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# A SIX-CHANNEL MICROSTRIP DIPLEXER FOR MULTI-SERVICE WIRELESS COMMUNICATION SYSTEMS

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## **1** Introduction

Diplexers with multiple bandpass channels are essential components in multi-service and multiband communication systems. They are used for controlling the transmitted and received signals in the RF front ends systems. Specifications of a welldesigned multi-channel diplexer are low loss, high isolation and compact geometry. The compact microstrip structures with lightweight and twodimensional geometry are appropriate components to design microwave multi-channel diplexers and multiplexers. Therefore, several diplexers, triplexers and multiplexers have been designed using various microstrip structures [1-9]. Six-channel diplexers in [1, 2], four-channel diplexers in [3, 4], two-channel diplexers in [5, 6], and eight-channel diplexer in [7] were introduced. In [1], magnetically quarter

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#### Abstract:

In this paper, a six-channel microstrip diplexer is designed and fabricated. It operates at 0.75/0.85/1/1.25/1.6/1.8 GHz for multi-service wireless communication systems. It consists of two stub-loaded resonators, which are integrated by coupled lines. The channels are close together, which makes the proposed diplexer suitable for frequency division duplex (FDD) schemes. The proposed structure has a compact size of 0.025  $\lambda_g^2$ where  $\lambda_g$  is the guided wavelength calculated at 0.75 GHz. The other advantages of the introduced *multi-channel diplexer are the low insertion losses* of 1.62/1.27/0.43/0.53/1.26 and 1 dB, as well as good return losses of 26/26/25/25/21.7 and 22 dB at 0.75/0.85/1/1.25/1.6/1.8 GHz respectively. A good isolation of less than 22 dB is obtained between the channels. In order to design the presented diplexer a designing technique is used which is based on the proposing of an equivalent approximated LC model and calculating the inductors and capacitors. To confirm the simulation results, the introduced diplexer is fabricated and measured.

wavelength coupled step impedance resonators by grounded via hole were used to obtain six passbands at 1.575/1.8/2.4/3.5/5.2/5.8 GHz. The proposed structure in [1] provides relatively compact size but the multiplexers and diplexers in [2-9] take up a lot of space. A new method of harmonic suppression was applied to achieve six passbands at 10/12/19/21/32/35 (GHz) in [2]. However, there are large insertion and return losses in its passbands. In [3], coupled hairpin resonators, in [4] quad-mode stub-loaded resonators, in [5] simple coupled lines, in [6] triangular open loop resonator and in [7] coupled loops with step impedance structures were utilized to design multi-channel diplexers. Due to the difficulty of designing multi-channel diplexers [1-4, 7], they have been less designed than singleband diplexers [3, 4] and multiplexers [8, 9]. The microstrip triplexer presented in [8] operates at 3.3/3.89/4.56 GHz. It is large in size and has a high insertion and return losses. In [9], a microstrip multiplexer with six passbands at six ports was realized. Designing the multiplexer in [9] was carried out by a combination of several lumped inductors and microstrip coupled lines. In [10], the design of a dual-frequency microstrip diplexer is investigated using the microstrip cells analysis and coupled lines components. In [11], a compact and high-isolation six-channel microstrip diplexer is presented using two pairs of multimode resonators. In [12], a compact tunable microstrip eight-channel multiplexer is investigated using dual-mode stubloaded resonators. In [13], a new quad-channel diplexer operated at 2.45 GHz, 4.2 GHz, 3.5 GHz and 5.2 GHz is proposed, which is composed of folded defected stepped impedance resonators (DSIRs) and feeding lines. In [14], two quadchannel bandpass filters have been designed based on a novel circular multi-mode resonator.

