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Search for $b \to u$ transitions in $B^0 \to D^0 K^{*0}$ decays

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We present a study of the decays $B^0 \to D^0 K^{*0}$ and $B^0 \to \overline{D}^0 K^{*0}$ with $K^{*0} \to K^+\pi^-$. The D^0 and the $\overline{D}^0$ mesons are reconstructed in the final states $f = K^+\pi^-$, $K^+\pi^-\pi^0$, $K^+\pi^-\pi^+\pi^-$ and their charge conjugates. Using a sample of 465 million $B\overline{B}$ pairs collected with the BABAR detector at the PEP-II asymmetric-energy e^+e^- collider at SLAC, we measure the ratio $R_{ADS} \equiv [\Gamma(\overline{B}^0 \to [f]_D\overline{K}^{*0}) + \Gamma(B^0 \to [\bar{f}]_D K^{*0})]/[\Gamma(\overline{B}^0 \to [\bar{f}]_D\overline{K}^{*0}) + \Gamma(B^0 \to [f]_D K^{*0})]$ for the three final states. We do not find significant evidence for a signal and set the following limits at 95% probability: $R_{ADS}(K\pi) < 0.244$, $R_{ADS}(K\pi\pi^0) < 0.181$ and $R_{ADS}(K\pi\pi\pi) < 0.391$. From the combination of these three results, we find that the ratio r_S between the $b \to u$ and the $b \to c$ amplitudes lies in the range $[0.07, 0.41]$ at 95% probability.

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Various methods have been proposed to determine the Unitarity Triangle angle γ [1, 2, 3] of the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix [4] using $B^- \to \tilde{D}^{(*)0}K^{(*)-}$ decays, where the symbol $\tilde{D}^{(*)0}$ indicates either a $D^{(*)0}$ or a $\overline{D}^{(*)0}$ meson. A B^- meson can decay into a $\tilde{D}^{(*)0}K^{(*)-}$ final state via a $b \to c$ or a $b \to u$ process. CP violation may occur due to interference between the amplitudes when the $D^{(*)0}$ and $\overline{D}^{(*)0}$ decay to the same final state. These processes are thus sensitive to $\gamma = \arg\{-V_{ub}^*V_{ud}/V_{cb}^*V_{cd}\}$. The sensitivity to γ is proportional to the ratio between the $b \to u$ and $b \to c$ transition amplitudes (r_B), which depends on the B decay channel and needs to be determined experimentally.

In this paper we consider an alternative approach, based on neutral B mesons, which is similar to the ADS method [2] originally proposed for charged $B^- \to \tilde{D}^{(*)0}K^{(*)-}$ decays. We consider the decay channel $B^0 \to \tilde{D}^0 K^{*0}$ with $K^{*0} \to K^+\pi^-$ (charge conjugate processes are assumed throughout the paper and K^{*0} refers to the $K^*(892)^0$). This final state can be reached through $b \to c$ and $b \to u$ processes as shown in Fig. 1. The flavor of

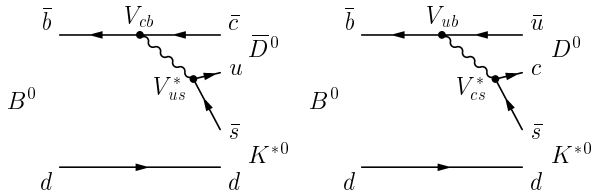FIG. 1: Feynman diagrams for $B^0 \to \overline{D}^0 K^{*0}$ (left, $\bar{b} \to \bar{c}$ transition) and $B^0 \to D^0 K^{*0}$ (right, $\bar{b} \to \bar{u}$ transition).

the B meson is identified by the charge of the kaon produced in the K^{*0} decay. The neutral D mesons are reconstructed in three final states, $f = K^+\pi^-$, $K^+\pi^-\pi^0$, $K^+\pi^-\pi^+\pi^-$. We search for $B^0 \to [\bar{f}]_D[K^+\pi^-]_{K^{*0}}$ events, where the CKM-favored $B^0 \to \overline{D}^0 K^{*0}$ decay, followed by the doubly Cabibbo-suppressed $\overline{D}^0 \to \bar{f}$ decay, interferes with the CKM-suppressed $B^0 \to D^0 K^{*0}$ decay, followed by the Cabibbo-favored $D^0 \to \bar{f}$ decay. These are called "opposite-sign" events because the two kaons in the final state have opposite charges. We also reconstruct a larger sample of "same-sign" events, which

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mainly arise from CKM-favored $B^0 \to \overline{D}^0 K^{*0}$ decays followed by Cabibbo-favored $\overline{D}^0 \to f$ decays.

