

A Physiological Intensive Control Insulin-Nutrition-Glucose (ICING) Model Validated in Critically Ill Patients

Jessica Lin^a, Normy N. Razak^b, Christopher G. Pretty^b,
Aaron Le Compte^b, Paul Docherty^b, Jacquelyn D. Parente^b,
Geoffrey M. Shaw^c, Christopher E. Hann^b, J. Geoffrey Chase^b

^a*Department of Medicine, University of Otago Christchurch, New Zealand*

^b*Center for Bioengineering, University of Canterbury, New Zealand*

^c*Department of Intensive Care Medicine, Christchurch Hospital, New Zealand*

Abstract

Intensive insulin therapy (IIT) and tight glycaemic control (TGC), particularly in intensive care units (ICU), are the subjects of increasing and controversial debate in recent years. Model-based TGC has shown potential in delivering safe and tight glycaemic management, all the while limiting hypoglycaemia. A comprehensive, more physiologically relevant Intensive Control Insulin-Nutrition-Glucose (ICING) model is presented and validated using data from critically ill patients. Two existing glucose-insulin models are reviewed and formed the basis for the ICING model. Model limitations are discussed with respect to relevant physiology, pharmacodynamics and TGC practicality. Model identifiability issues are carefully considered for clinical settings. This article also contains significant reference to relevant physiology and clinical literature, as well as some references to the modeling efforts in this field.

Identification of critical constant population parameters were performed

in two stages, thus addressing model identifiability issues. Model predictive performance is the primary factor for optimizing population parameter values. The use of population values are necessary due to the limited clinical data available at the bedside in the clinical control scenario. Insulin sensitivity, S_I , the only dynamic, time-varying parameter, is identified hourly for each individual. All population parameters are justified physiologically and with respect to values reported in the clinical literature. A parameter sensitivity study confirms the validity of limiting time-varying parameters to S_I only, as well as the choices for the population parameters. The ICING model achieves median fitting error of $<1\%$ over data from 173 patients ($N = 42,941$ hrs in total) who received insulin while in the ICU and stayed for ≥ 72 hrs. Most importantly, the median per-patient one-hour ahead prediction error is a very low 2.80% [IQR 1.18, 6.41%]. It is significant that the 75th percentile prediction error is within the lower bound of typical glucometer measurement errors of 7–12%. These results confirm that the ICING model is suitable for developing model-based insulin therapies, and capable of delivering real-time model-based TGC with a very tight prediction error range. Finally, the detailed examination and discussion of issues surrounding model-based TGC and existing glucose-insulin models render this article a mini-review of the state of model-based TGC in critical care.

Key words: model-based control, tight blood glucose control, TGC, blood glucose, insulin therapy, insulin sensitivity, critical care, predictive performance

1. Introduction

Since the landmark study in surgical intensive care unit (ICU) patients by Van Den Berghe et al. [1], which reduced mortality 18-45% using tight glycaemic control (TGC), the attitude towards tolerating hyperglycaemia in critically ill patients has changed. Hyperglycaemia worsens outcomes, increasing the risk of severe infection [2], myocardial infarction [3], and critical illnesses such as polyneuropathy and multiple organ failure [1]. However, repeating these results has been difficult, and thus the role of tight glycaemic control during critical illness and suitable glycaemic ranges have been under scrutiny in recent years [4, 5, 6, 7, 8, 9, 10, 11]. However, conclusions are varied with both success [1, 12, 13, 14], failure, [15] and, primarily, no clear outcome [16, 17, 18, 19, 20, 21].

Although it is now becoming an unacceptable practice to allow excessive hyperglycaemia and its associated effects [8, 22, 23, 24], moderately elevated blood glucose levels are tolerated or recommended [11] because of the fear of hypoglycaemia and higher nursing effort frequently associated with TGC [8, 10, 25, 26]. Interestingly, some TGC studies that reported a mortality reduction also had reduced and relatively low hypoglycaemic rates [13, 14], whereas almost all other reports had increased and often excessive hypoglycaemia [15, 17]. Finally, model-based and model-derived TGC methods have shown the ability to provide very tight control with little or no hypoglycaemia [13, 27, 28, 29, 30].

Many studies have developed glucose-insulin models with varying degrees of complexity for a wide range of uses, primarily in research studies of insulin sensitivity [27, 31, 32, 33, 34, 35, 36]. A more comprehensive model review

can be found in [28]. For a model to be successful in delivery of TGC, it needs to reflect observable physiology, as well as known biological mechanisms. In addition, it should be uniquely identifiable, and the type and number of parameters to be identified should reflect the clinically available data that will provide validation. Finally, the most important aspect for a model to be used in model-based TGC is its predictive ability, where most studies provide only fitting error as validation [29, 33, 36, 37].

This paper presents a more comprehensive model, ICING (Intensive Control Insulin-Nutrition-Glucose model), for the use of glycaemic control particularly in the ICU. The model addresses several incomplete or implicit physiological aspects from prior models by Chase et al. [27] and Lotz et al. [38]. Model limitations are discussed with respect to physiology, pharmacodynamics and TGC practicality. Model identifiability issues are carefully considered for clinical settings. The ICING model is validated using clinical data from critically ill patients and assessed for both its fitting, and more critically for TGC, predictive performance. Finally, issues surrounding TGC and existing glucose-insulin models are extensively reviewed and discussed.

2. Glucose-Insulin Physiology Model

Two clinically validated glucose-insulin physiology models set the basis of this study. Both models share the same basic structure of the Minimal Model [32]. The model from Chase et al. [27] was developed and validated for glycaemic level management in the ICU. This model captures the fundamental dynamics seen in critically ill patients, yet has a relatively simple mathematical structure enabling rapid identification of patient-specific parameters

[39]. This model only requires measurements in blood glucose levels (BG), therefore it can be used by the bedside for clinical real-time identification and control. This structure has been widely used in clinical TGC studies and other analyses [30, 40, 37].

The second model from Lotz et al. [38] was developed for diagnosis of insulin resistance. The modeled insulin sensitivity has high correlation to the euglycaemic hyperinsulinemic clamp (EIC) and high repeatability [38, 41]. This model has more patient specific parameters, but is not suitable for real-time patient-specific parameter identification because it also requires non-real-time plasma insulin and C-peptide assays [42]. Recent work has sought to eliminate this issue in healthy subjects, but at a loss of precision [43].

2.1. Critical Care Glucose-Insulin Model (ICU Model)

Equations (1)–(5) presents the model used for glycaemic control in intensive care from Chase et al. [27], hereafter referred to as the “ICU Model”.

ICU Model

$$\dot{G} = -p_G G(t) - S_I(G(t) + G_E) \frac{Q(t)}{1 + \alpha_G Q(t)} + \frac{P(t)}{V_G} \quad (1)$$

$$\dot{Q} = -kQ(t) + kI(t) \quad (2)$$

$$\dot{I} = -\frac{nI(t)}{1 + \alpha_I I(t)} + \frac{u_{ex}(t)}{V_I} \quad (3)$$

$$P(t_i < t < t_{i+1}) = \bar{P}_{i+1} + (P(t_i) - \bar{P}_{i+1})e^{-k_{pd}(t-t_i)} \quad \text{where } \bar{P}_{i+1} < P(t_i) \quad (4)$$

$$P(t_i < t < t_{i+1}) = \bar{P}_{i+1} + (P(t_i) - \bar{P}_{i+1})e^{-k_{pr}(t-t_i)} \quad \text{where } \bar{P}_{i+1} > P(t_i) \quad (5)$$

The symbols G [mmol/L] denotes the glucose above an equilibrium level,

G_E [mmol/L]. Plasma insulin is I [mU/L] and exogenous insulin input is $u_{ex}(t)$ [mU/min]. The effect of previously infused insulin being utilized over time in the interstitium is represented by Q [mU/L], with k [1/min] accounting for the effective life of insulin in the system. Patient endogenous glucose removal and insulin sensitivity are p_G [1/min] and S_I [L/mU/min] respectively. The parameter V_I [L] is the insulin distribution volume and n [1/min] is the constant first order decay rate for insulin from plasma. External nutrition is $P(t)$ [mmol/min]. In Equations (4)–(5), k_{pr} [1/min] and k_{pd} [1/min] are the rise and decay rates of exogenous (enteral) plasma glucose appearance, and \bar{P}_i and \bar{P}_{i+1} are the stepwise consecutive enteral glucose feed rates used to model dextrose control. The glucose distribution volume is V_G [L]. Michaelis-Menten functions are used to portray saturations, with parameter α_I [L/mU] used for saturation of plasma insulin disappearance, and α_G [L/mU] for saturation of insulin-stimulated glucose removal.

This model was developed and validated in critical care glycaemic control studies [27, 36, 37, 44]. All the compartmental transport and utilisation rates are treated as constants except insulin sensitivity S_I . Insulin sensitivity S_I is the critical dynamic parameter, and is typically fitted to patient data hourly, producing a step-wise hourly varying profile. The SPRINT glycaemic control protocol [13, 45, 46] was developed using this model. Importantly, the pre-trial virtual trial simulation of SPRINT gave very similar results to the subsequent actual clinical implementation results [27], providing a further measure of validation.

However, this model does not realistically describe the gastric uptake of glucose. Equations (4) and (5) express simple exponential rises and decays of

glucose absorption, which eventually reach a steady state equal to the feeding rate. This simple expression works well in critical care where nasogastric feeding rate is not adjusted frequently. If the feeding rate is changed more frequently than once every 2 hours, Equations (4) and (5) fail to describe the gastric absorption correctly.

This model also employs an “equilibrium blood glucose level” term, G_E , which is usually set to either the patient’s blood glucose level at the start of insulin therapy or a long moving average. This term effectively addresses the endogenous balance of glucose and insulin. Hence, this model does not explicitly express endogenous insulin production. Thus, when there is a significant shift in this balance in a patient, for any number of reasons [36, 44, 47], G_E often needs to be adjusted to capture the patient’s (then) current clinical glucose-insulin dynamics. Hence, the term is non-physiological, unidentifiable and was ignored in later model evolutions [30, 48, 49].

