A Novel Differential Evolution Algorithm for TWET-NFSSP with SDSTs and RDs

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Abstract. A novel differential evolution (DE) algorithm, namely DE_TWET, is presented to deal with the no-wait flow-shop scheduling problem (NFSSP) with sequence-dependent setup times (SDSTs) and release dates (RDs). The criterion is to minimize a total weighted earliness/tardiness (TWET) cost function. The presented algorithm is a hybrid of DE, problem's properties, and a special designed local search. In DE_TWET, DE is adopted to execute global search in the solution space, and the problem's properties are utilized to give a speed-up evaluation method and construct the local search, and the special local search is designed to enhance the local search ability of DE. Experimental results and comparisons demonstrate the effectiveness and robustness of the presented algorithm.

Introduction

With the development of *just-in-time* (JIT) manufacturing systems, the study on the scheduling problems with both earliness and tardiness (E/T) costs is of greater significance. In this paper, a typical production scheduling problem with strong engineering background [1,2], the no-wait flow-shop scheduling problem (NFSSP) with sequence-dependent setup times (SDSTs) and release dates (RDs), is considered, whose criterion is to minimize a total weighted earliness/tardiness (TWET) cost function. In such a case, each job *j* must be processed through all machines without any interruption, and both the setup times and the release dates need to be explicitly treated, and an optimal schedule is the one that all jobs finish exactly on their due dates. This type of model is classified as $Fm/no-wait, ST_{sd}, r_j / \sum (w'_j E_j + w''_j T_j)$, which can also be identified as TWET-NFSSP with SDSTs and RDs. Because $1// \sum T_j \propto Fm/no-wait, ST_{sd}, r_j / \sum (w'_j E_j + w''_j T_j)$ (i.e., $1// \sum T_j \propto Fm/no-wait, ST_{sd}, r_j / \sum (w'_j E_j + w''_j T_j)$), it can be concluded that $Fm/no-wait, ST_{sd}, r_j / \sum (w'_j E_j + w''_j T_j)$ is NP-hard [3]. Moreover, literature review show that the researches on the scheduling problems with both sequence-dependent setup times and release dates are very limited [4]. Thus, it is meaningful and practical to develop an effective algorithm for the considered problem.

Differential evolution (DE) algorithm, which was first designed for optimizing complex continuous problems [5], is one of the latest population-based evolutionary methods. Owing to its quick convergence and easy implementation, nowadays, the DE algorithm has gained many successful applications in different fields. However, due to DE's continuous nature, the applications of the DE-based algorithms to scheduling problems are still limited. Tasgetiren *et al.* [6] devised a DE-based algorithm for flow-shop scheduling problems (FSSPs) to minimize makespan. Onwubolu and Davendra [7] developed a DE-based approach for FSSPs, where makespan, mean flowtime, and total tardiness were considered. Qian *et al.* [8] designed an very efficient DE-based algorithm for

749

NFSSPs with the makespan criterion. Wang *et al.* [9] proposed an efficient discrete differential evolution algorithm for FSSPs with blocking. Recently, Hu *et al.* [10] presented a hybrid DE algorithm (DE_NTJ) for Fm/no - wait, ST_{sd} , $r_j / \sum U_j$, which is the current best approach for the problem considered. To the best of our knowledge, there has no promising results on Fm/no - wait, ST_{sd} , $r_j / \sum (w'_j E_j + w''_j T_j)$, and there has no published work addressing it by using DE-based algorithm.

In the current paper, a novel DE algorithm (DE_TWET) is proposed to deal with TWET-NFSSP with SDSTs and RDs. In our DE_TWET, firstly, a largest-order-value (LOV) in [11] is utilized to map the real-valued vectors or individuals in DE to job permutations so as to make DE suitable for solving NFSSP; secondly, a speed-up evaluation method based on the property of the considered scheduling problem is given to calculate the cost function efficiently; thirdly, the DE-based search is adopted to perform global exploration in the solution space and guide the whole search to the promising regions/solutions, while a special local search based on problem's properties is developed to emphasize exploitation from those regions. Test results and comparisons demonstrate the efficiency and robustness of the proposed DE_TWET.

