

Modeling of Sorption Enhanced Steam Methane Reforming in an adiabatic fixed bed reactor

J.R. Fernandez^{a,*}, J.C. Abanades^a, R. Murillo^b

^aInstituto Nacional del Carbón, CSIC-INCAR Spanish Research Council, C/ Francisco Pintado Fe, 26, 33011, Oviedo. Spain.

^bInstituto de Carboquímica, CSIC-ICB Spanish Research Council, C/ Miguel Luesma Castán 4, 50015, Zaragoza. Spain.

Dr. Jose Ramon Fernandez (corresponding author). Instituto Nacional del Carbón, (CSIC), Francisco Pintado Fe, 26, 33011 Oviedo, Spain.

Tel. +34985118980; Fax. +34985297662; e-mail address: jramon@incar.csic.es

ABSTRACT

Sorption enhanced methane reforming (SER), employing a CaO-based solid as a high temperature CO₂ sorbent, is generally considered to be a promising route for H₂ production. In this paper we present a dynamic pseudo-homogeneous model to describe the operation of a packed bed reactor in which the SER reaction is carried out under adiabatic conditions. This reactor can be implemented according to several process schemes, including a novel Ca/Cu looping process for hydrogen generation with inherent CO₂ capture. The proposed SER model is based on the well-established principles of gas-solid contact and heat transfer in fixed-bed reactors and on the kinetic expressions published in the literature that describe the main reactions involved in the process. The resulting model describes the transient performance of the SER reaction and confirms the theoretical viability of this critical reaction stage in a large scale H₂ production facility. It is demonstrated that the SER process can yield a CH₄ conversion

and H₂ purity of up to 85% and 95%, respectively, under operating conditions of 923 K, 3.5 MPa, a steam/carbon ratio of 5 and a space velocity of 3.5 kg/m²s.

Keywords: CO₂ capture; carbonation; packed bed; catalysis; chemical reactors; dynamic simulation

1. Introduction

Hydrogen is an important raw material in the chemical and petroleum industries. It can also be used as a clean source of energy for electricity generation, which will lead to a huge increase in the demand for hydrogen in the future. There is also considerable interest worldwide in developing new CO₂ capture technologies focused on the mitigation of climate change (Metz et al., 2005). These conditions will serve as a stimulus for developing new processes for large scale hydrogen production from fossil fuels in combination with CO₂ capture (“pre-combustion” CO₂ capture systems), in order to reduce the energy penalty and the costs traditionally associated with the CO₂ capture process.

Steam methane reforming (SMR) is nowadays the main process for large-scale production of hydrogen (Rostrup-Nielsen et al., 2002). The first stage of this heterogeneous catalytic process is usually performed at high temperature and pressure (typically 1073 K-1273 K and 2 MPa-3.5 MPa), followed by an additional shift reaction at a lower temperature (around 473 K-673 K) in order to maximize the H₂ yield. However, both the reforming and water gas shift reactions are equilibrium limited, so that it is not possible to achieve the complete conversion of CH₄ and CO in a single stage under the usual reactor conditions. If the CO₂ is removed from the product gas as soon as it is formed, the normal equilibrium is displaced in favor of the hydrogen yield

in accordance with Le Chatelier's principle, so almost complete conversion can be achieved.

In the sorption enhanced reforming process (SER) a CO₂ sorbent is used, together with a reforming catalyst in the same reactor, to remove CO₂ from the gas phase (Hufton et al., 1999; Harrison, 2008). When using CaO as sorbent in the reforming process, higher methane and CO conversions can be attained at lower temperatures (around 923 K) and a product that contains more than 95% H₂ (dry basis) is possible (Balasubramanian et al., 1999). Additional benefits derivable from the SER process with CaO are the minimization of the coking potential, the elimination of the downstream H₂ purification steps, the diminution of excess steam in the reforming operation, and the reduction of CO in the gas effluent to ppm levels (Lopez Ortiz and Harrison, 1999; Lee et al., 2004; Yi and Harrison, 2005; Yoon et al., 2007; Li and Cai, 2007; Harrison, 2008; Lysikov et al., 2008; Martavaltzi and Lemonidou, 2010).

The SER process with CaO as CO₂-sorbent is slightly exothermic so that no additional energy is required to produce hydrogen. CaO-based sorbents are commonly used in SER because they are able to reduce CO₂ to very low concentrations at moderate temperatures (823-973 K). Calcium oxide may be the most technically and economically viable option because it can be obtained from a wide range of abundant, natural and inexpensive sources including limestone, dolomite and calcium hydroxide (Florin and Harris, 2008). However, it is well known that CaO from natural limestones undergoes a rapid loss of reactivity after several carbonation/calcination cycles (Abanades, 2002). Nevertheless, there are numerous reports in the literature on CaO-based synthetic materials for applications similar to SER, in which a high residual activity (>0.3 mol fraction) is maintained even after a large number of

carbonation/calcination cycles (Stevens et al., 2007; Manovic and Anthony, 2008; Manovic and Anthony, 2009; Blamey et al., 2010).

In the present paper, we report on the development of a dynamic pseudo-homogeneous reactor model to analyze the SER reaction on a large scale (10 kg/s of CH₄ fed into the reformer reactor) and investigate the most suitable material parameters and reactor conditions for its optimum performance. The model was constructed to suit the boundary conditions imposed by the new Ca/Cu looping process described in Abanades et al. (2010) and Fernández et al. (2012), but it should also be applicable to other processes, based on the Sorption Enhanced Reforming principles. Several important modeling works on sorption enhanced reforming have been published in recent years that may be useful purposes of comparison. Xiu et al. (2002) developed a theoretical model that simulates a SER process under non-isothermal, non-adiabatic, and non-isobaric conditions. Mass and thermal dispersion in the axial direction were considered, with negligible radial gradients. They achieved a product gas stream with H₂ purity of 88% (dry basis) with only small traces of CO₂ and CO, at operating conditions of 723 K, 0.45 MPa, a steam/carbon ratio of 6 and a feed gas velocity of 0.08 m/s. Lee et al. (2004) devised a dynamic pseudo-homogeneous and non-adiabatic model for SER with CaO as the CO₂ acceptor. They found that H₂ purity is sensitive to the temperature of the wall, pressure and feed composition. Rusten et al. (2007) simulated a SER operation carried out in a fixed-bed reactor with lithium zirconate as CO₂ sorbent using a transient one-dimensional model with axial dispersion. More recent works in which sorption enhanced reforming has been theoretically and experimentally investigated in order to interpret experimental results from small laboratory scale reactors include those of Li and Cai (2007) and Reijers et al. (2009). However, to our knowledge, there is no modeling work on SER reactor performance under adiabatic

conditions, the most natural choice for large scale reactor designs, since adiabatic conditions would make it possible to take full advantage of the thermal neutrality of the overall SER reaction. Furthermore, a smaller number of adiabatic reactors with a larger cross-sectional area (with respect to the state-of-the-art multitubular reforming reactors) would avoid the need to install costly heat transfer equipment around the reactors.

In this paper we describe the performance on a large scale of an adiabatic sorption enhanced reforming reactor using a multi-component system with a pressure drop and overall mass and energy balances. The validity of the model's predictions was checked by comparing the simulated results with experimental data taken from the literature (Lee et al. 2004; Li and Cai 2007). Furthermore, a sensitivity analysis of the model's predictions for the main material properties (carbonation reaction rate constant and CaO sorbent capacity) was also carried out. A simulation of the SER reactor's performance is carried out in part II of this work in order to determine the operational window that would ensure optimal performance of the SER process in terms of H₂ yield and CH₄ conversion. The effect of the principal operating conditions such as steam/carbon ratio, temperature, total pressure and catalyst/sorbent ratio is also analyzed.

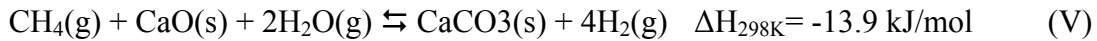
2. Mathematical model description

The SER reactor operation must be described using a dynamic model due to the time-dependent nature of CO₂ capture, as shown in Fig. 1. The reaction front that evolves with time generates a gas composition as a function of the operating conditions in the reaction front. The main chemical reactions that participate in the steam methane reforming are as follows:





Reactions (I) and (II) are highly endothermic, so they are favored by high temperatures, while the water gas shift reaction (III) is exothermic and therefore it is promoted by low temperatures. As pointed out above, in the sorption enhanced reforming (SER) based on CaO-based sorbents, CO₂ is removed as it is formed by reacting with the active calcium oxide, reaction (IV). This reaction is also highly exothermic, so that the enthalpy of the overall reaction is almost neutral, reaction (V).



The reactor model has been designed for adiabatic conditions so that it can profit from the thermal neutrality of the overall SER reaction by using CaO as a regenerable CO₂ sorbent (reaction V). Moreover, an ideal plug flow pattern is assumed while the reactor is operating. This plug flow assumption is based on the high velocities that can be expected in a large scale reactor. The design will be such as to maximize the reactor capacity per unit of cross-sectional area and high superficial gas velocities will be used (typically higher than 0.5 m/s), as generally occurs in conventional large-scale reforming reactors (Dybkjaer, 1995; Rostrup-Nielsen et al., 2002).

Following the criteria in the dispersion model reported by Levenspiel (1979) and considering the operating conditions listed in Table 3, the Peclet number ($Pe = uL/D_e$) is higher than 800, so that the degree of dispersion of the gas flowing through the reactor will be minimal and a plug flow can be considered reasonable for the SER performance described in this work.

Superficial gas velocities higher than 0.5 m/s also lead to a high turbulent regime and therefore high mass and heat transfer coefficients between gas and solids can be assumed. Using the physical properties and operating conditions presented in Table 2 and Table 3, a gas-solid heat transfer coefficient (h_{fs}) of about 0.13 kW/m²K is obtained (Dixon, 1979; Borman et al., 1992). This value implies a very fast gas-solid transfer with no appreciable difference between the gas and solid temperatures at any point in the reactor. Because of the similarities between the equations governing heat and mass transfer, the gas-solid mass transfer coefficients (k_{fs}) can be calculated by means of analogous correlations to those employed to estimate heat transfer coefficients. For the conditions employed in this work, a gas-solid mass transfer coefficient of about 0.17 m/s was obtained (McCabe et al., 1985). Therefore, a rapid gas-solid mass transfer inside the matrix of the solid bed during the SER operation can be assumed, as reported by Breault (2006).

In summary, plug flow without axial dispersion may be assumed as a reasonable representation of the flow pattern in the large scale SER reactor used in this work. Moreover, the interparticle concentration and temperature gradients can be considered negligible at the scale of several millimeters, as is the case in large scale conventional reformers. An ideal gas behavior, a constant bed void fraction, a uniform particle size for the reactor-packed materials, a perfect mixing of the catalyst and sorbent pellets and a negligible catalyst deactivation were also assumed for this model.