This model also has relatively simple insulin kinetics compared to other more extensive models [50, 51, 52, 53]. It does not explicitly express different routes of insulin clearance and transport from plasma. Instead, the lumped out-flux from plasma is expressed by a saturable term $-nI/(1 + \alpha_I I)$. In addition, as only kI appears as an input to interstitial insulin Q , the difference between n and k is implicitly the insulin clearance by liver and kidneys, which was validated in Lotz et al. [41]. The insulin flux between plasma and interstitial is also only one way in this model, ignoring the diffusion from interstitium back to plasma, as it was designed for TGC using IV insulin boluses. Therefore, the insulin concentration gradient between plasma and the interstitium using bolus delivery is generally large enough that diffusion

back to plasma is negligible. However, the use of boluses is less typical in general clinical settings and neglecting diffusion can introduce error in either case.

2.2. Glucose-Insulin Model for Insulin Sensitivity Test (S_I Test Model)

Equations (6)–(8) presents the model used for insulin sensitivity testing from Lotz et al. [38], hereafter referred to as the “ S_I Test Model”.

S_I Test Model

$$\dot{G} = -p_G G(t) - S_I(G(t) + G_E) \frac{Q(t)}{1 + \alpha_G Q(t)} + \frac{P(t)}{V_G} + EGP(t) \quad (6)$$

$$\dot{Q} = \frac{n_I}{V_Q} (I(t) - Q(t)) - n_C Q(t) \quad (7)$$

$$\begin{aligned} \dot{I} = & -n_K I(t) - \frac{n_L I(t)}{1 + \alpha_I I(t)} - \frac{n_I}{V_P} (I(t) - Q(t)) + \frac{u_{ex}(t)}{V_P} \\ & + (1 - x_L) \frac{u_{en}(t)}{V_P} \end{aligned} \quad (8)$$

The nomenclature for this model is largely the same as that for the ICU Model in Section 2.1. This model has more parameters and more extensive insulin kinetics. It includes the endogenous glucose production rate EGP [mmol/L/min], as well as the endogenous insulin production u_{en} [mU/min]. The endogenous insulin production can be calculated from C-peptide measurements using a well validated insulin-C-peptide kinetics model [54]. Endogenous insulin goes through first pass hepatic extraction, where x_L is the fraction of extraction. This model also has more explicitly defined physiologically specific insulin transport parameters compared to the

ICU Model, where n_K is the kidney clearance rate of insulin from plasma [1/min], n_L is the liver clearance rate of insulin from plasma [1/min], n_I is the diffusion constant of insulin between compartments [L/min], and n_C is the cellular insulin clearance rate from interstitium [1/min]. Finally, it also uses different volumes for each compartment, where V_P is the plasma volume (+Fast exchanging tissues) [L] and V_Q is the interstitial fluid volume [L]. The experimental V_P and V_Q are however very close [38].

In [38, 42], measurements from insulin and C-peptide are used to identify n_L and x_L for each person. S_I and V_G are then calculated for each person using BG measurements. All other parameters are treated as population constants. The insulin sensitivity S_I identified using this model correlates highly ($r > 0.97$) to EIC results [38, 41]. Therefore, this model is effective as a diagnostic tool for insulin resistance. However because plasma insulin and C-peptide measurements cannot be obtained in real time, this model cannot be readily adapted for TGC for ICU patients.

2.3. Intensive Control Insulin-Nutrition-Glucose Model (ICING Model)

The new and more physiologically comprehensive model developed from the best aspects of both models [27, 38] is defined:

$$\dot{BG} = -p_G BG(t) - S_I BG(t) \frac{Q(t)}{1 + \alpha_G Q(t)} + \frac{P(t) + EGP_b - CNS}{V_G} \quad (9)$$

$$\dot{Q} = n_I(I(t) - Q(t)) - n_C \frac{Q(t)}{1 + \alpha_G Q(t)} \quad (10)$$

$$\begin{aligned} \dot{I} = & -n_K I(t) - \frac{n_L I(t)}{1 + \alpha_I I(t)} - n_I(I(t) - Q(t)) + \frac{u_{ex}(t)}{V_I} \\ & + (1 - x_L) \frac{u_{en}}{V_I} \end{aligned} \quad (11)$$

$$\dot{P1} = -d_1 P1 + D(t) \quad (12)$$

$$\dot{P2} = -\min(d_2 P2, P_{max}) + d_1 P1 \quad (13)$$

$$P(t) = \min(d_2 P2, P_{max}) + PN(t) \quad (14)$$

$$u_{en}(t) = k_1 e^{-\frac{I(t)k_2}{k_3}} \quad \text{when C-peptide data is not available} \quad (15)$$

The nomenclature for this model is largely the same as defined in Sections 2.1 and 2.2. However, “equilibrium blood glucose level” G_E is no longer present, and $BG(t)$ is the absolute BG level per more recent works [55, 30, 48]. A constant “basal” endogenous glucose production term EGP_b [mmol/min], which is the endogenous glucose production rate for a patient receiving no exogenous glucose or insulin, is thus added. This model has an additional insulin independent [56] central nervous system glucose uptake, CNS , with an experimental value between 0.29–0.38 mmol/min [56, 57, 58, 59, 60, 61, 62, 63, 64].

In Equation (9), insulin independent glucose removal (excluding central nervous system uptake CNS) and the suppression of endogenous glucose production from EGP_b with respect to $BG(t)$ are compounded and represented by p_G . Insulin mediated glucose removal and the suppression of EGP from EGP_b are similarly compounded and represented by S_I . Consequently, S_I effectively represents the whole-body insulin sensitivity, which includes tissue insulin sensitivity and the action of Glucose Transporter-4 (GLUT-4). The action of GLUT-4 is associated with the compounding effect of receptor-

binding insulin and blood glucose, and its signaling cascade is also dependent on metabolic condition and can be affected by medication [65, 66, 67, 68]. Therefore, S_I is time varying and can reflect evolving patient condition. Its variation through time can be significant, particularly for highly dynamic, critically ill patients [40, 37].

Equations (10) and (11) define the insulin pharmacokinetics similarly to [38] and Equations (7)–(8). Insulin clearance from plasma is saturable, as well as its degradation after receptor binding in the interstitium [69]. The receptor-bound insulin $Q/(1 + \alpha_G Q)$ is also the insulin effective for glucose removal to cells. Hence this term also appears in Equation (9) for glucose dynamics. Note that n_I in Equations (10) and (11) has unit [1/min] rather than [L/min] as in Equations (7) and (8). This is because the new model in Equations (9)–(15) does not use different volumes for plasma and interstitial insulin distribution, since the experimental values are very similar in [38, 70]. To compare and convert n_I from Lotz et al., its value needs to be divided by V_P from Lotz et al.

Equations (12)–(14) present the gastric absorption of glucose, where $P1$ [mmol] represents the glucose in the stomach and $P2$ [mmol] is for the gut. Transport rates between the compartments are d_1 [1/min] and d_2 [1/min]. Amount of dextrose from enteral feeding is $D(t)$ [mmol/min]. Glucose appearance, $P(t)$ [mmol/min] from enteral food intake $D(t)$, is the glucose flux out of the gut $P2$. This flux is saturable, and the maximal out flux is $P_{max} = 6.11$ [mmol/min]. Typically, for ICU patients on enteral feeding, P_{max} is not reached. Any additional parenteral dextrose is represented by $PN(t)$. This dextrose absorption model conserves ingested glucose, and

therefore is also suitable for modeling meal ingestion over a short period of time in contrast to the simpler model of Equations (4) and (5).

Equation (15) is a generic representation of endogenous insulin production when C-peptide data is not available from the patient for specific identification of its production. Endogenous insulin production, with the base rate being k_1 [mU/min], is suppressed with elevated plasma insulin levels. The exponential suppression is described by generic constants k_2 and k_3 .

3. Model Validation Methods

Validation of the glucose-insulin model presented in Equations (9)–(14) is performed using data from 173 patients (42,941 total hours) that were on the SPRINT TGC protocol [13] for 3 or more days, which also had a statistically significant hospital mortality reductions. These patients also had long enough stays to exhibit periods of both dynamic evolution and metabolic stability. The median APACHE II score for this cohort is 19 [IQR 16, 25] and the median age is 64 [IQR 49, 73] yrs old. The percentage of operative patients is 33%.

Insulin sensitivity, S_I is the critical patient specific parameter that is fitted hourly to clinical blood glucose measurements using an integral-based fitting method [39]. The rest of the parameters are kept as population constants. This approach was verified for the ICU model via a sensitivity study [39]. (A sensitivity study is also performed in this study for the ICING model – see Section 3.4). The model is assessed for its accuracy by fitting errors, as well as robustness, or adaptability, by prediction errors. Fitting error is simply the error between the measured and the modelled blood glucose levels.

When an hourly S_I is identified, a prediction of blood glucose level in one hour using this identified S_I is also made given the clinical record of insulin and nutrition support. The prediction error is then the error between the prediction and the actual blood glucose level.

Intra- and inter-patient variability are examined by looking at the data on a *by-cohort* or *per-patient* basis. *By-cohort* analysis looks at the statistics on all the available hourly fitting and prediction errors (weighting each hour equally), whereas *per-patient* analysis looks at the statistics on each individual patient (weighting each patient equally).

Essentially the model improvements from the ICU model to the ICING model are made in two stages: firstly on the glucose compartment, secondly on the insulin pharmacokinetics. During each stage, the important population constant parameters are optimised using grid-search methods. The grid-search approach is robust to measurement noise and can provide an assessment of parameter sensitivity.

During the first stage of improvements on the glucose compartment, EGP_b and p_G are optimised as a pair. The insulin pharmacodynamics are kept as in Equations (2)–(3) during this stage – as the constant parameters in Equations (10)–(11) are yet to be optimised. In the second stage of model improvement, the ICING model takes its complete form and the constant insulin pharmacokinetics parameters are optimised. Finally a re-assessment of p_G and EGP_b , as well as a parameter sensitivity using the completed ICING model are performed.

3.1. Identification of p_G and EGP_b – Stage 1

In the first stage of model improvement, p_G and EGP_b are optimised as a pair. Constant parameter values used in this stage of parameter identification can be seen in Table 1. These constant parameters are consistent with values found in surveys of population studies [36, 37, 55], and have been verified for their suitability of being set to population constants in a previous parameter sensitivity study [39] and clinical glycaemic control studies [30, 36, 44, 48].