The remainder of this paper are partitioned into four sections. Section 2 introduces the mathematical model of TWET-NFSSP with SDSTs and RDs. Section 3 presents DE_TWET in details. Section 4 provides and discusses test results and comparisons. Finally, Section 5 gives some concluding remarks and suggestions of future research.

TWET-NFSSP with SDSTs and RDs

The NFSSP with SDSTs and RDs can be described as follows. There are n jobs and m machines. Each of n jobs will be sequentially processed on machine 1,2,...,m. The processing time of each job on each machine is deterministic. At any time, preemption is forbidden and each machine can process at most one job. To satisfy the no-wait restriction, each job must be processed without interruptions between consecutive machines. Thus, all jobs are processed in the same sequence on all machines. In a flow-shop with SDSTs, setup must be performed between the completion time of one job and the start time of another job on each machine, and setup time depends on both the current and the immediately preceding jobs at each machine. In a flow-shop with RDs, if a machine is ready to process a job but the job has not been released yet, it stays idle until the release date of the job.

NFSSP with SDSTs. Let $\pi = [j_1, j_2, \dots, j_n]$ denote the schedule or permutation of jobs to be processed, $p_{j_i,l}$ the processing time of job j_i on machine l, sp_{j_i} the total processing time of job j_i on all machines, $ML_{j_i,l}$ the minimum delay on the machine l between the completion of job j_{i-1} and j_i , L_{j_{i-1},j_i} the minimum delay on the first machine between the start of job j_{i-1} and j_i , $s_{j_{i-1},j_i,l}$ the sequence-dependent setup time between job j_{i-1} and j_i on machine l. Let $p_{j_0,l} = 0$ for l = 1, ..., m. Then $ML_{j_i,l}$ can be calculated as follows:

$$ML_{j_{i},l} = \begin{cases} \max\{s_{j_{i-1},j_{i},1} + p_{j_{i},1} - p_{j_{i-1},2}, s_{j_{i-1},j_{i},2}\} + p_{j_{i},2}, l = 2\\ \max\{ML_{j_{i},l-1} - p_{j_{i-1},l}, s_{j_{i-1},j_{i},l}\} + p_{j_{i},l}, \quad l = 3,...,m \end{cases}$$
(1)

Accordingly, L_{j_{i-1},j_i} can be calculated by using the following formula:

$$L_{j_{i-1},j_i} = ML_{j_i,m} + sp_{j_{i-1}} - sp_{j_i}.$$
(2)

2.2 TWET-NFSSP with SDSTs. Denote r_{j_i} the arrival time of job j_i , St_{j_i} the process start time of job j_i on machine 1, C_{j_i} the completion time of job j_i on machine m, d_{j_i} the due date of job j_i , E_{j_i} the earliness of job j_i on machine m, T_{j_i} the tardiness of job j_i on machine m, and $TWET(\pi)$ the total weighted earliness/tardiness cost function. Then St_{j_i} can be written as follows:

$$St_{j_{i}} = \begin{cases} \max\{ML_{j_{i},m} - sp_{j_{i}}, r_{j_{i}}\}, i = 1\\ St_{j_{i-1}} + \max\{L_{j_{i-1},j_{i}}, r_{j_{i}} - St_{j_{i-1}}\}, i = 2, ..., n \end{cases}$$
(3)

So, C_{j_i} , E_{j_i} , T_{j_i} , and $TWET(\pi)$ can be calculated as follows:

$$C_{j_i} = St_{j_i} + sp_{j_i}, i = 1, \dots, n,$$
(4)

$$E_{j_i} = \max(d_{j_i} - C_{j_i}, 0), i = 1, \dots, n,$$
(5)

$$T_{j_i} = \max(C_{j_i} - d_{j_i}, 0), i = 1, \dots, n,$$
(6)

$$TWET(\boldsymbol{\pi}) = \sum_{i=1}^{n} (w'_{j_i} E_{j_i} + w''_{j_i} T_{j_i}), \ w'_{j_i} > 0, w''_{j_i} > 0.$$
⁽⁷⁾

The aim of this paper is to find a permutation π^* in the set of all permutations Π such that

$$TWET(\boldsymbol{\pi}^*) = \min_{\boldsymbol{\pi} \in \prod} TWET(\boldsymbol{\pi}) .$$
(8)

DE_TWET for TWET-NFSSP with SDSTs and RDs

In this section, we will propose DE_TWET for TWET-NFSSP with SDSTs and RDs after explaining the solution representation, speed-up evaluation method, DE-based global search, and special designed local search.

