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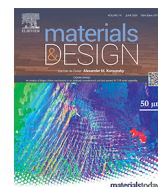
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# Understanding ordered structure in hematite nanowhiskers synthesized via thermal oxidation of iron-based substrates

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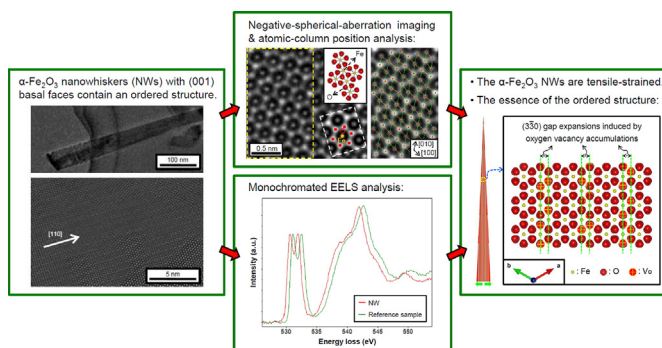
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## HIGHLIGHTS

- $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> nanowhiskers (NWs) with (001) basal faces synthesized via thermal oxidation of iron-based substrates are strained.
- The ordered structure in the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> (NWs) is periodic interplanar gap expansions induced by oxygen vacancy accumulations.
- The ordered structure forms to accommodate tensile strain.
- Integrating negative-spherical-aberration imaging and monochromated EELS is effective in analyzing strained metal oxides.

## GRAPHICAL ABSTRACT



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## ABSTRACT

Hematite ( $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>) nanowhiskers (NWs) with (001) basal faces synthesized via thermal oxidation of iron-based substrates are known to contain an ordered structure. The ordered structure has been identified to be related to oxygen vacancy ordering. However, the cause of its formation remains a mystery. In this study, with a high-resolution transmission electron microscopy (HR-TEM) investigation based on negative-Cs imaging (NCSI) and atomic-column position analysis, we observed tensile strain in the above-mentioned  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NWs and revealed that the ordered structure was actually periodic interplanar gap expansions induced by oxygen vacancy accumulations. These findings were further confirmed in a monochromated electron energy loss spectroscopy (EELS) analysis of the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NWs. The EELS data indicated that, in comparison to pristine  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>, the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NWs possessed expanded average Fe—O and O—O interatomic distances and were oxygen-deficient. Clarifying oxygen deficiency in the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NWs was not attributed to an insufficient oxygen supply during the NW growth, we concluded the ordered structure formed to accommodate tensile strain in the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NWs. This work demonstrates the applicability of integrating NCSI and monochromated EELS for the examination of strain-induced microstructural and microchemical variations in lightly strained metal oxides.

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## 1. Introduction

One-dimensional hematite ( $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>) nanostructures have recently attracted intense research interest because they are promising photoanode materials for photoelectrochemical water splitting. Constructing  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> photoanodes with arrayed one-dimensional  $\alpha$ -

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Fe<sub>2</sub>O<sub>3</sub> nanostructures removes the performance limitation imposed by the inherently short hole diffusion length of α-Fe<sub>2</sub>O<sub>3</sub> and can improve the electron collection efficiency [1]. Large-area synthesis of arrayed α-Fe<sub>2</sub>O<sub>3</sub> nanowhiskers (NWs) can be simply and economically realized through thermal oxidation of an iron-based substrate [2–4]. In the situation the oxidation temperature is below 570 °C, an iron oxide scale composed of a magnetite (Fe<sub>3</sub>O<sub>4</sub>) layer and an α-Fe<sub>2</sub>O<sub>3</sub> layer is expected to initially form on the iron-based substrate. The interfacial stress between these two scale layers then becomes a driving force that pumps iron atoms toward the outmost surface, thereby governing the growth of α-Fe<sub>2</sub>O<sub>3</sub> NWs [5].

In microstructural studies of α-Fe<sub>2</sub>O<sub>3</sub> NWs synthesized via the thermal oxidation route, researchers have typically observed superstructure modulation in high-resolution transmission electron microscopy (HR-TEM) images of NWs with (001) basal faces. The superstructure modulation indicates the presence of an ordered structure in the NWs, which has long been regarded as ordered oxygen-deficient planes [3,6,7]. A small number of oxygen vacancies in an α-Fe<sub>2</sub>O<sub>3</sub> photoanode is indicative of a higher majority carrier density for the photoanode [8,9]. Thus, the reverse flow of electrons from the photoanode inside toward the semiconductor-liquid junction is restrained during photoelectrochemical reactions [10]. On the basis of this interpretation, the ordered structure is thought to improve the photoelectrochemical performance of the host α-Fe<sub>2</sub>O<sub>3</sub> NWs. It is a long-standing aspiration for understanding the formation of the ordered structure. Chen et al. claimed the ordered oxygen vacancy planes in α-Fe<sub>2</sub>O<sub>3</sub> NWs synthesized via a plasma oxidation process formed to relax stress originating from the lattice mismatch between α-Fe<sub>2</sub>O<sub>3</sub> and Fe [11]. However, as they did not anticipate the formation of a multilayered iron oxide scale, their argument does not explain the analogous phenomenon observed in α-Fe<sub>2</sub>O<sub>3</sub> NWs synthesized via thermal oxidation of iron-based substrates. According to our own literature survey, no convincing explanation for the formation of the ordered structure has been reported.

For transition metal oxides whose metal cations can adapt to multiple oxidation states, the oxygen vacancy formation energy is reduced by the introduction of tensile strain which to some degree relieves the electron–electron electrostatic repulsion along the broken bonds [12]. In view of the fact that the growth of α-Fe<sub>2</sub>O<sub>3</sub> NWs synthesized via the thermal oxidation route is governed by the interfacial stress between the layers of the iron oxide scale, it is reasonable to deduce the emergence of the ordered structure is related to strain. Because the lattice framework of α-Fe<sub>2</sub>O<sub>3</sub> is comprised of oxygen anions, analytical methods that can provide information about the spatial arrangement of oxygen atoms are highly demanded for proving this deduction. Following the development of spherical-aberration (Cs) correction for TEM, HR-TEM analysis based on negative-Cs imaging (NCSI) is now available. It is recognized as a powerful technique for imaging low-atomic-number elements, such as oxygen and nitrogen [13–16]. Herein, we report the first NCSI-based HR-TEM observation of α-Fe<sub>2</sub>O<sub>3</sub> NWs with (001) basal faces synthesized via the thermal oxidation route. By performing a positional analysis of the detected oxygen columns, we revealed the essence and formation reason of the ordered structure within the α-Fe<sub>2</sub>O<sub>3</sub> NWs. The findings of the HR-TEM investigation were further confirmed in a monochromated electron energy loss spectroscopy (EELS) analysis of the α-Fe<sub>2</sub>O<sub>3</sub> NWs. This work demonstrates that the integration of NCSI and monochromated EELS is an effective means by which to analyze strain-induced microstructural and microchemical variations in lightly strained metal oxides.

