L-BFGS algorithm version presented in [74]. The cost gradient  $\nabla j(c)$  is computed by solving the adjoint model; the latter is obtained by automatic differentiation using Tapenade software [75]. Detailed know-hows on VDA may be found e.g. in the online courses [76, 51].

To be solved efficiently this optimization problem needs to be "regularized". Indeed the friction and the bathymetry may trigger indiscernible surface signatures therefore leading to an ill-posed inverse problem; we refer e.g. to [35] for the theory of regularization of such inverse problems and to [1] for a discussion focused on the present inverse flow problem.

Following [1], the optimization problem (eq. (A.3)) is regularized as follows. First the regularization term  $j_{reg}$ is added to the cost function (eq. (A.1)). We simply set:  $j_{reg}(c) = \frac{1}{2} ||b''(x)||_2^2$ . Therefore this term imposes (as weak constraints) the inferred bathymetry profile b(x) to be an elastic interpolating the values of b at the control points (i.e. a cubic spline).

A specificity of the present context is the large inconsistency between the large observation grid (altimetry points) and the finer model grid. Between the sparse observations points (equivalently the control points), the bathymetry profile b(x) is reconstructed as a piecewise linear function. It is worth to point out that the resulting reconstruction is consistent with the physical analysis presented in [52, 55]. (This study analyses the adequation between the SW model (eq. (1)) behavior and the WS signature).

1007 Next and following [77, 78, 1], the following change of control variable is made:

$$k = B^{-1/2} \left( c - c_{prior} \right)$$
 (A.4)

where c is the original control vector,  $c_{prior}$  is a prior value of c and B is a covariance matrix. The choice of B is crucial in the VDA formulation; its expression is detailed below. After this change of variable the new optimization problem reads:

$$\min_{k} \mathbf{J}(k) \text{ with } \mathbf{J}(k) = j(c) \tag{A.5}$$

It is easy to show that this leads to the following new optimality condition:  $B^{1/2}\nabla j(c) = 0$ ; somehow a preconditioned optimality condition. For more details and explanations we refer to 79, 80 and [1] in the present inversion context.

Assuming uncorrelated controls the matrix B is defined as block diagonal such that  $B = \text{diag} (B_Q, B_{Qlat,1}, \dots, B_{Qlat,L}, B_b, B_\alpha, T)$ Still following [1], the covariance matrices  $B_Q$ ,  $B_{Qlat}$  and  $B_b$  are set as the classical second order auto-regressive correlation matrices:

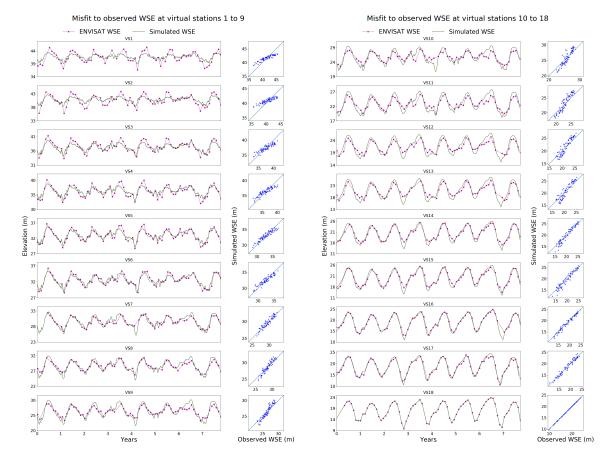
$$(B_Q)_{i,j} = (\sigma_Q)^2 \exp\left(-\frac{|t_j - t_i|}{\Delta t_Q}\right), \ \left(B_{Q_{lat,l}}\right)_{i,j} = (\sigma_{Q_{lat}})^2 \exp\left(-\frac{|t_j - t_i|}{\Delta t_Q}\right) \text{ and } (B_b)_{i,j} = (\sigma_b)^2 \exp\left(-\frac{|x_j - x_i|}{L_b}\right)$$
(A.6)

The VDA parameters  $\Delta t_Q$  and  $L_b$  represent prior hydraulic scales and act as correlation lengths. We refer to [5] for a thorough analysis of the discharge inference in terms of frequencies and wave lengths and [1] in the present river-observation context. In the present study, the friction parameters applied to deca-kilometric patches are assumed to be uncorrelated thus the matrices  $B_{\alpha}$  and  $B_{\beta}$  are diagonal:

$$(B_{\alpha})_{i,i} = (\sigma_{\alpha})^2, (B_{\beta})_{i,i} = (\sigma_{\beta})^2$$
(A.7)

The scalar values  $\sigma_{\Box}$  may be viewed as variances; their values are given in the numerical results section.

Finally, in a noised observation context and to avoid overfitting noisy data, we denote by  $\delta$  the noise level such that  $||Z_{obs} - Z_{true}||^2 \leq \delta$  with  $Z_{obs}$  the observed and  $Z_{true}$  the true WS elevation profiles. A common technique to avoid overfitting noisy data, in the context of Tykhonov's regularization of ill-posed problems, is Morozov's discrepancy principle, (see e.g. [35] and references therein): the regularization parameter  $\gamma$  (see eq. (A.1)) is chosen a posteriori such that j does not decrease below the noise level.