Solution Representation. Owing to the continuous nature of the individuals in DE, the standard encoding scheme of DE cannot be directly applied to NTJ-NFSSP with SDSTs and RDs. In this paper, we adopt a largest-order-value (LOV) rule in [11] to map DE's *i*th individual $X_i = [x_{i,1}, x_{i,2}, \dots, x_{i,n}]$ to the job permutation vector $\boldsymbol{\pi}_i = [j_{i,1}, j_{i,2}, \dots, j_{i,n}]$. According to LOV rule, $X_i = [x_{i,1}, x_{i,2}, \dots, x_{i,n}]$ are firstly ranked by descending order to get the sequence $\varphi_i = [\varphi_{i,1}, \varphi_{i,2}, \dots, \varphi_{i,n}]$. Then the job permutation $\boldsymbol{\pi}_i$ is calculated by the following formula:

$$j_{i,\varphi_{i,k}} = k . (9)$$

According to our tests, LOV rule can achieve better results than the well-known random key representation.

Speed-up Evaluation Method. Based on the mathematical model of TWET-NFSSPs with SDSTs and RDs in Section 2, L_{j_{i-1},j_i} is only decided by the job j_{i-1} and j_i . By utilizing this property, one method can be adopted to reduce the computing complexity (CC) of $T_T(\boldsymbol{\pi})$. That is, L_{j_{i-1},j_i} , sp_{j_i} and

 $\sum_{i=1}^{n} sp_{j_i}$ can be calculated and saved in the initial phase of DE_TWET and then can be used as constant values in the global and local search phase of DE_TWET, which can reduce the CC of $TWET(\pi)$ from O(nm) to O(n).

DE-based Global Search. Since many published works show that DE-based search has the strong ability of obtaining enough promising regions over the solution space, we use it to execute global search in the solution space. DE algorithm introduced by Storn and Price [5] is a branch of

population-based evolutionary algorithms for solving optimization problems over continuous domain. In the basic DE algorithm, it uses simple differential operator to create new candidate solutions and one-to-one competition strategy to select each new candidate. During its evolutionary phase, the searching behavior of each DE's individual is dynamically adjusted according to the differentiations among population. In our DE_TWET, DE/rand-to-best/1/exp scheme [12] is adopted to perform DE-based global search, in which base vector is the best individual of the present population. So, the information of the best individual can be utilized by all individuals in the population.

Special Designed Local Search.

Interchange-based Neighborhoods. Because *interchange* is an effective neighborhood in the published papers, we select it as the fundamental neighborhood for local search. Denote *interchange*(π , u, v) the interchange of the job at the *u*th dimension (i.e., j_u) and the job at the *v*th dimension (i.e., j_v). The *interchange*-based neighborhood of π can be expressed as

$$N_{interchange}(\boldsymbol{\pi}) = \{ \, \boldsymbol{\pi}^{n,u,v} = interchange(\boldsymbol{\pi}, u, v) | \, u = 1, ..., n - 1 \text{ and } v = u + 1, ..., n \, \}.$$
(10)

As for a fixed u, the subset of $N_{interchange}(\pi)$ can be written as

$$N_{interchange}(\boldsymbol{\pi}, u) = \{ \boldsymbol{\pi}^{n, u, v} = interchange(\boldsymbol{\pi}, u, v) | v = u + 1, ..., n \}.$$
(11)

Thus, it has

$$N_{interchange}(\boldsymbol{\pi}) = N_{interchange}(\boldsymbol{\pi}, 1) \cup N_{interchange}(\boldsymbol{\pi}, 2) \cup \cdots \cup N_{interchange}(\boldsymbol{\pi}, n-1).$$
(12)

Obviously, the sizes of $N_{interchange}(\pi)$ and $N_{interchange}(\pi, u)$ are n(n-1)/2 and n-u, respectively.