In order to reduce the systematic uncertainties, we measure ratios of decay rates:

$$R_{ADS} \equiv \frac{\Gamma(\overline{B}^0 \to [f]_D \overline{K}^{*0}) + \Gamma(B^0 \to [\bar{f}]_D K^{*0})}{\Gamma(\overline{B}^0 \to [\bar{f}]_D \overline{K}^{*0}) + \Gamma(B^0 \to [f]_D K^{*0})} \quad (1)$$

$$A_{ADS} \equiv \frac{\Gamma(\overline{B}^0 \to [f]_D \overline{K}^{*0}) - \Gamma(B^0 \to [\bar{f}]_D K^{*0})}{\Gamma(\overline{B}^0 \to [f]_D \overline{K}^{*0}) + \Gamma(B^0 \to [\bar{f}]_D K^{*0})} \quad (2)$$

where R_{ADS} is the ratio between opposite- and same-sign events.

The K^{*0} resonance has a natural width ($50~\text{MeV}/c^2$) that is larger than the experimental resolution. This introduces a phase difference between the various amplitudes. We therefore introduce effective variables r_S, k, and δ_S [5], obtained by integrating over the region of the $B^0 \to \tilde{D}^0 K^+\pi^-$ Dalitz plot dominated by the K^{*0} resonance, defined as follows:

$$r_S^2 \equiv \frac{\Gamma(B^0 \to D^0 K^+\pi^-)}{\Gamma(B^0 \to \overline{D}^0 K^+\pi^-)} = \frac{\int dp\, A_u^2(p)}{\int dp\, A_c^2(p)}, \quad (3)$$

$$ke^{i\delta_S} \equiv \frac{\int dp\, A_c(p)A_u(p)e^{i\delta(p)}}{\sqrt{\int dp\, A_c^2(p)\, \int dp\, A_u^2(p)}}. \quad (4)$$

From their definition, $0 \le k \le 1$ and $\delta_S \in [0, 2\pi]$. The amplitudes for the $b \to c$ and $b \to u$ transitions, $A_c(p)$ and $A_u(p)$, are real and positive and $\delta(p)$ is the relative strong phase. The variable p indicates the position in the $\tilde{D}^0 K^+\pi^-$ Dalitz plot. The parameter k accounts for contributions, in the K^{*0} mass region, of higher-mass resonances. In the case of a two-body B decay, r_S and δ_S become $r_B = A_u/A_c$ and δ_B (the strong phase difference between A_u and A_c) with $k = 1$. As shown in [6], the distribution of k can be obtained by simulation studies based on realistic models for the different resonance contributions to the decays of neutral B mesons into $\tilde{D}^0 K^{\mp}\pi^{\pm}$ final states. When considering the region in the $B^0 \to \tilde{D}^0 K^+\pi^-$ Dalitz plane where the invariant mass of the kaon and the pion is within $48~\text{MeV}/c^2$ of the nominal K^{*0} mass [7], the distribution of k is narrow, and is centered at 0.95 with a root-mean-square width of 0.03.

Because of CKM factors and the fact that both diagrams in Fig. 1 are color-suppressed, the average amplitude ratio r_S in $B^0 \to \tilde{D}^0 K^{*0}$ is expected to be of order 0.3, larger than the analogous ratio for the charged $B^- \to D^{0(*)}K^{(*)-}$ decays, which is of order 0.1 [8, 9]. This implies better sensitivity to γ for the same number of events, an expectation that applies to all $B^0 \to D^{0(*)}K^{(*)0}$ decays, and that motivates the use of neutral B meson decays to determine γ. Currently, the experimental knowledge of r_S [6, 10] is $r_S < 0.54$ at 95% probability.