The kinetics of the key reforming and shift reactions were obtained using the Langmuir-Hinshelwood equations reported by Xu and Froment (1989). This reaction kinetic model can be expressed as:

$$R_1 = \frac{1}{(DEN)^2} \frac{k_1}{P_{H_2}^{2.5}} \left(P_{CH_4} P_{H_2O} - \frac{P_{H_2}^3 P_{CO}}{K_1} \right) \quad (1)$$

$$R_2 = \frac{1}{(DEN)^2} \frac{k_2}{P_{H_2}^{2.5}} \left(P_{CH_4} P_{H_2O}^2 - \frac{P_{H_2}^4 P_{CO_2}}{K_2} \right) \quad (2)$$

$$R_3 = \frac{1}{(DEN)^2} \frac{k_3}{P_{H_2}} \left(P_{CO} P_{H_2O} - \frac{P_{H_2} P_{CO_2}}{K_3} \right) \quad (3)$$

$$DEN = 1 + K_{CO} P_{CO} + K_{H_2} P_{H_2} + K_{CH_4} P_{CH_4} + K_{H_2O} \frac{P_{H_2O}}{P_{H_2}} \quad (4)$$

where $p_i = x_i P$ ($i = CH_4, H_2O, H_2, CO_2, CO$, P is the total pressure and x_i the gas-phase mole fraction of component i), k_1, k_2 and k_3 are the rate constants, and K_1, K_2 and K_3 are the equilibrium constants. The expressions of these parameters are listed in Table 1.

According to Eq. (1 to 3), the rate of consumption and formation of component i , r_i (kmol/kg_{cat} s) can be calculated as follows:

$$r_i = \sum_{j=1}^3 \varphi_{ij} R_j \quad (i=1-5 \text{ component}, j=1-3) \quad (5)$$

where φ_{ij} is the stoichiometric coefficient of component i . If i refers to a reactant, φ_{ij} is negative, and if i refers to a product, φ_{ij} is positive. From this it follows that the rate of consumption or formation for each component is:

$$r_{CH_4} = -R_1 - R_2 \quad (5-a)$$

$$r_{H_2O} = -R_1 - 2R_2 - R_3 \quad (5-b)$$

$$r_{H_2} = 3R_1 + 4R_2 + R_3 \quad (5-c)$$

$$r_{CO_2} = R_2 + R_3 \quad (5-d)$$

$$r_{CO} = R_1 - R_3 \quad (5-e)$$

To describe the carbonation kinetics of CaO-based sorbents, many expressions have been reported in the literature (Bathia and Perlmutter 1983; Lee et al., 2004; Li and Cai, 2007; Grasa et al., 2008; Grasa et al., 2009). For this work we have chosen the empirical equation used by Rodriguez et al. (2011) to interpret the pilot results from the capture of CO₂ by CaO, for which a first-order carbonation reaction rate is assumed:

$$\frac{dX}{dt} = k_{carb}(X_{max} - X)(v_{CO_2} - v_{CO_2,eq}) \quad (6)$$

where k_{carb} is the reaction rate constant of active CaO (determined as 0.35 s⁻¹), X_{max} is the maximum carbonation conversion of CaO, and v_{CO_2} and $v_{CO_2,eq}$ are the gas-phase mole fraction and the equilibrium mole fraction of CO₂ in the reactor, respectively. Likewise, k_{carb} can be considered to be independent of the temperature in the range of temperatures used in this paper, which is consistent with earlier studies published by Bhatia and Perlmutter (1983) and more recent works (Dennis and Hayhurst, 1987; Li and Cai, 2007). The volume fraction of CO₂ in the equilibrium can be estimated using Eq. (7) (Baker, 1962).

$$v_{CO_2,eq} = 4.137 \cdot 10^7 \exp\left(\frac{-20474}{T}\right) \quad (7)$$

The molar rate of CO₂ removed per unit mass of CaO, r_{carb} (kmol/kg_{cat}s), can be calculated from Eq. (8), where M_{CaO} is the molecular weight of CaO.

$$r_{carb} = \frac{\eta}{M_{CaO}} \left(\frac{dX}{dt} \right) \quad (8)$$

On the basis of the assumptions outlined above, the pseudo-homogeneous model of the differential mass balance for a packed bed can be written as:

$$\varepsilon \frac{\partial C_i}{\partial t} = \frac{\partial(u C_i)}{\partial z} + \eta(1 - \varepsilon)\rho_{cat}r_t - (1 - \varepsilon)\rho_{CaO} r_{carb} \quad (9)$$

where C_i is the molar concentration of species i , ε is the bed void fraction, u is the superficial velocity, η is the effectiveness factor for both reforming and carbonation reactions, ρ_{cat} and ρ_{CaO} are the apparent densities of the catalyst and CaO, respectively. An effectiveness factor of about 0.3 was considered in order to tackle possible diffusion resistance in the gas-solid reactions involved in the SER process. This assumption is consistent with the results obtained in SER operations with large pellets (up to 0.007 m) at high pressure (Solsvik and Jakobsen, 2011). The last term on the right of Eq. (9) is not zero only for the CO_2 mass balance and represents the molar rate of CO_2 removed by the carbonation of CaO per unit bed-volume of the reactor.

The pseudo-homogeneous energy balance for an adiabatic packed bed reactor according to a plug flow pattern can be expressed as:

$$\left[(1 - \varepsilon) \rho_s c_{ps} + \varepsilon \rho_g c_{pg} \right] \frac{\partial T}{\partial t} = - \frac{\partial (u \rho_g c_{pg} T)}{\partial z} - (1 - \varepsilon) \rho_{cat} \sum \eta R_j H_{Rj} - (1 - \varepsilon) \rho_{CaO} r_{carb} H_{carb} \quad (10)$$

where ρ_s is the average apparent density of the solids in the reactor, ρ_g is the gas phase density and c_{ps} and c_{pg} are the solid and gas heat capacities, respectively. H_{Rj} represents the heat of reaction j in reactions (I) to (III) and H_{carb} represents the heat of the CaO carbonation reaction in reaction (IV).

The distribution of pressure (MPa/m) along the packed bed can be described by the Ergun equation as follows (Ergun, 1952).

$$\frac{dP}{dz} = - [K_D u - K_V u^2] 10^{-5} \quad (11)$$

$$K_D = \frac{150 \mu_g (1 - \varepsilon)^2}{d_p^2 \varepsilon^3} \quad (12)$$

$$K_V = \frac{1.75 (1 - \varepsilon)}{d_p \varepsilon^3} \frac{M_g P}{0.082 T} \quad (13)$$

where P is the local pressure at the axial coordinate, K_D and K_V are parameters corresponding to the viscous and the kinetic pressure loss terms, u is the superficial velocity, μ_g is the viscosity of the fluid, ε is the bed porosity, d_p is the particle diameter. M_g is the molecular weight of the gas and T is the local temperature.

The mathematical model is mainly composed of partial differential equations, algebraic equations, and initial and boundary conditions. The model has been implemented and solved using MATLAB programming software. The partial differential equations, Eq. (9) (one for each component $i = \text{CH}_4, \text{H}_2\text{O}, \text{H}_2, \text{CO}_2, \text{CO}$) and Eq. (10) were converted to a set of ordinary differential equations with initial conditions by discretizing the spatial derivative in axial direction (z) employing backward finite differences. For example, a typical bed reactor length of 7 m long was divided into 39 sections with 40 nodes and the resulting predictions were virtually identical with further increases in the number of nodes.

The initial and boundary conditions in Eqs. (11), (12) and (13) are as follows:

$$C_i = C_{i,0} \quad T = T_0 \quad \text{at } t=0 \quad (14)$$

$$C_i = C_{i,\text{in}} \quad T = T_{\text{in}} \quad P = P_{\text{in}} \quad \text{at } z=0 \quad (15)$$

The initial concentrations of the gas species in the reactor should be set to zero, but they were actually considered as equal to 10^{-6} in order to avoid denominators equal to zero in the equations described above. The system formed by the ordinary differential equations and the other algebraic equations mentioned above was simultaneously solved employing the “ode15s.m” function, which is a MATLAB tool for solving initial value problems for stiff ordinary differential equations.

The model predictions were first checked for consistency at different operating conditions by closing all the mass and energy balances involved in the process for different times during a complete SER cycle. Equilibrium conditions were reached during the SER performance (prebreakthrough) and during the SMR operation (postbreakthrough), when considering fast reforming and carbonation kinetics. As mentioned above, we are not aware of any published works on sorption enhanced reforming processes performed in adiabatic fixed-bed reactors. For this reason, the model had to be validated by comparing our simulation results with experimental data taken from previous works on SER in non-adiabatic and non-isothermal fixed-bed reactors (Lee et al. 2004; Li and Cai 2007). For this validation, the model developed in this paper was adapted slightly to the conditions established in the above mentioned works. An additional term on the right side of the energy balance, Eq. (10), was included in order to account for the heat transfer through the reactor wall when an external source of energy is supplied to a non-adiabatic system:

$$\left[(1 - \varepsilon) \rho_s c_{ps} + \varepsilon \rho_g c_{pg} \right] \frac{\partial T}{\partial t} - \frac{\partial (u \rho_g c_{pg} T)}{\partial z} - (1 - \varepsilon) \rho_{cat} \sum \eta R_j H_{Rj} - (1 - \varepsilon) \rho_{cat} r_{carb} H_{carb} + h_w (T_w - T) \frac{4}{D_r} \quad (16)$$

where h_w is the heat transfer coefficient through the reactor wall, T_w is the reactor wall temperature and D_r is the inner diameter of the reforming reactor. Moreover, the carbonation kinetics employed in these works was also taken into account for the validation of the model. In the simulations, the operating temperature was varied between 923 K and 1023 K, the operating pressure between 0.1 MPa and 1.5 MPa, the S/C molar ratio between 3 and 7 and the residence time between 0.1 s^{-1} and 0.38 s^{-1} . The

results obtained were very similar to the simulated and experimental data reported by Lee et al. (2004) and Li and Cai (2007).

In order to choose a certain set of operating conditions to run the model and analyze the performance of the reactor, the equilibrium limitations of the reactions need to be taken into account. This matter has been dealt with in detail in previous works on sorption enhanced reforming, as recently reviewed by Harrison (2008) and is only briefly discussed here. The presence of a CO₂ sorbent in a steam methane reforming process shifts the equilibrium to the formation of H₂ with the result that an almost complete conversion of methane can be achieved. For example, if a SER operation is performed at 1.5 MPa and around 923 K with a steam/carbon molar ratio of 5 in the feed, it is possible to obtain a gas product with a H₂ content of about 97% (dry basis) (Fig. 2, right). Balasubramanian et al. (1999) achieved similar results working at these experimental conditions. It is also interesting to note that the hydrogen yield barely changes in the range of temperatures in which the carbonation occurs because of the quasi thermal neutrality of reaction (V). Although higher operating temperatures allow higher conversions of methane, the CO₂ capture efficiency decreases if the process is carried out over 1023 K, so that maximum H₂ production is achieved around 923-1023 K, depending on the operating pressure.

As can be seen in Fig. 2 (left), hydrogen production is favored at low pressures because of the increase in the number of moles in the products of reaction (V). However, the widespread interest in employing hydrogen for power generation and the high cost of H₂ compression found in other industrial applications suggest that it would be more profitable to perform the SER process at high pressure (1.5-3.5 MPa) (Metz et al., 2005; Harrison, 2008).