The range of the grid search covers $p_G = 0.001 \rightarrow 0.1$ [1/min] with increments of 0.001, and $EGP_b = 0.0 \rightarrow 3.5$ [mmol/min] with increments of 0.1. Fitting and prediction errors are calculated for each p_G , EGP_b coordinate for each patient to find the optimal combination.

3.2. Identification of Insulin Kinetics Parameters – Stage 2

Model improvements on Insulin pharmacokinetics are made in the second stage, and the model takes its final form as defined in Equations (9)–(15). Parameters associated with insulin kinetics are identified in this stage. Lotz et al. [38] uses measurements from insulin and C-peptide to identify patient specific liver clearance n_L and first pass endogenous insulin hepatic uptake x_L in Equations (7)–(8). The value for kidney clearance, n_K , was taken from a well validated population model of C-peptide kinetics, and the transcapillary diffusion rate n_I was calculated by a method proposed by the same authors [54]. For this study, ICU patient data does not contain the insulin measurements to allow for unique identification of n_L and x_L . However, the transition from Equations (2) and (3) to Equations (10) and (11) makes n_I the critical parameter to be investigated.

Table 1: Models and constant parameter values and/or ranges

<i>Constant Parameters</i>	<i>ICU Model [27]</i>	<i>S_I Test Model [38]</i>	<i>ICING Model (Final)</i>
G_E [mmol/L]	starting BG*	starting BG*	-
<i>CNS</i> [mmol/min]	-	-	0.3
α_G [L/mU]	0.0154	0	0.0154
V_G [L]	13.3	10.00–15.75	13.3
α_I [L/mU]	0.0017	0.0017	0.0017
n [1/min]	0.16	-	-
k [1/min]	0.0198	-	-
p_G [1/min]	0.01	0.01	<i>to be identified</i>
<i>EGP_b</i> [mmol/min]	-	-	<i>to be identified</i>
n_I	-	0.21–0.36 [L/min]	<i>to be identified</i> [1/min]
n_C [1/min]	-	0.032–0.033	$= n_I$
n_L [1/min]	-	0.10–0.21	0.1578
n_K [1/min]	-	0.053–0.064	0.0542
x_L	-	0.50–0.95	0.67
V_I [L]	3.15	-	3.15
V_Q [L]	-	4.44–7.47	-
V_P [L]	-	3.90–5.96	-
k_{pr} [1/min]	0.0347	-	-
k_{pd} [1/min]	0.0069	-	-
d_1 [1/min]	-	-	0.0347
d_2 [1/min]	-	-	0.0069
P_{max} [mmol/min]	-	-	6.11
k_1 [mU/min]	-	-	45.7
k_2	-	15	1.5
k_3	-	-	1000

The interstitial insulin transfer rate, k , in Equation (2) was calculated to correspond to the active interstitial insulin half-life [44]. Effectively, Equation (2) thus represents a delay compartment for insulin action in the interstitium, and can be re-written:

$$Q(t) = k \int_0^t I(\tau) e^{-k(t-\tau)} d\tau \quad (16)$$

On the other hand, the analytical solution of Q in Equation (10) is:

$$Q(t) = n_I \int_0^t I(\tau) e^{-(n_I+n_C)(t-\tau)} d\tau \quad (17)$$

Therefore, the decay rate of interstitial insulin is $n_I + n_C$ in Equation (10), and this rate should be comparable to k in Equation (2).

Studies indicated that steady state interstitial to plasma insulin ratio is between 0.4 – 0.6 [71, 72, 73]. Lotz et al. [38] uses a population value of 0.5 for this ratio. Therefore $n_I = n_C$ can be assumed from the steady state calculation using Equation (10) provided the steady state Q is low so $Q/(1 + \alpha_G Q) \approx Q$.

In this study, a grid search of n_I is used to obtain a suitable model value. Again, integral fitting is used to identify hourly S_I . The grid covers $n_I = n_C = 10^{-4} \rightarrow 0.02$ [1/min]. The fitting and prediction error are calculated at each grid for each patient. Other constant parameter values are listed in Table 1. The value for n_K is taken from Van Cauter et al. [54] and n_L is the mean fitted value found in Lotz et al. [38, 70]. First pass hepatic insulin uptake, x_L was also a fitted parameter in Lotz et al. [38], and is coupled with liver clearance n_L . In this study, x_L is assumed to be 0.67, which is within the range reported by Lotz et al. [38, 70]. In this study, x_L

has a relatively insignificant role, as patients on intensive insulin therapy can be assumed to have their endogenous insulin production suppressed due to elevated plasma insulin levels. The other constant parameters are kept the same as in the identification of p_G and EGP_b .

3.3. Re-assessment of p_G and EGP_b

A re-assessment of the population constant values of p_G and EGP_b is performed using the complete ICING model. The grid analysis covers $p_G = 0.005 \rightarrow 0.025$ [1/min] and $EGP_b = 0.5 \rightarrow 2.5$ [mmol/min] with an increment step of 0.0033 and 0.33 respectively.

3.4. Parameter sensitivity analysis

The robustness of model population parameters n_L , n_K , n_C and α_G on the model fit and predictive performance of the ICING model is tested by modifying individual model values (summarized in Table 1) by $\pm 50\%$. While one parameter is being altered, the rest of the parameters are kept at their original values in Table 1. Changes in model performance can indicate the suitability of their assumed values, and whether or not they should be used as population constants.

4. Results

4.1. p_G and EGP_b – Stage 1

The *per-patient* median fitting and prediction errors over the ranges $p_G = 0.001 \rightarrow 0.1$ [min^{-1}] and $EGP_b = 0 \rightarrow 3.5$ [mmol/min] are shown in Figure 1. Sub-figures 1(a) and 1(c) show the median of all median

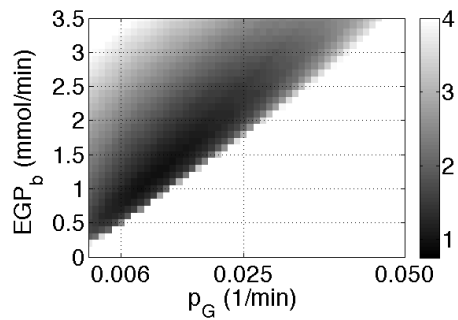
hourly % errors for each patient. Sub-figures 1(b) and 1(d) show the median range of the 90% confidence interval in hourly % error for each patient. Smaller (tighter) range means tighter distribution with less outliers. In general, lower fitting and prediction errors and error ranges are produced in the lower p_G and lower EGP_b regions, where the plot is darkest.

Figure 2(a) shows the cumulative distribution function of the prediction error over all available hourly data for the selected p_G and EGP_b combinations. The performance is very similar for $[p_G, EGP_b] = [0.002, 0.5]$, $[0.006, 0.8]$ and $[0.006, 1.16]$. However, the predictive performance is significantly worse for $EGP_b = 2.3$ mmol/min, where this value is tested to demonstrate the impact of applying an extreme, supra-physiological value across the entire cohort. In contrast, Figure 2(b) shows the cumulative distribution function of the fitting error for the same combinations of p_G and EGP_b values. The model clearly delivers the best fitting error with $[p_G, EGP_b] = [0.006, 1.16]$.

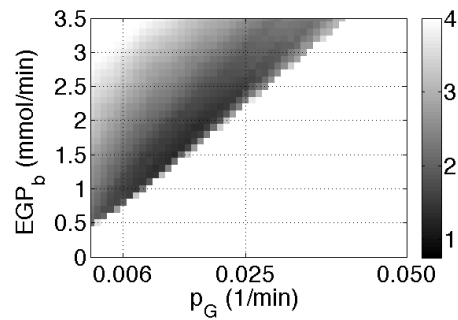
From the figures of prediction and fitting error generated, it can be observed that the best balance between fitting and prediction is achieved by the combination $[p_G, EGP_b] = [0.006, 1.16]$. Glucose metabolism studies reported EGP values range from $0.91 \rightarrow 1.4$ [mmol/min] [48, 74, 75]. The value for EGP_b identified in this study is therefore physiologically valid. Reported values for p_G from studies have been shown to range between $0.004 \rightarrow 0.047$ min^{-1} [32, 76, 77, 78]. Therefore, the identified $p_G = 0.006$ [1/min] is also physiologically valid.

4.2. Insulin Kinetics Parameters – Stage 2

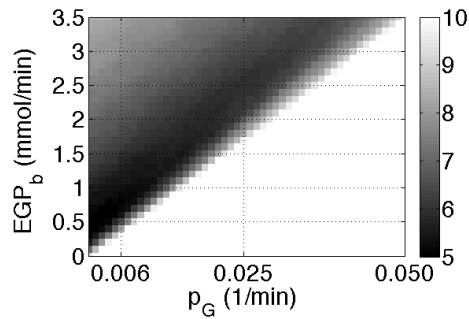
The median of the 25th, 50th and 75th percentile fitting and prediction errors for each patient across $n_I = 10^{-4} \rightarrow 0.02$ min^{-1} in the full ICING



