

BAREKENG: Jurnal Ilmu Matematika dan Terapan September 2020 Vol. 14 Issue 3 Page 309–320 P-ISSN: 1978-7227 E-ISSN: 2615-3017 doi: https://doi.org/10.30598/barekengvol14iss3pp309-320

National Accredited in SINTA 3, Decree No.: 28/E/KPT/2019

A COMPARISON OF CENTRALITY MEASURES IN SUSTAINABLE

DEVELOPMENT GOALS

Sena Ariesandy¹, Ema Carnia², Herlina Napitupulu^{3*}

^{1,2,3} Department of Mathematics, Faculty of Mathematics and Natural Sciences, Universitas Padjadjaran Jln. Raya Bandung Sumedang km 21 Jatinanagor, Sumedang, 45363, Indonesia,

e-mail: ¹sena16002@mail.unpad.ac.id; ²ema.carnia@unpad.ac.id; ^{3*}herlina@unpad.ac.id Corresponding author*

Abstract

The Millennium Development Goals (MDGs), which began in 2000 with 8 goal points, have not been able to solve the global problems. The MDGs were developed into Sustainable Development Goals (SDGs) in 2015 with 17 targeted goal points achieved in 2030. Until now, methods for determining the priority of SDGs are still attractive to researchers. Centrality measure is one of the tools in determining the priority goal points on a network by using graph theory. There are four measurements of centrality used in this paper, namely degree centrality, betweenness centrality, closeness centrality, and eigenvector centrality. The calculation results obtained from the four measurements are compared dan analyzed, to conclude which goal points are the most prior and the least prior. Furthemore, in this paper we present other example with simple graph to show that each different centrality calculation possibly resulted different priority node, the calculation of this illustration is done using a Python's library named NetworkX.

Keywords: Sustainable Development Goals, Centrality Measures, Degree Centrality, Betweenness Centrality, Closeness Centrality, Eigenvector Centrality, Centralization

Submitted: 05th February 2020

Accepted: 01st July 2020

This is an open access article under the <u>CC-BY-SA</u> license



1. INTRODUCTION

Sustainable Development Goals (SDGs), known as Global Goals, are sustainable development with objective to solve global problems such as overcoming environmental, political, and economics problems. In September 2015, the SDGs was agreed at a general meeting of the United Nations with 17 goals consisting of 169 targets, as a continuation from the 8 goals of MDGs.

In these 17 SDGs goal can be interpreted as goal that most influence other related goals. The reason of finding these priority goal points as a must is because of the limited funds, resources, and time that affect its completion. Social Network Analysis can be interpreted as a study about a relationship between variables (both economics, social, environmental and institutional variables) using graph theory [8]. Then, by examine the relationships structure between these variables in a group, may reveal how much the relationship between these variables occurs. In Social Network Analysis, the goal points of SDGs and their links are represented in a form of graphs. Goal points are represented by nodes while relationships between goal points are represented by edges. According to Blanc ([1]), a relationship of the goal points is the relationship of targets related to an existing goal points. For example, the target point from Goal 1, namely poverty, is related to the target point from Goal 2, namely hunger, then there is an interlinkage between that goal points. The SDGs graph representation used in this research is a weighted graph taken from ([1]) which means interlinkages between one goal point and another contained magnitude.

Research on centrality measures was introduced by Freeman ([5]) in his paper entitled "Centrality in Social Networks Conceptual Clarification". In 2008, Cadini ([3]) in a paper entitled "Using Centrality Measures to Rank the Importance of a Complex Network Infrastructure" discussed the calculation of centrality measures in power network systems. In implementing the SDGs, the application of centrality measures has been examined by Zhou and Moinuddin ([9]) for some country. Blanc in [1] studying and resulting the linkages/ links between the goal points alone for the global scope. In this paper we discussed in detail the application of centrality measures (that commonly applied in social network) based on the SDGs interlinkages produced in Blanc's research. In addition, authors want to point out that each centrality could show different characters, so that it could represent the centrality of different aspects.