In view of these considerations, we carried out our study on SER at high pressure despite the unfavorable equilibrium conditions, due to the need to maximize the reactor performance per unit of cross-sectional area for any large scale CO₂ capture system. These conditions are also important for the SER stage of the Cu/Ca process (Abanades et al., 2010; Fernandez et al., 2012). To operate at high pressure, a high S/C molar ratio must be fed into the reforming reactor in order to obtain a gas product with hydrogen purities of over 90% (dry basis) and elevated methane conversions of around 85%, as can be seen in Fig. 2 (right). Moreover, high concentrations of H₂ and low levels of CO in the product stream reduce the carbon deposition, thereby avoiding catalyst deactivation and the blockage of the reforming reactor, which are serious problems in conventional SMR (Tavares et al., 1996; Alstrup et al., 1998). However, the latent heat of water cannot be totally recovered from the steam (Stevens et al., 2005). Therefore we must consider as a reasonable trade-off running the SER reactor in the reference case at 3.5 MPa at a S/C ratio of 5.

The choice of reactor length and the superficial gas velocity or throughput per unit reaction area, must again be a trade-off between the gas-solid contact time requirements and the maximum allowable pressure drop along the reactor. At this preliminary design stage, we have adopted a reactor length of 7 m and an inlet mass flow velocity (CH₄+steam) of 3.5 kg/m²s. These allow reasonable cycle times (Fernández et al., 2012) and lead a sharp breakthrough during the SER reaction stage. In so far as particle size and bed porosity are concerned, which are important variables in Eqs. (9-13), we have chosen for the reference case 0.01 m and 0.5, respectively, which are values commonly found inside the normal operating ranges in conventional steam reforming (Xu and Froment, 1989; Rostrup-Nielsen et al., 2002).

Finally, in order to obtain concrete solutions for the model, it is necessary to define the composition of the material in the bed. When the reactor is designed for typical SER operations a 30% weight of Ni-based conventional steam reforming has proved to be sufficient (Balasubramanian et al., 1999; Lopez Ortiz et al., 2001) for achieving enough catalytic activity for the reforming reactions. This can of course be largely reduced by using a more active reforming catalyst with noble transition metals (Jones et al., 2008). In the case of SER in the initial stage of the Cu/Ca looping process (Abanades et al., 2010), the right proportions of Cu and CaO need to be fulfilled and it is even more important to minimize the proportion of the catalyst (Fernandez et al., 2012), although several authors have shown that Cu-based catalysts provide enough activity to carry out the SMR at high temperature (up to 973 K) (Podbrscek et al., 2009).

A summary of the reactor characteristics and operating conditions for the reference case is provided in Table 3. These together with the physical parameters included in Table 2 and the initial and boundary conditions of Eqs. (14-15) make it possible to obtain a complete solution for the model.

3. Dynamic behavior of the fixed bed reactor for sorption enhanced reforming

The previous model has been designed to analyze the dynamic evolution of the molar concentrations of CH₄, H₂ and CO₂ in the axial direction of an adiabatic fixed-bed reforming reactor, performing with the operating conditions outlined in Table 3 and evolving with time until the breakthrough curves appear, which is when the CaO sorbent in the bed has been almost completely converted. The simulation also allows the evolution of the axial temperature profiles and its impact on the reactor performance to be studied.

Fig. 3 confirms the general trends observed in the SER reactors. As the gas stream passes through the bed, the molar concentration of CH_4 (and H_2O) progressively decreases while the concentration of H_2 increases via the reforming and water gas shift (WGS) reactions (reaction I to III). In the zones in which the CaO-based sorbent is active, the CO_2 formed is almost completely removed via reaction IV. The high operating pressure facilitates very fast carbonation rates. As in other sorption enhanced reforming reactors, this carbonation reaction shifts the equilibrium to a higher CH_4 conversion and a higher H_2 yield than the maximum achieved in a conventional SMR. As the carbonation front advances, the inactive sorbent is left behind and consequently, the reactor performs there as a conventional steam reformer (with a lower conversion of CH_4 , a lower H_2 yield and with no CO_2 capture).

As for the evolution of the axial temperature profiles (Fig. 3, bottom right), the temperature near the reactor entrance initially drops to about 868 K from the initial 923 K. This is because the highly endothermic reforming reactions (I) and (II) are faster than the exothermic CaO carbonation reaction (IV), resulting in a considerable drop in the temperature in the initial part of the reactor. When the gases reach the area with active CaO, the heat supplied by the carbonation reaction makes the overall reaction slightly exothermic and the heat is transported downstream, heating the solids up to slightly above the initial temperature of 923 K. In this way, the carbonation front raises the temperature of the bed as it moves towards the reactor exit.

The SER operation can be divided into three periods according to the evolution of the outlet temperature and gas composition with time (Fig. 4). During the prebreakthrough period ($t < 720$ s), the reforming, WGS and CaO carbonation reactions take place simultaneously and the composition of the product gas is close to the SER equilibrium (i. e. a H_2 mole percent of above 94% and a content of CO_2 of about 0.1%

on a dry basis). During the breakthrough period, which takes place approximately from $t=720$ s to $t=1500$ s, the CO_2 capture efficiency begins to diminish because the CaO -sorber is approaching its point of maximum conversion (X_{max}). The extent of the reforming and the WGS reactions is gradually reduced, resulting in a decrease in hydrogen purity and in methane conversion. When all the sorber is saturated with CO_2 ($t>1500$ s), the separation is no longer effective and only the reforming and shift reactions occur. In the postbreakthrough period the bed performs as a stationary reforming reactor producing a gas stream close to the SMR equilibrium, as illustrated in Fig. 4 (53% of H_2 , 33% of CH_4 , 13% of CO_2 and 1% of CO on a dry basis).

Because of the slight exothermicity of the overall reforming and carbonation reaction (reaction V), the exit gas gradually increases its temperature during the prebreakthrough period. At the beginning of the breakthrough (about $t=720-900$ s) the maximum temperature reached is 955 K which represents a rise of 32 K above the feed gas temperature, as shown in Fig. 4 (right).

So far, the SER performance has been theoretically designed and experimentally implemented to function close to isothermal conditions (Harrison, 2008). This configuration has possibly been inherited from conventional SMR operation, in which a large amount of external heat must be supplied to the reformer in order to achieve the temperature that allows the endothermic steam reforming reaction to take place. However, only adiabatic conditions would make it possible to take full advantage of the SER thermal neutrality and maximize the energy efficiency of the process thereby eliminating the need for heat transfer equipment around the reactor. To investigate the difference between the two performances, we introduced into our model Eq. (16) for the simulation of the operation under non-adiabatic (quasi-isothermal) conditions ($T_w=923$

K), similar to previous works (Lee et al., 2004; Li and Cai, 2007), but taking into account common operating parameters shown in Table 3.

As can be seen in Fig. 5, during the prebreakthrough period ($t < 720$ s), there is a substantial difference in the temperature of the flue gas in both configurations. However, this does not translate into any difference in hydrogen yield or methane conversion and the resulting composition of the product gas is almost the same. During the breakthrough period, the CaO-based sorbent is approaching its point of maximum conversion and the CO₂ capture efficiency begins to decay. Therefore, the proportion of CO₂ in the flue gas gradually increases. At the beginning of the breakthrough (from $t = 720$ s to $t = 1080$ s), the temperature of the product gas under adiabatic conditions is higher than that obtained under quasi-isothermal conditions (Fig. 5, right). Higher temperatures during this transient period from SER to SMR lead to a higher CO₂ yield. Therefore, the carbonation rate increases, (Eq. 6), and the CaO sorbent rapidly approaches its total saturation point, resulting in a shorter breakthrough period under adiabatic conditions. These results confirm that the adiabatic configuration provides the most favorable performance for carrying out the sorption enhanced reforming in fixed beds under alternative reaction conditions.

On the other hand, breakthroughs are expected to occur at well defined points of time and close to those achieved considering infinite reactions rates (dotted vertical line in Fig. 4). However, it is clear that, in order to obtain a hydrogen product gas of high purity, it is necessary to choose a point in time before the end of the breakthrough, because during this period a significant part of the CaO-sorbent has still not been converted. Consequently, the duration of the SER stage will be a trade-off that leads to the production of a high level of H₂ with a minimum loss of CH₄ and CO and a high degree of carbonation of the CaO-sorbent. In order to clarify this point, we must

consider the sensitivity of the model predictions of the breakthrough curves to certain critical material properties that may affect the reactivity of CaO and its absorption capacity.

The sorption capacity and reactivity of the CaO-based material may play a decisive role in the overall efficiency and viability of any process based on the SER principle. The proportion of any solids other than the active CaO in the fixed bed must be kept to a minimum in order to reduce the heat required for the endothermic sorbent regeneration. This is even more important in the case of the Ca/Cu looping process (Abanades et al., 2010), where all the heat required for the calcination of the sorbent must be supplied by the reduction of a certain amount of CuO, which is accompanied in the matrix bed by CaO and a reforming catalyst (Fernández et al., 2012).

As for the kinetics of carbonation, a higher sorbent capacity, expressed in terms of maximum carbonation conversion (X_{\max}), tends to accelerate the removal of CO₂ in the SER, as shown in Eq. (6). Natural limestone can achieve a stable X_{\max} (after hundreds of cycles of absorption and desorption) of less than 0.10 (Grasa and Abanades, 2006) which would correspond to a sorbent capacity of about only 1 mol CO₂/kg sorbent. On the other hand, some novel synthetic CO₂-sorbents have sorbent capacities of about 5 mol CO₂/kg, as reported in the literature (Ochoa et al., 2005; Manovic et al., 2009; Halabi et al., 2011). Several works in the literature dealing with CaO-based synthetic sorbents for SER or similar applications report that these sorbents maintain a high residual activity (higher than 0.3 mol fraction) even after a large number of carbonation/calcinations cycles (Stevens et al., 2007; Manovic and Anthony, 2008; Manovic and Anthony, 2009; Blamey et al., 2010).

The profiles of the product gas composition on a dry basis at different maximum carbonation conversions (X_{\max}) are represented in Fig. 6. A hydrogen purity of close to equilibrium (95% on a dry basis) can be achieved with sorbents with high residual activity (X_{\max} higher than 0.2). However, less active sorbents lead to lower H_2 yields and shorter reactor operational times before the breakthrough. For this reason, natural limestones can be ruled out as sorbent candidates for this process. The prebreakthrough period can be extended from 600 s to 1200 s by using sorbents with a maximum carbonation conversion of between 0.2 and 0.4.

The carbonation rate corresponding to two sorbents with different maximum carbonation conversions at different reformer locations is represented in Fig. 7. The sorption waves moving on along the fixed-bed demonstrate that the carbonation reaction takes place in a narrow reaction front as the feeding gas is introduced and the CO_2 -sorbent is saturated. The sorbent with the higher sorption capacity significantly improves the carbonation kinetics, accelerating the carbonation rate (r_{carb}) by a factor of 2.5. The maximum local carbonation rate achieved with the natural sorbent ($X_{\max}=0.1$) was found to be $5.55 \cdot 10^{-6}$ kmol/kg s, while with the synthetic sorbent ($X_{\max}=0.4$) a carbonation rate of about $1.25 \cdot 10^{-5}$ kmol/kg s was achieved. Moreover, Fig. 7 shows that the stationary SER period before the saturation of the bed can be extended considerably by employing materials with a higher sorption capacity, as indicated above.

