Decomposition of Timed Decision Tables and its Use in Presynthesis Optimizations

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Abstract − *Presynthesis optimizations transform a behavioral HDL description into an optimized HDL description that results in improved synthesis results. In this paper we introduce the decomposition of Timed Decision Tables (TDT), a tabular model of system behavior. The TDT decomposition is based on the kernel extraction algorithm. By experimenting using named benchmarks, we demonstrate how TDT decomposition can be used in presynthesis optimizations.*

1 Introduction

Presynthesis optimizations have been introduced in [1] as source-level transformations that produce "better" HDL descriptions. For instance, these transformations are used to reduce control-flow redundancies and make synthesis result relatively insensitive to the HDL coding-style. They are also used to reduce resource requirements in the synthesized circuits by increasing component sharing at the behavior-level [2].

The TDT representation consists of a main table holding a set of rules (similar to the specification in a FSMD [3]), an auxiliary table which specifies concurrencies, data dependencies, and serialization relations among data-path computations, or *actions*, and a delay table which specifies the execution delay of each action.

The rule section of the model is based on the notions of *condition* and *action*. A condition may be the presence of an input, or the outcome of a test condition. A conjunction of several conditions defines a *rule*. A decision table is a collection of rules that map condition conjunctions into sets of actions. Actions include logic, arithmetic, input-output(IO), and message-passing operations. We associate an execution delay with each action. Actions are grouped into action sets, or compound actions. With each action set, we associate a

concurrency type of *serial, parallel*, or *data-parallel* [4]. The structure of the rule section can be found in [1]

In additional to the set of rules specified in a main table (the rule section), the TDT representation includes two auxiliary tables to hold additional information about the execution delay of each action, serialization, data dependency, and concurrency type between each pair of actions.

Example 1.1. Consider the following TDT:

c_1	Y	Y	N	
c_2	Y	N	X	**delay**
$a_{1,1}$	1	0	0	1
$a_{1,2}$	1	0	0	3
$a_{2,1}$	0	1	0	4
$a_{2,2}$	0	1	0	2
$a_{3,1}$	0	0	1	6
$a_{3,2}$	0	0	1	1

	$a_{1,1}$	$a_{1,2}$	$a_{2,1}$	$a_{2,2}$	$a_{3,1}$	$a_{3,2}$
$a_{1,1}$		s				
$a_{1,2}$						
$a_{2,1}$				d		
$a_{2,2}$						
$a_{3,1}$						p
$a_{3,2}$						

An 'X' in the condition column indicates a Don't Care associated with the particular condition. When c_1 = 'Y' and c_2 = 'Y', actions $a_{1,1}$ and $a_{1,2}$ are selected for execution. Since action $a_{1,2}$ is specified as a successor of $a_{1,1}$, action $a_{1,1}$ is executed with a one cycle delay followed by the execution of $a_{1,2}$. Symbols 'd' and 'p' indicate actions that are data-parallel and parallel actions respectively. □

The execution of a TDT consists of two steps: (1) select a rule to apply, (2) execute the action sets that the selected rule maps to. More than two action sets may be selected for execution. The order in which to execute those action sets are determined by the concurrency types, serialization relations, and data dependencies specified among those action sets [4], indicated by 's', 'd', and 'p' in the table above. An action in a TDT may be another TDT. This is referred to as a *call* to the TDT contained as an action in the calling TDT.

Example 1.2. Consider the following calling hierarchy:

TDT_1

c_1	Y	N
a_1	1	0
TDT_2	0	1

TDT_2

c_2	Y	N
a_2	1	0
a_3	0	1

0

When $c_1 = $ 'N' the action needs to be invoked is the call to TDT_2, forces evaluation of condition c_2 resulting in actions a_2 or a_3 being executed. No additional information such as concurrency types needs to be specified between action a_1 and TDT_2 since they lie on different control paths. □

Procedure/function calling hierarchy in input HDL descriptions results in a corresponding TDT hierarchy. TDTs in a calling hierarchy are typically merged to increase the scope of presynthesis optimizations. Merging flattens the calling hierarchy specified in original HDL descriptions. In this paper we present TDT decomposition which is the reverse of the merging process. By first flattening the calling hierarchy and then extracting the commonalities, we may find a more efficient behavior representation which leads to improved synthesis results. This allows us to restructure HDL code. In this paper, we introduce HDL code-restructuring using TDT merging and decomposition transformations. This optimization belongs to a group of presynthesis optimizations such as column/row reduction and action sharing that have been presented earlier [1, 4, 2].

