

Electronic and spin structure of the wide-band-gap topological insulator: Nearly stoichiometric $\text{Bi}_2\text{Te}_2\text{S}$

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We have grown the phase-homogeneous ternary compound with composition $\text{Bi}_2\text{Te}_{1.85}\text{S}_{1.15}$ very close to the stoichiometric $\text{Bi}_2\text{Te}_2\text{S}$. The measurements performed with spin- and angle-resolved photoelectron spectroscopy as well as density functional theory and GW calculations revealed a wide-band-gap three-dimensional topological insulator phase. The surface electronic spectrum is characterized by the topological surface state (TSS) with Dirac point located above the valence band and Fermi level lying in the band gap. TSS band dispersion and constant energy contour manifest a weak warping effect near the Fermi level along with in-plane and out-of-plane spin polarization along the $\bar{\Gamma}-\bar{K}$ line. We identified four additional states at deeper binding energies with high in-plane spin polarization.

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I. INTRODUCTION

Topological insulators (TIs) are characterized by an insulating energy gap in the bulk and the gapless spin-polarized metallic surface states with linear Dirac conelike dispersion in the energy-momentum space with helical spin textures protected by time-reversal symmetry, which can favor the quantum spin transport without heat dissipation [1,2].

The binary tetradymitelike Bi chalcogenides Bi_2Se_3 and Bi_2Te_3 are widely regarded as model examples of the three-dimensional topological insulators since they host a single metallic Dirac state [1–7]. However, these compounds are not insulators, but have metallic bulk conductivity as a consequence of unintentional doping by defects: the Se vacancies in Bi_2Se_3 and Bi-Te antisite defects in Bi_2Te_3 [4,5,8]. The isolation of the surface states from the bulk electronic states and the Fermi level (E_F) located in the bulk band gap is the minimal requirement for the quantum spin transport. To this end, various experimental efforts exploited the tune of E_F with doping [7,9]. On the other hand, the dopants themselves could become a scattering source and therefore reduce spin lifetime [10]. One of the strategies to control the native defects in Te- and Se-containing TIs is using ternary Bi-Te-Se alloy systems.

It was demonstrated that the solutions with Te-rich and Se-poor conditions minimize the defects and manifest a single Dirac cone that intersects the Fermi level [8,10–13].

The electronic structure of tetradymite itself, $\text{Bi}_2\text{Te}_2\text{S}$, has been calculated in several works [14–16] alongside other ternary compounds. In contrast to $\text{Bi}_2(\text{Te}_{1-x}\text{Se}_x)_3$ solid solutions, $\text{Bi}_2\text{Te}_2\text{S}$ is a separate compound of the B_2Te_3 - Bi_2S_3 system [17,18]. According to the recent review on natural tetradymites by Cook *et al.* [19], a homogeneity region for the compound seems to occupy a wide range of compositions (30–40 mol.% of Bi_2S_3). On the other hand, Glatz [20] has assumed that $\text{Bi}_2\text{Te}_2\text{S}$ forms two phases—an incongruent close-to-stoichiometric (Te-rich) β phase and a sulfur-rich γ phase with congruent melting. The latter phase with composition of $\text{Bi}_2\text{Te}_{1.6}\text{S}_{1.4}$ and cell parameters of $a = 4.196(4)$ Å and $c = 29.44(3)$ Å was studied by Ji *et al.* [21]. The angle-resolved photoemission spectroscopy (ARPES) measurements revealed that the S-rich phase is a three-dimensional (3D) TI with a band gap of 200 meV.

This work aims to provide a detailed characterization of the electronic and spin structures of topological and higher binding-energy (BE) surface states in the nearly stoichiometric $\text{Bi}_2\text{Te}_2\text{S}$ grown by a modified vertical Bridgman method. We show that the surface electronic spectrum of this compound is characterized by the topological surface state (TSS), which Dirac point is located above the valence band and Fermi level

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lying in the band gap. Owing to its remarkable electronic properties consisting of ≈ 400 meV bulk band gap and weakly warped topological Dirac state, the $\text{Bi}_2\text{Te}_2\text{S}$ can be regarded as the model topological insulator to a greater extent than the extensively used Bi_2Se_3 . Apart from the interesting property related to the TSS, the topological insulator manifests an electronic structure, which can be a fruitful playground for more traditional effects in electronic surface science: band bending near the surface, formation of the quantum well states, and the Rashba-split deep surface states.

