# $A b$ initio ground state potential energy surfaces for $\mathrm{Rg}-\mathrm{Br}_{2}(\mathrm{Rg}=\mathrm{He}, \mathrm{Ne}, \mathrm{Ar})$ complexes 

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#### Abstract

High-level $a b$ initio molecular electronic structure calculations are performed for $\mathrm{Rg}-\mathrm{Br}_{2}$ ( Rg $=\mathrm{He}, \mathrm{Ne}, \mathrm{Ar}$ ) complexes at $\operatorname{CCSD}(\mathrm{T})$ (coupled cluster using single and double excitations with a noniterative perturbation treatment of triple excitations) level of theory. Specific augmented correlation consistent basis sets are used for each noble atom ( Rg ), supplemented with an additional set of bond functions. Effective-core potentials (ECPs), augmented with diffusion ( $s p$ ) and polarization ( $3 d f$ ) functions, have been employed for the bromine atoms. For all complexes, the $\operatorname{CCSD}(\mathrm{T})$ potential energy surfaces (PESs) show double-minimum topology, with wells at both linear and T-shaped configurations; the linear minimum is found to be deeper than the T-shaped one. Vibrational corrections are taken into account for all the complexes and their effects in the stability of the linear and T-shaped conformers are examined. For each complex and each configuration (linear and T-shaped), $R_{e}$ equilibrium intermolecular distances, $D_{e}$ and $D_{0}$ dissociation energies, are evaluated and compared with previous theoretical and/or experimental results. © 2002 American Institute of Physics. [DOI: 10.1063/1.1473800]


## I. INTRODUCTION

The rare gas-halogen van der Waals (vdW) molecules provide relatively simple systems for which intermolecular potentials and dynamical processes can be studied in great detail by both experimentalists and theoreticians (see Refs. 1 and 2). One of the most interesting subjects of the rare gas dihalogen complexes turns out to be the structural analysis of their ground electronic state. Ab initio results predict global minima for linear configurations of these complexes ${ }^{3-7}$ whereas experimental data were consistent with the T-shaped configuration for the ground $(X)$ and electronically excited (B) states. Huang et al. ${ }^{8}$ have shown that this disagreement between theory and experiment is due to the zero-point vibrational energy that favors the T-shaped isomer.

Among the rare gas-dihalogen species, the most detailed theoretical studies have been performed for $\mathrm{Rg}-\mathrm{Cl}_{2}$ complexes (see Ref. 9 and references therein) and, in contrast, less attention has been paid to $\mathrm{Rg}-\mathrm{Br}_{2}$ systems, despite the experimental data available. In studying the dynamics of rare gas-dihalogen molecules, pairwise additive atom-atom potentials have been commonly used (see Refs. 10 and 11) with success in describing some important phenomena, but more detailed theoretical studies have shown ${ }^{12}$ that atom-atom forms are not consistent with experimental observations. Therefore, high-level ab initio theory should be employed to describe the weak van der Waals interactions.
$\mathrm{He}-\mathrm{Br}_{2}$ is one of the most studied complexes. Potential energy surfaces based on MP4 ab initio calculations have been reported ${ }^{12}$ for its ground $(X)$ and excited $(B)$ states and dynamical quantum calculations have been carried out ${ }^{10,12,13}$ emphazing the importance of the anisotropy of the PES for

[^0]the ground electronic state of $\mathrm{He}-\mathrm{Br}_{2}$. Later, another MP4 surface has been calculated ${ }^{14}$ and used to calculate an excitation spectrum of $\mathrm{He}-\mathrm{Br}_{2}$. Recently, a study based on $\operatorname{CCSD}(\mathrm{T})$ approach has been presented for $\mathrm{Ne}-\mathrm{Br}_{2}$ (Ref. 15) and, for $\mathrm{Ar}-\mathrm{Br}_{2}$, ab initio results ${ }^{16}$ at $\operatorname{CCSD}(\mathrm{T})$ level have established the double minimum topology of its potential energy surface but show a considerable underestimation of the binding energy of the complex.

The aim of this study is to present high-level $a b$ initio calculations, as accurately as currently possible at an $a b$ initio level, and to reproduce reliable PESs comparable to the available experimental data for weakly bound systems, for $\mathrm{Rg}-\mathrm{Br}_{2}$ complexes. Thus, we report on theoretical predictions of the linear and T-shaped structures, energies, and vibrational frequencies of $\mathrm{Rg}-\mathrm{Br}_{2}$ systems, and we compare our results with the best available values.

The paper is organized as follows. In Sec. II we outline the computational details of our $a b$ initio calculations. In Sec. III we discuss our ab initio results for each complex, we present the parametrized potential energy surfaces and discuss on equilibrium geometries, binding energies, and vibrational frequencies and compare with experimental data or previous ab initio studies. Conclusions constitute the closing section.