On the other hand, it is well known that the initial stage of the carbonation reaction is rapid and kinetically controlled, and that it is then followed by a subsequent stage which is much slower and controlled by the diffusion of CO_2 in the product layer (Bhatia and Perlmutter, 1983). According to Eq. (6), the velocity of the initial carbonation stage is mainly determined by the carbonation rate constant (k_{carb}). As pointed out above, natural

limestones present values of k_{carb} of around 0.35 s^{-1} . It is possible to find in the literature several works that employ synthetic CO_2 sorbents with a higher mechanical and chemical stability but with less reactivity (lower k_{carb}) (Lee et al., 2004; Li and Cai, 2007). Nevertheless, there are also many works that have attempted to obtain sorbents with a better stability and reactivity than natural sorbents by using new synthesis routes (Stevens et al., 2007; Blamey et al., 2010) or recently developed materials that combine both sorbent and catalyst properties (Martavaltzi et al., 2010; Meyer et al., 2011).

The effect of the carbonation rate constant (k_{carb}) on the evolution of the outlet gas composition and temperature with time is represented in Fig. 8, under conditions of 923 K, 3.5 MPa, by feeding $3.5 \text{ kg/m}^2\text{s}$ with a S/C molar ratio of 5 and assuming a maximum carbonation conversion for the sorbent (X_{max}) of 0.4. As can be seen in Fig. 8, a less reactive sorbent with half the reactivity of a natural limestone ($k_{\text{carb}}=0.18 \text{ s}^{-1}$) does not allow the SER equilibrium (97% on a dry basis) to be reached and therefore a lower degree of hydrogen purity is obtained (92% on a dry basis). Moreover, less reactive sorbents do not lead to sharp breakthroughs, which involve shorter cycles during the SER operation if the objective is to obtain a gas product with high H_2 purity and a minimum loss of CH_4 and CO .

However, natural limestones and more reactive sorbents ($k_{\text{carb}}>0.35 \text{ s}^{-1}$) allow a SER performance close to equilibrium and a maximum H_2 content of about 97% is therefore obtained. Hypothetical more reactive sorbents than natural limestones would allow sharper breakthroughs to be reached, but the resulting stationary period (prebreakthrough) would not be much longer. As pointed out above, the prebreakthrough period with a natural limestone as CO_2 sorbent takes place during the first 720 s of the SER performance under the operating conditions listed in Table 3. The

use of a hypothetical sorbent 10 times more reactive ($k_{\text{carb}}=3.5 \text{ s}^{-1}$) only extends the prebreakthrough period from 720 s to 900 s, as shown in Fig. 8 (left).

As for the temperature profiles of the flue gas, these are more affected by the carbonation rate constant. If the carbonation reaction is very slow, this exothermic reaction takes place gradually along the fixed bed, while the rapid endothermic reforming reaction occurs in a narrow front. The result is a slight increase in the flue gas temperature during the SER operation. If the sorbent is highly reactive leading to a much faster CO_2 absorption, all the reactions involved in the SER process take place simultaneously in the same reaction fronts along the fixed-bed, with the result that the maximum temperature achieved increases, as can be seen in Fig. 8 (right). If a slow-reacting sorbent is used ($k_{\text{carb}}=0.18 \text{ s}^{-1}$), the maximum temperature achieved during the SER operation is 943 K, whereas T_{max} increases up to 990 K if an extremely high reactive sorbent ($k_{\text{carb}}=3.5 \text{ s}^{-1}$, 10 times greater than the carbonation constant for a natural CO_2 -sorbent) is used since this entails practically instantaneous carbonation. This value is close to 1006 K, which is the maximum temperature theoretically estimated for an adiabatic SER process, if instantaneous kinetics are considered (Fernández et al., 2012). Furthermore, the minimum temperature reached during the postbreakthrough period is not affected by the carbonation kinetics. In either case, the saturated bed cools down to a stationary temperature of about 868 K.

The carbonation rate (r_{carb}) for two CO_2 sorbents of different reactivity (a natural limestone and a hypothetical synthetic sorbent 10 times more reactive) in different reformer locations is represented in Fig. 9. The results show that a higher carbonation rate constant (k_{carb}) significantly improves the carbonation kinetics. The maximum local carbonation rate with the natural limestone ($k_{\text{carb}}=0.35 \text{ s}^{-1}$) was found to be around 1.4

10^{-5} kmol/kg s, while the synthetic sorbent ($k_{\text{carb}}=3.5 \text{ s}^{-1}$) attained a carbonation rate higher than $1.11 \cdot 10^{-4}$ kmol/kg s. A great increase in the reactivity of the sorbent leads to very narrow carbonation reaction fronts. However, the use of very reactive sorbents does not involve higher velocities of the carbonation reaction front along the fixed-bed. Fig. 9 shows that both sorbents exhibit their maximum local carbonation rate for every axial location at similar operating times. Therefore, efforts to develop more reactive synthetic CO_2 sorbents would only lead to shorter breakthroughs with similar stationary SER periods before bed saturation.

As explained above, sorbents with a higher reactivity accelerate the removal of CO_2 in the SER and therefore it is possible to perform close to equilibrium at higher space velocities. Fig. 10 shows the composition and temperature profiles of the product gas on a dry basis at different space velocities (2.1, 3.5 and $7 \text{ kg/m}^2\text{s}$) for sorbents with a different carbonation rate constant (0.18, 0.35 and 0.70 s^{-1}), at 923 K, 3.5 MPa and a S/C molar ratio of 5. Under these operating conditions, the maximum superficial velocity reached by the gas in the reforming reactor would be 0.3, 0.5 and 1 m/s, respectively.

Slow-reacting CO_2 sorbents do not allow the maximum hydrogen purity determined by the equilibrium at elevated space velocities to be achieved. Higher residence times are therefore needed. These will require longer operational periods to permit total sorbent saturation and entail higher capital investment and operating costs. However, highly reactive materials lead to a maximum hydrogen production at higher space velocities, which in turn entails shorter SER cycles for total sorbent carbonation.

As indicated in Fig. 10, a CO_2 sorbent with slow carbonation kinetics ($k_{\text{carb}}=0.18 \text{ s}^{-1}$) requires low space velocities ($2.1 \text{ kg/m}^2\text{s}$) in order to achieve the maximum degree of

H₂ purity determined by the SER equilibrium (95% on a dry basis). Under these operating conditions, the postbreakthrough period is finally achieved after 2700 s of performance. If a sorbent with a significantly higher carbonation rate is used ($k_{\text{carb}}=0.70 \text{ s}^{-1}$, twice the carbonation rate constant of a natural CO₂-sorbent), the SER operation can be carried out at a space velocity of about 7 kg/m²s (around 1 m/s under these operating conditions) which corresponds approximately to velocities usually employed in conventional steam reformers at industrial scale (Rostrup-Nielsen et al., 2002). Moreover, the duration of the cycle up to total sorbent saturation can be reduced from 2700 s to 780 s. Neither the maximum temperature reached in the SER operation (953 K) nor the minimum temperature in the postsbreakthrough period (868 K) are affected by the use of the maximum allowable space velocity for achieving equilibrium according to the carbonation kinetics of the sorbent, as can be seen in Fig. 10.

The above analysis highlights the importance of CaO reactivity (fast reaction rate) and the carrying capacity of synthetic CO₂ sorbents for SER applications. In order to be able to design compact reactors that optimize the production of hydrogen with sharp breakthroughs, it is essential to employ materials with maximum carbonation conversions (X_{max}) of at least 0.4 (about 3-4 times higher than natural sorbents) and with a carbonation rate constant (k_{carb}) at least similar to those measured in natural limestones. There are two major ways to achieve this condition: (i) to design stable materials with the appropriate properties (high X_{max} or high k_{carb}) or (ii) to design intermediate steps for sorbent reactivation. Promising results have been recently published in both directions (see review of Blamey et al., 2010), stimulating a huge amount of interest in the use of CaO-based sorbents in the sorption enhanced reforming process.

5. Conclusions

Adiabatic sorption-enhanced steam reforming (SER) reactors using CaO as a CO₂ sorbent can be mathematically described using well established principles for fixed-bed reactors. The resulting pseudo-homogeneous model is able to describe the transient behaviour of the SER process from a set of initial conditions to a point beyond the breakthrough associated to the full conversion of the CaO. Three different periods have been established: (i) prebreakthrough, in which the reactor can perform close to the SER equilibrium in which case the hydrogen yield is maximum and the CO₂ production is negligible; (ii) breakthrough in which CO₂ capture efficiency decays because the sorbent is approaching its maximum limit of conversion, and (iii) postbreakthrough in which the CO₂-sorbent reaches total saturation and consequently the reactor performs like a conventional steam methane reformer. The process was found to be highly efficient at 923 K, 3.5 MPa, feeding a S/C molar ratio of 5 and at a space velocity of 3.5 kg/m²s, yielding a hydrogen purity of about 95%, a methane conversion of about 85% and negligible traces of CO₂. The limiting aspect of the SER process was found to be basically the carbonation kinetics, making it necessary to use lower space velocities than those employed in the conventional steam reforming (SMR). Natural limestones can be ruled out as CaO precursors for this process. CO₂-sorbents with a high sorption capacity are more suitable because they permit faster carbonation kinetics and a longer operational time before the breakthrough.

Acknowledgements

The authors acknowledge the grant awarded by the Spanish Science and Innovation Ministry under the project ENE2009-11353 and CSIC (201280E017).

Nomenclature

C_i	concentration of component i in the reactor, kmol/m^3
$C_{i,\text{in}}$	concentration of component i in the feed, kmol/m^3
$C_{i,0}$	initial concentration of component i , kmol/m^3
C_{pg}	specific heat capacity of the gas, kJ/kg K
C_{ps}	specific heat capacity of the solid, kJ/kg K
D_e	effective diffusivity, m^2/s
d_p	particle diameter, m
D_r	inner diameter of the reactor, m
H_{carb}	heat of CaO carbonation, kJ/kmol
h_{fs}	fluid-gas heat transfer coefficient, $\text{kW}/(\text{m}^2 \text{K})$
H_{Rj}	heat of reaction j ($j=\text{I, II, III}$), kJ/kmol
h_w	heat transfer coefficient through the reactor wall, $\text{kW}/(\text{m}^2 \text{K})$
k_{carb}	rate constant of CaO carbonation, s^{-1}
k_g	thermal gas conductivity, $\text{kW}/(\text{m K})$
k_j	rate constant of reaction j ($j= \text{I, II, III}$), $\text{kmol MPa}^{0.5}/\text{kg s}$
K_i	adsorption constant of component i , $i=\text{CO, H}_2, \text{CH}_4 \text{ MPa}^{-1}$; $i=\text{H}_2\text{O}$ dimensionless
K_j	equilibrium constant of reaction j , $j=\text{I, II MPa}^2$; $j=3$ dimensionless
k_{fs}	gas-solid mass transfer coefficient, m/s
L	reactor length, m
M_{CaO}	molecular weight of CaO, kg/kmol
M_g	molecular weight of the gas, kg/kmol
P	total pressure, MPa