II. EXPERIMENTAL AND COMPUTATIONAL DETAILS

The synthesis of charge was done by careful fusion of elementary Bi, Te, and S in a horizontal quartz ampoule. Then the charge was transferred into a carbon-coated ampoule with conical tip and recrystallized by the modified vertical Bridgman method [22,23]. At both stages, the ampoules were evacuated down to 10^{-3} torr before sealing. The samples cut from the obtained single-crystalline boule had a composition $\text{Bi}_2\text{Te}_{1.85}\text{S}_{1.15}$ according to energy-dispersive x-ray chemical analysis. Powder diffraction data confirmed the tetradymite structure with cell parameters $a = 4.241$ Å, $c = 29.578$ Å (Fig. 1). According to differential thermal analysis, the sample melts congruently at ≈ 595 °C. The obtained data do not allow unambiguous attribution of the grown crystal to the γ or β phase described in Ref. [20]. We state the production of a phase-homogeneous single-crystal material with a composition much closer to the stoichiometry of $\text{Bi}_2\text{Te}_2\text{S}$ than that studied in Ref. [21]. The measured in-plane Seebeck coefficient of the grown sample demonstrated -250 $\mu\text{V}/\text{K}$ at room temperature, suggesting an n -type conductivity. This value is comparable with the in-plane Seebeck coefficient of Bi_2Te_3 , equal to -280 $\mu\text{V}/\text{K}$. The resistivity of the grown crystal showed a slightly higher value than for ternary compounds of the $\text{Bi}_2(\text{Te}_{1-x}\text{Se}_x)_3$ series [13].

The ARPES experiment was performed at Laser-ARPES at the Hiroshima Synchrotron Radiation Center (HiSOR) using s -polarized light of 6.45 eV and measured with a hemispherical analyzer (VG Scienta SES R4000) at 70 K. The sample was cleaved *in situ* at room temperature in an ultrahigh vacuum below 1×10^{-8} Pa. The spin-resolved energy distribution

curves (EDCs) are acquired with the efficient spin-resolved spectroscopy ESPRESSO end station at HiSOR [24,25] at 70 and 15 K. An He I_α discharge lamp and p -polarized synchrotron light of 17 eV are used as the excitation source for the spin-resolved photoemission experiment. The overall energy resolutions are set to 20 meV at the spin-ARPES end station.

Electronic structure calculations were carried out within the density functional theory (DFT) and GW approaches. The ground state has been obtained using the projector augmented-wave method [26,27] realized in the VASP code [28,29]. For this calculation, the Perdew, Burke, and Ernzerhof exchange-correlation functional [30] with DFT-D3 van der Waals correction [31] was applied and the spin-orbit coupling was accounted in self-consistent electronic structure calculations. We applied $7 \times 7 \times 7$ Γ -centered k -point sampling of the Brillouin zone. The GW correction has been calculated with *a posteriori* treatment of spin-orbit effects: this contribution is taken from the DFT calculations. Next, from the quasiparticle spectrum, we construct a bulk tight-binding model using the WANNIER90 code [32]. The chosen basis consists of six spinor p -type orbitals for each atom: $|p_x^\uparrow\rangle$, $|p_y^\uparrow\rangle$, $|p_z^\uparrow\rangle$, $|p_x^\downarrow\rangle$, $|p_y^\downarrow\rangle$, and $|p_z^\downarrow\rangle$. The low-lying s orbitals are not taken into consideration. The surface tight-binding model is derived from the bulk one with the inclusion of band-bending effects obtained from surface calculations within DFT [33]. To study the electronic structure of $\text{Bi}_2\text{Te}_{1.85}\text{S}_{1.15}$, which differs from the stoichiometric compound, an extra 7.5% of sulfur is randomly distributed within each Te atomic layer. First, the bulk GW calculations have been performed for the hypothetical Bi_2S_3 with the same lattice parameters as for $\text{Bi}_2\text{Te}_2\text{S}$. Then we used the virtual crystal approximation to construct the tight-binding Hamiltonian for the bulk $\text{Bi}_2\text{Te}_{1.85}\text{S}_{1.15}$ as follows: $\hat{H}_{\text{Bi}_2\text{Te}_{1.85}\text{S}_{1.15}} = 0.925\hat{H}_{\text{Bi}_2\text{Te}_2\text{S}} + 0.075\hat{H}_{\text{Bi}_2\text{S}_3}$. The band-bending effect in the surface tight-binding model for nearly stoichiometric $\text{Bi}_2\text{Te}_{1.85}\text{S}_{1.15}$ was taken to be the same as for the $\text{Bi}_2\text{Te}_2\text{S}$ compound.