## II. COMPUTATIONAL DETAILS

The $a b$ initio calculations are performed using the GAUSSIAN 98 package. ${ }^{17}$ All computations are carried out at the $\operatorname{CCSD}(\mathrm{T})$ level of theory. For bromine atoms the Stuttgart group (SDD) effective core potential ${ }^{18}$ is employed. The valence electrons are described using the SDD basis set augmented with $(s p)$ diffusion and ( $3 d f$ ) polarization functions, denoted as $\mathrm{SDD}+\mathrm{G}(3 d f)$. The exponents of diffusion and polarization functions used for bromine associated with
the SDD ECP were those specified in the literature. ${ }^{15,19,20}$ Such ECPs basis sets have been used ${ }^{19-21}$ in calculations of halogen-containing molecules. In particular, $\operatorname{CCSD}(T)$ calculations for the $\mathrm{Br}_{2}$ molecule using the $\mathrm{SDD}+\mathrm{G}(3 d f)$ basis set ${ }^{15}$ are in very good agreement with experimental data and recent $\operatorname{CCSD}(\mathrm{T}) a b$ initio calculations using the extended SDB-cc-pVQZ basis set. ${ }^{22}$

For van der Waals complexes, efficient basis sets can be constructed with the use of midbond functions. Studies by Tao and $\operatorname{Pan}^{23}$ have shown the importance of these property specific basis sets; they provide an efficient way ${ }^{3,24}$ to saturate the dispersion energy, the dominant attractive force in the case of vdW complexes (e.g., $\mathrm{Rg}-\mathrm{X}_{2}, \mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{Br}$ ). The justification for using basis sets with bond functions is based on comparison with results obtained using larger basis sets in recent studies on weakly bound systems. ${ }^{9,25-28}$ For example, potential energy surfaces for $\mathrm{Rg}-\mathrm{F}_{2}$ and $\mathrm{Rg}-\mathrm{Cl}_{2}$ complexes have been already re-examined ${ }^{9,26}$ using basis sets augmented with bond functions. The high quality of the results obtained with basis sets augmented with bond functions became even more convincing when comparison has been made ${ }^{25}$ with interaction energies for $\mathrm{Ar}-\mathrm{HCl}$ at the complete basis set limit.

The exponents of the bond functions are known to be quite system independent ${ }^{29}$ and, after studying the efficiency of some of them performing systematic calculations, we select the $(3 s 3 p 2 d 2 f 1 g)$ bond functions with exponents given in Ref. 27. Therefore, for the Rg atom we used augmented correlation consistent (aug-cc-pVnZ, $\mathrm{n}=\mathrm{Q}, 5$ ) basis sets incorporated in the GAUSSIAN 98 programs supplemented with an additional set $(3 s 3 p 2 d 2 f 1 g)$ of bond functions ${ }^{27}$ and will be denoted as aug-cc-pVnZ+ $(3 s 3 p 2 d 2 f 1 g)$, n $=\mathrm{Q}, 5$. We place the bond functions in the middle of the van der Waals bond and in all calculations $6 d$ and $10 f$ Cartesian functions are used.

In our study, for each complex, the results obtained with aug-cc-pVnZ+( $3 s 3 p 2 d 2 f 1 g)$ basis sets were in better agreement with experimental data than those obtained using aug-cc-pVnZ basis sets, demostrating that the use of bond functions clearly gives much more efficient basis sets. To better illustrate the importance of bond functions we report on the dissociation energies for the $\mathrm{Rg}-\mathrm{Br}_{2}$ complexes, taken using aug-cc-pVnZ basis sets with and without $(3 s 3 p 2 d 2 f 1 g)$ bond functions. For $\mathrm{He}-\mathrm{Br}_{2}$ we get a difference of $11 \mathrm{~cm}^{-1}$ in the $D_{e}$ values of the T-shaped and linear configurations, for $\mathrm{Ne}-\mathrm{Br}_{2}$ a difference of $35 \mathrm{~cm}^{-1}$ and for $\mathrm{Ar}-\mathrm{Br}_{2}$ is $98 \mathrm{~cm}^{-1}$, resulting in a significant improvement with respect to the corresponding values when using aug-cc-pVnZ, $\mathrm{n}=\mathrm{Q}, 5$ basis sets for the Rg atoms. We should note that results obtained with the aug-cc-pVnZ, n $=\mathrm{Q}, 5$ basis with and without bond functions are qualitatively similar. The difference between the energies of the linear and the T-shaped structures is preserved, with the T-shaped configurations being always higher in energy that the linear ones, independently of the use of the bond functions.

## III. RESULTS

## A. Ab initio calculations

The potential energy surfaces for $\mathrm{He}-\mathrm{Br}_{2}, \mathrm{Ne}-\mathrm{Br}_{2}$, and $\mathrm{Ar}-\mathrm{Br}_{2}$ complexes are examined using the supermolecular approach. In a supermolecular calculation, the interaction energy between a pair of atoms or molecules, is given by

$$
\begin{equation*}
\Delta E=E_{\mathrm{Rg}-\mathrm{Br}_{2}}-E_{\mathrm{BSSE}-E_{\mathrm{Rg}}-E_{\mathrm{Br}_{2}}, ~}^{\text {, }} \tag{1}
\end{equation*}
$$

