# Impurity diffusion of <sup>141</sup>Pr in LaMnO<sub>3</sub>, LaCoO<sub>3</sub> and LaFeO<sub>3</sub> materials

Marián Palcut,<sup>†</sup><sup>a</sup> Jens S. Christensen,<sup>b</sup> Kjell Wiik<sup>a</sup> and Tor Grande<sup>\*a</sup>

Received 30th May 2008, Accepted 25th July 2008 First published as an Advance Article on the web 24th September 2008 DOI: 10.1039/b808789j

The impurity diffusion of  $Pr^{3+}$  in dense polycrystalline LaMnO<sub>3</sub>, LaCoO<sub>3</sub> and LaFeO<sub>3</sub> was studied at 1373–1673 K in air in order to investigate cation diffusion in these materials. Cation distribution profiles were measured by secondary-ion mass spectrometry and it was found that penetration profiles of  $Pr^{3+}$  had two distinct regions with different slopes. The first, shallow region was used to evaluate the bulk diffusion coefficients. The activation energies for bulk diffusion of  $Pr^{3+}$  in LaMnO<sub>3</sub>, LaCoO<sub>3</sub> and LaFeO<sub>3</sub> were  $126 \pm 6$ ,  $334 \pm 68$  and  $258 \pm 75$  kJ mol<sup>-1</sup>, respectively, which are significantly lower than previously predicted by atomistic simulations. The bulk diffusion of  $Pr^{3+}$  in LaMnO<sub>3</sub> was enhanced compared to LaCoO<sub>3</sub> and LaFeO<sub>3</sub> due to higher concentrations of intrinsic point defects in LaMnO<sub>3</sub>, especially La site vacancies. Grain-boundary diffusion coefficients of  $Pr^{3+}$  in LaCoO<sub>3</sub> and LaFeO<sub>3</sub> materials were evaluated according to the Whipple–Le Claire equation. Activation energies for grain-boundary diffusion of  $Pr^{3+}$  in LaCoO<sub>3</sub> materials were  $264 \pm 41$  kJ mol<sup>-1</sup> and  $290 \pm 36$  kJ mol<sup>-1</sup> respectively. Finally, a correlation between activation energies for cation diffusion in bulk and along grain boundaries in pure and substituted LaBO<sub>3</sub> materials (B = Cr, Fe, Co) is discussed.

## Introduction

Materials based on perovskite-type  $LaBO_3$  oxides (B = Cr, Mn, Fe, Co) are widely used as high temperature devices since the appropriate substitution with alkaline earth metals and 3d-elements can tailor their transport properties.<sup>1–3</sup> Strontiumdoped lanthanum chromites and manganites, for example, are state-of-the-art interconnect and cathode materials, respectively, in solid oxide fuel cells.4-7 Sr- and Fe-substituted lanthanum cobaltites are valuable as oxygen-permeable membranes and other electrochemical devices.<sup>8,9</sup> These devices operate under various thermodynamic gradients. The thermodynamic forces applied at high temperatures may induce a significant cation displacement leading to structural changes and degradation over time.<sup>10,11</sup> To avoid these undesirable effects and achieve an optimal performance of the device, knowledge of cation diffusion is essential. It is generally observed that cations move significantly slower than oxygen in perovskite-type oxides and thus, cation diffusion limits a number of mass transport processes.<sup>12,13</sup> It is, therefore, surprising to realize that only a few studies have been previously devoted to experimental determination of cation diffusion coefficients. Pure and substituted  $LnCrO_3$  (Ln = La, Y, Nd)<sup>14-22</sup> and LnFeO<sub>3</sub> (Ln = La, Y, Gd, Nd)<sup>23-27</sup> materials are the most studied materials in this respect. Cation diffusion in simple oxides has been studied by diffusion couple measurements, tracer diffusion and inter-diffusion experiments (see ref. 28 for review).

La<sup>3+</sup> diffusion in LaMnO<sub>3</sub> and LaCoO<sub>3</sub> materials has previously not been studied experimentally. LaMnO<sub>3</sub> is known to possess large deviations from the nominal stoichiometry.<sup>29,30</sup> This leads to formation of cation vacancies on both La and Mn sites, tending more towards La vacancies at high temperatures. Interstitial defects are unfavourable due to the close atomic packing in the perovskite lattice. The examination of cation transport in LaMnO3 by atomistic simulation techniques suggests that the lanthanum diffusion is likely to take place by a vacancy migration between neighbouring sites.<sup>31,32</sup> Calculated migration energy of La vacancy is 3.93 eV (379 kJ mol<sup>-1</sup>) and increases with distortion from the cubic form.<sup>31</sup> Our previous experimental studies, focused on the diffusion-controlled kinetics of the perovskite phase formation, suggested that the mobility of both Mn<sup>3+</sup> and Co<sup>3+</sup> were higher than the La<sup>3+</sup> mobility.<sup>33,34</sup> The solid-state reaction method allowed only for the determination of the diffusion coefficient for the faster moving cation. In these studies, the La3+ diffusion coefficients in LaMnO3 and LaCoO<sub>3</sub> were not obtained.

Tracer diffusion experiments may give valuable information about cation mobility provided that the appropriate tracer is available.<sup>35</sup> These experiments are based on depth penetration profiles and thus, they can also be useful in determining the actual transport paths in the material.<sup>36,37</sup> It is known that the diffusion in ionic materials is significantly enhanced along grain boundaries and possibly also dislocations.<sup>38–40</sup> The relative contribution of the bulk diffusion and the grainboundary diffusion is highly valuable since most technological applications involve polycrystalline materials. Experiments highlighting diffusion mainly in the La sublattice can be

<sup>&</sup>lt;sup>a</sup> Department of Materials Science and Engineering, Norwegian University of Science and Technology, 7491 Trondheim, Norway. E-mail: tor.grande@material.ntnu.no

<sup>&</sup>lt;sup>b</sup> Department of Physics, University of Oslo, 0316 Oslo, Norway

<sup>†</sup> Present address: Institute of Materials Science, Faculty of Materials Science and Technology, Slovak University of Technology, 91724 Trnava, Slovakia.

efficiently performed by the use of other lanthanoids as impurity tracers. Lanthanoid cations,  $\text{Ln}^{3+}$ , in low concentrations, especially those with similar ionic radii and ionic charge, are expected to replace lanthanum in crystal lattice without significantly changes in the crystal structure of the material.