## 2. Experimental details

The α-Fe<sub>2</sub>O<sub>3</sub> NWs investigated in the present study were grown on an ultrasonically cleaned 45 Permalloy sheet (The Nilaco Corp.) by atmospheric thermal oxidation at 550 °C for 20 h. The morphology of the as-synthesized α-Fe<sub>2</sub>O<sub>3</sub> NWs (Fig. S1) is similar to that of α-Fe<sub>2</sub>O<sub>3</sub>

NWs synthesized via thermal oxidation of iron foils in a 200 Torr pure oxygen atmosphere [5]. HR-TEM and EELS were performed with a monochromator-equipped double-Cs-corrector transmission/scanning transmission electron microscope (TEM/STEM) (JEM-ARM200F, JEOL Ltd.) operated at an acceleration voltage of 200 kV. The Cs value for HR-TEM imaging was set to −14 μm. EELS acquisitions of the O K-edge and Fe L<sub>2,3</sub>-edge were performed with the scanning transmission electron microscopy (STEM)-EELS method under the dual-EELS mode [17], for which the spectrometer (GIF Quantum ERS, Gatan Inc.) was focused on the zero-loss peak (ZLP); the convergence and collection semi-angles were 32.3 and 28.2 mrad, respectively, and the energy dispersion was 0.05 eV/channel. Each resultant EELS spectrum was obtained from a summation of 10,000 spectra according to a 100 × 100 EELS spectrum image (Fig. S2). The ZLP full-width-at-half-maximum (FWHM) values for acquiring the O K-edge spectra and Fe L<sub>2,3</sub>-edge spectra were 0.25 and 0.2 eV, respectively (Fig. S3). HR-TEM image simulations were carried out with the xHREM program (HREM Research Inc.). The positional analysis of the detected atomic columns was performed using the PPA DigitalMicrograph plug-in (HREM Research Inc.).

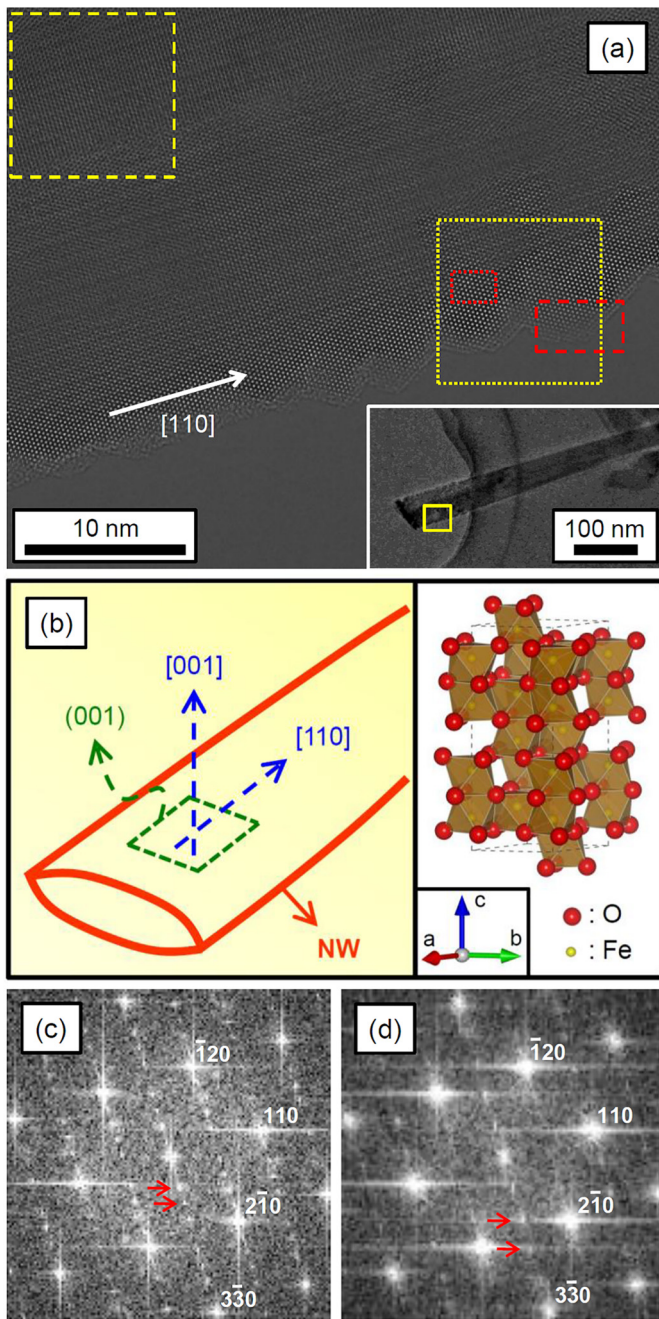
## 3. Results and discussion

A HR-TEM image of an as-synthesized α-Fe<sub>2</sub>O<sub>3</sub> NW with (001) basal faces is shown in Fig. 1a, in which there is clear superstructure modulation. The relation between the geometric shape and the crystallographic orientation of the α-Fe<sub>2</sub>O<sub>3</sub> NW is illustrated in Fig. 1b. According to the fast-Fourier-transform (FFT) patterns of the marked areas in Fig. 1a (Fig. 1c and d), the superstructure modulation period is five times the interplanar spacing of the (3 $\bar{3}$ 0) planes at the NW edge, yet it becomes twice of that at the inner part. Both of these modulation periods have been reported previously with the ordered structure was regarded as ordered oxygen-deficient planes [3,6]. However, this is the first report of their combined presence in a single α-Fe<sub>2</sub>O<sub>3</sub> NW. Our finding suggests the period of the ordered structure is determined by the local structural or geometric characteristics of the NW. Because the NW edge and the NW bulk were found predominantly different in thickness, we considered this factor determined the period of the ordered structure.