III. RESULTS AND DISCUSSIONS

The DFT calculations [Fig. 2(a)] for stoichiometric $\text{Bi}_2\text{Te}_2\text{S}$ reproduce the results of earlier works [14,15], demonstrating an indirect bulk gap of ~ 300 meV with the valence-band maximum (VBM) situated in the $\bar{\Gamma}-\bar{M}$ direction at $k_{\parallel} = 0.19$ Å $^{-1}$ and spin-polarized topological surface state at $\bar{\Gamma}$ lying at 130 meV below VBM. It was shown earlier that the inclusion of many-body effects within the GW approximation decreases the size of the bulk band gap at the Brillouin-zone center in the TI spectrum and increases the absolute band gap lowering the valence-band maximum [16,34–38], and even converting the indirect gap into the direct one in the case of Bi_2Se_3 [38,39]. The calculated quasiparticle spectrum of $\text{Bi}_2\text{Te}_2\text{S}$ [Fig. 2(b)] demonstrates the increase of the indirect bulk band gap up to 390 meV and reduction in the difference between the VBM and maximum of the valence band at $\bar{\Gamma}$ by 95 meV. Such changes in the bulk states also result in modification of the surface states and lead to pulling out the Dirac point above the VBM in accordance with experimental finding (which we show below). Accounting for the deviation of composition from stoichiometry does not lead to sizable modification of the bulk

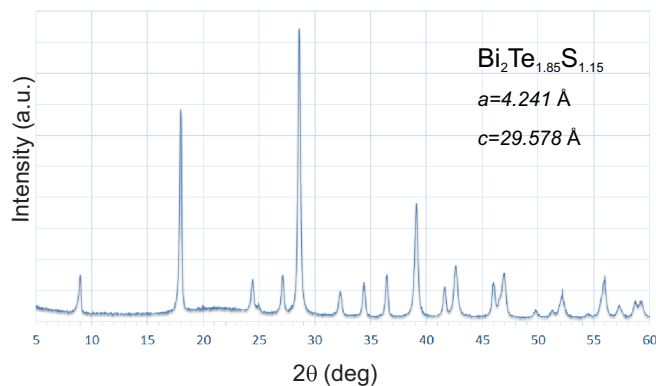


FIG. 1. X-ray powder diffraction pattern for $\text{Bi}_2\text{Te}_{1.85}\text{S}_{1.15}$ single-crystal sample.

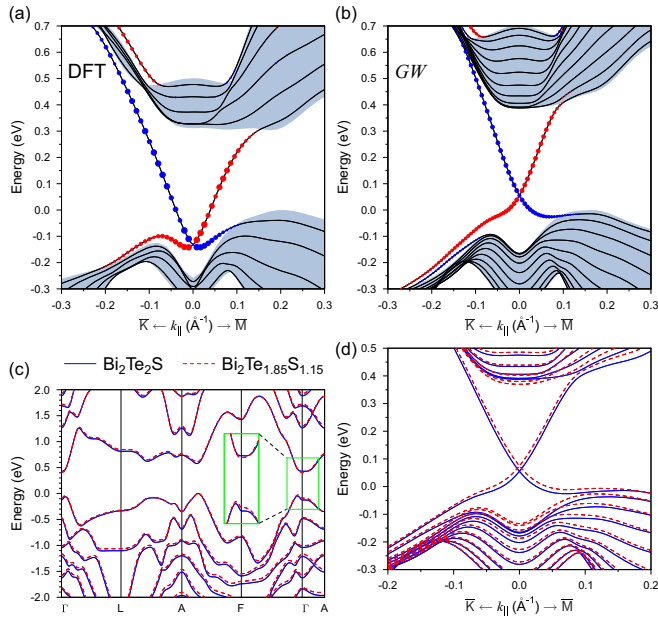


FIG. 2. The surface electronic spectrum of the $\text{Bi}_2\text{Te}_2\text{S}$ calculated within the (a) DFT and (b) GW approaches. The comparison of the $\text{Bi}_2\text{Te}_2\text{S}$ and $\text{Bi}_2\text{Te}_{1.85}\text{S}_{1.15}$ GW spectra for (c) bulk and (d) surface.