In the present work we aim to study the impurity diffusion of  $Pr^{3+}$  in LaBO<sub>3</sub> oxides (B = Mn, Fe, Co) by secondary-ion mass spectrometry (SIMS) at 1373–1673 K in air. Praseodymium was chosen due to its similar atomic radius to lanthanum and comparable chemical properties.<sup>41,42</sup> Praseodymium is, next to cerium, the closest neighbour to lanthanum in the periodic table and it has only one stable, naturally occurring isotope (<sup>141</sup>Pr).

## Experimental

Intensity (a. u.)

20

Powders of LaMnO<sub>3</sub>, LaFeO<sub>3</sub> and LaCoO<sub>3</sub> were prepared by spray pyrolysis. The precursor consisted of aqueous nitrate solutions of cations mixed in stoichiometric amounts. The solution was supplied to the furnace with a speed of  $2 \ 1 \ h^{-1}$ , atomized and pyrolyzed in a continuous air flow at approximately 1133 K. Collected raw powders were calcined at 1173 K for 2 h and subsequently ball-milled for 18 h in order to break agglomerates. Phase purity of LaMnO<sub>3</sub>, LaFeO<sub>3</sub> and LaCoO<sub>3</sub> materials was confirmed by X-ray diffraction (SIEMENS D5005, Siemens Germany). No extra diffraction lines due to secondary phases could be observed in any of the three materials. The diffraction lines could be indexed to the space group reported for the three compounds,  $R\bar{3}c$  (LaMnO<sub>3</sub>, LaCoO<sub>3</sub>) and *Pnma* (LaFeO<sub>3</sub>) and refined lattice parameters for the three compounds LaFeO<sub>3</sub>, LaCoO<sub>3</sub> and LaMnO<sub>3</sub> were in good accord with data reported in the PDF database. The X-ray diffraction (XRD) data for the compounds are given in Fig. 1.

Fine powders were shaped into cylindrical green bodies (10 mm in diameter, 2–3 mm thick) by uniaxial (LaFeO<sub>3</sub> and LaCoO<sub>3</sub>) or isostatic pressing (LaMnO<sub>3</sub>). Ethyl cellulose (0.7 weight%) was needed to improve the strength of the green body. The pellets of LaFeO<sub>3</sub> and LaMnO<sub>3</sub> materials were



20

50

40

sintered at 1723 K for 2 h in air, while the LaCoO<sub>3</sub> pellets were sintered in air at 1523 K for 6 h. The final densities of the pellets, measured by the Archimedes method, were  $6.32 \pm$  $0.05, 6.54 \pm 0.03$  and  $6.71 \pm 0.05$  g cm<sup>-3</sup> for LaMnO<sub>3</sub>, LaFeO<sub>3</sub> and LaCoO<sub>3</sub> respectively. These values correspond to 96.2, 98.5 and 92.0% of crystallographic densities for LaMnO<sub>3</sub>, LaFeO<sub>3</sub> and LaCoO<sub>3</sub> respectively. The porosity of the pellets was observed to be essentially only closed porosity. Microstructure of the materials was studied by low vacuum scanning electron microscope (Hitachi S3500N). Grain size was estimated from the number of grain boundaries observed per distance unit of thermally etched surfaces. Dense pellets were ground and polished down to 0.25 µm with a diamond paste to achieve a homogeneous and smooth surface necessary for diffusion experiments.

Diffusion source was prepared from an aqueous  $Pr(NO_3)_3$  solution ( $c = 0.05 \text{ mol } \text{dm}^{-3}$ ). Three droplets of the solution were placed on a sample's surface and solvent was slowly evaporated at 393 K. This treatment provided a uniform, approximately 1 µm thick layer of  $Pr^{3+}$ . Samples were slowly heated to 743 K to remove volatile nitric oxides and transform praseodymium nitrate into the oxide. Samples were finally annealed at 1373, 1473, 1573 and 1673 K in air for 20, 5, 2 and 1 h respectively. Heating and cooling rates were both 600 K  $h^{-1}$ . At the conditions of the annealing the tracer source was a single oxide phase with the valence of Pr close to Pr(III).

Cation distribution in LaMnO<sub>3</sub>, LaFeO<sub>3</sub> and LaCoO<sub>3</sub> materials was studied by secondary-ion mass spectrometry (SIMS) using a CAMECA ims 7f instrument. The area of  $200 \times 200 \ \mu m$  was sputtered with a ~500 nA  $O_2^+$  primary beam (10 keV) in order to create a rectangular crater. The signal from the crater was optically gated-only the signal from the inner area of the crater with dimensions of approximately  $60 \times 60 \ \mu m$  was monitored in order to avoid negative interferences (edge and wall effects). The intensity of the signal was measured by switching between the secondary ion signals of different elements since the magnetic sector of the instrument could register only one element at a time. In the case of LaFeO<sub>3</sub> a neutralizing electron beam was used to compensate for the materials poor electrical conductivity. The intensity of the signal for each element was obtained as a function of the sputtering time. The final intensity profiles of the impurity tracer were normalized by the concentration of one of the matrix elements to compensate for variations instrumental variations. The depth of the crater was measured with a surface profilometer (Dektak 8). A depth penetration profile was calculated assuming a constant erosion rate of the material.

#### Results

The microstructures of the LaMnO<sub>3</sub>, LaFeO<sub>3</sub> and LaCoO<sub>3</sub> materials prepared for the diffusion experiments are shown in Fig. 2 and 3. Both LaMnO<sub>3</sub> and LaFeO<sub>3</sub> (Fig. 2) were fully dense after sintering at temperatures above 1673 K. The average grain size was  $2.5 \pm 0.3 \mu m$  for LaMnO<sub>3</sub> and  $2.9 \pm 0.4 \mu m$  for LaFeO<sub>3</sub>. Complete densification of LaCoO<sub>3</sub> was more complicated due to the rapid grain growth and corresponding trapping of spherical pores inside the grains at

30



Fig. 2 Fracture surfaces showing the microstructure of (a) LaMnO<sub>3</sub> and (b) LaFeO<sub>3</sub> after sintering at 1723 K for 2 h.