2. METHOD

In this section, the theory of graph, centrality measures, eigenvectors and centralizations are explained in details.

These methods are very broad in use in the study of network analysis, and because the aim of this paper is to look at various aspects of centrality, these four uses of centrality are very appropriate. This method shows the character of each measurement from graph theory point of view. An explanation of the characteristics of each measurement is given in the discussion section.

2.1. Graph ([7])

A graph G = (V, E) consist of V, a nonempty set of nodes (or vertices) and E, a set of edges. Each Edge has either one or two nodes associated with it, called its endpoints. An edge is said to connect its endpoints.

2.2. Centrality

Centrality measurement was firstly developed in Social Network Analysis (SNA). Research on centrality measures is currently also being done in determining priority goal points on SDGs. The relationship between goal points of Sustainable Development Goals is represented in the graph and then its centrality is calculated to see which goals are the most priority. The meaning of priorities in SDG's can be seen from various points of view depending on the objectives to be achieved. Therefore, different centrality calculations are performed in this research namely degree centrality, betweenness centrality, closeness centrality, and eigenvector centrality. The calculation of degree centrality and eigenvector centrality focus more on the degree of each node without regard to the weight of the graph while betweenness centrality and closeness centrality focus more to the calculation of the shortest path.

2.2.1. Degree Centrality ([4])

Degree centrality is used in estimating the importance of a direct relationship between a node and other

node in the network. A formula in calculating the degree of centrality, $C_D(v)$, is given by:

$$C_D(v) = \frac{d(v)}{n-1} \tag{1}$$

where d(v) is the number of degrees in a graph or the number of interactions that node v has with other nodes in a network and n is the number of nodes in the network.

2.2.2. Betweenness Centrality ([4])

Betweenness centrality calculates how often a node is passed by another node to go to a particular node in the network. The Dijkstra algorithm is used in determining the shortest path. The formula in calculating betweenness centrality, $C_B(v)$, is:

$$C_B(v) = \frac{2}{(n-1)(n-2)} \sum_{s \neq t \neq v \in V} \frac{\sigma_{st}(v)}{\sigma_{st}}$$
(2)

Where σ_{st} is the number of shortest paths from node s to t and $\sigma_{st}(v)$ the number of shortest paths from node s to t passing through node v.

2.2.3. Closeness Centrality ([4])

Closeness centrality is used to calculate the average distance between a node and all other nodes in the network or in other words measure the closeness of a node with other nodes either directly or indirectly. The formula for calculating closeness centrality is:

$$C_{\mathcal{C}}(v) = \frac{n-1}{\sum_{t \in V} d(v,t)}$$
(3)

where d(v, t) is a shortest path distance from node v to node t and n is a number of nodes on the network.

In betweenness centrality and closeness centrality, the shortest path is used in the calculation of the node. In this study, the Dijkstra algorithm is used in determining the shortest path. This algorithm is one of the simple methods that provides optimum value in searching the shortest path ([2]). The name of the Dijkstra algorithm is derived from its inventor, Edsger Dijkstra.

2.2.4. Eigenvector Centrality ([10])

Eigenvector centrality performs measurements that give higher weight to nodes that are connected to other nodes and also have high centrality values. Let the adjacency matrix A contain entries in the form of $A_{v,t}$ and **x** is the eigenvector with the dominant eigenvalue λ . The eigenvector point centrality of a node v, namely x_v , can be calculated by the following formula:

$$C_E(v) := x_v = \frac{1}{\lambda} \sum_{t \neq v \in V} A_{v,t} x_t \tag{4}$$

In determining the dominant eigenvector of adjacency matrix *A*, a method so called Power Iteration is used simplify the calculation. The detail explanation is given in the following section.

2.3. Power Iteration ([6])

Power iteration, also known as power method, is an algorithm for calculating eigenvalues. For example, given a matrix A that can be diagonalized, the algorithm will produce eigenvector that correspond to dominant eigenvalue λ which is the largest eigenvalue (in absolute value) of matrix A, so that $A\mathbf{x} = \lambda \mathbf{x}$.

