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ENDOGENOUS GROWTH, CONVEXITY OF DAMAGE AND CLIMATE RISK: HOW NORDHAUS' FRAMEWORK SUPPORTS DEEP CUTS IN CARBON EMISSIONS*

Simon Dietz and Nicholas Stern

'To slow or not to slow' (Nordhaus, 1991) was the first economic appraisal of greenhouse gas emissions abatement and founded a large literature on a topic of worldwide importance. We offer our assessment of the original article and trace its legacy, in particular Nordhaus's later series of 'DICE' models. From this work, many have drawn the conclusion that an efficient global emissions abatement policy comprises modest and modestly increasing controls. We use DICE itself to provide an initial illustration that, if the analysis is extended to take more strongly into account three essential elements of the climate problem – the endogeneity of growth, the convexity of damage and climate risk – optimal policy comprises strong controls.

1. To Slow or Not to Slow

'To slow or not to slow' by Bill Nordhaus (1991) is a landmark in economic research. As the first analysis of the costs and benefits of policies to abate greenhouse gas emissions,¹ it opened the profession to a new field of application – climate change. Its importance is partly illustrated by the number of times that it has been cited – on 1,150 occasions according to Google Scholar; 398 times according to the narrower, journals-only measure in ISI Web of Knowledge.²

The context within which Nordhaus's paper was written helps us understand its contribution. While the basic science of the greenhouse effect was set out in the nineteenth century by Fourier, Tyndall and Arrhenius, discussions surrounding the possible role of humans in enhancing it – and therefore causing global warming and climate change – began in earnest in the 1970s. For at least a decade, climate change remained largely a scientific/environmentalist's issue, debated in specialist conferences and networks (Agrawala, 1998). Indeed, it is important to stress that the science of climate change was running years ahead of the economics (something that arguably remains the case today in understanding the impacts of climate change; Stern, 2013).

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¹ Shortly afterwards Bill Cline (1992) published what is generally considered to be the other foundational analysis of climate mitigation benefits and costs.

² Both accessed on 24 March 2014. However, these citation counts likely understate the paper's legacy considerably, since many will instead cite later work that is based on it (see Section 1).

By the late 1980s, however, climate change was becoming both a policy issue and increasingly political. In 1988, the Intergovernmental Panel on Climate Change (IPCC) was established and in 1990 it published the first of its regular and influential Assessment Reports to member governments. In 1989, the first meeting of (22) Heads of State to discuss climate change was held in the Netherlands and various other major international summits that year also put it on the agenda. Most OECD countries already had their first climate-change targets by 1990 (Gupta, 2010), for instance the European Community, as it was then, had pledged to stabilise its carbon dioxide emissions at 1990 levels by 2000. In 1992, virtually all countries signed up to the United Nations Framework Convention on Climate Change (UNFCCC) at a major summit on the environment and development in Rio de Janeiro, with its objective to achieve ‘stabilization of greenhouse gas concentrations in the atmosphere at a level that would prevent dangerous anthropogenic interference with the climate system’ (Article 2).

Yet despite the obvious ecological risks of unmitigated climate change, the question remained whether the benefits of avoiding these risks would outweigh the perhaps substantial cost of cutting emissions.³ This is the central question that ‘To slow or not to slow’ sought to tackle, by combining a simple model of social welfare and production with an externality from greenhouse gas emissions, in general equilibrium. This model took ‘existing models and simplified them into a few equations that are easily understood and manipulated’ (p. 920), something that has become a hallmark of Nordhaus’s work in the area. In summary, the main components of the model are:

- (i) a single equation of motion for the global mean temperature, which rises in response to the difference between the temperature that would be obtained in long-run equilibrium, given the current atmospheric stock of greenhouse gases, and the current temperature;
- (ii) an equation of motion for the atmospheric stock of greenhouse gases, in which some fraction of current emissions adds to the stock, at the same time as some fraction of the current stock ‘decays’ by diffusing into the deep ocean;⁴
- (iii) a social welfare function that is the discounted sum over time of utility *per capita*;⁵
- (iv) utility takes the form of the logarithm of consumption *per capita* of a single, aggregate good;

³ There is a problem in using the language of benefit–cost analysis, if it is interpreted in its common and narrow, marginal, fairly undynamic way and where risk is also treated narrowly. Climate-change policy raises major questions of the strategic management of potentially immense risks and where different paths will have different endogenous learning and discovery. This broader perspective is a major focus of this study and should be central to economic research on the topic.

⁴ To get an idea of the simplicity of the modelling framework, especially the science module, note that a fully fledged atmosphere–ocean general circulation model such as that of the UK Hadley Centre would comprise hundreds of thousands of equations.

⁵ There is little plausibility in moral philosophy for a social welfare function that is the sum across generations of the (discounted) utility *per capita* of each generation, irrespective of the number of people in a generation, unless population is constant. Adding the (undiscounted) total utility of each generation is essentially utilitarian. Pure-time discounting can be given a utilitarian interpretation if the discounting is based on the probability of existence as a function of time, and that becomes an exponential function in continuous time if the end of the world is the first event in a Poisson process.

- (v) consumption *per capita* is given by (exogenous) output, less the total cost of abating emissions, and the total cost of climate change;
- (vi) a reduced-form abatement cost function, in which the total cost of abatement depends on global aggregate emissions and emissions abatement; and
- (vii) reduced-form damage, in which the total cost of climate change depends on global mean temperature but where global mean temperature is an index of a wider set of climatic changes including changes in precipitation and sea level.

This modelling framework has had a lasting influence on the field and indeed several elements of it still constitute the ‘industry standard’ today. The most notable example of this is perhaps the idea of reduced-form damage.

According to the model, Nordhaus found that an optimal cut in the current flow of global emissions of 11% relative to the base level should be made in a medium scenario (given a rate of pure-time preference of 1% per annum and ‘medium’ damage). In a ‘high’ scenario, with no pure-time discounting and ‘high’ damage, a cut of global emissions of around one third would be optimal. The concluding Section of this article lays out these results, without commenting on the plausibility of the various scenarios. Nonetheless, that the optimal emissions cuts were not more than one third implied that only modest targets could be supported by economic analysis of this kind, in comparison with some targets being discussed in the political arena. As the editor of the issue in which the paper appeared wrote, it is ‘certainly a sobering antidote to some of the more extravagant claims for the effects of global warming’ (Greenaway, 1991, p. 903).

2. The DICE Model Framework

While it was very much the purpose of ‘To slow or not to slow’ to cast climate-change mitigation as a dynamic, investment problem, in which abatement costs could be paid up front, so that climate change could be avoided several decades into the future, the model dynamics were unsatisfactory – the economy was assumed to be in a so-called ‘resource steady state’, in which all physical flows are constant. Therefore, we were asked to consider the setting as being the middle of the twenty-first century, when such conditions might plausibly hold (we can now see that this is highly unlikely). Optimal emissions abatement was calculated by evaluating a marginal change to the steady-state level (and thus the optimal cuts mentioned above were in the steady state). Time was still relevant though, because, while the change in abatement costs was instantaneous, the change in damage costs would be experienced only after a delay (Equations 7–9, p. 926).