This paper is organized as follows. The next section introduces the notion of TDT decomposition and relates it to the problem of kernel extraction in an algebraic representation of TDTs. Section 3 presents an algorithm for TDT decomposition based on kernel extraction. Section 4 shows the implementation details of the algorithm and presents the experimental results. Finally, Section 5 concludes and presents our future plan.

2 TDT Decomposition

TDT decomposition is the process of replacing a flattened TDT with a hierarchical TDT that represents an equivalent behavior. As we mentioned earlier, decomposition is the reverse process of merging and together with merging, it allows us to produce HDL descriptions that are optimized for subsequent synthesis tasks and are relatively insensitive to coding styles. Since this decomposition uses procedure calling abstraction, arbitrary partitions of the table (condition/action) matrices are not useful.

Example 2.1. Consider the following TDT.

c_1	Y	Y	Y	Y	Y	Y	Y	Y	N	N	N	N
c_2	Y	Y	Y	N	N	N	N	N				
c_3				Y	Y	Y	Y	N				
c_4	Y	N	N									
c_5		Y	N									
c_6				Y	Y	N	N		Y	Y	N	N
c_7				Y	N	Y	N		Y	N	Y	N
a_1	1	1	1					1	1	1	1	1
a_2	1	1	1	1	1	1	1		1	1	1	1
a_3	1		1									
a_4	1											
a_5	1	1										
a_6				1		1			1		1	
a_7				1	1	1			1	1	1	
a_8				1	1		1		1	1		1
a_9								1				

Notice the common patterns in condition rows in c_6 and c_7, and action rows in a_6, a_7, and a_8. □

Above in Example 2.1 is a flattened TDT. The first three columns have identical condition entries in c_1 and c_2, and identical action entries in a_1 and a_2. These columns differ in rows corresponding to conditions $\{c_4, c_5\}$ and actions $\{a_3, a_4, a_5\}$, which appear only in the first three columns. This may result, for example, from merging a sub-TDT consisting of only conditions $\{c_4, c_5\}$ and actions $\{a_3, a_4, a_5\}$.

Figure 1 shows a hierarchy of TDTs which specify the same behavior as Example 2.1. The equivalence can be verified by merging the hierarchy of TDTs [4]. Note that the conditions and actions are partitioned among these TDTs.

TDT_1:

c_1	Y	Y	Y	N
c_2	Y	N	N	
c_3		Y	N	
a_1	1		1	1
a_2	1	1		1
TDT_2	1			
TDT_3		1		1
a_9			1	

TDT_2:

c_4	Y	N	N
c_5		Y	N
a_3	1		1
a_4	1		
a_5	1	1	

TDT_3:

c_6	Y	Y	N	N
c_7	Y	N	Y	N
a_6	1		1	
a_7	1	1	1	
a_8	1	1		1

Figure 1: One possible decomposition of the TDT in Example 2.1.

The commonality in the flattened TDT may not result from multiple calls to a procedure as indicated by TDT_3 in Figure 1. It could also be a result of commonality in the input HDL specification. If this is the case, extraction will lead to a size reduction in the synthesized circuit.

It is not always possible to decompose a given TDT into a hierarchical TDT as shown in Figure 1 above. Neither is it always valid to merge the TDT hierarchy into flattened TDT [4]. These two transformations are valid only when the specified concurrency types, data dependencies, and serializations are preserved. In this particular example, we assume that the order of execution of all actions follows the order in which they appear in the condition stub. For the transformations to be valid, in this particular example, we also note that the actions a_1 and a_2 do not modify conditions in called TDTs namely c_4 through c_7.

The structural requirements for TDT decomposition can be efficiently captured by a two-level algebraic representation of TDTs [2]. This representation only captures the control dependencies in action sets and hence is strictly a sub set of TDT information. We also restrict the TDT model to only limited-entry forms, one where actions matrix is a Boolean matrix. The utility of this form has been demonstrated earlier with respect to modeling of exception conditions [4]. For each con-

dition variable c, we define a positive condition literal, denoted as l_c, which corresponds to an 'Y' value in a condition entry. We also define a negative condition literal, denoted as $l_{\bar{c}}$, which corresponds to an 'N' value in a condition entry.