The algorithm of power iteration starts with the initialization of vector \mathbf{b}_0 which is an estimate of initial calculation of the dominant eigenvector. This method is explained as:

$$\mathbf{b}_{k+1} = \frac{A\mathbf{b}_k}{\|A\mathbf{b}_k\|} \tag{5}$$

where $||A\mathbf{b}_k||$ is the norm value of the product of the matrix A with the vector \mathbf{b}_k in the k-th iteration. The iterations will continue until $|||A\mathbf{b}_{k+1}|| - ||A\mathbf{b}_k||| < \epsilon$, where ϵ is a very small real number. The obtained \mathbf{b}_{k+1} is taken as an eigenvector centrality where its point centrality $C_E(v)$ is the component of the eigenvector \mathbf{b}_{k+1} .

2.4. Centralization

In addition, this paper will also calculate the centralization value of degree centrality, betweenness centrality, closeness centrality, and eigenvector centrality. Centralization of a network is a calculation of how central the most central node, in relation to the centrality value of other nodes ([5]). Centralization is calculated using the following formula:

$$S^{2} = \frac{\sum_{i=1}^{n} [C_{x}(v_{i}) - \bar{C}_{x}]^{2}}{n}$$
(6)

where x is the type of centrality, n is the number of nodes in the graph, $C_x(v_i)$ is centrality measure value at each node v_i , and \bar{C}_x is the average value of centrality measures.

3. RESULTS AND DISCUSSION

In this research, the graph representation of Sustainable Development Goals is taken from the deep research of SDGs linkages by Blanc written in paper entitled "Towards integration at last? Sustainable development goals as a target network" ([1]). The graph is redrawn as can be seen in Figure 1.

The graph formed from Blanc is a representation of the graph SDGS where the goal points are represented by the nodes, and the relationship between the goal points is represented by the edges of graph. Weights in graph linkages of Fig. 1 indicate the number of targets linking different goals. For example, SDG peaceful and inclusive societies (no. 16) is linked with SDG on gender (no. 5) through four targets. If there is no target on one goal point related to the other end point, there is no edge connecting the goal point. The circles representing the goals on climate, land, energy and water have been singled out for purposes of comparison with other mappings in that paper. In this paper our purpose is to determine which goal points are more prior by measuring the degree centrality, betweenness centrality, closeness centrality, and eigenvector centrality of each goal point. The results and discussion are given in detail in this section.

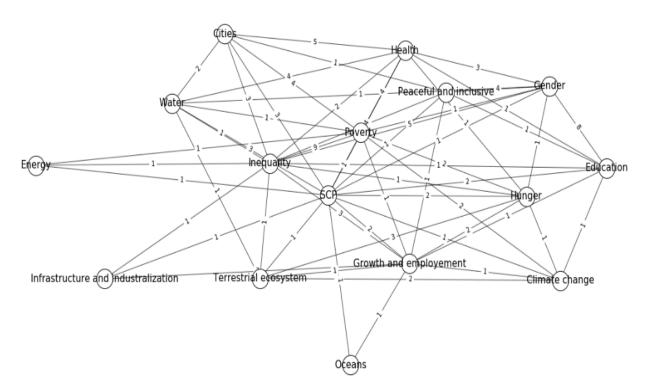


Figure 1. Graph representation of SDGs linkages taken from [1]

3.1. Degree Centrality

The value of degree centrality at each node is presented in Table 1. Based on the results of the data in Table 1, it is found that the largest degree centrality value is at the 12th goal point, namely Responsible Consumption and Production followed by the 10th goal point, namely Reduced Inequalities, while the

lowest degree centrality values are at the 14th goal point namely Life Below Water and 7th and 9th goal points in a row namely Affordable and Clean energy and Industry, Innovation, and Infrastructure. That is, when viewed on the Sustainable Development Goals, the 12th point has a high interaction with other goal points or in other words, the Responsible Consumption and Production has the most part goal points that are related among the other goal points. Following is the example of the calculation of degree centrality of node 12.