where $E_{\mathrm{Rg}-\mathrm{Br}_{2}}$ is the energy of the complex $(\mathrm{Rg}$ $=\mathrm{He}, \mathrm{Ne}, \mathrm{Ar})$ and the $E_{\mathrm{Rg}}, E_{\mathrm{Br}_{2}}$ are the energies of the monomers. The results are corrected for the basis-set superposition error ( $E_{\text {BSSE }}$ ) using the standard counterpoise method. ${ }^{30}$ We used Jacobi coordinates $(r, R, \theta)$ to describe the triatomic complexes, where $R$ is the intermolecular distance of Rg atom from the center of mass of $\mathrm{Br}_{2}, r$ is the bond length of $\mathrm{Br}_{2}$, and $\theta$ is the angle between the $\mathbf{R}$ and $\mathbf{r}$ vectors. For each of the $\mathrm{Rg}-\mathrm{Br}_{2}$ molecules, we examined several intermolecular distances $R(2.5 \leqslant R \leqslant 10 \AA)$, and for each of them we performed calculations for $\theta=0^{\circ}, 30^{\circ}, 60^{\circ}, 90^{\circ}$ with fixed $r=2.28 \AA$. The results for each system are listed in three tables: Table I contains the $\operatorname{CCSD}(\mathrm{T})$ interaction energies for $\mathrm{He}-\mathrm{Br}_{2}$, Table II for $\mathrm{Ne}-\mathrm{Br}_{2}$ and Table III for the $\mathrm{Ar}-\mathrm{Br}_{2}$ complex.

For $\mathrm{He}-\mathrm{Br}_{2}$, we get [see Figs. 1(a), 2(a), and Table IV] at $\theta=0^{\circ}, D_{e}=222.5 \mu E_{h}\left(48.8 \mathrm{~cm}^{-1}\right)$ and $R=4.42 \AA$, for $\theta=90^{\circ} D_{e}=183.5 \mu \mathrm{E}_{h}\left(40.3 \mathrm{~cm}^{-1}\right)$ and $R=3.58 \AA$. These results are in agreement with previous ab initio calculations, ${ }^{14}$ although our calculations give lower interaction energies $\left(5.8 \mathrm{~cm}^{-1}\right.$ for the linear isomer and $1.3 \mathrm{~cm}^{-1}$ for the T-shaped one) than in the previous study (see Table IV). Furthermore, our calculations predict a larger (by $8.5 \mathrm{~cm}^{-1}$ ) difference between the energies of the two structures than the results of Williams. ${ }^{14}$ In Table IV we also present results on the $D_{e}$ and $R_{e}$ values given by a IDIM PT1 semiempirical model. ${ }^{10}$ This model predicts double mini-

TABLE I. $\operatorname{CCSD}(\mathrm{T})$ interaction energies for the $\mathrm{He}-\mathrm{Br}_{2}$ molecule obtained with the aug-cc-pV5Z $+(3 s 3 p 2 d 2 f 1 g)$ basis set for the He and SDD $+\mathrm{G}(3 d f) \mathrm{ECP}$ for Br at $\theta=0^{\circ}, 30^{\circ}, 60^{\circ}$, and $90^{\circ}$. $r$ fixed at $2.28 \AA$.

|  | $\Delta E\left(\mu E_{h}\right)$ |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| $R^{\mathrm{a}}(\AA)$ | $\theta=0^{\circ}$ | $\theta=30^{\circ}$ | $\theta=60^{\circ}$ | $\theta=90^{\circ}$ |
| 2.5 | 1914.3 |  |  |  |
| 3.0 | -132.0 | 8084.9 | 4673.3 | 249.1 |
| 3.25 | -222.4 |  |  | -95.1 |
| 3.5 | -197.8 |  |  | -180.1 |
| 3.75 | -150.0 |  | -46.7 | -141.3 |
| 4.0 | -109.1 |  | -90.2 | -107.2 |
| 4.25 | -77.6 | -16.8 | -88.3 | -79.4 |
| 4.5 | -55.2 | -104.2 |  |  |
| 4.75 |  | -109.5 | -56.9 | -43.0 |
| 5.0 | -29.0 | -91.3 | -32.3 |  |
| 5.5 | -3.8 | -52.3 | -6.7 | -5.3 |
| 7.0 | -0.8 | -1.7 | -1.3 | -1.2 |
| 9.0 |  |  |  |  |

${ }^{\text {a }}$ For linear configurations $R$ is the distance to the nearest Br atom and for all the other configurations the distance from He atom to the $\mathrm{Br}_{2}$ center of mass.

TABLE II. $\operatorname{CCSD}(\mathrm{T})$ interaction energies for the $\mathrm{Ne}-\mathrm{Br}_{2}$ molecule obtained with the aug-cc-pVQZ+ $(3 s 3 p 2 d 2 f 1 g)$ basis set for the Ne and SDD $+\mathrm{G}(3 d f) \mathrm{ECP}$ for Br at $\theta=0^{\circ}, 30^{\circ}, 60^{\circ}$, and $90^{\circ}$. $r$ fixed at $2.28 \AA$.