Fig. 3 (a) Grain size and (b) fracture surface of LaCoO<sub>3</sub> after sintering at 1523 K for 6 h.

high temperatures. Nevertheless, it was possible to obtain a dense material, with only closed porosity, after sintering at 1523 K for 6 h (Fig. 3). The average grain size of LaCoO<sub>3</sub> was 7.9  $\pm$  1.0 µm. The porosity of all materials was closed (Fig. 2 and 3), and any penetration of the diffusion source into open pores could be excluded. As shown later the diffusion profiles of Pr did not provide any signature of penetration of the Pr source into open pores.

A typical crater resulting from ion sputtering is given in Fig. 4. The surface roughness of the bottom of the crater didn't exceed  $\pm 2 \ \mu m$ .

Typical element distribution profiles obtained by SIMS are given in Fig. 5. Signals of matrix elements (La and Mn, Fe and Co) were measured in all samples. Since the concentration of the matrix elements (Mn, Fe and Co) in the materials was assumed to be constant, any variation in their signals reflected mostly the instrumental variations during the measurements. The signals of elements in LaFeO<sub>3</sub> were significantly lower compared to the LaMnO<sub>3</sub> and LaCoO<sub>3</sub> materials due to the low electrical conductivity of LaFeO<sub>3</sub>.

In most of the impurity depth profiles two distinct regions with different slopes could be recognized. The first part of the diffusion profile (region 1) was attributed to the parallel bulk and grain-boundary diffusion. The first region for the LaMnO<sub>3</sub> samples was significantly deeper and less steep compared to the LaFeO<sub>3</sub> and LaCoO<sub>3</sub> materials (Fig. 5a). This behaviour reflects enhanced praseodymium diffusion in LaMnO<sub>3</sub> relative to the two other materials. Both LaCoO<sub>3</sub> and LaFeO<sub>3</sub> showed similar behaviour with a relatively shallow first part of the diffusion profile followed by a broad second region (region 2)



**Fig. 4** Depth profile of a crater after ion sputtering illustrated on the LaCoO<sub>3</sub> specimen. Total time of sputtering was 6 h.

with a significantly smaller slope (Fig. 5). Praseodymium diffusion was studied at four different temperatures. The results obtained at 1373, 1473 and 1673 K had the same characteristic features as those already given in Fig. 5.

Diffusion in polycrystalline materials takes place simultaneously inside the grains (in the crystal lattice) and along grain



Fig. 5 Element depth profiles in  $LaMnO_3$  (top),  $LaCoO_3$  (middle) and  $LaFeO_3$  (bottom) after the thermal anneal of praseodymium at 1573 K for 2 h in air.

boundaries. The apparent diffusion coefficient,  $D_{\text{eff}}$ , can be given by Hart's equation,<sup>43</sup>

$$D_{\rm eff} = g D_{\rm GB} + (1 - g) D_{\rm L} ,$$
 (1)

where  $D_{GB}$  and  $D_L$  are the grain-boundary and lattice (bulk) diffusion coefficients, respectively and g is the fraction of atomic sites that are situated at the grain boundaries (or dislocations). The fraction of atomic sites at the grain

boundaries can be estimated by the volume fraction of grain boundaries in the polycrystal. Since  $g \ll 1$ , eqn (1) simplifies to  $D_{\text{eff}} \approx D_{\text{L}} + gD_{\text{GB}}$ . It is seldom possible, however, to completely decouple the grain-boundary diffusion from the bulk diffusion due to the leakage of diffusing species from boundary to the adjoining grains. Harrison<sup>44</sup> provided the analysis of the problem using a model of parallel grain boundaries. This model distinguishes three limiting cases of diffusion kinetics. In type A, the extensive lattice and grainboundary diffusion occur and they are mixed across the grains. In type B kinetics, fast diffusion along the grain boundaries is accompanied by a small leakage of the diffusing species into grains. Finally, in the type C diffusion kinetics, the lattice diffusion is completely eliminated.

Region 1 was used to estimate the lattice diffusion coefficient of <sup>141</sup>Pr in the LaBO<sub>3</sub> materials (B = Mn, Fe, Co). The solution of the diffusion equation

$$\frac{\partial c(x,t)}{\partial t} = D_1 \frac{\partial^2 c(x,t)}{\partial x^2} \tag{2}$$

is for diffusion from a thin-film source given as<sup>45</sup>

$$c(x,t) = c_0(t) \exp\left(-\frac{x^2}{4D_1 t}\right)$$
(3)

where c(x,t) is the concentration of the diffusing species, t is the annealing time, x is the distance from the surface,  $c_0(t)$  is the surface concentration of diffusant and  $D_1$  is the apparent diffusion coefficient in region 1. The ratio  $\frac{c(x,t)}{c_0(t)}$  was replaced by the intensity ratio of <sup>141</sup>Pr signal since the intensity was assumed to be proportional to concentration. Representative fit to the experimental data are shown in Fig. 6. The fitted slopes of  $\log(\frac{I}{I_0})$  vs.  $x^2$  obtained for the three materials are given in Table 1.

Region 2 was used to obtain data on grain-boundary diffusion of <sup>141</sup>Pr according to the Whipple–Le Claire equation, <sup>37,46,47</sup>

$$s\delta D_{\rm GB} = 0.3292 \sqrt{\frac{D_{\rm L}}{t}} \left( -\frac{\partial \log c}{\partial x^{6/5}} \right)^{-5/3} \tag{4}$$

where s is a segregation factor and  $\delta$  is the grain-boundary width. First, slope of  $\log(\frac{I}{T_0})$  vs.  $x^{1.2}$  plot in region 2 was obtained. The triple product  $s\delta D_{\rm GB}$  was then calculated assuming that  $D_{\rm L} = D_1$ . Finally the critical parameters,  $\alpha$ and  $\beta$ , were calculated according to equations<sup>37</sup>

$$\alpha = \frac{s\delta}{2\sqrt{D_{\rm L}t}}\tag{5}$$

$$\beta = \frac{s\delta D_{\rm GB}}{2D_{\rm L}\sqrt{D_{\rm L}t}} \tag{6}$$

 $s\delta = 10^{-7}$  cm was adopted in order to calculate  $\alpha$ . Representative fit to the experimental data for two of the materials are shown in Fig. 6. The numerical values for fit to the experimental data are given in Table 1. The grain-boundary diffusion coefficients in LaMnO<sub>3</sub> were not evaluated since bulk diffusion was dominating and the second region is suggested to reflect only the impurity level of Pr in the material.