In this paper, a compact six-channel diplexer is introduced, which operates at the resonance frequencies of 0.75/0.85/1/1.25/1.60/1.8 GHz for frequency division duplex (FDD) scheme [15-16] and multi-band wireless applications. It consists of new stub-loaded U-shape resonators, which are integrated by the coupled lines. The proposed diplexer is compact with low insertion loss that is designed to satisfy the requirements of multi-band communication systems. The steps of designing are organized as following:

First, an approximated LC circuit of a basic microstrip structure is proposed; then the values of lumped elements are calculated according to the transmission line theory. Next, the EM simulation results are compared to the simulation results of the LC model. This comparison partially verifies the approximated LC circuit. After that, the input impedance of the proposed basic structure is checked out to obtain the resonance modes. Finally, the compatibility of the obtained resonance conditions with the calculated lumped elements is presented, which verifies the designing methodology.

### 2 Designing method

The block diagram in Figure 1a shows how our sixchannel diplexer works. Port 2 is connected to a transmitter, port 3 is connected to a receiver and port 1 is common between the transmitter and receiver. The signals are received and sent through port 1 by an antenna. Figure 1b depicts a basic configuration to implement the presented block diagram. It consists of three microstrip-coupled lines, which integrate two resonators. Resonator 1 and coupled lines create three passbands at 0.75 GHz, 1 GHz and 1.6 GHz while resonator 2 and coupled lines create the other passbands at 0.85 GHz, 1.25 GHz and 1.8 GHz. We assume that the basic structure of the resonators 1 and 2 are similar. The proposed resonators are composed of the microstrip stub loaded coupled lines.

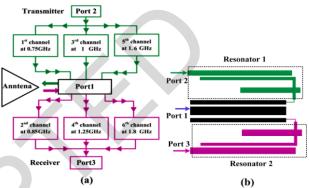


Figure 1. (a) Block diagram of the proposed sixchannel diplexer (b) proposed basic configuration to implement the block diagram.

In Figure 2, an equivalent LC circuit of the proposed basic structure is outlined on the basic layout configuration. The corresponding LC circuit of each microstrip cell is drawn itself. The open ends of the stubs are replaced by the capacitor Co. Several inductors and capacitors model the coupled lines. An inductor is related to a half line and capacitors show the coupling between lines. These capacitors are  $C_R$  for resonators and  $C_C$  for the middle coupled lines.  $L_{S1}$  and  $L_{S2}$  are the inductors of the open stubs connected to the Resonator 1 and Resonator 2, respectively.

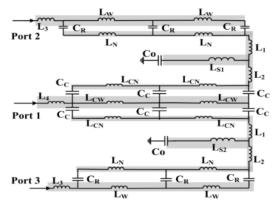


Figure 2. Equivalent LC circuit of the proposed basic structure.

Figure 2 depicts an approximate equivalent circuit. Since bents have a significant effect at the frequencies above 10 GHz, we ignored them [17]. Meanwhile, the equivalent circuit is a lossless passive network. In addition, the equivalent model of coupled lines is replaced approximately. Since we use an approximated model, we ignored a capacitor considering the dielectric effect of the substrate to have easier calculations.

The layout of the Resonator 1 and coupled lines connected to port 1 is presented in Figure 3a, which creates three passbands. This is a symmetric structure that obtains three channels. The resonator 2 and the middle coupled lines must create other channels. The equivalent LC circuit of Figure 3a is shown in Figure 3b. According to the presented dimensions in Figure 3a and based on the transmission line theory, the values of lumped elements can be calculated. They will be obtained using the input impedance of a transmission line Z<sub>in</sub>. A microstrip cell with the characteristic impedance "Zc", thickness "h", effective dielectric constant " $\varepsilon_{re}$ ", width "w" and length "l" has the input impedance Z<sub>in</sub> that can be calculated at a frequency of "*f*" as follows [18]:

$$Z_{in} = jZc \tan\left(\frac{\pi l f \sqrt{\varepsilon_{re}}}{150}\right) \quad , where: \varepsilon_{re} = \left(\frac{\varepsilon_r + 1}{2} + \frac{\varepsilon_r - 1}{2\sqrt{1 + 12\frac{h}{w}}}\right) \tag{1}$$
  
and 
$$Zc = \frac{120\pi}{\left[\frac{w}{h} + 1.393 + 0.677\ln(1.44 + \frac{w}{h})\right]\sqrt{\varepsilon_{re}}}$$