|  | $\Delta E\left(\mu E_{h}\right)$ |  |  |  |
| :--- | :---: | ---: | :---: | ---: |
| $R^{\mathrm{a}}(\AA)$ | $\theta=0^{\circ}$ | $\theta=30^{\circ}$ | $\theta=60^{\circ}$ | $\theta=90^{\circ}$ |
| 2.5 | 5413.5 |  |  |  |
| 3.0 | -104.4 |  |  | -1658.9 |
| 3.25 | -413.4 |  |  | -377.6 |
| 3.5 | -401.6 | 7682.1 | -170.0 | -369.5 |
| 3.75 | -315.3 |  | -226.0 | -228.4 |
| 4.0 | -230.7 |  | -203.2 | -168.5 |
| 4.25 | -164.4 | -95.8 | -161.9 |  |
| 4.5 | -116.8 | -252.7 | -122.8 | -90.4 |
| 4.75 |  | -247.5 | -67.9 |  |
| 5.0 | -60.9 | -200.0 | -13.6 | -10.8 |
| 5.5 |  | -111.1 | -2.6 | -2.3 |
| 7.0 | -7.6 | -19.5 | -3.5 |  |
| 9.0 | -1.8 |  |  |  |

${ }^{\text {a }}$ For linear configurations $R$ is the distance to the nearest Br atom and for all the other configurations the distance from Ne atom to the $\mathrm{Br}_{2}$ center of mass.
mum topology for the ground $\mathrm{He}-\mathrm{Br}_{2}$ state with almost similar energies for the two isomers; $38.0 \mathrm{~cm}^{-1}$ for the linear and $37.9 \mathrm{~cm}^{-1}$ for the T-shaped.

For $\mathrm{Ne}-\mathrm{Br}_{2}$, we get [see Figs. 1(b), 2(b), and Table IV] at $\theta=0^{\circ} D_{e}=426.7 \mu E_{h}\left(93.6 \mathrm{~cm}^{-1}\right)$ and $R=4.49 \AA$, and at $\theta=90^{\circ} \quad D_{e}=391.6 \mu E_{h}\left(85.9 \mathrm{~cm}^{-1}\right)$ and $R=3.60 \AA$. Again, the interaction energies predicted by our calculation are lower than the ones obtained in a previous $\operatorname{CCSD}(\mathrm{T}) a b$ initio calculation ${ }^{15}$ for both conformers (see Table IV). The differences account $26.3 \mathrm{~cm}^{-1}$ for the linear structure and $25.4 \mathrm{~cm}^{-1}$ for the T-shaped one, and this improvement in the binding energies for $\mathrm{Ne}-\mathrm{Br}_{2}$ fully justifies the use of the bond functions.

For $\mathrm{Ar}-\mathrm{Br}_{2}$ [see Figs. 1(c), 2(c), and Table IV], $D_{e}$ $=1197.1 \mu E_{h}\left(262.7 \mathrm{~cm}^{-1}\right)$ and $R=4.63 \AA$ at $\theta=0^{\circ}$, and $D_{e}=1031.3 \mu E_{h}\left(226.4 \mathrm{~cm}^{-1}\right)$ and $R=3.8 \AA$ at $\theta=90^{\circ}$.

TABLE III. $\operatorname{CCSD}(\mathrm{T})$ interaction energies for the $\mathrm{Ar}-\mathrm{Br}_{2}$ molecule obtained with the aug-cc-pVQZ $+(3 s 3 p 2 d 2 f 1 g)$ basis set for the Ar and $\mathrm{SDD}+\mathrm{G}(3 d f) \mathrm{ECP}$ for Br at $\theta=0^{\circ}, 30^{\circ}, 60^{\circ}$, and $90^{\circ} . r$ fixed at $2.28 \AA$.

|  | $\Delta E\left(\mu E_{h}\right)$ |  |  |  |
| :--- | ---: | ---: | ---: | ---: |
| $R^{\mathrm{a}}(\AA)$ | $\theta=0^{\circ}$ | $\theta=30^{\circ}$ | $\theta=60^{\circ}$ | $\theta=90^{\circ}$ |
| 2.5 | 18822.4 |  | 4636.2 |  |
| 3.0 | 667.9 |  |  | 684.9 |
| 3.25 | -926.7 |  |  | -701.6 |
| 3.5 | -1200.6 | 26025.0 |  | -115.6 |
| 3.75 | -1047.8 |  | -953.7 | -773.0 |
| 4.0 | -809.3 |  | -622.3 | -591.8 |
| 4.25 | -595.3 | 334.5 | -538.9 |  |
| 4.5 | -430.0 | -567.1 | -742.6 | -427.4 |
| 4.75 |  | -666.5 | -245.8 | -326.8 |
| 5.0 | -225.3 | -401.2 | -48.9 | -38.5 |
| 5.5 | -27.4 | -71.4 | -9.4 | -8.0 |
| 7.0 | -6.1 | -12.4 |  |  |
| 9.0 |  |  |  |  |

${ }^{\text {a }}$ For linear configurations $R$ is the distance to the nearest Br atom and for all the other configurations the distance from Ar atom to the $\mathrm{Br}_{2}$ center of mass.