The ratios R_{ADS} and A_{ADS} are related to r_S, γ, k and

δ_S through the following relations:

$$R_{ADS} = r_S^2 + r_D^2 + 2kk_D r_S r_D \cos\gamma \cos(\delta_S + \delta_D), (5)$$

$$A_{ADS} = 2kk_D r_S r_D \sin\gamma \sin(\delta_S + \delta_D)/R_{ADS}, \quad (6)$$

where

$$r_D^2 \equiv \frac{\Gamma(D^0 \to f)}{\Gamma(D^0 \to \bar{f})} = \frac{\int dm \; A_{DCS}^2(m)}{\int dm \; A_{CF}^2(m)}, \quad (7)$$

$$k_D e^{i\delta_D} \equiv \frac{\int dm \; A_{CF}(m) A_{DCS}(m) e^{i\delta(m)}}{\sqrt{\int dm \; A_{CF}^2(m) \; \int dm \; A_{DCS}^2(m)}}, \quad (8)$$

with $0 \leq k_D \leq 1$, $\delta_D \in [0, 2\pi]$, $A_{CF}(m)$ and $A_{DCS}(m)$ the magnitudes of the Cabibbo-favored and the doubly-Cabibbo-suppressed amplitudes, $\delta(m)$ the relative strong phase, and the variable m the position in the D Dalitz plot. In the case of a two-body D decay, $k_D = 1$, r_D is the ratio between the doubly-Cabibbo-suppressed and the Cabibbo-favored decay amplitudes and δ_D is the relative strong phase.

Determining r_S, γ and δ_S from the measurements of R_{ADS} and A_{ADS}, with the factor k fixed, requires knowledge of the parameters (k_D, r_D, δ_D), which depend on the specific neutral D meson final states. The ratios r_D for the three D decay modes have been measured [7], as has the strong phase δ_D for the $K\pi$ mode [11]. In addition, experimental information is available on k_D and δ_D for the $K\pi\pi^0$ and $K\pi\pi\pi$ modes [12]. The smallness of the r_D ratios implies good sensitivity to r_S from a measurement of R_{ADS}. For the same reason, and since, with the present statistics, the asymmetries A_{ADS} cannot be extracted from data, the sensitivity to γ is reduced. The aim of this analysis is therefore the measurement of r_S. In the future, good knowledge of all the r_D, k_D and δ_D parameters, and a precise measurement of the R_{ADS} ratios for the three channels, will allow γ and δ_S to be determined from this method as well.

The results presented here are obtained with 423 fb^{-1} of data collected at the $\Upsilon(4S)$ resonance with the BABAR detector at the PEP-II e^+e^- collider at SLAC [13], corresponding to 465 million $B\overline{B}$ events. An additional "off-resonance" data sample of 41.3 fb^{-1}, collected at a center-of-mass (CM) energy 40 MeV below the $\Upsilon(4S)$ resonance, is used to study backgrounds from continuum events, $e^+e^- \to q\bar{q}$ ($q = u, d, s$, or c). The BABAR detector is described elsewhere [14].

The event selection is based on studies of off-resonance data and Monte Carlo (MC) simulations of continuum and $e^+e^- \to \Upsilon(4S) \to B\overline{B}$ events. All the selection criteria are optimised by maximising the function $S/\sqrt{S+B}$ on opposite-sign events, where S and B are the expected numbers of opposite-sign signal and background events, respectively.

The neutral D mesons are reconstructed from a charged kaon and one or three charged pions and, in the $K\pi\pi^0$ mode, a neutral pion. The π^0 candidates are reconstructed from pairs of photon candidates, each with energy greater than 70 MeV, total energy

greater than 200 MeV and invariant mass in the interval [118, 145] MeV/c^2. The π^0 candidate's mass is subsequently constrained to its nominal value [7].

The invariant mass of the particles used to reconstruct the D is required to lie within 14 MeV/c^2 ($\simeq 1.9\sigma$), 20 MeV/c^2 ($\simeq 1.5\sigma$) and 9 MeV/c^2 ($\simeq 1.6\sigma$) of the nominal D^0 mass, for the $K\pi$, $K\pi\pi^0$ and $K\pi\pi\pi$ modes, respectively. For the $K\pi\pi\pi$ mode we also require that the tracks originate from a single vertex with a probability greater than 0.1%.