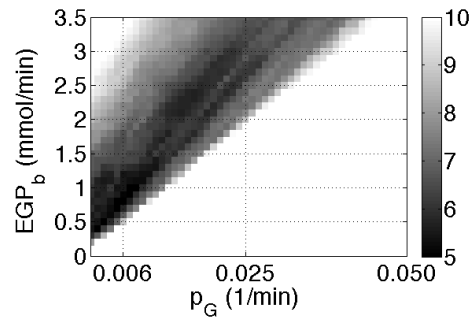
(a) Median % fitting error



(b) 90% confidence interval in % fitting error

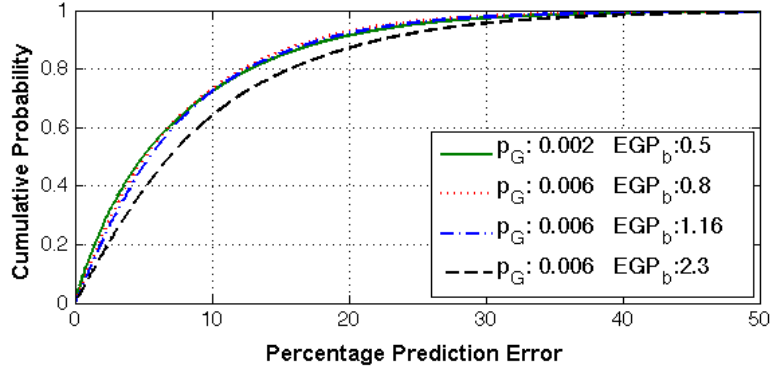


(c) Median % prediction error

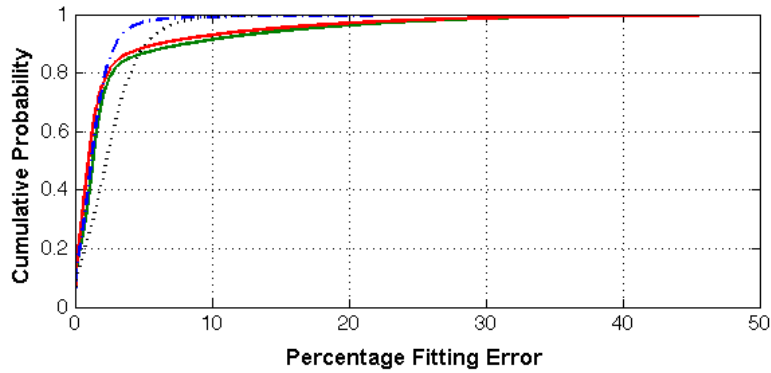


(d) 90% confidence interval in % prediction error

Figure 1: *Per-patient* percentage fitting and prediction error with respect to p_G and EGP_b . Each coordinate plots the median of the results from individual patients. 1(a) and 1(c) show the median of the median hourly % error for each patient. 1(b) and 1(d) show the median range of the 90% confidence interval in hourly % error for each patient. Smaller (tighter) range means tighter distribution with less outliers.



(a) Prediction error (%)



(b) Fitting error (%)

Figure 2: Cumulative distribution functions (cdf) of *by-cohort* prediction and fitting errors with different combinations of p_G and EGP_b . Every hourly error contribute to the cdf.

model are shown in Figure 3. It can be seen that $n_I = 0.003 \text{ min}^{-1}$ provides the best predictive performance while fitting error is low through the entire range.

Patient 5004 is shown in Figure 4 as an example of typical model fit using the fully identified ICING model. The results show the model is capable of capturing the patient's highly variable dynamics during critical illness,

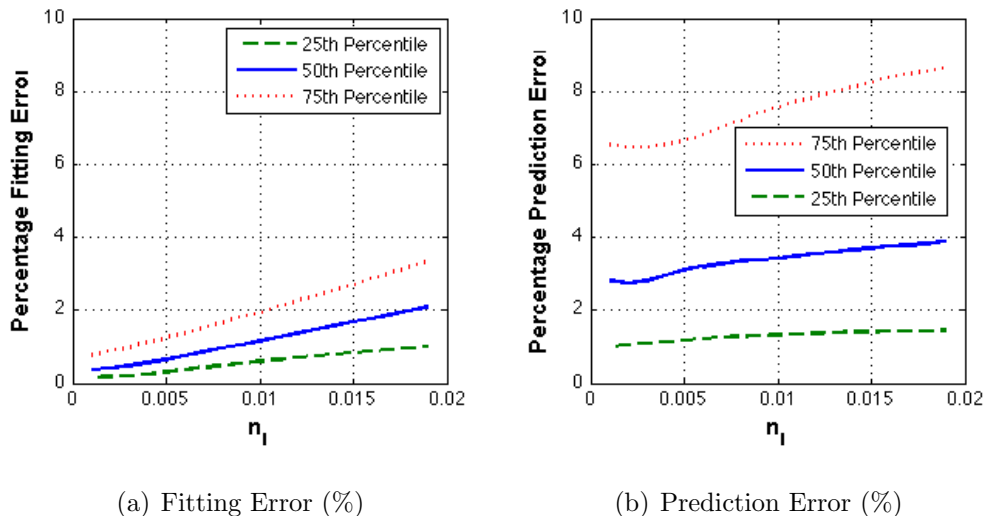


Figure 3: Fitting and prediction error from n_I grid search.

particularly from the 50th hour to the end of the patient’s stay, where the insulin requirement varied significantly from hour to hour.

In Figure 4, only *end-of-hour* insulin levels in plasma and interstitial are plotted for readability. The response curves from insulin injections plotted *by the minute* can be seen in Figure 5. The impact of n_I on modeled insulin can be seen with two different values used. The receptor bound insulin using $n_I = 0.0476 \text{ min}^{-1}$ from Lotz et al. [38] peaks and decays a lot faster than having the smaller $n_I = 0.003 \text{ min}^{-1}$ found in grid search. More importantly, the large n_I value does not allow receptor-bound insulin levels to accumulate over time. Applying this large n_I value, the model fails to capture a patient’s long term glucose-insulin response. The per-patient fitting error also increases to 5.32 [IQR 0.98, 9.70]% from 2.80 [IQR 1.18, 6.41]%. More specifically, over 25% of the hourly modeled BG fails to capture clinical

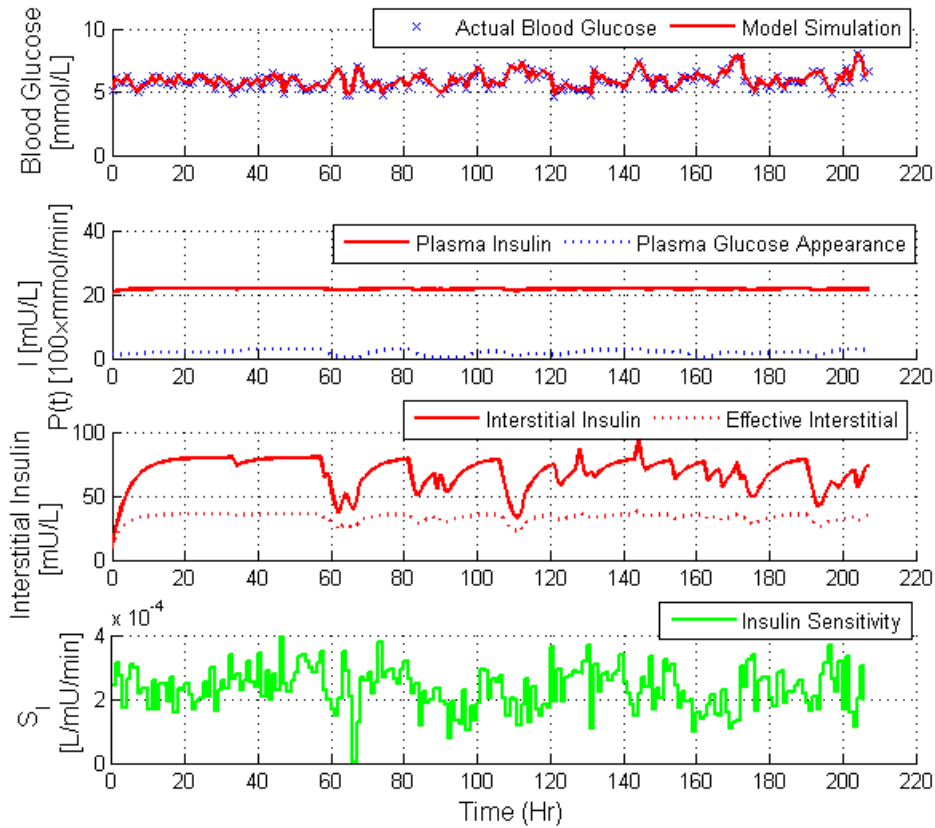


Figure 4: Model simulation results on Patient 5004 using the parameters identified for the ICING model. Only *end-of hour* data are plotted for readability. In the top panel, the solid line (–) illustrates the blood glucose model simulation while crosses (×) represents the actual blood glucose measurements. The second panel demonstrates the plasma insulin appearance (–) and plasma glucose appearance (⋯). The third panel shows the interstitial insulin (–) and the effective (receptor-bound) interstitial insulin (⋯). Model fitted insulin sensitivity is displayed in the bottom panel.

measurements, which typically have a measurement error of 7%.

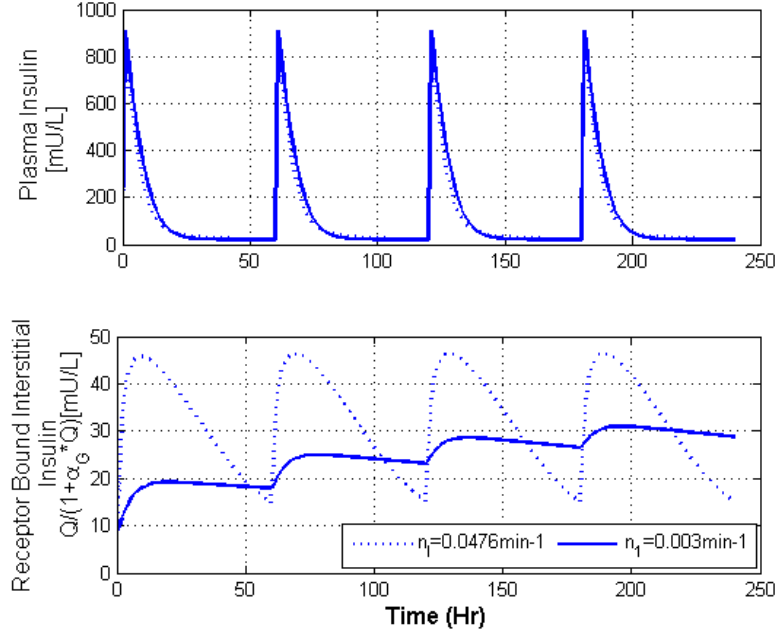


Figure 5: Dose response curves of plasma insulin and receptor bound interstitial insulin from an insulin injection of 3U at the beginning of each hour.

The improvements in model performance from the the ICU model, through improvements in glucose compartment (Stage 1), and finally the ICING model in Equations (9)–(15) are shown in Table 2. The table shows the median and IQR for absolute percentage model fit and predictive error for the total 42941 hours of clinical data from 173 patients. Results are shown on both per-patient and by cohort basis to highlight any inter- and intra-patient variability in model performance.

