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# Measurement of $t\bar{t}$ spin correlation in $p\bar{p}$ collisions using the CDF II detector at the Tevatron

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The  $t\bar{t}$  spin correlation at production is a fundamental prediction of QCD and a potentially incisive test of new physics coupled to top quarks. We measure the  $t\bar{t}$  spin state in  $p\bar{p}$  collisions at  $\sqrt{s} = 1.96$  TeV using 1001 candidate events in the lepton plus jets decay channel reconstructed in the CDF II detector. In the helicity basis, for a top-quark mass of 172.5 GeV/ $c^2$ , we find a spin correlation coefficient  $\kappa = 0.60 \pm 0.50$  (stat)  $\pm 0.16$  (syst), consistent with the QCD prediction,  $\kappa \approx 0.40$ .

DOI: 10.1103/PhysRevD.83.031104

PACS numbers: 12.38.Qk, 13.85.-t, 14.65.Ha

In quark-pair production by the strong interaction, the quark spins are entangled according to the short distance dynamics of quantum chromodynamics (QCD) [1]. The spin state is observable in angular correlations among the quark decay products induced by the V - A (vector minus axial-vector) nature of the weak interaction but is typically destroyed by the depolarizing effects of hadronization before the decay can proceed. The top quark is an exception to this rule. Because of its large mass, the top-quark lifetime is shorter than the fragmentation timescale, cutting off the long distance QCD effects and transmitting the  $t\bar{t}$  production configuration to the final state. Measurement of the  $t\bar{t}$ spin configuration is a first look at a bare-quark pair at production. The measurement tests the fundamental predictions of QCD [1-5] and could be a sensitive discriminant of new physics coupled to top quarks [6,7]. For example, a  $t\bar{t}$ resonance appearing as an excess in the  $t\bar{t}$  invariant-mass spectrum can be verified as a Kaluza-Klein graviton through measurement of the spin correlation as described in Ref. [7].

Because final state charged leptons have the strongest correlation to the top-quark spin, the  $t\bar{t}$  spin correlation is usually discussed in terms of the dilepton final state  $t\bar{t} \rightarrow (W^+b)(W^-\bar{b}) \rightarrow (\bar{\ell}\nu)(\ell'\bar{\nu}')b\bar{b}$  [4]. This mode suffers from a small branching ratio and poor definition of the top-quark kinematics due to the presence of two undetectable neutrinos. A previous measurement of the  $t\bar{t}$  spin correlation was limited to a small sample of just six events in this mode [8].

We report on a new measurement of the  $t\bar{t}$  spin correlation in  $p\bar{p}$  collisions at 1.96 TeV with a data sample corresponding to an integrated luminosity of 4.3 fb<sup>-1</sup> collected with the CDF II detector at the Fermilab Tevatron. We measure the spin correlation of pairproduced quarks for the first time in the lepton plus jets decay topology,  $t\bar{t} \rightarrow (W^+b)(W^-\bar{b}) \rightarrow (u\bar{d}b)(\ell \bar{\nu} \bar{b})$  or  $t\bar{t} \to (W^+b)(W^-\bar{b}) \to (\bar{\ell}\nu b)(\bar{u}d\bar{b})$  [9]. In this decay mode, we take advantage of a large branching ratio compared to the dilepton channel and the well-constrained  $t\bar{t}$ kinematics in the lepton plus jets final state with only one neutrino. The measurement relies critically on a new technique for identifying the final state down-type quark (d or s), which has the same spin-analyzing power as a charged lepton. We expect the spin correlation measurement to show the dominance of  $t\bar{t}$  production via the J = 1

 $q\bar{q}$  annihilation channel that occurs in ~85% of  $p\bar{p}$  collisions at the Tevatron [10].