$$C_D(12) = \frac{d(12)}{n-1} = \frac{14}{16-1} = 0.9333333$$

The value of degree centralization is obtained as follows,

$$S^{2} = \frac{\sum_{i=1}^{n} [C_{D}(v_{i}) - \bar{C}_{D}]^{2}}{n} = 0.0430556$$

Nodes (v_i)	Goal Points	$C_D(v_i)$	Nodes (v_i)	Goal Points	$C_D(v_i)$
1	Poverty	0.6666667	9	Infrastructure and industralization	$0.2000000^{(15)}$
2	Hunger	0.5333333	10	Inequality	$0.8000000^{(2)}$
3	Health	0.5333333	11	Cities	0.4000000
4	Education	0.4666667	12	SCP	0.9333333 ⁽¹⁾
5	Gender	0.5333333	13	Climate change	0.4000000
6	Water	0.4666667	14	Oceans	0.1333333 ⁽¹⁶⁾
7	Energy	$0.2000000^{(15)}$	15	Terrestrial ecosystem	0.4000000
8	Growth and employement	0.6666667	16	Peaceful and inclusive	0.4000000

3.2. Betweenness Centrality

The value of betweenness centrality at each node is presented in Table 2. Based on the results in Table 2, it the greatest value of betweenness centrality is in the 12th goal point, Responsible Consumption, followed by the 10th goal point, Reduced Inequalities, while the lowest betweenness centrality values are at the 11th goal point, Sustainable Cities and Communities, and 14th goal point, Life Below Water. We can interpret that the 12th goal point becomes a very important intermediary bridge among other goal points. In other words, if the goal points are related to the other goal points the problem will be solved, then the 12th goal points that become the intermediary bridge also solved. Following is the example of the calculation of betweenness centrality of node 12.

$$C_B(12) = \frac{2}{(n-1)(n-2)} \sum_{s \neq t \neq v \in V} \frac{\sigma_{st}(12)}{\sigma_{st}}$$
$$= \frac{2}{15 \cdot 14} \left(1 + \frac{1}{3} + \frac{1}{3} + \frac{1}{2} + \dots + \frac{1}{2} + \frac{1}{2} \right) = \frac{39349}{161700} = 0.2433457$$

The value of betweenness centralization is obtained as follows,

$$S^{2} = \frac{\sum_{i=1}^{n} [C_{B}(v_{i}) - \bar{C}_{B}]^{2}}{n} = 0.0041692$$

Nodes (v)	Goal Points	${\cal C}_{B}'({m v})$	Nodes (v)	Goal Points	${\cal C}_{B}'(v)$
1	Poverty	0.0497317	9	Infrastructure and industralization	0.0050794
2	Hunger	0.0618254	10	Inequality	0.1432966 ⁽²⁾
3	Health	0.0064214	11	Cities	0.0013605 ⁽¹⁶⁾
4	Education	0.1074765	12	SCP	$0.2433457^{(1)}$
5	Gender	0.0330128	13	Climate change	0.0324651
6	Water	0.0346681	14	Oceans	$0.0026455^{(15)}$
7	Energy	0.0098413	15	Terrestrial ecosystem	0.0327740
8	Growth and employement	0.1158019	16	Peaceful and inclusive	0.1123497

Table 2. Betweenness Centrality for each node v

3.3. Closeness Centrality

The value of closeness centrality at each node is presented in Table 3. Based on the results of the data in Table 3, it is found that the greatest value of closeness centrality is in the 12th goal point, which is Responsible Consumption, followed by the 8th goal point, which is Decent Work and Economic Growth, while the lowest closeness centrality values are at the 11th goal point, which is Sustainable Cities and Communities, and 3th goal point, which is Good Health and Well-Being. It means, the 12th goal point becomes a very important intermediary bridge among other goal points. In other words, if the goal points are related to the other goal points and the problem will be solved, then the 12th goal points that become the intermediary bridge also solved. Following is the example of the calculation of closeness centrality of node 12.