FIG. 1. Contour plots of the $\mathrm{Rg}-\mathrm{Br}_{2}$ potential energy surfaces, $V(R, \theta)$ [Eq. (3)]. (a) For $\mathrm{He}-\mathrm{Br}_{2}$ contour intervals are of $10 \mathrm{~cm}^{-1}$ and for energies from -45 to $15 \mathrm{~cm}^{-1}$. (b) For $\mathrm{Ne}-\mathrm{Br}_{2}$ contour intervals are of $15 \mathrm{~cm}^{-1}$ and for energies from -90 to $15 \mathrm{~cm}^{-1}$. (c) For $\mathrm{Ar}-\mathrm{Br}_{2}$ contour intervals are of $50 \mathrm{~cm}^{-1}$ and for energies from -260 to $40 \mathrm{~cm}^{-1}$. The $\mathrm{Br}-\mathrm{Br}$ bond length is fixed at $2.28 \AA$.


FIG. 2. Potential energy curves for $\mathrm{Rg}-\mathrm{Br}_{2}$ complexes, calculated at $\operatorname{CCSD}(\mathrm{T})$ level with the $\mathrm{SDD}+\mathrm{G}(3 d f)$ basis set for Br and aug-cc-pV5Z $+(3 s 3 p 2 d 2 f 1 g)$ basis set for He (a), aug-cc-pVQZ+ ( $3 s 3 p 2 d 2 f 1 g)$ basis set for $\mathrm{Ne}(\mathrm{b})$ and $\mathrm{Ar}(\mathrm{c})$. Ab initio results are indicated by open symbols, circles for $\theta=0^{\circ}$ and squares for $\theta=90^{\circ}$. Full lines are for the parametrized potential curves $V\left(R, \theta_{i}\right)_{i=1,4}$ [Eq. (2)].

TABLE IV. Binding energies ( $D_{e}$ and $D_{0}{\text { in } \mathrm{cm}^{-1}}^{\text {}}$ ) and equilibrium distances (in $\AA$ ) for the indicated $\mathrm{Rg}-\mathrm{Br}_{2}$ ( $\mathrm{Rg}=\mathrm{He}, \mathrm{Ne}, \mathrm{Ar}$ ) complexes.

| Complex |  | Linear |  |  | T-shaped |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $D_{\text {e }}$ | $D_{0}$ | $R_{\text {e }}$ | $D_{\text {e }}$ | $D_{0}$ | $R_{\text {e }}$ |
| $\mathrm{He}-\mathrm{Br}_{2}$ | This work | 48.8 | 17.2 | 4.42 | 40.3 | 17.7 | 3.58 |
|  | Best $a b$ initio value (Refs. 1, 14) | 43.0 |  | 4.50 | 39.0 |  | 3.70 |
|  | Semiempirical value (Ref. 10) | 38.0 | 16.8 | 4.93 | 37.9 | 17.3 | 3.63 |
|  | Experimental value (Refs. 1, 31) |  |  |  |  | $17.0 \pm 1.5$ |  |
| $\mathrm{Ne}-\mathrm{Br}_{2}$ | This work | 93.6 | 68.0 | 4.49 | 85.9 | 67.3 | 3.60 |
|  | Best ab initio value (Ref. 15) | 67.3 | 46.2 | 4.61 | 60.5 | 46.7 | 3.73 |
|  | Semiempirical value (Ref. 33) |  |  |  |  | 71.25 | 3.64 |
|  | Experimental value (Ref. 32) |  |  |  |  | $70.5 \pm 2.0$ | 3.67 |
| $\mathrm{Ar}-\mathrm{Br}_{2}$ | This work | 262.7 | 228.0 | 4.63 | 226.4 | 203.5 | 3.80 |
|  | Best $a b$ initio value (Ref. 16) | 162.6 |  | 4.85 | 145.3 |  | 3.99 |
|  | Semiempirical value (Ref. 16) | 256.6 | 220.0 | 4.60 | 247.2 | 213.5 | 3.65 |

Recent $a b$ initio $\operatorname{CCSD}(\mathrm{T})$ calculations by Naumkin and McCourt ${ }^{16}$ for the $\mathrm{Ar}-\mathrm{Br}_{2}$ ground state have estimated $162.6 \mathrm{~cm}^{-1}$ and $145.3 \mathrm{~cm}^{-1}$ for the $D_{e}$ of the two isomers (see Table IV). In order to represent their ab initio data, Naumkin and McCourt ${ }^{16}$ have suggested diatomics-inmolecules (DIM) based models predicted a $D_{e}$ value of $256.1 \mathrm{~cm}^{-1}$ for the linear isomer and $247.2 \mathrm{~cm}^{-1}$ for the T-shaped (see Table IV). Both estimates (ab initio and semiempirical) are higher than our predictions.

