POPULATION SEQUENCING FROM CHROMATOGRAM DATA*

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One of the key components of sequencing technologies is proper separation of a single species/strain/allele of the targeted sequence from a sample. In traditional techniques, this has been achieved chemically (e.g., using specific primer sequences), however, multiple different but related species can still possibly be picked up with the same primer. This is especially problematic in sequencing RNA or proviral DNA, when the virus in question is highly variable and each individual is infected with a different swarm of viral strains. In case of HIV, for example, when the dominant sequences in the population differ by one or more insertions and deletions, the standard sequencing techniques fail to recover any of the components strains sufficiently well. We show that the chromatograms of mixed sequences can be used to accurately infer the individual strains, removing the need for additional sequencing steps, e.g. new primer synthesis or cloning of individual viral variants. To this purpose, we have developed a statistical generative model of raw chromatogram data and an appropriate inference algorithm based on maximizing the likelihood of an observed chromatogram. To illustrate this technique, we used an automated ABI 3730XL sequencer to capture mixed samples of pro-viral DNA of HIV-infected patients. The chromatograms of the mixed samples were analyzed by the presented algorithm, providing the inferred individual strains for each mixture as output. The mixture components were then compared with the sequences of the original clones. In many cases, the separated components had fewer than 1%differences to the ground truth which compares favorably to the output of the basic sequencer, whose errors went up to 40%.

1. Introduction

In immunology research, obtaining as complete as possible a population of viral strains by sequencing a single sample is highly desirable, but difficult

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due to drawbacks of current sequencing technology. Sequencing highly polymorphic organisms, such as viruses, is complicated by diversity present in a sample. Current Sanger sequencing typically provides only the readout of a single dominant strain in the mix with some detectable ambiguities corresponding to individual site polymorphisms. However, linking polymorphic variants at different sites and disambiguating complete multiple strains is not possible using standard software. Furthermore, signals from strains with very low concentrations is obliterated by more dominant strains.

The field of gene sequencing is at the crossroads. On the one hand, new techniques such as those proposed by 454 Life Sciences ¹, allow sequencing of a large number of short (up to about 100 nucleotides) subsequences, possibly allowing detection of segments of strains that are present in fairly low concentrations. On the other hand, assembly of short segments acquired this way into full strains is an area of active research, while the more traditional Sanger sequencing provides much longer readouts, but the problem of extraction of multiple strains from these signals is unsolved. It is possible that the combination of these two techniques will lead to best results. In this paper, we provide a new algorithm for analysis of chromatogram data that can help resolve the problem of disambiguating multiple strains from a single chromatogram signal, which on the one hand, makes Sanger technology more directly useful for population sequencing, and on the other provides a way for improving new generation of sequencing solutions, by providing a multi-strain skeleton for mapping short readouts.

Intermediate output of sequencing technologies (e.g., smoothed chromatograms obtained by ABI sequencers) can often appear to be of low quality when in fact it should be appreciated as containing *more* usable data than a clean, high quality signal. Unreadable chromatograms are often caused by the presence of multiple strains or alleles of the targeted sequence region, especially when these strains differ from each other by one or more deletions and/or insertions. This situation will tend to appear in the most important sequencing tasks — the ones targeting variable regions of the sequence of interest. One such example is HIV sequencing, wherein a large fraction of chromatograms is discarded even though the very cause of the unreliable readout — the presence of multiple HIV strains — is of great interest to the research community.

In §3, we point out the cues that could reveal the individual strains in the chromatograms of mixtures, then develop a statistical generative model that uses these cues to assign likelihood to different chromatogram decodings, and the inference algorithm that separates the components in the mixture by maximizing this likelihood. We also present preliminary,

but strongly indicative experimental validation of the algorithm: we show that in controlled mixing situations, where we can know the sequences for the mixed strains, we can infer the component mixtures with high accuracy (less than 1% of erroneously decoded nucleotides). The mixed components all have insertions and deletions, and they also differ by up to 10% of point mutations, which makes the decoding especially error prone using standard sequencing methods (up to 40% error).