The tracks used to reconstruct the K^{*0} are constrained to originate from a common vertex and their invariant mass is required to lie within 48 MeV/c^2 of the nominal K^{*0} mass [7]. We define θ_H as the angle between the direction of flight of the K and B in the K^{*0} rest frame. The distribution of $\cos\theta_H$ is proportional to $\cos^2\theta_H$ for signal events and is expected to be flat for background events. We require $|\cos\theta_H| > 0.3$. The charged kaons used to reconstruct the $\tilde{D}^0$ and K^{*0} mesons are required to satisfy kaon identification criteria, based on Cherenkov angle and dE/dx measurements and are typically 85% efficient, depending on momentum and polar angle. Misidentification rates are at the 2% level.

The B^0 candidates are reconstructed by combining a $\tilde{D}^0$ and K^{*0} candidate, constraining them to originate from a common vertex with a probability greater than 0.1%. In forming the B, the D mass is constrained to its nominal value [7]. The distribution of the cosine of the B polar angle with respect to the beam axis in the e^+e^- CM frame $\cos\theta_B$ is expected to be proportional to $1 - \cos^2\theta_B$. We require $|\cos\theta_B| < 0.9$. We measure two almost independent kinematic variables: the beam-energy substituted mass $m_{\rm ES} \equiv \sqrt{(E_0^{*2}/2 + \vec{p}_0 \cdot \vec{p}_B)^2/E_0^2 - p_B^2}$, and the energy difference $\Delta E \equiv E_B^* - E_0^*/2$, where E and p are energy and momentum, the subscripts B and 0 refer to the candidate B and e^+e^- system, respectively, and the asterisk denotes the e^+e^- CM frame. The distributions of $m_{\rm ES}$ and ΔE peak at the B mass and zero, respectively, for correctly reconstructed B mesons. The B candidates are required to have ΔE in the range $[-16, 16]$ MeV ($\simeq 1.3\sigma$), $[-20, 20]$ MeV ($\simeq 1.5\sigma$) and $[-19, 19]$ MeV ($\simeq 1.4\sigma$) for the $K\pi$, $K\pi\pi^0$ and $K\pi\pi\pi$ modes, respectively. Finally we consider events with $m_{\rm ES}$ in the range $[5.20, 5.29]$ GeV/c^2.

We examine background B decays that have the same final state reconstructed particles as the signal decay to identify modes with peaking structure in $m_{\rm ES}$ or ΔE that can potentially mimic signal events. We identify three such "peaking background" modes in the opposite-sign sample: $B^0 \to D^-[K^{*0}K^-]\pi^+$ (for $K\pi$), $B^0 \to D^-[K^{*0}K^-]\rho^+[\pi^+\pi^0]$ (for $K\pi\pi^0$) and $B^0 \to D^-[K^{*0}K^-]a_1^+[\pi^+\pi^+\pi^-]$ (for $K\pi\pi\pi$). To reduce their contribution we veto all candidates for which the invariant mass of the K^{*0} and the K^- from the D^0 lies within 6 MeV/c^2 of the nominal D^- mass.

After imposing the vetoes, the contributions of the peaking backgrounds to the $K\pi$, $K\pi\pi^0$ and $K\pi\pi\pi$ samples are predicted to be less than 0.07, 0.05 and 0.12

events, respectively, at 95% probability. Other possible sources of peaking background are $B^0 \to D^0 \rho^0$ and $B^0 \to D^{*-}[D^0\pi^-]\pi^+$, which contribute to the three decay modes in both the same- and opposite-sign samples. These events could be reconstructed as signal, due to misidentification of a π as a K. We impose additional restrictions on the identification criteria of charged kaons from K^* decays to reduce the contribution of these backgrounds to a negligible level. Charmless B decays, like $B^0 \to K^{*0}K\pi$, can also contribute. The number of expected charmless background events, evaluated with data from the $\tilde{D}^0$ mass sidebands, is N_{peak}=0.5 $\pm$ 0.5 (0.1 $\pm$ 1.2) in the same (opposite) sign samples.

In case of multiple D candidate (less than 1% of events), we choose the one with reconstructed $\tilde{D}^0$ mass closest to the nominal mass [7]. In the case of two B candidates reconstructed from the same $\tilde{D}^0$, we choose the candidate with the largest value of $|\cos\theta_H|$.