## B. Analytical representation of the PESs

For each $\theta$, the calculated interaction energies (see Tables I, II, III) are fitted to an analytical expression. Various potential forms are tested for the $V\left(R, \theta_{i}\right), i=1-4$ curves, including Morse, Degli Esposti, and Werner, ${ }^{34}$ and combinations of Morse-vdW, Morse-Born-Mayer-vdW type. We found that the Morse-vdW type form was the most flexible, allowing for an accurate representation of the ab initio points at short $(1.5 \leqslant R \leqslant 3.0 \AA$ ) and large ( $R \geqslant 10.0 \AA$ ) distances, ensuring a correct asymptotic behavior. Therefore, we use
this analytical expression to fit the $\operatorname{CCSD}(\mathrm{T})$ data for each complex. The potential function has the following form,

$$
\begin{align*}
V\left(R, \theta_{i}\right)= & D_{e}^{i}\left(\exp \left(-2 \alpha^{i}\left(R-R_{e}^{i}\right)\right)\right. \\
& \left.-2 \exp \left(-\alpha^{i}\left(R-R_{e}^{i}\right)\right)\right)-\frac{C_{6}^{i}}{R^{6}}-\frac{C_{8}^{i}}{R^{8}} \tag{2}
\end{align*}
$$

with parameters $D_{e}^{i}, \alpha^{i}, R_{e}^{i}, C_{6}^{i}$, and $C_{8}^{i}, i=1-4$. For each $\mathrm{Rg}-\mathrm{Br}_{2}$ complex, and each angle we fitted the ab initio points given in Tables I, II, and III to the expression given in Eq. (2). All adjustable parameters for each $\mathrm{Rg}-\mathrm{Br}_{2}$ complex are listed in Table V using a nonlinear least square calculation. We should note that the above parameters do not have physical meaning and they simply serve the fitting procedure. The average absolute deviation (standard deviation) between the original $a b$ initio data and the fit was smaller than $0.55 \mu E_{h}\left(0.12 \mathrm{~cm}^{-1}\right)$ for $\mathrm{He}-\mathrm{Br}_{2}, 0.64 \mu E_{h}\left(0.14 \mathrm{~cm}^{-1}\right)$ for $\mathrm{Ne}-\mathrm{Br}_{2}$ and $3.0 \mu E_{h}\left(0.7 \mathrm{~cm}^{-1}\right)$ for $\mathrm{Ar}-\mathrm{Br}_{2}$ for energies $\Delta E \leqslant 1000 \mathrm{~cm}^{-1}$.

To represent the two-dimensional interaction potentials

TABLE V. Parameters for the $V\left(R, \theta_{i}\right), i=1-4$ potential [Eq. (2)] for the indicated $\mathrm{Rg}-\mathrm{Br}_{2}(\mathrm{Rg}=\mathrm{He}, \mathrm{Ne}, \mathrm{Ar})$ complexes. Distances are in $\AA$ and energies in $\mathrm{cm}^{-1}$.

| $\theta$ | $D_{e}$ | $\alpha$ | $R_{e}$ | $\mathrm{C}_{6}$ | $\mathrm{C}_{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{He}-\mathrm{Br}_{2}$ complex |  |  |  |  |  |
| $0^{\circ}$ | 51.1559 | 1.91746 | 4.33265 | 351738.0 | -7.053 81e06 |
| $30^{\circ}$ | 6.80833 | 1.80298 | 4.92556 | 206838.0 | 38079.4 |
| $60^{\circ}$ | 8.33059 | 1.70709 | 4.49513 | 180297.0 | $-1.79557 e 06$ |
| $90^{\circ}$ | 5.81244 | 1.65289 | 4.18463 | 97681.0 | 137714.0 |
| $\mathrm{Ne}-\mathrm{Br}_{2}$ complex |  |  |  |  |  |
| $0^{\circ}$ | 22.5201 | 1.97739 | 4.78441 | 383914.0 | $6.34979 e 06$ |
| $30^{\circ}$ | 15.5201 | 1.83880 | 4.88177 | 400073.0 | $1.32119 e 06$ |
| $60^{\circ}$ | 13.3680 | 1.74322 | 4.55066 | 334625.0 | -1.509 96e06 |
| $90^{\circ}$ | 10.8445 | 1.69859 | 4.20071 | 225779.0 | 129474.0 |
| $\mathrm{Ar}-\mathrm{Br}_{2}$ complex |  |  |  |  |  |
| $0^{\circ}$ | 334.0670 | 1.76570 | 4.48161 | $2.43358 e 06$ | $-6.34372 e 07$ |
| $30^{\circ}$ | 343.3370 | 1.68328 | 4.40510 | $2.56572 e 06$ | -8.745 64e07 |
| $60^{\circ}$ | 23.5244 | 1.52175 | 5.03527 | 555289.0 | $1.39325 e 07$ |
| $90^{\circ}$ | 10.8432 | 1.56397 | 4.86562 | 545334.0 | $1.01310 e 07$ |

of the $\mathrm{Rg}-\mathrm{Br}_{2}$ complexes we use an expansion in Legendre polynomials,

$$
\begin{equation*}
V(R, \theta)=\sum_{\lambda} V_{\lambda}(R) P_{\lambda}(\cos \theta) \tag{3}
\end{equation*}
$$