**Fig. 6** Penetration profiles of the  $Pr^{3+}$  cations in (a) LaMnO<sub>3</sub>, (b) and (c) LaCoO<sub>3</sub>, (d) and (e) LaFeO<sub>3</sub> at 1673 K. The fitted curves are given for the respective bulk and grain-boundary regions. The intensity of  $Pr^{3+}$  was normalized by the intensity of one of the matrix elements to compensate for instrumental variations during sputtering.

#### Discussion

## 1. Bulk diffusion

Praseodymium is an impurity element in LaBO<sub>3</sub> materials. It is, therefore, of interest to compare the influence of  $Pr^{3+}$  on the structural properties of the LaBO<sub>3</sub> materials. Praseodymium replaces lanthanum in the crystal lattice. Nevertheless, it has a smaller ionic radius which reduces the Goldschmidt tolerance factor and enhances the distortion from the ideal cubic perovskite structure. Crystal structure of  $La_{1-x}Pr_xCoO_3$  single crystals has been recently studied by Kobayashi *et al.*<sup>48</sup> The  $La_{1-x}Pr_xCoO_3$  materials are rhombohedral for  $0 \le x \le 0.3$  and orthorhombic for  $0.7 \le x \le 1$ . The lattice volume decreases monotonically with increasing Pr content due to the smaller ionic radius of  $Pr^{3+}$ .

Structural properties of  $\text{La}_{1-x} \text{Pr}_x \text{MnO}_{3+\delta}$  have been studied by Dyakonov *et al.*<sup>49</sup>  $\text{La}_{1-x} \text{Pr}_x \text{MnO}_{3+\delta}$  has a rhombohedral structure for x = 0, orthorhombic with small Jahn–Teller distortion of MnO<sub>6</sub> octahedra for 0.1 < x < 0.6 and highly distorted orthorhombic modifications for x > 0.6. The effect of Pr on lattice distortion is minimal at concentrations below 10%. Since the praseodymium concentration in the samples was significantly lower than La content (Fig. 5), the effect of praseodymium on crystal structure of LaBO<sub>3</sub> materials can be neglected.

The diffusion coefficients for  $Pr^{3+}$  in LaBO<sub>3</sub>, *D*, may be expressed by an Arrhenius law

$$D = D_0 \exp\left(-\frac{E_{\rm A}}{RT}\right) \tag{7}$$

β

 $32.7 \times 10^{3}$ 

 $4.13 \times 10^{3}$ 

 $5.05 \times 10^{3}$ 

 $2.74 \times 10^{3}$ 

 $29.1 \times 10^{3}$ 

 $59.7 \times 10^{3}$ 

 $12.0 \times 10^{3}$ 

 $20.4 \times 10^{3}$ 

Table 1	Lattice a	nd grain-boundary diffusion of
T/K	t/h	$-\frac{\partial \log(I_{\rm Pr}/I_M)}{\partial x^2}/{\rm cm}^{-2}$
LaMnO	3	
1373	20	$(5.92 \pm 0.07) \times 10^5$
1473	5	$(9.93 \pm 0.05) \times 10^5$
1573	2	$(1.37 \pm 0.01) \times 10^{6}$
1673	1	$(1.63 \pm 0.01) \times 10^{6}$
LaCoO <sub>3</sub>		
1373	20	$(21.6 \pm 1.4) \times 10^{8}$
1473	5	$(2.76 \pm 0.04) \times 10^{8}$
1573	2	$(4.08 \pm 0.25) \times 10^8$
1673	1	$(1.63 \pm 0.03) \times 10^{8}$
$LaFeO_3$		
1373	20	$(21.3 \pm 1.2) \times 10^{8}$
1473	5	$(37.6 \pm 3.1) \times 10^{8}$
1573	2	$(44.1 \pm 5.6) \times 10^8$
1673	1	$(5.54 \pm 0.08) \times 10^8$
where <i>i</i> and the atomist activati formati produc	$D_0$ is a pr e other s ic point c on energ on and r t of fact	e-exponential factor, $E_A$ a ymbols have their usual r of view, established for diff y reflects a sum of the enti- nigration and the pre-exp- ors reflecting probability
vacance	v iumps <sup>3</sup>	<sup>5,50</sup> The bulk diffusion coe
the La	MnO <sub>2</sub> I a	FeQ, and LaCoQ, materi
	vino3, La	in CO3 and LaCOO3 materia
F1g. /.	TT1 110	n i 1
	The diff	fusion coefficients decreas

data for <sup>141</sup>Pr in LaMnO<sub>3</sub>, LaFeO<sub>3</sub> and LaCoO<sub>3</sub>

 $D_{\rm L}/{\rm cm}^2~{\rm s}^{-1}$ 

 $6.39 \times 10^{-13}$  $1.52 \times 10^{-12}$  $2.79 \times 10^{-12}$  $4.63 \times 10^{-12}$ 

 $1.74 \times 10^{-16}$ 

 $5.46 \times 10^{-15}$ 

 $9.24 \times 10^{-15}$  $4.63 \times 10^{-14}$ 

 $1.77 \times 10^{-16}$ 

 $4.01\times\ddot{10}^{-16}$ 

 $8.55\times10^{-16}$ 

 $1.36 \times 10^{-14}$ 

 $-\frac{\partial \log(I_{\rm Pr}/I_M)}{2}/{\rm cm}^{-1.2}$ 

 $2302\pm8$ 

 $2316 \pm 6$ 

 $2596 \pm 4$ 

 $2157 \pm 7$ 

 $2448 \pm 15$ 

 $2237 \pm 7$ 

 $1616\pm7$ 

 $1349 \pm 4$ 

n activation energy neaning. From the usion in metals, the halpies for vacancy onential factor is a of the individual efficients of Pr<sup>3+</sup> in als are compared in se in the following The Arrhenius activation energies are  $126 \pm 6$ ,  $334 \pm 68$  and  $258 \pm 75$  kJ mol<sup>-1</sup> for LaMnO<sub>3</sub>, LaCoO<sub>3</sub> and LaFeO<sub>3</sub> respectively. Pr<sup>3+</sup> diffusion in LaMnO<sub>3</sub> is significantly enhanced. Since LaMnO<sub>3</sub> has large deviations from stoichiometry,<sup>30</sup> this observation is not unexpected. In the following discussion we shall compare the experimental cation diffusivities in LaMnO<sub>3</sub> with predictions from atomistic simulations.

