

# Particle bee algorithm for tower crane layout with material quantity supply and demand optimization



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## ABSTRACT

The tower crane layout (TCL) problem, a typical construction site layout (CSL) problem, is currently used in a wide range of construction projects and site conditions. The tower crane is a key facility used in the vertical and horizontal transportation of materials, particularly heavy prefabrication units such as steel beams, ready-mixed concrete, prefabricated elements, and large-panel formwork. Matching the location of tower cranes to material supply and engineering demands is a combinatorial optimization issue within the TCL problem that is difficult to resolve. Swarm intelligence (SI) is a popular artificial intelligence technique that is used widely to resolve complex optimization problems. Various SI-based algorithms have been developed that emulate the collective behavior of animals such as honey bees (bee algorithm, BA) and birds (particle swarm optimization, PSO). This study applies the particle bee algorithm (PBA), a hybrid swarm algorithm that integrates the respective advantages of honey bee and bird swarms, to the TCL problem. The performances of PBA, BA, and PSO are compared in terms of their effectiveness in resolving a practical TCL problem in construction engineering. Results show that the PBA performs better than both the BA and PSO algorithms.

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## 1. Introduction

Construction site layout (CSL) problems are interesting because they introduce the consideration of layout esthetics and usability qualities into the facility design process [1]. The CSL problem identifies a feasible location for a set of interrelated facilities that meets all design requirements and maximizes design quality in terms of design preferences while minimizing the total cost associated with interactions among these facilities.

Artificial intelligence (AI)-based algorithms have previously been applied to solve CSL problems. Elbeitagi and Hegazy [2] used a hybrid neural network to determine optimal site layout. Yeh [3] applied annealed neural networks to solve construction site-level CSL problems. Li and Love [4] and Osman et al. [5] used a genetic algorithm (GA) to solve site layout problems in unequally sized facilities. The objective functions of these algorithms work to optimize inter-facility interactions in terms of variables such as transportation costs and trip frequencies. Hegazy et al. [6] developed a comprehensive system for site layout planning based on GA. Elbeitagi et al. [7] presented a practical model for schedule-dependent site layout planning in construction that combined a knowledge-based system, fuzzy logic, and GA.

Tower crane layout (TCL), a typical CSL problem, is suited to a wide range of construction work assignments and site conditions. The tower

crane is a key facility used in the vertical and horizontal transportation of materials, particularly heavy prefabrication units such as steel beams, ready-mixed concrete, prefabricated elements, and large-panel formwork [8].

In large construction projects, several cranes are often used to handle transportation tasks, particularly in situations in which a single crane cannot cover all demand and supply points and/or when the capacity of a single crane cannot meet construction-schedule needs. Many factors influence tower crane location [9]. Currently, locations are typically determined through trial and error based on site topography/shape and overall task-coverage requirements. The complex factors involved in crane location and the lack of quantitative references often leave managers with little choice but to rely on experience and/or instinct [9]. Zhang et al. [9] and Tam et al. [8] developed an analytical model to model the travel time of tower crane hooks. In determining the time required for a hook to travel from one position to another, they considered factors related to physical parameters such as the topographical layout, building tower layout, and adjacent environment, which are unique to each site. The proper positioning of tower cranes and related material supply and demand points is critical to overall work efficiency on a construction site. Ideally, a tower crane jib should reach and cover all sections of all buildings on a construction site in order to allow the transport of construction materials between all supply and demand points [8].

Many research studies that address the problem of optimizing the location and transportation time of tower cranes have been published. Zhang et al. [9] used a Monte Carlo simulation to optimize tower crane

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**Table 3**  
Coordinates of supply points.

	S1	S2	S3	S4	S5	S6	S7	S8	S9
X	73	83	87	73	55	35	22	36	55
Y	26	31	45	67	73	67	46	27	15
Z	2	2	1.5	1.5	1.5	0	0	1	1

In this step, new particle bees from elite and best bees are produced using Eq. (1). Elite and best bee velocity updates are performed as indicated in Eq. (2). This study further proposed a neighborhood-windows (NW) technique to improve PSO searching efficiency as shown in Eq. (3). Thus, after  $x_{id}(t + 1)$  is substituted into Eq. (1) and Eq. (2), the NW ensures PSO searching within the designated  $x_{idmin}$  and  $x_{idmax}$ . In other words, if the sum of  $x_{id}(t + 1)$  exceeds  $x_{idmin}$  or  $x_{idmax}$  then  $x_{id}(t + 1)$  is limited to  $x_{idmin}$  or  $x_{idmax}$ .

$$x_{id}(t + 1) = x_{id}(t) + v_{id}(t + 1) \quad (1)$$

where  $x_i$  is  $i$ th  $x$  and  $i = 1$  to  $n$ ;  $v_i$  is  $i$ th  $v$ ;  $d$  is dimension in  $x_i$  or  $v$  and  $d = 1$  to  $D$ ;  $t$  is iteration;  $x_{id}(t)$  is  $d$ th dimension in  $i$ th  $x$  and in  $t$  iteration;  $v_{id}(t + 1)$  is  $d$ th dimension in  $i$ th  $v$  and in  $t + 1$  iteration;  $x_{id}(t + 1)$  is  $d$ th dimension in  $i$ th  $x$  and in  $t + 1$  iteration;  $n$  is the number of particles.