where the $V_{\lambda}(R)$ coefficients are obtained by a collocation method. Figure 1 presents two-dimensional contour plots of the $V(R, \theta)$ surfaces for all the $\mathrm{Rg}-\mathrm{Br}_{2}$ complexes in the $X Y$-plane. The equipotential curves are shown for Rg moving around of a $\mathrm{Br}_{2}$ molecule with fixed $r_{e}=2.28 \AA$. For each complex, the linear potential well is deeper than the perpedicular well and the barriers between the two wells are at energies $-18.1 \mathrm{~cm}^{-1}$ for $\mathrm{He}-\mathrm{Br}_{2},-44.5 \mathrm{~cm}^{-1}$ for $\mathrm{Ne}-\mathrm{Br}_{2}$ and $-126.5 \mathrm{~cm}^{-1}$ for $\mathrm{Ar}-\mathrm{Br}_{2}$. The isomerization barrier for $\mathrm{He}-\mathrm{Br}_{2}$ is rather low, so the lowest vibrational levels are expected to be extended in both wells. For $\mathrm{Ne}-\mathrm{Br}_{2}$ and $\mathrm{Ar}-\mathrm{Br}_{2}$ the isomerization barriers are high enough, so the lowest vibrational levels of these complexes are expected to be mostly localized in either the linear or T-shaped well.

## C. Vibrational analysis

As mentioned before, the zero-point energy plays an extremely important role in the stabilization of the T-shaped structures for all these complexes. Therefore, zero-point energies are calculated here for the $\mathrm{Rg}-\mathrm{Br}_{2}$ complexes. The harmonic approximation is expected to underestimate the zero-point energy for these complexes, therefore, we performed quantum mechanical calculations to evaluate the $D_{0}$ for these systems. The Hamiltonian has the form

$$
\begin{equation*}
\hat{H}=-\frac{\hbar^{2}}{2 \mu_{1}} \frac{\partial^{2}}{\partial R^{2}}+\frac{\hat{j}^{2}}{2 \mu_{2} r_{e}^{2}}+\frac{\hat{l}^{2}}{2 \mu_{1} R^{2}}+V\left(r_{e}, R, \theta\right), \tag{4}
\end{equation*}
$$

where $\mu_{1}^{-1}=m_{\mathrm{Rg}}^{-1}+\left(2 m_{\mathrm{Br}}\right)^{-1}$ and $\mu_{2}^{-1}=m_{\mathrm{Br}}^{-1}+m_{\mathrm{Br}}^{-1}$ are the reduced masses, $m_{\mathrm{Rg}}(\mathrm{Rg}=\mathrm{He}, \mathrm{Ne}, \mathrm{Ar})$ and $m_{\mathrm{Br}}$ are the atomic masses, $\hat{l}$ and $\hat{\jmath}$ are the angular momenta associated with the vectors $\mathbf{R}$ and $\mathbf{r}$, respectively, leading to a total angular momenta $\hat{J}=\hat{l}+\hat{\jmath}$. $r_{e}$ is fixed to the equilibrium $\mathrm{Br}-\mathrm{Br}$ bond length, and the potential for each complex is given by the $V(R, \theta)$ expansion [Eq. (3)].

Using the one-dimensional potentials given in Eq. (3), numerical basis functions $\left\{f_{n}(R)\right\}_{n=1, \ldots, 12}$ are obtained by solving the one-dimensional Schrödinger equation. For each angle $\theta$, we choose three basis functions and we orthonormalized them using the Gram-Schmidt procedure. For a zero total angular momentum, $\hat{l}=-\hat{\jmath}$, the corresponding twodimensional Hamiltonian is represented in the radial, $\left\{f_{n}(R)\right\}$, and the angular, $\left\{P_{m}(\cos \theta)\right\}$, basis functions and the calculated eigenvalues correspond to the vibrational energy levels. The results of these calculations, in comparison with the best available data for the $\mathrm{Rg}-\mathrm{Br}_{2}$ complexes are summarized in Table IV. In Fig. 3 we present contour plots of the probability density distributions for the two lowest vdW vibrational levels ( $n=0, n=1$ ) for each of the $\mathrm{Rg}-\mathrm{Br}_{2}$ molecules.

For $\mathrm{He}-\mathrm{Br}_{2}$ complex the lowest two ( $n=0,1$ ) vdW vibrational levels for $J=0$ are found at energies of -17.7 and $-17.2 \mathrm{~cm}^{-1}$, respectively, with a very small energy difference between them $\left(\approx 0.5 \mathrm{~cm}^{-1}\right)$, and slightly above the


FIG. 3. Contour plots of the probability density distributions for the $n=0$ and $n=1$ vdW levels calculated using the $V(R, \theta)$ [Eq. (3)] for each $\mathrm{Rg}-\mathrm{Br}_{2}$ complex. (a) For $\mathrm{He}-\mathrm{Br}_{2}$ contour lines are for $1.0,0.5,0.1,0.01,0.001$, (b) for $\mathrm{Ne}-\mathrm{Br}_{2}$ contour lines are for 2.0, 1.0, 0.1, 0.01, 0.001, (c) for $\mathrm{Ar}-\mathrm{Br}_{2}$ contour lines are for $5.0,1.0,0.1,0.01,0.001$.
isomerization barrier. The $n=0$ eigenfunction is mainly localized in the T-shaped well, whereas the $n=1$ corresponds to linear configurations [see Figs. 2(a) and 3(a)]. However, we should note [see Fig. 3(a)] that both the $n=0$ and $n=1$ wave functions are extended to linear and T-shaped configurations. As we see, zero-point vibrational corrections bring the energies of the two configurations to approximately the same level and they reverse the ordering of the two minima, with the T-shaped to be the lowest one. This is in accord with predictions based on semiempirical data ${ }^{10}$ and on an indirect experimental estimate ${ }^{1,31}$ (see Table IV).