2. Chromatography Background

Chromatography is a fast and effective mode for sequencing DNA, and is most commonly performed with the *chain termination method* ⁹. First, DNA molecules selected for sequencing will be amplified through rounds of PCR. Once the concentration is sufficiently high, a final annealing is performed. Previously, this would require the four deoxyribonucleotide triphospates (dNTPs: dATP, dCTP, dGTP, dTTP) as nucleotide building blocks to help grow the strands, but this time a small amount of a synthetic dideoxynucleotides (ddNTPs: ddATP, ddCTP, ddGTP, ddTTP) are added instead. They differ by not having a hydroxide ion on their sugar component where the next nucleotide would attach; thus, the growing chain terminates. This process takes place stochastically at different locations in the strand for each molecule, thus the resulting mixture will contain some DNA fragments of each intermediate length.

Secondly, polyacrylamide gel electrophoresis is applied to sort fragments by mass (i.e. length). The mixture is placed into gel-filled capillaries ¹⁰ and a voltage is applied to draw the DNA fragments to one end. Upon reaching this point, they pass by a laser, and since ddNTPs are also labeled with different fluorescent compounds ⁸, they emit a color distinct to each nucleotide that can be detected and recorded. The ABI 3730 machine automates this process and includes four-channel scanning of the lanes, base-calling (interpreting the traces of the scanner), and output into a standard AB1 file.

Because this process, like PCR, relies on primers to isolate DNA, it is susceptible to getting mixtures DNA sequences that differ in regions outside the primer. This is a common cause of noisy chromatogram trace files that confound standard base-callers looking for pure traces. We believe that there are important cues in these mixed chromatogram files, such as precise positioning and amplitude of peaks, that should enable decoding of chromatograms with more than one sequence.

3. The statistical generative model of chromatograms

The built-in ABI base-calling software is designed to operate on clean data and thus disregards much of the signal amplitude and position information present in chromatograms. More sophisticated base-callers, such as Phred² account for uncertainty and release confidence measures for each base they call, but they still only model and extract a single sequence from each chromatogram input.

In order to develop an algorithm for extracting more information from mixtures, we first develop a generative model that describes the variability typically observed in chromatograms of mixed signals through various involved variables such as component sequences, their amplitudes, and their phase offsets. The model is statistical in nature, and is described by conditional probability distributions which allow various types of noise and uncertainty in the model. The product of these conditionals forms the joint probability distribution over all model variables, and given a noisy chromatogram, the estimate of the variables of interest (*e.g.*, the component sequences) can be obtained by statistical inference.

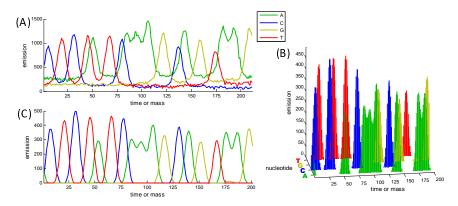


Figure 1. Chromatography data from the ABI 3730, with one trace for each nucleotide. (A) shows raw data, before correcting for gel and mobility effects and smoothing, as shown in (C). (B) shows how the data can be seen as a four-channel histogram of DNA sequence fragments terminated by ddNTPs.

We will describe the model from bottom up, starting with a simple model of a chromatogram trace obtained from the ABI sequencer. ABI sequencer performs low-level signal processing on raw channel traces as shown in Fig. 1A, correcting for nonlinear gel mobility effects, and other effects which we are currently not modeling. Beginning with the signal for one

chromatography

nucleotide, x(t), we can consider the signal as a histogram of terminating ddNTP appearance frequencies plotted against time (or mass), t, as illustrated in Fig. 1B. We construct a probability model of the data and express the likelihood of the data given the model as:

$$P(x \mid \text{model}) = \prod_{t} P[\text{ddNTP appearance at t}]^{x(t)}$$
(1)

If we treat ddNTP as being normally-

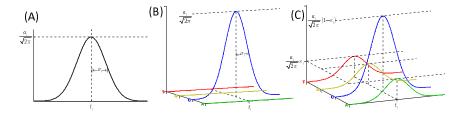


Figure 2. Peaks in a chromatogram treated as components in a Gaussian mixture model. (A) shows the basic model with peak amplitude (a_i) , position (t_i) , and width (σ_i) parameters. (B) generalizes to a four-channel signal with the peak being located in exclusively in one nucleotide's channel. (C) further generalizes this by modelling uncertainty (allowing 'leakage') of proportion ε_i to other nucleotide channels.

