

Kondo Physics in a Rare Earth Ion with Well Localized $4f$ Electrons

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Dilute Nd in simple cubic LaB_6 shows electrical resistance and specific heat features at low temperature consistent with a Kondo scale of $T_K \lesssim 0.3$ K. Nd has a well-localized $4f^3$ $J = 9/2$ Hund's rule configuration which is not anticipated to be Kondo coupled to the conduction electrons in LaB_6 . We conjecture that the unexpected Kondo effect arises via participation of $4f$ quadrupolar degrees of freedom of the Nd crystal-field, ground-state quartet.

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The Kondo effect underpins a broad range of correlated electron behavior, [1,2] including exotic superconductivity in $4f$ and $5f$ intermetallics, [3] but is unexpected in materials with well-localized f levels. Spin interactions of $4f$ -electrons with conduction states are normally either of the Heisenberg exchange or of the Coqblin-Schrieffer type. The former exchange is ferromagnetic and arises from the Coulomb interaction in conjunction with the antisymmetry of the wave function. It scales with the so-called de Gennes factor, $(g - 1)^2 J(J + 1)$ (where g is the gyromagnetic ratio and J is the total angular momentum of the state), and manifests itself in the Curie-Weiss magnetic susceptibility, spin disorder scattering in the electrical resistivity, and the depression of superconducting transition temperatures, for isostructural rare earths with well localized $4f$ levels. Ce and Yb do not follow this scaling in most cases (as of course divalent Eu does not as well), because their exchange is of the Coqblin-Schrieffer type, [4] coming from the hybridization of the $4f$ levels with conduction electrons, leading to an antiferromagnetic exchange, the general condition for the development of the Kondo effect at low temperature. The $4f$ levels of Nd^{3+} impurities in a metal are deep and only slightly hybridized [5]. The exchange interaction is expected to be of the ferromagnetic Heisenberg type and, for this reason, the Kondo-like features for Nd impurities in LaB_6 we report in this Letter are surprising. What is essentially an old and well understood phenomenon makes a new appearance in LaB_6 : Nd which is both unexpected and needing explanation.

The rare earth hexaborides crystallize in the CaB_6 simple cubic structure which can be pictured as a CsCl

arrangement of B_6 octahedra and rare earth atoms. The boron network requires two electrons to form a closed shell configuration, leaving one conduction electron per unit cell in the hexaborides formed by trivalent rare earths. This electronic description has been well confirmed by band structure calculations [6] as well as extensive de Haas-van Alphen measurements [7–9], and agrees exactly with Hall effect measurements [8,10]. NdB_6 is a $T_N = 8.6$ K type I antiferromagnet. The $4f^3$ $J = 9/2$ crystal field scheme for the full cubic site symmetry of the Nd ion has been determined by both inelastic neutron [11] and Raman scattering [12] experiments to be a ground state Γ_8^2 quartet, with the Γ_8^1 quartet and Γ_6 doublet lying at 135 and 278 K above the ground state, respectively. An analysis of the temperature dependent specific heat using this magnetic level scheme, in addition to the lattice specific heat of LaB_6 , led to the surprising conclusion that the electronic specific heat of NdB_6 above T_N equaled 90 mJ/mole Nd K^2 [13]. This has prompted the investigation of the single ion properties of Nd dissolved in the isoelectronic, isostructural host LaB_6 reported here. We find that Nd diluted in simple cubic LaB_6 exhibits electrical resistance, magnetic susceptibility, and specific heat features at low temperature, which are consistent with a Kondo scale of $T_K \lesssim 0.3$ K. We argue that quadrupolar interactions between the $4f$ and the conduction electrons, which give rise to the formation of the spin singlet, are most likely responsible for this behavior.

All measurements were performed on single crystals grown from Al flux using high purity elemental rare earth from the Ames Laboratory. Specific heat measurements

using the relaxation method were carried out down to approximately 0.3 K in a commercial setup for the $0 \leq \mu_0 H \leq 9$ T magnetic field range. Magnetic susceptibility measurements were performed in a commercial superconducting quantum interference device magnetometer for temperatures down to 2 K, and in a homemade Hall microprobe magnetometer installed in a ^3He setup for the lower temperature range. The four-probe resistivity was measured to low temperature in a ^3He cryostat or in a PPMS system. Contact leads (25 μm gold wire) were soldered to the samples using pure indium. In our experiments, we used a dc (less than 1 mA) or low-frequency ac current. We etched the crystals in concentrated HCl to clean the surfaces before performing our measurements.