$$v_{id}(t + 1) = w \times v_{id}(t) + c_1 \times Rand \times [P_{id}(t) - x_{id}(t)] + c_2 \times Rand \times [G_d(t) - x_{id}(t)] \quad (2)$$

where  $v_{id}(t)$  is  $d$ th dimension in  $i$ th  $v$  and in  $t$  iteration;  $w$  is inertia weight and controls the magnitude of the old velocity  $v_{id}(t)$  in the calculation of the new velocity;  $P_{id}(t)$  is  $d$ th dimension in  $i$ th local best particle and in  $t$  iteration;  $G_d(t)$  is  $d$ th dimension global best particle in  $t$  iteration;  $c_1$  and  $c_2$  determine the significance of  $P_{id}(t)$  and  $G_d(t)$ ;  $Rand$  is a uniformly distributed real random number within the range 0 to 1. Furthermore,  $v_{id}$  at any time-step of the algorithm is constrained by parameters  $v_{max}$  and  $v_{min}$ . The swarm is initialized by assigning each particle to a uniformly and randomly chosen position in the search space. Velocities are initialized randomly in the range  $v_{max}$  to  $v_{min}$ . Particle velocities on

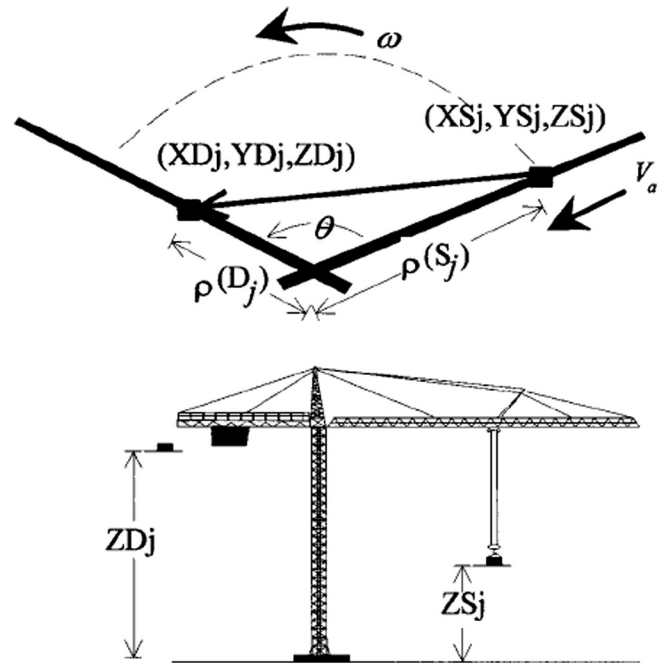


Fig. 3. Hook travel time.

each dimension are clamped to a maximum velocity  $v_{max}$ . If the velocity of that dimension exceeds  $v_{max}$  or  $v_{min}$  (user-specified parameters), dimension velocity is limited to  $v_{max}$  or  $v_{min}$ .

$$x_{idmin} \leq x_{id}(t + 1) \leq x_{idmax} \quad (3)$$

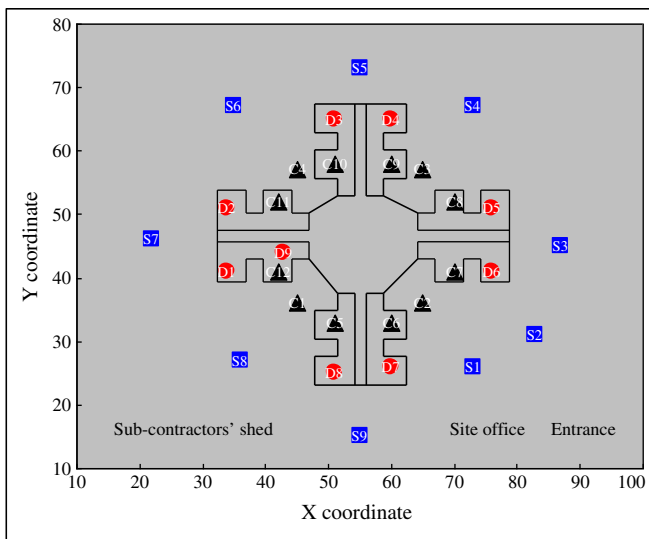
where  $x_i$  is  $i$ th  $x$  and  $i = 1$  to  $n$ ;  $d$  is dimension in  $x_i$  and  $d = 1$  to  $D$ ;  $t$  is iteration;  $x_{id}(t + 1)$  is  $d$ th dimension in  $i$ th  $x$  and in  $t + 1$  iteration;  $n$  is the number of particles.

- Step (5) Select best sites ( $b$ ) from scout bees. Best sites are selected for each best bee, the total number of which equals one-quarter of the number of scout bees.
- Step (6) Best bees start the PSO procedure using the NW  $Pbest$  iteration. In this step, new particle bees from elite and best bees are produced using Eq. (1). Elite and best bee velocity updates are acquired using Eq. (2). The NW technique improves PSO search efficiency, as shown in Eq. (3).
- Step (7) Recruit random bees ( $r$ ) for other visited sites. The random bees in the population are assigned randomly around the search space scouting for new potential solutions. The total number of random bees is one-quarter of the number of scout bees.