in the DNA chain, the probability model becomes a familiar mixture of Gaussians with a latent class variable $\mathbf{c} = \{c_1, c_2, \ldots, c_t, \ldots\}$ assigning a class label to each time value:

$$P\left[\mathrm{ddNTP} \text{ appearance at } t\right] = a_{c_t} \frac{1}{\sqrt{2\pi\sigma_{c_t}}} e^{-\left(t - t_{c_t}\right)^2 / 2\sigma_{c_t}^2} \tag{2}$$

where the model parameters, Θ , are as follows: a_{c_t} represents the amplitude (mixture proportion), t_{c_t} the peak position (mean of the Gaussian), and σ_{c_t} the peak width (standard deviation of the Gaussian). One such peak (with index $c_t = i$) is shown in Fig. 2A. This leads to the following complete log-likelihood of the data and class labels:

$$\log P(X, \mathbf{c}|\Theta) = \sum_{t} x(t) \log \left\{ \frac{a_{c_t}}{\sqrt{2\pi\sigma_{c_t}}} e^{-\left(t - t_{c_t}\right)^2 / 2\sigma_{c_t}^2} \right\}$$
(3)

The EM algorithm could be used to infer class labels and learn model parameters separately for each of the four data channels, $\{x^{A}(t), x^{C}(t), x^{G}(t)\}$, but we find it advantageous to consider the channels jointly, storing a class label for each (channel, time value) pair, c_{lt} . We also introduce a nucleotide parameter, $\ell_{c_{lt}}$, for each class:

$$\log P(X, \mathbf{c}|\Theta) = \sum_{l \in \{A, C, G, T\}} \sum_{t} x^{l}(t) \log \left\{ \left[l = \ell_{c_{l}} \right] \frac{a_{c_{lt}}}{\sqrt{2\pi}\sigma_{c_{lt}}} e^{-\left(t - t_{q_{l}}\right)^{2}/2\sigma_{q_{l}}^{2}} \right\}$$
(4)

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Here the Iverson notation is used where [true] = 1 and [false] = 0; this peak-to-nucleotide assignment is shown in Fig. 2B. It is important to keep class labels consistent with nucleotide parameters *i.e.* the label of channel A at time t, c_{At} , should index a Gaussian whose nucleotide label is also A, which means $\ell_{At} = A$ or else (4) will give a log-likelihood of $-\infty$. This leads to optimization difficulties in the EM algorithm — nucleotide labels will never greedily optimize beyond initialization — so we introduce a nucleotide 'uncertainty' or 'leakage' parameter, ε_{lt} , (see Fig. 2C) representing the proportion of the Gaussian placed on all other nucleotides. The complete log-likelihood then becomes:

$$\log P(X, \mathbf{c}|\Theta) = \sum_{t,l} x^l(t) \log \left\{ a_{c_{lt}} \frac{\varepsilon_{c_{lt}}^{[l=\ell_{c_{lt}}]} (1-3\varepsilon_{c_l})^{[l\neq\ell_{c_{lt}}]}}{\sqrt{2\pi}\sigma_{c_{lt}}} \exp\left(\frac{-(t-t_{c_{lt}})^2}{2\sigma_{c_{lt}}^2}\right) \right\}$$
(5)

Next, we label each Gaussian with an ordered pair (i, k) where *i* indexes the base pair (there are typically several hundred in a chromatogram) and $k = \{1, \ldots, K\}$ indexes the strain number. We confine our experimental results to chromatograms containing K = 2 distinct strains.

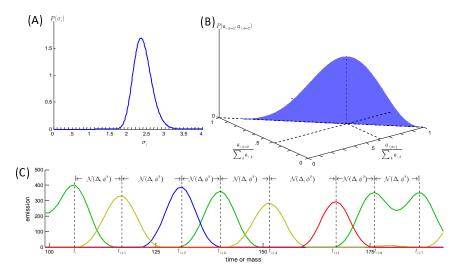


Figure 3. Conjugate priors on latent model variables. Because peak widths are wellknown to fall within a certain range, it is given a tight gamma prior distribution as illustrated in (A). Mixing proportions are assumed to be a shared property of the entire mixture (one concentration per strain), and this is controlled with a Dirichlet prior as illustrated in (B) in two dimensions. Peaks spacing is fairly constant (C) – in increments equivalent to the incremental mass of each DNA fragment – so they are given a Gaussian prior around the previous peak location plus a global constant, Δ .