The final model achieved improvements in performance compared to the

ICU model in Equations (1)–(5). The predictive ability of the ICING model improved significantly with much lower median prediction errors. More importantly, the spread of error is tighter, evident by a much lower upper quartile (75th percentile) error, which is now within measurement error for both *by-cohort* and *per-patient* results. The main reduction is in the upper quartile cohort prediction error, which is reduced to 6.47% from 10.64%, indicating significantly better management of inter-patient variability in the final model.

Main results in Table 2 show:

1. Improvement in glucose compartment reduces **intra-patient** variability with lower *per-patient* upper quartile prediction.
2. Finalised ICING model reduces **inter-patient** variability with lower upper quartile *by-cohort* prediction errors.

4.3. Re-Identification of p_G and EGP_b

Grid search for the re-identification of p_G and EGP_b near the previously identified $[p_G, EGP_b] = [0.006, 1.16]$ from Section 4.1 re-affirm these values. This combination of p_G and EGP_b values provides very low fitting and prediction errors in the grid search region, and does not require adjustments.

4.4. Parameter Sensitivity

The parameter sensitivity study results for n_K , n_L , n_C and α_G are shown in Table 3. Changes of $\pm 50\%$ from their final parameter values for the ICING model in Table 1 have no clinically (as opposed to statistically) significant effect on simulation results in terms of prediction error, fitting error and

Table 2: Comparison of median and IQR for prediction and fitting error

Prediction Error (%) median [IQR]			
	<i>Original ICU Model</i>	<i>Improved Glucose Compartment</i>	<i>ICING Model</i>
Per-Patient [#]	5.90 [4.75,7.51]	5.23 [4.20,6.36]	2.80 [1.18,6.41]
By Cohort ⁺	5.59 [2.46,10.64]	5.02 [2.11,10.34]	2.81 [1.08,6.47]
Fitting Error (%) median [IQR]			
Per-Patient [#]	1.11 [0.84,1.63]	0.86 [0.58,1.18]	0.50 [0.21,0.99]
By Cohort ⁺	1.02 [0.41,1.94]	0.71 [0.23,1.44]	0.47 [0.20,0.97]
S_I (10^{-3} L/mU/min) median [IQR]			
Per-Patient [#]	0.25 [0.11,0.45]	0.21 [0.13,0.41]	0.31 [0.23,0.40]
By Cohort ⁺	0.24 [0.14,0.40]	0.21 [0.14,0.32]	0.31 [0.20,0.48]

[#] Per-patient analysis weights each patient equally, indicating *inter-patient* variability.

⁺ By-cohort analysis weights each hour of data equally, indicating *intra-patient* variability.

identified insulin sensitivity, S_I . The values for p_G , EGP_b and n_I are 0.006 [1/min], 1.16 [mmol/min] and 0.003 [1/min] respectively. These sensitivity study results suggest n_K , n_L , n_C and α_G can be fixed at their current population values without over simplifying the model. However, α_G does produce a notable shift in insulin sensitivity, S_I as expected, given their trade-off relationship mathematically. A previous study showed changes in α_G produce a magnification in insulin sensitivity S_I without compromising model performance unless it approaches non-physiological levels [79].

Table 3: Sensitivity analysis on prediction error, fitting error and S_I

	Baseline	n_K			n_L		
		+50%	-50%	+50%	-50%	+50%	-50%
Prediction Error (%)	2.81	2.82	2.78	2.88	2.73		
median [IQR]	[1.08,6.47]	[1.09,6.49]	[1.05,6.46]	[1.12,6.51]	[1.03,6.43]		
Fitting Error (%)	0.47	0.51	0.43	0.54	0.39		
median [IQR]	[0.20,0.97]	[0.22,1.02]	[0.18,0.90]	[0.24,1.08]	[0.17,0.84]		
S_I (10^{-3} L/mU/min)	0.31	0.35	0.28	0.37	0.26		
median [IQR]	[0.20,0.48]	[0.22,0.53]	[0.18,0.43]	[0.24,0.58]	[0.17,0.38]		
		n_C			α_G		
		+50%	-50%	+50%	-50%		
Prediction Error (%)	2.93	2.75	2.74	3.02			
median [IQR]	[1.13,6.52]	[1.04,6.46]	[1.03,6.40]	[1.17,6.55]			
Fitting Error (%)	0.54	0.42	0.41	0.62			
median [IQR]	[0.24,1.08]	[0.18,0.88]	[0.17,0.87]	[0.28,1.17]			
S_I (10^{-3} L/mU/min)	0.35	0.29	0.39	0.25			
median [IQR]	[0.22, 0.54]	[0.19,0.42]	[0.26,0.57]	[0.16,0.40]			

*Baseline is the model performance when no change is made to the constant parameters, and is the same as shown in Table 2 for the ICING model. Each time a parameter is studied, the other parameters are kept at the original constant values for the ICING model shown in Table 1.

5. Discussion

The new ICING model presented in this study is an integration and improvement of two clinically validated glucose-insulin physiological models [27, 38]. This new model has more explicit physiological relevance without increasing the number of patient-specific parameters to be identified. In particular, the insulin kinetics is expressed with distinctive routes for insulin clearance and transport from plasma, which reflects biological mechanisms. A more realistic model for gastric glucose absorption accounting for the stomach, gut and saturable glucose appearance is also introduced.

Parameters for endogenous glucose removal p_G , and basal endogenous glucose production EGP_b trade off each other. Therefore, it is important that they are identified as a pair. The definition for EGP_b implies this parameter stays constant for any given patient. The decision to keep p_G as a constant is based on its relatively constant behaviour in ICU patients [39]. Grid analysis for the identification of p_G and EGP_b as constants population parameters found the most suitable combination of parameter values in reported physiological ranges [32, 48, 74, 76].

Many models have tried to include an estimated time-varying function for endogenous glucose production, typically for use in experimental tracer studies [80, 81, 82, 83]. Others developed functions based on study data [34, 84, 85, 86, 87]. In reality, tracer studies require different assumptions depending on experimental settings, and results are highly variable between individuals and influenced by different conditions [75, 88, 89, 90, 91, 92]. This study uses a basal endogenous glucose production EGP_b as a constant in the mathematical model. This choice allows the variation in actual endogenous

glucose production be described by combining EGP_b , variable suppression via p_G and G , and also S_I and I . More importantly, this approach allows S_I be uniquely identified given the available data is limited to 1-2 hourly BG measurements. The value for p_G found in this study is somewhat at the lower end of the range found in other studies [32, 76, 77, 78]. It is suspected for hyperglycaemic ICU patients that the suppression of EGP by plasma glucose levels is minimized compared to otherwise healthy subjects, which has been reported elsewhere due to high levels of circulating catecholamines, thus reducing the suppression of EGP from elevated G and I [2, 3, 93, 94, 95].

Glucose uptake is strongly correlated with interstitial insulin [96]. However, interstitial insulin concentrations and dynamics are difficult or impossible to measure experimentally. This study attempted to find a realistic description of interstitial insulin by linking plasma insulin and BG response through known biological mechanisms and parameter identification. The diffusion rate between plasma and the interstitial space n_I , was identified as the critical parameter, and its population value is chosen using grid search. The identified optimal parameter value provided low fitting and prediction error in BG and particularly reduced inter-patient variability in prediction error.

“Effective” insulin half lives have been reported to be between 25–130 mins (k in Equation (16) or $n_I + n_C$ in Equation (17) to be between 0.0277–0.0053 min^{-1}) [31, 97, 98]. The value for k in the Critical Care Model was 0.0198 min^{-1} , which corresponds to a interstitial half life of 35 mins. The value for $n_I + n_C$ in the ICING model is 0.006 since $n_I = n_C = 0.003 \text{ min}^{-1}$, and correspond to a half life of 115.5 mins. The half lives from both models,

although both within the reported ranges, were on the opposite ends of the spectrum. However, when k was chosen for the Critical Care Model, clinical data were limited for its optimization [27, 36, 44]. The grid search on n_I performed in this study clearly optimized this value for model performance using currently available data.

The value for n_I identified for the new model is very low compared to that of Lotz et al. [38, 70] (0.003 v.s. $\sim 0.0476 \text{ min}^{-1}$). Lotz et al. [38, 70] used a method to calculate n_I adopted from Van Cauter et al. [54]. This method estimates n_I from an individual’s age, sex, weight, BSA, BMI and diagnosis of type 2 diabetes, developed using a model for C-peptide and its measurements. However, the n_I population value calculated using this method fails to capture long term blood glucose-insulin dynamics. Specifically, insulin “pooling” and delayed utilization effects have been observed in critically ill patients by Doran et al. [47, 99]. With n_I at such a high value, these features are lost from the model because the modeled insulin degradation is too fast. Note that given $n_I = n_C = 0.0476 \text{ min}^{-1}$, the interstitial half life of insulin from Lotz et al. [38] is more than 3 times shorter than the shortest reported time.

The discrepancy between n_I found in this study and Lotz et al. [38] may have several explanations. These explanations include inherently different plasma-interstitium diffusion rates under critical illness and insulin diffusion across barrier being a saturable process. The latter possibility arises because the experimental diffusion rates are determined by using C-peptide measurements. Although C-peptide has very similar molecular properties to insulin, it does not go through a high and variable degree of first pass extraction in

the portal vein [54]. Therefore its concentration is several folds higher than insulin in plasma. If the diffusion process is to any level saturable [50], the rates determined using C-peptide measurements will not be reflective of insulin. In addition, the plasma concentration achieved in critically ill patients is very different to that in EIC experiments or otherwise healthy diabetic individuals. Patients in [70] were subjected to an overnight fast. Hence, their plasma concentrations are relatively low and diffusion rates are faster for the short, very low insulin dose tests used in that research. In contrast, critically ill patients are often hyperinsulinaemic and infused with large amount of insulin. These ideas need to be further investigated with more insulin and C-peptide studies.

