Upper limits from the LIGO and TAMA detectors on the rate of gravitational-wave bursts

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We report on the first joint search for gravitational waves by the TAMA and LIGO collaborations. We looked for millisecond-duration unmodelled gravitational-wave bursts in 473 hr of coincident data collected during early 2003. No candidate signals were found. We set an upper limit of 0.12 events per day on the rate of detectable gravitational-wave bursts, at 90% confidence level. From simulations, we estimate that our detector network was sensitive to bursts with root-sum-square strain amplitude above approximately $1-3 \times 10^{-19} \text{ Hz}^{-1/2}$ in the frequency band 700-2000 Hz. We describe the details of this collaborative search, with particular emphasis on its advantages and disadvantages compared to searches by LIGO and TAMA separately using the same data. Benefits include a lower background and longer observation time, at some cost in sensitivity and bandwidth. We also demonstrate techniques for performing coincidence searches with a heterogeneous network of detectors with different noise spectra and orientations. These techniques include using coordinated signal injections to estimate the network sensitivity, and tuning the analysis to maximize the sensitivity and the livetime, subject to constraints on the background.

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At present several large-scale interferometric gravitationalwave detectors are operating or are being commissioned:

I. INTRODUCTION

GEO [1], LIGO [2], TAMA [3], and Virgo [4]. In addition, numerous resonant-mass detectors have been operating for a number of years [5, 6, 7]. Cooperative analyses by these observatories could be valuable for making confident detections of gravitational waves and for extracting maximal information from them. This is particularly true for gravitationalwave bursts (GWBs) from systems such as core-collapse supernovae [8, 9, 10, 11], black-hole mergers [12, 13], and gamma-ray bursters [14], for which we have limited theoretical knowledge of the source and the resulting gravitational

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waveform to guide us. Advantages of coincident observations include a decreased background from random detector noise fluctuations, an increase in the total observation time during which some minimum number of detectors are operating, and the possibility of locating a source on the sky and extracting polarization information (when detectors at three or more sites observe a signal) [15]. Independent observations using different detector hardware and software also decrease the possibility of error or bias.

There are also disadvantages to joint searches. Most notably, in a straightforward coincidence analysis the sensitivity of a network is limited by the least sensitive detector. In addition, differences in alignment mean that different detectors will be sensitive to different combinations of the two polarization components of a gravitational wave. This complicates attempts to compare the signal amplitude or waveform as measured by different detectors. Finally, differences in hardware, software, and algorithms make collaborative analyses technically challenging.

In this article we present the first observational results from a joint search for gravitational waves by the LIGO and TAMA collaborations. We perform a coincidence analysis targeting generic millisecond-duration GWBs, requiring candidate GWBs to be detected by all operating LIGO and TAMA interferometers. This effort is complementary to searches for GWBs performed independently by LIGO [16] and TAMA [17] using the same data that we analyze here. Our goal is to highlight the strengths and weaknesses of our joint search relative to these single-collaboration searches, and to demonstrate techniques for performing coincidence searches with a heterogeneous network of detectors with different noise spectra and orientations. This search could form a prototype for more comprehensive collaborative analyses in the future.

In Section II we review the performance of the LIGO and TAMA detectors during the joint observations used for this search. We describe the analysis procedure in Section III, and the tuning of the analysis in Section IV. The results of the search are presented in Section V. We conclude with some brief comments in Section VI.

II. LIGO-TAMA NETWORK AND DATA SETS

The LIGO network consists of a 4 km interferometer "L1" near Livingston, Louisiana and 4 km "H1" and 2 km "H2" interferometers which share a common vacuum system on the Hanford site in Washington. The TAMA group operates a 300 m interferometer "T1" near Tokyo. These instruments attempt to detect gravitational waves by monitoring the interference of the laser light from each of two perpendicular arms. Minute differential changes in the arm lengths produced by a passing gravitational wave alter this interference pattern. Basic information on the position and orientation of the LIGO and TAMA detectors can be found in [18, 19]. Detailed descriptions of their operation can be found in [2, 16, 17, 20].

In a search for gravitational-wave bursts, the key characteristics of a detector are the orientation, the noise spectrum and its variability, and the observation time.

The response of an interferometer to a gravitational wave depends on the relative orientation of the source and the detector, as well as on the signal polarization. Figure 1 shows the variation in the polarization-averaged sensitivities of the LIGO and TAMA detectors as a function of the sky position of the source. It is clear from these figures that LIGO and TAMA have maximum sensitivity to different portions of the sky. This complicates a search based on coincident detections: there is a loss of sensitivity to weak signals; and it is difficult to compare quantitatively the signal amplitude or waveform as measured by the LIGO and TAMA detectors since they will not, in general, be the same. (This was not a significant problem in previous multi-detector searches by LIGO [16, 21] and the IGEC [7], since they employed approximately co-aligned detectors.) We account for these effects by using coordinated simulations to guide the tuning of our analysis so as to maximize the detection efficiency of the network, and we forego amplitude and waveform consistency tests between LIGO and TAMA; see Sections III, IV.

The data analyzed in this search were collected during the LIGO science run 2 (S2) and the TAMA data taking run 8 (DT8), between 14 February 2003 and 14 April 2003. Figures 2 and 3 show representative strain noise spectra from each detector during S2/DT8. Ignoring differences in antenna response, requiring coincident detection of a candidate signal by both LIGO and TAMA means that the sensitivity of the network will be limited by the least sensitive detector. This motivates concentrating our efforts on the frequency band where all detectors have comparable sensitivity; i.e., near the minimum of the noise envelope. Specifically, we choose to search for GWBs that have significant power in the frequency range 700-2000 Hz. Restricting the frequency range in this manner reduces the background due to coincident noise fluctuations, while preserving the sensitivity of the network to GWBs that are detectable by both LIGO and TAMA. Note also that the LIGO collaboration has carried out an independent GWB analysis of the S2 data concentrating on the band 100-1100 Hz [16]. There is thus no danger in missing a real detectable burst which might have occurred at lower frequencies, since it should have been detected by this complementary search.