Nordhaus himself was well aware of the shortcomings and indeed a preliminary version of a more fully dynamic model had already been presented at a workshop by the time ‘To slow or not to slow’ had been published. This new model was called DICE (for a ‘dynamic integrated climate-economy’ model) (Nordhaus, 1992, 1993*a,b*, 1994). Many elements of ‘To slow or not to slow’ could still be found in the original DICE model, including the equation of motion of the atmospheric stock of CO₂, log utility and reduced-form abatement and damage costs. But at the core was a Ramsey–Cass–Koopmans model of economic growth, allowing evaluation not only of the optimal steady state but also of the optimal transition path. The social welfare function

was modified to include population, with the objective becoming the (pure-time) discounted sum of total, instantaneous social utility, while a slightly more complex model of temperature change was also added. Once again, the results of the analysis with DICE pointed to modest emissions controls, modestly increasing over time – from 10% initially to 15% in the later twenty-first century.

Since these first studies with the DICE model, it has become the pre-eminent integrated assessment model (IAM) in the economics of climate change. New versions have been published periodically (Nordhaus and Boyer, 2000; Nordhaus, 2008), and a regionally disaggregated model (RICE) was also developed (Nordhaus and Yang, 1996). However, to look only at Nordhaus's own studies with DICE is to understate its contribution hugely, because, by virtue of its simple and transparent unification of growth theory with climate science (not to mention Nordhaus's considerable efforts to make the model code publicly available), it has come to be very widely used by others. The uses to which it has been put are too numerous to cover in a comprehensive manner. Some of the more significant examples include: the introduction of induced innovation in the energy sector (Popp, 2004); explicit evaluation of optimal adaptation policy (de Bruin *et al.*, 2009); consideration of uncertainty and learning (Kolstad, 1996; Keller *et al.*, 2004); and treating consumption of material goods and environmental quality separately, thus allowing evaluation of relative price changes (Sterner and Persson, 2008).

Some of these extensions have challenged the broad conclusion that optimal emissions control is modest. And indeed it is important to stress two things. First, through his own updating of DICE, Nordhaus's position, as formalised in the model and its results, has shifted over the years towards stronger emissions reductions, albeit incrementally. Second, one can readily see in Nordhaus's writings an awareness of the limitations of IAMs like DICE. Nonetheless, it is fair to say the perception remains that an analysis of the costs and benefits of climate change in an IAM does not support strong emissions cuts, under standard assumptions. For instance, in the wake of the publication of the *Stern Review on the Economics of Climate Change* (Stern, 2007) (which in fact used an IAM other than DICE), it has been suggested that the difference in policy recommendations between the Review and other studies lies very largely in the specification of a low pure-time discount rate (Nordhaus, 2007), a rate that some have questioned.⁶ A central purpose of the rest of this article is to explore whether a recommendation of modest emissions reductions does indeed follow from using the DICE framework. We ask, can the framework support strong controls on emissions, if restrictive assumptions about growth, damage and climate risk are relaxed? These assumptions arguably lead to gross underestimation of the benefits of emissions reductions in DICE and other IAMs (Stern, 2013).

First, we incorporate endogenous drivers of growth and we allow climate change to damage these drivers. This is in stark contrast to the current generation of IAMs, which rests directly or indirectly on the Ramsey–Cass–Koopmans model, where the major

⁶ A careful exploration of the strong basis in moral philosophy for low pure-time discounting is provided in Stern (2014a,b). In many IAM studies, high pure-time discounting is introduced without much discussion.

source of growth *per capita* in the long run is exogenous improvements in productivity, but where climate change only impacts on current output.⁷ There are compelling reasons for thinking that climate change could have long-lasting impacts on growth (Stern, 2013) and there is now an emerging body of empirical evidence pointing in this direction (Dell *et al.*, 2012), even though climatic conditions in the recent past have been relatively stable compared with what we now have to contemplate.

Second, we assume that the damage function linking the increase in global mean temperature with the instantaneous reduction in output is highly convex at some temperature. Consideration of some of the science, for example, on tipping points, leads us in this direction (Weitzman, 2012). By contrast, most existing IAM studies assume very modest curvature of the damage function. The DICE default is quadratic and it is well known that with the standard values of the functions' coefficients an implausible 18°C or so of warming is required in order to reduce global output by 50%.⁸

Third, we allow for explicit and large climate risks. We do so by considering the possibility of high values of the climate-sensitivity parameter; i.e. the increase in global mean temperature, in equilibrium, accompanying a doubling in the atmospheric concentration of carbon dioxide. We conduct sensitivity analysis on high values but also specify a probability distribution reflecting the latest scientific knowledge on the climate sensitivity as set out in the recent IPCC report (IPCC, 2013). Its key characteristic is a fat tail of very high temperature outcomes that are assigned low probabilities. By contrast, most IAM studies have ignored this key aspect of climate risk by proceeding with a single, best guess value for the climate sensitivity, typically corresponding to the mode of the IPCC distribution. We note, linking the second and third points here, that the model temperature increase under business as usual a century or so from now of 3.5 or 4°C (IPCC, 2013) could be extremely damaging – this is not just a 'tail' issue.

Otherwise we remain faithful to the standard DICE framework, in order to make as clear as possible the difference that these three extensions make. Most notably, we retain its usual parameterisation of social values, where the rate of pure-time preference is 1.5% and the elasticity of marginal social utility of consumption is 1.5, so that with growth of consumption *per capita* of, say, 2%, the social discount rate would be 4.5%. We have written elsewhere about why we think it is inappropriate to posit such a high rate of pure-time preference (Stern, 2013, 2014 *a,b*) – and we return to explain why in Section 5 – but for the purpose of clarity of comparison we set aside our misgivings, concerning this and other features, in the modelling that comprises the core of this study. More generally, there is a powerful case for arguing that this type of model, with one good and exogenous population, has very serious defects in its ability to capture key aspects of a problem for which destruction of the environment and potential loss of life on a major scale are central.

⁷ While a reduction in current output may impact future growth via reduced savings – for a given savings rate – we hypothesise that this effect is weak compared with direct reductions in the capital stock and reductions in productivity. Fankhauser and Tol (2005) also find a weak impact of climate change on growth via savings, using DICE. They did not, however, consider that climate damage could work on the capital stock or on productivity.

⁸ Nordhaus sees the specification of the damage function for warming above 3°C as a 'placeholder' (Stern, 2013) but it is a placeholder that can have a powerful effect on the conclusions as we will see below.