Speed-up Search Method for $N_{interchange}(\pi)$. Let $FindBestN_{interchange}(\pi)$ denote the search procedure of finding the best neighbor π_{best} in $N_{interchange}(\pi)$, and $\pi^{n,u,v} = [j'_1, j'_2, ..., j'_u, ..., j'_v, ..., j'_n]$. When u = 2, ..., n-1 and i = 1, ..., u-1, it has $j_i = j_i'$, $St_{j_{u-1}} = St_{j'_{u-1}}$, and $\sum_{i=1}^{u-1} (w'_{j'_i}E_{j'_i} + w''_{j'_i}T_{j'_i}) = \sum_{i=1}^{u-1} (w'_{j_i}E_{j_i} + w''_{j_i}T_{j_i})$. Then, based on Eq. 4-Eq. 7, when u > 1, it has

$$TWET(\boldsymbol{\pi}^{n,u,v}) = \sum_{i=1}^{u-1} (w'_{j'_i} E_{j'_i} + w''_{j'_i} T_{j'_i}) + \sum_{i=u}^{n} (w'_{j'_i} E_{j'_i} + w''_{j'_i} T_{j'_i})$$

= $\sum_{i=1}^{u-1} (w'_{j_i} E_{j_i} + w''_{j_i} T_{j_i}) + \sum_{i=u}^{n} (w'_{j'_i} E_{j'_i} + w''_{j'_i} T_{j'_i}).$ (13)

Therefore, in $FindBestN_{interchange}(\boldsymbol{\pi})$, St_{j_i} and $\sum_{l=1}^{i} (w'_{j_ll}E_{j_{ll}} + w''_{j_{ll}}T_{j_{ll}})$ (i = 1, ..., n-2) can be calculated and saved before scanning or evaluating the neighbors in $N_{interchange}(\boldsymbol{\pi})$, and they can be used as constant values for evaluating $TWET(\boldsymbol{\pi}^{n,u,v})$, which can reduce the CC of $FindBestN_{interchange}(\boldsymbol{\pi})$ to some extent. In other words, if u > 1, $St_{j'u-1}$ and $\sum_{i=1}^{u-1} (w'_{j'_i}E_{j'_i} + w''_{j'_i}T_{j'_i})$ need not be computed and can be replaced with $St_{j_{u-1}}$ and $\sum_{i=1}^{u-1} (w'_{j_i}E_{j_i} + w''_{j_i}T_{j_i})$, respectively, and $St_{j'u}$ can be computed directly from $St_{j_{u-1}}$. In DE_TWET's local search, the above speed-up search method is utilized in $FindBestN_{interchange}(\boldsymbol{\pi})$, which is denoted as $SP_FindBestN_{interchange}(\boldsymbol{\pi})$.

Two Strategies for $SP_FindBestN_{interchange}(\pi)$. Denote $SP_FindBestN_{interchange}(\pi, u)$ the search procedure of finding the best neighbor $\pi^{u}_{local_best}$ in $N_{interchange}(\pi, u)$ by using speed-up search method in subsection 3.4.2. The procedure of $SP_FindBestN_{interchange}(\pi)$ is given as follows:

Step 1: Set u = 1 and $\pi_{\text{best}} = \pi$;

Step 2: $\pi^{u}_{local best} = SP_FindBestN_{interchange}(\pi, u);$

Step 3: If $TWET(\pi_{local_best}^{u}) < TWET(\pi_{best})$, then $\pi_{best} = \pi_{local_best}^{u}$; Step 4: If u < n-1, then u = u+1 and go to Step 2; Step 5: Output π_{best} . In order to reach quite different regions, two strategies are adopted in $SP_FindBestN_{interchange}(\pi)$.