A further important issue addressed throughout this study is model identifiability. Given the limited data available, it is crucial to maintain a model that is uniquely identifiable with bedside (glucose) measurements. Although the model presented in this study requires many population assumptions, and resulted in a much simpler structure compared to many others [33, 34, 35, 100], it is able to accurately capture the highly dynamic response in critical illness. It is the authors' conclusion that given limited data in a noisy and highly variable environment, such as critical care, a model that requires the minimal number of parameters to be identified will potentially cope most successfully both mathematically and clinically. Given all the parameters kept as population constants have been carefully studied and their sensitivity analysed, this paper presents a clinically applicable yet comprehensive glucose-insulin model that is uniquely identifiable for each patient at any given time. The low, and more importantly tightly distributed, pre-

diction errors, where few fail to be within the clinical measurement error of 7-12% [13, 27], indicates the model is well suited for use in real-time, patient-specific TGC.

However, all models have limitations and this model would benefit from further investigation into some parameters. The critical parameters are those that influence the shape of $Q/(1+\alpha_G Q)$, as this level is the ultimate unknown (being unmeasurable) and the critical link between insulin and BG response. These parameters are effectively n_I and α_G , as the parameters that only appear in the plasma insulin equation (Equation (11)) can be more readily identified given insulin and C-peptide measurements. Simulation studies had been carried out to investigate the impact of these parameters, namely “effective” insulin half life and insulin-stimulated glucose removal saturation [44, 79]. Both variables have direct impact on S_I . However, given that both parameters are kept in reported range of physiological levels, their variation simply creates a shift or magnification in the identified S_I profiles and do not compromise model fitting or prediction performance. Ultimately, it is the control, or prediction performance, that is the most critical for a model designed for model-based therapeutics.

6. Conclusions

A new, more comprehensive glucose-insulin model is presented and validated using data from critically ill patients. The model is capable of accurately capturing long term dynamics and evolution of a critically ill patient’s glucose-insulin response. Insulin sensitivity S_I is the only parameter that is identified hourly for each individual. Its identification is guaranteed

to be unique given the integral fitting method used in this study. Population constant parameters p_G , EGP_b and n_I have been identified in steps to avoid model identifiability issues. Parameter sensitivity analysis further confirms the validity of limiting time-varying parameters to S_I only. The model achieved low fitting and, most importantly, low prediction error when fitted to blood glucose data from critically ill patients. Fitting errors and the 75th percentile prediction errors were all well below measurement error for 173 patient and 42,941 hours of data. The new model outperforms its critical care predecessors, and has greater physiological relevance and more detailed insulin kinetics. This model therefore offers a platform to develop robust insulin therapies for tight glycaemic control.

References

- [1] G. Van Den Berghe, P. Wouters, F. Weekers, C. Verwaest, F. Bruyninckx, M. Schetz, D. Vlasselaers, P. Ferdinande, P. Lauwers, R. Bouillon, Intensive insulin therapy in the critically ill patients, *The New England Journal of Medicine* 345 (19) (2001) 1359–67.
- [2] B. Bistrian, Hyperglycemia and Infection: Which is the Chicken and Which is the Egg?, *J Parenter Enteral Nutr* 25 (4) (2001) 180–181.
- [3] K. McCowen, C. Friel, J. Sternberg, S. Chan, R. Forse, P. Burke, B. Bistrian, Hypocaloric total parenteral nutrition: effectiveness in prevention of hyperglycemia and infectious complications—a randomized clinical trial, *Crit Care Med* 28 (11) (2000) 3606–11.
- [4] M. J. Schultz, M. J. de Graaff, M. A. Kuiper, P. E. Spronk, The

new Surviving Sepsis Campaign recommendations on glucose control should be reconsidered, *Intensive Care Med* 34 (4) (2008) 779–80, doi:10.1007/s00134-008-1027-6.

- [5] G. Van Den Berghe, A. Wilmer, I. Milants, P. J. Wouters, B. Bouckaert, F. Bruyninckx, R. Bouillon, M. Schetz, Intensive insulin therapy in mixed medical/surgical intensive care units: benefit versus harm, *Diabetes* 55 (11) (2006) 3151–9, doi:10.2337/db06-0855.
- [6] J.-C. Preiser, NICE-SUGAR: the end of a sweet dream?, *Critical Care* 13 (3) (2009) 143, doi:10.1186/cc7790.
- [7] P. Kalfon, J.-C. Preiser, Tight glucose control: should we move from intensive insulin therapy alone to modulation of insulin and nutritional inputs?, *Critical Care* 12 (3) (2008) 156, doi:10.1186/cc6915.
- [8] J.-C. Preiser, P. Devos, Clinical experience with tight glucose control by intensive insulin therapy, *Critical Care Medicine* 35 (9 Suppl) (2007) S503–7, doi:10.1097/01.CCM.0000278046.24345.C7.
- [9] J. G. Chase, G. M. Shaw, Is there more to glycaemic control than meets the eye?, *Critical Care* 11 (4) (2007) 160, doi:10.1186/cc6099.
- [10] I. Vanhorebeek, L. Langouche, G. Van Den Berghe, Tight blood glucose control: What is the evidence?, *Critical Care Medicine* 35 (Suppl) (2007) S496–S502, doi:10.1097/01.CCM.0000278051.48643.91.
- [11] E. S. Moghissi, M. T. Korytkowski, M. DiNardo, D. Einhorn, R. Hellman, I. B. Hirsch, S. E. Inzucchi, F. Ismail-Beigi, M. S. Kirkman,

- G. E. Umpierrez, American Association of Clinical Endocrinologists and American Diabetes Association consensus statement on inpatient glycemic control, *Endocr Practice* 15 (4) (2009) 353–69.
- [12] G. Van Den Berghe, A. Wilmer, G. Hermans, W. Meersseman, P. J. Wouters, I. Milants, E. V. Wijngaerden, H. Bobbaers, R. Bouillon, Intensive insulin therapy in the medical ICU, *The New England Journal of Medicine* 354 (5) (2006) 449–61, doi:10.1056/NEJMoa052521.
- [13] J. Chase, G. Shaw, A. J. Le Compte, T. Lonergan, M. Willacy, X. Wong, J. Lin, T. Lotz, D. Lee, C. E. Hann, Implementation and evaluation of the SPRINT protocol for tight glycaemic control in critically ill patients: a clinical practice change, *Crit Care* 12 (2) (2008) R49, doi:10.1186/cc6868.
- [14] J. S. Kinsley, Effect of an intensive glucose management protocol on the mortality of critically ill adult patients, *Mayo Clin Proc* 79 (8) (2004) 992–1000.
- [15] The NICE-SUGAR Study Investigators, Intensive versus Conventional Glucose Control in Critically Ill Patients, *The New England Journal of Medicine* 360 (13) (2009) 1283–97, doi:10.1056/NEJMoa0810625.
- [16] R. Shulman, S. J. Finney, C. O’Sullivan, P. A. Glynne, R. Greene, Tight glycaemic control: a prospective observational study of a computerised decision-supported intensive insulin therapy protocol, *Critical Care* 11 (4) (2007) R75, doi:10.1186/cc5964.

- [17] F. M. Brunkhorst, C. Engel, F. Bloos, A. Meier-Hellmann, M. Ragaller, N. Weiler, O. Moerer, M. Gruendling, M. Oppert, S. Grond, D. Olthoff, U. Jaschinski, S. John, R. Rossaint, T. Welte, M. Schaefer, P. Kern, E. Kuhnt, M. Kiehntopf, C. Hartog, C. Natanson, M. Loeffler, K. Reinhart, for the German Competence Network Sepsis (SepNet), Intensive insulin therapy and pentastarch resuscitation in severe sepsis, *The New England Journal of Medicine* 358 (2) (2008) 125–39, doi:10.1056/NEJMoa070716.
- [18] G. De La Rosa, J. Donado, A. Restrepo, A. Quintero, L. González, N. Saldarriaga, M. Bedoya, J. Toro, J. Velásquez, J. Valencia, C. Arango, P. Aleman, E. Vasquez, J. Chavarriaga, A. Yepes, W. Pulido, C. Cadavid, Grupo de Investigacion en Cuidado intensivo: GICI-HPTU, Strict glycaemic control in patients hospitalised in a mixed medical and surgical intensive care unit: a randomised clinical trial, *Critical Care* 12 (5) (2008) R120, doi:10.1186/cc7017.
- [19] R. S. Wiener, D. C. Wiener, R. J. Larson, Benefits and risks of tight glucose control in critically ill adults: a meta-analysis, *JAMA* 300 (8) (2008) 933–44, doi:10.1001/jama.300.8.933.
- [20] M. Treggiari, V. Karir, N. Yanez, N. Weiss, Intensive insulin therapy and mortality in critically ill patients, *Crit Care* 12 (1) (2008) R29.
- [21] D. E. G. Griesdale, R. J. de Souza, R. M. van Dam, D. K. Heyland, D. J. Cook, A. Malhotra, R. Dhaliwal, W. R. Henderson, D. R. Chittock, S. Finfer, D. Talmor, Intensive insulin therapy and mortality among

- critically ill patients: a meta-analysis including NICE-SUGAR study data, *CMAJ* 180 (8) (2009) 821–7, doi:10.1503/cmaj.090206.
- [22] M. Brownlee, Biochemistry and molecular cell biology of diabetic complications, *Nature* 414 (6865) (2001) 813–20, doi:10.1038/414813a.
- [23] I. Hirsch, M. Brownlee, Should minimal blood glucose variability become the gold standard of glycemic control?, *J Diabetes Complications* 19 (3) (2005) 178–81.
- [24] M. Egi, R. Bellomo, E. Stachowski, C. French, G. Hart, Variability of blood glucose concentration and short-term mortality in critically ill patients, *Anesthesiology* 105 (2) (2006) 244–52.
- [25] J. G. Chase, S. Andreassen, K. Jensen, G. M. Shaw, Impact of human factors on clinical protocol performance: a proposed assessment framework and case examples, *Journal of Diabetes Science and Technology* 2 (3) (2008) 409–16.
- [26] D. Aragon, Evaluation of nursing work effort and perceptions about blood glucose testing in tight glycemic control, *Am J Crit Care* 15 (4) (2006) 370–7.
- [27] J. G. Chase, G. M. Shaw, T. Lotz, A. J. Le Compte, J. Wong, J. Lin, T. Lonergan, M. Willacy, C. E. Hann, Model-based insulin and nutrition administration for tight glycaemic control in critical care, *Current Drug Delivery* 4 (4) (2007) 283–96.