3. Extending DICE

3.1. *Endogenous Growth*

In standard DICE, the production function is:

$$Y_t = F(K_t, L_t) = (1 - \hat{D}_t)(1 - \Lambda_t)A_t K_t^\alpha L_t^{1-\alpha}, \quad (1)$$

where A_t is the exogenous element of total factor productivity (TFP) at time t , K is capital, L is labour and $\alpha \in (0, 1)$ is the capital exponent. \hat{D} is the standard DICE damage multiplier (see below for a definition) and the key point is that this is the only pathway through which climate change affects growth – directly by multiplication with gross output in each period. Λ represents emissions abatement costs. In all of our analysis, we maintain standard assumptions about Λ and L , detailed in Appendix A alongside many other aspects of the model.

In (1) the long-run growth rate of output, ignoring for one moment the role of climate change, is given by the sum of the growth rates of A_t and L_t as in the standard Solow (1956) model. Climate-change damage \hat{D}_t (and abatement costs Λ_t) affect the level of output in each period, which means that they can have two effects on the long-run growth rate of output. First, period-to-period changes in \hat{D}_t can effectively change the long-run output growth rate. Second, depending on the rates of saving and capital depreciation, \hat{D}_t can impact the long-run growth rate by affecting capital investment and in turn the stock of K in future periods.

Yet one of the central points of this study is that this is a very narrow story of how climate change impacts on growth. We, therefore, consider two extensions to (1). Both are endogenous growth models, incorporating knowledge spillovers from the accumulation of capital by firms. And in both models, damage from a changing climate not only fall on gross output at a particular point in time, they also permanently reduce output possibilities at future points in time through their effect on endogenous determinants of growth.

3.1.1. *A model of capital damage, and knowledge proportional to the capital stock*

Our first growth model incorporates knowledge spillovers via the capital stock in the tradition of Arrow (1962), Romer (1986) and others. We combine this formulation with a partitioning of the damage multiplier between output and capital. The production function becomes

$$Y_t = (1 - D_t^Y)(1 - \Lambda_t)A_t K_t^{\alpha+\beta} L_t^{1-\alpha}, \quad (1.K)$$

where D^Y now denotes the damage that directly reduce annual output. In this model, we think of the economy as being composed of a number of firms, each making investments. Growth is driven in part by learning-by-doing, which in turn depends on each firm's net investment, so that when the firm's capital stock increases, so does economy-wide productivity. We also make the standard assumption in this tradition that knowledge is a pure public good. The elasticity of output with respect to knowledge is $\beta > 0$, so that the knowledge process has a productivity factor K^β . These assumptions have the effect of increasing the overall capital exponent to $\alpha + \beta$. We continue to assume an exogenous element of TFP A . This could be taken to represent elements of productivity not captured in knowledge spillovers but we use it here

principally for the narrower, instrumental purpose of calibrating (1.K) on (1) in the absence of climate-change damage and emissions abatement costs, thus achieving a controlled comparison of different production specifications.

We suppose there is further damage from climate change that reduces the capital stock, which we label D^K , so we obtain the following equation of motion of capital:

$$K_{t+1} = (1 - D_t^K)(1 - \delta^K)K_t + I_t, \quad (2)$$

where $\delta^K \in [0, 1]$ is the depreciation rate on capital and $I_t = sY_t$ is investment, given savings rate s (see Appendix A). In specifying D^K we have in mind the representation of two phenomena. First, D^K includes permanent, direct climate damage to the capital stock, for example, if climate change increases the likelihood of storms and those storms damage infrastructure, or the abandonment of capital in coastal areas due to sea-level rise. Second, D^K could indirectly include broader impacts of climate change on productivity via the endogenous growth mechanism (1.K). One effect it could pick up is of a changing climate on the productivity of capital stocks, accumulated during a different and more stable climatic regime. For example, water supply infrastructure may become less productive, given a long-run change in precipitation. Another could be that, if investment is increasingly diverted towards repair and replacement of capital damaged by extreme weather, it may produce fewer knowledge spillovers. Appendix A contains further details of how, for our simulation work, we partition damage D between D^Y and D^K .

In sum, according to this model of growth and climate damage, some part of the instantaneous impacts of climate change falls on capital rather than output, so that this type of damage represents a permanent reduction in output possibilities in the future. Moreover since the economy's stock of knowledge is proportional to its stock of capital, the negative effect on future output possibilities is magnified.

3.1.2. A model of endogenous TFP and damage to TFP

One constraining feature of production functions like (1.K) is that, since knowledge is in one-for-one correspondence with the aggregate capital stock, it will depreciate just as fast. If one considers a typical depreciation rate for economy-wide capital of 10% per year (indeed $\delta^K = 0.1$ in DICE), the implication is a rapid diminution of economy-wide knowledge over time. While the literature on measuring the returns to R&D investment points to annual depreciation of around 15% of private, firm-level R&D capital – see Hall *et al.* (2009) for a review, what we have here is a much broader construct of knowledge concerned with overall skills and know-how. Therefore, we offer an alternative formulation of endogenous growth – new as far as we are aware – in which TFP is endogenous and depreciates more slowly than capital.

We revert to the standard production function, modelling TFP through a separate relation. The production function is hence:

$$Y_t = (1 - D_t^Y)(1 - \Lambda_t)\bar{A}_t K_t^\alpha L_t^{1-\alpha}. \quad (1.TFP)$$

Capital and TFP have different dynamics. The equation of motion of the capital stock is simply given by

$$K_{t+1} = (1 - \delta^K)K_t + I_t. \quad (2')$$

Notice that in this specification, we do not allow climate damage to impact the capital stock, although doing so would be straightforward by reverting to (2). The equation of motion of TFP is given by

$$\bar{A}_{t+1} = (1 - D_t^A)(1 - \delta_t^A)\bar{A}_t + a(I_t), \quad (3)$$

where δ_A is the net depreciation rate for productivity. We can think of δ^A as encapsulating both:

- (i) depreciation of productivity through erosion or displacement of skills and know-how; and
- (ii) implicit, autonomous growth of TFP, which captures among other things institutional innovations, beyond the scope of this model.

Given these two effects, δ^A could in principle be negative but here we assume it is positive and less than δ^K .

D^A is the part of damage that reduces productivity. It captures the productivity effects of climate change mentioned above. Appendix A again explains how we partition D between D^Y and D^A .

$a(I_t)$ is a 'spillovers' function that converts the flow of capital investment in each period into a flow of knowledge externalities across activities as a whole. This means that the stock of TFP is augmented by knowledge spillovers, as well as changing over time according to the balance of depreciation and autonomous growth due to other factors, which is encoded in δ^A . In general, assume $d' \geq 0$. More specifically, in order to again calibrate this model to standard DICE in the absence of climate damage and abatement costs, it is necessary to assume further $d' > 0$, $d'' < 0$, since in the standard DICE model the growth rate of TFP falls rapidly in the initial periods.⁹ These properties can be satisfied by

$$a(I_t) = \gamma_1 I_t^{\gamma_2},$$

where $\gamma_1 > 0$ and $\gamma_2 \in (0, 1)$. Summing up, in this formulation some part of the instantaneous impacts of climate change falls on TFP, permanently reducing future output possibilities.