Table I shows the amount of time in S2/DT8 during which each detector was operating. As we shall see in Section IV B, the LIGO-TAMA network achieved its lowest background rate during periods when both of the LIGO Hanford interferometers (H1 and H2) and at least one of the LIGO Livingston and TAMA interferometers (L1 and T1) were operating. Restricting our analysis to these detector combinations gives us three independent data sets: the quadruple-coincidence data set, denoted H1-H2-L1-T1; the data set during which L1 was not operating, denoted H1-H2-nL1-T1, and the data set during which T1 was not operating, denoted H1-H2-L1-nT1 ("n" for "not operating"). The observation time for each of these data sets is also shown in Table I.

The LIGO-TAMA quadruple-coincidence data set (H1-H2-L1-T1) is particularly well-suited to making confident detections of gravitational-wave bursts, since combining so many detectors naturally suppresses the background from accidental coincidences – to well below one per year, in our case –



FIG. 1: Polarization-averaged antenna amplitude responses $(F_+^2 + F_\times^2)^{1/2} \in [0, 1]$, in Earth-based coordinates. [See equation (4.3) and [19] for definitions of these functions and of Earth-based coordinates.] The top plot is for the LIGO Hanford detectors (H1, H2). The middle plot is for LIGO Livingston (L1). The bottom plot is for TAMA (T1). High contour values indicate sky directions of high sensitivity. The directions of maximum (null) sensitivity for each detector are indicated by the * (.) symbols. The directions of LIGO's maximum sensitivity lie close to areas of TAMA's worst sensitivity and vice versa.

while maintaining high detection sensitivity. Meanwhile, the triple-coincidence data sets (H1-H2-nL1-T1 and H1-H2-L1-nT1) contribute the bulk of our observation time. In particular, the high T1 duty cycle (82%) allows us to use the large amount of H1-H2 data in H1-H2-nL1-T1 coincidence that would otherwise be discarded because of the poor L1 duty cycle (33%).

The LIGO-TAMA detector network therefore has more than twice as much useful data as the LIGO detectors alone. This increase in observation time allows a proportional decrease in the limit on the GWB rate which we are able to set with the combined detector network (for negligible background), and increases the probability of seeing a rare strong gravitational-



FIG. 2: S2-averaged amplitude noise spectra for the LIGO detectors, and a representative DT8 spectrum for the TAMA detector. We focus on GWBs which have significant energy in the frequency range 700-2000 Hz (indicated by the vertical dashed lines), where each interferometer has approximately the same noise level.



FIG. 3: The same amplitude noise spectra as in Figure 2, focusing on the frequency range 700-2000 Hz. The peaks at multiples of 400/3 Hz in the TAMA spectrum are due to a coupling between the radio-frequency modulation signal and the laser source; these frequencies are removed by the data conditioning discussed in Section III A 2.

wave event. Furthermore, while the LIGO-TAMA network uses only half of the TAMA data, we shall see that the suppression of the background by coincidence allows it to place stronger upper limits on weak GWBs than can TAMA alone.

The LIGO and TAMA detectors had not yet reached their design sensitivities by the time of the S2/DT8 run; nevertheless, the quantity of coincident data available – nearly 600 hours – provided an excellent opportunity to develop and test joint searches between our collaborations. In addition, the sensitivity of these instruments in their common frequency band was competitive with resonant-mass detectors (see for

detector	observation	fraction of total
combination	time (hr)	observation time
H1	1040	74%
H2	821	58%
L1	536	38%
T1	1158	82%
H1-H2-L1-T1	256	18%
H1-H2-nL1-T1	320	23%
H1-H2-L1-nT1	62	4%
network totals	638	45%

TABLE I: Observation times and duty cycles of the LIGO and TAMA detectors individually, and in various combinations, during S2/DT8. The symbol nL1 (nT1) indicates times when L1 (T1) was not operating. The network data sets are disjoint (non-overlapping).

example [22]), but with a much broader bandwidth. Finally, there is always the possibility of a fortunate astrophysical event giving rise to a detectable signal.

III. ANALYSIS METHOD

Our analysis methodology is similar, though not identical, to that used in the LIGO S1 and S2 un-triggered GWB searches [16, 21]. The essential steps are illustrated in Figure 4. These are:

- 1. Search the data from each detector separately for burst events.
- 2. Look for simultaneous ("coincident") events in all operating detectors.
- 3. Perform a waveform consistency test on the data from the LIGO interferometers around the time of each coincidence.
- 4. Estimate the background rate from coincident detector noise fluctuations by repeating the coincidence and waveform consistency tests after artificially shifting in time the events from different sites.
- 5. Compare the number of coincidences without time shifts to that expected from the background to set an upper limit on the rate of detectable bursts. (A significant excess of events indicates a possible detection.)
- 6. Estimate the network sensitivity to true GWBs (i.e., the false dismissal probability) by adding simulated signals to the detector data and repeating the analysis.

In the following subsections we describe these steps in more detail. In addition, the various thresholds used for event generation, coincidence, etc., are tuned to maximize the sensitivity of the analysis; this tuning is described in Section IV B.

The LIGO software used in this analysis is available publicly [23].