Based on our preliminary conditions h=0.508 mm,  $\varepsilon_r$ =3.15 and the widths are 0.6 mm or 1.2 mm. For w=0.6 mm, the characteristic impedance and effective dielectric constant are  $68.98 \Omega$  and 2.37, respectively. Similarly, for w=1.2 mm, the characteristic impedance and effective dielectric constant are 46.74  $\Omega$  and 2.51, respectively. The lumped inductors are obtained by calculating Zin. For each inductor "L" we can write  $L = Z_{in} / (j2\pi fL)$ , where Zin gets different values for each microstrip cell. However, for the shunt stub, L<sub>S1</sub> will be calculated by  $Z_{in} = j2\pi f L_{s1} + 1/(j2\pi f C_0)$ . Meanwhile, we assumed Co=1.3 pF to calculate  $L_{SI}$ . The inductors of the LC circuit are calculated and listed in Table 1. According to Equation (1), the inductors have different values at each resonance frequencies. Based on the EM simulation, the results obtained from the layout in Figure 3a, this basic microstrip structure resonates at three different frequencies i.e. 0.96/1.9/2.9 GHz. Therefore, the lumped inductors are calculated at these frequencies. Some values in Table 1 are negative that represent the capacitive modes and we ignore them. The same values in Table 1 are due to the symmetric structure of basic layout. Using the calculated data in Table 1, the LC circuit presented in Figure 3b is simulated. Then this simulation is compared to the EM simulator as shown in Figure 3c and Figure 3d. The EM and schematic simulation results are approximately similar, which verifies the proposed LC model. Similar to the layout results, the schematic results are obtained by advanced design system (ADS) software. The open stubs  $L_1$  and  $L_2$  resonate at lower frequency. The capacitors of couplings (Cc and  $C_R$ ) are small to represent the coupling features so that they will be in fF. As shown in Figure 3c, both EM and schematic simulation results are approximately similar. However, there are some differences such as the frequency shift around 0.5 GHz, which is due to the approximation of LC circuit.

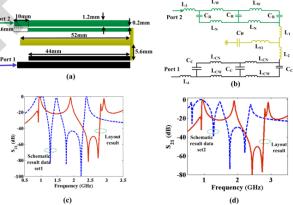


Figure 3. (a) Basic structure consisting of the Resonator 1 and coupled lines, (b) LC model of the proposed basic structure, (c) comparison of layout and schematic simulations for  $L_1=L_2=0.48$  nH,  $L_3=L_4=2.84$  nH,  $L_{S1}=6.03$  nH, Co=1.3 pf,  $L_W=L_{CW}=20.52$  nH,  $L_N=L_{CN}=49.34$  nH and  $C_R=C_C=220$ fF, (d) comparison of layout and schematic simulations for  $L_1=L_2=0.48$  nH,  $L_3=L_4=2.84$  nH,  $L_{S1}=6.03$  nH, Co=1.3 pf,  $L_W$ =20.52 nH,  $L_N=49.34$  nH,  $C_R=220$  fF,  $L_{CW}=2.134$ nH,  $L_{CN}=2.159$  nH and  $C_C=14.4$  nf.

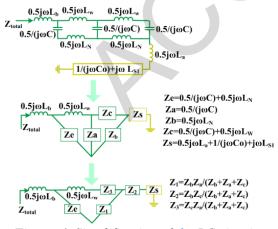
Table 1. Lumped element values calculated at three various frequencies (inductors are in nH).