We measured electrical resistivity, magnetization and heat capacity on $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ single crystals for $0 \leq x \leq 0.06$. In order to avoid any uncertainty in the Nd content, the very same samples were used in all experiments. The Nd compositions in the LaB_6 crystals were in general quite different from the nominal charge compositions. Therefore the Nd concentration was determined from low-temperature susceptibility and magnetization measurements, such as shown in Figs. 1(a)–1(c), using the crystal field scheme determined by neutron and Raman scattering in NdB_6 . Since the effective moments for the Γ_8^2 and Γ_6 are quite close, nearly the same Nd composition would be determined from the susceptibility measurement assuming either ground state. The specific heat measurements confirmed unequivocally that the ground state of Nd ions in

LaB_6 is the Γ_8^2 quartet as in pure NdB_6 . Figure 1(c) shows that the initial susceptibility χ_{init} of our samples has no term proportional to x^2 . Neither we find such term in the saturation magnetization which varies linearly with the Nd composition. We conclude therefore that the concentration of magnetic pairs or clusters, which usually give rise to the x^2 variation of magnetization, is negligible in our samples, [14] in agreement with electron microprobe results. On the other hand, the induced magnetization in the paramagnetic state is $M = \chi_1 H + \chi_3 H^3 + \dots$, where the nonlinear susceptibility χ_3 probes quadrupolar fluctuations as shown for several rare-earth compounds [15,16]. The measured χ_3 for $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ single crystals is shown in Fig. 1(d). Its behavior points unequivocally to the importance of the quadrupolar interactions as discussed below.

A Kondo rise in the low-temperature resistivity ρ of dilute $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ can be seen in Fig. 2. The comparison with the LaB_6 resistivity data, also shown in Fig. 2, rules out that the minimum in ρ at approximately 10 K arises from impurities in the source material. Beyond this temperature, the resistivity of diluted alloys varies with T as that of the pure LaB_6 sample. This indicates that the structural disorder is alike in all samples, and gives rise roughly to the same residual resistivity. The magnitude of the low-temperature rise in resistivity $\Delta\rho$, plotted in the inset of Fig. 2, is 3 $\mu\Omega\text{ cm}$ per mole Nd. For the well studied case of $\text{La}_{1-x}\text{Ce}_x\text{B}_6$ the value per Ce is 50 times larger, [17] where $T_K = 0.86$ K [18]. The excess resistivity goes nearly as $A - BT^{1/2}$ which points to non-Fermi

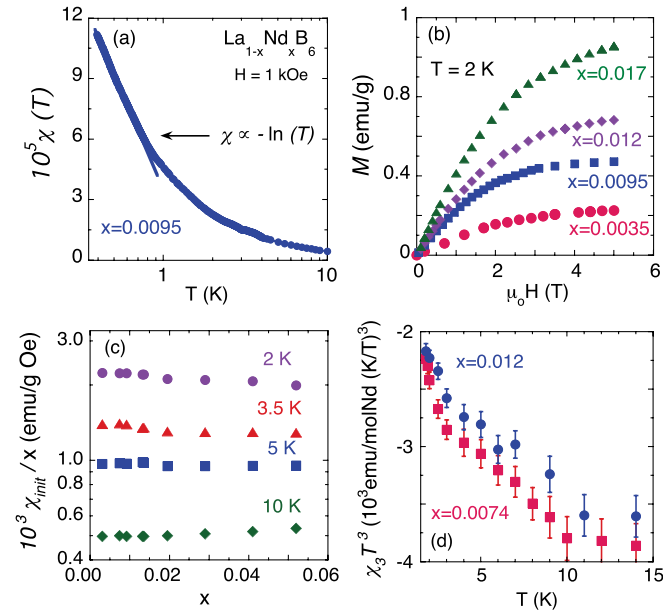


FIG. 1 (color online). (a) Low-temperature magnetic susceptibility for $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ ($x = 0.0095$) single crystal. A $\chi \propto -\ln(T)$ variation is shown for $T \lesssim 1$ K. (b) $M(H)$ at $T = 2$ K for various $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ single crystals. (c) χ_{init}/x versus x at various temperatures. (d) The measured nonlinear susceptibility χ_3 times T^3 at low temperatures.