FIG. 4: Schematic of our analysis pipeline. Data from each detector is analyzed for bursts using the TFClusters (TFC) or Excess Power (POW) algorithm. Optionally, a time shift of 5 - 115 s is added to the event triggers from some sites. We look for simultaneous events from each operating detector, then apply the *r*-statistic waveform consistency test to the data from the LIGO detectors. Surviving coincidences are possible GWBs if no time shifts were used; otherwise they are accidental coincidences (background). The detection efficiency of the network is estimated by adding simulated GWBs to the data from each detector and repeating the analysis. Note that one of the L1 or T1 detectors may not be operating at any given time.

A. Event trigger generation

To maintain sensitivity to the widest range of signals, our burst-detection algorithms do not use templates. Instead, they look for transient excesses of power in the detector output. The production of lists of transient events, or *event triggers*, was done independently by LIGO and TAMA, using different algorithms. Since both of the algorithms used have been described elsewhere, we review them only briefly.

1. TFClusters

The LIGO triggers were produced using the TFClusters burst-detection algorithm [21, 24].

Before processing in TFClusters, the data from a given detector are first high-pass filtered and whitened using a linear predictor error filter [25, 26]. The TFClusters algorithm then constructs a time-frequency spectrogram of the filtered data by segmenting the data into 50% overlapping time intervals and Fourier transforming. The fraction p of highestpower pixels in each frequency bin are selected as *black* pixels, where p is the black pixel probability. (Note that this thresholding is inherently adaptive, so that the rate of triggers is not unduly affected by slow trends in the noise floor.) Event triggers are formed from clusters of nearest-neighbor black pixels that exceed a specified size. In keeping with our choice of frequency band, only triggers that overlap 700-2000 Hz are retained; all others are discarded. These triggers are then passed to a function which makes refined estimates of their peak time, duration, central frequency, bandwidth, and signal-to-noise ratio.

2. Excess Power

The TAMA triggers are generated using an excess power algorithm, following the procedure used in a TAMA-only search for GWBs [17].

The TAMA data are first conditioned to remove lines (including the peaks at multiples of 400/3 Hz visible in Fig. 3). It is then divided into 87.5% overlapping segments and Fourier transformed. The resulting spectrogram is normalized by the background estimated over the previous 30 min. The signalto-noise ratio (SNR) is then summed over a fixed set of frequency bins in the range 230-2500 Hz, and a trigger produced when the SNR exceeds the threshold $\rho_0 = 4$. Triggers separated by less than 25 ms are reported as a single event characterized by the peak time, duration, and SNR. (Due to the use of a frequency mask, no frequency information is assigned to the trigger.) Finally, triggers occurring simultaneously with excursions in the intensity of the light in the recycling cavity are vetoed (ignored), as are triggers that fail a time-scale test designed to pass only millisecond-duration events [17].

B. Coincidence and background

To minimize the possibility of falsely claiming a gravitational-wave detection, we require any candidate GWB to be observed simultaneously by all operating detectors. In this section we explain how the coincidence test was imposed, and how the background rate was estimated.

1. Coincidence

The coincidence test is very simple. Each event *i* is characterized by a peak time t_i and a duration Δt_i . Events from two detectors are defined to be in coincidence if the difference in their peak times satisfies

$$|t_i - t_j| < w + \frac{1}{2} (\Delta t_i + \Delta t_j).$$
 (3.1)

Here w is a coincidence "window" which accounts for the light travel time between the detectors in question; in practice we use windows 10 - 20 ms longer than the light travel time for safety. The duration-dependent term allows for the estimated peak time of coincident triggers to be farther apart if the triggers are long compared to the coincidence window [27]; one may consider this as an allowance for the uncertainty in the determination of the peak time. A set of event triggers i, j, \ldots, k is defined to be in coincidence if each pair (i, j), (i, k), (j, k), etc., is in coincidence.

Ideally, the window w for each pair of detectors should be as short as possible, to minimize the rate of accidental coincidences between noise events in the various detectors, while still being long enough that all simulated signals detected are in coincidence. The windows for our analysis are determined using the simulations described in Section IV B.

It is observed that triggers in the S2 and DT8 data tend to be produced in clusters, on time scales of order 1 s or less.



FIG. 5: Autocorrelogram of trigger peak times from each detector. These are histograms of the difference in peak time between each pair of triggers from a given detector, binned in 0.2 s intervals. The horizontal axis is the time difference (units of s); the vertical axis is the number of trigger pairs per bin divided by the observation time and the bin width (units of s^{-2}). With this normalization, the mean value is the square of the trigger rate. An autocorrelogram value significantly above the mean indicates a correlation in the time of event triggers. Each detector shows some excess above Poisson rates at delays of up to a few seconds. The sharp dip in the T1 curve near zero time is due to the clustering of the T1 triggers. The smaller relative fluctuations in the L1 and T1 curves are due to the much higher trigger rates from these detectors, which results in more triggers per bin.

We therefore count groups of coincident triggers that are separated in time by less than 200 ms as a single GWB candidate when estimating the GWB rate.

Note that no attempt is made to compare the amplitude or SNR of events between detectors. Such comparisons are difficult due to the differences in alignment of the detectors (except for the H1-H2 pair); see Figure 1. We do, however, impose a test on the consistency of the waveform shape as measured by the various LIGO detectors; see Section III C.

2. Background

Even in the absence of real gravitational-wave signals, one expects some coincidences between random noise-generated events. We estimate this background rate by repeating the coincidence procedure after adding artificial relative time shifts of $\pm 5, 10, \ldots, 115$ s to the triggers from the LIGO Hanford and/or TAMA sites, as indicated in Figure 4. (We do not shift the triggers from H1 and H2 relative to each other, in case there are true correlated noise coincidences caused by local environmental effects.) These shifts are much longer than the light travel time between the sites, so that any resulting coincidence cannot be from an actual gravitational wave. They are also longer than detector noise auto-correlation times (see Figure 5), and shorter than time scales on which trigger rates vary, so that each provides an independent estimate of the accidental coincidence rate.