Elements	L <sub>1</sub>	$L_2$	L3	L4	L <sub>S1</sub>	Lw	L <sub>N</sub>	Lcw	LCN
Values at 0.96GHz	0.48	0.48	0.989	0.989	6.03	2.134	2.159	2.134	2.159
Values at 1.9GHz	1.817	1.817	2.84	2.84	0.49	20.52	49.34	20.52	49.34
Values at 2.9GHz	1.9	1.9	3.67	3.67	-25	-4.23	-7.36	-4.23	-7.36

Similarly, the elements of the LC model in Figure 3d are L<sub>1</sub>=L<sub>2</sub>=0.48 nH, L<sub>3</sub>=L<sub>4</sub>=2.84 nH, L<sub>S1</sub>=6.03 nH, Co=1.3 pf, L<sub>w</sub> =20.52 nH, L<sub>N</sub>=49.34 nH,  $C_{R=220}$  fF,  $L_{CW}=2.134$  nH,  $L_{CN}=2.159$  nH and C<sub>C</sub>=14.4 nf. In order to create three passbands through the port 2 and port 1, the input impedance between ports 1 and 2 can be zero. For the microstrip structure presented in Figure 3b, the total input impedance viewed from port 2 can be calculated using a simplified LC circuit. Figure 4 shows the steps of simplification to calculate the total input impedance  $Z_{total}$ , where  $\omega$  is the angular frequency. Due to the symmetrical structure, first we assume C<sub>R</sub>=C<sub>C</sub>=C, L<sub>W</sub>=L<sub>CW</sub>, L<sub>N</sub>=L<sub>CN</sub>, L<sub>2</sub>=L<sub>1</sub>=La and  $L_3=L_4=L_b$ , then, we connect same potential nodes, which leads to reduce the LC circuit as shown in Figure 4. Finally, with a delta star transformation the LC circuit is simplified. Therefore, the Z<sub>total</sub> is calculated as follows:

$$Z_{total} = 0.5 j\omega L_b + Z_2 + Z_s + \frac{(0.5 j\omega L_w + Z_3) \times (Z_1 + Z_e)}{0.5 j\omega L_w + Z_3 + Z_1 + Z_e}$$
(2)

The values of  $Z_1$ ,  $Z_2$ ,  $Z_3$ ,  $Z_5$  and  $Z_6$  are shown in Figure 4.



*Figure 4. Simplification of <u>the</u> LC circuit to calculate Z<sub>total</sub>.* 

For the even mode, the resonance condition is achieved when  $Z_{total}^{-1} = 0$ . Therefore, we can write a resonance condition as follows:

$$0.5 j\omega L_{w} + Z_{3} + Z_{1} + Z_{e} = 0 \Rightarrow 0.5 j\omega L_{w} + \frac{Z_{a}Z_{c} + Z_{b}Z_{a}}{Z_{b} + Z_{a} + Z_{c}} +$$

$$\frac{0.5}{j\omega C} + 0.5 j\omega L_{N} = 0 \Rightarrow \omega^{2}C(L_{w} + L_{N}) = [\frac{(3 - 2\omega^{2}C(L_{w} + L_{N}))}{2 - \omega^{2}C(L_{w} + L_{N})}] \Rightarrow$$

$$\omega = \begin{cases} (C(L_{w} + L_{N}))^{-0.5} \\ 3(C(L_{w} + L_{N}))^{-0.5} \end{cases}$$
(3)

According to Equation (3), coupled lines create two resonance frequencies. In this case, the third passband channel should be created by the condition of odd mode resonance frequency. If we select the calculated inductors as  $L_W=2.134$  nH and  $L_N=2.159$ *nH*, for the resonance frequency of f=0.96 GHz from Equation (3), the coupling capacitor C will be  $C = C_C = C_R = 169.48$  nf but for f = 1.9 GHz,  $L_W = 20.52$ *nH* and  $L_N = 49.34$  *nH* the coupling capacitor will be 300.43 fF, which is calculated by  $\omega = 3[C(L_w + L_N)]^{-0.5}$ . This value of C is so near to that so we selected to compare the EM simulator with the LC simulation results. This verifies the design methodology. The layout configuration of the proposed diplexer is designed based on the geometrical structure of Figure 2 and explained designing method. The proposed six-channel diplexer is presented in Figure 5. Additional optimizations are carried out to tune the resonance frequencies and miniaturization. For example, the shunt direct stubs are changed to spirals to save the overall size. In Figure 6, current density distribution of the proposed diplexer is shown.