**Table 4**  
Parameter values used in the experiments.

PSO		BA		PBA	
$n$	100	$n$	100	$n$	100
$w$	0.9–0.7	$e$	$n/2$	$e$	$n/2$
$v$	$X_{min}/10 - X_{max}/10$	$b$	$n/4$	$b$	$n/4$
		$r$	$n/4$	$r$	$n/4$
		$n_1$	2	$w$	0.9–0.7
		$n_2$	1	$v$	$X_{min}/10 - X_{max}/10$
				<i>Pelite</i>	15
				<i>Pbest</i>	9

$n$  = population size (colony size);  $w$  = inertia weight;  $v$  = limit of velocity;  $e$  = elite bee number;  $b$  = best bee number;  $r$  = random bee number;  $n_1$  = elite bee neighborhood number;  $n_2$  = best bee neighborhood number; *Pelite* = PSO iteration of elite bees; *Pbest* = PSO iteration of best bees.



▲ Ci: Position of tower crane point ( $i=1\sim12$ )  
● Di: Position of demand point ( $i=1\sim9$ )  
■ Si: Position of supply point ( $i=1\sim9$ )

Fig. 2. A reference of tower crane layout.

**Table 5**  
Parameter values used in single tower crane.

	CU	$\alpha$	$V_h$	$\beta$	$V_a$	$V_w$	M	DY	IS	MS	MST	RS	LC	LA
Crane #1	1.92	1	60	0.25	53.3	7.57	1000	80	5000	500	10	2000	100	5

Step (8) Self-parameter-updating (SPU) for elite, best and random bees.

Furthermore, in order to prevent being trapped into a local optimum in high dimensional problems, this study proposed a solution, i.e., the self-parameter-updating (SPU) technique, the idea for which came from Karaboga [20]. Eq. (4) shows the SPU equation.

$$x_{id(new)} = x_{id(cur)} + 2 \times (Rand - 0.5) \times (x_{id(cur)} - x_{jk}) \quad (4)$$

$$j = \text{int}(Rand \times n) + 1 \quad (5)$$

$$k = \text{int}(Rand \times d) + 1 \quad (6)$$

where  $x_i$  is  $i$ th  $x$  and  $i = 1$  to  $n$ ;  $d$  is dimension in  $x_i$  and  $d = 1$  to  $D$ ;  $x_{id(cur)}$  is  $d$ th dimension in  $i$ th  $x$  and in current solution;  $x_{id(new)}$  is  $d$ th dimension in  $i$ th  $x$  and in new solution;  $Rand$  is a uniformly distributed real random number within the range 0 to 1;  $j$  is the index of the solution chosen randomly from the colony as shown in Eq. (5),  $k$  is the index of the dimension chosen randomly from the dimension as shown in Eq. (6);  $n$  is the number of scout bees.

In step (8), after elite, best and random bees have been distributed based on fitness, fitnesses are checked to determine whether they are to be abandoned or memorized using Eq. (4). Therefore, if fitnesses of elite, best or random bees are both improved using Eq. (4) and improved over previous fitnesses, the new fitnesses are memorized. In step (3) through step (8), this differential recruitment is a key operation of the PBA.

Step (9) Convergence?

In this step, only the bee with the highest fitness will be selected to form the next bee population. These steps are repeated until the stop criterion is met and bees are selected to be abandoned or memorized.

In PBA, scout bees are used to classify both elite and best bees. Classification is controlled by scout bee fitness and optimized by control parameters called “*Pelite*” and “*Pbest*”, which are important PBA control parameters. In PBA, the idea of *Pelite* for elite bees gives a higher

**Table 6**  
The result of three algorithms.

	Iteration	Mean	Worst	Best	Std
PBA	100	7.62E+05	8.92E+05	7.08E+05	6.64E+04
	300	7.34E+05	8.50E+05	6.21E+05	5.31E+04
	500	7.44E+05	8.28E+05	6.19E+05	5.63E+04
	1000	7.08E+05	8.12E+05	5.83E+05	6.28E+04
	5000	<b>7.03E+05</b>	8.55E+05	<b>5.41E+05</b>	5.99E+04
BA	100	9.52E+05	9.83E+05	9.10E+05	1.46E+04
	300	9.30E+05	9.56E+05	8.83E+05	1.64E+04
	500	9.17E+05	9.46E+05	<b>8.35E+05</b>	2.14E+04
	1000	9.12E+05	9.35E+05	9.03E+05	6.39E+03
	5000	<b>8.86E+05</b>	9.08E+05	8.59E+05	1.55E+04
PSO	100	9.29E+05	1.01E+06	8.90E+05	2.88E+04
	300	9.05E+05	1.00E+06	7.87E+05	4.25E+04
	500	8.84E+05	9.40E+05	8.24E+05	2.88E+04
	1000	8.82E+05	9.73E+05	7.91E+05	3.69E+04
	5000	<b>8.68E+05</b>	9.46E+05	<b>7.50E+05</b>	3.87E+04

Bold are the best Mean and best solution results of these mention algorithms.

potential to search optimization solutions. The idea of *Pbest* for best bees gives a second opportunity to search optimization solutions because luck continues to play a role in resource identification. Therefore, in this study, *Pelite* is always larger than *Pbest*. In a robust search process, exploration and exploitation processes must be carried out together. In PBA, while elite bees (*Pelite*) implement the exploitation process in the search space, best bees (*Pbest*) and random bees control this process.