band spectrum [see Fig. 2(c)]. The main change introduced by the appearance of an extra sulfur on the tellurium layers of a quintuple layer block is the reduction of the Γ gap (by 54 meV), while the absolute gap is reduced by 20 meV only. The resulting bulk gap of 370 meV is more than 100 meV larger than the GW gap in prototypical TI Bi_2Se_3 [39]. At the same time, the deviation from stoichiometry does not change the dispersion of the TSS and only moves up the Dirac point by 19 meV [Fig. 2(d)]. Since the small deviation from the stoichiometric composition does not lead to any noticeable changes in the bulk and surface electronic spectra, below, for simplicity, we will call the grown near-stoichiometric compound as $\text{Bi}_2\text{Te}_2\text{S}$.

Figure 3 shows the experimental electronic structure close to E_F on $\text{Bi}_2\text{Te}_2\text{S}$ along the $\bar{\Gamma}-\bar{M}$ direction. Measurements were performed at different photon energies (6.45, 17, and 21 eV) and light polarization (s , p , and unpolarized light) at 70 K, except for the spectra at 17 eV obtained at 15 K. Variation of the photon energy leads to a modulation of the

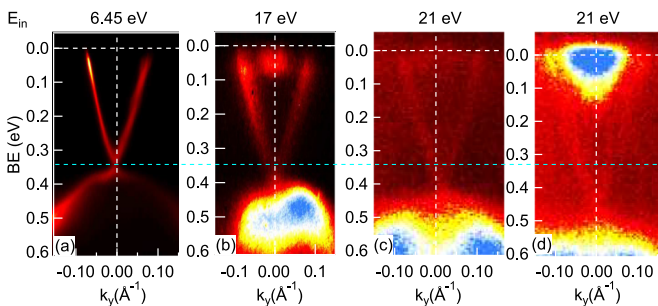


FIG. 3. ARPES spectra measured along $\bar{\Gamma}-\bar{M}$ with different photon energies: (a) 6.45 eV (s polarization) at 70 K, (b) 17 eV (p polarization) at 15 K, and (c),(d) 21.2 eV at 70 K. (d) Measurements on the same sample after 1 h of exposure to the discharge He lamp.

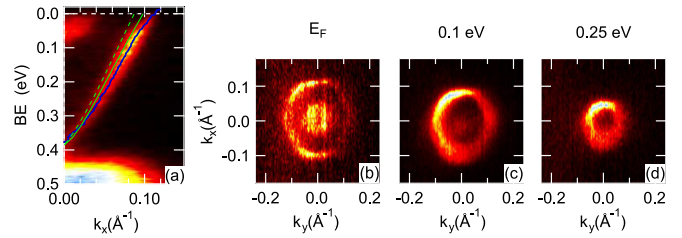


FIG. 4. (a) $E(k)$ photoemission map along $\bar{\Gamma}-\bar{K}$. The solid blue curve is a guide for the eyes; the solid and dashed green curves are dispersions of the TSS calculated within the DFT and GW approaches, respectively. (b),(c) Constant energy contours of the topological surface state at different binding energies from 0 to 0.25 eV. Measurements were performed with p -polarized light at 15 K.

photoemission intensity for both the topological surface state and the valence-band states [Figs. 3(a)–3(d)]. Figure 3(a) displays a single Dirac cone. The Dirac point (DP) and VBM are visible at binding energy of 0.34 and 0.36 eV, respectively. As far as the conduction band is not visible in the ARPES spectrum, we can estimate the bulk gap as of ≈ 400 meV, which is in fine agreement with the calculation result and is twice as large as the bulk gap reported for $\text{Bi}_2\text{Te}_{1.6}\text{S}_{1.4}$ (200 meV) [21].

A different position of the Dirac point is observed by changing the photon source. A fresh sample exposed to synchrotron light does not exhibit any shift of the Dirac point, which is always present in case of He I_α unpolarized light excitation. The position of the Dirac point shifts rigidly towards higher binding energy [Figs. 3(c) and 3(d)] and a two-dimensional electron gas appears at the Fermi level [Fig. 3(d)]. The binding energy of the Dirac point saturates after 1 h exposure to an He discharge lamp. Similar behavior is observed for other topological insulators originating from the band-bending effect as a consequence of the n -type doping provided by adsorption of residual gases [40–42].