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We use additional information in the form of conjugate prior distributions over parameters to help with sequencing. First, we put a gamma prior on σ_{ik}^{-2} reflecting the knowledge that peak width (i.e. ddNTP mass) is relatively constant between molecules:

$$P(\sigma_{ik}^{-2}) \propto \left(\sigma_{ik}^{-2}\right)^{\gamma-1} e^{-\sigma_{ik}^{-2}/\beta} \tag{6}$$

where γ and β are shared shape and scale hyperparameters, respectively, dependent on signal resolution only. This is shown in Fig. 3A.

Chromatography emission levels *i.e.* amplitudes on chromatogram traces are proportional to the concentration of DNA fragments with a particular terminating ddNTP nucleotide. These tend to decrease as fragment mass increases (strains lengthen) beyond a certain point and signal quality degrades. In small neighborhoods, however, relative amplitudes of peaks should be approximately proportional to the relative concentrations of strains and thus can provide a clue for decoding. We use a Dirichlet prior with one hyperparameter (μ_1, \ldots, μ_K) per strain so $P(a_{ik}) \propto (a_{ik})^{\mu_k}$, where μ_k is a constant reflecting the relative abundance of the strain in the mixture. See Fig. 3B for a multidimensional illustration of this distribution.

As discussed previously, the position of each peak in a chromatogram trace is proportional to the time a DNA fragment terminating at that location takes to reach the sensor. This time may depend on the mass, orientation, and shape of each fragment, with fragments from the same strain being correlated by these properties. For example, the mass of fragments in each strain grows in discrete steps corresponding to the mass of each dNTP, and so after enough differences between strains, the mass difference may become sufficient to incur a delay of one strain with respect to the other as they travel through the gel. Thus, it is important to capture statistical dependencies among the assigned peak positions by modeling the i^{th} peak position in the k^{th} strain as being normally-distributed about the previous peak position in the same strain, plus a constant, Δ :

$$P(t_{ik}|t_{i-1,k}) = \frac{1}{\sqrt{2\pi}\phi_k} e^{-(t_{ik}-t_{i-1,k}-\Delta)^2/2\phi^2}$$

Here, Δ is assumed to be a constant dependant on the sample resolution of the chromatogram, and ϕ^2 a shared variance representing the importance placed on this prior. This is illustrated in Fig. 3C.

The model can specialize on a certain species by involving its diversity profile. For our purposes, we use an HIV profile, H, computed from the data in ⁷. This profile consists of position-independent multinomial distributions (over four nucleotides) for the 9700 HIV base positions. The assigned peaks describe a decoding of each strain k, and this decoding is expected to be in accordance with this profile, given some alignment \mathbf{b}_k .

While this alignment is most generally another mapping of the base pairs, in our implementation of the model we consider the chromatograms in shorter overlapping windows and so it is sufficient to describe the alignment \mathbf{b}_k as a single specific location in the profile. We use this information as a prior on the nucleotide assignments of each peak as follows:

$$P(\ell_{ik}|b_{ik}) = (1 - 3\varepsilon_{ik}) \cdot h_{b_{ik}}(\ell_{ik}) + \varepsilon_{ik} \cdot (1 - h_{b_{ik}}(\ell_{ik}))$$

where b_{ik} is a base position pointer into the profile for the i^{th} peak in the k^{th} strain and $H = \{h_1(l), h_2(l), \ldots, h_{9700}(l)\}$ with $l \in \{A, C, G, T\}$ is the HIV diversity profile. For example, the probability that the nucleotide at position 6500 in the envelope region of the profile is 'G' is $h_{6500}(G)$.

To compute the most likely decodings for all strains, in our preliminary experiments we used a fast approximate variational inference technique ⁵. We approximate the product of the likelihood, $P(X, C|\Theta)$, and the priors described above, with another distribution, Q(C):

$$P(X, \mathbf{c}|\Theta)P(\sigma_{ik}^{-2})P(a_{ik})P(t_{ik})P(\ell_{ik}|b_{ik}) \approx Q(\mathbf{c})$$
(7)

where

$$Q(\mathbf{c}) = \prod_{i} \prod_{k} \prod_{l} \prod_{l} \prod_{t} q_{iklt}^{[c_{lt}=(i,k)] \cdot x^{l}(t)} \text{ s.t. } \sum_{i,k} q_{iklt} = 1 \ \forall l,t$$
(8)