$$C_{C}(12) = \frac{n-1}{\sum_{t \in V} d(12, t)} = \frac{15}{13} = 0.6521739$$

The value of closeness centralization is obtained as follows

$$S^{2} = \frac{\sum_{i=1}^{n} [C_{C}(v_{i}) - \bar{C}_{C}]^{2}}{n} = 0.0044150$$

Nodes (v)	Goal Points	$C_{C}(v)$	Nodes (v)	Goal Points	$C_{C}(v)$
1	Poverty	0.5555556	9	Infrastructure and industralization	0.4838710
2	Hunger	0.5000000	10	Inequality	0.5769231
3	Health	0.4166667 ⁽¹⁵⁾	11	Cities	0.3750000 ⁽¹⁶⁾
4	Education	0.5769231	12	SCP	0.6521739 ⁽¹⁾
5	Gender	0.5357143	13	Climate change	0.5357143
6	Water	0.5000000	14	Oceans	0.4545455
7	Energy	0.5172414	15	Terrestrial ecosystem	0.5357143
8	Growth and employement	$0.6000000^{(2)}$	16	Peaceful and inclusive	0.5357143

3.4. Eigen vector Centrality

The value of eigenvector centrality at each node is presented in Table 4. Based on the results of the data in Table 4, it is found that the greatest value of eigenvector centrality is in the 12th goal point, which is Responsible Consumption, followed by the 10th goal point, which is Reduced Inequalities, while the lowest closeness centrality values are at the 14th goal point, which is Life Below Water, and 9th goal point, which Industry, Inovation, and Infrastructure. It means, on the Sustainable Development Goals, Responsible Consumption and Production has extensive direct interaction with other goal points so that the Responsible Consumption and Production has a strategic position to connect the other goal points. Following is the example of the calculation of eigenvector point centrality of node 12. Following is the example of the calculation of eigenvector centrality using Power method in iteration 2nd and 8th, this iteration converges in 9th iteration, so that $C_E = \mathbf{b_9}$.

• The 2nd iteration:

 $\begin{aligned} \left| |Ab_2| \right| &= 8.238907, \left| \left| |Ab_2| \right| - ||Ab_1| \right| \right| &= 0.037135 \\ \mathbf{b_2} &= \left[0.3167936, 0.2858869, 0.2781603, 0.2472536, \\ 0.2781603, 0.2472536, 0.1390801, 0.2858870, \\ 0.1390801, 0.3167936, 0.2202102, 0.3477003, \\ 0.2124835, 0.0927201, 0.2202102, 0.2202102 \right] \end{aligned}$

• The 8th iteration:

 $\begin{aligned} \left| |Ab_8| \right| &= 8.246703, \left| \left| |Ab_8| | - ||Ab_7| \right| \right| &= 0.000001 \\ \mathbf{b}_8 &= \left[0.3180555, 0.2778104, 0.2768045, 0.2392692, \\ 0.2703975, 0.2436250, 0.1252324, 0.2882918, \\ 0.1216475, 0.3393867, 0.2137566, 0.3742264, \\ 0.2070504, 0.0804252, 0.2099411, 0.2100369 \right] \end{aligned}$

The value of closeness centralization is obtained as follows,

$$S^{2} = \frac{\sum_{i=1}^{n} [C_{E}(v_{i}) - \bar{C}_{E}]^{2}}{n} = 0.0060492$$