### 3. Case study of the tower-crane-layout problem

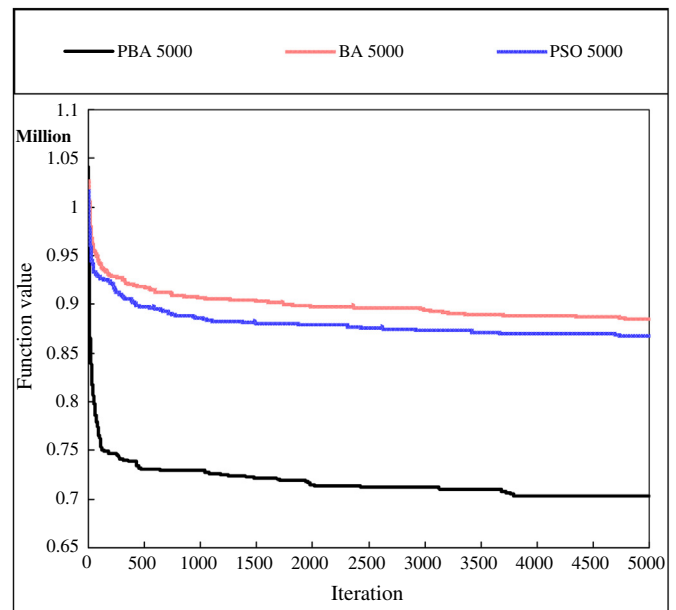
#### 3.1. Modeling of the multi-tower crane layout problem

##### 3.1.1. A reference tower crane layout

In the past, project engineers considered site conditions, building structure, construction sequence, market conditions, and climate conditions in order to determine the tower crane layout (TCL) and the location of associated tower cranes, supply points, demand points, and supporting equipment. In this study, the TCL was modeled based on the minimum operation time cited in previous studies [10,11]. Tam and Hoang considered only a per-crane-operation-time cost of material operation flow and neglected other important cost factors such as rent, labor and, tower crane setup. Therefore, the current study extends their work by designing a TCL model that more practically reflects the actual conditions on a construction site. This study adopts and modifies a project as a reference [10] case study in order to determine optimal TCL with material quantity supply and demand through PSO, BA, and PBA. The project includes 12 potential tower crane locations, with the coordinates of each shown in Table 1. Furthermore, the project includes 9 supply points and 9 demand points, with coordinates shown, respectively, in Tables 2 and 3. Fig. 2 shows the completed site map for this project.

##### 3.1.2. Objective function

In this study, the particle bee algorithm (PBA) was used to optimize the location of the tower crane. PBA was further used to optimize the



**Fig. 4.** Evolution of mean best values for single TCL problem.

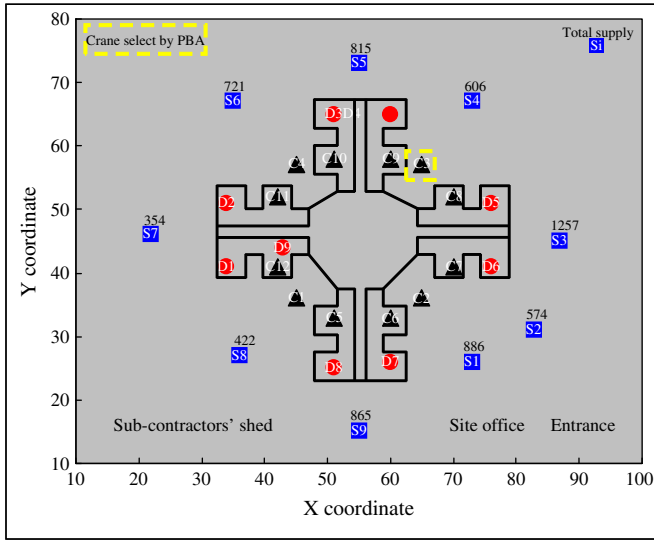


Fig. 5. PBA best single tower crane layout design.

operating distance and frequency between demand and supply points in terms of total operating costs based on the material requirements at demand and supply points. The objective function of the TCL problem was required to satisfy two requirements: (1) The function must be high only for those solutions with a high design preference and (2) The function must be high only for those solutions that satisfy the layout constraints. Therefore, this study was based on Ref. [10] and gives the total objective function as shown in Fig. 3 and Eq. (8). While the linear problem in Eq. (8) may be resolved using the mixed-integer-linear program (MILP) [10], using this program leaves many variables, including the tower crane position variable, and the supply to demand connecting variable, still to be optimized. Therefore, this study compares the performance of PBA against the abovementioned optimization methods in terms of accurately determining the variables in Eq. (8).

$$\text{Minimize } TC = \sum_{i=1}^n \sum_{j=1}^m \sum_{k=1}^o T_i \times Q_{jk} \times CU_i + R + S + L \quad (8)$$

$$T_i = \max(T_{hi}, T_{vi}) + \beta \times \min(T_{hi}, T_{vi}) \quad (9)$$

$$T_{hi} = \max(T_{ai}, T_{wi}) \alpha_i \times \min(T_{ai}, T_{wi}) \quad (10)$$

$$T_{vi} = |ZS_m - ZD_o| / V_{hi} \quad (11)$$

$$T_{ai} = |\rho(D_o) - \rho(S_m)| / V_{ai} \quad (12)$$

$$T_{wi} = \frac{1}{V_i} \times \arccos\left(\frac{l_p^2 - \rho(D_o)^2 - \rho(S_m)^2}{2 \times \rho(D_o) \times \rho(S_m)}\right) \quad (13)$$