The HR-TEM image in Fig. 1a was acquired with a relatively large overfocus setting to make the superstructure modulation more visible. However, the excessive overfocus led to a drawback that the oxygen columns were unable to be visualized. To ascertain the microstructural essence of the superstructure modulation, we adjusted the overfocus to ~6 nm to satisfy the NCSI criterion (Fig. S4). A bright-atomic-contrast HR-TEM image of the area enclosed within the red dotted box in Fig. 1a is shown in Fig. 2a. A simulated HR-TEM image of an ideal α-Fe<sub>2</sub>O<sub>3</sub> lattice with a specimen thickness of 6.9 nm and an overfocus value of 6 nm is superimposed on this experimental image. The yellow arrows mark the positions corresponding to the dark stripes in the superstructure modulation in Fig. 1a. It is now clear that the crystallographic position of each dark stripe is at the interplanar gap between two adjacent (3 $\bar{3}$ 0) planes, which we designate as a (3 $\bar{3}$ 0) gap. With a careful examination of Fig. 2a, we noticed that the (3 $\bar{3}$ 0) gaps corresponding to the dark stripes were also darker than their nearby ones, which was mainly due to lower image intensity of many of the areas each between two neighboring oxygen columns laying to either side of a dark stripe (Fig. S5). This finding implies a number of the oxygen columns flanking the dark stripes are lower in column occupancy or considerably displace from the neutral positions.

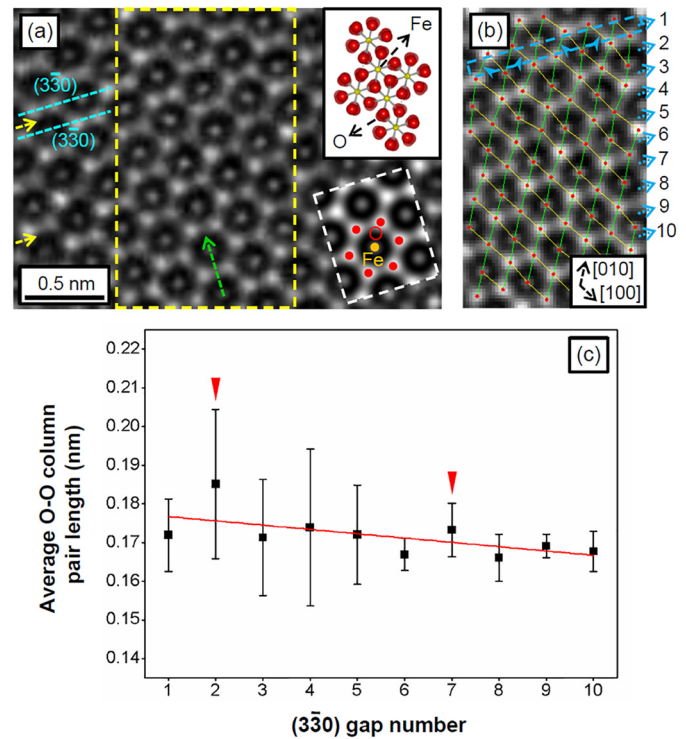
Using the peak pairs analysis algorithm [18], we extracted the positions of the atomic-columns enclosed within the yellow dashed box in Fig. 2a and constructed a set of O—O and Fe—O column pairs whose base vectors are parallel to the [100] and [010] directions (Fig. 2b). It can be observed that the lengths of these atomic-column pairs and the angles between joint atomic-column pairs become increasingly





**Fig. 1.** (a) HR-TEM image of an as-synthesized  $\alpha$ - $\text{Fe}_2\text{O}_3$  NW with (001) basal faces. The boxed region in the inset TEM image shows the location of HR-TEM observation. (b) Relation between the geometric shape and the crystallographic orientation of the  $\alpha$ - $\text{Fe}_2\text{O}_3$  NW. At right is shown the crystallographic unit cell of  $\alpha$ - $\text{Fe}_2\text{O}_3$ . (c) and (d) FFT patterns of the areas respectively enclosed within the yellow dashed and yellow dotted boxes in (a). The repetitions of the extra spots are indicated by the red arrows.

irregular as the local thickness of the NW increases. This indicates the presence of thickness-dependent distortion in the  $\alpha$ - $\text{Fe}_2\text{O}_3$  NW lattice. The atomic-column pair set was further divided into ten segments (the upper and lower edges were excluded) each corresponded to a numbered  $(\bar{3}\bar{3}0)$  gap in Fig. 2b. Estimating the average O—O column pair length for each numbered  $(\bar{3}\bar{3}0)$  gap (Fig. 2c), we observed a trend that the average O—O column pair length for a  $(\bar{3}\bar{3}0)$  gap increased with the local NW thickness became thicker. Therefore, the thickness-dependent lattice distortion should be a reflection of the presence of thickness-dependent tensile strain in the  $\alpha$ - $\text{Fe}_2\text{O}_3$  NW. Another noteworthy point in Fig. 2c is that the average O—O column pair



**Fig. 2.** (a) Bright-atomic-contrast HR-TEM image of the area enclosed within the red dotted box in Fig. 1a. The positions corresponding to the dark stripes are indicated by the yellow arrows. The green arrow indicates the direction of thickness increase. The upper inset shows the structural model of the  $\alpha$ - $\text{Fe}_2\text{O}_3$  unit cell in the [001] direction. The lower inset is the simulated HR-TEM image. (b) Atomic-column position analysis of the region enclosed within the yellow dashed box in (a). Column pairs with the base vector parallel to the [100] direction are marked by the yellow lines, and column pairs with the base vector parallel to the [010] direction by the green lines. (c) Average O—O column pair lengths for the numbered  $(\bar{3}\bar{3}0)$  gaps in (b). The linear fit of the data is indicated by the red line. The red arrows indicate the  $(\bar{3}\bar{3}0)$  gaps corresponding to the dark stripes. In (b), the dashed box encloses  $(\bar{3}\bar{3}0)$  gap 1, and the blue arrows indicate the O—O column pairs astride this  $(\bar{3}\bar{3}0)$  gap.

lengths for  $(\bar{3}\bar{3}0)$  gaps corresponding to the dark stripes (i.e.,  $(\bar{3}\bar{3}0)$  gaps 2 and 7) display apparent positive quantity deviations from the fitted data trend. This explains why these two  $(\bar{3}\bar{3}0)$  gaps are relatively darker. More specifically, this indicates that the dark stripes are related to  $(\bar{3}\bar{3}0)$  gap expansions.