3.2. Convexity of Damage

The standard DICE damage function is of a convenient reduced form that has come to be widely used in the field:

$$\hat{D}_t = 1 - 1/(1 + \pi_1 T_t + \pi_2 T_t^2), \quad (4)$$

where T is the global mean atmospheric temperature relative to the period just before the industrial revolution. The coefficients π_1 and π_2 are estimated by fitting the function on data points, which comprise the sum of underlying sectoral studies of climate damage at particular degrees of global warming (mostly $T = 2.5 - 3^\circ\text{C}$),

⁹ Whether such concavity is theoretically or empirically plausible is not for this study.

for example, studies of crop losses and changing energy demand for space cooling and heating.¹⁰ We should recognise, however, that these are ‘quasi’ data points, since $T = 3^\circ\text{C}$ has not been seen on the planet for around 3 million years and might lead to radical transformations in global climatic patterns. Making assumptions about the form of (2) is made still more difficult by the complete absence of evidence on aggregate impacts for $T \geq 3^\circ\text{C}$. The quadratic form was originally selected largely for convenience¹¹ but it results in implausibly low damage at high temperatures (Stern, 2008; Weitzman, 2012). This has prompted Weitzman (2012) to suggest the following modification:

$$D_t = 1 - 1/(1 + \pi_1 T_t + \pi_2 T_t^2 + \pi_3 T_t^{6.754}), \quad (4')$$

where the coefficient π_3 and its corresponding exponent are together used to satisfy the assumption that, at $T = 6$, 50% of output is lost.¹² This is the functional form we use in this study¹³ but, in addition to Weitzman’s calibration of π_3 , we offer a second, alternative calibration such that $D_t = 0.5$ when $T = 4$. Science and impact studies tell us that, not only could we cross several key physical tipping points in the climate system by the time the 4°C mark is reached (Lenton *et al.*, 2008), the impacts of such warming on the natural environment, economies and societies could be severe, with reason to believe in the risk of vast movements of population and associated conflict, unrest and loss of life (Stern, 2013). Global mean temperatures regularly exceeding 4°C above pre-industrial have probably not been seen for at least 10 million years (Zachos *et al.*, 2008) and are within the range of difference between today and the peak of the last Ice Age, when large ice sheets covered northern Europe and North America (IPCC, 2013), radically influencing where people could be. Given the potential magnitude of transformation illustrated by this example, the assumption that $D_t = 0.5$ when $T = 4$ may be no less plausible, to put it cautiously, than assuming, as (2) does with the standard parameterisation, that $D_t = 0.04$ when $T = 4$, i.e. only 4% of output is lost as a result of temperatures not seen for 10 million plus years.

In our first growth model, we partition damage as expressed in (4') between damage affecting output D^Y and those affecting capital D^K , while in our second model damage are partitioned between output and TFP as in (3). We do so in a similar way to Moyer *et al.* (forthcoming) and the procedure is described in detail in Appendix A.

¹⁰ Note that within this set of studies are some estimates of the money value of direct welfare losses due to climate change, e.g. impacts on health and the amenity value of the environment.

¹¹ Which is why Nordhaus himself describes such functions and the assumptions they embody about damage at different temperatures as ‘placeholders subject to further research’ (Stern, 2013). However, we will see data points of 4, 5 or 6°C , if we are negligent and unlucky, within decades. Hence, it makes sense to try different formulations as representing different possibilities, including of the extremely damaging circumstances the science suggests as possible.

¹² A quadratic function could not be made to simultaneously fit the existing data, while satisfying this additional assumption; it would give excessive damage for smaller temperature increases.

¹³ Elsewhere Dietz *et al.* (2007a,b,c); Stern (2007, 2008) we investigated models based on the PAGE IAM, in which damage was a power function of temperature. We examined the sensitivity of damage to the exponent of the power function up to a value of three.

3.3. *Climate Risk*

Our last extension to the basic framework involves the climate sensitivity parameter. We take two approaches here. First, we explore high values of this parameter in sensitivity analysis. Second, we replace its sure value with a probability density function (pdf). Climate sensitivity is a key factor in driving the change in temperature in DICE, as it is in many other simple climate models. Thus, it is a natural example of large-scale risk. Others would be relevant too, such as the scale of damage for a given temperature increase, the scale of loss of life and so on.

The equation of motion of temperature is given by:

$$T_t = T_{t-1} + \kappa_1 \left[F_t - \frac{F_{2 \times \text{CO}_2}}{S} (T_{t-1}) - \kappa_2 (T_{t-1} - T_{t-1}^{\text{LO}}) \right], \quad (5)$$

where F_t is radiative forcing, $F_{2 \times \text{CO}_2}$ is the radiative forcing resulting from a doubling in the atmospheric stock of carbon dioxide, S is the climate sensitivity, T^{LO} is the temperature of the lower oceans, κ_1 is a parameter determining speed of adjustment and κ_2 is the coefficient of heat loss from the atmosphere to the oceans. Cialel *et al.* (2014) contains a detailed explanation of the physics behind this equation.

In standard DICE $S = 3^\circ\text{C}$. However, it has long been known that there is substantial uncertainty about S (Charney, 1979). Moreover investigations in recent years (as collected by Meinshausen *et al.*, 2009) have tended to yield estimates of the pdf of S that have a large positive skew and in most cases the right-hand tail can indeed be defined as ‘fat’.¹⁴ In the latest IPCC report (IPCC, 2013), a subjective pdf is offered that is the consensus of the panel’s many experts. According to this distribution, S is ‘likely’ between 1.5 and 4.5°C, where likely corresponds to a subjective probability of anywhere between 0.66 and 1. It is ‘extremely unlikely’ to be less than 1C, where extremely unlikely indicates a probability of ≤ 0.05 , while it is ‘very unlikely’ to exceed 6°C, where this denotes a probability of ≤ 0.1 . We thus choose values of $S \in \{1.5, 3, 6\}$ for sensitivity analysis.

For our stochastic modelling we fit a continuous pdf to these data, using the mid-points of the IPCC probability ranges. In doing so, we face a choice over the type of function to fit. We performed a test of the fit of various functional forms, in terms of root-mean-square error, to the IPCC probability statements and found that the log-logistic function demonstrated the best fit among those we examined. The log-logistic function also has the advantage of having a tail of intermediate ‘fatness’ relative to other forms, thus, in this sense, it constitutes a middle-of-the-road assumption:

$$f(S) = \frac{a \times \left(\frac{S}{b}\right)^{a-1}}{b \left[1 + \left(\frac{S}{b}\right)^a\right]}, \quad (6)$$

where $a \approx 4.2$ and $b \approx 2.6$ are the shape and scale parameters respectively giving mean S of 2.9, a standard deviation of 1.4 and the 95th percentile at 5.3.