The overall reconstruction efficiencies for signal events are $(13.2 \pm 0.1)\%$, $(5.2 \pm 0.1)\%$ and $(6.5 \pm 0.1)\%$ for the $K\pi$, $K\pi\pi^0$ and $K\pi\pi\pi$ modes, respectively.

After applying the selection criteria described above, the remaining background is composed of continuum events and combinatorial $B\overline{B}$ events. To discriminate against the continuum background events (the dominant background component), which, in contrast to $B\overline{B}$ events, have a jet-like shape, we use a Fisher discriminant $\mathcal{F}$ [15]. The discriminant $\mathcal{F}$ is a linear combination of four variables calculated in the CM frame. The first discriminant variable is the cosine of the angle between the B thrust axis and the thrust axis of the rest of the event. The second and third variables are $L_0 = \sum_i p_i$, and $L_2 = \sum_i p_i|\cos\theta_i|^2$, where the index i runs over all the reconstructed tracks and energy deposits in the calorimeter not associated with a track, the tracks and energy deposits used to reconstruct the B are excluded, p_i is the momentum, and θ_i is the angle with respect to the thrust axis of the B candidate. The fourth variable is $|\Delta t|$, the absolute value of the measured proper time interval between the B and $\bar{B}$ decays, calculated from the measured separation between the decay points of the B and $\bar{B}$ along the beam direction.

The coefficients of $\mathcal{F}$, chosen to maximize the separation between signal and continuum background, are determined using samples of simulated signal and continuum events and validated using off-resonance data.

The signal and background yields are extracted, separately for each channel, by maximizing the extended likelihood $\mathcal{L} = (e^{-N'})/(N!) \cdot N'^N \cdot \prod_{j=1}^{N} f(\mathbf{x}_j \mid \theta, N')$. Here $\mathbf{x}_j = \{m_{ES}, \mathcal{F}\}$, θ is a set of parameters, N is the number of events in the selected sample and N' is the expectation value for the total number of events. The

term $f(\mathbf{x} \mid \theta, N')$ is defined as :

$$f(\mathbf{x} \mid \theta, N')N' = \frac{R_{ADS}N_{DK^*}}{1 + R_{ADS}} f_{SIG}^{OS}(\mathbf{x}|\theta_{SIG}^{OS})$$

$$+ \frac{N_{DK^*}}{1 + R_{ADS}} f_{SIG}^{SS}(\mathbf{x}|\theta_{SIG}^{SS}) +$$

$$+ N_{bkg}^{OS} f_{bkg}^{OS}(\mathbf{x}|\theta_{bkg}^{OS}) + N_{bkg}^{SS} f_{bkg}^{SS}(\mathbf{x}|\theta_{bkg}^{SS}) \qquad (9)$$

where N_{DK^*} is the total number of signal events, R_{ADS} is the ratio between opposite- and same-sign signal events, and "bkg" refers to continuum or $B\overline{B}$ background, and N_{cont}^{SS}, N_{cont}^{OS}, $N_{B\overline{B}}^{SS}$, and $N_{B\overline{B}}^{OS}$ are the number of same- and opposite-sign events for continuum and $B\overline{B}$ backgrounds. The probability density functions (PDFs) f are derived from MC and are defined as the product of one-dimensional distributions of m_{ES} and $\mathcal{F}$. The m_{ES} distributions are modeled with a Gaussian for signal, and threshold functions with different parameters for the continuum and $B\overline{B}$ backgrounds. The threshold function is expressed as follows:

$$A(x) = x \sqrt{1 - (\frac{x}{x_0})^2} \cdot e^{c\,(1-(\frac{x}{x_0})^2)}, \qquad (10)$$

where x_0 represents the maximum allowed value for the variable x described by $A(x)$ and c accounts for the shape of the distribution. The $\mathcal{F}$ distributions are modeled with Gaussians.

From the fit to data we extract N_{DK^*}, R_{ADS}, and the background yields (N_{cont}^{SS}, N_{cont}^{OS}, $N_{B\overline{B}}^{SS}$, and $N_{B\overline{B}}^{OS}$). We allow the mean of the signal m_{ES} PDF and parameters of the continuum m_{ES} PDF's to float.

The fitting procedure is validated using ensembles of simulated events. A large number of pseudo-experiments is generated with probability density functions and parameters as obtained from the fit to the data. The fitting procedure is then performed on these samples. We find no bias on the number of fitted events for any of the components.