Experimental diffusion coefficients of Pr<sup>3+</sup> and Mn<sup>3+</sup> cations in LaMnO<sub>3</sub> are compared in Fig. 8. Activation energy for Mn<sup>3+</sup> transport, determined by diffusion couple experiments, is 280  $\pm$  40 kJ mol<sup>-1</sup>.<sup>33</sup> The activation energy for Pr<sup>3+</sup> transport is significantly lower than the activation energy for



Fig. 7 Bulk diffusion coefficients of praseodymium cations in LaMnO<sub>3</sub> ( $\bullet$ ), LaCoO<sub>3</sub> ( $\blacksquare$ ) and LaFeO<sub>3</sub> materials ( $\nabla$ ) in air.



 $s\delta D_{GB}/cm^3 s^{-1}$ 

 $4.04 \times 10^{-17}$ 

 $4.47 \times 10^{-17}$ 

 $7.60 \times 10^{-16}$ 

 $3.59 \times 10^{-15}$ 

 $3.67 \times 10^{-17}$ 

 $1.28 \times 10^{-16}$ 

 $5.10\times\tilde{10^{-16}}$ 

 $3.89 \times 10^{-15}$ 

α

0.0141

0.00505

0.00613

0.00387

0.0141

0.0186

0.0201

0.00714

**Fig. 8** Cation diffusion coefficients in LaMnO<sub>3</sub> in air: Pr bulk  $(\bullet)$ ,  $Mn(\bigcirc)$ .<sup>33</sup>

 $Mn^{3+}$  diffusion.  $Ln^{3+}$  diffusion in perovskites is most likely to take place by a vacancy migration mechanism between neighbouring sites. Mn migration mechanism, however, is probably more complicated since an oxygen ion is situated between two neighbouring Mn sites. Reported activation energies for La vacancy migration in LaMnO3 based on atomistic simulations are 3.93 eV (379 kJ mol<sup>-1</sup>) for a cubic and 4.14 eV (400 kJ mol<sup>-1</sup>) for a rhombohedrally distorted perovskite lattice.31 Corresponding activation energies for Mn vacancy diffusion were 14.71 eV (1420 kJ mol<sup>-1</sup>) for cubic and 15.73 eV (1520 kJ mol<sup>-1</sup>) for rhombohedral LaMnO<sub>3</sub>.<sup>31</sup> We suggest that Mn<sup>3+</sup> and Ln<sup>3+</sup> diffusion in LaMnO<sub>3</sub> occur by vacancy mechanism between neighbouring sites, but cation migration in LaMnO<sub>3</sub> is probably facilitated due to the significant amount of intrinsic point defects on cation sites in the crystal lattice.

The non-stoichiometry of LaMnO<sub>3</sub> is well known (more precisely written  $La_{1-\delta}Mn_{1-\delta}O_3$  for La : Mn ratio equal to 1). Experimental results show that the oxidative non-stoichiometry leads to the formation of cation vacancies on both La and Mn sites.<sup>51–53</sup> LaMnO<sub>3</sub> has a solid solubility range that is tempera-ture- and  $p_{O_2}$ -dependent.<sup>30,33</sup> The sublattice occupation of LaMnO<sub>3</sub> was recently studied by neutron diffraction.<sup>54</sup> In the



Fig. 9 Possible jumping mechanisms for  $Mn^{3+}$  cations in LaMnO<sub>3</sub> projected to the (100) plane.<sup>31</sup> Mn cations are represented by small open circles, Mn vacancies by small open squares, oxygen anions by large open circles, La cations by line-shaded circles and La vacancies by line-shaded squares.

course of the Rietveld refinement of these data, several models of the different site occupancy were tested. The analysis showed that the structure of La-deficient material with a nominal cation composition La: Mn = 0.91:1 could be given as  $[La_{0.922}Mn_{0.013}]MnO_3$ .<sup>54</sup> This result leads to the conclusion that Mn cations may occupy also vacant La sites. Mn diffusion between neighbouring sites in LaMnO<sub>3</sub> could be, therefore, facilitated by jumps via vacant La sites. Transport paths for the migration of Mn cations in LaMnO<sub>3</sub> have been recently proposed.<sup>31</sup> The projections into the (100) plane with and without La vacancies are compared in Fig. 9.31 Mechanism A indicate a diagonal mechanism in the presence of La cations,<sup>31</sup> mechanism B reflects an energetically easier curved transport path around O anions<sup>31</sup> and mechanism C shows a facilitated Mn transport path in the presence of La vacancies. Note that the La, Mn and O ions are not situated in the same plane. La ions are in the plane behind and above the plane formed by Mn and O ions.

The impurity diffusion coefficients of  $Pr^{3+}$  are lower than the chemical diffusion coefficients of Mn<sup>3+</sup> in LaMnO<sub>3</sub> of about one order of magnitude (Fig. 8). Platinum markers introduced in diffusion couple experiments showed that chemical diffusion of  $La^{3+}$  was significantly slower than Mn<sup>3+</sup> diffusion.<sup>33</sup> It was shown that LaMnO<sub>3</sub> formed in the course of reaction between La<sub>2</sub>O<sub>3</sub> and Mn<sub>3</sub>O<sub>4</sub> phases had significant composition gradients.<sup>33</sup> At the phase boundary with La<sub>2</sub>O<sub>3</sub> it had La excess, and correspondingly, low concentration of La vacancies.33 Material prepared for tracer diffusion experiments, on the other hand, was homogeneous also evidenced by the signals of <sup>55</sup>Mn and <sup>138</sup>La which did not significantly vary over the entire sputtering process (Fig. 5). The difference between the chemical and tracer diffusion coefficients of Ln<sup>3+</sup> cations in LaMnO<sub>3</sub> is therefore proposed to be related to the varying concentration of La vacancies dependent on the activity of La<sub>2</sub>O<sub>3</sub> in LaMnO<sub>3</sub>. It has also been observed that the cation diffusion coefficients obtained by tracer diffusion experiments had lower activation energies.<sup>34</sup> This is probably owing to the fact that, in tracer diffusion experiments, material with its equilibrium number of vacancies is first prepared at a high temperatures and then annealed with a tracer at lower temperatures. If the vacancy concentration is frozen-in at lower temperatures, the activation energy from tracer diffusion experiments may reflect only the enthalpy for vacancy migration. Activation energies extracted from solid state reaction kinetics are higher since they are proposed to reflect the contribution from both the vacancy formation and the migration of ions.