We define a '·' operator between two action literals and two conditions literals which represents a conjunction operation. This operation is both commutative and associative [4].

A TDT is a set of rules, each of which consists of a condition part which determines when the rule is selected, and an action part which lists the actions to be executed once a rule is selected for execution. The condition part of a rule is represented as

$$\prod_{ce(i)\neq\text{`}X\text{'};\; i=1,ncond} \kappa_i \tag{1}$$

$$\kappa_i \;=\; \left\{ \begin{array}{l} l_{c_i}, \text{when } ce(i) = \text{`Y'} \\ l_{\bar{c}_i}, \text{when } ce(i) = \text{`N'} \end{array} \right.$$

where $ncond$ is the number of conditions in the TDT and $ce(i)$ is the condition entry value at the ith condition row for this rule. The action part of a rule is represented as

$$\prod_{ae(i)\neq\text{`}0\text{'};\; i=1,nact} l_{a_i} \tag{2}$$

where $nact$ is the number of actions in the TDT and $ae(i)$ is the action entry value at the ith action row for this rule. A rule is a tuple, denoted by

$$(\mathcal{K} : \alpha)$$

As will become clear later, for the purpose of TDT decomposition a rule can be expressed as a product of corresponding action and condition literals. We call such a product a *cube*. For a given TDT, T, we define an algebraic expression, E_T, that consists of disjunction of cubes corresponding to rules in T.

For simplicity, we can drop the '·' operator and ':' denotation and use 'c' or 'a' instead of l_c and l_a in the algebraic expressions of TDTs. These symbols follow only algebraic laws for symbolic computation. For treatment of this algebra, the reader is referred to [4].

Example 2.2. Here is the algebraic expression for the TDT in Example 2.1.

$E_{TDT\ 2.1}$
$=\quad c_1 c_2 c_4 a_1 a_2 a_3 a_4 a_5 + c_1 c_2 \bar{c}_4 c_5 a_1 a_2 a_5$
$+\quad c_1 c_2 \bar{c}_4 \bar{c}_5 a_1 a_2 a_3 + c_1 \bar{c}_2 c_3 c_6 c_7 a_2 a_6 a_7 a_8$
$+\quad c_1 \bar{c}_2 c_3 c_6 \bar{c}_7 a_2 a_7 a_8 + c_1 \bar{c}_2 c_3 \bar{c}_6 c_7 a_2 a_6 a_7$
$+\quad c_1 \bar{c}_2 c_3 \bar{c}_6 \bar{c}_7 a_2 a_8 + c_1 \bar{c}_2 \bar{c}_3 a_1 a_9$
$+\quad \bar{c}_1 c_6 c_7 a_1 a_2 a_6 a_7 a_8 + \bar{c}_1 c_6 \bar{c}_7 a_1 a_2 a_7 a_8$
$+\quad \bar{c}_1 \bar{c}_6 c_7 a_1 a_2 a_6 a_7 + \bar{c}_1 \bar{c}_6 \bar{c}_7 a_1 a_2 a_8$

Note that there is no specification on delay, concurrency type, serialization relation, and data dependency. Also notice that 'c', '$\bar{c}$', and 'a' are short-hand notations for 'l_c', '$l_{\bar{c}}$', 'l_a' respectively. □

2.1 Kernel Extraction

During TDT decomposition, it is important to keep an action literal or condition literal within one sub-TDT, that is, the decomposed TDTs must partition the condition and action literals. To capture this, we introduce the notion of *TDT support*.

Definition 2.1 The **TDT-support** of an expression E_T is the set of action literals in E_T and positive condition literals corresponding to condition literals that appear in E_T.