P_i	partial pressure of component i , MPa
P_{in}	pressure at the reactor entrance, MPa
r_{carb}	rate of CaO carbonation, $\text{kmol}/\text{kg}_{cat} \text{ s}$
r_i	rate of formation/consumption of component i , $\text{kmol}/\text{kg s}$
R	ideal gas constant, $\text{kJ}/\text{kmol K}$
R_j	rate of reaction j ($j=I, II, III$), $\text{kmol}/\text{kg s}$
t	time, s
T	temperature, K
T_w	reactor wall temperature, K
T_{in}	feed gas temperature, K
T_0	initial temperature of the solids in the reactor, K
u	superficial velocity of gas, m/s
x_i	gas-phase mole fraction of component i , dimensionless
X	fractional carbonation conversion of CaO, dimensionless
X_{max}	maximum fractional carbonation conversion of CaO, dimensionless
z	axial coordinate in bed, m

Greek letters

ε	bed void fraction, dimensionless
ϕ_{ij}	stoichiometric coefficient of component i , dimensionless
ρ_{CaO}	apparent density of CaO-based material, kg/m^3
ρ_{cat}	apparent density of reforming catalyst, kg/m^3
ρ_g	gas phase density, kg/m^3
ρ_s	apparent density of the two mixed solids in the reactor, kg/m^3
η	effectiveness factor, dimensionless

v_{CO_2} gas-phase mole fraction of CO_2 , dimensionless
 $v_{CO_2,eq}$ gas-phase equilibrium mole fraction of CO_2 , dimensionless
 μ_g viscosity of gas, MPa s

References

- Abanades, J. C., 2002. The maximum capture efficiency of CO_2 using a carbonation/calcinations cycle of $CaO/CaCO_3$. *Chemical Engineering Journal* 90, 303-306.
- Abanades, J. C., Murillo, R., Fernandez, J.R.; Grasa, G., Martinez, I., 2010. New CO_2 capture Process for Hydrogen production Combining Ca and Cu Chemical Loops. *Environmental Science & Technology* 44, 6901-6904.
- Alstrup, I., Tavares, M. T., Bernardo, C. A., Sorensen, O., Rostrup-Nielsen, J. R., 1998. Carbon formation on nickel and nickel-copper alloy catalyst. *Materials and Corrosion* 49, 367-372.
- Balasubramanian, B., Lopez Ortiz, A., Kaytakoglu, S., Harrison, D.P., 1999. Hydrogen from methane in a single-step process. *Chemical Engineering Science* 54, 3543-3552.
- Baker, E. H. 1962. The calcium oxide-calcium dioxide system in the pressure range 1-300 atmospheres. *Journal of the Chemical Society* 464-470.
- Blamey, J., Anthony, E. J., Wang, J., Fennell, P. S., 2010. The calcium looping cycle for large-scale CO_2 capture. *Progress in Energy and Combustion Science* 36 (2), 260-279.

- Bhatia, S. K., Perlmutter, D. D. 1983. Effect of the product layer on the kinetics of the CO₂-lime reaction. *AIChE Journal* 29, 79-86.
- Borman, P. C., Borkink, J. G. H., Westerterp, K. R., 1992. Heat transport in a wall heated tubular packed bed reactor at elevated pressures and temperatures. *Chemical Engineering Communications* 114, 17-47.
- Breault, W. B. 2006. A review of gas-solid dispersion and mass transfer coefficient correlations in circulating fluidized beds. *Powder Technology* 163, 9-17.
- Dennis, J. S., Hayhurst, A. N. 1987. The effect of CO₂ on the kinetics and extent of calcinations of limestone and dolomite particles in fluidized beds. *Chemical Engineering Science* 42, 2361-2372.
- Dixon, A. D., 1979. Theoretical prediction of effective heat transfer parameters in packed beds. *AIChE Journal* 25, 663-676.
- Dybkjaer, I., 1995. Tubular reforming and autothermal reforming of natural gas -an overview of available processes. *Fuel Processing Technology* 42, 85-107.
- Ergun, S. 1952. Fluid flow through packed columns. *Chemical Engineering Progress* 48, 89-94.
- Fernández, J.R.; Abanades, J. C., Murillo, R., Grasa, G., 2012. Conceptual design of a hydrogen production process from natural gas with CO₂ capture using a Ca-Cu chemical loop. *International Journal of Greenhouse Gas Control*, 6, 126-141.
- Florin, N. H.; Harris, A. T., 2008. Enhanced hydrogen production from biomass with in situ carbon dioxide capture using calcium oxide sorbents. *Chemical Engineering Science* 63, 287-316.

- Grasa, G., Abanades, J. C. 2006. Capture Capacity of CaO in Long Series of Carbonation/Calcination cycles. *Industrial & Engineering Chemistry Research* 45, 8846-8851.
- Grasa, G., Abanades, J. C., Alonso, M., González, B. 2008. Reactivity of highly cycled particles of CaO in a carbonation/calcinations loop. *Chemical Engineering Journal* 137, 561-567.
- Grasa, G., Murillo, R., Alonso, M., Abanades, J. C. 2009. Application of the Random Pore Model to the Carbonation Cyclic Reaction. *AIChE Journal* 55, 1246-1255.
- Grasa, G., Abanades, J. C., Alonso, M., González, B. 2008. Reactivity of highly cycled particles of CaO in a carbonation/calcinations loop. *Chemical Engineering Journal* 137, 561-567.
- Halabi, M. H., de Croon, M. H. J. M., van der Schaaf, J., Cobden, P. D., Schouten, J. C. 2011. Reactor modeling of sorption enhanced autothermal reforming of methane. Part I: Performance study of hydrotalcite and lithium zirconate-based process. *Chemical Engineering Journal* 168, 872-882.
- Halabi, M. H., de Croon, M. H. J. M., van der Schaaf, J., Cobden, P. D., Schouten, J. C. 2011. Effect of operational parameters. Part II: Performance study of hydrotalcite and lithium zirconate-based process. *Chemical Engineering Journal* 168, 872-882.
- Harrison, D. P., 2008. Sorption-Enhanced Hydrogen Production: A Review. *Industrial & Engineering Chemistry Research* 47, 6486-6501.
- Huften, J. R., Mayorga, S., Sircar, S. 1999. Sorption-enhanced reaction process for hydrogen production. *AIChE Journal* 45, 248-256.

- Jones, G., Jakobsen, J. G., Shim, S. S., Kleis, J., 2008. First principles calculations and experimental insight into methane steam reforming over transition metal catalysts. *Journal of Catalysis* 259, 147-160.
- Lee, D. K., Baek, I. H., Yoon, W. L., 2004. Modeling and simulation for the methane steam reforming enhanced by in situ CO₂ removal utilizing the CaO carbonation for H₂ production. *Chemical Engineering Science* 59, 931-942.
- Levenspiel, O. S., 1979. *The Chemical Reactor Omnibook*, Oregon State University Book Stores.
- Li, Z., Cai, N., 2007. Modeling of Multiple Cycles for Sorption-Enhanced Steam Methane Reforming and Sorbent Regeneration in Fixed Bed Reactor. *Energy & Fuels* 21, 2909-2918.
- Lopez Ortiz, A., Harrison, D.P., 2001. Hydrogen Production Using Sorption-Enhanced Reaction. *Industrial & Engineering Chemistry Research* 40, 5102-5109.
- Lysikov, A. I., Trukhan, S. N., Okunev, A. G., 2008. Sorption enhanced hydrocarbons reforming for fuel cell powered generators. *International Journal of Hydrogen Energy* 33, 3061-3066.
- Manovic, V., Anthony, E. J., 2008. Thermal activation of CaO-based sorbent and self-reactivation during CO₂ capture looping cycles. *Environmental Science & Technology* 42, 4170-4174.
- Manovic, V., Anthony, E. J., 2009. Long-term behavior of CaO-based pellets supported by calcium aluminate cements in a long series of CO₂ capture cycles. *Industrial & Engineering Chemistry Research* 48, 8906-8912.

- Martavaltzi, C. S., Lemonidou, A. A., 2010. Hydrogen production via sorption enhanced reforming of methane: Development of a novel hybrid material-reforming catalyst and CO₂ sorbent. *Chemical Engineering Science* 65, 4134-4140.
- McCabe W. L., Smith, J. C., Harriot, P. 1985. *Unit Operations in Chemical Engineering*, McGraw-Hill, New York.
- Meyer, J., Mastin, J., Bjornebole, T. K., Ryberg, T.; Eldrup, N., 2011. Techno-economical study of the Zero Emission Gas power concept. *Energy Procedia*. 4, 1949-1956.
- Metz, B., Davidson, O., de Coninck, H., Loos, M., Meyer, L., 2005. *IPPC Special Report on Carbon Dioxide Capture and Storage*, Intergovernmental Panel on Climate Change. Cambridge University Press.
- Ochoa-Fernandez, E., Rusten, H. K., Jakobsen, H. A., Holmen, A., Chen, D., 2005. Sorption enhanced hydrogen production by steam methane reforming using Li₂ZrO₃ as sorbent: sorption kinetics and reactor simulation. *Catalysis Today* 106, 41-46.
- Podbrscek, P., Orel, Z. C., Macek, J., 2009. Low temperature synthesis of porous copper/zinc oxide. *Materials Research Bulletin* 44, 1642-1646.
- Reijers, H. T. J.; Boon, J., Elzinga, G. D., Cobden, P. D., Haije, W. G., van den Brink, R. W. 2009. Modeling Study of the Sorption-Enhanced Reaction Process for CO₂ Capture. I. Model Development and Validation. *Industrial & Engineering Chemistry Research* 48, 6966-6974

- Reijers, H. T. J.; Boon, J., Elzinga, G. D., Cobden, P. D., Haije, W. G., van den Brink, R. W. 2009. Modeling Study of the Sorption-Enhanced Reaction Process for CO₂ Capture. II. Application to Steam-Methane Reforming. *Industrial & Engineering Chemistry Research* 48, 6966-6974
- Rodríguez, N., Alonso, M., Abanades, J. C. 2011. Experimental Investigation of a Circulating Fluidized-Bed Reactor to Capture CO₂ with CaO. *AIChE Journal* 57, 1356-1366
- Rostrup-Nielsen, J. R., Sehested, J., Norskov, J. K., 2002. Hydrogen and Synthesis Gas by Steam and CO₂ Reforming. *Advances in Catalysis* 47, 65-139.
- Rusten, H. K., Ochoa-Fernández, E., Chen, D., Jakobsen, H. A., 2007. Numerical Investigation of Sorption Enhanced Steam Methane Reforming Using Li₂ZrO₃ as CO₂-acceptor. *Industrial & Engineering Chemistry Research* 46, 4435-4443.
- Solsvik, J., Jakobsen, H. A., 2011. A numerical study of a two property catalyst/sorbent pellet design for the sorption-enhanced steam–methane reforming process: Modeling complexity and parameter sensitivity study. *Chemical Engineering Journal* 178, 407-422.
- Stevens, J. F., Krishnamurthy, B., Atanassova, P., Spilker, K., 2007. Development of 50 kW Fuel Processor for Stationary Fuel Cell Applications, Final Report, DOE/GO/13102-1.
- Tavares, M. T., Alstrup, I., Bernardo, C. A., Rostrup-Nielsen, J. R., 1996. Carbon deposition and CO methanation on silica-supported nickel and nickel copper catalysts in CO+H₂ mixtures. *Journal of Catalysis* 158, 402-410.