The first one is a first move strategy. That is, if the first neighbor π_{first}^{u} in $N_{interchange}(\pi, u)$ that can improve π_{best} is obtained, $SP_FindBestN_{interchange}(\pi, u)$ terminates and outputs π_{first}^{u} . The second one is a promising region search strategy. That is, the permutation π in $SP_FindBestN_{interchange}(\pi, u)$ is replaced by π_{best} , which is helpful in executing the search immediately from the current promising regions found by $SP_FindBestN_{interchange}(\pi, u)$. Denote $FirstS_SP_FBN_{interchange}(\pi, u)$ the procedure of $SP_FindBestN_{interchange}(\pi, u)$ with the first move strategy. Then, a changed search procedure with the above two strategies, namely $TwoS_SP_FBN_{interchange}(\pi, KL)$, can be given as follows:

Step 1: Set u = KL and $\boldsymbol{\pi}_{\text{best}} = \boldsymbol{\pi}$;

Step 2: $\pi^{u}_{local_best} = FirstS_SP_FBN_{interchange}(\pi_{best}, u);$

Step 3: If $TWET(\boldsymbol{\pi}_{local best}^{u}) < TWET(\boldsymbol{\pi}_{best})$, then $\boldsymbol{\pi}_{best} = \boldsymbol{\pi}_{local best}^{u}$;

Step 4: If u < n-1, then u = u + 1 and go to Step 2;

Step 5: Output π_{best} .

 $TwoS_SP_FBN_{interchange}(\pi, KL)$ is the key element of DE_TWET's local search. KL is a variable in $TwoS_SP_FBN_{interchange}(\pi, KL)$, which is used to control the actual search range in $N_{interchange}(\pi)$ and can be set to any value in $\{1, \dots, n-1\}$. Obviously, the larger value of KL is set to, the smaller search range in $N_{interchange}(\pi)$ is.

Procedure of Local Search. Let *insert*(π , u, v) denote the insertion of j_u in the vth dimension of π . The procedure of DE_TWET's local search is given as follows:

Step 1: Convert DE's individual $X_i(t)$ to a job permutation $\pi_{i=0}$ according to the LOV rule.

Step 2: Perturbation phase.

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Set \boldsymbol{\pi}_{i} = \boldsymbol{\pi}_{i}.
             For kk = 1 to KM
                  Randomly select ii and ll, where |ii - ll| > n/3;
                  \boldsymbol{\pi}_i = insert(\boldsymbol{\pi}_{i-t}, ii, ll);
                  \boldsymbol{\pi}_{i t} = \boldsymbol{\pi}_{i};
             End.
Step 3: Exploitation phase.
             Set loop=0;
             repeat
                  \boldsymbol{\pi}_{i-1} = TwoS\_SP\_FBN_{interchange}(\boldsymbol{\pi}_i, KL);
                  If TWET(\boldsymbol{\pi}_{i-1}) \leq TWET(\boldsymbol{\pi}_i) then
                       \boldsymbol{\pi}_i = \boldsymbol{\pi}_{i-1};
                  else
                        loop++;
                  end:
             until loop=1.
Step 4: If TWET(\boldsymbol{\pi}_i) \leq TWET(\boldsymbol{\pi}_{i-0}), then \boldsymbol{\pi}_{i-0} = \boldsymbol{\pi}_i.
Step 5: Convert \boldsymbol{\pi}_{i=0} back to X_i(t).
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In the above procedure, Step 2 is the perturbation phase, which can avoid cycling and overcome local optima, and Step 3 executes exploitation from the region obtained by Step 2.

DE_TWET. According to the above solution representation, speed-up evaluation method, speed-up evaluation method, and special designed local search, the procedure of DE_TWET is presented as follows:

Step 0: Let t denote a generation, Pop(t) a population with size N_p in generation t, $X_i(t)$ the *i*th individual with dimension N(N = n) in Pop(t), $x_{i,l}(t)$ the *l*th variable of individual $X_i(t)$, tmp_l the *l*th variable of tmp, *CR* the crossover probability, and random(0,1) the random value in the interval [0,1]. The objective value of each individual is calculated by using speed-up evaluation method.

Step 1: Input N, $N_p \ge 3$, $CR \in [0,1]$, let bounds be $lower(x_{i,l}) = 0$ and $upper(x_{i,l}) = 4$, $l = 1, \dots, N$.

Step 2: Calculate and save sp_{j_i} and L_{j_{i-1},j_i} ($j_{i-1}, j_i \in 1,...,n$). //prepare for using speed-up

// evaluation method

Step 3: Population initialization.

 $x_{i,l}(0) = lower(x_{i,l}) + random(0,1) * (upper(x_{i,l}) - lower(x_{i,l})), l = 1, \dots, N \text{ for}$

 $i=1,\cdots,N_p$.