The H1-H2-nL1-T1 and H1-H2-L1-nT1 data sets each come from 2 sites, so that we have 46 nonzero relative time shifts in $\{-115, -110, \dots, 115\}$ s. Hence, the small-

est nonzero background rate that can be measured for these data sets is approximately $(46T)^{-1}$, where T is the observation time [28]. The H1-H2-L1-T1 network has 3 sites, for a total of $47^2 - 1 = 2208$ independent time shifts. We use all of these time shifts, so the smallest nonzero background rate that we can measure for the quadruple-coincidence data set is approximately $(2208T)^{-1}$.

C. Waveform consistency test

The event generation and coincidence procedures outlined above are designed to detect simultaneous excesses of power in each detector, without regard to the waveform of the event. To test if the waveforms as measured in each detector are consistent with one another (as one would expect for a GWB), we apply a test based on the linear correlation coefficient between data streams, the *r*-statistic [29]. We will see in Section IV B that the *r*-statistic test is very effective at eliminating accidental coincidences, with very little probability of rejecting a true gravitational-wave signal. (See also [16] for demonstrations of the *r*-statistic with other simulated GWB waveforms.)

The r-statistic test consists of computing the crosscorrelation of the time-series data from pairs of detectors around the time of a coincidence. A GWB will increase the magnitude of the cross-correlation above that expected from noise alone. The measured cross-correlations are compared to those expected from Gaussian noise using a Kolmogorov-Smirnov test with 95% confidence level. If not consistent, then the logarithmic significance (negative log of the probability) of each cross-correlation is computed and averaged over detector pairs. We refer to the resulting quantity as Γ . If the maximum averaged significance exceeds a threshold Γ_0 , then the coincidence is accepted as a candidate GWB; otherwise it is discarded. The threshold Γ_0 is chosen sufficiently high to reduce the background by the desired amount without rejecting too many real GWB signals. For more details on the test, see [29].

The *r*-statistic test was developed for use in LIGO searches, and it is based on the premise that a real gravitational-wave signal will have similar form in different detectors. It is not clear that it can be applied safely to detectors with very different orientations (such as LIGO and TAMA), which see different combinations of the two polarizations of a gravitational wave. Since this matter is still under study, we use the *r*-statistic test to compare data between the LIGO detectors only (i.e., H1-H2, H2-L1, and L1-H1, but not including T1).

D. Statistical analysis

Our scientific goal of this search is to detect GWBs, or in the absence of detectable signals, to set an upper limit on their mean rate, and to estimate the minimum signal amplitude to which our network is sensitive.

The coincidence procedure described in Section III B produces two sets of coincident events. The set with no artificial time shift is produced by background noise and possibly also by gravitational-wave bursts. The time-shifted set contains only events produced by noise, and hence characterizes the background.

Given the number of candidate GWBs and the estimate of the number of accidental coincidences expected from the background, we use the Feldman-Cousins technique [30] to compute the 90% confidence level upper limit or confidence interval on the rate of detectable gravitational-wave bursts. In practice, since we are not prepared to claim a detection based only on such a statistical analysis, we choose in advance to use only the upper value of the Feldman-Cousins confidence interval. We report this upper value $R_{90\%}$ as an upper limit on the GWB rate, regardless of whether the Feldman-Cousins confidence interval is consistent with a rate of zero. Because of this modification our upper limit procedure has a confidence level greater than 90%; i.e., our upper limits are conservative.

The rate upper limit $R_{90\%}$ from the Feldman-Cousins procedure applies to GWBs for which our network has perfect detection efficiency. For a population of GWB sources for which our detection efficiency is $\epsilon(h)$, where h is the GWB amplitude and $0 \le \epsilon(h) \le 1$, the corresponding rate upper limit $R_{90\%}(h)$ is

$$R_{90\%}(h) \le \frac{R_{90\%}}{\epsilon(h)}$$
. (3.2)

This defines a region of rate-versus-strength space which is excluded at 90% confidence by our analysis. The exact domain depends on the signal type through our efficiency $\epsilon(h)$. We will construct such exclusion regions for one hypothetical population of GWB sources.

IV. SIMULATIONS AND TUNING

There are a number of parameters in the analysis pipeline of Figure 4 that can be manipulated to adjust the sensitivity and background rate of our network. The most important are the thresholds for trigger generation (the TFClusters black pixel probability p and the Excess Power SNR threshold ρ_0), the rstatistic threshold Γ_0 , and the coincidence windows w for each detector pair. Our strategy is to tune these parameters to maximize the sensitivity of the network to millisecond-duration signals while maintaining a background of less than 0.1 surviving coincidences expected over the entire S2/DT8 data set.

A. Simulations

The LIGO-TAMA network consists of widely separated detectors with dissimilar noise spectra and antenna responses. To estimate the sensitivity of this heterogeneous network we add (or "inject") simulated gravitational-wave signals into the data streams from each detector, and re-analyze the data in exactly the same manner as is done in the actual gravitationalwave search; this is indicated in Figure 4 by the "simulated signals" box. These injections are done coherently; i.e., they correspond to a GWB incident from a specific direction on the sky. The simulated signals include the effects of the antenna response of the detectors, and the appropriate time delays due to the physical separation of the detectors.