Figure 4(a) shows band energy dispersion along the $\bar{\Gamma}-\bar{K}$ direction. Although the GW calculation results are in perfect agreement with experiment in part of the bulk gap and the Dirac-point position, the DFT calculation reproduces the experimental TSS slope slightly better [see the green solid and dashed curves in Fig. 4(a)]. The constant energy contours of the TSS evolve from the hexagonal to a circular shape in going from binding energy of 0.25 to 0 eV [Figs. 4(b) and 4(c)], indicating a weak warping effect [12,43,44].

We estimated the energy of the Dirac point, the effective mass m^*/m of the TSS, the Dirac velocity v , and the warping strength coefficient λ by analyzing the photoemission data according to Refs. [43,44], as reported in Table I. As can be seen from the table, the TSS of $\text{Bi}_2\text{Te}_2\text{S}$ has the warping comparable with that in Bi_2Se_3 and a Fermi velocity in between those in prototypical TIs Bi_2Te_3 and Bi_2Se_3 .

Representative spin-resolved EDCs for in-plane and out-of-plane components were measured at different k points, as displayed in Fig. 5. $\text{Bi}_2\text{Te}_2\text{S}$ has a sizable in-plane and out-of-plane spin component (50% and 20%, respectively), and the up and down spins are reversed between opposite k points along the $\bar{\Gamma}-\bar{K}$ and $\bar{\Gamma}-\bar{M}$ cuts. This is in agreement with previous results on binary and ternary topological insulators

TABLE I. m^*/m , v , and λ obtained from the analysis of the ARPES data. Values for Bi_2Te_3 and Bi_2Se_3 are taken from Ref. [44].

	$\text{Bi}_2\text{Te}_2\text{S}$	Bi_2Te_3	Bi_2Se_3
DP (eV)	0.34	0.29	0.33
m^*/m	0.19	-0.3	0.3
v (eV \AA)	3.2	3.8	2.1
λ (eV \AA^{-3})	60	210	50

where an out-of-plane spin polarization is concomitant with TSS hexagonal warping [12,43,44].

Figure 6(a) shows the ARPES spectra for deep-lying states taken at He I_α along the $\bar{\Gamma}$ - \bar{K} direction. The characteristic features of the photoemission data are (i) two upward-convex parabolic states S_1 centered at $\pm 0.11 \text{\AA}^{-1}$, with maximum at BE = 0.7 eV and separated in two subbands for $k \geq |0.25| \text{\AA}^{-1}$; (ii) the bright feature S_2 at BE = 1.23 eV; (iii) an upward-convex arc S_3 with binding-energy maximum at 1.75 eV at $k = 0$; (iv) two upward-convex parabolic states S_4 centered at $\pm 0.15 \text{\AA}^{-1}$, with maximum at BE = 2.3 eV and crossing point at BE = 2.6 eV. Figure 6(b) shows the calculated spectrum. The comparison with the calculations allows us to determine the nature of each state appearing in the photoemission map. The S_1 state can be assigned to the Rashba-split state, residing near the bottom of the first local valence-band gap, which is typical for tetradymitelike TIs [45]. It manifests as a peculiar band deviating from typical Rashba-split states by the suppression of the inner Rashba-split band in the vicinity of the Brillouin-zone center due to hybridization with bulk states. The bright feature at BE = 1.23 eV (S_2) in the photoemission map derives from the spin-split band residing in the second local valence-band gap at ≈ -0.7 eV [Fig. 6(b)]. The wide arc S_3 can be assigned to the fourth bulk valence band in