There will inevitably be a considerable amount of uncertainty in some strain assignments where amplitude, profile, and spacing cues for peaks are inconsistent. In these cases, reversing a close decision involves switching peaks between strains which does not happen easily if the Gaussians are already mostly-fit and the free energy is near a local minimum. For this reason, we introduce a final latent variable, \mathbf{r} , associated with each peak position, i, and use it to enumerate all possible strain permutations. For two-strain case, there are 2! = 2 possible permutations, namely $(1, 2) \rightarrow (1, 2)$ and $(1, 2) \rightarrow (2, 1)$. The Q-distribution is modified accordingly:

$$Q(\mathbf{c}, \mathbf{r}) = Q(\mathbf{c}) \cdot \prod_{i} \prod_{\kappa=1}^{K!} (\rho_{i\kappa})^{[r_i = \kappa^{\text{th permutation}]}} \text{ s.t. } \sum_{\kappa=1}^{K!} \rho_{i\kappa} = 1 \quad \forall i \qquad (9)$$

We then proceed to minimize the free energy:

$$F = \int_{\mathbf{r}} \int_{\mathbf{c}} Q(\mathbf{c}, \mathbf{r}) \log \frac{Q(\mathbf{c}, \mathbf{r})}{P(\mathbf{X}, \mathbf{c} | \Theta) P(\sigma^{-2}) P(\mathbf{a}) P(\mathbf{t}) P(\ell | \mathbf{b})}$$
(10)

Minimization is efficiently performed by setting parameter derivatives to zero (i.e. co-ordinate descent). The one exception is the **b** profile pointer parameter, which we learn in each iteration by maximizing the correlation between overlapping windows (e.g. 30 base pairs) of the decoded sequence and the profile.

4. Experimental Results: Identifying mixtures of sequences

We tested our algorithm on ten chromatograms obtained from HIV patients in the Centre for Clinical Immunology and Biomedical Statistics in Perth, Australia. Four of the chromatograms, labeled 'C3', 'G4', 'A1', and 'A2', were obtained from 'clean' samples, *i.e.*, the chromatogram contained one unambiguous sequence. The remaining six ('A4', 'D4', 'F3', 'C1', 'E1', 'G1') were created by mixing clean samples in different proportions in the lab, and then performing chromatography on them.

After analyzing these six chromatograms with our algorithm, we aligned the inferred mixture strains with each of the ground truth sequences comprising the mixture, and obtained error rates shown in Table 1. ABI basecalling refers to the decoding provided by the standard ABI software, designed with the assumption that the sample is clean. Since the samples were in fact mixed, ABI software must fail to decode one of the sequences, and so we report a single error rate for the one that was bestdecoded. To establish an error rate for ABI software, we compared its decoding with both mixture components as shown in Fig. 4.

Figure 4 shows alignment and error rates of each the six mixed chromatograms to the corresponding pair of mixture component chromatograms. As chromatogram quality declines after several hundred bases (and may be spotty at the beginning too), we compute error rates only in central regions (kept consistent across all algorithms for each sample) shown as green backgrounds. The component sequences were substantially different from each other: sequences C3 and G4 contained much of the gp120 envelope region in HXB2 and differed in 16% of the sites. In addition, while C3 and G4 have the same start, they differ by an insertion of three nucleotides followed later by a deletion of three nucleotides. Clean sequences A1 and A2 contained the gp41 envelope region and differed in 14%of sites, and also exhibit differences due to insertion/deletions. The sample mixes were created so that they lead to typical ambiguous chromatograms that HIV researchers encounter in practice, but in a controlled environment where the ground truth is known. It should be noted that ENV genes are very important for vaccine design, as the ENV protein is potentially exposed to antibodies. However, the immune pressure leads to high variability in this region of HIV, and so most of the ENV chromatograms are not single-strain. More often than not, they are similar to the mixtures we analyze here. In practice, however, a mixed sample is typically discarded and a new sample is taken.

Table 1 shows that in most cases our method dramatically outperforms the single sequence decoding provided by the ABI software, while, impor-