- Twiggs, M. V. 1989. Catalyst Handbook, Wolfe Publishing Ltd., UK.
- Xiu, G. H., Li, P., Rodrigues, A. E. 2002. Sorption-enhanced reaction process with reactive regeneration. *Chemical Engineering Science* 57, 3893-3908.
- Xu, J., Froment, G. F., 1989. Methane steam reforming, methanation and water-gas shift: I. Intrinsic kinetics. *AIChE Journal* 35, 88-96.
- Yi, K. B., Harrison, D. P., 2005. Low-Pressure Sorption-Enhanced Hydrogen Production. *Industrial & Engineering Chemistry Research* 44, 1665-1669.
- Yoon, Y. I., Baek, I. H., Park, S. D., 2007. Enhancement of H₂ production by combination with CO₂ absorption in steam methane reforming in bench scale. *Journal of Industrial Engineering Chemistry* 13 (5), 842-849.

Figure captions

Fig. 1. General scheme of the composition and temperature profiles in the reaction front during the SER in a fixed-bed reactor.

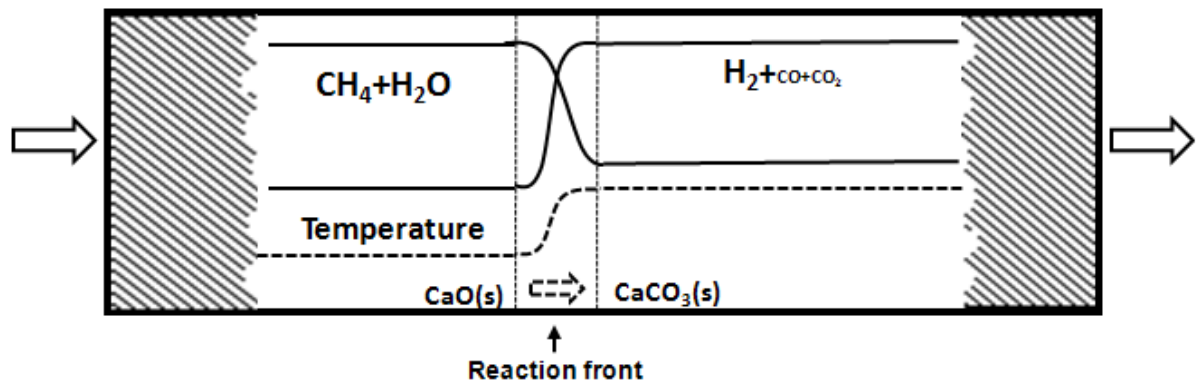


Fig. 2. Effect of pressure, temperature and S/C molar ratio in hydrogen production and methane conversion on the sorption enhanced reforming equilibriums; (S/C=5, left and P=3.5 MPa, right).

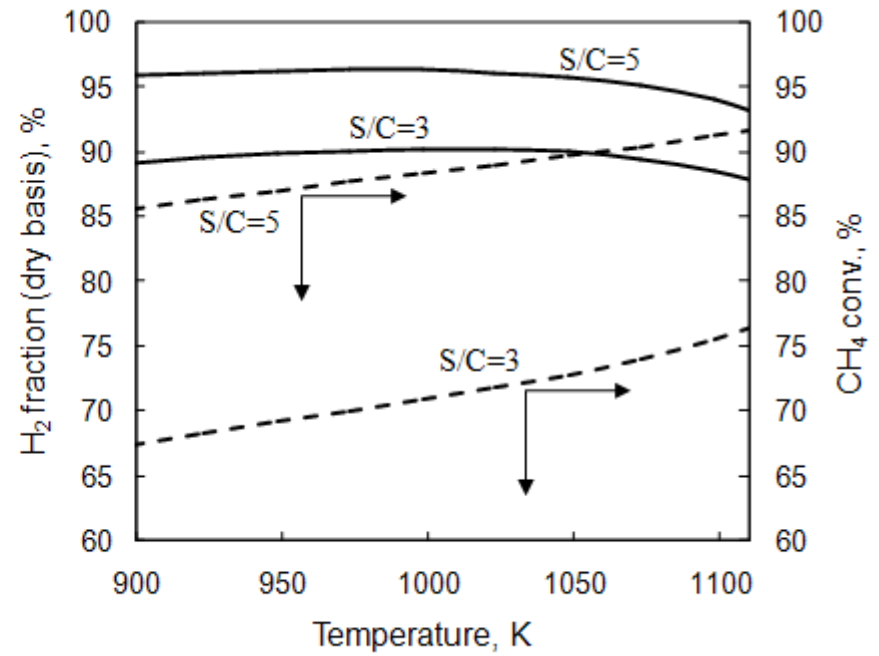
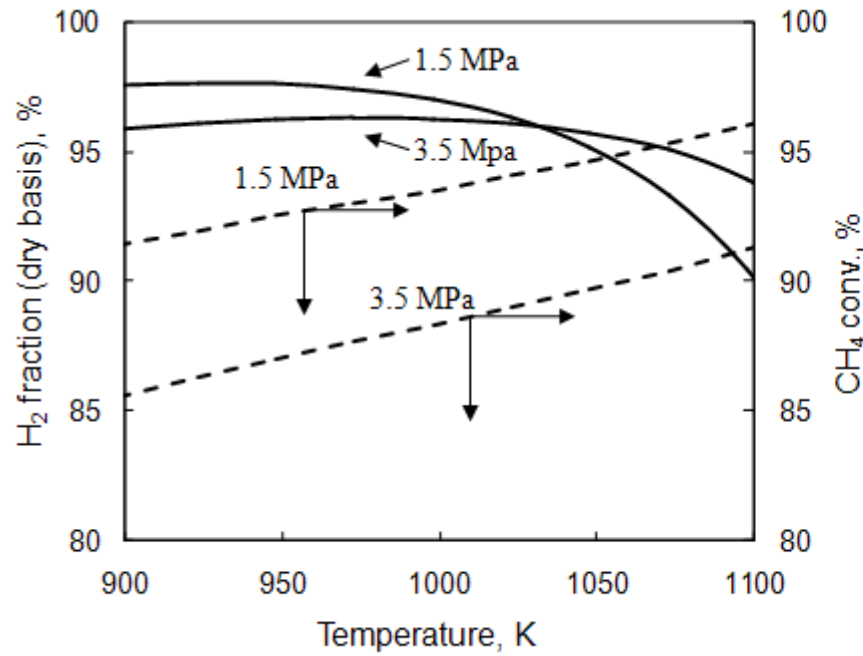


Fig. 3. Dynamic profiles of CH₄, H₂, CO₂ and temperature in a SER operation carried out in an adiabatic fixed-bed reactor (at the conditions shown in Table 3: 923 K, 3.5 MPa, S/C molar ratio of 5).

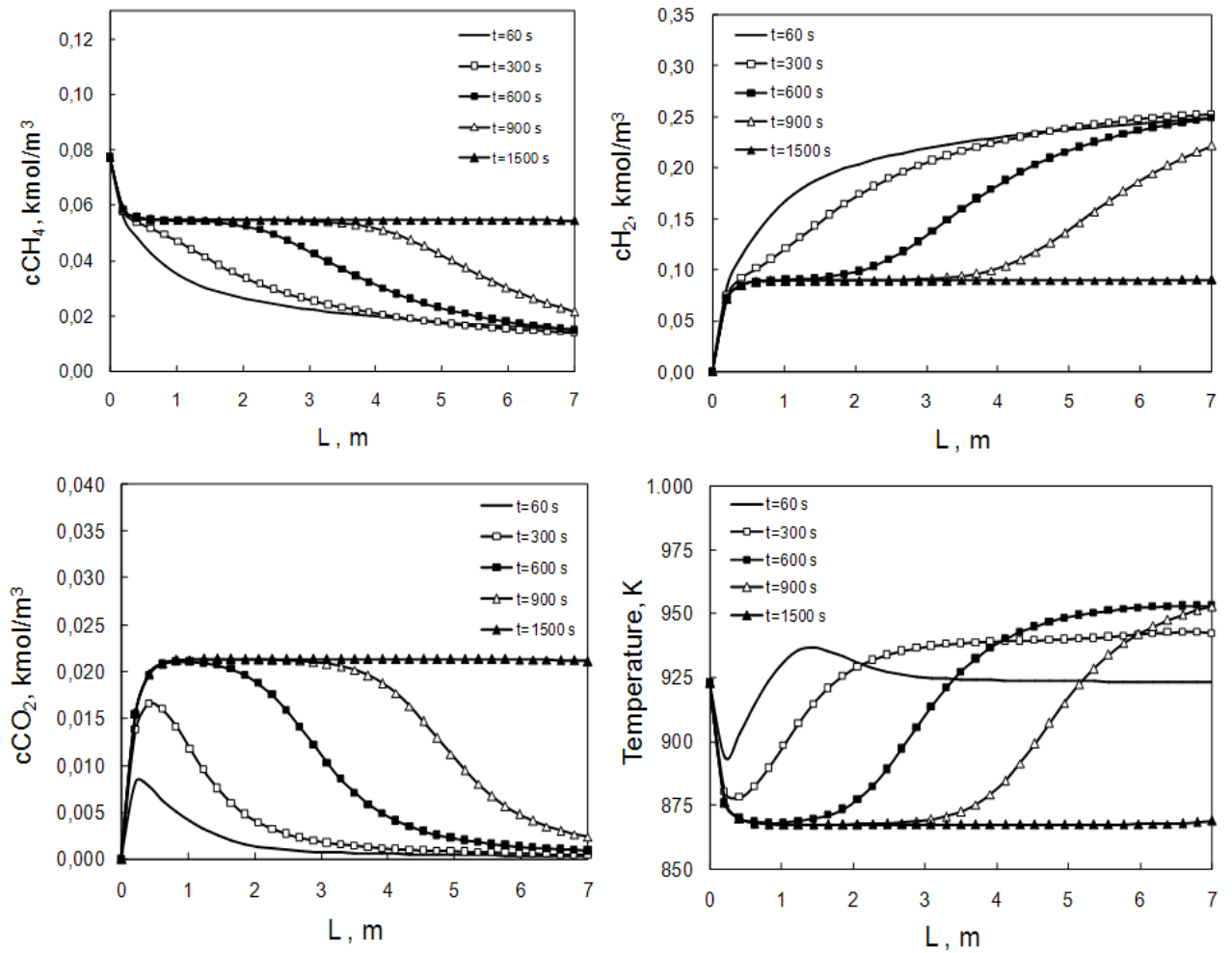


Fig. 4. Product gas composition on a dry basis and temperature evolution of the gases leaving the reactor time on stream (at the conditions shown in Table 3: 923 K, 3.5 MPa, S/C molar ratio of 5).