Example 2.3. Expression $c_1 \bar{c}_2 c_3 \bar{c}_6 \bar{c}_7 a_2 a_8$ is a cube. Its TDT support is $\{c_1, c_2, c_3, c_6, c_7, a_1, a_8\}$. □

We consider here TDT decompositions into sub-TDTs that have disjoint TDT-supports. TDT decomposition uses algebraic division of TDT-expressions to identify sub TDTs. We define the algebraic division as follows:

Definition 2.2 Let $\{f_{dvnd}, f_{dvsr}, f_{quot}, f_{rem}\}$ be algebraic expressions. We say that f_{dvsr} is an **algebraic divisor** of f_{dvsr} when we have $f_{dvnd} = f_{dvsr} \cdot f_{quot} + f_{rem}$, the TDT-support of f_{dvsr} and the TDT-support of f_{quot} are disjoint, and $f_{dvsr} \cdot f_{quot}$ is non-empty.

An algebraic divisor is called a *factor* when the remainder is void. An expression is said to be *cube free* when it cannot be factored by a cube.

Definition 2.3 A **kernel** of an expression is a cube-free quotient of the expression divided by a cube, which is called the **co-kernel** of the expression.

Example 2.4. Rewrite the algebraic form of $TDT_{Example\ 2.1}$ as follows.

$E_{TDT2.1}$
$=\quad c_1 c_2 a_1 a_2 (c_4 a_3 a_4 a_5 + \bar{c}_4 c_5 a_5 + \bar{c}_4 \bar{c}_5 a_3)$
$+\quad c_1 \bar{c}_2 c_3 a_2 (c_6 c_7 a_6 a_7 a_8 + c_6 \bar{c}_7 a_7 a_8 + \bar{c}_6 c_7 a_6 a_7 + \bar{c}_6 \bar{c}_7 a_8)$
$+\quad c_1 \bar{c}_2 \bar{c}_3 a_1 a_9$
$+\quad \bar{c}_1 a_1 a_2 (c_6 c_7 a_6 a_7 a_8 + c_6 \bar{c}_7 a_7 a_8 + \bar{c}_6 c_7 a_6 a_7 + \bar{c}_6 \bar{c}_7 a_8)$

The expression $c_4 a_3 a_4 a_5 + \bar{c}_4 c_5 a_5 + \bar{c}_4 \bar{c}_5 a_3$ is a kernel of $TDT_{Example\ 2.1}$ with a corresponding co-kernel $c_1 c_2 a_1 a_2$. Similarly, $c_6 c_7 a_6 a_7 a_8 + c_6 \bar{c}_7 a_7 a_8 + \bar{c}_6 c_7 a_6 a_7 + \bar{c}_6 \bar{c}_7 a_8$ is also a kernel of $TDT_{Example\ 2.1}$, with two corresponding co-kernels: $c_1 \bar{c}_2 c_3 a_2$ and $\bar{c}_1 a_1 a_2$. □

3 Algorithm for TDT Decomposition

This section presents an algorithm for TDT decomposition. The core of the algorithm is similar to the techniques used in multi-level logic optimization. Therefore we first discuss how to compute algebraic kernels from TDT-expressions before we show the complete algorithm which calls the kernel computing core and addresses some important issues such as preserving data-dependencies between actions through TDT decomposition.

3.1 Algorithms for Kernel Extraction

A naive way to compute the kernels of an expression is to divide it by the cubes corresponding to the power set of its support set. The quotients that are not cube free are weeded out, and the others are saved in the kernel set [5]. This procedure can be improved in two ways: (1) by introducing a recursive procedure that exploits the property that a kernel of a kernel of an expression is also the kernel of this expression, (2) by reducing the search by exploiting the commutativity of the '·' operator. Algorithm 3.1 shows a method adapted from a kernel extraction algorithm due to Brayton and McMullen [6], which takes into account the above two properties to reduce computational complexity.

Algorithm 3.1 A Recursive Procedure Used in Kernel Extraction

INPUT: a TDT expression e, a recursion index j;
OUTPUT: the set of kernels of TDT expression e;
extractKernelR(e, j) {
   $K = 0$;
   for $i = j$ to n **do**
     if $(| \text{getCubeSet}(e, l_i)| \geq 2)$ **then**
       C = largest cube set containing l_i s.t.
         $\text{getCubeSet}(e, C) = \text{getCubeSet}(e, l_i)$;
       if $(l_k \notin C \; \forall k < i)$ **then**
         $K = K \cup extractKernelR(e/e^C, i + 1)$
   endfor
   $K = K \cup e$;
   return(K);
}

In the above algorithm, $getCubeSet(e, C)$ returns the set of cubes of e whose support includes C. We order the literals so that condition literals appear before action literals. We use n as the index of the last condition literal since a co-kernel containing only action literals does not correspond a valid TDT decomposition. Notice that l_c and $l_{\bar{c}}$ are two different literals as we explained earlier. The algorithm is applicable to cube-free expressions. Thus, either the function e is cube-free or it is made so by dividing it by its largest cube factor, determined by the intersection of the support sets of all its cubes.