The results for N_{DK^*}, R_{ADS} and the background yields are summarized in Table I. The total number of opposite-sign signal events in the three channels is $N_{SIG}^{OS} = 24.4_{-10.9}^{+13.7}$ (statistical uncertainty only). Projections of the fit onto the variable m_{ES} are shown

TABLE I: Fit results for N_{DK^*}, R_{ADS} and the number of background events, for the three channels. The uncertainties are statistical only.

channel	$K\pi$	$K\pi\pi^0$	$K\pi\pi\pi$
N_{DK^*}	74 ± 12	146 ± 17	101 ± 17
R_{ADS}	$0.067_{-0.054}^{+0.070}$	$0.060_{-0.037}^{+0.055}$	$0.137_{-0.095}^{+0.113}$
$N_{B\overline{B}}^{SS}$	75 ± 16	265 ± 33	345 ± 35
$N_{B\overline{B}}^{OS}$	40 ± 17	215 ± 41	327 ± 48
N_{cont}^{SS}	387 ± 22	2497 ± 56	2058 ± 53
N_{cont}^{OS}	1602 ± 41	7793 ± 96	6372 ± 91

in Fig. 2 for the opposite- and same-sign samples. To enhance the visibility of the signal, events are required to satisfy $\mathcal{F} > 0.5$ for $K\pi$, $\mathcal{F} > 0.7$ for $K\pi\pi^0$, and $\mathcal{F} > 1$ for $K\pi\pi\pi$. These requirements have an efficiency of about 67%, 67% and 50% for signal and 9%, 5% and 3% for continuum background.

The systematic uncertainties on R_{ADS} are summarized in Table II. To evaluate the contributions related to the m_{ES} and $\mathcal{F}$ PDFs, we repeat the fit by varying all the PDF parameters that are fixed in the final fit within their statistical errors, as obtained from the parametrization on simulated events. To evaluate the uncertainty arising from the assumption of negligible peaking background contributions, we repeat the fit by varying the number of these events within their statistical errors. In this evaluation, we consider all the possible sources of such backgrounds, coming from charmless B decays and from B decays with a D meson in the final state, as discussed above. For the multi-body D decays, the selection efficiency on same- and opposite-sign events has been confirmed to be the same, regardless of the difference in the Dalitz structure, within a relative error of 3%. Finally, a systematic uncertainty associated with cross feed between same- and opposite-sign events is evaluated from MC studies to be $(3.5 \pm 0.5)\%$, $(4.6 \pm 0.6)\%$ and $(1.9 \pm 0.4)\%$ for the $K\pi$, $K\pi\pi^0$ and $K\pi\pi\pi$ modes, respectively. The total systematic uncertainties are defined by adding the individual terms in quadrature.

TABLE II: Systematic uncertainties ΔR_{ADS}, in units of $[10^{-2}]$, for $R_{ADS}^{K\pi}$, $R_{ADS}^{K\pi\pi^0}$ and $R_{ADS}^{K\pi\pi\pi}$.

Source	$K\pi$	$K\pi\pi^0$	$K\pi\pi\pi$
Sig. PDF	0.19	0.11	0.82
Cont. PDF	0.32	0.02	0.29
$B\bar{B}$ PDF	0.57	0.16	1.48
Peaking bkg	1.70	0.87	1.40
$\epsilon_{CF}/\epsilon_{DCS}$	-	0.17	0.39
cross-feed	0.04	0.05	0.02
TOTAL	1.8	0.91	2.2

The final likelihood $\mathcal{L}(R_{ADS})$ for each decay mode is obtained by convolving the likelihood returned by the fit with a Gaussian whose width equals the systematic uncertainty. Figure 3 shows $\mathcal{L}(R_{ADS})$ for all three channels, where we exclude the unphysical region $R_{ADS} \leq 0$. The integral of the likelihood corresponding to $R_{ADS} < 0$ is 9.5% for $K\pi$, 15.8% for $K\pi\pi^0$ and 5.5% for $K\pi\pi\pi$. The significance of observing a signal is evaluated in each channel using the ratio $\log(\mathcal{L}_{max}/\mathcal{L}_0)$, where $\mathcal{L}_{max}$ and $\mathcal{L}_0$ are the maximum likelihood values obtained from the nominal fit and from a fit in which the signal component is fixed to zero, respectively. We observe a ratio R_{ADS} different from zero with a significance of 1.1, 1.7 and 1.4 standard deviations for the $K\pi$, $K\pi\pi^0$ and $K\pi\pi\pi$ modes, respectively. Since the measurements for the R_{ADS} ratios are not statistically significant, we calculate 95%