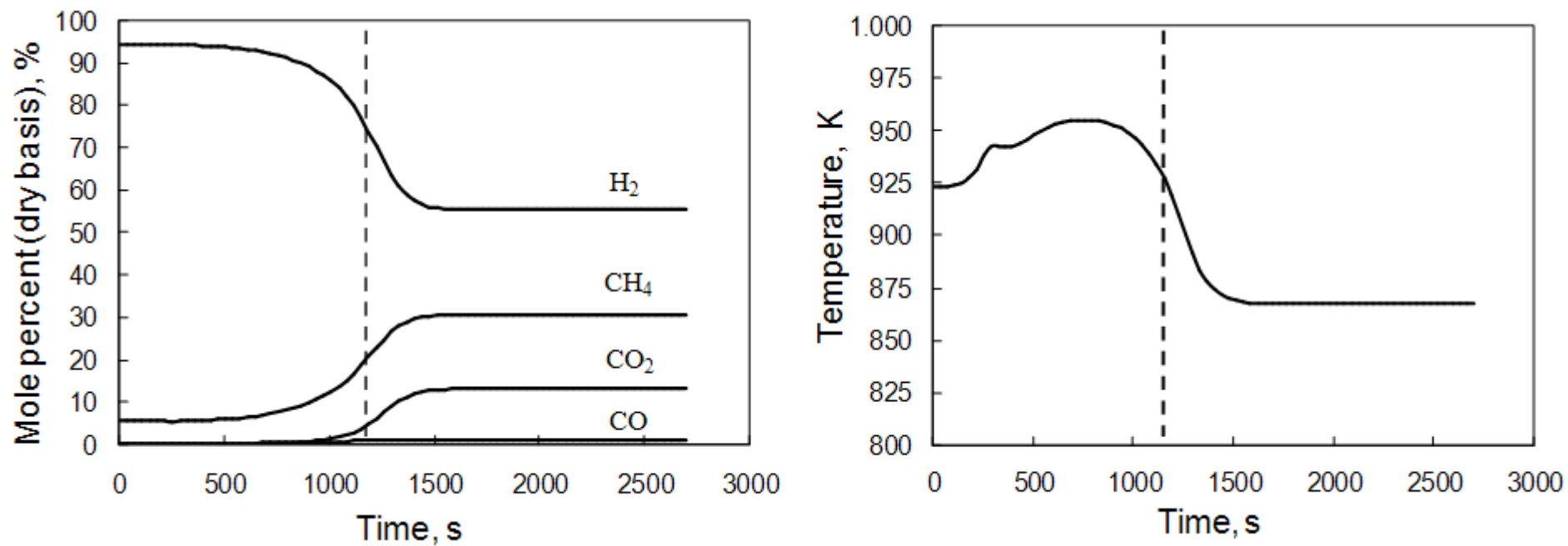


Fig. 5. Comparison of adiabatic and non-adiabatic SER performance in terms of product gas composition and temperature profiles time on stream (at the conditions shown in Table 3: 923 K, 3.5 MPa, S/C molar ratio of 5).

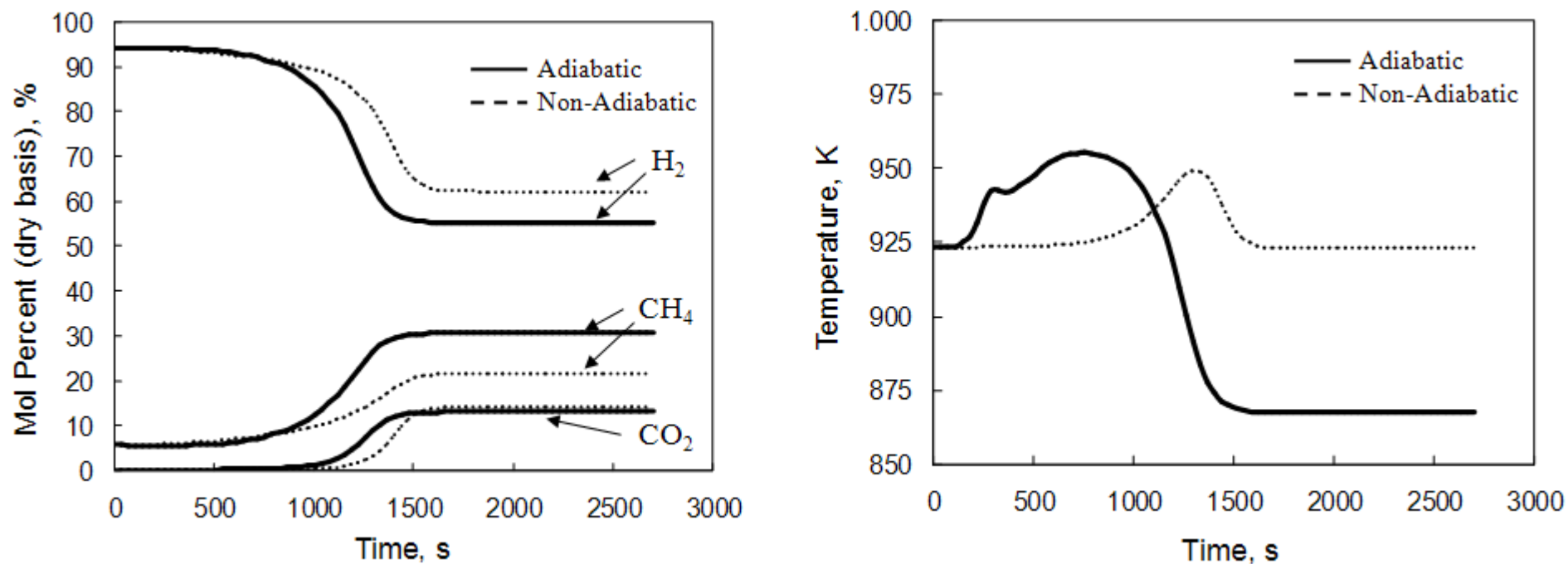


Fig. 6. Dynamic H₂ and CO₂ profiles on a dry basis at the reactor exit at different maximum carbonation conversions (923 K, 3.5 MPa, S/C molar ratio of 5, 2 kg/m²s and $k_{\text{carb}}=0.35 \text{ s}^{-1}$).

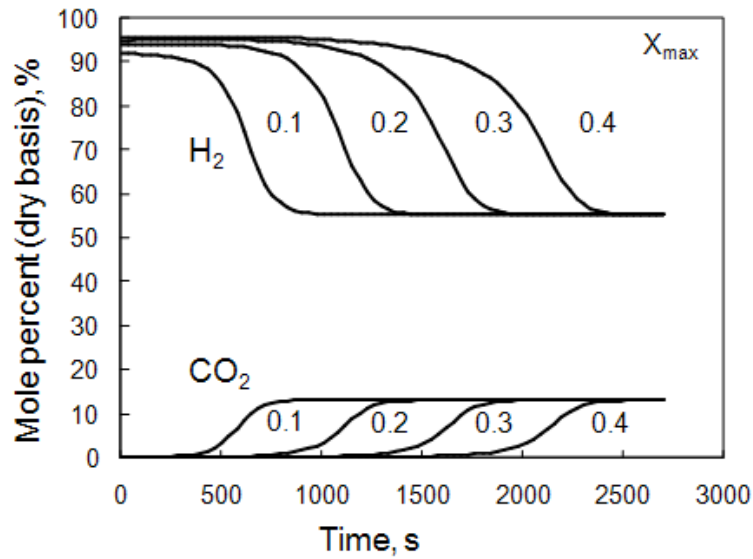


Fig. 7. Effect of maximum carbonation conversion on the carbonation rate at different locations along the reformer (923 K, 3.5 MPa, S/C molar ratio of 5, 2 kg/m²s and $k_{\text{carb}}=0.35 \text{ s}^{-1}$).

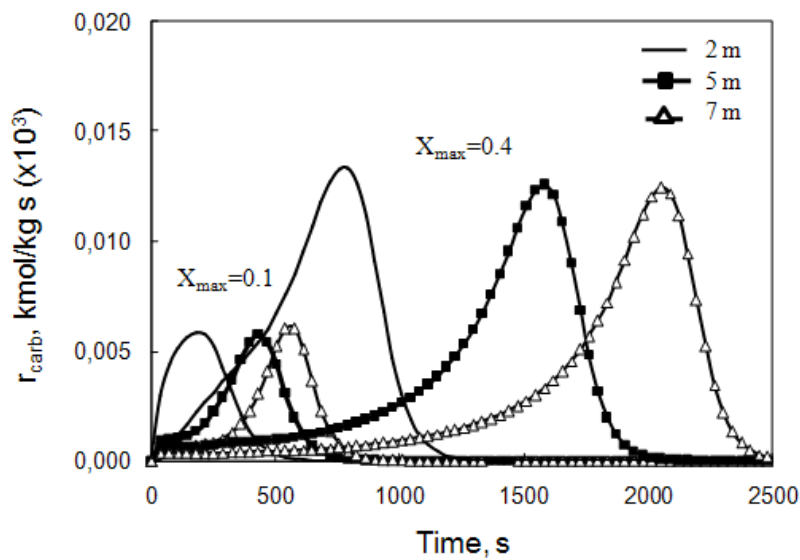


Fig. 8. Effect of carbonation kinetics on the product gas composition on a dry basis and on the temperature profile with the reaction time on stream (at the conditions shown in Table 3: 923 K, 3.5 MPa, S/C molar ratio of 5).

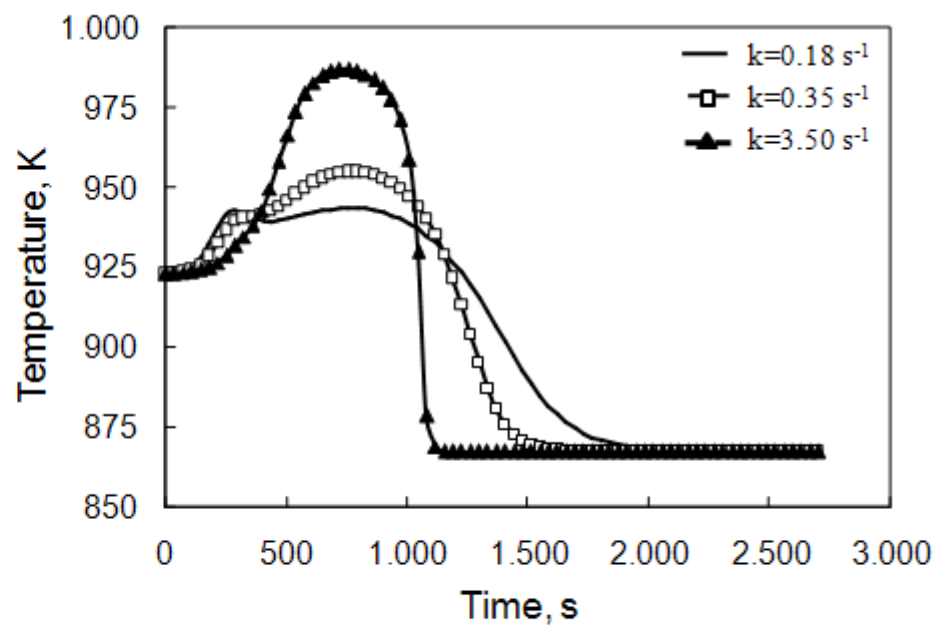
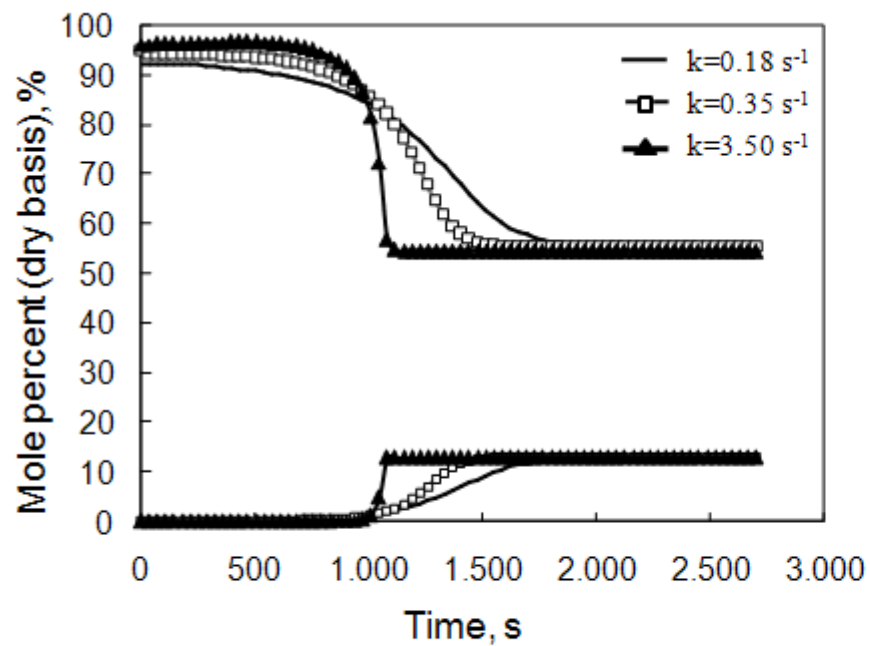


Fig. 9. Effect of carbonation rate constant on carbonation rate at different locations along the reformer (at the conditions shown in Table 3: 923 K, 3.5 MPa, S/C molar ratio of 5).