¹⁴ Where the density in the upper tail approaches zero more slowly than the exponential distribution.

It is worth emphasising, before moving on to the results, that there are other potentially significant sources of risk attending to the impacts of greenhouse gas emissions. Some of these are in the climate system – for instance the effective heat capacity of the oceans (Calel *et al.*, 2014) – yet a focus on S captures the essence of physical climate risk in a clear and simple way. Other sources of risk relate to damage for any given temperature and could also be modelled with probabilities, were the evidence to justify doing so. However, as we have argued, the damage functional form and parameterisation are currently very poorly constrained by evidence, and therefore it seems appropriate to instead pursue this, potentially very important source of risk, via a more simple sensitivity analysis on different functions as proposed in subsection 3.2.

4. Results

4.1. Baseline

At the heart of this exercise is an investigation into the prospects for growth and damage in a changing climate. Figure 1 plots baseline consumption *per capita* – i.e. in the absence of controls on carbon dioxide emissions imposed by a social planner – under various scenarios over the next two centuries. The upper panel plots the forecasts of the model with production (1.K) and damage from climate change on the capital stock, while the lower panel plots the forecasts of the model with production (1.TFP), where TFP growth is endogenous and where climate change reduces TFP.

The ‘standard’ trajectory represents the forecast of the standard DICE model without the various extensions we are considering in this article. The starting year is 2005. It is of course the same in both panels and notice immediately by how much consumption *per capita* increases in it, powered largely by exogenous productivity growth¹⁵ – in 2205 it is more than 15 times the 2005 level. This is despite a large increase in the atmospheric stock of carbon dioxide and in the global mean temperature (discussed below). Without large assumed improvements in the exogenous element of TFP, the increase in *per capita* consumption would be much smaller.

Changing the model of growth begins to yield more pessimistic forecasts, although it does not by itself qualitatively alter the tendency for the future to be much better off than the present. Under the model with capital damage, consumption/head in 2205 is 13.3 times higher than in 2005, while under the model of productivity damage it is 11.4 times higher. Since the total damage multiplier D_t in (4) is the same in the two models, simply being partitioned differently between damage on output, capital and TFP (see Appendix A), the larger effect in the model of productivity damage partly reflects the longer lasting impact of climate change in this model, where depreciation of productivity is slow compared with capital.

The divergence in forecasts is much more marked, however, when we layer on greater convexity of damage as in (4'). With Weitzman's (2012) calibration, consumption *per capita* grows much more slowly after 2150 in the model of capital

¹⁵ With no growth in labour, the long-run output growth rate implied by (1) is simply that of exogenous TFP.

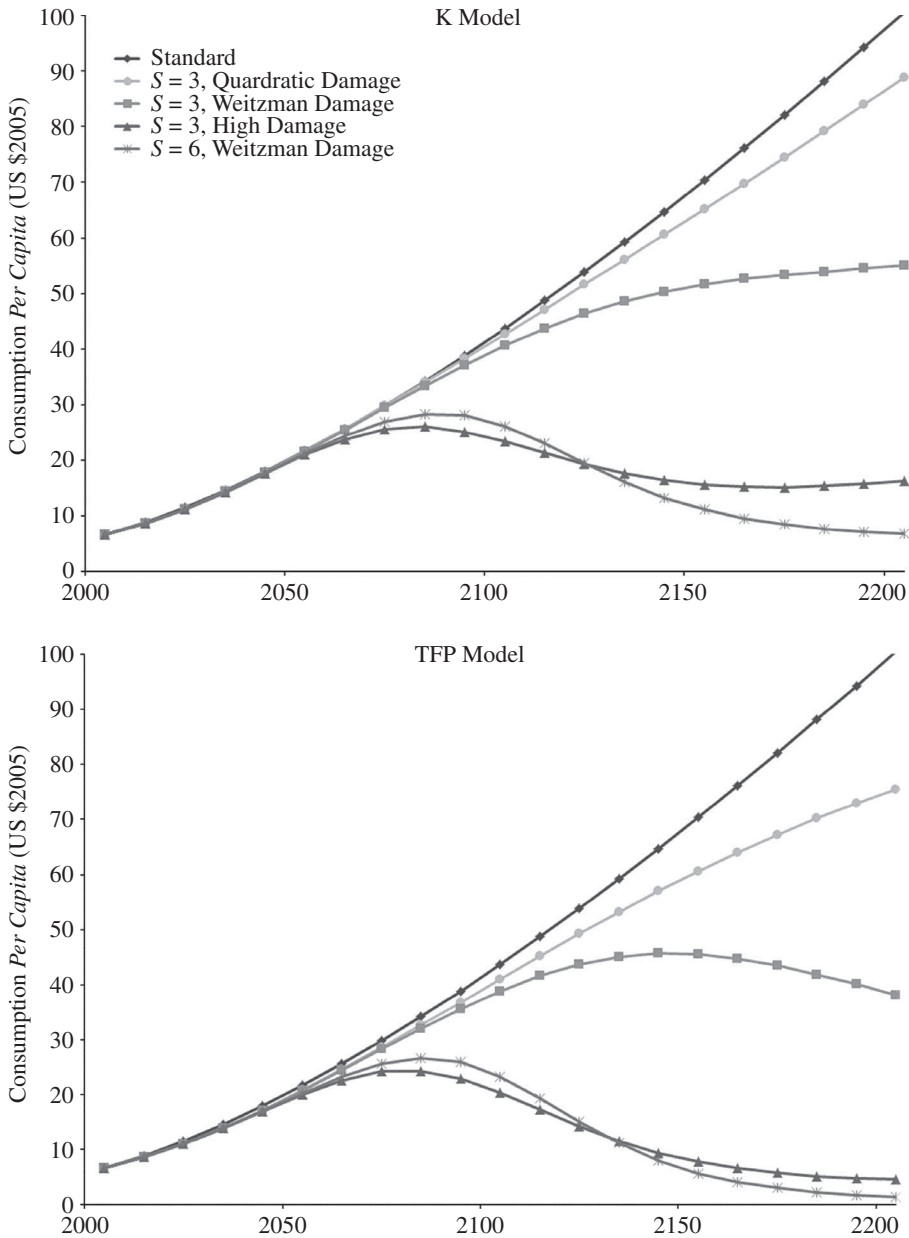


Fig. 1. Baseline Consumption Per Capita, 2005–2205

Notes. The upper panel corresponds to the model with capital damage and with knowledge proportional to the aggregate capital stock, while the lower panel corresponds to the model of endogenous TFP Growth and TFP damage.

damage, while in the model of TFP damage it peaks around 2150 before actually falling thereafter. By 2205, it is only 8.3 and 5.8 times higher respectively than today. If the damage function is set such that damage equivalent to 50% of global output are

assumed to occur upon 4°C warming, the collapse in living standards is much stronger, with consumption/head peaking before the end of this century and ending up in both models around or below the present level in real terms. A similar forecast is generated by Weitzman damage, when we instead increase the climate sensitivity parameter S to 6°C, which has a probability, as described above, of up to 0.1 according to IPCC. The two growth models yield similar forecasts in these cases, demonstrating the diminished importance of growth assumptions when instantaneous damage are severe and or warming is very rapid.