Example 3.1. After running Algorithm 3.1 on the algebraic expression of $TDT_{2.1}$ we get the following kernels:

$$
\begin{aligned}
k_1 &= E_{TDT\,2.1}; \\
k_2 &= c_2 a_1 a_2 c_4 a_3 a_4 a_5 + c_2 a_1 a_2 \bar{c}_4 c_5 a_5 + c_2 a_1 a_2 \bar{c}_4 \bar{c}_5 a_3 \\
&+ \bar{c}_2 c_3 a_2 c_6 c_7 a_6 a_7 a_8 + \bar{c}_2 c_3 a_2 c_6 \bar{c}_7 a_7 a_8 + \bar{c}_2 c_3 a_2 \bar{c}_6 c_7 a_6 a_7 \\
&+ \bar{c}_2 c_3 a_2 \bar{c}_6 \bar{c}_7 a_8; \\
k_3 &= c_4 a_3 a_4 a_5 + \bar{c}_4 c_5 a_5 + \bar{c}_4 \bar{c}_5 a_3; \\
k_4 &= c_6 c_7 a_6 a_7 a_8 + c_6 \bar{c}_7 a_7 a_8 + \bar{c}_6 c_7 a_6 a_7 + \bar{c}_6 \bar{c}_7 a_8; \\
k_5 &= c_5 a_5 + \bar{c}_5 a_3; \\
k_6 &= c_7 a_6 + \bar{c}_7; \\
k_7 &= c_7 a_6 a_7 + \bar{c}_7 a_8;
\end{aligned}
$$

Note that k_6 has a cube with no action literals. This represents a TDT rule with no action selected for execution. □

3.2 TDT Decomposition

Our TDT decomposition scheme works as follows. First, the algebraic expression of a TDT is constructed. Then a set of kernels are extracted from the algebraic expression. The kernels are eventually used to reconstruct a TDT representation in hierarchical form. Not all the algebraic kernels may be useful in TDT decomposition since the algebraic expression carries only a subset of the TDT information. We use a set of filtering procedures to delete from the kernel sets kernels which corresponds to invalid TDT transformations or transformations producing models that results in inferior synthesis results.

Algorithm 3.2 TDT Decomposition

INPUT: a flattened TDT tdt;
OUTPUT: a hierarchical TDT with root tdt';
decomposeTDT(tdt)
{
   $sop \leftarrow$constructAlgebraicExpression(tdt);
   $K \leftarrow$extractKernel(sop);
   trimKernel1(K, sop);
   trimKernel2(K, sop, td);
   trimSelf(k, sop);
   trimKernel3(k, sop);
   $tdt' \leftarrow$reconstruct_TDT_with_Kernels(tdt, K);
   return tdt'
}

The procedure $constructAlgebraicExpression()$ builds the algebraic expression of tdt following Algorithm 3.3. The function $expression()$ builds an expression out of a set of sets according to the data structure we choose for the two-level algebraic expression for TDTs. The complexity of the algorithm is $O(AR + CR)$ where A is the number of action in tdt, R is the number of rules in tdt, and C is the number of conditions in tdt.

Algorithm 3.3 Constructing Algebraic Expressions of TDTs

constructAlgebraicExpression(tdt) {
   for $i = 1$, C **do**
     construct a positive condition literal l_{c_i};
     construct a negative condition literal $l_{\bar{c}_i}$;
   endfor
   for $i = 1$, A **do**
     construct an action literal l_{a_i}
   endfor
   $R \leftarrow \phi$; // empty set
   for $i = 1$, R **do**
     $r \leftarrow \phi$;
     for $j = 1$, C **do**
       if $(ce(i, j) == \text{'Y'})$ **then**

$r \leftarrow r \cup \{l_{c_i}\};$
    if $(ce(i,j) == \text{'N'})$ **then**
      $r \leftarrow r \cup \{l_{\bar{c}_i}\};$
   endfor;
    $R \leftarrow R \cup r;$
  endfor
  return expression(R);
}

Procedure $extractKernel(sop)$ calls the recursive procedure $extractKernelR(sop, 1)$ to get a set of kernels of sop, the algebraic expression of tdt.