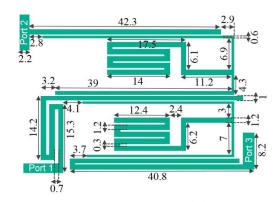


Figure 5. Dimensions of proposed diplexer (in mm).

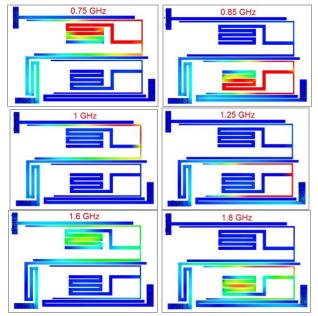


Figure 6. Current density distribution of the proposed diplexer.

### **3** Results and discussion

The designed multi-channel diplexer is simulated by the ADS full wave EM simulator and fabricated on the substrate RT\_Duroid\_5880 with the dielectric constant 2.22, loss tangent = 0.0008 and thickness of 0.508 mm. Finally, it is measured by the Agilent Network Analyser N5230A. The overall size of the proposed structure is 52.1mm×35.1mm  $(0.19\lambda_g \times 0.13\lambda_g)$ , where  $\lambda_g$  is the guided wavelength calculated at 0.75 GHz. Figures 7a and 7b depict the simulated and measured frequency responses consisting of the proposed diplexer. A photograph of the fabricated diplexer and  $S_{11}$  are shown in Figure 7c. According to the obtained results, the proposed diplexer has a frequency response at the central frequencies of 0.75 GHz, 1 GHz and 1.6 GHz (port 2) and 0.85 GHz, 1.25 GHz and 1.8 GHz (port3). At the central frequencies, the insertion losses are 1.62 dB, 1.27 dB, 0.43 dB, 0.53 dB, 1.26 dB and 1 dB and the return losses are 26 dB, 26 dB, 25 dB, 25 dB, 21.7 dB and 22 dB, respectively. The performance of the proposed six-channel diplexer is compared with the six-channel diplexers, fourchannel diplexers, two-channel diplexers, eightchannel diplexers and multiplexers. The comparison results are summarized in Table 3. According to Table 3, the realized diplexer not only has a

minimum circuit size, but also good insertion losses and reasonable return losses at all passbands achieved.

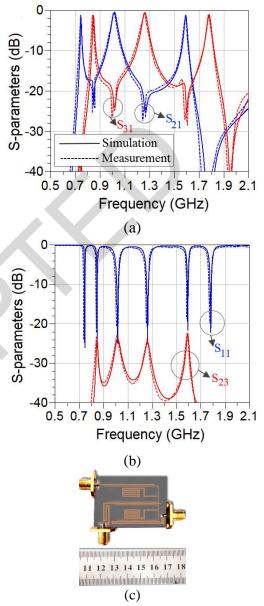


Figure 7. (a) Simulated and measured S<sub>21</sub> and S<sub>31</sub>
(b) simulated and measured S<sub>11</sub> and S<sub>23</sub>
(narrowband response), (c) fabricated diplexer.