Step 4: Set t=1 and select an individual $X_{best}(0)$ from Pop(0) as best with the minimum objective value.

Step 5: Evolution phase (Step 5 through Step 11). Set i=1.

Step 6: Set the trial vector $tmp = X_i(t-1)$ and L' = 0. Randomly select $r1, r2 \in (1, \dots, N_p)$, where $r1 \neq r2 \neq i$, and randomly select $l \in (1, \dots, N)$.

Step 7: Perform DE's *Mutation* and *Crossover*.

Step 7.1: Let $tmp_l = tmp_l + F * (best_l - tmp_l) + F * (x_{r1,l}(t-1) - x_{r2,l}(t-1))$.

If $tmp_l < lower(x_{i,l})$, then let $tmp_l = 2*lower(x_{i,l}) - tmp_l$.

If $tmp_l > upper(x_{i,l})$, then let $tmp_l = 2 * upper(x_{i,l}) - tmp_l$.

Step 7.2: Set $l = (l \mod N) + 1$ and L' = L' + 1.

Step 7.3: If (random(0,1) < CR) and (L' < N), go to Step 7.1.

Step 8: Perform DE's Selection.

If $(f(tmp) \le f(X_i(t-1)))$, then set $X_i(t) = tmp$;

else, set $X_i(t) = X_i(t-1)$.

Step 9: If f(tmp) < f(best), then best = tmp.

Step 10: Set i=i+1. If $i \le N_p$, then go to Step 6.

Step 11: Apply special designed local search to best.

Step 12: Set t=t+1. If $t \le t$ max (the maximum number of iteration), then go to Step 5.

Step 13: Output best and its objective value.

It can be seen that DE_TWET not only applies the DE-based algorithm to obtain promising regions within the entire solution space, but also applies a special designed local search to enhance the search quality. Because both global and local search are well balanced, DE_TWET is expected to achieve good results.

Test Results and Comparisons

Experiment Setup. Some random generated instances with different scales are used to test the performance of DE_TWET. That is, the $n \times m$ combinations are: {20, 30, 50, 70, 100}×{10, 20}. The processing time $p_{j_i,l}$ and the setup time $s_{j_{i-1},j_i,l}$ are generated from a uniform distribution [1,

100]. The job arrival time r_{j_i} is an integer that is randomly generated in $[0,150n\alpha]$, where the parameter α is used to control the jobs' arrival speeds. The values of α are set to 0, 0.2, 0.4, 0.6, 0.8, 1 and 1.5, respectively. Moreover, the due date of each job is specified as follows:

Step 1: For each problem p, randomly generate a permutation of the jobs.

Step 2: Calculate the completion time of each job in the permutation specified in Step 1.

Step 3: Specify the due date of each job by

$$d_{p,j_i} = C_{p,j_i} + random[-C_{p,j_i}, 0],$$
(14)

where d_{p,j_i} is the due date of job j_i to problem p, C_{p,j_i} is the completion time of job j_i to problem p, and $random[-C_{p,j_i},0]$ is a random value in the interval $[-C_{p,j_i},0]$. For each instance at each α , every algorithm independently run 20 replications for comparison. Thus, it has a total of 70 different instances.

For the purpose of evaluating the effectiveness of DE_TWET, we carry out simulations to compare our DE_TWET with an iterated greedy heuristic (IG) [13] and a hybrid DE (DE_NTJ) [10]. IG is the new state-of-the-art approach for solving FSSPs with SDSTs [13], and DE_NTJ is one of the current best algorithms for NFSSPs with SDSTs and RDs [10]. Moreover, we also compare DE_TWET with its five variants, whose abbreviations are as follows:

(1) DE_TWET_S1: In DE_TWET's local search, only speed-up evaluation method is used.

(2) DE_TWET_S12: In DE_TWET's local search, only speed-up evaluation method and speed-up search method are used.

(3) DE_TWET_noST2: In DE_TWET's local search, the promising region search strategy (i.e., strategy two) is not used.

(4) DE_TWET_0.3n: In Step 3 of DE_TWET's local search, KL is set to round(0.3*n), where round(a) is a round function rounds a real-type value a to an integer-type value.