probability limits by integrating the likelihoods, starting from $R_{ADS} = 0$. We obtain $R_{ADS}(K\pi) < 0.244$, $R_{ADS}(K\pi\pi^0) < 0.181$ and $R_{ADS}(K\pi\pi\pi) < 0.391$ at 95% probability. The overall significance of observing an R_{ADS} signal, evaluated from the combination of the three measurements, is 2.5 standard deviations.

Following a Bayesian approach, the measurements of the R_{ADS} ratios are translated into a likelihood for r_S. A large number of simulated experiments for the parameters on which R_{ADS} depends (see Eq. 5) are performed. For each experiment, the values of $R_{ADS}(K\pi)$, $R_{ADS}(K\pi\pi^0)$ and $R_{ADS}(K\pi\pi\pi)$ are obtained and a weight $\mathcal{L}(R_{ADS}(K\pi))\mathcal{L}(R_{ADS}(K\pi\pi^0))\mathcal{L}(R_{ADS}(K\pi\pi\pi))$ is computed. In the extraction procedure to determine r_S, we use the experimental distributions for the r_D ratios, $\delta_D(K\pi)$, $k_D(K\pi\pi^0)$, $\delta_D(K\pi\pi^0)$, $k_D(K\pi\pi\pi)$ and $\delta_D(K\pi\pi\pi)$ [7, 11, 12]. All the remaining phases are extracted from a flat distribution in the range $[0, 2\pi]$. r_S is extracted from a flat distribution in the range $[0, 1]$ and k is extracted from a Gaussian distribution with mean 0.95 and standard deviation 0.03. We obtain the likelihood $\mathcal{L}(r_S)$ shown in Fig. 4. The most probable value is $r_S = 0.26$ and we obtain, by integrating the likelihood, the following 68% and 95% probability regions:

$$r_S \in [0.18, 0.34] @ 68\% \text{ probability},$$
$$r_S \in [0.07, 0.41] @ 95\% \text{ probability}.$$

Given the functional dependence of R_{ADS} on r_S ($R_{ADS} \sim r_S^2$), the likelihoods corresponding to $R_{ADS} < 0$ have no effective role in the extraction of r_S. The dependence of the r_S likelihood shown in Fig. 4 on the choice of the prior distributions in the extraction procedure has been studied. While the 68% and 95% probability regions are quite stable, the likelihood shows a dependence on the choice of the prior distribution for values of r_S close to zero. For this reason, the region near zero should not be used to evaluate the significance. The significance to observe r_S different from zero corresponds to the significance for R_{ADS}, and is evaluated from the combined fit to be 2.5 standard deviations. The result obtained for r_S with the procedure described above is consistent with the result found from a direct fit to data assuming the simplified expression $R_{ADS} = r_S^2$.