$$\rho(D_o) = \sqrt{(XD_o - XCr_i)^2 + (YD_o - YCr_i)^2} \quad (14)$$

$$\rho(S_m) = \sqrt{(XS_m - XCr_i)^2 + (YS_m - YCr_i)^2} \quad (15)$$

$$l_p \sqrt{(XD_o - XS_m)^2 + (YD_o - YS_m)^2} \quad (16)$$

$$R = \sum_i^n M_i \times (\text{int}(DY_i/30) + 1) \quad (17)$$

$$S = \sum_i^n IS_i + MS_i \times MST_i + RSI_i \quad (18)$$

$$L = \sum_i^n LC_i \times LA_i \times DY_i \quad (19)$$

where  $TC$  is total cost;  $n$  is the number of crane;  $m$  is the number of supply points;  $o$  is the number of demand points;  $T_i$  is hook travel time by  $i$ th crane;  $T_{hi}$  is hook horizontal travel time by  $i$ th crane;  $Q_{jk}$  is quantity of material flow from  $S_j$  to  $D_k$ ;  $CU_i$  is cost of material flow from  $S_j$  to  $D_k$  per unit quantity and unit time by  $i$ th crane (defined value is \$1.92 [10]);  $\alpha_i$  is degree of coordination of hook movement in radial and tangential directions in horizontal plane by  $i$ th crane (defined value is 1 [9]);  $T_{vi}$  is hook vertical travel time by  $i$ th crane;  $V_{hi}$  is hoisting velocity of hook by  $i$ th crane (in this study setting the values are between 35 to 60 m/min [10]);  $\beta_i$  is the degree of coordination of hook movement in vertical and horizontal planes by  $i$ th crane (defined value is 0.25 [9]);  $T_{ai}$  is time for trolley radial movement by  $i$ th crane;  $V_{ai}$  is radial velocity of trolley by  $i$ th crane (in this study setting the values are between 33.1 to 53.3 m/min [10]);  $T_{wi}$  is time for trolley tangent movement by  $i$ th crane;  $l_i$  is distance between supply and demand points;  $V_{wi}$  is slewing velocity of jib (in this study setting the values are between 2.8 to

Table 7  
PBA best capacity of demand and supply points design.

		D1	D2	D3	D4	D5	D6	D7	D8	D9	Actual supply	Limit supply	Supply degree
C3	S1	237	0	0	208	0	231	96	0	114	886	1500	59%
	S2	154	0	111	0	0	0	82	227	0	574	1000	57%
	S3	97	151	0	179	264	0	0	314	252	1257	1500	84%
	S4	136	0	315	0	0	102	0	0	53	606	1000	61%
	S5	58	252	140	0	0	0	0	0	365	815	1500	54%
	S6	0	218	0	50	0	0	361	0	92	721	1000	72%
	S7	0	71	77	45	0	161	0	0	0	354	1500	24%
	S8	0	0	0	69	120	106	83	44	0	422	1000	42%
	S9	218	108	57	49	116	0	78	215	24	865	1500	58%
Total											6500	11,500	57%
Actual demand		900	800	700	600	500	600	700	800	900	6500		
Limit demand		900	800	700	600	500	600	700	800	900	6500		

**Table 8**  
Parameter values used in multi tower crane.

	CU	$\alpha$	$V_h$	$\beta$	$V_a$	$V_w$	M	DY	IS	MS	MST	RS	LC	LA
Crane #1	1.92	1	60	0.25	53.3	7.57	1000	80	5000	500	10	2000	100	5
Crane #2	1.92	1	35	0.25	33.1	2.8	1000	80	5000	500	10	2000	100	5

7.57 rad/min [10]);  $\rho(D_i)$  is horizontal distance from tower to demand point;  $\rho(S_i)$  is horizontal distance from tower to supply point;  $Cr_i(XCr_i, YCr_i, ZCr_i)$  is coordinate of tower crane;  $D_i(XD_i, YD_i, ZD_i)$  is coordinate of demand point  $i$ ;  $S_i(XS_i, YS_i, ZS_i)$  is coordinate of supply point  $i$ ;  $R$  is total rent cost;  $S$  is tower crane total setup cost;  $L$  is total labor cost;  $M_i$  is rent cost per month by  $i$ th crane (defined value is \$1000 [26]);  $DY_i$  is days of renting tower crane/labor work by  $i$ th crane (defined value is \$80 [26]);  $IS_i$  is tower crane initial setup cost (defined value is \$5000 [26]);  $MS_i$  is tower crane modified setup cost by  $i$ th crane (defined value is \$500 [26]);  $MST_i$  is modified setup times by  $i$ th crane (defined value is 10 [26]);  $RS_i$  is disassembly cost (defined value is \$2000 [26]);  $LC_i$  is labor cost per person by  $i$ th crane (defined value is \$100 [26]);  $LA_i$  is labor amount by  $i$ th crane (defined value is 5 person [26]).

Subject to

If actual supply capacities (i) > limit supply capacities (i) then  $TC = TC + 40,000$ .

If actual demand capacities (i) < limit demand capacities (i) then  $TC = TC + 40,000$ .

Notice: the objective function limit of actual supply capacities should be smaller or equal to limit supply capacities. Besides, the objective function limit of actual demand capacities should be equal to limit demand capacities. The subject will give a penalty when objective function breaks the above rules.