Changes in the atmospheric stock of carbon dioxide and global mean temperature, which drive these growth prospects, are shown in Figures B1 and B2 respectively in Appendix B. Baseline emissions will take the atmospheric stock of carbon dioxide to nearly 800 ppm by the end of this century in all the scenarios considered. The stock continues to increase after 2100 but there is some feedback of climate damage on emissions, which works through the depressive effect of climate damage on growth and of growth on emissions. The principal determinant of global mean temperature is the value of the climate sensitivity parameter. With the typical central estimate of 3°C, the global mean temperature is forecast to be in the region of 3.5°C above the pre-industrial level by 2100, while if $S = 6$ it could be more than 5°C above pre-industrial.

4.2. *Optimal Controls*

We now move to examining the optimal controls on emissions, set by a social planner. As Appendix A explains, the social planner's objective is to maximise the sum over time of discounted total utility by choosing a set of emissions control quantities and prices from 2015 until 2245, with a given abatement cost function (see Appendix A). We present results covering the rest of this century. Table 1 lists the optimal emissions control rate (the percentage or fractional reduction in emissions from the baseline) under various scenarios, while Table 2 does the same for the optimal carbon price.¹⁶ It is clear from the Tables that modifying the growth model and the associated pathways through which climate change can affect the economy, as well as increasing the convexity of the damage function, and increasing the climate sensitivity, can significantly increase the optimal emissions control rate and the associated carbon price, both initially and throughout.

Let us focus on initial control quantities and prices – these give us something with which to compare current global policy efforts and debates. In standard DICE the emissions control rate, that is the percentage reduction in industrial carbon dioxide emissions, is 0.158 in 2015, with an associated carbon price of \$44/tC in 2005 prices (divide by roughly 3.7 to obtain estimates/tCO₂, and multiply by c. 1.16 to bring up to 2012 prices¹⁷). If we switch from this standard model of exogenous

¹⁶ Where the optimal carbon price is defined as the marginal cost of abatement at the optimal emissions level calculated. Whether it is reasonable to interpret this as a price depends on the convexity of the abatement cost curve, i.e. it depends on there being rising marginal costs. It has been contended that marginal costs do not rise but these are issues for another paper.

¹⁷ World Bank data on GDP deflator, from <http://data.worldbank.org/indicator/NY.GDP.DEFL.KD.ZG>, retrieved on 22 November 2013.

Table 1
Optimal Emissions Control Rate, 2015–2105. $S = 3$ Unless Otherwise Indicated

Standard	2015	2025	2035	2045	2055	2065	2075	2085	2095	2105
<i>Capital models</i>										
Quadratic damage	0.213	0.289	0.356	0.424	0.495	0.565	0.636	0.706	0.777	0.848
Weitzman damage	0.235	0.322	0.401	0.484	0.568	0.650	0.730	0.805	0.875	0.944
Weitzman damage, $S = 6$	0.360	0.494	0.619	0.751	0.883	1	1	1	1	1
High damage	0.342	0.471	0.591	0.709	0.814	0.901	0.970	1	1	1
<i>Productivity models</i>										
Quadratic damage	0.272	0.365	0.444	0.528	0.614	0.702	0.792	0.882	0.974	1
Weitzman damage	0.290	0.392	0.480	0.573	0.667	0.761	0.852	0.942	1	1
Weitzman damage, $S = 6$	0.432	0.584	0.722	0.868	1	1	1	1	1	1
High damage	0.396	0.538	0.663	0.783	0.891	0.984	1	1	1	1

Table 2
Optimal Carbon Prices (2005 US\$/tC), 2015–2105. $S = 3$ Unless Otherwise Indicated

Standard	2015	2025	2035	2045	2055	2065	2075	2085	2095	2105
<i>Capital models</i>										
Quadratic damage	76	129	182	245	316	393	476	563	656	752
Weitzman damage	91	156	226	310	405	506	609	711	812	912
Weitzman damage, $S = 6$	196	337	495	684	895	1097	1074	1052	1032	1012
High damage	178	309	455	617	774	909	1017	1052	1032	1012
<i>Productivity models</i>										
Quadratic damage	118	196	272	363	466	580	705	840	984	1012
Weitzman damage	133	222	313	420	541	670	806	945	1032	1012
Weitzman damage, $S = 6$	271	456	653	888	1121	1097	1074	1052	1032	1012
High damage	233	393	559	738	911	1066	1074	1052	1032	1012

growth to (1.K) with capital damage, the optimal emissions control rate rises to 0.213 (optimal carbon price = \$76/tC). Further extending this model to incorporate highly convex damage with Weitzman's (2012) parameterisation, it rises to 0.235 (optimal price = \$91/tC), while with our high damage function scenario it is 0.342 (optimal price = \$178/tC). When Weitzman damage are combined with a high climate sensitivity, the optimal control rate is 0.36, brought about by an optimal price levied at \$196/tC. Some caution should be exercised, however, in interpreting the relevance of these strong initial control rates and prices, because DICE, as a model of medium and long-run dynamics, lacks adjustment costs, which could render such a rapid decarbonisation infeasible.

In the endogenous growth model (1.TFP) where instantaneous climate damage work on TFP as well as output, the increase in the controls is even stronger. With quadratic damage, the optimal control rate on emissions is 0.272 with an associated carbon price of \$118/tC. Moving to Weitzman damage increases this to 0.29 (optimal carbon price = \$133/tC), while with our high damage function scenario

the controls are respectively 0.396 and \$233/tC. When Weitzman damage is combined with a high climate sensitivity they are respectively 0.432 and \$271/tC. Notice for both growth models the marked rise in the carbon price when we move from Weitzman to high damage or from $S = 3$ to $S = 6$, which reflects convexity in the marginal abatement cost function. Nonetheless, the same remarks regarding adjustment costs and their potential effect on the optimal controls apply here.

Figures B3 and B4 in Appendix B show the consequences of the optimal controls for global mean temperature and the atmospheric stock of CO₂. Compared with the baseline, it can be seen that maximisation of social welfare implies significant reductions in both climate variables. With Weitzman damage, the build-up of atmospheric CO₂ is limited to 524 ppm in the model of capital damage and 489 ppm in the model of TFP damage, while with the more pessimistic parameterisation of the damage function the corresponding maximum concentrations are 459 and 444 ppm. These numbers are broadly in line with the types of stabilisation concentrations recommended by many scientists. In sharp contrast, with standard DICE the optimal emissions controls allow atmospheric CO₂ to rise throughout this century and peak at around 735 ppm in the middle of the next century. The resulting warming depends on the climate sensitivity.