References C/P*	C/D*	Personance fragmancing (CHz)	Insertion losses (dB)	Size $(2\pi^2)$	
	C/P∗	Resonance frequencies (GHz)	Return Loss (dB)	Size (λg <sup>2</sup> )	
This Work 6/3	0.75/0.85/1/1.25/1.60/1.8	1.62/1.27/0.43/0.53/1.26/1	0.025		
	0/3	0.75/0.85/1/1.25/1.60/1.8	26/26/25/25/21.7/22	0.025	
[1] 6/3	6/2	1.57/1.8/2.4/3.5/5.2/5.8	1.5/1.1/1.5/1.2/2/2	- 0.027	
	0/3	1.57/1.8/2.4/5.5/5.2/5.8	Better than 20dB at all channels	0.027	
[2] 6.	6/3	10/12/19/21/32/35	2.2/3.1/3.2/2/2.8/3	4	
	0/3	10/12/19/21/32/33	Better than 10dB at all channels		
[3] 4/3	1/2	0.9/1.5/2.4/3.5	2.02/1.56/2.08/2.52	- 0.042	
	4/3	0.9/1.3/2.4/3.3	Better than 13dB at all channels	0.042	
[4] 4/3	1/2	0.9/1.2/1.5/1.8	1.36/1.5/1.3/1.6	0.049	
	4/3	0.9/1.2/1.3/1.8	17.5/18.3/19.6/20.2		
[5] 2/3	2/2	1.8 /2.4	2.2/2.1	0.064	
	2/3	1.8/2.4	11.9/12.0		
[6] 2/3	2/2	2.2 /2.55	1.5/1.3	- 0.102	
	2/3	2.3 /2.55	Better than 21dB at all channels	0.102	
[7] 8/3	0/2	0.9/1.2/1.5/1.8/2.1/2.4/2.7/3	2.1/2.3/2.4/2.6/2.3/2.2/2.8/2.3	- 0.1	
	0/3	0.9/1.2/1.3/1.6/2.1/2.4/2.1/5	Better than 13dB at all channel		
[8] 3/4	2/4	3.3/ 3.89/4.56	2.2/ 2.3/2.3	- 0.275	
	5/4	5.5/ 5.89/4.50	Better than 14dB at all channels		
[9] 6/7	6/7	0.8/1.1/1.4/1.7/2/2.3	2.13/2.3/2.2/2.1/2.08/2.76	- 0.048	
	0/ /	0.8/1.1/1.4/1.7/2/2.3	Better than 11dB at all channels		
[10] 2/3	2/3	2.36/4	0.2/0.4	- 0.096	
	2/3	2.50/4	15/11		
[11] 6/3	6/3	1.8/2.4/3/3.84.7/5.8	1.8/1.9/1/1.5/2.1/2.6	- 0.057	
	0/5	1.0/2.4/5/5.04.7/5.0	11.7/28.4/16.8/16.9/10.1/15.8		
[12] 8	8/8	0.85/1.05/1.3/1.5/1.65/1.85/2.05/2.3	2.7/2.4/2.4/3/3.4/3.8/4.2/4.6	- 0.105	
	0,0	0.00, 1.00, 1.0, 1.00, 1.00, 2.00, 2.0	Better than 15		
[13] 2/4	2/4	2.45/4.2/3.5/5.2	0.22/0.3/1.32/2.12	- 0.88	
	-		Better than 10	0.00	

# 4 Conclusion

This paper presented a microstrip six-channel diplexer with a compact size of  $0.19\lambda_g \times 0.13\lambda_g$ , low insertion losses and good return losses. It is designed to operate at 0.75 GHz, 1 GHz, 1.6 GHz, 0.85 GHz, 1.25 GHz and 1.8 GHz for multi-band and multi-service wireless networks. The proposed structure consists of two stub loaded U-shape resonators which are integrated by the coupled lines. This diplexer in comparison to several types of diplexers and multiplexers had the minimum size. Meanwhile, a challenge is in the number of passbands where due to higher design difficulty of six-channel diplexers, they have been less designed. Another advantage of the proposed multi-channel diplexer was its close channels, which make it appropriate for the frequency division duplex (FDD) applications.

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