We work in the helicity basis, where the spinquantization axis is defined as the direction of motion of the t (or  $\overline{t}$ ) quark in the  $t\overline{t}$  rest frame. There are other quantization axes which predict a larger value for the spin correlation [3], but they do not provide any significant increase in the statistical sensitivity of our approach, so we work with the simpler helicity basis. A quark is called right-handed $(t_R)$ /left-handed $(t_L)$  if its spin is oriented along/opposite to its direction of motion. In the  $t\bar{t}$  rest frame the quarks move back-to-back; thus the same-spin states with J = 1 are those with opposite helicity:  $\bar{t}_L t_R$ and  $\bar{t}_R t_L$ . Near the energy threshold for  $t\bar{t}$  production, the opposite-helicity fraction is predicted in the standard model (SM) to be ~67% for  $t\bar{t}$  production via  $q\bar{q}$  annihilation, while for top quarks with large momenta compared to the top-quark mass, helicity is approximately conserved and this fraction rises to  $\sim 100\%$  [1,3]. Integrating over all top-quark momenta according to the parton distribution functions and adding the small (  $\sim 15\%$ ) J = 0 contribution from gluon-gluon fusion processes, we expect to find an opposite-helicity fraction [1,3]

$$F_{\rm OH} = \frac{\sigma(\bar{t}_R t_L) + \sigma(\bar{t}_L t_R)}{\sigma(\bar{t}_R t_R) + \sigma(\bar{t}_L t_L) + \sigma(\bar{t}_R t_L) + \sigma(\bar{t}_L t_R)} \approx 0.70.$$
(1)

 $F_{\rm OH}$  is simply related to the spin correlation coefficient  $\kappa$  that measures the fractional difference between the number of events in which the top-quark spins are aligned and the number of events in which they have opposite directions:  $\kappa = 2F_{\rm OH} - 1$ . We thus expect  $\kappa \approx 0.40$  [1,3], while for uncorrelated spins,  $\kappa = 0.0$  and  $F_{\rm OH} = 0.5$ .

In top-quark decays in the SM the V - A couplings fix the angular distributions of the decay products according to the polarization of the parent top quark via

$$\frac{1}{\Gamma}\frac{d\Gamma}{d\cos\theta_i} = \frac{1}{2}(1 \pm A_i\cos\theta_i),\tag{2}$$

where the positive/negative sign is used for right-handed/ left-handed quarks, and the helicity angle  $\theta_i$  is defined as the angle between the spin-quantization direction and the momentum of the decay particle in the rest frame of its parent top quark. In the V – A weak decay, the spinanalyzing-power coefficient  $A_i$  is equal to +1.0 for the charged lepton or down-type quark, -0.41 for the bottom quark, and -0.31 for the neutrino or up-type quark, with the signs reversed for antitop-quark decays [3]. The  $t\bar{t}$  spin correlation connects the daughter helicity angles on each side of the decay. The differential cross-section in these variables is

$$\frac{1}{\sigma} \frac{d^2 \sigma}{d(\cos\theta_i) d(\cos\theta_j)} = \frac{1 + \kappa A_i A_j \cos\theta_i \cos\theta_j}{4}, \quad (3)$$

where i and j refer to top-quark and antitop-quark decay products, respectively [3].

For each of the four possible  $t\bar{t}$  helicity states, we create model templates for the distributions of  $\cos\theta_l \cos\theta_d$  and  $\cos\theta_l \cos\theta_b$ , where the charged lepton l is a decay product from one top quark in the pair and the quarks d and b are decay products from the other quark. We then find the relative normalization of these model templates that gives the best fit to a two-dimensional distribution of these variables in the data. The model templates account for all acceptance effects and dilutions due to event reconstruction, so that the parton-level value of  $F_{\text{OH}}$  follows directly from the template fit to the data.

CDF II [11] is a general purpose, azimuthally and forward-backward symmetric detector. Charged-particle directions and momenta are measured with a silicon tracker [12] and a drift chamber [13] in a 1.4 T solenoidal magnetic field. Electromagnetic and hadronic calorimeters [14] are located beyond the solenoid and allow for jet and missing  $E_T$  reconstruction. Beyond the calorimeter, muon chambers [15] provide coverage for the pseudorapidity range  $|\eta| \leq 1.0$ . We use a cylindrical coordinate system with its origin at the center of the detector and the z axis along the proton direction [16].

Lepton plus jets events are selected by requiring one electron or muon with transverse momentum of at least 20 GeV/c and  $|\eta| < 1.0$ , missing transverse energy of at least 20 GeV, and four or more jets with transverse energy of at least 20 GeV and  $|\eta| < 2.0$ , at least one of which must be tagged as a b jet by the presence of a displaced secondary vertex [17]. This selection yields 1001 total candidate events, 224 of which have two tagged b jets.