These simulations require that we specify a target population, including the waveform and the distribution of sources over the sky. We select a family of simple waveforms that have millisecond durations and that span the frequency range of interest, 700-2000 Hz. Specifically, we use linearly polarized Gaussian-modulated sinusoids:

$$h_{+}(t) = h_{\rm rss} \left(\frac{\pi}{2f_0^2}\right)^{-1/4} \sin\left[2\pi f_0(t-t_0)\right] e^{-\frac{(t-t_0)^2}{\tau^2}}, \quad (4.1)$$

$$h_{\times}(t) = 0.$$

(Other waveforms, along with these, have been considered in [16, 17, 21].) Here t_0 is the peak time of the signal envelope. The central frequency f_0 of each injection is picked randomly from the values 700, 849, 1053, 1304, 1615, 2000 Hz, which span our analysis band in logarithmic steps. The efficiency of detection of these signals thus gives us a measure of the network sensitivity averaged over our band. We set the envelope width as $\tau = 2/f_0$, which gives durations of approximately 1-3ms. The corresponding quality factor is $Q \equiv \sqrt{2}\pi f_0 \tau = 8.9$ and the bandwidth is $\Delta f = f_0/Q \simeq 0.1 f_0$, so these are narrow-band signals.

The quantity h_{rss} in equation (4.1) is the root-sum-square amplitude of the plus polarization:

$$\left[\int_{-\infty}^{\infty} dt \, h_{+}^{2}(t)\right]^{1/2} = h_{\rm rss} \tag{4.2}$$

We find h_{rss} to be a convenient measure of the signal strength. While it is a detector-independent amplitude, h_{rss} has the same units as the strain noise amplitude spectrum of the detectors, which allows for a direct comparison of the signal amplitude relative to the detector noise. All amplitudes quoted in this report are h_{rss} amplitudes.

Lacking any strong theoretical bias for probable sky positions of sources of short-duration bursts, we distribute the simulated signals isotropically over the sky. We select the polarization angle randomly with uniform distribution over $[0, \pi]$.

A total of approximately 16800 of these signals were injected into the S2/DT8 data. For each signal, the actual waveform h(t) as it would be seen by a given detector was computed,

$$h(t) = F^{+}h_{+}(t) + F^{\times}h_{\times}(t) = F^{+}h_{+}(t), \qquad (4.3)$$

and h(t) was added to the detector data. Here F^+ , F^{\times} are the usual antenna response factors, which are functions of the sky direction and polarization of the signal relative to the detector (see for example [19]). The signals in the different detectors were also delayed relative to one another according to the sky position of the source.

These simulated signals were shared between LIGO and TAMA by writing the signals h(t) in frame files [31, 32], including the appropriate detector response and calibration effects. These signal data were added to the data streams from the individual detectors before passing through TFClusters or

Excess Power. In addition to providing estimates of the network detection efficiency, the ability of these two independent search codes to recover the injected signals is an important test of the validity of the pipeline.

An injected signal is considered detected if there is a coincident event from the network within 200 ms of the injection time. The network efficiency $\epsilon(h_{\rm rss})$ is simply the fraction of events of amplitude $h_{\rm rss}$ which are detected by the network. We find that good empirical fits to the measured efficiencies can be found in the form

$$\epsilon(h_{\rm rss}) = \frac{1}{1 + \left(\frac{h_{\rm rss}}{h_{\rm rss}^{50\%}}\right)^{\alpha\left[1 + \beta \tanh\left(h_{\rm rss}/h_{\rm rss}^{50\%}\right)\right]}}, \qquad (4.4)$$

where $h_{\rm rss}^{50\%} > 0$, $\alpha < 0$, and $-1 < \beta \le 0$. Here $h_{\rm rss}^{50\%}$ is the amplitude at which the efficiency is 0.5, α parameterizes the width of the transition region, and β parameterizes the asymmetry of the efficiency curve about $h_{\rm rss} = h_{\rm rss}^{50\%}$. When presenting efficiencies we will use fits of this type.

As we shall see, the efficiency transitions from zero (for weak signals) to unity (for strong signals), over about an order of magnitude in signal amplitude. It proves convenient to characterize the network sensitivity by the single number $h_{\rm rss}^{50\%}$ at which the efficiency is 0.5. This amplitude is a function of the trigger-generation thresholds; it and the background rate are the two performance measures that we use to guide the tuning of our analysis.

B. Tuning procedure

As stated earlier, our tuning strategy is to maximize the detection efficiency of the network while maintaining a background rate of less than approximately 0.1 events over the entire data set. For simplicity, we chose a single tuning for the production and analysis of all event triggers from all data sets. This strategy is implemented as follows:

- 1. For TFClusters, the efficiency for detecting the sine-Gaussian signals and the background rate are measured for each detector for a large number of parameter choices. For each black-pixel probability p (which determines the background rate) the other ETG parameters are set to obtain the lowest $h_{rss}^{50\%}$ value [33]. The TAMA Excess Power algorithm is tuned independently for short-duration signals as described in [17]. The resulting performance of each detector is shown in Figure 6.
- 2. The coincidence window w for each detector pair in equation (3.1) is fixed by performing coincidence on the triggers from the simulated signals. We find that selecting windows only slightly larger (by ~ 1 ms) than the light travel time between the various detector pairs (see Table II) ensures that all of the injections detected by all interferometers produce coincident triggers. For simplicity, we use a single window of w = 20 ms for coincidence between any LIGO detectors [34] and a single

detector pair	separation (km)	separation (ms)
LHO-LLO	3002	10.0
LLO-TAMA	9683	32.3
TAMA-LHO	7473	24.9

TABLE II: Separation of the LIGO and TAMA interferometers, using data from [19].

window of w = 43 ms for coincidence between any LIGO detector and TAMA. These choices correspond to using the longest possible time delay plus a ~ 10 ms safety margin.