	Tuble 4	Engenveetor	Joint Centrality for each node v			
Nodes (v)	Goal Points	$C_E(v)$	Nodes (v)	Goal Points	$C_E(v)$	
1	Poverty	0.3180284	9	Infrastructure and industralization	0.1215391 ⁽¹⁵⁾	
2	Hunger	0.2777375	10	Inequality	0.3395592 ⁽²⁾	
3	Health	0.2767879	11	Cities	0.2137019	
4	Education	0.2391863	12	SCP	0.3744126 ⁽¹⁾	
5	Gender	0.2763845	13	Climate change	0.2070591	
6	Water	0.2435802	14	Oceans	0.0803640 ⁽¹⁶⁾	
7	Energy	0.1251408	15	Terrestrial ecosystem	0.2098625	
8	Growth and employement	0.2883242	16	Peaceful and inclusive	0.2099709	

3.5. Discussion

Comparison of the four centrality measures in Table 5, shows that the most priority factor is at node 12th, which is Responsible Consumption and Production. This goal point should be the main focus in the global problems that faced by various countries in the world. Meanwhile, the goal point with small priorities are Sustainable Cities and Communities and Life Below Water. Calculated in terms of the degree centrality or direct relationship between the goal points, Life Below Water is the smallest value of priority. Whereas if calculated in terms of the shortest distance, Sustainable Cities and Communities has the smallest prior value. The comparison between all centrality results are given as well in the form of bar chart in Figure 2.

	Table 5. Comparison of Centrality Measures						
Node	Cool points	Degree	Betweenness	Closeness	Eigenvector		
Noue	Goal points	Centrality	Centrality	Centrality	Centrality		
1	Poverty	0.6666667	0.0497317	0.5555556	0.3180158		
2	Hunger	0.5333333	0.0618254	0.5000000	0.2777054		
3	Health	0.5333333	0.0064214	0.4166667	0.2767806		
4	Education	0.4666667	0.1074765	0.5769231	0.2391494		
5	Gender	0.5333333	0.0330128	0.5357143	0.2763789		
6	Water	0.4666667	0.0346681	0.5000000	0.2435601		
7	Energy	0.2000000	0.0098413	0.5172414	0.1251007		
8	Growth and employment	0.6666667	0.1158019	0.6000000	0.2883394		
9	Infrastructure and industrialization	0.2000000	0.0050794	0.4838710	0.1214916		
10	Inequality	0.8000000	0.1432966	0.5769231	0.3396349		
11	Cities	0.4000000	0.0013605**	0.3750000**	0.2136775		
12	SCP	0.93333333*	0.2433457*	0.6521739*	0.3744944*		
13	Climate change	0.4000000	0.0324651	0.5357143	0.2070639		
14	Oceans	0.13333333**	0.0026455	0.4545455	0.0803373		
15	Terrestrial ecosystem	0.4000000	0.0327740	0.5357143	0.2098282		
16	Peaceful and inclusive	0.4000000	0.1123497	0.5357143	0.2099419		
	Centralization	0.0430556	0.0041692	0.0044150	0.0060492**		

Table 5	Comparison	of Centrality	Measures
Table 3.	Comparison	of Centranty	wieasures

Note: Value with asterisks (*) mean the greatest value in its centrality measures, meanwhile with double asterisks (**) are the smallest in its centrality measures.