3.2. Results and discussion for the single-tower crane problem

This study was adapted from 30 experimental runs. The values listed in Table 4 are the results of 100, 300, 500, 1000 and 5000 iterations using BA, PSO, and PBA. The parameter values used for the single tower crane design are listed in Table 5. Table 6 and Fig. 4 present the evolution of the TCL problem result. As seen in Table 6, the best mean fitness and best solution for PBA are, respectively, 7.03E+05 and 5.41E+05. These values are better than those obtained using either BA (8.86E+05 and 8.35E+05) or PSO (8.68E+05 and 7.50E+05). Thus, PBA obtained a better evolution result than either BA or PSO.

**Table 9**  
The result of three algorithms.

	Iteration	Mean	Worst	Best	Std
PBA	100	1.34E+06	1.45E+06	1.22E+06	5.03E+04
	300	1.29E+06	1.44E+06	1.20E+06	6.77E+04
	500	1.27E+06	1.38E+06	1.07E+06	7.41E+04
	1000	1.23E+06	1.35E+06	1.07E+06	6.69E+04
	5000	<b>1.20E+06</b>	1.36E+06	1.06E+06	6.46E+04
	10,000	1.21E+06	1.28E+06	<b>1.03E+06</b>	5.55E+04
BA	100	1.51E+06	1.54E+06	1.48E+06	1.53E+04
	300	1.49E+06	1.52E+06	1.45E+06	1.59E+04
	500	1.48E+06	1.51E+06	1.45E+06	1.48E+04
	1000	1.46E+06	1.49E+06	1.43E+06	1.40E+05
	5000	1.44E+06	1.48E+06	<b>1.39E+06</b>	5.68E+05
	10,000	<b>1.43E+06</b>	1.46E+06	1.40E+06	1.66E+04
PSO	100	1.46E+06	1.55E+06	1.39E+06	3.64E+04
	300	1.44E+06	1.51E+06	1.39E+06	3.61E+04
	500	1.42E+06	1.51E+06	1.35E+06	4.00E+04
	1000	1.41E+06	1.46E+06	1.36E+06	2.67E+04
	5000	<b>1.38E+06</b>	1.47E+06	<b>1.30E+06</b>	4.42E+04
	10,000	1.39E+06	1.47E+06	1.31E+06	4.21E+04

Bold are the best Mean and best solution results of these mention algorithms.

Fig. 5 shows the optimal location alternative for the single tower crane, with the best tower crane location shown at C3. Table 7 shows the optimal design for demand and supply point capacities. As seen in Fig. 5 and Table 7, supply points S1 through S6 are closest to C3 and are thus associated with higher degrees of supply completion (886, 574, 1257, 606, 815, and 721, respectively) than S7 through S9 (354, 422, and 865, respectively), which are relatively more remote from C3. C8 was the best tower crane location identified in Ref. [11]. C3 and C8 are located very near one another. The prioritized supply points for Ref. [11] were points 1, 2, and 5, all of which are in close proximity to C8. Thus, this study obtained a solution very similar to Ref. [11]. Furthermore, the results demonstrate that PBA not only optimizes the tower crane location but also minimizes operating costs in line with demand and supply point capacity requirements.

3.3. Results and discussion for the multi-tower crane problem

In order to compare the cost inferences made for the single-tower-crane and multi-tower-crane problems in terms of the costs of rent, labor, and crane setup, this study also adapted the multi-tower-crane study from 30 experimental runs. The values listed in Table 4 are the results of 100, 300, 500, 1000 and 5000 iterations using BA, PSO, and PBA. The parameter values used for the single tower crane design are listed in Table 8. Table 9 and Fig. 6 present the evolution of the TCL problem result. As seen in Table 9, the best mean fitness and best solution for PBA are, respectively, 1.20E+06 and 1.03E+06, which are better than those obtained by either BA (1.43E+06 and 1.39E+06) or PSO (1.38E+06 and 1.30E+06). These results show that PBA obtained an evolution result that is better than either BA or PSO.

Fig. 7 shows the optimal location alternative for the multi-tower cranes, with the best tower crane locations shown at C5 and C9.

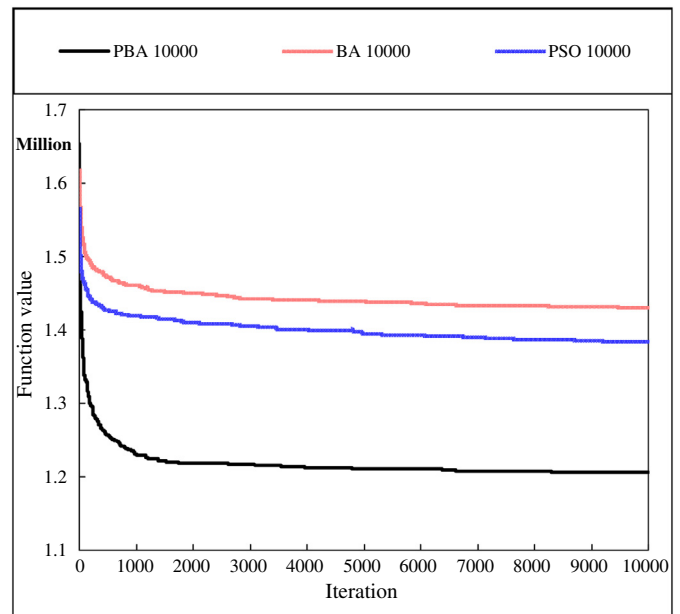


Fig. 6. Evolution of mean best values for multi TCL problem.