4.3. *Optimal Control Under Stochastic Warming*

Thus, far we have computed the optimal controls, contingent on a set of point values of the climate sensitivity parameter, $S \in \{1.5, 3, 6\}$. A fuller specification of climate risk involves characterising a probability distribution over different values of S , as we described in Section 3, and solving for the optimal path of emissions controls. The planner's problem is specified as maximising expected social welfare, where expectations are formed before the first period commences and are not revised (see Appendix A for further details of the optimal control problem).¹⁸ Expected values are formed in a Monte Carlo simulation, sampling (via the Latin Hypercube method) 500 times from $f(S)$ in (6).

Tables 3 and 4 report the optimal control quantities and prices respectively for the two growth models, each run with the various different damage functions. Since this exercise constitutes a fuller specification of climate risk, these might be considered our headline results. Notice that, comparing them with Tables 1 and 2, the effect of randomising S depends on the damage function – the optimal controls are higher under random S , given Weitzman or high damage, but lower given quadratic damage. Remember that $f(S)$ in (3) is not a mean-preserving spread around $S = 3$. Rather, mean S is 2.9 and, as a distribution with a large positive skew, significantly more than half of the probability mass lies below the mean. When one bears in mind that what

¹⁸ In line with much of the literature, we simplify the problem by omitting the possibility of learning about the climate sensitivity from observations obtained after the first period has commenced. So the planner must stick to optimal controls computed at the outset, a so-called open-loop control. Were it possible to learn about climate sensitivity from observations and to change policy settings in response – a closed-loop policy – the planner could of course achieve at least as high a level of social welfare, most probably much higher.

Table 3
Optimal Emissions Control Rate Under Random S, 2015–2105

	2015	2025	2035	2045	2055	2065	2075	2085	2095	2105
Standard	0.158	0.184	0.211	0.240	0.270	0.302	0.335	0.370	0.407	0.446
<i>Capital models</i>										
Quadratic damage	0.204	0.277	0.341	0.406	0.474	0.543	0.611	0.681	0.750	0.819
Weitzman damage	0.250	0.344	0.434	0.532	0.631	0.732	0.831	0.925	0.993	0.993
High damage	0.393	0.542	0.688	0.841	0.986	0.998	0.998	0.998	0.999	0.999
<i>Productivity models</i>										
Quadratic damage	0.261	0.350	0.427	0.508	0.591	0.677	0.765	0.854	0.944	1
Weitzman damage	0.307	0.417	0.518	0.627	0.743	0.862	0.982	0.999	1	1
High damage	0.481	0.656	0.825	1	1	1	1	1	1	1

Table 4
Optimal Carbon Prices (2005 US\$/tC) Under Random S, 2015–2105

	2015	2025	2035	2045	2055	2065	2075	2085	2095	2105
<i>Capital models</i>										
Quadratic damage	70	119	169	226	293	365	442	528	614	707
Weitzman damage	101	176	261	368	490	625	769	914	1019	999
High damage	229	399	598	838	1093	1092	1071	1050	1030	1010
<i>Productivity models</i>										
Quadratic damage	110	181	253	338	435	543	664	792	930	1012
Weitzman damage	147	248	359	494	657	839	1040	1050	1032	1012
High damage	329	563	830	1146	1121	1097	1074	1053	1032	1012

ultimately matters is the pdf of consumption *per capita* that results from $f(S)$, it should start to become clear that, when the damage function has modest curvature, the effect of randomising S on the optimal controls can be to lower them, but when the damage function has strong curvature the opposite is true, because the tail of high temperatures exerts an ever larger relative effect on consumption *per capita*, utility and social welfare.

Figures B5 and B6 in Appendix B show the consequences of the optimal controls for the atmospheric stock of CO₂ and global mean temperature respectively.¹⁹ Figure B5 shows that the optimal mean stock of atmospheric CO₂ peaks in our endogenous growth models at no more than about 500 ppm, and as little as 420 ppm, depending on the growth model and damage function. These stock levels are well below those in the standard DICE model. Those combinations of growth model

¹⁹ Since the climate sensitivity is uncertain, so, obviously, is the change in the global mean temperature, and since this goes on to affect emissions via damage, there is also some uncertainty in the longer run about the atmospheric stock of CO₂. Therefore, both figures report mean values from the Monte Carlo simulation. In the case of the atmospheric stock of CO₂, the uncertainty is very small (no more than 1 ppm), but in the case of global mean temperature it is considerably larger. Therefore, in the latter case we also show the 90% confidence interval, in 2205, from the Monte Carlo simulation to the right of the main chart.

and damage function yielding higher climate impacts support a lower optimal stock. Compared with Figure B3 we can see that the optimal stock is lower under random S than when $S = 3$. Figure B6 shows that mean temperature is kept to a maximum of around 2°C except in two cases. First, in model (1.K) with capital damage, when the damage function is quadratic, mean warming peaks at around 2.5°C early next century. Second, in standard DICE mean warming peaks at *c.* 3.5°C. Notice the spreads around mean warming and in particular the very large 90% confidence interval around warming in standard DICE, where the 90th percentile reaches as much as 5.6°C. Optimal emissions controls in our extended models of DICE cut this tail of high temperatures significantly, due to their damaging consequences in the short and long run.

5. Conclusions

‘To slow or not to slow’ (Nordhaus, 1991) and its subsequent development into the dynamic DICE model have given us what seems to be a coherent and powerful framework for assessing the costs and benefits of climate-change mitigation. But it has in-built assumptions on growth, damage and risk, which together result in gross underassessment of the overall scale of the risks from unmanaged climate change (Stern, 2013). This criticism applies with just as much force to most of the other IAMs that DICE has inspired. The purpose of this article has been to show how these unrealistic assumptions might be relaxed and what would be the consequences of doing so, in terms of optimal emissions reductions and carbon prices, atmospheric concentrations of carbon dioxide and global mean temperature.

The first assumption we have relaxed is that the underlying drivers of economic growth are exogenous and unaffected by climate change. Instead we look at two models of endogenous growth, in which the damage from climate change affect the drivers of long-run growth, not just current output. The second assumption we have relaxed is that the damage function relating instantaneous climate damage to the increase in global mean temperature is only weakly convex. Instead, we allow for the possibility that instantaneous damage increase rapidly, particularly once the global mean temperature reaches 4–6°C above the pre-industrial level. We suggest this representation is more plausible, given the scale of change that such warming could bring; at the very least, simulations based on weak convexity should not dominate our attention as they have come to do. The third assumption we have relaxed is that the climatic response to greenhouse gas emissions is moderate and moreover is precisely understood. Very few, if any, commentators would explicitly claim that climate sensitivity is precisely understood, of course. Nonetheless, most economic modelling is undertaken using only a single, central estimate of the climate sensitivity parameter, fixed in the centre of the distribution of available estimates from the science. We explore risk in this crucial parameter.