(5) DE_TWET_0.6n: In Step 3 of DE_TWET's local search, KL is set to round(0.6*n).

DE_TWET's parameters are set as follows: the population size popsize = 30, the scaling factor F = 0.7, the crossover parameter CR = 0.1, the local search variable KM = 3, and the local search variable KL = 1. Moreover, all values of w'_{j_i} and w''_{j_i} in $TWET(\pi)$ are set to 0.1. To make a fair comparison, all the compared algorithms use the same runtime limit of 2nm milliseconds as a termination criterion. We code all procedures in Delphi 7.0 and run all tests on an Intel Q8200 2.33GHz PC with 3 GB memory.

Performance Metrics. Denote $\pi_{ini}(\alpha)$ the permutation in which jobs are ranked by ascending value of job's release date at α , $TWET(\pi(\alpha))$ the total weighted earliness/tardiness of the permutation $\pi(\alpha)$ at α , $avg_TWET(\pi(\alpha))$ the average value of $TWET(\pi(\alpha))$, $best_TWET(\pi(\alpha))$ the best value of $TWET(\pi(\alpha))$, worst $TWET(\pi(\alpha))$ the worst value of $TWET(\pi(\alpha))$ $(TWET(\boldsymbol{\pi}_{ini}(\alpha)) - avg_TWET(\boldsymbol{\pi}(\alpha)))/TWET(\boldsymbol{\pi}_{ini}(\alpha))$ $ARI(\alpha)$ = 100% the × average percentage improvement over $TWET(\boldsymbol{\pi}_{ini}(\alpha))$, $BEI(\alpha) = (TWET(\boldsymbol{\pi}_{ini}(\alpha)))$ percentage best $_TWET(\boldsymbol{\pi}(\alpha)))/TWET(\boldsymbol{\pi}_{ini}(\alpha)) \times 100\%$ the best improvement over $TWET(\boldsymbol{\pi}_{ini}(\alpha))$, $WRI(\alpha) = (TWET(\boldsymbol{\pi}_{ini}(\alpha)) - worst TWET(\boldsymbol{\pi}(\alpha))) / TWET(\boldsymbol{\pi}_{ini}(\alpha)) \times 100\%$ the worst percentage improvement over $TWET(\boldsymbol{\pi}_{ini}(\alpha))$, $SD(\alpha)$ the standard deviation of $TWET(\pi(\alpha))$ at α , S_{α} the set of all values of α , and $|S_{\alpha}|$ the number of different values in S_{α} . Then, we define four metrics to evaluate the performances of the compared algorithms, i.e., $ARI = \sum_{\alpha \in S\alpha} ARI(\alpha) / |S_{\alpha}| \quad , \quad BEI = \sum_{\alpha \in S\alpha} BEI(\alpha) / |S_{\alpha}| \quad , \quad WRI = \sum_{\alpha \in S\alpha} WRI(\alpha) / |S_{\alpha}| \quad , \quad \text{and}$ $SD = \sum_{\alpha \in S\alpha} SD(\alpha) / |S_{\alpha}|$.

Comparisons of DE_TWET with Its Five Variants. In order to investigate DE_TWET's local search ability, we compare DE_TWET with its five variants. Statistical results can be found in Table 1. In Table 1, it can be seen from ARI metric that DE_TWET can obtain better results than its five variants for most instances, which manifest the importance of simultaneously adopting two speed-up methods and two strategies in local search and show the necessity of setting KL to the smallest value. From SD metric, it can be seen that the SD values of DE_TWET are smaller than those of five variants for almost all instances. This means DE TWET is more robust than its five variants.