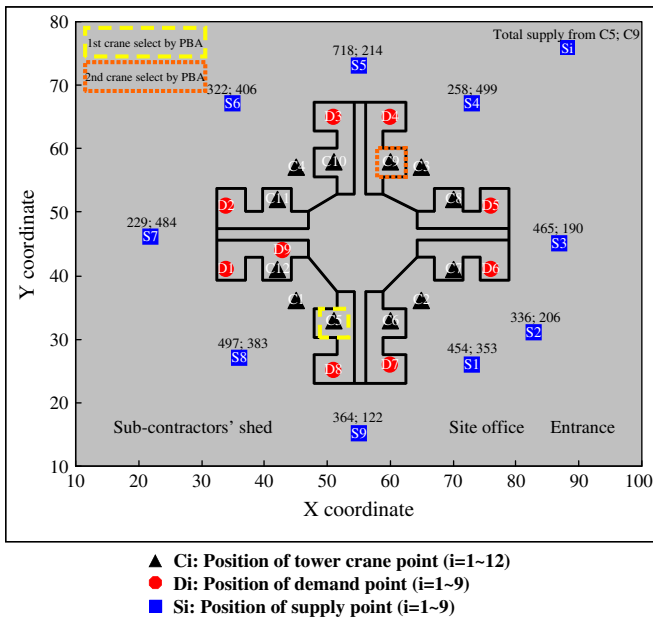


Fig. 7. PBA best multi tower crane layout design.

Table 10 shows the optimal design for demand and supply point capacities. Fig. 7 and Table 10 show that supply points S1, S2, and S7 through S9 are all close to location C5. Supply points S1, S2, S8, and S9 are associated with higher degrees of supply completion (454, 336, 497, and 364, respectively), while supply point S7 (229) is not. Furthermore, supply points S3 through S6 are all close to location C9, with supply points S4 and S6 associated with higher degrees of supply completion (499 and 406, respectively) and supply points S3 and S5 (190 and 214, respectively) associated with lower degrees. This result shows that while the PBA is able to optimize the tower crane location, the algorithm does not minimize the operating costs related to demand and supply point capacities in high-dimensional problems (the dimension in this case study is 164). Nevertheless, the single tower crane is the best overall choice in terms of total operation cost in this proposed practical TCL when rent, labor and, crane setup costs are factored into cost considerations.

Table 10  
PBA best capacity of demand and supply points design.

		D1	D2	D3	D4	D5	D6	D7	D8	D9	Actual supply	Limit supply	Supply degree
C5	S1	0	0	0	5	71	127	148	0	103	454	750	61%
	S2	119	66	0	0	20	0	0	0	131	336	500	67%
	S3	430	0	0	35	0	0	0	0	0	465	750	62%
	S4	0	88	170	0	0	0	0	0	0	258	500	52%
	S5	0	204	0	183	0	0	0	206	125	718	750	96%
	S6	0	0	54	129	89	0	0	50	0	322	500	64%
	S7	0	19	101	64	0	0	0	0	45	229	750	31%
	S8	39	27	0	0	166	78	0	107	80	497	500	99%
	S9	0	0	111	61	0	0	0	161	31	364	750	49%
	Total											3643	5750
C9	S1	118	127	0	0	0	0	37	0	71	353	750	47%
	S2	40	0	0	10	17	0	139	0	0	206	500	41%
	S3	0	18	0	0	0	0	0	93	79	190	750	25%
	S4	0	0	140	0	0	139	91	129	0	499	500	100%
	S5	21	0	65	21	0	73	34	0	0	214	750	29%
	S6	133	26	46	0	0	0	92	0	109	406	500	81%
	S7	0	225	13	26	56	0	125	0	39	484	750	65%
	S8	0	0	0	47	81	114	0	54	87	383	500	77%
	S9	0	0	0	19	0	69	34	0	0	122	750	16%
	Total											2857	5750
Actual demand		900	800	700	600	500	600	700	800	900	6500		
Limit demand		900	800	700	600	500	600	700	800	900	6500		

## 4. Conclusion and recommendation

### 4.1. Conclusion

This study compared the relative performance of the particle bee algorithm (PBA), particle swarm optimization (PSO), and bee algorithm (BA) in resolving a proposed hypothetical tower crane layout (TCL) problem. Results show that the PBA performed better than the other two algorithms. In the single-tower crane design section, the best mean fitness and best solution for PBA were  $7.03E+05$  and  $5.41E+05$ , respectively, which were better than the solutions obtained by BA ( $8.86E+05$  and  $8.35E+05$ ) and PSO ( $8.68E+05$  and  $7.50E+05$ ). This result shows that the PBA not only optimizes the location of the tower crane but also minimizes the operating costs for the demand and supply point capacities. In the multi-tower crane design section, the best mean fitness and best solution for PBA were  $1.20E+06$  and  $1.03E+06$ , respectively, which were better than the solutions obtained by BA ( $1.43E+06$  and  $1.39E+06$ ) and PSO ( $1.38E+06$  and  $1.30E+06$ ). This result indicates that although the PBA performs well in optimizing the location of tower cranes, the algorithm is unable to minimize operating costs for the demand and supply point capacities for high-dimensional problems. From the perspective of total operation cost, the single-tower crane is the overall best choice in this practical case study when rent, labor and, crane setup costs are factored into cost considerations.

### 4.2. Recommendation

Factors considered in the alternative approach to tower-crane layout design and device selection include the maximum carrying load of crane hooks and the maximum radius of the crane. This study assumes that the selected tower crane is able to handle the maximum weight of materials and covers the entire work area and thus ignores maximum material weight and the maximum radius of the crane as optimization design factors. Nevertheless, these issues are practical tower crane layout problems faced on the construction site and may be interesting topics for future research.