Carrying out a close inspection to  $(\bar{3}\bar{3}0)$  gap 2 in Fig. 2b, we found the configuration of the oxygen columns flanking this defect-associated  $(\bar{3}\bar{3}0)$  gap exhibited a non-negligible deviation from the ideal condition; also, the column displacements were found lacking uniformity in terms of quantity and vector (Fig. S6). Such a situation implies the ordered dark stripes cannot be simply attributed to pure lattice modulation like the case in a strained  $\text{LaCoO}_3$  film [19]. It is known, for tensile-strained transition metal oxides, chemical expansion arising from oxygen vacancy formation provides an alternative way in contrast to shear lattice distortion to accommodate tensile strain [20], for which a situation that oxygen vacancies distribute orderly has also been reported [21,22]. On the basis of our microstructural observation result, it is possible that the dark stripes result from ordered oxygen vacancy formation. In truth, using low-angle annular dark-field (LAADF)-STEM, Lee et al. have found oxygen vacancy ordering in  $\alpha$ - $\text{Fe}_2\text{O}_3$  NWs synthesized via thermal oxidation of a  $\text{Fe}_{64}\text{Ni}_{36}$  substrate [6]. It should be noted that an individual oxygen column in the (001) planes of  $\alpha$ - $\text{Fe}_2\text{O}_3$  actually consists of three sub-columns whose centers are slightly apart from each other; this is illustrated in the upper inset of Fig. 2a. Therefore, once there is an uneven oxygen vacancy accumulation in the sub-columns, the projected potential center of this oxygen column

will shift from its neutral position. This mechanism and the accompanying chemical expansion make a reasonable explanation to the irregular displacements of the oxygen columns flanking the dark stripes, because the conditions of oxygen vacancy accumulation for these oxygen columns can be different from each other. Another point worth to mention is that, in the view of our argument, the dark stripes (i.e., the expanded  $(\bar{3}\bar{3}0)$  gaps) must result in width reductions of their neighboring  $(\bar{3}\bar{3}0)$  gaps. Therefore, in Fig. 2c, the relative reductions of the average O—O column pair lengths for  $(\bar{3}\bar{3}0)$  gaps 1, 3, 6, and 8 also suggest the ordered dark stripes are periodic  $(\bar{3}\bar{3}0)$  gap expansions induced by oxygen vacancy accumulations. We should emphasize that our HR-TEM investigation delivers a new interpretation of the ordered structure different from that suggested in the previous studies, in which the ordered structure is considered to be oxygen-deficient  $(\bar{3}\bar{3}0)$  planes periodically distributing in every five or ten times the interplanar spacing of the  $(\bar{3}\bar{3}0)$  planes [3,6,7]. Since Cs-uncorrected HR-TEM was employed in the previous studies, they were unable to detect the oxygen columns in the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NWs, which prevented them from obtaining precise structural information of the ordered structure.

Because no apparent dark stripes were observed at the very edge of the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NW in Fig. 1a, the situation of atomic-column arrangement in this region can be valuable information compared with the analysis results shown in Fig. 2. The bright-atomic-contrast HR-TEM image of the area within the red dashed box in Fig. 1a is shown in Fig. 3a, where the atomic-column configuration is fairly regular. Atomic-

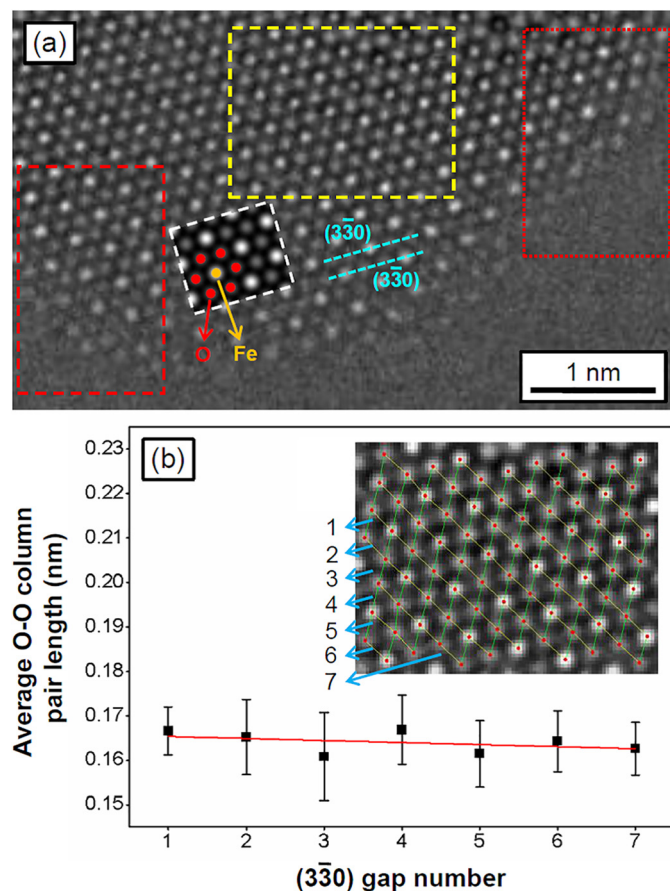


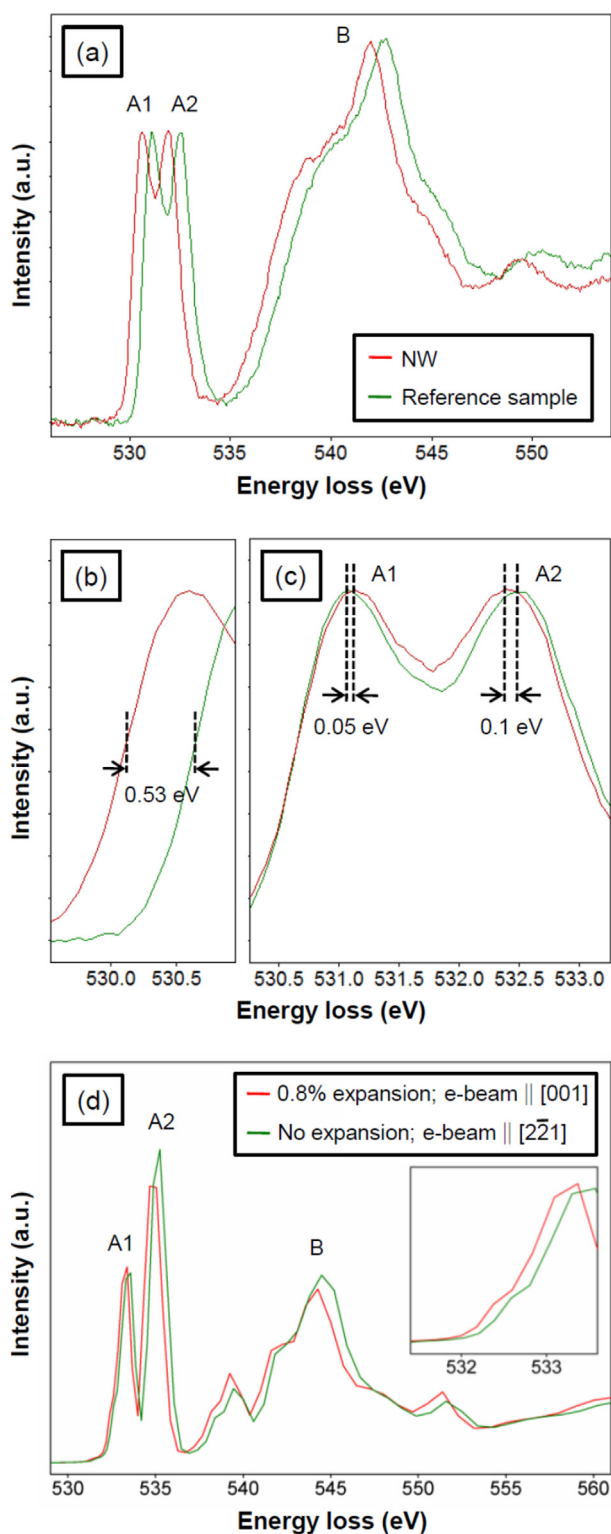
Fig. 3. (a) Bright-atomic-contrast HR-TEM image of the area enclosed in the red dashed box in Fig. 1a. The inset shows a simulated HR-TEM image with a specimen thickness of 1.37 nm and an overfocus value of 6 nm. (b) Average O—O column pair lengths for the numbered  $(\bar{3}\bar{3}0)$  gaps indicated in the inset atomic-column position analysis result that obtained in the region enclosed within the yellow dashed box in (a). The linear fit of the data is indicated by the red line.