Bulk diffusion coefficients of Pr<sup>3+</sup> in LaFeO<sub>3</sub> and LaCoO<sub>3</sub> are lower comparing to LaMnO<sub>3</sub> (Fig. 7). Activation energies are  $334 \pm 68$  kJ mol<sup>-1</sup> for LaCoO<sub>3</sub> and  $258 \pm 75$  kJ mol<sup>-1</sup> for LaFeO<sub>3</sub> respectively. The crystal structure of LaFeO<sub>3</sub> is orthorhombic, while LaCoO3 is rhombohedral. The activation energies for La<sup>3+</sup> vacancy migration in rhombohedral and orthorhombic perovskite from atomistic simulations are 4.14 and 4.22 eV respectively.<sup>31</sup> The observed difference in activation energies between LaCoO<sub>3</sub> and LaFeO<sub>3</sub> may, therefore, be due to difference in the deviation from cubic symmetry and difference in unit cell volume. Nevertheless, it has to be kept in mind that data obtained for LaFeO<sub>3</sub> are the least accurate. LaFeO3 was the least conducting material and, correspondingly, a positive charge was built in the samples during the sputtering with  $O_2^+$ . Although the electron beam was used to neutralize the positive charge, charging of the specimens contributed to the low signal of the ions.

The cation diffusion coefficients in LaFeO<sub>3</sub> and LaCoO<sub>3</sub> are compared in Fig. 10 and 11. The actual cation diffusivities of  $Pr^{3+}$  in LaCoO<sub>3</sub> and LaFeO<sub>3</sub> differ by about one order of magnitude, being higher for LaCoO<sub>3</sub>. The B<sup>3+</sup> cation diffusion dominated over the  $Pr^{3+}$  tracer diffusion in these materials. This is in agreement with predictions from platinum marker experiments.<sup>23,34</sup> LaFeO<sub>3</sub> and LaCoO<sub>3</sub> are, compared to LaMnO<sub>3</sub>, stoichiometric compounds ("line compounds") and do not form solid solutions. The amount of intrinsic



**Fig. 10** Cation diffusion coefficients in LaFeO<sub>3</sub> in air: Pr bulk ( $\nabla$ ), Pr grain boundary ( $\nabla$ ) and Fe ( $\odot$ ).<sup>23</sup>



**Fig. 11** Cation diffusion coefficients in LaCoO<sub>3</sub> in air: Pr bulk ( $\blacksquare$ ), Pr grain boundary ( $\bullet$ ) and Co ( $\checkmark$ ).<sup>34</sup>

cation vacancies in LaFeO<sub>3</sub> and LaCoO<sub>3</sub> are expected to be significantly lower since oxygen vacancies are dominating, while cation vacancies dominate in LaMnO<sub>3</sub>.<sup>29,30</sup>

## 2. Grain-boundary diffusion

Diffusion in polycrystalline materials is a complex process requiring several elementary steps. In LaMnO<sub>3</sub>, we observed that the mean diffusion length was larger than average grain size ( $\sqrt{(Dt)} > d$ . This observation justifies A-type diffusion kinetics.<sup>37</sup> Obtained diffusion coefficient (Table 1) is, therefore, an effective quantity. As a first approximation we have used the coefficient as a bulk diffusion coefficient.

Type B kinetics was observed for LaFeO<sub>3</sub> and LaCoO<sub>3</sub> materials. The mean diffusion path in region 1 was smaller than the average grain size and larger than expected grainboundary width ( $\delta \ll \sqrt{Dt} < d$ . Grain-boundary chemistry was studied for Ca-substituted LaCrO<sub>3</sub>.<sup>55</sup> The width of grain boundary was around 1 nm. Critical parameters for the separation of diffusion into bulk and grain boundaries were  $\alpha \ll 1$  and  $\beta \gg 1$  (Table 1). These values justify the use of eqn (4) for separation of diffusion into bulk and grain boundaries.<sup>37</sup> The  $\beta$  parameter reflects the relative portion of grain-boundary diffusion in materials (eqn (6)). The  $\beta$  values for LaCoO<sub>3</sub> are higher than the  $\beta$  values for LaFeO<sub>3</sub> (except the 1373 K experiment, see Table 1). The different portions of the GB diffusion in the LaFeO<sub>3</sub> and LaCoO<sub>3</sub> materials can be rationalized due to the different portions of the grain boundaries coming from different grain sizes of the materials. LaCoO<sub>3</sub> had significantly larger grain size than LaFeO<sub>3</sub> (Fig. 2 and 3) and thus, the relative portion of grain-boundary diffusion was smaller.