For $\mathrm{Ne}-\mathrm{Br}_{2}$ system, the $n=0,1 \mathrm{vdW}$ vibrational levels for $J=0$ are at energies of -68.0 and $-67.3 \mathrm{~cm}^{-1}$, respectively, with an energy difference of only $0.7 \mathrm{~cm}^{-1}$. These figures are within the error bar of the experimental estimate ${ }^{32}$ of $D_{0}=70.5 \pm 2.0 \mathrm{~cm}^{-1}$ (see Table IV). The $n=0$ eigenfunction localized in the linear isomer and the $n=1$ in the T-shaped one [see Figs. 2(b) and 3(b)]. It is interesting to note that the zero-point corrections does not alter the stability of the two minima for the $\mathrm{Ne}-\mathrm{Br}_{2}$.

For $\mathrm{Ar}-\mathrm{Br}_{2}$ molecule, we found the $n=0,1 \mathrm{vdW}$ vibrational levels at energies of -228.0 and $-203.5 \mathrm{~cm}^{-1}$ with an energy difference of $24.5 \mathrm{~cm}^{-1}$. Our calculations indicate that the linear well still remains significantly deeper than the T-shaped one, even when the zero-point vibrational energy is included. Figures 2(c) and 3(c) show that the $n=0$ eigenfunction corresponds to linear configurations, while the $n$ $=1$ to T-shaped configurations. To our knowledge there is no experimental information available for the $D_{0}$ value of $\mathrm{Ar}-\mathrm{Br}_{2}$ complex. On the other hand, the previous ab initio calculations ${ }^{16}$ underestimate considerably the binding energy
of $\mathrm{Ar}-\mathrm{Br}_{2}$ (see Table IV). Therefore, we can only make a comparison with an available semiempirical estimate ${ }^{16}$ based on a scaled DIM model (see Table IV).

## IV. CONCLUSIONS

We have presented results of $a b$ initio calculations for the interaction of $\mathrm{Rg}=\mathrm{He}, \mathrm{Ne}, \mathrm{Ar}$, with $\mathrm{Br}_{2}$ molecule using $\operatorname{CCSD}(\mathrm{T})$ approach. The (aug-cc-pVnZ, $\mathrm{n}=\mathrm{Q}, 5$ ) $+(3 s 3 p 2 d 2 f 1 g)$ basis sets have been employed for the rare gas atoms and the SDD effective core potential basis sets supplemented with diffusion and polarization functions $[\mathrm{SDD}+\mathrm{G}(3 d f)]$ for the Br atoms. The $\operatorname{CCSD}(\mathrm{T})$ calculations, the most accurate to date for all the $\mathrm{Rg}-\mathrm{Br}_{2}$ ( Rg $=\mathrm{He}, \mathrm{Ne}, \mathrm{Ar})$ molecules, are in good accord with available experimental data. High quality basis sets and correlation treatments are essential for obtaining an accurate description of van der Waals complexes. As in all previous ab initio studies, each surface has a double minimum topology with linear and T-shaped isomers. The $\operatorname{CCSD}(\mathrm{T})$ interaction energies for the linear configurations are found to be lower than the T-shaped ones for all the $\mathrm{Rg}-\mathrm{Br}_{2}$ complexes studied.

Zero-point vibrational energy corrections are found to be very important in the stability of the linear and T-shaped isomers. The most interesting appears to be the case of $\mathrm{He}-\mathrm{Br}_{2}$ for which the ground vibrational state is found to correspond mainly to T-shaped structure, whereas the first vibrational state corresponds to the linear configuration and is only $0.4 \mathrm{~cm}^{-1}$ higher than the ground one. For $\mathrm{Ne}-\mathrm{Br}_{2}$ and $\mathrm{Ar}-\mathrm{Br}_{2}$ the zero-point vibrational effects are less important and does not reverse the ordering of the two minima. For $\mathrm{He}-\mathrm{Br}_{2}$ and $\mathrm{Ne}-\mathrm{Br}_{2}$, molecules the geometries and their binding energies predicted by the $\operatorname{CCSD}(\mathrm{T})$ calculations are in excellent agreement with experimental estimates. ${ }^{12,13,32}$ For all the $\mathrm{Rg}-\mathrm{Br}_{2}$ complexes, the present results are more reliable than the best available ones. Work is in progress for constructing three-dimensional potential energy surfaces for these complexes to study their dynamics and spectra. Preliminary results ${ }^{35}$ on the $B \leftarrow X$ excitation spectrum of $\mathrm{HeBr}_{2}$ show that the double minimum surface presented here for the ground $(X)$ state describes very well the experimental spectrum of the $\mathrm{HeBr}_{2}$ complex, ${ }^{12}$ indicating that for the $\mathrm{HeBr}_{2}$ the two structures are likely very close in energy and therefore, both of them can be determined by the experiment.

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