Some kernels appear only once in the algebraic expression of a TDT. These kernels would not help in reducing the resource requirement and therefore they are trimmed from K using procedure $trimKernel1()$. The number of co-kernels corresponds to the number of times sub-TDT that corresponds to a certain kernel is called in the hierarchy of TDTs.

Since information such as data dependency are not captured in algebraic form of TDTs, the kernels in K may not corresponds to a decomposition which preserves data-dependencies specified in the original TDT. These kernels are trimmed using procedure $trimKernel2()$.

Algorithm 3.4 Removing Kernels Which Corresponds to an Invalid TDT Transformations

$trimKernel2(K, e, tdt)$ {
  foreach $k \in K$ **do**
    flag $\leftarrow 0;$
    foreach $q \in co - Kernels(k, e)$ **do**
      foreach *action literal* l_a *of* q **do**
        if *a modifies any condition of* k **then**
          foreach *action literal* l_α *in* k **do**
            if $(l_a$ *appears before* $l_\alpha)$ **then**
              flag $\leftarrow 1;$
          endforeach
        endforeach
      endforeach
    if *(flag == 0)* **then**
      $K \leftarrow K - \{k\};$
  endforeach
}

The worst case complexity of this algorithm is $O(AR + CR)$ since the program checks no more than once on each condition/action literal corresponding to a condition entry or action entry of tdt.

Example 3.2. Now we look at kernel $k_4 = c_6 c_7 a_6 a_7 a_8 + c_6 \bar{c}_7 a_7 a_8 + \bar{c}_6 c_7 a_6 a_7 + \bar{c}_6 \bar{c}_7 a_8$. Suppose it corresponds to TDT_3. Also suppose in Example 2.1, a_2 modifies c_6 and the result of a_2 is also used in a_6. Because a_2 modifies c_6, in the hierarchical TDT we need to specify that a_2 comes after TDT_3 to preserve the behavior. However, this violates the data dependency specification between a_2 and a_6. Therefore,

under this condition given above, k_4 will be eliminated by $trimKernel2()$. □

An expression may be a kernel of itself with a co-kernel of '1' if it is kernel free. However this kernel is not useful for TDT decomposition. We use a procedure $trimSelf()$ to delete an expression from its own kernel set for TDT decomposition. Also, as we mentioned earlier, a kernel of an expression's kernel is itself a kernel of this expression. However, in this paper, we consider TDT decomposition involving only two levels of calling hierarchies at a time. For this reason, we use $trimKernel3()$ delete "smaller" kernels which are also kernels of other kernels of an expression.

Finally, we reconstruct a hierarchical TDT representation using the remaining algebraic kernels of the TDT expression. The algorithm is outlined below. It consists two procedures: $reconstruct\_TDT\_with\_Kernel()$, and $constructTDT()$ which is called by the other procedure to build a TDT out of an algebraic expression. Again, the worse case complexity of the algorithm is $O(CR + AR)$.

Algorithm 3.5 Construct a Hierarchical TDT Using Kernels

INPUT: a flattened TDT tdt, its algebraic expression exp, a set of kernels K of exp;
OUTPUT: a new hierarchical TDT;
re_Construct_TDT_with_Kernels(tdt, K, exp) {
  foreach $k \in K$ **do**
    $t \leftarrow$ constructTDT(tdt, k)
    generate a new action literal l_t for t;
    compute q and r s.t. $exp = k \cdot q + r$;
    $e \leftarrow l_t \cdot q + r$;
  endforeach
  return constructTDT(tdt, e);
}

Example 3.3. Assume expression $c_6 c_7 a_6 a_7 a_8 + c_6 \bar{c}_7 a_7 a_8 + \bar{c}_6 c_7 a_6 a_7 + \bar{c}_6 \bar{c}_7 a_8$ is the only kernel left after trimming procedures performed on the kernel set of the algebraic expression of $TDT_{Example\ 2.1}$. The following hierarchical TDT will be constructed.