- [28] J. G. Chase, G. Shaw, X. Wong, T. Lotz, J. Lin, C. E. Hann, Model-based Glycaemic Control in Critical Care - A review of the state of the possible, *Biomedical Signal Processing & Control* 1 (1) (2006) 3–21.
- [29] R. Hovorka, J. Kremen, J. Blaha, M. Matias, K. Anderlova, L. Bosanska, T. Roubicek, M. E. Wilinska, L. J. Chassin, S. Svacina, M. Haluzik, Blood glucose control by a model predictive control algorithm with variable sampling rate versus a routine glucose management protocol in cardiac surgery patients: a randomized controlled trial, *The Journal of Clinical Endocrinology and Metabolism* 92 (8) (2007) 2960–4, doi:10.1210/jc.2007-0434.
- [30] A. Le Compte, J. G. Chase, A. Lynn, C. E. Hann, G. Shaw, X.-W. Wong, J. Lin, Blood Glucose Controller for Neonatal Intensive Care: Virtual Trials Development and First Clinical Trials, *Journal of Diabetes Science and Technology* 3 (5) (2009) 1066–1081.
- [31] A. Mari, A. Valerio, A Circulatory Model for the Estimation of Insulin Sensitivity, *Control Eng Practice* 5 (12) (1997) 1747–1752.
- [32] R. Bergman, L. Phillips, C. Cobelli, Physiologic evaluation of factors controlling glucose tolerance in man: measurement of insulin sensitivity and beta-cell glucose sensitivity from the response to intravenous glucose, *J Clin Invest* 68 (6) (1981) 1456–1467.
- [33] R. S. Parker, F. J. Doyle, Control-relevant modeling in drug delivery, *Advanced Drug Delivery Reviews* 48 (2-3) (2001) 211–28.

- [34] R. Hovorka, L. J. Chassin, M. Ellmerer, J. Plank, M. E. Wilinska, A simulation model of glucose regulation in the critically ill, *Physiological Measurement* 29 (8) (2008) 959–78, doi:10.1088/0967-3334/29/8/008.
- [35] R. Hovorka, L. J. Chassin, M. E. Wilinska, V. Canonico, J. A. Akwi, M. O. Federici, M. Massi-Benedetti, I. Hutzli, C. Zaugg, H. Kaufmann, M. Both, T. Vering, H. C. Schaller, L. Schaupp, M. Bodenlenz, T. R. Pieber, Closing the loop: the adicol experience, *Diabetes Technology & Therapeutics* 6 (3) (2004) 307–18, doi:10.1089/152091504774197990.
- [36] X. Wong, I. Singh-Levett, L. Hollingsworth, G. Shaw, C. E. Hann, T. Lotz, J. Lin, O. Wong, J. G. Chase, A novel, model-based insulin and nutrition delivery controller for glycemic regulation in critically ill patients, *Diabetes Technol Ther* 8 (2) (2006) 174–90.
- [37] J. Lin, D. Lee, J. G. Chase, G. M. Shaw, A. J. Le Compte, T. Lotz, J. Wong, T. Lonergan, C. E. Hann, Stochastic modelling of insulin sensitivity and adaptive glycemic control for critical care, *Computer Methods and Programs in Biomedicine* 89 (2) (2008) 141–52, doi:10.1016/j.cmpb.2007.04.006.
- [38] T. F. Lotz, J. G. Chase, K. A. McAuley, G. M. Shaw, X.-W. Wong, J. Lin, A. J. Le Compte, C. E. Hann, J. I. Mann, Monte Carlo analysis of a new model-based method for insulin sensitivity testing, *Computer Methods and Programs in Biomedicine* 89 (3) (2008) 215–25, doi:10.1016/j.cmpb.2007.03.007.
- [39] C. E. Hann, J. G. Chase, J. Lin, T. Lotz, C. V. Doran, G. M.

- Shaw, Integral-based parameter identification for long-term dynamic verification of a glucose-insulin system model, *Computer Methods and Programs in Biomedicine* 77 (3) (2005) 259–70, doi: 10.1016/j.cmpb.2004.10.006.
- [40] J. Lin, D. Lee, J. Chase, G. Shaw, C. E. Hann, T. Lotz, J. Wong, Stochastic modelling of insulin sensitivity variability in critical care, *Biomedical Signal Processing and Control* 1 (3) (2006) 229–242, doi: 10.1016/j.bspc.2006.09.003.
- [41] T. Lotz, J. G. Chase, K. McAuley, D. Lee, J. Lin, C. E. Hann, J. Mann, Transient and steady-state euglycemic clamp validation of a model for glycemic control and insulin sensitivity testing, *Diabetes Technology and Therapeutics* 8 (3) (2006) 338–46.
- [42] T. Lotz, U. Göldenbott, J. G. Chase, P. Docherty, C. E. Hann, A minimal C-peptide sampling method to capture peak and total prehepatic insulin secretion in model-based experimental insulin sensitivity studies, *Journal of Diabetes Science and Technology* 3 (4) (2009) 875–86.
- [43] P. D. Docherty, J. G. Chase, T. Lotz, C. E. Hann, G. M. Shaw, J. Berkeley, J. I. Mann, K. A. McAuley, DISTq: An iterative analysis of glucose data for low-cost, real-time and accurate estimation of insulin sensitivity, *The Open Medical Informatics Journal* 3 (2009) 65–76, ISSN 1874-4311.
- [44] J. G. Chase, G. Shaw, J. Lin, C. Doran, C. E. Hann, M. Robertson, P. Browne, T. Lotz, G. Wake, B. Broughton, Adaptive bolus-based

targeted glucose regulation of hyperglycaemia in critical care, *Med Eng Phys* 27 (1) (2005) 1–11.

- [45] T. Lonergan, A. J. Le Compte, M. Willacy, J. G. Chase, G. M. Shaw, X.-W. Wong, T. Lotz, J. Lin, C. E. Hann, A simple insulin-nutrition protocol for tight glycemic control in critical illness: development and protocol comparison, *Diabetes Technol Ther* 8 (2) (2006) 191–206, doi: 10.1089/dia.2006.8.191.
- [46] T. Lonergan, A. J. Le Compte, M. Willacy, J. G. Chase, G. M. Shaw, X.-W. Wong, T. Lotz, J. Lin, C. E. Hann, A Pilot Study of the SPRINT Protocol for Tight Glycaemic Control in Critically Ill Patients, *Diabetes Technology and Therapeutics* 8 (4) (2006) 449–462.
- [47] C. Doran, N. Hudson, K. Moorhead, J. G. Chase, G. Shaw, C. E. Hann, Derivative weighted active insulin control modelling and clinical trials for ICU patients, *Med Eng Phys* 26 (10) (2004) 855–66.
- [48] A. Blakemore, S.-H. Wang, A. J. Le Compte, G. M. Shaw, X.-W. Wong, J. Lin, T. Lotz, C. E. Hann, J. G. Chase, Model-Based Insulin Sensitivity as a Sepsis Diagnostic in Critical Care, *Journal of Diabetes Science and Technology* 2 (3) (2008) 468–177.
- [49] J. Chase, S. Andreassen, U. Pielmeier, C. E. Hann, K. McAuley, J. Mann, A glucose-insulin pharmacodynamic surface modeling validation and comparison of metabolic system models, *Biomedical Signal Processing and Control* 4 (4) (2009) 355–363.

- [50] B. Thorsteinsson, Kinetic models for insulin disappearance from plasma in man, *Dan Med Bull* 37 (2) (1990) 143–53.
- [51] E. Ferrannini, C. Cobelli, The kinetics of insulin in man. II. Role of the liver, *Diabetes Metab Rev* 3 (2) (1987) 365–97.
- [52] E. Ferrannini, C. Cobelli, The kinetics of insulin in man. I. General aspects, *Diabetes Metab Rev* 3 (2) (1987) 335–63.
- [53] G. Toffolo, M. Campioni, R. Basu, R. Rizza, C. Cobelli, A minimal model of insulin secretion and kinetics to assess hepatic insulin extraction, *Am J Physiol Endocrinol Metab* 290 (1) (2006) E169–E176.
- [54] E. Van Cauter, F. Mestrez, J. Sturis, K. Polonsky, Estimation of insulin secretion rates from C-peptide levels. Comparison of individual and standard kinetic parameters for C-peptide clearance, *Diabetes* 41 (3) (1992) 368–77.
- [55] X.-W. Wong, J. G. Chase, C. E. Hann, T. F. Lotz, J. Lin, A. J. Le Compte, G. M. Shaw, Development of a Clinical Type 1 Diabetes Metabolic System Model and in Silico Simulation Tool, *Journal of Diabetes Science and Technology* 2 (3) (2008) 424–435.
- [56] S. G. Hasselbalch, G. M. Knudsen, C. Videbaek, L. H. Pinborg, J. F. Schmidt, S. Holm, O. B. Paulson, No effect of insulin on glucose blood-brain barrier transport and cerebral metabolism in humans, *Diabetes* 48 (10) (1999) 1915–21.
- [57] S. G. Hasselbalch, P. L. Madsen, G. M. Knudsen, S. Holm, O. B. Paulson, Calculation of the FDG lumped constant by simultaneous

- measurements of global glucose and FDG metabolism in humans, *J Cereb Blood Flow Metab* 18 (2) (1998) 154–60.
- [58] S. G. Hasselbalch, P. L. Madsen, L. P. Hageman, K. S. Olsen, N. Justesen, S. Holm, O. B. Paulson, Changes in cerebral blood flow and carbohydrate metabolism during acute hyperketonemia, *Am J Physiol* 270 (5 Pt 1) (1996) E746–51.
- [59] A. D. Baron, G. Brechtel, P. Wallace, S. V. Edelman, Rates and tissue sites of non-insulin- and insulin-mediated glucose uptake in humans, *Am J Physiol* 255 (6 Pt 1) (1988) E769–74.
- [60] H. Takeshita, Y. Okuda, A. Sari, The effects of ketamine on cerebral circulation and metabolism in man, *Anesthesiology* 36 (1) (1972) 69–75.
- [61] P. J. Cohen, S. C. Alexander, T. C. Smith, M. Reivich, H. Wollman, Effects of hypoxia and normocarbica on cerebral blood flow and metabolism in conscious man, *Journal of Applied Physiology* 23 (2) (1967) 183–9.
- [62] G. Strauss, K. Moller, F. Larsen, J. Kondrup, G. M. Knudsen, Cerebral glucose and oxygen metabolism in patients with fulminant hepatic failure, *Liver Transplantation* 9 (12) (2003) 1244–1252.
- [63] N. Hattori, S.-C. Huang, H.-M. Wu, E. Yeh, T. C. Glenn, P. M. Vespa, D. McArthur, M. E. Phelps, D. A. Hovda, M. Bergsneider, Correlation of Regional Metabolic Rates of Glucose with Glasgow Coma Scale After Traumatic Brain Injury, *J Nucl Med* 44 (11) (2003) 1709–16.