In summary, we have presented a search for $b \to u$ transitions in $B^0 \to \tilde{D}^0 K^{*0}$ decays, analysed through an ADS method. We see indications of a signal at the level of 2.5 standard deviations including systematic uncertainties. The most probable value for r_S extracted from this result is $r_S = 0.26$, where the 68% and 95% probability regions are indicated above. This result is in agreement with the phenomenological expectations from Ref. [16], and shows that the use of these decays and related ones [6] for the determination of γ is interesting in present and future facilities.
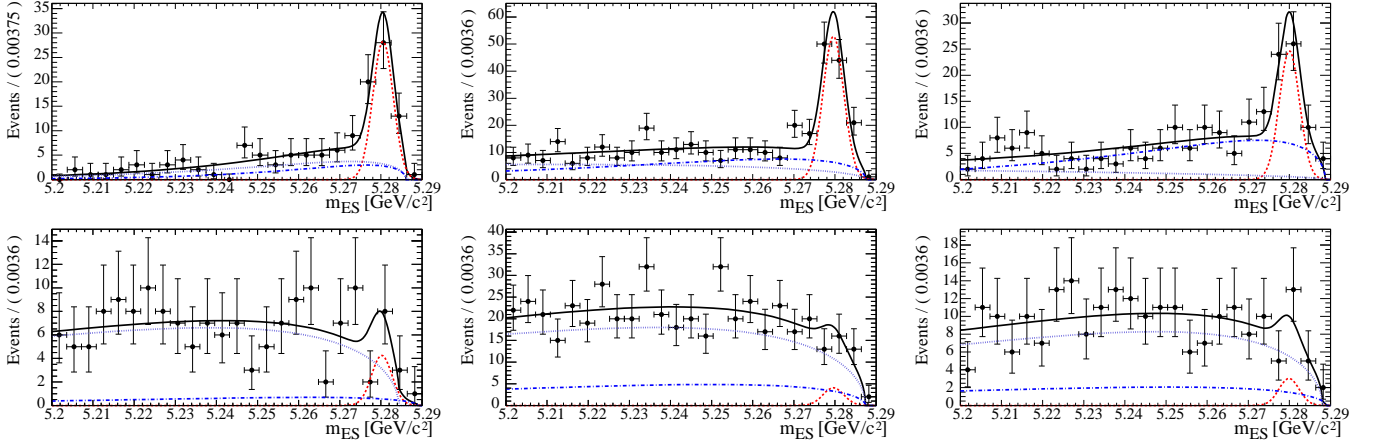
FIG. 2: Projections of the fit onto the variable m_{ES} after a cut on $\mathcal{F}$ is applied (> 0.5 for $K\pi$, > 0.7 for $K\pi\pi^0$ and > 1 for $K\pi\pi\pi$), to enhance the signal. The plots are shown for $K\pi$ (left), $K\pi\pi^0$ (middle) and $K\pi\pi\pi$ (right), same-sign (top) and opposite-sign (bottom) events. The points with error bars are data. The dashed, dotted and dash-dotted lines represent the signal, continuum background and $B\overline{B}$ background contributions, respectively. The solid line represents the sum of all the contributions.
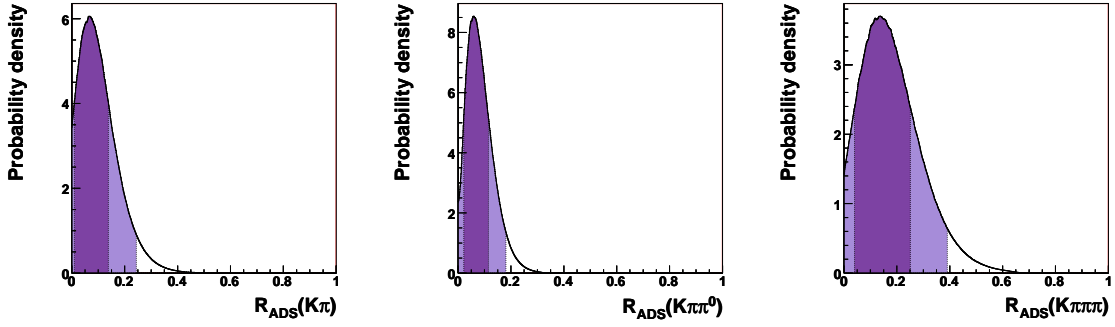
FIG. 3: Likelihood function for $R_{ADS}(K\pi)$ (left), $R_{ADS}(K\pi\pi^0)$ (middle) and $R_{ADS}(K\pi\pi\pi)$ (right), for $R_{ADS} \geq 0$, thus excluding unphysical values. The dark and light shaded zones represent the 68% and 95% probability regions, respectively.
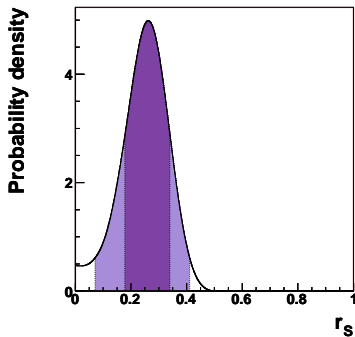
FIG. 4: Likelihood function for r_S from the combination of the measurements of R_{ADS} obtained in the three D decay channels. The dark and light shaded zones represent the 68% and 95% probability regions, respectively.

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