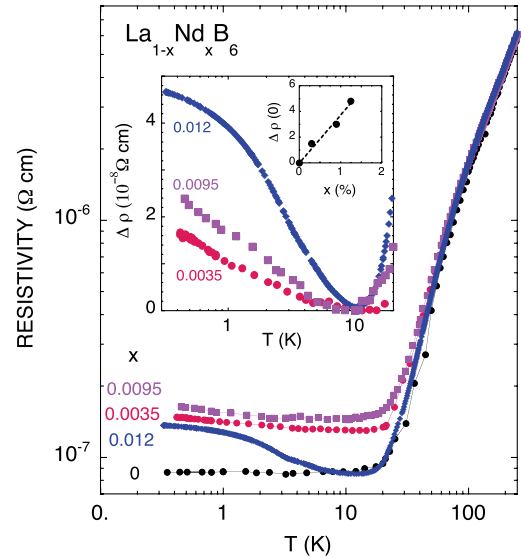


FIG. 2 (color online). Electrical resistivity for $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ single crystals. The main panel shows the temperature dependence of the electrical resistivity for $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ single crystals in zero magnetic field. The Kondo contribution to the resistivity in the low-temperature region is shown in the inset. How this contribution varies with Nd content x is plotted in the inset of the inset.

liquid-like behavior. We observe the rise in the resistivity for a very small Nd-doping only ($x \lesssim 0.03$) as shown in the inset of Fig. 2. With increasing x , one might expect sufficient strain in $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ to lift the degeneracy of the ground-state quartet. If the fourfold degeneracy is central to the presence of the Kondo features found in these alloys, then the effect should strongly weaken with Nd concentration.

In panels (a) and (b) of Fig. 3 we show the T -dependence of the specific heat (C) of dilute $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ for the $x = 0.0095$ and 0.0295 , respectively, in addition to isomorphous nonmagnetic LaB_6 . The strong dependence of C on H at the lowest T is brought about by the Nd ions. This magnetic contribution (C_m) superposes on the lattice contribution at higher temperatures, which is given by the data for LaB_6 compound. Furthermore, the electronic specific heat seen in LaB_6 (linear term $C_{\text{el}} \propto T$ in Fig. 3) should be expected to contribute likewise to $\text{La}_{1-x}\text{Nd}_x\text{B}_6$. Therefore, $C_m(T, H)$ is easily obtained by subtracting C of LaB_6 from the total C of $\text{La}_{1-x}\text{Nd}_x\text{B}_6$. Thus, by taking the integral $\int_0^\infty (C_m/T) dT$, the magnetic entropies (S_m) are calculated and depicted in panels (c) and (d) of Fig. 3 for $x = 0.0095$ and 0.0295 , respectively. For $\mu_0 H > 1$ T, $C_m(T, H)$ is well within our experimentally accessible temperature window. Indeed, extrapolating linearly C_m/T as $T \rightarrow 0$ K yields an S_m content for $T \lesssim 0.3$ K that is less than 2% of the total S_m content. For $H = 0$, the lack of experimental C_m for $T \lesssim 0.3$ K has been taken into account by matching the limiting S_m at high T with the value obtained from the in-field data. After scaling S_m to the proper Nd concentration, one can see that there is an entropy of $R \ln(4)$ per mole Nd involved

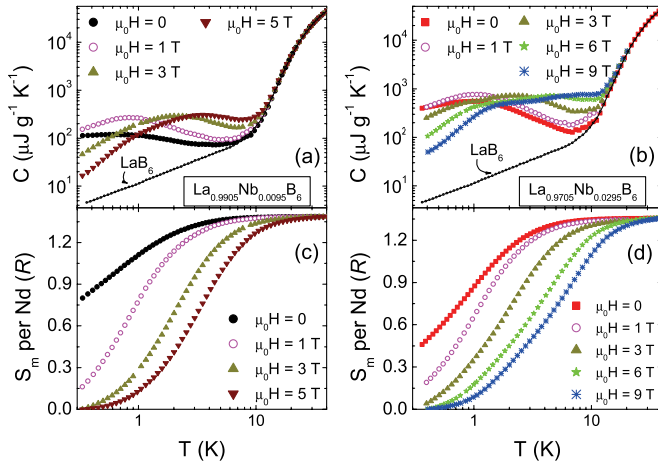


FIG. 3 (color online). Specific heat for $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ single crystals. Top panels (a) and (b) show the temperature dependencies of the experimental specific heat C for $\text{La}_{0.9905}\text{Nd}_{0.0095}\text{B}_6$ and $\text{La}_{0.9705}\text{Nd}_{0.0295}\text{B}_6$ single crystals, respectively, along with C of the isomorphous LaB_6 , at various magnetic fields, as labeled. Bottom panels (c) and (d) show how the excess (magnetic) entropy S_m per Nd ion, normalized to the gas constant R , varies with temperature for the same single crystals as in (a) and (b), respectively.

in the excess specific heat of $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ above that of LaB_6 , indicating that (i) the $4f^3$ ground state is compensated by the conduction electrons and some other effects as $T \rightarrow 0$ K and (ii) the ground state is a quartet, as is Ce in $\text{La}_{1-x}\text{Ce}_x\text{B}_6$ [19]. Assuming that about half of the zero-field entropy of a Kondo system is reached at the characteristic temperature T_K , the development of S_m in panels (c) and (d) would suggest that T_K is of order of $\lesssim 0.3$ K for the samples studied.