column position analysis was performed on the area enclosed within the yellow dashed box in Fig. 3a, and the related results are shown in Fig. 3b. It can be observed that at this very edge area, there is still a weak positive dependence between the average O—O column pair length for a  $(\bar{3}\bar{3}0)$  gap and the local NW thickness. The standard deviation values for the data points in Fig. 3b are in the range between 5.3 and 9.9 pm. A comparable result was reported by Gauquelin et al. [23]; in their study, the precision of NCSI on the position determination of oxygen columns in bulk-like NdGaO<sub>3</sub> was measured to be 12.97 pm and was predominantly limited by image distortions. The small standard deviation values in Fig. 3b indicate the sample drift, environmental interference, and aberration parameters fluctuation were effectively suppressed in our HR-TEM observation. If the minute amount of tensile strain and surface relaxation at the very edge of the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NW, which to some degree deteriorate the regularity of the atomic-column arrangement, are overlooked, the precision of our NCSI-based atomic-column position analysis is considered to be better than 10 pm. Therefore, in Fig. 2c, the relatively large standard deviation values for the data points corresponding to  $(\bar{3}\bar{3}0)$  gaps 1 to 5 are indeed due to more severe local lattice distortion at the thicker region. To sum up, thickness-dependent tensile strain is present in the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NW, for which the strain accommodation is realized by lattice distortion and periodic  $(\bar{3}\bar{3}0)$  gap expansions suggested to be induced by oxygen vacancy accumulations.

A monochromated EELS analysis was performed to examine inter-atomic distances and evaluate oxygen deficiency in the studied  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NWs. The O K-edge EELS spectra of an as-synthesized  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NW with (001) basal faces and a stoichiometric  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> reference sample (commercial  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> powder, purchased from Sigma-Aldrich Inc., had been annealed at 500 °C in air for 20 h) are shown in Fig. 4a. The spectra have been normalized to the maximum of peak A1. The sample orientations for the EELS experiment were confirmed to be that the incident electron beam was nearly parallel to the [001] direction of the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NW and the  $[\bar{2}\bar{2}1]$  direction of the reference sample. Normally, the onset of an O K-edge core-excitation spectrum of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> is considered to be at the first inflection point in the spectrum and is linked with the conduction band minimum (CBM) of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> [24]. Considering the initial rise of the NW O K-edge EELS spectrum might include signal contributions associated with the shallow intra-bandgap defect states arising from the presence of oxygen vacancies [25], we thus determined the onsets of the O K-edge EELS spectra using the signal intensity at the first inflection point in the O K-edge EELS spectrum of the reference sample (Fig. 4b). This substantially ensures the onset of the NW O K-edge EELS spectrum represents the intrinsic CBM of the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> NW.

Peaks A1 and A2 in the O K-edge EELS spectra are known as pre-peaks and are respectively related to the  $t_{2g}$  and  $e_g$  bands of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> [26]. Horizontally aligning the onsets of the O K-edge EELS spectra (Fig. 4c), we observed that the NW spectrum revealed a  $\sim 0.05$ -eV relative right shift at peak A1 and a  $\sim 0.1$ -eV relative left shift at peak A2. Because the  $(\text{FeO}_6)^{9-}$  octahedral units in  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> are actually trigonally distorted from octahedral symmetry, in a crystal-field-based scenario, the  $t_{2g}$  band is further split into two sub-bands designated as  $a_{1g}$  and  $e_g(\pi)$ . The electronic orbitals of the  $a_{1g}$  sub-band lie parallel to the c-axis of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>, while the orbitals of the  $e_g(\pi)$  sub-band perpendicular to it [27,28]. This fact makes the position of peak A1 to be associated with the sample orientation (for normal STEM-EELS, where the collection semi-angle is significantly larger than the O K-edge characteristic angle, the overall electron momentum transfer is predominantly along directions perpendicular to the incident electron beam). According to our EELS experiment condition, the c-axis momentum transfer for the incident electrons takes a smaller signal contribution weight in the NW O K-edge EELS spectrum than in the O K-edge EELS spectrum of the reference sample. Therefore, it is possible that peak A1 in the NW O K-edge EELS spectrum is centered closer to the position corresponding to the  $e_g(\pi)$  sub-band and so slightly further from the onset. Because the trigonal distortion of the  $(\text{FeO}_6)^{9-}$  octahedral units does not cause a





**Fig. 4.** (a) O K-edge EELS spectra of an as-synthesized  $\alpha\text{-Fe}_2\text{O}_3$  NW with (001) basal faces and a stoichiometric  $\alpha\text{-Fe}_2\text{O}_3$  reference sample. (b) Signal threshold regions in the spectra in (a). The dashed lines mark the determined onset positions. (c) Pre-peak regions in the spectra in (a); the NW spectrum has been shifted horizontally from its original position to compensate for the difference in the onset energy. (d) Simulated O K-edge EELS spectra of  $\alpha\text{-Fe}_2\text{O}_3$  with and without 0.8% lattice expansion. The inset shows the enlarged image of the spectrum onset regions in the simulated spectra.