- 3. To obtain the best network sensitivity versus background rate, we select the single-detector ETG thresholds (p, ρ_0) to match $h_{rss}^{50\%}$ as closely as possible between the detectors. (This is similar in spirit to the IGEC tuning [7], although not the same, as we are not able to easily compare the amplitude of individual events from our misaligned broadband detectors.) In practice, the TAMA detector has slightly poorer sensitivity than the LIGO detectors. We therefore set the TAMA threshold as low as we consider feasible, $\rho_0 =$ 4; this sets the sensitivity of the network as a whole. We then choose the LIGO single-detector thresholds for similar efficiency.
- 4. The final threshold is that for the *r*-statistic, denoted β . In practice we find that the *r*-statistic has negligible effect on the network efficiency for $\beta < 5$. We set $\beta = 3$, which proved sufficient to eliminate all time-lagged (accidental) coincidences while rejecting less than 1% of the injected signals.

Figure 6 shows the resulting $h_{\rm rss}^{50\%}$ and background rate for each of the three coincidence combinations. Table III shows trigger rates and livetimes for each coincidence combination.

We note from Figure 6 that the network background rates are 5-9 orders of magnitude smaller than the rates of the individual detectors. Roughly speaking, adding a detector with event rate R_i and coincidence window w to the network changes the network background rate by a factor of approximately $2R_iw$. From the single-detector rates of Figure 6 or Table III we estimate that H1 and H2 each reduce the background rate by $\sim 10^3$, L1 by ~ 50 , and T1 by ~ 10 . This is why we require both H1 and H2 to be operating: they suppress strongly the background for our network.

We have confirmed that the background rate estimated from time shifts is consistent with that expected from Poisson statistics. Assuming Poisson statistics, the expected background rate R for a set of N detectors with rates R_i is approximately

$$R \approx \frac{1}{w} \prod_{i=1}^{N} 2R_i w \tag{4.5}$$

where we assume a single coincidence window w for simplicity. Using this formula and the single-detector rates from



FIG. 6: Amplitude $h_{\text{TSS}}^{50\%}$ for 50% detection efficiency versus background rate for each of the individual detectors, and for the three coincidence combinations. The circles on the single-detector curves indicate the tuning selected for trigger generation. The circle, square, and triangle denote the resulting amplitude at 50% efficiency and an upper limit on the background rate for the H1-H2-L1-T1, H1-H2nL1-T1, and H1-H2-L1-nT1 networks after the *r*-statistic with these tuning choices. (We can only compute upper limits on the background rates for coincidence because no time-shifted coincidences survive the waveform consistency test.) The efficiency is averaged over all of the sine-Gaussian signals in our analysis band.

Table III, one predicts background rates before the r-statistic consistent with those determined from time delays. This agreement gives increased confidence in our background estimation.

It is also worth noting that the 50% efficiency point $h_{\rm rss}^{50\%}$ is a very shallow function of the background rate for multiple detectors. Hence, there is little value in lowering the trigger thresholds to attempt to detect weaker signals. For example, allowing the triple-coincidence background rate of TFClusters (the rate for the H1-H2-L1-nT1 data) to increase by 3 orders of magnitude lowers $h_{\rm rss}^{50\%}$ by less than a factor of 2. For four detectors, $h_{\rm rss}^{50\%}$ varies even more slowly with the background rate. This is why we tune for $\ll 1$ background event over the observation time; there is almost no loss of efficiency in doing so.

To avoid bias from tuning our pipeline using the same data from which we derive our upper limits, the tuning was done without examining the full zero-time-shift coincidence trigger sets. Instead, preliminary tuning was done using a 10% subset of the data, referred to as the *playground*, which was not used for setting upper limits. Final tuning choices were made by examining the time-shifted coincidences and the simulations over the full data set. As it happens, the only parameter adjusted in this final tuning was the *r*-statistic threshold Γ_0 ; we required the full observation time to have enough background coincidences to allow reasonably accurate estimates of the background suppression by the *r*-statistic test.

Figure 7 shows the efficiency of the LIGO-TAMA network as a function of signal amplitude for each of the three data sets,



FIG. 7: Detection efficiency over the various data sets individually, and combined, using the final tuning. The combined efficiency curve is the average of the curves for the three data sets, weighted by their observation times. These efficiencies are averaged over all of the sine-Gaussian signals in our analysis band. There is a statistical uncertainty at each point in these curves of approximately 1-3% due to the finite number of simulations performed.

and also the average efficiency weighted by the observation time of each data set. By design, the efficiencies are very similar, with $h_{\rm rss}^{50\%}$ values in the range $1-2 \times 10^{-19}$ Hz^{-1/2}.

Figure 8 shows how the combined efficiency varies across our frequency band; the weak dependence on the central frequency of the injected signal is a consequence of the flatness of the envelope of the detector noise spectra shown in Figure 3. This is corroborated by the efficiency for the H1-H2-L1-nT1 data set (without TAMA), shown in Figure 9. The improvement in the low-frequency sensitivity for this data set indicates that TAMA limits the network sensitivity at low frequencies, as expected from the noise spectra.

C. Systematic and statistical uncertainties

The only significant systematic uncertainty in our analysis is in the overall multiplicative scale of the calibration (the coupling of strain to the output of the individual detectors). The "1- σ " uncertainties were estimated as ~9% for L1 and ~4% for each of H1, H2, and T1 [35]. Simple Monte-Carlo modeling indicates that, with 90% confidence, the $h_{rss}^{50\%}$ value for any given network combination will not be more than 4% larger than the estimated value due to these uncertainties. We allow for this uncertainty in our rate-versus-strength plots by shifting our limit curves to larger h_{rss} by 4%.

The main statistical uncertainty in our results is in the efficiency at any given signal amplitude, due to the finite number of simulations performed. This can be quantified through the uncertainty in the parameters found for the efficiency fits (4.4), and is typically less than 5%. We account for this by shifting our rate-versus-strength upper limit curves upward at



FIG. 8: Detection efficiency for the combined data set, by central frequency f_0 of the sine-Gaussian signal in equation (4.1). There is a statistical uncertainty at each point in these curves of approximately 2-4% due to the finite number of simulations performed.