The zero-field magnetic contributions of Nd ions to the specific heat (C_m) are shown in the top panel of Fig. 4. The dominant Schottky-type feature is seen to broaden and shift downward as x decreases from 0.0295 to 0.0095 . By applying a magnetic field, these specific heat contributions gain height and get narrower, being no longer dependent on the Nd concentration for any field higher than 1–2 T (Fig. 3). For $\mu_0 H \geq 6$ T, we clearly distinguish two separate anomalies in C_m (bottom panel of Fig. 4), which we associate with the two doublets into which the Γ_8^2 quartet splits in a magnetic field. They have different g factors, depending on the angle of the field with the crystallographic axis. The exact value of the g factors for Nd also depends on the crystalline field splitting of the ion. For Nd,

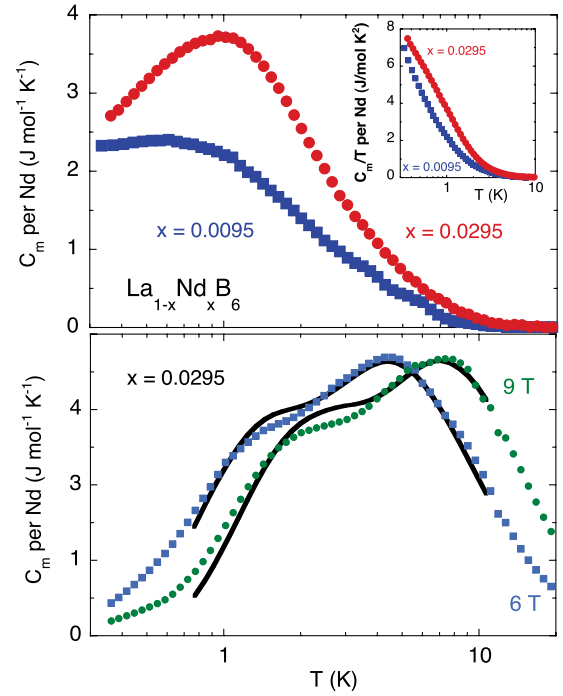


FIG. 4 (color online). Magnetic specific heat for $\text{La}_{1-x}\text{Nd}_x\text{B}_6$ single crystals. Top: Temperature dependencies of the experimental zero-field magnetic specific heat (C_m) per Nd ion for $\text{La}_{0.9905}\text{Nd}_{0.0095}\text{B}_6$ and $\text{La}_{0.9705}\text{Nd}_{0.0295}\text{B}_6$ single crystals, respectively. The same data, plotted as C_m/T vs. $\log(T)$, are in the inset. Bottom: Magnetic specific heat for $\text{La}_{0.9705}\text{Nd}_{0.0295}\text{B}_6$ single crystal between 0.3 and 20 K at various magnetic fields, as labeled. Solid lines are fits to the Schottky anomalies for the corresponding fields.

and for the field along (100) direction, the ratio of the g factors is $2.94/1.92 \approx 1.7$, using the Lea-Leask-Wolf table for $J = 9/2$ and $x = -0.90$ [20]. This is very close to what we obtain from a fitting of the Schottky four-level specific heat to the experimental $\text{LaB}_6:\text{Nd}$ data at $\mu_0 H = 6$ and 9 T (solid lines in Fig. 4).

The observed behavior agrees with the following picture. Neglecting the possibility of a hybridization between the localized and conduction states, leaves us only with the ferromagnetic Coulomb exchange. We ascribe the Kondo-like phenomena to the coupling of the conduction electrons with the quadrupolar momentum of the Nd sites. Because the magnetic degrees of freedom strongly couple with the quadrupolar ones, the degeneracy is lifted at $T = 0$. A sufficiently high magnetic field and increasing x break the Kondo-like coupling.