TDT_1:

c_1	Y	Y	Y	Y	Y	N
c_2	Y	Y	Y	N	N	
c_3				Y	N	
c_4	Y	N	N			
c_5		Y	N			
a_1	1	1	1		1	1
a_2	1	1	1	1		1
a_3	1		1			
a_4	1					
a_5	1	1				
TDT_3				1		1
a_9					1	

TDT_3:

c_6	Y	Y	N	N
c_7	Y	N	Y	N
a_6	1		1	
a_7	1	1	1	
a_8	1	1		1

□

4 Implementation and Experimental Results

To show the effect of using TDT decomposition in presynthesis optimizations, we have incorporated our decomposition algorithm in PUMPKIN, the TDT-based presynthesis optimization tool [4]. Figure 2 shows the flow diagram of the process of presynthesis optimizations. The ellipse titled "kernel extraction" in Figure 2 shows where the TDT decomposition algorithm fits in the global picture of presynthesis optimizations using TDT.
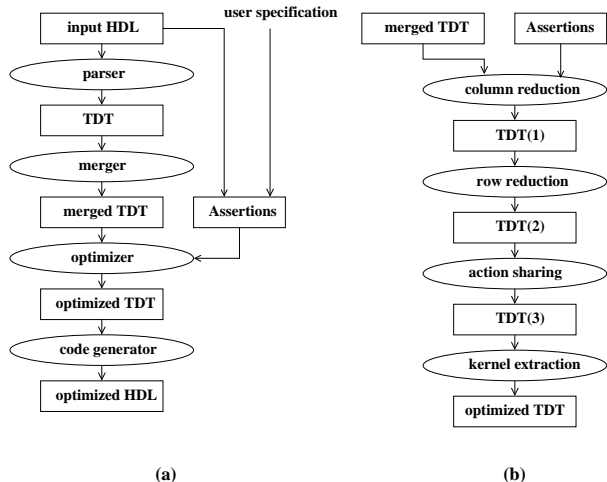

Figure 2: Flow diagram for presynthesis optimizations: (a) the whole picture, (b) details of the optimizer.

Our experimental methodology is as follows. The HDL description is compiled into TDT models, run through the optimizations, and finally output as a HardwareC description. This output is provided to the Olympus High-Level Synthesis System [7] for hardware synthesis under minimum area objectives. We use Olympus synthesis results to compare the effect of optimizations on hardware size. Hardware synthesis was performed for the target technology of LSI Logic 10K library of gates. Results are compared for final circuits sizes, in terms of number of cells. To evaluate the effectiveness of this step, we have turned off other optimizations and run PUMPKIN with several high-level synthesis benchmark designs.

Table 1 shows the results of TDT decomposition on examples designs. The design 'daio' refers to the HardwareC design of a Digital Audio Input-Output chip (DAIO) [8]. The design 'comm' refers to the HardwareC design of an Ethernet controller [9]. The design 'cruiser' refers to the HardwareC design of a vehicle controller. The description 'State' is the vehicle speed regulation module. All designs can be found in the high-level synthesis benchmark suite [7]. The percentage of circuit size reduction is computed for each description and listed in the last column of Table 1. Note that this improvement depends on the amount of commonality existing in the input behavioral descriptions.

Table 1: Synthesis Results: cell counts before and after TDT decomposition is carried out.

design	module	circuit size (cells)		Δ%
		before	after	
daio	phase_decoder	1252	1232	2
	receiver	440	355	19
comm	DMA_xmit	992	770	22
	exec_unit	864	587	32
cruiser	State	356	308	14

5 Conclusion and Future Work

In this paper, we have introduced TDT decomposition as a complementary procedure to TDT merging. We have presented a TDT decomposition algorithm based on kernel extraction on an algebraic form of TDTs. Combining TDT decomposition and merging, we can restructure HDL descriptions to obtain descriptions that lead to either improved synthesis results or more efficient compiled code. Our experiment on named benchmarks shows a size reduction in the synthesized circuits after code restructuring.

As a future work, we are exploring HDL optimization strategies based various presynthesis optimization techniques that lead to best synthesis results.

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