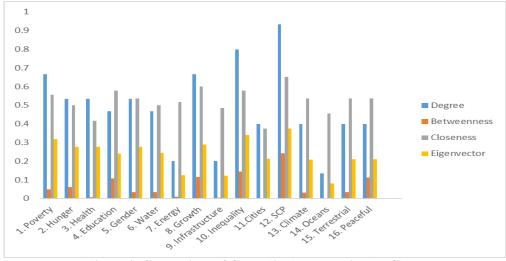
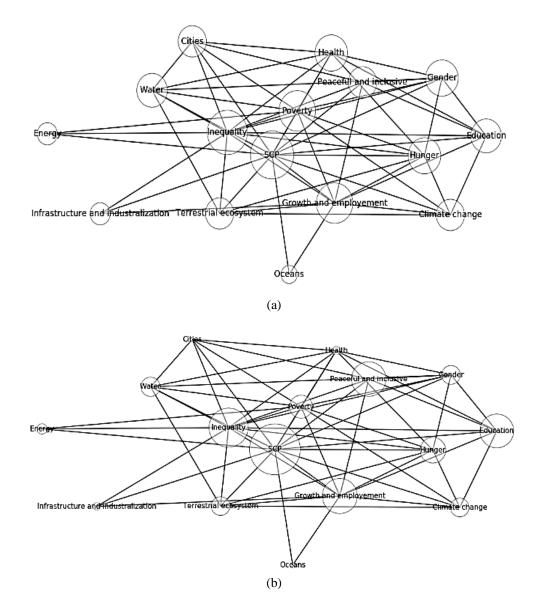
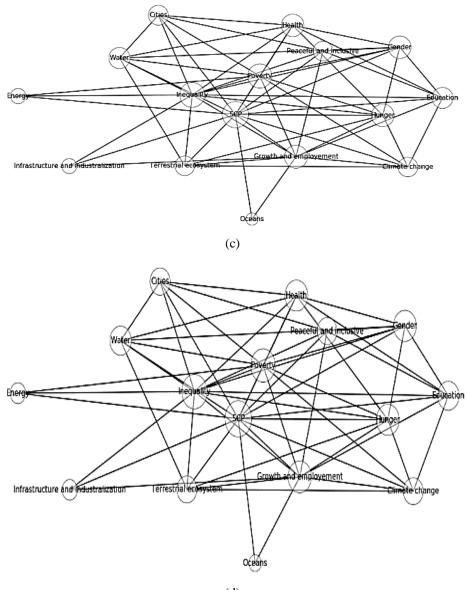


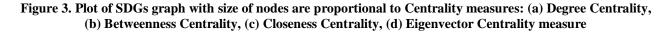
Figure 2. Comparison of Centrality Measures in Bar Chart

Visualization of the graph based on the four centrality calculations is given in Figure 3, where the size of the nodes in each figure is based on the size of each type of centrality





(d)



3.5.1. Counter Example of priority node in each centrality

In this section, we will explain through illustration of simple graph as shown in Figure 4, that another type of graph may resulted to different priority node for different centrality measures. The four centrality measures of graph in Figure 4 are calculated as seen in Table 6.

The calculation of centrality measures can be done using library NetworkX in software Python 3.7, we give the coding program below. Please note that the two dots in line 4 and 5 of coding below supposed to be filled with the complete nodes and edges of graph G respectively, but for simplicity in this paper it is left only by dots. In this coding, since the weight of each edge of Graph Figure 4 is equal to 1 thus we didn't add a weight in edge. The value displays in Table 6 only 5 decimal places taken.

Based on the results on Table 4, it can be seen that centrality measures can be varied. For degree centrality node, the 2nd and 11th nodes have the greatest value. The priority on betweenness centrality and closeness centrality node is in point 1st. While the eigenvector centrality node priority is in 2nd and 11th node. This illustration shows for any graph probably resulted to different priority node in different centrality measures

Cod	Coding program using Spyder (Python 3.7)				
1	import matplotlib.pyplot as plt				
2	import networkx as nx				
3	<pre>G = nx.Graph()</pre>				
4	V = [1, 2,, 15]				
5	$E = [(1,3), (1,9), \dots, (14,15)]$				
6	G.add nodes from(V)				
7	G.add edges from (E)				
8	Cd = nx.degree centrality(G)				
9	print(Cd)				
10	Cb = nx.betweenness centrality(G)				
11	print(Cb)				
12	Cc = nx.closeness centrality(G)				
13	print(Cc)				
14	Ce = nx.eigenvector centrality(G)				
15	print(Ce)				