substantial split of the  $e_g$  band [29], the position of peak A2 is independent of the sample orientation. Hence, the observed relative shift at peak A2 indicates the difference in energy between the  $e_g$  band and

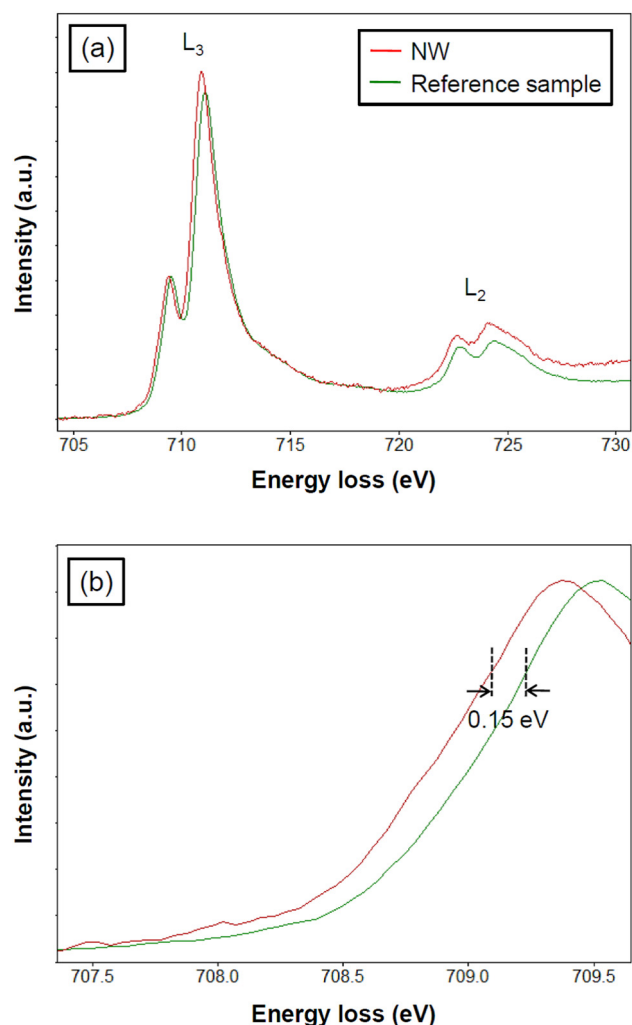
the CBM for the  $\alpha\text{-Fe}_2\text{O}_3$  NW is smaller than that for pristine  $\alpha\text{-Fe}_2\text{O}_3$ . Since, for the energy band structure of  $\alpha\text{-Fe}_2\text{O}_3$ , the CBM is equivalent to the bottom edge of the  $t_{2g}$  band, this finding indicates that the  $\alpha\text{-Fe}_2\text{O}_3$  NW exhibits a diminished octahedral ligand field splitting. Essentially, this can be attributed to reduced Fe 3d-O 2p orbital hybridization [26] and so means the average Fe—O interatomic distance in the  $\alpha\text{-Fe}_2\text{O}_3$  NW is larger [30].

According to the real-space multiple-scattering theory, forming the main peak (i.e., peak B in Fig. 4a) in an O K-edge core-excitation spectrum of  $\alpha\text{-Fe}_2\text{O}_3$  is a result of scattering resonances each govern by the first oxygen shell around an excited oxygen anion [31]. If the spectrum onset is defined as the energy level of zero kinetic energy for the ejected core electrons, the difference in energy between the main peak and the spectrum onset should retain the relation in Eq. (1) when the  $\alpha\text{-Fe}_2\text{O}_3$  lattice is slightly distorted [31].

$$\Delta E \times R^2 = \text{constant} \quad (1)$$

where  $\Delta E$  is the energy difference, and  $R$  represents the average radius of the first oxygen shell. The values of  $\Delta E$  in the O K-edge EELS spectra of the NW and reference sample were measured to be 11.8 and 12.0 eV, respectively. This means that the average O—O interatomic distance in the  $\alpha\text{-Fe}_2\text{O}_3$  NW is 0.8% longer than in pristine  $\alpha\text{-Fe}_2\text{O}_3$ . Because the lattice framework of  $\alpha\text{-Fe}_2\text{O}_3$  is comprised of oxygen anions, this further suggests the lattice of the  $\alpha\text{-Fe}_2\text{O}_3$  NW is expanded relative to that of pristine  $\alpha\text{-Fe}_2\text{O}_3$ . Another indication of the presence of lattice expansion in the  $\alpha\text{-Fe}_2\text{O}_3$  NW is the energy shift between the O K-edge EELS spectrum onsets (measured to be 0.53 eV). Since the ionicity of  $\alpha\text{-Fe}_2\text{O}_3$  is high [32], the energy of the O 1s core electrons in  $\alpha\text{-Fe}_2\text{O}_3$  should be sensitive to variations in the average Fe—O interatomic distance [33]. More specifically, it is believed an expansion in the  $\alpha\text{-Fe}_2\text{O}_3$  lattice parameters, which corresponds to an increase in the average Fe—O interatomic distance in  $\alpha\text{-Fe}_2\text{O}_3$ , will cause a greater increase in the O 1s electron energy and a smaller decrease in the CBM energy, thereby leading to a downshift in the O K-edge onset. To verify this, we have simulated the O K-edge EELS spectra of  $\alpha\text{-Fe}_2\text{O}_3$  with and without 0.8% lattice expansion (see supplementary information for the detail). The simulation results in Fig. 4d clearly indicate that lattice expansion results in a downfield shift in the O K-edge onset of  $\alpha\text{-Fe}_2\text{O}_3$ . Note that the onset shift in the simulated spectra ( $\sim 0.15$  eV) is smaller than in the experimental spectra. A possible reason accounting for this is that only uniform lattice expansion was considered in simulating the O K-edge EELS spectrum of lattice-expanded  $\alpha\text{-Fe}_2\text{O}_3$ .