Non- $t\bar{t}$  backgrounds are well-constrained by precision  $t\bar{t}$  cross-section measurements [18], with a predicted total of 215 ± 48 background events. Non- $t\bar{t}$  models are checked against background-enriched sidebands with no tagged *b* jets and are found to give very good representations of the normalizations and kinematics in all variables, including lepton and jet energies and angular distributions.

The helicity angles are determined in a complete reconstruction of the  $t\bar{t}$  kinematics in  $t\bar{t} \rightarrow (Wb)(Wb) \rightarrow (\ell \nu b)(udb)$ , where we constrain  $M(\ell \nu) = M(ud) = 80.4 \text{ GeV}/c^2$ , the mass of the W boson, and  $M(\ell \nu b) = M(udb) = 172.5 \text{ GeV}/c^2$ , the top-quark

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mass, and require any tagged *b* jets to be identified with *b* partons. The constraints were chosen to be close to the world averages in Ref. [19]. Each of the 24 possible jet-toparton assignments is evaluated using a  $\chi^2$  comparison to the  $t\bar{t}$  hypothesis with the above constraints, and we choose the assignment with the lowest  $\chi^2$  value [20]. This procedure correctly assigns all jets to the corresponding partons in approximately 37% of events. All effects of angular acceptance and jet reconstruction and misassignment are fully modeled by our simulated samples.

Down-type-quark identification relies on the V – A decay correlation that tends to send the down-type quark in the direction opposite that of the hadronically decaying W boson in the top-quark rest frame. We therefore assign the down-type quark as the jet that, in the W boson rest frame, is closest to the bottom jet identified as coming from the same top quark as the W boson [3]. Simulation studies show that this algorithm correctly identifies the down-type quark 60% of the time.

The same-helicity and opposite-helicity model templates are created with a customized version of the HERWIG event generation software package [21] that implements the angular distribution of Eq. (2) for the charged lepton or down-type quark, with a tunable choice of rightor left-handed top quarks, and preserves all the other expected spin correlations [22]. We create four different simulated samples, corresponding to the four possible top-quark-pair helicity states:  $\bar{t}_L t_R$ ,  $\bar{t}_R t_L$ ,  $\bar{t}_L t_L$ , and  $\bar{t}_R t_R$ . QCD interactions respect both the parity symmetry (P) and the combined symmetry of parity and charge conjugation (*CP*). Because *CP* transforms  $\bar{t}_R t_R \rightarrow t_L \bar{t}_L$ , we can define the same-helicity (SH) model template shape to be the symmetric sum of  $\sigma(\bar{t}_R t_R) + \sigma(t_L \bar{t}_L)$ . Since P transforms  $\bar{t}_R t_L \rightarrow \bar{t}_L t_R$ , we let the opposite-helicity (OH) model template shape be the symmetric sum of  $\sigma(\bar{t}_R t_L) + \sigma(\bar{t}_L t_R)$ .

Figure 1 compares the SH and OH model templates after detector simulation, event selection, and reconstruction in the two distributions that we use for the measurement,  $\cos\theta_l \cos\theta_d$  and  $\cos\theta_l \cos\theta_b$ . Our sensitivity results from the SH model template being shifted towards negative values of  $\cos\theta_l \cos\theta_d$ , while the OH model template is shifted towards positive values, with the opposite shifts occurring in the  $\cos\theta_l \cos\theta_b$  distribution.

We perform our measurement using a binned likelihood fit to find the relative normalization of these model templates that gives the best simultaneous representation of  $\cos\theta_l \cos\theta_d$  and  $\cos\theta_l \cos\theta_b$  in our data. The background normalization is constrained to be close to the predicted value, with a Gaussian uncertainty, but the same-helicity fraction  $F_{\rm SH}$  and opposite-helicity fraction  $F_{\rm OH}$  are allowed to float freely. We do not require that  $F_{\rm SH}$  and  $F_{\rm OH}$  be constrained to physical values between 0 and 1, but we do require  $F_{\rm SH} + F_{\rm OH} = 1$ . The fit runs over all bins in a two-dimensional distribution of  $\cos\theta_l \cos\theta_d$  vs  $\cos\theta_l \cos\theta_b$ . The expected statistical uncertainty for  $F_{\rm OH}$  is



FIG. 1 (color online). Distributions of the  $\cos\theta_l \cos\theta_d$  and  $\cos\theta_l \cos\theta_b$  variables, after detector simulation, event selection, and reconstruction, in our same-helicity and opposite-helicity simulated  $t\bar{t}$  samples.

approximately 0.23, corresponding to an uncertainty for  $\kappa$  of 0.46, and is independent of the actual value of  $F_{\rm OH}$  and  $\kappa$ .