FIG. 9: Detection efficiency for the H1-H2-L1-nT1 data set (i.e., with only the LIGO detectors operating), by central frequency f_0 of the sine-Gaussian signal in equation (4.1). There is a statistical uncertainty at each point in these curves of approximately 2-6% due to the finite number of simulations performed. The improved efficiency for lower-frequency signals indicates that sensitivity at these frequencies is limited by the TAMA detector. This behavior is consistent with the noise spectra shown in Figure 3.

each amplitude by 1.28 times the estimated statistical uncertainty in the corresponding efficiency. (The factor 1.28 gives a 90% limit, assuming Gaussian statistics.)

V. ANALYSIS RESULTS

After making the final tuning choices, we performed the coincidence analysis without time shifts for all three data sets. No event triggers survived the coincidence and *r*-statistic tests, so we have no candidate gravitational-wave signals.

Table III shows for each data set the rate of triggers, the number of coincident events before and after the *r*-statistic test, and the total amount of data analyzed after removing the playground and accounting for the dead time of the TAMA vetoes. Also shown are the number of accidental coincidences and the effective observation time from the time-shift experiments, which provide our estimate of the background rates. Finally, the upper limits on the rate of detectable gravitationalwave bursts are shown.

As discussed in Section III D, our upper limits are obtained using the Feldman-Cousins procedure [30]. This algorithm compares the observed number of events to that expected from the background. As a rule, for a fixed number of observed events, the upper limit is stronger (lower) for higher backgrounds. Since our backgrounds are too low to be measured accurately (there are no surviving time-shifted coincidences after the *r*-statistic), we conservatively assume zero background in calculating our upper limits. Since there are also no surviving coincidences without time shifts, the rate limits from the Feldman-Cousins procedure take on the simple form

$$R_{90\%}^i = \frac{2.44}{T_i} \tag{5.1}$$

where T_i is the observation time for a particular network combination (see Table IV of [30] with b = 0, n = 0). This gives the limits shown in Table III. Additionally, since all three data sets have essentially zero background, we can treat them collectively as a single experiment by summing their observation times and the number of detected events (which happens to be zero):

$$R_{90\%}^{\text{combined}} = \frac{2.44}{\sum_{i} T_{i}}$$
(5.2)

The resulting upper limit of 0.12 detectable events per day at 90% confidence is the primary scientific result of this analysis.

By dividing the rate upper limits by the efficiency for a given population of GWB sources, as in equation (3.2), we obtain upper limits on the GWB rate as a function of the burst amplitude. Averaging over the network combinations gives

$$R_{90\%}^{\text{combined}}(h_{\text{rss}}) = \frac{2.44}{\sum_{i} \epsilon_i (h_{\text{rss}}) T_i}$$
(5.3)

For example, for our tuning population of isotropically distributed sources of sine-Gaussian GWBs, and averaging over all f_0 (i.e., using the efficiencies in Figure 7), one obtains the rate-versus-strength upper limits shown in Figure 10. GWB rates and amplitudes above a given curve are excluded by that data set with at least 90% confidence.

A. Comparison to other searches

The LIGO-TAMA search for GWBs is one of several such searches reported recently. Table IV shows the observation

Data Set	H1-H2-L1-T1	H1-H2-nL1-T1	H1-H2-L1-nT1	Combined
$R_{\rm H1}~({\rm s}^{-1})$	0.0157	0.0151	0.0137	
$R_{\rm H2}~({\rm s}^{-1})$	0.0164	0.0183	0.0150	
$R_{\rm L1}~({\rm s}^{-1})$	0.399	-	0.377	
$R_{\rm T1}~({\rm s}^{-1})$	1.03	1.04	-	
N	0/0	1/0	0/0	1/0
T (hr)	165.3	257.0	51.2	473.5
N _{bck}	31/0	57/0	0/0	
$T_{\rm bck}$ (hr)	3.422×10^{5}	1.139×10^{4}	2.243×10^{3}	
$\langle N \rangle$	0.015/<0.0005	1.3/<0.03	< 0.03/< 0.03	< 1.4 / < 0.05
$R_{90\%} ({\rm day}^{-1})$	0.35	0.23	1.1	0.12

TABLE III: Results of the LIGO-TAMA analysis for each data set separately, and combined. $R_{\rm H1}$, etc., are the measured single-detector trigger rates. N is the total number of coincidences before/after the r-statistic waveform consistency test. T is the total observation time analyzed, after removal of the playground and veto dead times. $N_{\rm bck}$ and $T_{\rm bck}$ are the corresponding summed numbers from the time-shift experiments. $\langle N \rangle$ is the expected number of accidental coincidences during the observation time. (For $N_{\rm bck} = 0$, we estimate $\langle N \rangle < T/T_{\rm bck}$.) $R_{90\%}$ is the resulting upper limit on the rate of detectable gravitational-wave events, at 90% confidence.



FIG. 10: Rate-versus-strength upper limits from each LIGO-TAMA data set, and combined, for the isotropic distribution of sources of sine-Gaussian GWBs described in Section IV A. The region above any curve is excluded by that experiment with at least 90% confidence. These curves include the allowances for uncertainties in the calibration and in the efficiencies discussed in Section IV C.

time, rate upper limit, and approximate frequency band for LIGO-TAMA, the LIGO-only S2 search [16], the TAMA-only DT9 search [17], and the IGEC search [7]. Our limit of 0.12 events per day is the strongest limit yet placed on gravitational-wave bursts by broadband detectors. Even so, it is still approximately a factor of 30 larger than the IGEC limit, which was derived from approximately two years of data from a network of 5 resonant-mass detectors. Note however that the broadband nature of the LIGO and TAMA detectors means that they are sensitive to a wider class of signals than resonant-mass detectors; the IGEC search is only sensitive to GWBs with significant power at the resonant frequencies of all of the operating detectors.