- [64] E. M. Bingham, D. Hopkins, D. Smith, A. Pernet, W. Hallett, L. Reed, P. K. Marsden, S. A. Amiel, The role of insulin in human brain glucose metabolism: an 18fluoro-deoxyglucose positron emission tomography study, *Diabetes* 51 (12) (2002) 3384–90.
- [65] A. M. McCarthy, J. S. Elmendorf, GLUT4’s itinerary in health & disease, *Indian J Med Res* 125 (3) (2007) 373–88.
- [66] L. J. Foster, A. Klip, Mechanism and regulation of GLUT-4 vesicle fusion in muscle and fat cells, *Am J Physiol, Cell Physiol* 279 (4) (2000) C877–90.
- [67] N. J. Bryant, R. Govers, D. E. James, Regulated transport of the glucose transporter GLUT4, *Nat Rev Mol Cell Biol* 3 (4) (2002) 267–77, doi:10.1038/nrm782.
- [68] S. K. Andersen, J. Gjedsted, C. Christiansen, E. Tønnesen, The roles of insulin and hyperglycemia in sepsis pathogenesis, *Journal of Leukocyte Biology* 75 (3) (2004) 413–21, doi:10.1189/jlb.0503195.
- [69] W. C. Duckworth, R. G. Bennett, F. G. Hamel, Insulin degradation: progress and potential, *Endocr Rev* 19 (5) (1998) 608–24.
- [70] T. Lotz, High Resolution Clinical Model-Based Assessment of Insulin Sensitivity, PhD Thesis, Mechanical Engineering, University of Canterbury, Christchurch, New Zealand .
- [71] S. Gudbjörnsdóttir, M. Sjöstrand, L. Strindberg, J. Wahren, P. Lönnroth, Direct measurements of the permeability surface area for

- insulin and glucose in human skeletal muscle, *The Journal of Clinical Endocrinology and Metabolism* 88 (10) (2003) 4559–64.
- [72] M. Sjöstrand, A. Holmäng, P. Lönnroth, Measurement of interstitial insulin in human muscle, *Am J Physiol* 276 (1 Pt 1) (1999) E151–4.
- [73] M. Sjostrand, A. Holmang, L. Strindberg, P. Lonroth, Estimations of muscle interstitial insulin, glucose, and lactate in type 2 diabetic subjects, *Am J Physiol Endocrinol Metab* 279 (5) (2000) E1097–103.
- [74] L. Tappy, M. Berger, J. M. Schwarz, M. McCamish, J. P. Revelly, P. Schneiter, E. Jéquier, R. Chioléro, Hepatic and peripheral glucose metabolism in intensive care patients receiving continuous high- or low-carbohydrate enteral nutrition, *JPEN Journal of parenteral and enteral nutrition* 23 (5) (1999) 260–7.
- [75] C. Chambrier, M. Laville, R. B. K, M. Odeon, P. Boulétreau, M. Beylot, Insulin sensitivity of glucose and fat metabolism in severe sepsis, *Clin Sci* 99 (4) (2000) 321–8.
- [76] C. Cobelli, A. Caumo, M. Omenetto, Minimal model SG overestimation and SI underestimation: improved accuracy by a Bayesian two-compartment model, *Am J Physiol* 277 (3 Pt 1) (1999) E481–488.
- [77] C. McDonald, A. Dunaif, D. Finegood, Minimal-model estimates of insulin sensitivity are insensitive to errors in glucose effectiveness, *J Clin Endocrinol Metab* 85 (7) (2000) 2504–2508.
- [78] G. Pillonetto, G. Sparacino, P. Magni, R. Bellazzi, C. Cobelli, Minimal model $S_I = 0$ problem in NIDDM subjects: nonzero Bayesian estimates

- with credible confidence intervals, *Am J Physiol Endocrinol Metab* 282 (3) (2002) E564–573.
- [79] J. G. Chase, G. M. Shaw, J. Lin, C. V. Doran, M. Bloomfield, G. C. Wake, B. Broughton, C. Hann, T. Lotz, Impact of Insulin-Stimulated Glucose Removal Saturation on Dynamic Modelling and Control of Hyperglycaemia, *International Journal of Intelligent Systems Technologies and Applications (IJISTA)* 1 (1/2) (2004) 79–94.
- [80] C. Dalla Man, A. Caumo, R. Basu, R. Rizza, G. Toffolo, C. Cobelli, Minimal model estimation of glucose absorption and insulin sensitivity from oral test: validation with a tracer method, *American Journal of Physiology-Endocrinology and Metabolism* 287 (4) (2004) E637–E643.
- [81] A. Avogaro, P. Vicini, A. Valerio, A. Caumo, C. Cobelli, The hot but not the cold minimal model allows precise assessment of insulin sensitivity in NIDDM subjects, *Am J Physiol* 270 (3 Pt 1) (1996) E532–40.
- [82] A. Caumo, C. Cobelli, Hepatic glucose production during the labeled IVGTT: estimation by deconvolution with a new minimal model, *Am J Physiol* 264 (5 Pt 1) (1993) E829–41.
- [83] A. Mari, J. Wahren, R. A. DeFronzo, E. Ferrannini, Glucose absorption and production following oral glucose: comparison of compartmental and arteriovenous-difference methods, *Metab Clin Exp* 43 (11) (1994) 1419–25.

- [84] D. Araujo-Vilar, C. A. Rega-Liste, D. A. Garcia-Estevez, F. Sarmiento-Escalona, V. Mosquera-Tallon, J. Cabezas-Cerrato, Minimal model of glucose metabolism: modified equations and its application in the study of insulin sensitivity in obese subjects, *Diabetes Research and Clinical Practice* 39 (2) (1998) 129–41.
- [85] U. Picchini, A. D. Gaetano, S. Panunzi, S. Ditlevsen, G. Mingrone, A mathematical model of the Euglycemic Hyperinsulinemic Clamp, *Theor Biol Med Model* 2 (2005) 44.
- [86] E. Ruiz-Velázquez, R. Femat, D. Campos-Delgado, Blood glucose control for type I diabetes mellitus: A robust tracking H_∞ problem, *Control Engineering Practice* 12 (2004) 1179–1195.
- [87] H. E. Silber, P. M. Jauslin, N. Frey, R. Gieschke, U. S. H. Simonsson, M. O. Karlsson, An integrated model for glucose and insulin regulation in healthy volunteers and type 2 diabetic patients following intravenous glucose provocations, *The Journal of Clinical Pharmacology* 47 (9) (2007) 1159–71, doi:10.1177/0091270007304457.
- [88] A. D. Cherrington, D. Edgerton, D. K. Sindelar, The direct and indirect effects of insulin on hepatic glucose production in vivo, *Diabetologia* 41 (9) (1998) 987–96.
- [89] M. Mevorach, A. Giacca, Y. Aharon, M. Hawkins, H. Shamoan, L. Rossetti, Regulation of endogenous glucose production by glucose per se is impaired in Type 2 diabetes mellitus, *The Journal of Clinical Investigation* 102 (4) (1998) 744–753.

- [90] L. U. Monzillo, O. Hamdy, Evaluation of insulin sensitivity in clinical practice and in research settings, *Nutr Rev* 61 (12) (2003) 397–412.
- [91] A. Cherrington, Banting Lecture 1997. Control of glucose uptake and release by the liver in vivo, *Diabetes* 48 (5) (1999) 1198–214.
- [92] D. Elahi, G. Meneilly, K. Minaker, D. Andersen, J. Rowe, Escape of hepatic glucose production during hyperglycemic clamp, *Am J Physiol* 257 (5 Pt 1) (1989) E704–11.
- [93] B. Mizock, Alterations in fuel metabolism in critical illness: hyperglycaemia, *Best Pract Res Clin Endocrinol Metab* 15 (4) (2001) 533–51.
- [94] A. Thorell, O. Rooyackers, P. Myrenfors, M. Soop, J. Nygren, O. Ljungqvist, Intensive insulin treatment in critically ill trauma patients normalizes glucose by reducing endogenous glucose production, *J Clin Endocrinol Metab* 89 (11) (2004) 5382–6.
- [95] K. M. Dungan, S. S. Braithwaite, J.-C. Preiser, Stress hyperglycaemia, *Lancet* 373 (9677) (2009) 1798–807.
- [96] R. Poulin, G. Steil, D. Moore, M. Ader, R. Bergman, Dynamics of glucose production and uptake are more closely related to insulin in hindlimb lymph than in thoracic duct lymph., *Diabetes* 43 (2) (1994) 180(11).
- [97] A. Natali, A. Gastaldelli, S. Camastra, A. Sironi, E. Toschi, A. Masoni, E. Ferrannini, A. Mari, Dose-response characteristics of insulin action on glucose metabolism: a non-steady-state approach, *Am J Physiol Endocrinol Metab* 278 (5) (2000) E794–801.

- [98] K. Turnheim, W. Waldhausl, Essentials of insulin pharmacokinetics, *Wien Klin Wochenschr* 100 (3) (1988) 65–72.
- [99] C. Doran, J. G. Chase, G. Shaw, K. Moorhead, N. Hudson, Automated insulin infusion trials in the intensive care unit, *Diabetes Technol Ther* 6 (2) (2004) 155–65.
- [100] R. S. Parker, F. J. Doyle, N. A. Peppas, The intravenous route to blood glucose control, *IEEE engineering in medicine and biology magazine: the quarterly magazine of the Engineering in Medicine & Biology Society* 20 (1) (2001) 65–73.