Instance	nce DE_TWET_S1		DE_TWET_S12		DE_TWET_noST2		DE_TWET_0.3n		DE_TWET_0.6n		DE_T	WET
n, m	ARI	\overline{SD}	ARI	SD	ARI	SD	ARI	SD	ARI	SD	ARI	SD
20, 10	45.827	0.728	46.662	0.247	46.569	0.323	43.119	1.749	39.501	1.888	46.655	0.207
20, 20	43.094	0.384	43.527	0.116	43.503	0.149	42.218	1.084	41.012	1.046	43.479	0.123
30, 10	51.787	1.015	53.547	0.420	53.522	0.345	44.417	3.743	41.091	2.365	53.570	0.246
30, 20	54.753	0.726	56.054	0.253	56.024	0.265	51.304	1.918	49.800	1.505	56.027	0.247
50, 10	58.414	1.644	61.389	0.442	61.266	0.420	42.194	5.772	39.124	2.778	61.581	0.334
50, 20	55.472	1.699	58.618	0.385	58.383	0.508	43.949	3.678	44.459	1.998	58.693	0.379
70, 10	57.447	2.245	62.067	0.526	61.164	0.971	28.760	6.178	28.003	3.873	62.414	0.406
70, 20	58.895	2.337	63.425	0.386	63.120	0.479	40.245	5.328	42.068	2.492	63.552	0.325
100, 10	62.876	1.555	65.642	0.680	64.044	1.547	23.096	5.885	24.262	4.065	66.508	0.405
100, 20	63.296	1.402	66.545	0.422	65.799	0.652	32.481	6.390	34.898	3.006	66.979	0.346
average	55.186	1.374	57.748	0.388	57.339	0.566	39.178	4.172	38.422	2.502	57.946	0.302

Table 1 Statistical results of testing DE_TWET and its variants

Comparisons of DE_TWET, IG, and DE_NTJ. To show the effectiveness of DE_TWET, we carry out some comparisons with IG [13] and DE_NTJ [10]. The test results of the three algorithms are shown in Table 2. From Table 2, it can be concluded that the searching quality of DE_TWET is better than that of IG for almost all instances and is superior or comparable to that of DE_NTJ. Therefore, it is concluded that DE_TWET is an effective and robust algorithm for dealing with TWET-NFSSP with SDSTs and RDs.

Table 2 Statistical results of testing DE_TWET, IG, and DE_NTJ

Instance IG				DE NTJ				DE TWET				
n, m	BEI	ARI	WRI	SD	BEI	ARI	WRI	SD	BEI	ARI	WRI	SD
20, 10	46.846	46.014	45.213	0.497	46.875	46.641	45.905	0.263	46.875	46.655	46.201	0.207
20, 20	43.222	42.219	41.084	0.649	43.615	43.550	43.262	0.097	43.615	43.479	43.165	0.123
30, 10	53.838	52.655	51.019	0.857	54.035	53.614	53.127	0.254	54.005	53.570	53.095	0.246
30, 20	55.960	54.837	53.378	0.789	56.352	56.101	55.503	0.246	56.360	56.027	55.496	0.247
50, 10	61.668	60.824	59.848	0.497	61.900	61.351	60.613	0.346	62.153	61.581	60.917	0.334
50, 20	58.847	57.944	56.801	0.589	59.246	58.337	57.497	0.504	59.347	58.693	57.827	0.379
70, 10	62.987	61.984	60.873	0.566	62.311	60.904	59.288	0.737	63.240	62.414	61.654	0.406
70, 20	63.633	62.942	61.919	0.434	63.815	62.975	62.211	0.477	64.124	63.552	62.907	0.325
100, 10	67.143	66.527	65.953	0.389	66.667	66.011	65.397	0.410	67.138	66.508	65.743	0.405
100, 20	67.386	66.730	65.954	0.437	66.836	66.153	65.525	0.372	67.465	66.979	66.380	0.346
average	58.153	57.268	56.204	0.570	58.165	57.564	56.833	0.371	58.432	57.946	57.338	0.302

Conclusion and Future Research

To the best of the current authors' knowledge, this is the first report on the application of differential evolution (DE) algorithm for NFSSP with SDSTs and RDs with the criterion to minimize the total weighted earliness/tardiness. In our presented algorithm, DE-based global search was used to perform exploration for promising regions within the entire solution space, while a special local search based on problem's properties was developed to stress exploitation in these regions. Due to the hybridization of DE and local search, DE_TWET's search behavior can be enriched and its search ability can be enhanced. Simulations and comparisons showed the effectiveness and robustness of DE_TWET. The future work is to develop some effective DE-based algorithms for dynamical scheduling and reentrant scheduling.

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