Network	T (day)	$R_{90\%} ({\rm day}^{-1})$	band (Hz)
LIGO-TAMA S2/DT8	19.7	0.12	700-2000
LIGO-only S2	10.0	0.26	100-1100
TAMA-only DT9	8.1	0.49	230-2500
IGEC	707.9	0.0041	694-930

TABLE IV: Observation times, rate upper limits, and frequency bands for LIGO-TAMA and other recent burst searches [7, 16, 17]. The stated frequency range for the IGEC search is the range of the resonant frequencies of the detectors used. The IGEC upper limit applies only to signals with significant power at the resonant frequencies of all of the operating detectors.

Since our sine-Gaussian test waveforms are narrow-band signals, we cannot compare directly our sensitivity to that of the IGEC network. More concrete comparisons can be made between the performance of the LIGO-TAMA network and LIGO and TAMA individually, by considering the rateversus-strength upper limit for $f_0 = 849$ Hz sine-Gaussians. Figure 11 shows the upper limits for this waveform from the LIGO-only S1 and S2 searches [16, 21], the TAMA DT9 search [17], and the present analysis. Compared to LIGO alone, the much longer observation time afforded by joining the LIGO and TAMA detectors allows the LIGO-TAMA network to set stronger rate upper limits for amplitudes at which both LIGO and TAMA are sensitive. The joint network also enjoys a lower background rate from accidental coincidences, particularly for the quadruple-coincidence network: of order $1/40 \text{ yr}^{-1}$ for quadruple coincidence, versus of order 2 yr⁻¹ for the LIGO-only S2 analysis. However, the band of good sensitivity for LIGO-TAMA does not extend to low frequencies, due to the poorer TAMA noise level there. The LIGOonly analysis also has better sensitivity to weak signals, especially near the lower edge of our frequency band. Compared to TAMA alone, the LIGO-TAMA network has better sensitivity to weak signals because coincidence with LIGO lowers



FIG. 11: Comparison of the rate-versus-strength upper limits for $f_0 = 849$ Hz sine-Gaussians from the combined LIGO-TAMA data set (including systematic and statistical uncertainties) with those from the LIGO-only S1 and S2 bursts searches [16, 21] and the TAMA-only DT9 search [17]. The combined LIGO-TAMA network has a superior rate upper limit for strong signals due to its larger observation time, while the LIGO-only S2 network has better sensitivity to weak signals. The TAMA-only DT9 amplitude sensitivity is limited by the high SNR threshold needed achieve a background rate of order one event over the observation time. Note that the LIGO-only S2 search had a nominal frequency range of 100-1100 Hz, while the LIGO-TAMA search band is 700-2000 Hz.

the network background rate without requiring high thresholds for trigger generation. For example, while the TAMA noise levels were lower in DT9 than in DT8, the TAMA DT9 amplitude sensitivity is not as good as that of LIGO-TAMA due to the need to use a very high SNR threshold – $\rho_0 = 10^4$ – to reduce the TAMA-only background rate to of order one event over the observation time.

VI. CONCLUSION

The LIGO and TAMA collaborations have completed their first joint search for gravitational-wave bursts, using 473hr of coincident data collected during early 2003. We looked for millisecond-duration gravitational-wave bursts in the frequency range 700-2000 Hz, where all four of the detectors had comparable sensitivity. To maintain a low background, we analyzed data only from periods when at least three interferometers (including the two LIGO-Hanford interferometers) were operating, and we required candidate signals to be observed simultaneously in all of the operating detectors. We used coordinated injections of simulated gravitational-wave signals to estimate the detection efficiency of our heterogeneous network. We matched the efficiency between detectors to maximize the network sensitivity while limiting the background rate to less than 0.1 events expected over the entire observation time. No gravitational-wave candidates were observed, and we place an upper bound of 0.12 events per day on the rate of detectable millisecond-duration gravitational-wave bursts with at least 90% confidence. Simulations indicate that our network has a detection efficiency of at least 50% (90%) for narrow-band signals with root-sum-square strain amplitude greater than approximately 2×10^{-19} Hz^{-1/2} (10^{-18} Hz^{-1/2}) in the frequency band 700-2000 Hz.

This analysis highlights both advantages and disadvantages of joint coincidence searches compared to independent searches by LIGO and TAMA. Together, the LIGO-TAMA network has more than twice as much data with three or more detectors in simultaneous operation than LIGO alone, leading to stronger rate limits. We also enjoy a background rate of order one event per 40 years (or lower) in quadruple-coincidence operation. The lower background from coincidence also allows the TAMA data to be analyzed with lower thresholds for signal detection. These benefits come at some cost in detection efficiency and in bandwidth, particularly at low frequencies. This is a result of requiring coincident detection by all interferometers, in which case the network sensitivity is limited by the least sensitive detector at each frequency.

This analysis may serve as a prototype for more comprehensive collaborative searches in the future. One improvement would be to expand the detector network. For example, GEO, LIGO, and TAMA performed coincident data taking during Oct. 2003 - Jan. 2004; a GEO-LIGO-TAMA network would contain 5 interferometers at four sites, with excellent sky coverage. Another improvement would be to implement a fully coherent consistency test of coincident events, including all of the detectors in the network. For example, the Gursel-Tinto technique [15] would allow us to take advantage of the different detector orientations to try to extract sky direction and waveform information from detected gravitationalwave signals. It would also allow us to reject a coincidence if no consistent sky direction or waveform could be determined [36].

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