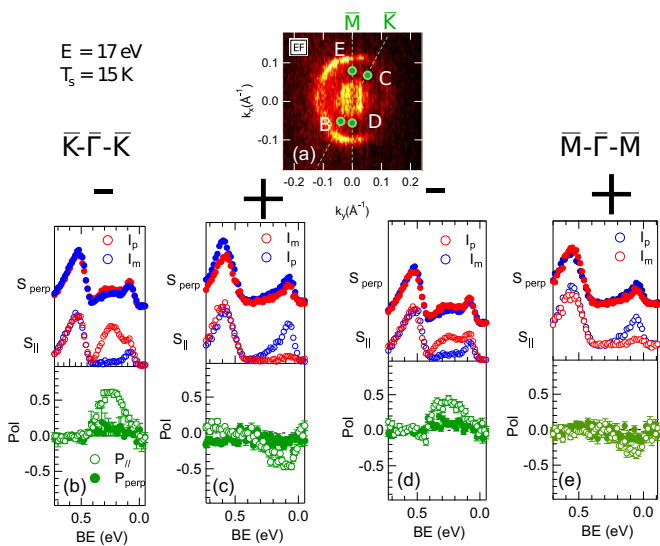


FIG. 5. (a) The constant energy contour of topological surface states at E_F . (b)–(e) Spin-resolved EDCs along $\bar{\Gamma}$ - \bar{K} and $\bar{\Gamma}$ - \bar{M} in k space as identified by the letters in (a). Measurements were performed with p -polarized light of 17 eV at 15 K.

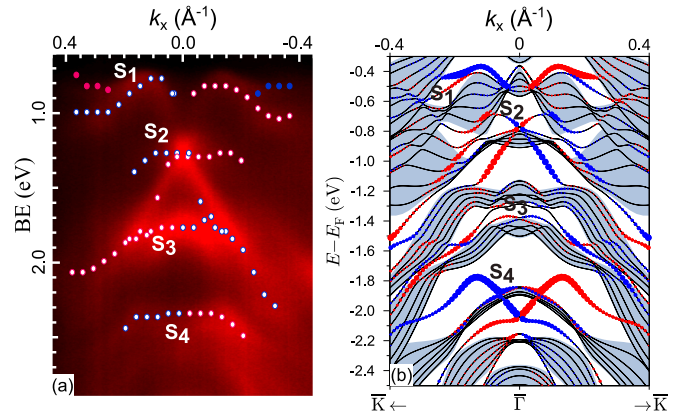


FIG. 6. (a) $E(k)$ photoemission map along $\bar{\Gamma}$ - \bar{K} . (b) Calculated spin-resolved surface electronic structure with in-plane positive and negative spin components marked by red and blue circles, respectively.

which a resonant state resides. Finally, the deepest feature in the ARPES spectrum, S_4 , derives from the surface states located in the fourth and fifth local valence-band gaps visible in Fig. 6(b) in the energy window of -1.8 – 2.2 eV. S_4 presents typical Rashba-like splitting with Rashba energy $E_R = 265$ meV and the momentum offset $k_R = 0.13 \text{\AA}^{-1}$.

To unravel the spin structure of higher binding-energy states, we performed the spin-ARPES measurement, excited with unpolarized He I_α light. Spin-up I^\uparrow (red) and spin-down I^\downarrow (blue) energy distribution curves as well as spin polarization P (green curves with error bar) are represented in the top panels of Fig. 7. Figures 7(a) and 7(b) represent, respectively, the in-plane and out-of-plane components of spin polarization \vec{P} (X and Z in the spin detector coordinates as defined in Ref. [25]) along the $\bar{\Gamma}$ - \bar{K} direction, and some selected spectra for the in-plane and out-of-plane components along the $\bar{\Gamma}$ - \bar{M} direction are shown in Figs. 7(c) and 7(d). Spin-polarization curves were calculated as $P = \frac{(I^\uparrow - I^\downarrow)}{(I^\uparrow + I^\downarrow)} \cdot \frac{1}{S_{\text{eff}}}$, where S_{eff} is the analyzer Sherman function. In Fig. 7(a), guide lines are drawn to highlight the S_1 – S_4 electronic states. At the $\bar{\Gamma}$ point, a null in-plane and out-of-plane spin polarization within the experimental error bar are observed for all the features (BE = 1, 1.45, 2, and 2.4 eV). Figures 7(e) and 7(f) show the resulting spin-polarization maps for the $P_{\text{in-plane}}$ and $P_{\text{out-of-plane}}$ spin components, respectively, along the $\bar{\Gamma}$ - \bar{K} direction. The $P_{\text{in-plane}}$ ($P_{\text{out-of-plane}}$) image is obtained by merging the polarization curves extracted from the analysis of EDCs measured in the k interval of $[-0.36, 0.36] \text{\AA}^{-1}$ with a step of 0.036\AA^{-1} [Figs. 7(a) and 7(b)]. The full data set acquisition of the $P_{\text{out-of-plane}}$ ($P_{\text{in-plane}}$) image took 12 h. As can be seen in Fig. 7(e), all the bands S_1 – S_4 demonstrate the in-plane spin orientation antisymmetric with respect to the $\bar{\Gamma}$ point. At the same time, the S_3 band manifests the spin polarization opposite to the other states. The extent of spin polarization of the S_2 state is smaller than the others, as follows from the low contrast in the in-plane polarization image. For $k_x \geq |0.25| \text{\AA}^{-1}$, the upper part of the S_1 band shows out-of-plane spin polarization as well as S_3 band [Fig. 7(f)].