Chromatogram label	Composition (ground truth)	Decoding Method	Mixture Estimate	Difference
F3		ABI basecaller	G4	42.54%
	$({50\% C3 + 50\% G4})$	decoded strain $#1$ #2	59% G4 + 41% C3	$0.55\%\ 2.39\%$
A4		ABI basecaller	C3	30.59%
	(62.5% C3 + 37.5% G4)	decoded strain $#1$ #2	${}^{60\%}_{40\%} {}^{C3}_{G4} + {}^{40\%}_{G4} {}^{G3}_{G4}$	$0.34\%\ 1.01\%$
D4		ABI basecaller	C3	0.75%
	(83% C3 + 17% G4)	decoded strain $#1$ #2	75% C3 + 25% G4	$0\% \\ 19.58\%$
C1		ABI basecaller	A2	38.35%
	(50% A1 + 50% A2)	decoded strain $#1$ #2	$\begin{array}{c} 59\% \mathrm{A1} + \\ 41\% \mathrm{A2} \end{array}$	$9.02\%\ 8.65\%$
E1		ABI basecaller	A1	9.86%
	(62.5% A1 + 37.5% A2)	decoded strain $#1$ #2	$\begin{array}{r} 64\% \mathrm{A1} + \\ 36\% \mathrm{A2} \end{array}$	$9.02\%\ 8.65\%$
G1		ABI basecaller	A1	1.62%
	(83% A1 + 17% A2)	decoded strain $#1$ #2	$\begin{array}{r} 74\% \mathrm{A1} + \\ 26\% \mathrm{A2} \end{array}$	2.83% 22.10%

Table 1. Error rates for identifying DNA mixtures by ABI base calls and our method, after alignment with ground truth. Some chromatograms deteriorate sooner than others, so we compute error rates for different regions of some samples as shown in Fig. 4's green backgrounds. Mixture concentration estimates are also shown for our method.

tantly, decoding both components from the mixture.

For example, we get good results for all mixture concentrations of C3 and G4. While we were able to extract both underlying clean sequences with low error rate, the traditional ABI base-caller's 30.6% error rate in mixture A4 and 42.6% in mixture F3 are higher than the genetic diversity in the region, thus rendering sequencing output useless. This is the reason why mixed chromatograms with insertions or deletions between strains in ENV region are typically discarded in the HIV community. In this case, C3 and G4 sequences, though binding to the same primer, differ by deletions and insertions which create more ambiguities than there really are site mutations. We should note that even extending the sequencing further into a less reliable part of the chromatogram, we were able to decode over 500 nucleotides from both strains with similarly low error rates.

It is interesting that in case of 50/50 mixtures, which we had expected to be harder due to equal expected amplitudes of both components, were decoded well by our algorithm. This indicates the strength of the position $(t_i - t_{i-1} \approx \Delta)$ cue for disambiguation. On the other hand, when one

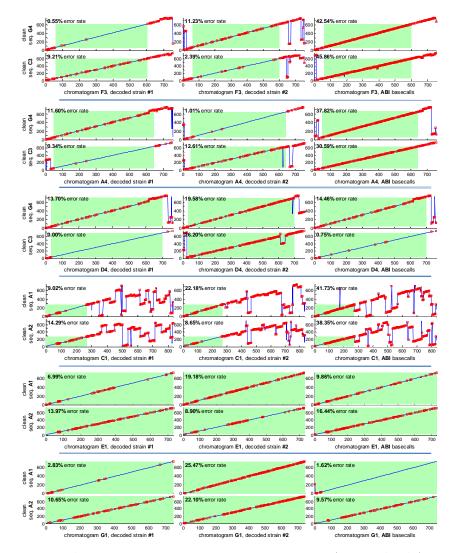


Figure 4. Alignment and differences between clean sequences (C3, G4, A1, A2) and mixed sequences (F3, A4, D4, C1, E1, G1) with differences marked as a red \Box . Error rates for the interpretable regions (shown with green background) appear in the upper-left for each algorithm. The multiple-strain decoding algorithm achieves much lower error rates than the ABI sequencer except in 83/17 mixtures with one extremely-dominant component.

strain is present in very low concentrations, the algorithm found it difficult to lift it out of the noise, which explains the worse performance for weaker

component of 83/17 mixes. In the case of chromatogram G1, if the algorithm decodes it assuming K = 1 strains instead of K = 2, the error rate is reduced to 1.48%, beating the ABI basecaller.

We also found that chromatogram amplitude was a fairly good indicator of the ground truth mixture proportions of the clean sequences in samples other than 50/50 mixtures. This was estimated from the μ_1 and μ_2 amplitude hyper-parameters, which were optimized in the algorithm.

5. Conclusion

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We have shown that for chromatograms of mixed sequences, probabilistic techniques can be employed to accurately infer the individual strains' sequences. This can be done by exploiting information overlooked by traditional base-callers, such as exact amplitude and position information.

This setup enabled us to identify and sequence mixtures of clean sequences in many cases. More sophisticated techniques, such as including raw (unsmoothed) trace data in the model, are currently being explored.

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