The grain-boundary diffusion coefficients of  $Pr^{3+}$  cations in LaCoO<sub>3</sub> and LaFeO<sub>3</sub> materials, given in Fig. 10 and 11, were calculated assuming that s = 1 and  $\delta = 1$  nm. The grainboundary diffusion coefficients are more than 5 orders of magnitude higher than the respective bulk diffusion coefficients (Fig. 10 and 11). The grain boundaries thus constitute a



**Fig. 12** Correlation between activation energies for bulk and grainboundary cation diffusion in perovskite-type oxides: ● tracer diffusion of  $Pr^{3+}$  in LaCoO<sub>3</sub> (present data), ■ tracer diffusion of  $Pr^{3+}$  in LaFeO<sub>3</sub> (present data), ◆ tracer diffusion of  $Cr^{3+}$  in LaCrO<sub>3</sub>,<sup>22</sup> ▼ tracer diffusion of  $Cr^{3+}$  in La<sub>0.9</sub>Sr<sub>0.1</sub>FeO<sub>3-δ</sub>,<sup>27</sup> ▲ diffusion of Nd<sup>3+</sup> in LaFeO<sub>3</sub>,<sup>26</sup> △ diffusion of Mn<sup>3+</sup> in La<sub>0.6</sub>Sr<sub>0.4</sub>Co<sub>0.2</sub>Fe<sub>0.8</sub>O<sub>3-δ</sub>.<sup>11</sup>

rapid transport path for  $Pr^{3+}$  cations in these materials. The activation energies for grain-boundary diffusion are  $264 \pm 41 \text{ kJ mol}^{-1}$  and  $290 \pm 36 \text{ kJ mol}^{-1}$  for LaCoO<sub>3</sub> and LaFeO<sub>3</sub> respectively. These values are similar to the respective activation energies for bulk diffusion. The activation energies for bulk and grain-boundary diffusion for perovskite-type oxides are compared in Fig. 12. The activation energies for bulk and grain-boundary diffusion of cations in perovskite-type oxides fall into one line with a slope of  $1.04 \pm 0.15$  irrespective of the type of experimental technique and perovskite material studied.

The relationship between activation energies for cation transport in bulk and grain boundaries has not been widely studied for oxide materials. Best to our knowledge, only one study reported relationship between activation energy for bulk and grain-boundary diffusion in cubic and tetragonal zirconia.56 The authors found that activation energy for grain-boundary diffusion is about 0.8 of bulk diffusion.<sup>56</sup> This value seems to be consistent with the one found in this study and suggests that the mechanism for cation diffusion in grain boundaries could be a simple vacancy hopping between neighbouring sites. Nevertheless, further systematic studies with oxide materials are apparently needed to confirm this hypothesis. Studies dealing with the grain boundaries of these perovskite materials have recently been reported.<sup>57</sup> These studies could be useful in this respect since they can shed further light into the defect chemistry of grain boundaries.

#### Conclusion

Impurity diffusion coefficients of  $Pr^{3+}$  cations in polycrystalline LaMnO<sub>3</sub>, LaFeO<sub>3</sub> and LaCoO<sub>3</sub> materials have been determined by secondary-ion mass spectrometry. Bulk and grain-boundary diffusion coefficients were obtained by fitting the tracer penetration profiles. The activation energy for bulk diffusion is considerably lower than predicted from atomistic consideration. Bulk diffusion is significantly enhanced in LaMnO<sub>3</sub> relative to LaFeO<sub>3</sub> and LaCoO<sub>3</sub> reflecting the higher cation-vacancy concentrations in LaMnO<sub>3</sub>. The similar activation energy of bulk and grain-boundary diffusion in LaFeO<sub>3</sub> and LaCoO<sub>3</sub> were found. This observation suggests that the transport mechanisms in the grains and along grain boundaries are related.

# Acknowledgements

M. P. thanks Øystein S. Andersen and Trine Øyås (both from Department of Materials Science and Engineering, Norwegian University of Science and Technology, NTNU, Trondheim) for the powder preparation by spray pyrolysis. This work was co-financed by Research Council of Norway (Grant no. 158517/431, Functional oxides for energy technology), NTNU and UNIFOR Oslo.

#### References

- 1 M. A. Peña and J. L. G. Fierro, Chem. Rev., 2001, 101, 1981.
- 2 H. U. Anderson, Solid State Ionics, 1992, 52, 33.
- 3 J. P. Attfield, Chem. Mater., 1998, 10, 3239.
- 4 N. Q. Minh, J. Am. Ceram. Soc., 1993, 76, 563.
- 5 J. P. P. Huijsmans, Curr. Opin. Solid State Mater. Sci., 2001, 5, 317.
- 6 N. P. Brandon, S. Skinner and B. C. H. Steele, Annu. Rev. Mater. Res., 2003, 33, 183.
- 7 L. J. Gauckler, D. Beckel, B. E. Buergler, E. Jud, U. P. Muecke, M. Prestat, J. L. M. Rupp and J. Richter, *Chimia*, 2004, 58, 837.
- 8 Y. Teraoka, T. Nobunaga, K. Okamoto, N. Miura and N. Yamazoe, *Solid State Ionics*, 1991, **48**, 207.
- 9 V. V. Kharton, E. N. Naumovich and A. V. Nikolaev, J. Membr. Sci., 1996, 111, 149.
- 10 S. P. S. Badwal, Solid State Ionics, 2001, 143, 39.
- 11 N. Sakai, T. Horita, K. Yamaji, M. E. Brito, H. Yokokawa, A. Kawakami, S. Matsuoka, N. Watanabe and A. Ueno, *J. Electro-chem. Soc.*, 2006, **153**, A621.
- 12 J. L. Routbort, K. C. Goretta, R. E. Cook and J. Wolfenstine, Solid State Ionics, 2000, 129, 53.
- 13 A. Domínguez-Rodríguez, M. Jiménez-Melendo, N. Chen, K. C. Goretta, S. J. Rothman and J. L. Routbort, J. Phys. III, 1994, 4, 253.
- 14 T. Akashi, M. Nanko, T. Maruyama, Y. Shiraishi and J. Tunabe, J. Electrochem. Soc., 1998, 145, 2090.
- 15 K. Kawamura, A. Saiki, T. Maruyama and K. Nagata, J. Electrochem. Soc., 1995, 142, 3073.
- 16 T. Akashi, Y. Mizuno, M. Nanko, T. Maruyama, A. Saiki, K. Tsukui and J. Tunabe, *Mater. Trans.*, 2001, 42, 1411.
- 17 T. Maruyama and T. Akashi, Proc. Electrochem. Soc., 1998, 97–24, 789.
- 18 J.-O. Hong, S. Miyoshi, A. Kaimai, Y. Nigara, T. Kawada and J. Mizusaki, Proc. Electrochem. Soc., 2001, 28, 49.
- 19 T. Horita, M. Ishikawa, K. Yamaji, N. Sakai, H. Yokokawa and M. Dokiya, *Solid State Ionics*, 1998, **108**, 383.
- 20 T. Horita, M. Ishikawa, K. Yamaji, N. Sakai, H. Yokokawa and M. Dokiya, *Solid State Ionics*, 1999, **124**, 301.
- 21 T. Horita, N. Sakai, T. Kawada, H. Yokokawa and M. Dokiya, J. Am. Ceram. Soc., 1998, 81, 315.
- 22 N. Sakai, K. Yamaji, T. Horita, H. Negishi and H. Yokokawa, *Solid State Ionics*, 2000, **135**, 469.
- 23 J. B. Smith and T. Norby, Solid State Ionics, 2006, 177, 639.
- 24 V. Buscaglia, F. Caracciolo, C. Bottino, M. Leoni and P. Nanni, *Acta Mater.*, 1997, 45, 1213.