The distance between Nd ions is not very large for the x values considered and is a random variable. Hence, in zero-applied field, the Nd ions are not totally independent but see each other. It is therefore expected that the interaction between Nd ions leads to an internal field that locally splits the Γ_8^2 ground-state, according to a distribution whose width decreases with the increase of the Nd concentration. This interferes with the Kondo-like screening and leads to a distribution of ‘‘Kondo temperatures’’: T_K differs at every site or locally in a region covering several unit cells. Both effects reduce the height of C_m and make the ‘‘Kondo resonance’’ broader. Assuming that (i) for $T < T_K$ the specific heat of an individual ion is proportional to T/T_K , and (ii) the distribution of T_K is reasonably flat, then $C_m/T \propto \ln(T_0/T)$, where T_0 is an average of T_K (see inset of Fig. 4) [21]. Similarly, the low-temperature zero-field susceptibility is proportional to $\ln(T_0/T)$ [see Fig. 1(a)]. A distribution of Kondo temperatures can also explain such behavior. The susceptibility for an individual ion for $T < T_K$ is proportional to $1/T_K$. A flat distribution of T_K then again leads to $\chi \propto -\ln(T)$ [21]. This agrees with our data. The excess resistivity $\Delta\rho \propto T^{1/2}$ over nearly a decade of temperature is also indicative of non-Fermi-liquid behavior.

We should stress that the estimated value of T_K ($\lesssim 0.3$ K) marks no more than a characteristic temperature scale (from competition between the ferromagnetic exchange and scattering on the quadrupolar momentum of Nd ions) and does not define the magnetic field scale same way as it does in the s - d model. For $\text{LaB}_6:\text{Nd}$, the magnetic-field scale is given by the field that splits the Γ_8^2 quartet into two doublets. In Fig. 4, the double-feature in the specific heat shows at $\mu_0 H = 6$ T, which corresponds to $T \approx 4$ K.

The low- T magnetic susceptibility data follow a Curie-Weiss law down to 2 K with an antiferromagnetic intercept of ≈ -0.3 K. The nonlinear susceptibility sheds additional light on the origin of the unexpected Kondo feature seen in the Nd alloys. For noninteracting ions and within a quartet consisting of two doublets with Zeeman splitting, given by g_1 and g_2 , respectively, the linear and nonlinear susceptibilities

are $\chi_1 = ((g_1^2 + g_2^2)/8T)(\mu_B^2/k_B)$ and $\chi_3 = -((g_1^4 + g_2^4 + 6g_1^2g_2^2)/(192 \times T^3))(\mu_B^4/k_B^3)$, respectively. The free-ion χ_3 is always negative reflecting the negative curvature of the Brillouin function. A plot of $\chi_3 T^3$ vs T then gives a constant and deviations from this constant are consequently brought about by the Kondo-like screening. An inspection of Fig. 1(d) shows that the measured $\chi_3 T^3$ for $\text{LaB}_6:\text{Nd}$ is both negative and, for $T \lesssim 10$ K, monotonically increasing with decreasing temperature. The observed magnitude and temperature dependence of χ_3 is similar for the other two samples studied. These results strongly favor the quadrupolar model in $\text{LaB}_6:\text{Nd}$.

Quadrupolar effects are strongly evident in the electronic properties of a number of rare earth intermetallics, most notably in the Pr skutterudites where they appear to give rise to heavy Fermion behavior [22,23]. However, one does not find single-ion Kondo behavior in the properties of dilute Pr dissolved in the La skutterudite analogs [24]. No heavy Fermion behavior has been seen in the stoichiometric Nd skutterudites. Raman experiments as well as detailed theoretical studies do indicate that one expects strong quadrupolar influence in the properties of NdB_6 [12,25,26]. Note that for $\text{La}_{1-x}\text{Ce}_x\text{B}_6$ strong Kondo features exist for all Ce concentrations and for large x anti-ferroquadrupolar order has been found [27].

It is established that quadrupolar degrees of freedom play a fundamental role for Ce and Nd ions with Γ_8 ground-state; they manifest themselves in first place through interactions among the ions. Impurities strain the lattice and the local lattice distortions couple to the quadrupolar, but not the spin, degrees of freedom of the $4f$ electrons. The quadrupolar intersite interactions are probably the main reason for why it is hard to observe the single ion limit in both, $\text{LaB}_6:\text{Nd}$ and $\text{LaB}_6:\text{Ce}$. The induced quadrupolar distortion could also lead to an interaction between the Γ_8 states and the conduction electrons. There is no consensus about the origin of the interactions. Kubo and Kuramoto [25] successfully described the excitation spectrum of NdB_6 using nearest-neighbor intersite exchange and quadrupolar interactions. A different approach emphasizing crystalline fields was proposed by Uimin and Brenig [28]. For CeB_6 , on the other hand, quadrupolar interactions between sites, [29] the RKKY interaction arising from the Coqblin-Schrieffer model, [30,31] and a detailed group theoretical study [32] have been presented. The well-localized nature of the $4f$ electrons in Nd compared to the considerable hybridization in Ce, suggests that the interaction mechanisms with the conduction states could be different for these two ions in the LaB_6 matrix.

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