Through an EELS-based stoichiometric comparison between an as-synthesized  $\alpha\text{-Fe}_2\text{O}_3$  NW with (001) basal faces and the reference sample (Fig. S7), we verified the synthesized  $\alpha\text{-Fe}_2\text{O}_3$  NWs with (001) basal faces were oxygen-deficient. However, since the difference in specimen thickness might introduce uncertainty into the stoichiometric comparison, examining whether a chemical shift [34] is present at the Fe  $L_{2,3}$ -edge core excitation of the  $\alpha\text{-Fe}_2\text{O}_3$  NWs helps reconfirm the oxygen deficiency in them, for which monochromated dual-EELS is an effective practical approach. The Fe  $L_{2,3}$ -edge EELS spectra of an as-synthesized  $\alpha\text{-Fe}_2\text{O}_3$  NW with (001) basal faces and the reference sample are shown in Fig. 5a. The two spectra have been normalized to the maximum of the first  $L_3$ -edge peak, and their onsets were determined with the same procedure used to determine the onsets of the O K-edge EELS spectra. It was found that the onset of the Fe  $L_{2,3}$ -edge EELS spectrum of the NW is  $\sim 0.15$  eV lower than that of the reference sample (Fig. 5b). Because the comparison benchmark was the spectrum onset, the near-edge fine structure variation associated with the lattice distortion and sample orientation difference was not a crucial factor affecting our edge shift determination. Therefore, the measured energy shift should be substantially attributed to a combination of the energy variations of the Fe  $2p_{3/2}$  core electrons and the CBM (for  $\alpha\text{-Fe}_2\text{O}_3$ , the Fe  $L_{2,3}$ -edge onset is also linked with the CBM). In light of the high ionicity of  $\alpha\text{-Fe}_2\text{O}_3$ , just like the aforesaid O K-edge situation, the energy of the Fe

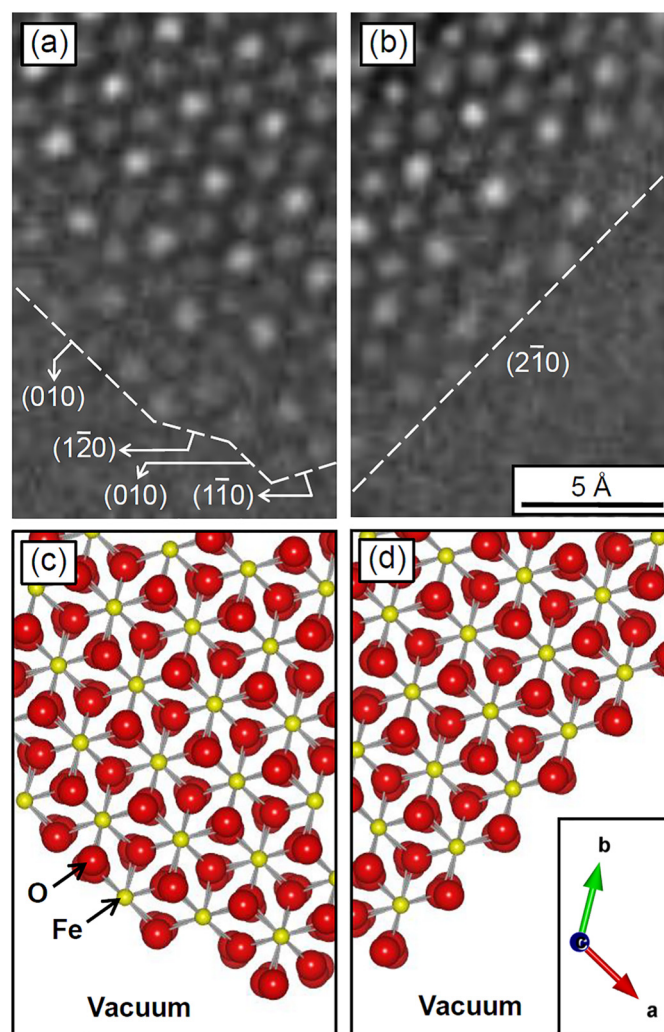


**Fig. 5.** (a) Fe  $L_{2,3}$ -edge EELS spectra of an as-synthesized  $\alpha$ - $\text{Fe}_2\text{O}_3$  NW with (001) basal faces and the reference sample. (b) Signal threshold regions in the spectra in (a). The dashed lines mark the onset positions.

$2p_{3/2}$  core electrons is more sensitive to lattice expansion than the CBM energy does. This implies the tensile strain in the  $\alpha$ - $\text{Fe}_2\text{O}_3$  NW will cause its Fe  $L_{2,3}$ -edge onset higher in energy than that of pristine  $\alpha$ - $\text{Fe}_2\text{O}_3$ . Therefore, ruling out the strain-related factor, we believe the energy shift between the Fe  $L_{2,3}$ -edge EELS spectrum onsets is essentially a chemical shift which indicates the iron cations in the  $\alpha$ - $\text{Fe}_2\text{O}_3$  NW are reduced.

In the present study, we adopted an atmospheric thermal oxidation process to synthesize  $\alpha$ - $\text{Fe}_2\text{O}_3$  NWs. Hence, oxygen deficiency in the studied  $\alpha$ - $\text{Fe}_2\text{O}_3$  NWs is not likely caused by an insufficient oxygen supply during the NW growth. Further evidence of this was obtained by inspecting the edge surface termination of the  $\alpha$ - $\text{Fe}_2\text{O}_3$  NWs. As representative examples, the enlarged images and corresponding structural models of the areas within the red dashed and red dotted boxes in Fig. 3a are shown in Fig. 6. It can be observed that the NW edge terminates with either the (110)-type or (100)-type facets. More importantly, the surface atom configurations at the NW edge are consistent with the stoichiometric predictions [35], meaning the  $\alpha$ - $\text{Fe}_2\text{O}_3$  NWs indeed grew with a sufficient oxygen supply. This fact strongly indicates that the emergence of oxygen vacancies in  $\alpha$ - $\text{Fe}_2\text{O}_3$  NWs with (001) basal faces synthesized via thermal oxidation of iron-based substrates is a consequence of tensile strain.

For the sequential oxide formation in synthesizing  $\alpha$ - $\text{Fe}_2\text{O}_3$  NWs via the thermal oxidation route [5], the topoaxial relation between the  $\alpha$ - $\text{Fe}_2\text{O}_3$  scale layer and the  $\text{Fe}_3\text{O}_4$  scale layer has been verified to be  $\alpha$ -



**Fig. 6.** Enlarged images of the areas within the red dashed box (a) and the red dotted box (b) in Fig. 3a. (c) and (d) Structural models respectively correspond to (a) and (b).