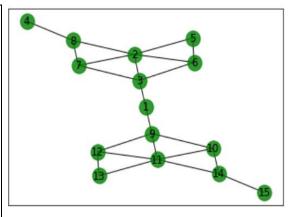


Figure 4. Graph for counterecample of centrality of priority node

Node	Centrality measures of each node							
node	Degree	Betweenness	Closeness	Eigenvector				
1	0.14285	0.53846*	0.41176*	0.19565				
2	0.35714*	0.20879	0.35000	0.37694*				
3	0.28571	0.53296	0.40000	0.32970				
4	0.07142	0.00000	0.22222	0.06267				
5	0.14285	0.00000	0.26923	0.19085				
6	0.21428	0.04945	0.32558	0.26629				
7	0.21428	0.09890	0.33333	0.27234				
8	0.21428	0.14285	0.28000	0.21124				
9	0.28571	0.53296	0.40000	0.32970				
10	0.21428	0.09890	0.33333	0.27234				
11	0.35714*	0.20879	0.35000	0.37694*				
12	0.21428	0.04945	0.32558	0.26629				
13	0.14285	0.00000	0.26923	0.19085				
14	0.21428	0.14285	0.28000	0.21124				
15	0.07142	0.00000	0.22222	0.06267				

Table 6. Centrality measures of each node of counterecample of priority node

4. CONCLUSION

Based on the calculation value of degree centrality, betweenness centrality, closeness centrality, and eigenvector centrality, it is obtained that the 12th goal point, Responsible Consumption and Production has the greatest centrality value compared to other goal points. It means, the 12th goal point is the most central goal point (for all measurements of centrality that has been done) so that it is considered as the most priority.

It can be seen that the 12th goal point is Responsible Consumption and Production has the highest centrality value compared to other goal points. In addition, it can be concluded that the greatest value of centralization is value degree centralization. So that the node is central to the calculation. degree centralization is the most influential node in the network.

So, we get the result that the 12th goal point, Responsible Consumption and Production is the most priority goal point. We quite sure that the method is good for problems that can be represented by linkages relations. Furthermore, in this paper the other example in the form of simple graph is explained that each different centrality measures type possibly resulted different priority node, instead one node only.

BIBLIOGRAPHY

- [1] D. L. Blanc, "Towards Integration at Last? The Sustainable Development Goals as a Networks of Targets", *Sustainable Development*, vol. 23, no. 3, pp. 176–187, May-Jun 2015.
- [2] U. Brandes, "A Faster Algorithm for Betweenness Centrality", *Journal of Mathematical Sociology*, vol. 25, no. 2, pp. 163-177, 2001
- [3] F. Cadini, E. Zio, C. A. Petrescu, "Using Centrality Measures to Rank the Importance of the Components of a Complex Network Infrastructure", In: Setola R., Geretshuber S. (eds). *Critical Information Infrastructure* Security. CRITIS 2008. Lecture Notes in Computer Science, vol. 5508, Berlin: Springer, 2008, pp. 155-167
- [4] C. Donninger. "The distribution of centrality in social network". Social Networks, vol. 8, no.2, pp. 191-203, June 1986
- [5] L.C. Freeman, "Centrality in Social Network Conceptual Clarification". *Social Networks*, vol. 1, issue 3, pp. 215-239, 1978-1979
- [6] N. Meganathan, "Eigenvector Centrality-Based Mobile Target Tracking in Wireless Sensor Networks" In N. Kamila (Ed.) Handbook of Research on Wireless Sensor Network Trends, Technologies, and Applications., Hershey PA: IGI Global, 2017, pp. 395-412
- [7] K. H. Rosen, *Discrete Mathematics and Its Applications*, 7th Edition, New York: McGraw-Hill Companies, Inc., 2012
- [8] M. Tsvetovat and A. Kouznetsov, Social Network Analysis for Startups, Sebastopol: O'Reilly Media, 2011
- [9] X. Zhou and M. Moinuddin, "Sustainable Development Goals Interlinkages and Network Analysis: A Practical Tool for SDG Integration and Policy Coherence", *Institute for Global Environmental Strategies* (*IGES*) *Research Report*, 2017
- [10] A. Lange, *Centrality in Strategic Transportation Network Design, An application to less-than-truckload networks.* Wiesbaden: Springer Gabler, 2019

Ariesandy, et al. | A Comparison of Centrality Measures in

320