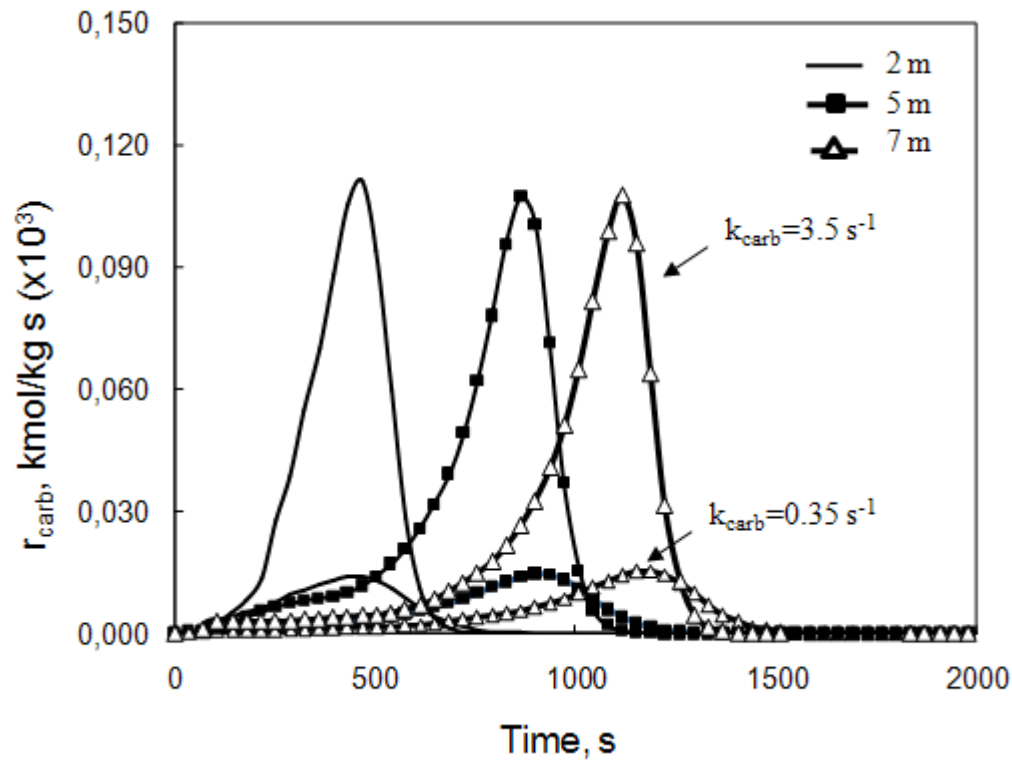


Fig. 10. Effect of carbonation rate constant on SER operational space velocities (923 K, 3.5 MPa, S/C molar ratio of 5).

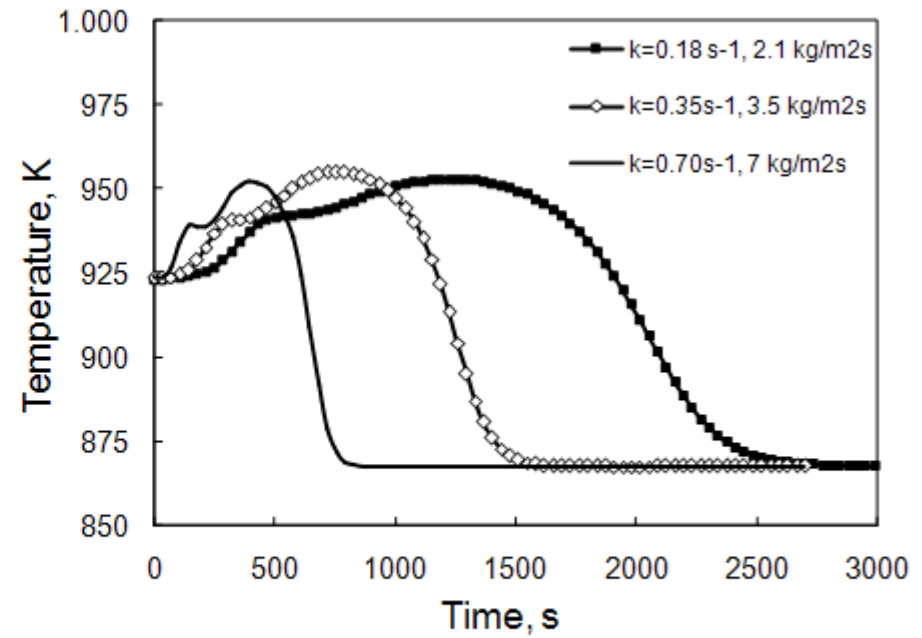
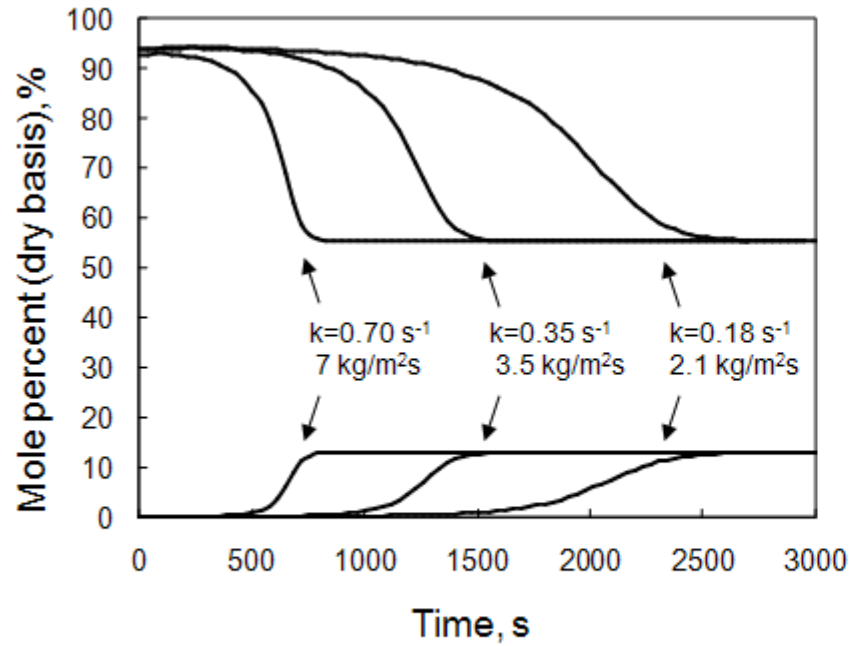


Table 1. Kinetic and equilibrium parameters in steam methane reforming (Xu and Froment, 1989; Twigg, 1989).

$$K_1 = \frac{1}{\exp(0.2513 Z^4 - 0.3665 Z^3 - 0.58101 Z^2 + 27.1337 Z - 3.2770)} \text{ atm}^2 \text{ }^a$$

$$K_3 = \exp(-0.29353 Z^3 + 0.63508 Z^2 + 4.1778 Z + 0.31688) \text{ }^a$$

$$Z = \frac{1000}{T} - 1$$

$$K_2 = K_1 K_3$$

$$k_1 = 1.842 \cdot 10^{-4} \exp\left[\frac{240100}{R} \left(\frac{1}{T} - \frac{1}{648}\right)\right] \text{ kmol bar}^{0.5} \text{ kg}^{-1} \text{ catalyst h}^{-1}$$

$$k_2 = 2.193 \cdot 10^{-5} \exp\left[\frac{243900}{R} \left(\frac{1}{T} - \frac{1}{648}\right)\right] \text{ kmol bar}^{0.5} \text{ kg}^{-1} \text{ catalyst h}^{-1}$$

$$k_3 = 7.556 \exp\left[\frac{67130}{R} \left(\frac{1}{T} - \frac{1}{648}\right)\right] \text{ kmol kg}^{-1} \text{ catalyst h}^{-1} \text{ bar}^{-1}$$

$$K_{CH_4} = 0.179 \exp\left[\frac{38280}{R} \left(\frac{1}{T} - \frac{1}{823}\right)\right] \text{ bar}^{-1}$$

$$K_{H_2O} = 0.4152 \exp\left[\frac{88680}{R} \left(\frac{1}{T} - \frac{1}{823}\right)\right]$$

$$K_{H_2} = 0.0296 \exp\left[\frac{82900}{R} \left(\frac{1}{T} - \frac{1}{648}\right)\right] \text{ bar}^{-1}$$

$$K_{CO} = 40.91 \exp\left[\frac{70650}{R} \left(\frac{1}{T} - \frac{1}{648}\right)\right] \text{ bar}^{-1}$$

^aTaken from Twigg (1989). The data reported by Xu and Froment (1989) are as follows: $K_1 = 4.707 \cdot 10^{12} \exp(-224000/RT) \text{ bar}^2$, $K_3 = 1.142 \cdot 10^{-2} \exp(37300/RT)$ (obtained for $T=948 \text{ K}$).

Table 2. Physical parameters used in the reactor model.

Parameters	Values
M_{CaO}	56 kg/kmol
C_{pg}	8.45 kJ/kg K
C_{ps}	0.98 kJ/kg K
μ_g	$1.81 \cdot 10^{-5}$ kg/m s
k_g	$3 \cdot 10^{-5}$ kW/m K

Table 3. Reactor characteristics and operating conditions for the reference case study.

Parameters	Values
Feed gas temperature, T_{in}	923 K
Initial solids temperature, T_0	923 K
Pressure	3.5 MPa
S/C molar ratio	5
Inlet gas mass flow velocity	3.5 kg/m ² s
X_{max}	0.4
η	0.3
ρ_{cat}	550 kg/m ³
ρ_{CaO}	1125 kg/m ³
ρ_s	1675 kg/m ³
d_p	0.01 m
L	7 m
ε	0.5