$\text{Fe}_2\text{O}_3$  [001]|| $\text{Fe}_3\text{O}_4$  [111] [36]. That is to say, the two phases joint on the basis of either superposing or coupling of the close-packed oxygen planes. The average interatomic distance between adjacent oxygen anions in a close-packed oxygen plane of  $\text{Fe}_3\text{O}_4$  is approximately 2% larger than that of  $\alpha$ - $\text{Fe}_2\text{O}_3$ . This means the underlying  $\text{Fe}_3\text{O}_4$  scale layer generates tensile stress in the  $\alpha$ - $\text{Fe}_2\text{O}_3$  scale layer. Because the tensile stress within the thin dense  $\alpha$ - $\text{Fe}_2\text{O}_3$  scale layer is not effectively relaxed, it then causes tensile strain in the  $\alpha$ - $\text{Fe}_2\text{O}_3$  NWs forming above the  $\alpha$ - $\text{Fe}_2\text{O}_3$  scale layer. It is now known that, of the growing  $\alpha$ - $\text{Fe}_2\text{O}_3$  NWs, those with (001) basal faces exhibit a strain accommodation pattern composed of lattice distortion and periodic  $(3\bar{3}0)$  gap expansions induced by oxygen vacancy accumulations (Fig. 7). The emergence of the induced  $(3\bar{3}0)$  gap expansions is reasonable from a thermodynamic perspective, because forming oxygen vacancies offers an effective route to reduce the strain energy; also, the interaction energy of oxygen vacancies is reduced through aggregation, which has been pointed out by Ong et al. in a study of  $\text{SrCrO}_{3-\delta}$  [37]. Owing to the effects of strain field and charge repulsion, the induced  $(3\bar{3}0)$  gap expansions repel one another. Their distribution period within a local range is expected to be governed by the repulsive forces between them. A similar phenomenon is seen in  $\text{SrCrO}_{3-\delta}$ , in which repulsion between the oxygen-deficient planes results in an ordering arrangement [37]. Since the degree of local strain in the  $\alpha$ - $\text{Fe}_2\text{O}_3$  NWs with (001) basal faces is thickness-dependent, the strain/electrical fields of the induced  $(3\bar{3}0)$  gap expansions are related to the local NW thickness. This means that

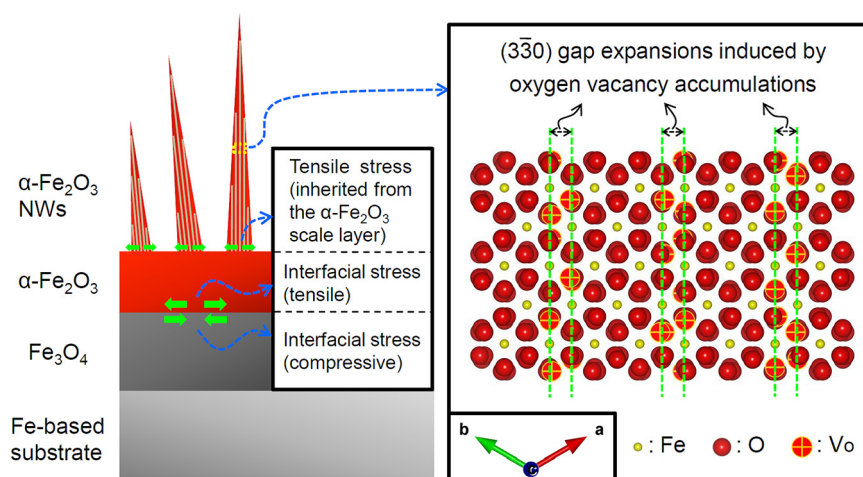


Fig. 7. Formation mechanism of the periodic  $(3\bar{3}0)$  gap expansions induced by oxygen vacancy accumulations. Vo stands for oxygen vacancy.

different defect periodicities can exist within a single  $\alpha\text{-Fe}_2\text{O}_3$  NW provided that the thickness of the NW edge and the NW bulk are sufficiently different.

As a technical advance in HR-TEM imaging, NCSI is an efficient and spatially precise technique [23] for investigating oxygen column displacements in strained metal oxides. Remedying the limitations of HR-TEM/STEM imaging, core-loss EELS is capable of analyzing the strain-induced microchemical variations in strained metal oxides. However, when the strain is minimal, feature changes in the EELS spectra are usually too subtle for typical EELS with a  $\sim 1$  eV FWHM energy resolution [38]. This limitation underscores the need to reduce the energy spread of the electron beam to the sub-eV level. Via this study, we have demonstrated the applicability of integrating NCSI and monochromated EELS for the analysis of strain-induced microstructural and microchemical variations in lightly strained metal oxides. It is believed this advanced technical integration can be an effective material characterization strategy for strain-based oxygen vacancy engineering [39,40].

#### 4. Conclusions

$\alpha\text{-Fe}_2\text{O}_3$  NWs with (001) basal faces were synthesized using an atmospheric thermal oxidation process. With NCSI and atomic-column position analysis, we observed thickness-dependent tensile strain in the  $\alpha\text{-Fe}_2\text{O}_3$  NWs and revealed that the ordered structure within the NWs was periodic  $(3\bar{3}0)$  gap expansions induced by oxygen vacancy accumulations. The HR-TEM investigation findings were further confirmed in the monochromated O K-edge and Fe  $L_{2,3}$ -edge EELS analysis. The O K-edge EELS result shows that the average Fe—O and O—O interatomic distances in the  $\alpha\text{-Fe}_2\text{O}_3$  NWs are larger than they are in pristine  $\alpha\text{-Fe}_2\text{O}_3$ . The Fe  $L_{2,3}$ -edge EELS result provides evidence of oxygen deficiency in the  $\alpha\text{-Fe}_2\text{O}_3$  NWs. The  $\alpha\text{-Fe}_2\text{O}_3$  NWs possess a stoichiometric surface termination, which indicates that the oxygen deficiency is not caused by an insufficient oxygen supply during the NW growth. Therefore, forming the ordered structure in the  $\alpha\text{-Fe}_2\text{O}_3$  NWs is a result of to create a thermodynamically preferred route for accommodating the tensile strain. With this work, we demonstrate the applicability of integrating NCSI and monochromated EELS for characterizing lightly strained metal oxides.

#### CRedit authorship contribution statement

**Ming-Wei Lai:** Conceptualization, Methodology, Investigation, Writing - original draft, Writing - review & editing. **Hiroki Kurata:** Conceptualization, Writing - original draft, Writing - review & editing, Supervision.

#### Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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#### Data availability statement

The data that support the findings of the present study are included within the article and its supplementary information. Other related data are available from the corresponding author upon request.

#### Appendix A. Supplementary information

Supplementary information to this article can be found online at <https://doi.org/10.1016/j.matdes.2020.108596>.

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