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## References

- [1] J.J. Michalek, R. Choudhary, P.Y. Papalambros, Architectural layout design optimization, *Eng. Optim.* 34 (5) (2002) 461–484.
- [2] E. Elbeitagi, T. Hegazy, A hybrid AI-based system for site layout planning in construction, *Comput. Aided Civ. Infrastruct. Eng.* 16 (2) (2001) 79–93.
- [3] I.-C. Yeh, Architectural layout optimization using annealed neural network, *Autom. Constr.* 15 (4) (2006) 531–539.
- [4] H. Li, P.E.D. Love, Genetic search for solving construction site-level unequal-area construction site layout problems, *Autom. Constr.* 9 (2) (2000) 217–226.
- [5] H.M. Osman, M.E. Georgy, M.E. Ibrahim, A hybrid CAD-based construction site layout planning system using genetic algorithms, *Autom. Constr.* 12 (6) (2003) 749–764.
- [6] T. Hegazy, E. Elbeltagi, EvoSite: evolution-based model for site layout planning, *J. Comput. Civ. Eng.* 13 (3) (1999) 198–206.
- [7] E. Elbeitagi, T. Hegazy, A.H. Hosny, A. Eldosouky, Schedule-dependent evolution of site layout planning, *Constr. Manag. Econ.* 19 (7) (2001) 689–697.
- [8] C.M. Tam, K.L. Tong Thomas, GA-ANN model for optimizing the locations of tower crane and supply points for high-rise public housing, *Constr. Manag. Econ.* 21 (3) (2003) 257–266.
- [9] P. Zhang, F.C. Harris, P.O. Olomolaiye, G.D. Holt, Location optimization for a group of tower cranes, *J. Constr. Eng. Manag.* 125 (2) (1999) 115–122.
- [10] C.M. Tam, K.L. Tong Thomas, Wilson K.W. Chan, Genetic algorithm for optimizing supply locations around tower crane, *J. Constr. Eng. Manag.* 127 (4) (2001) 315–321.
- [11] C. Huang, C.K. Wong, C.M. Tam, Optimization of tower crane and material supply location in a high-rise building site by mixed-integer linear programming, *Autom. Constr.* 20 (5) (2011) 571–580.
- [12] E. Bonabeau, M. Dorigo, G. Theraulaz, *Swarm Intelligence: From Natural to Artificial Intelligence*, Oxford University Press, New York, 1999.
- [13] M. Dorigo, *Optimization, Learning and Natural Algorithms*, Ph.D. Thesis Politecnico di Milano, Italy, 1992.
- [14] X.L. Li, A New Intelligent Optimization-artificial Fish Swarm Algorithm, Ph.D. Thesis Zhejiang University of Zhejiang, China, 2003.
- [15] J. Kennedy, R.C. Eberhart, Particle swarm optimization, In *Proceedings of the 1995 IEEE International Conference on Neural Networks*, Vol. 4, 1995, pp. 1942–1948.
- [16] D.T. Pham, E. Koc, A. Ghanbarzadeh, S. Otri, S. Rahim, M. Zaidi, The bees algorithm — a novel tool for complex optimization problems, In *Proceedings of the Second International Virtual Conference on Intelligent Production Machines and Systems*, 2006, pp. 454–461.
- [17] D.T. Pham, M. Castellani, The bees algorithm: modelling foraging behaviour to solve continuous optimization problems, *Proc. Inst. Mech. Eng. C J. Mech. Eng. Sci.* 223 (12) (2009) 2919–2938.
- [18] B. Yuce, M.S. Packianather, E. Mastrocinque, D.T. Pham, A. Lambiasi, Honey bees inspired optimization method: the bees algorithm, *Insects* 4 (2013) 646–662.
- [19] X.S. Yang, Engineering optimizations via nature-inspired virtual bee algorithms, *Lect. Notes Comput. Sci* 3562 (2005) 317–323.
- [20] D. Karaboga, B. Akay, A comparative study of artificial Bee colony algorithm, *Appl. Math. Comput.* 214 (2009) 108–132.
- [21] B. Basturk, D. Karaboga, An artificial Bee colony (ABC) algorithm for numeric function optimization, *IEEE Swarm Intelligence Symposium 2006*, Indianapolis, Indiana, USA, 2006.
- [22] L. Ozbakir, A. Baykasog, P. Tapkan, Bees algorithm for generalized assignment problem, *Appl. Math. Comput.* 215 (2010) 3782–3795.
- [23] K.E. Parsopoulos, M.N. Vrahatis, Parameter selection and adaptation in unified particle swarm optimization, *Math. Comput. Model.* 46 (1) (2007) 198–213.
- [24] T. Korenaga, T. Hatanaka, K. Uosaki, Improvement of particle swarm optimization for high-dimensional space, 2006 SICE-ICASE International Joint Conference, 2006.
- [25] M.Y. Cheng, L.C. Lien, A hybrid AI-based particle bee algorithm (PBA) for benchmark functions and facility layout optimization, *J. Comput. Civ. Eng.* 26 (5) (2012) 612–624.
- [26] M.Y. Cheng, J.C. Chen, Integrating barcode and GIS for monitoring construction progress, *Autom. Constr.* 11 (1) (2002) 23–33.