- 25 V. Buscaglia, M. T. Buscaglia, L. Giordano, A. Martinelli, M. Viviani and C. Bottino, *Solid State Ionics*, 2002, 146, 257.
- 26 J. B. Smith, T. Norby and A. Fossdal, J. Am. Ceram. Soc., 2006, 89, 582.
- 27 I. Wærnhus, N. Sakai, H. Yokokawa, T. Grande, M.-A. Einarsrud and K. Wiik, *Solid State Ionics*, 2004, **175**, 69.
- 28 R. Freer, J. Mater. Sci., 1980, 15, 803.
- 29 B. C. Tofield and W. R. Scott, J. Solid State Chem., 1974, 10, 183.
- 30 J. A. M. van Roosmalen, P. van Vlaanderen, E. H. P. Cordfunke, W. L. Ijdo and D. J. W. Ijdo, J. Solid State Chem., 1995, 114, 516.
- 31 R. A. De Souza, M. S. Islam and E. Ivers-Tiffée, J. Mater. Chem., 1999, 9, 1621.
- 32 M. S. Islam, Solid State Ionics, 2002, 154-155, 75.
- 33 M. Palcut, K. Wiik and T. Grande, J. Phys. Chem. C, 2007, 111, 813.
- 34 M. Palcut, K. Wiik and T. Grande, J. Phys. Chem. B, 2007, 111, 2299.
- 35 H. Mehrer, in *Diffusion in Condensed Matter: Methods, Materials, Models*, ed. P. Heitjans and J. Kärger, Springer, Berlin, Germany, 2005, p. 3.
- 36 M. Martin, in *Diffusion in Condensed Matter: Methods, Materials, Models*, ed. P. Heitjans and J. Kärger, Springer, Berlin Germany, 2005, p. 209.
- 37 C. Herzig and Y. Mishin, in *Diffusion in Condensed Matter: Methods, Materials, Models*, ed. P. Heitjans and J. Kärger, Springer, Berlin Germany, 2005, p. 337.
- 38 J. H. Harding, Interface Sci., 2003, 11, 81.
- 39 W. Preis, Phys. Chem. Chem. Phys., 2006, 8, 2629.
- 40 I. V. Belova and G. E. Murch, J. Phys. Chem. Solids, 2003, 64, 873.
- 41 G. H. Aylward and T. J. V. Findlay, *SI Chemical Data*, John Wiley & Sons, Sydney, Australia, 1971.
- 42 R. D. Shannon, Acta Crystallogr., Sect. A: Cryst. Phys., Diffr., Theor. Gen. Cryst., 1976, 32, 751.
- 43 E. W. Hart, Acta Metall., 1957, 5, 597.
- 44 L. G. Harrison, Trans. Faraday Soc., 1961, 57, 1191.
- 45 J. Crank, Mathematics of Diffusion, Oxford University Press, Great Britain, 1956.
- 46 A. D. Le Claire, Br J Appl Phys, 1963, 14, 351.
- 47 I. Kaur, Y. Mishin and W. Gust, Fundamentals of Grain and Interphase Boundary Diffusion, John Wiley & Sons Ltd., Chichester, Great Britain, 1995.
- 48 Y. Kobayashi, T. Mogi and K. Asai, J. Phys. Soc. Jpn., 2006, 75, 104703.
- 49 V. Dyakonov, F. Bukhanko, V. Kamenev, E. Zubov, S. Baran, T. Jaworska-Gołąb, A. Szytuła, E. Wawrzyska, B. Penc, R. Duraj, N. Stüsser, M. Arciszewska, W. Dobrowolski, K. Dyakonov, J. Pientosa, O. Manus, A. Nabialek, P. Aleshkevych, R. Puzniak, A. Wisniewski, R. Zuberek and H. Szymczak, *Phys. Rev. B*, 2006, 74, 24418.
- 50 E. P. Butler, H. Jain and D. M. Smyth, J. Am. Ceram. Soc., 1991, 74, 772.
- 51 L. Malavasi, C. Ritter, M. C. Mozzati, C. Tealdi, M. S. Islam, C. B. Azzoni and G. Flor, J. Solid State Chem., 2005, 178, 2042.
- 52 S. Miyoshi, J.-O. Hong, K. Yashiro, A. Kaimai, Y. Nigara, K. Kawamura, T. Kawada and Mizusaki, *Solid State Ionics*, 2002, 154–155, 257.
- 53 S. Miyoshi, J.-O. Hong, K. Yashiro, A. Kaimai, Y. Nigara, K. Kawamura, T. Kawada and S. Mizusaki, *Solid State Ionics*, 2003, 161, 209.
- 54 M. Wołcyrz, R. Horyń, F. Bourée and E. Bukowska, J. Alloys Compd., 2003, 353, 170.
- 55 N. Sakai, T. Tsunoda, N. Fukumoto, I. Kojima, K. Yamaji, T. Horita, M. Ishikawa, H. Yokokawa and M. Dokiya, *J. Electroceram.*, 1999, **4:S1**, 121.
- 56 S. Swaroop, M. Kilo, C. Argirusis, G. Borchardt and A. H. Chokshi, *Acta Mater.*, 2005, 53, 4975.
- 57 P. E. Vullum, A. T. J. van Helvoort, R. Holmestad, J. Mastin, O. E. Andersen, M. A. Einarsud and T. Grande, *J. Mater. Sci.*, 2007, 42, 6267.