## <sup>1028</sup> AppendixB. Extended friction calibration results

1027

Figure B.16: ENVISAT WS elevation misfit after friction calibration at all stations for M2a.

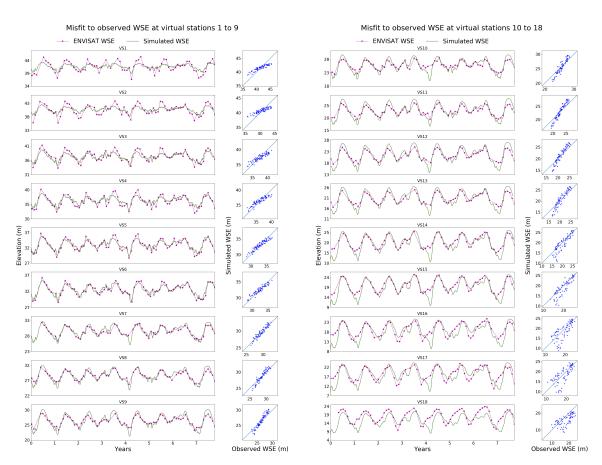


Figure B.17: ENVISAT WS elevation misfit after friction calibration at all stations for M2b.

AppendixC. Additional graphs and RMSE for lateral hydrograph inferences on the Negro River
 with DenseSet and SWOTNoiseSet observation patterns

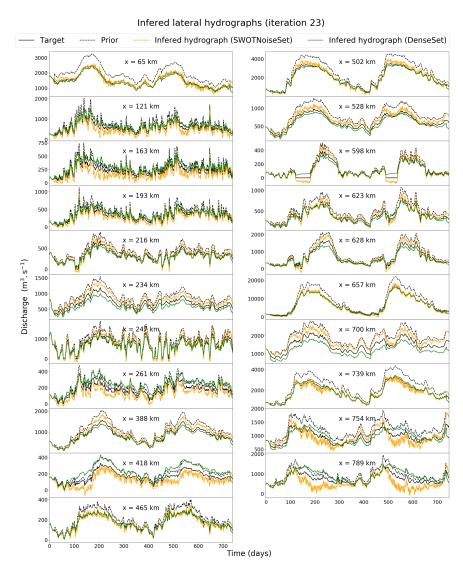


Figure C.18: Lateral hydrograph inferences from SWOTNoiseSet and DenseSet, using the  $Q_{FG}^{+30}$  inflow prior

1032

$x (\mathrm{km})$	$\mu$ (d)	$\sigma (m^3 s^{-1})$	DenseSet RMSE $(m^3 s^{-1})$	SWOTNoiseSet RMSE $(m^3 s^{-1})$
65		2500	79.62	122.34
121		1500	97.74	134.59
163		1000	64.17	70.44
193		1000	49.06	50.75
216		700	37.04	41.48
234		800	112.76	120.43
247		1000	89.82	105.24
261		800	56.57	45.62
388	]	1000	98.30	125.94
418		800	60.64	49.12
465	1	600	8.86	12.64
502		2000	116.21	194.86
528	]	1000	66.85	83.55
598		600	28.69	29.08
623		1000	40.75	44.83
628		1200	119.85	126.13
657	]	5000	421.26	578.31
700		1500	263.07	264.27
739		2800	127.97	173.35
754		2000	140.89	158.19
789		2400	249.73	283.92

<sup>(</sup>a) With prior  $Q_{FG}^{-30}$ 

$x (\mathrm{km})$	$\mu$ (d)	$\sigma (m^3 s^{-1})$	DenseSet RMSE $(m^3 s^{-1})$	SWOTNoiseSet RMSE $(m^3 s^{-1})$
65		2500	134.66	156.34
121		1500	142.70	138.31
163		1000	69.46	66.83
193		1000	45.66	43.47
216		700	45.31	47.28
234		800	128.18	130.98
247		1000	122.21	125.72
261		800	35.82	33.85
388		1000	146.13	149.39
418		800	33.81	32.22
465	1	600	13.53	15.37
502		2000	212.87	235.58
528		1000	87.67	91.96
598		600	28.62	28.85
623		1000	39.51	43.31
628		1200	123.45	126.71
657		5000	581.03	775.15
700		1500	250.54	256.81
739		2800	157.54	194.14
754		2000	147.88	154.01
789		2400	293.07	297.37

(b) With prior  $Q_{FG}^{+30}$ 

Table C.7: Inferred lateral inflows parameter weights and RMSE

- 1033 AppendixD. Technical specifications
- 1034 Host bridge: Intel Corporation 8th Gen Core Processor Host Bridge/DRAM Registers
- 1035 PCI bridge: Intel Corporation Xeon E3-1200 v5/E3-1500 v5/6th Gen Core Processor PCIe Controller
- 1036 Memory: 2x16Gb SODIMM DDR4 Synchronous 2667 MHz (0.4 ns)
- 1037 Resolution mode: sequential
- 1038 Resolution method: implicit-explicit preissmann scheme
- **Sample run:** inference of the full triplet on the Negro model (inferred control vector  $c_{filter}^*$  in subsection 5.2)
- Control vector components: 4x740 flow points, 436 bathymetry points, 17 friction patches (3413 total sought values)
- Total run time (direct): under 15 min
- Total run time (inverse): 20.8 h
- Number of iterations: 35
- Average iteration time length: 35.8 min