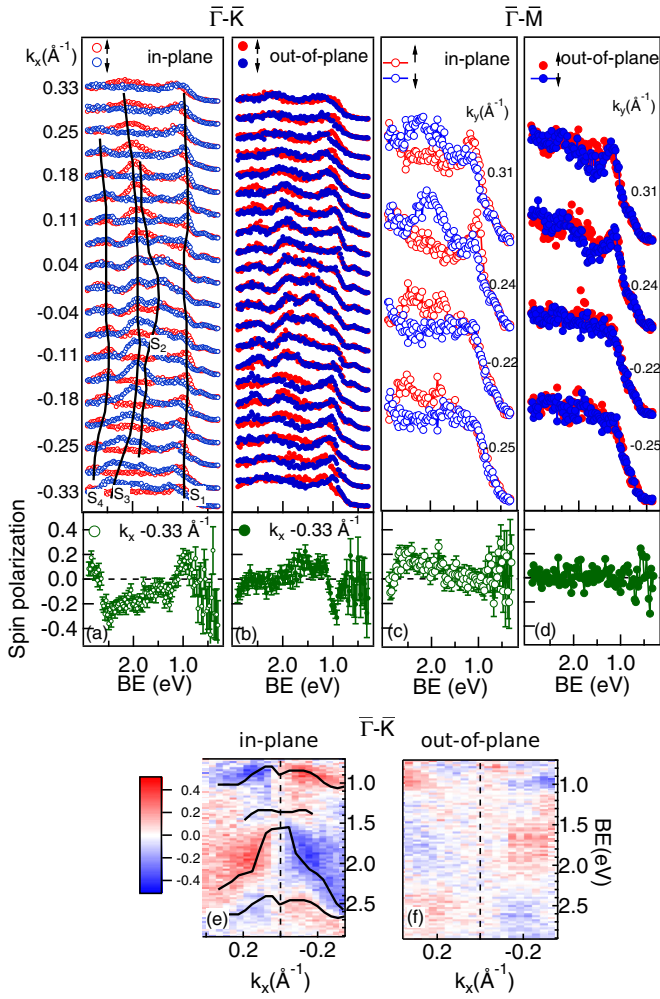


FIG. 7. (a) In-plane and (b) out-of-plane spin-resolved EDCs along the $\bar{\Gamma}$ - \bar{K} direction. Selected (c) in-plane and (d) out-of-plane spin-resolved EDCs along the $\bar{\Gamma}$ - \bar{M} direction, measured by rotating the sample azimuthal angle by 30° . All measurements were obtained by unpolarized He radiation at temperature of 15 K. Spin-polarization BE- k map of (e) $P_{\text{in-plane}}$ and (f) $P_{\text{out-of-plane}}$ spin components along the $\bar{\Gamma}$ - \bar{K} direction. Color strength denotes the photoemission intensity, with red and blue colors for positive and negative sign of the spin polarization, respectively, as indicated in the color bar.

IV. CONCLUSIONS

In summary, on the basis of the angle- and spin-resolved photoelectron spectroscopy as well as DFT and *GW* calculations, we have demonstrated that $\text{Bi}_2\text{Te}_2\text{S}$ in contrast to the earlier theoretical prediction [14,15] is an excellent 3D topological insulator characterized by ≈ 400 meV bulk band gap and topological Dirac state with Dirac point located above the valence band and below the Fermi level lying in the band gap. The gap in the nearly stoichiometric $\text{Bi}_2\text{Te}_2\text{S}$ compound is twice as large as in earlier studied S-rich phase. The helical spin texture and the spin polarizations of the TSS as well as deeper valence-band surface states have been revealed. The isolated Dirac cone on the surface of $\text{Bi}_2\text{Te}_2\text{S}$ will be particularly important for the study of topological transport properties. This phase-homogeneous ternary compound can be regarded as the model topological insulator that is promising for a variety of spintronic applications.

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