Additional contributions to the uncertainty result from incomplete knowledge of the background size and shape, of the exact detector response, and of the parton distribution functions (PDF) and are estimated by performing the measurement in simulated samples with reasonable variations in the model assumptions. These systematic

TABLE I. Systematic Uncertainties on  $F_{OH}$ .

Systematic	Uncertainty
Generator dependence	0.060
JES	0.042
ISR/FSR	0.030
Background shape	0.023
Color reconnection	0.009
PDF	0.007
Parton shower	0.006
Background size	0.002
Total uncertainty	0.083



FIG. 2 (color online). Distribution of the  $\cos\theta_l \cos\theta_d$  and  $\cos\theta_l \cos\theta_b$  variables in data compared to the sum of our background model, the same-helicity model template, and the opposite-helicity model template. The relative normalizations of the model distributions are determined by our fit result.

uncertainties are shown in Table I. The largest uncertainty, generator dependence, results from small biases seen when testing with simulated samples created using a range of generation software packages, including HERWIG [21], PYTHIA [23], ALPGEN [24], and MADEVENT [25]. Other significant contributions come from the uncertainty of the jet energy scale (JES) during event reconstruction and uncertainty in the amount of initial and final state radiation (ISR/FSR) in our observed  $t\bar{t}$  events. The small variation of  $F_{\rm OH}$  with the assumed value of the top-quark mass is not included in our systematic uncertainty; our measurement assumes a mass of 172.5 GeV/ $c^2$  for the top quark.

The final result of our fit to the two-dimensional distribution  $\cos\theta_l \cos\theta_d$  vs  $\cos\theta_l \cos\theta_b$  is shown in Fig. 2. This figure shows one-dimensional distributions of both variables, with our data being compared to the sum of the background model, same-helicity model, and opposite-helicity model, with the model normalizations determined by our fit result. Assuming the top-quark mass is 172.5 GeV/ $c^2$ , we find an opposite-helicity fraction of MEASUREMENT OF  $t\bar{t}$  spin correlation in  $p\bar{p}$ ...

$$F_{\rm OH} = 0.80 \pm 0.25 \text{ (stat)} \pm 0.08 \text{ (syst)}.$$

Converting this to the spin correlation coefficient, using  $\kappa = 2F_{\text{OH}} - 1$ , yields

$$\kappa = 0.60 \pm 0.50 \text{ (stat)} \pm 0.16 \text{ (syst)}.$$

This first measurement of the top-quark-pair spin correlation in the lepton plus jets decay channel agrees well with the theoretical prediction of  $\kappa \approx 0.40$  [1,3], although the statistical uncertainty is still large. Simulated experiments with larger data sets indicate that if the Tevatron data set reaches 15 fb<sup>-1</sup> before the end of the Tevatron lifetime, the expected statistical uncertainty on  $\kappa$  would be reduced to 0.26. This technique can thus be applied in future measurements with larger data sets collected at the Tevatron and LHC to constrain the  $t\bar{t}$  production spin structure or to connect with other anomalies that may show up in the reconstructable  $t\bar{t}$  kinematics of the lepton plus jet sample.

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We thank the Fermilab staff and the technical staffs of the participating institutions for their vital contributions. This work was supported by the U.S. Department of Energy and National Science Foundation; the Italian Istituto Nazionale di Fisica Nucleare; the Ministry of Education, Culture, Sports, Science and Technology of Japan; the Natural Sciences and Engineering Research Council of Canada; the National Science Council of the Republic of China; the Swiss National Science Foundation: the A. P. Sloan Foundation: the Bundesministerium für Bildung und Forschung, Germany; the World Class University Program, the National Research Foundation of Korea; the Science and Technology Facilities Council and the Royal Society, UK; the Institut National de Physique Nucleaire et Physique des Particules/CNRS: the Russian Foundation for Basic Research; the Ministerio de Ciencia e Innovación, and Programa Consolider-Ingenio 2010, Spain; the Slovak R & D Agency; and the Academy of Finland.

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