Overall, the scale of the risks from unmanaged climate change in this modelling framework is the convolution of these three extensions. We show that, with the models extended in this way, business-as-usual trajectories of greenhouse gas emissions give rise to potentially large impacts on growth and prosperity in the

future, especially after 2100. Indeed, these impacts are large enough to feed back into future emissions via reduced activity but the feedback is too small and too late for the system to self-regulate. Thus, optimal emissions control is strong and strongly increasing. As a guide, we find that these models suggest the carbon price in a setting of globally coordinated policy, such as a cap-and-trade regime or a system of harmonised domestic carbon taxes, should be in the range \$32–103/tCO₂ (2012 prices) in 2015. It must be remembered that the DICE model lacks adjustment costs, so the high end of the range should be interpreted cautiously. On the other hand, and potentially of great importance, we have, notwithstanding our extensions, omitted important risks in relation to the distribution of damage, which could give higher carbon prices. Within two decades, the carbon price should rise in real terms to \$82–260/tCO₂. Doing so would, according to the model, keep the expected atmospheric stock of carbon dioxide to a maximum of *c.* 425–500 ppm and the expected increase in global mean temperature to *c.* 1.5–2°C above pre-industrial.

The study is only a preliminary investigation, whose purpose was to illustrate or sketch the consequences of relaxing assumptions that have limited plausibility and possible large effects on policy conclusions. We have, for instance, restricted our attention to knowledge, accumulated through learning-by-doing, as the driver of long-run growth, though other sources of growth are important and other models might be deployed. Our exploration of the implications of risk has, for the sake of clarity, been limited to the climate sensitivity, though other sources of great risk exist in the physical climate system, not to mention in the economy. The models that we do use require the choice of parameter values, about some of which there is currently very little relevant empirical evidence. Given slow rates of learning about some IAM parameters, this should be regarded as an endemic problem, however (Pindyck, 2013). It is not the case that the standard model parameters are well constrained, whereas the new parameters we introduce are not. Future work building on our framework should also pay attention to the costs of rapid adjustment to a low-carbon economy and possible limits to the speed of decarbonisation. This work will need to go well beyond the choice of parameter values to consider new model structures.

This is not an article about the sensitivity of results to pure-time discounting, or other parameters and structures relevant to discounting. As we found in the technical Appendix to Stern (2007) and in Dietz *et al.* (2007*a,c*), lower pure-time discounting does indeed favour stronger and earlier action to curb emissions. Those results were from the 'PAGE' IAM (Hope, 2006) but we know from other work that this is also true of DICE (Nordhaus, 2007). We have argued elsewhere that careful scrutiny of the ethical issues around pure-time discounting points to lower values than are commonly assumed (usually with little serious discussion). Pure-time discounting is essentially discrimination by date of birth in the sense that a life, which is identical in all respects (including time patterns of consumption) but happens to start later, has a lower value. If, for example, the pure-time discount rate were 2%, a life starting 35 years later, but otherwise the same, would have half the value of a life starting now. The time horizon essential to a discussion of climate change makes careful examination of these ethical issues unavoidable.

Preliminary calculations indicate that low pure-time discounting will significantly increase the optimal controls in this article as well.

One cannot and should not expect a single model to capture all relevant issues and neither should we be able to resolve all difficulties within a single framework.²⁰ It is enough for a model to help raise and understand key aspects of a problem. This means that we should be grateful to Bill Nordhaus for providing one helpful vehicle. As it is expanded and different perspectives are brought in, including the possibility of major loss of life from climate change, then we would suggest the arguments for strong action will look still stronger.

Appendix A. Extended Model Description

Here, we offer an extended description of the DICE model, focusing on the major model equations and in particular on our modifications. Even more detail can be found on Nordhaus’s model website at <http://www.econ.yale.edu/~nordhaus/homepage/index.html>. Our analysis is based on the 2010 version of the model.

The model represents a social planner maximising a classical utilitarian objective functional by choosing the rate of control of industrial carbon dioxide emissions:

$$\max_{\{\mu_t\}_{t=1}^{T_{\max}}} W = \sum_{t=0}^{T_{\max}} u(c_t)L_t(1 + \rho)^{-t},$$

where $\mu \in [0, 1]$ is the emissions control rate, $u(c_t)$ is the instantaneous social utility of consumption *per capita* at time t and $\rho = 0.015$ is the utility discount rate. Note that c is not only time-dependent as the above equation implies, it is also state-dependent when we undertake stochastic modelling. We suppress notation of state-dependence for simplicity; bear in mind that, when running the model with a random parameter (the climate sensitivity S in (3)), we take the expectation of social welfare. T_{\max} is the terminal period, which is 2595. The model proceeds in time steps of ten years from 2005, so appropriate interpretations must be made in considering the various equations of motion. Notice that, since 2005 is in the past, our first control period is $t = 1$, i.e. 2015.²¹

The utility function is iso-elastic,

$$u(c_t) = \frac{c_t^{1-\eta}}{1-\eta},$$

where η is the elasticity of marginal social utility of consumption and is set to 1.5 to allow comparison with standard DICE.

As set out in the main body of the article, we explore two alternative production functions:

$$Y_t = (1 - D_t^Y)(1 - \Lambda_t)A_tK_t^{\alpha+\beta}L_t^{1-\alpha}, \tag{1.K}$$

$$Y_t = (1 - D_t^Y)(1 - \Lambda_t)\bar{A}_tK_t^{\alpha}L_t^{1-\alpha}. \tag{1.TFP}$$

²⁰ For example, the paradoxes of social choice theory can be better understood by broadening the philosophical perspective and are not easily resolved within the standard framework (Sen, 2009).

²¹ In fact, we need only solve μ_t from 2015 to 2245 inclusive, since DICE assumes that from 2255 onwards $\mu_t = 1$, because a zero-emissions backstop energy technology becomes competitive.

The capital elasticity $\alpha = 0.3$, while the elasticity of output with respect to knowledge, $\beta = 0.3$ (Mankiw *et al.*, 1995).

The equation of motion of capital in model (1.K) is

$$K_{t+1} = (1 - D_t^K)(1 - \delta^K)K_t + I_t,$$

where $\delta^K = 0.1$, while in model (1.TFP) we simply drop $(1 - D^K)$.

Output is either consumed or invested,

$$Y_t = C_t + I_t$$

where $C_t = c_t L_t$ is aggregate consumption and $I_t = sY_t$, where $s = 0.23$ is the savings rate (calibrated to long-run average optimal savings in standard DICE, without climate damage and emissions abatement costs and, in principle, some private inter-temporal objectives). We specify exogenous, constant savings in order to capture in a simple way the second-best context implied by fitting our models of endogenous growth to current macroeconomic data. In growth models with knowledge spillovers, the savings rate chosen by a planner will be greater than the savings rate emerging from a decentralised equilibrium of firms and households, because the marginal private return to investment does not include the spillovers.

A more elaborate analysis would permit households to choose their optimal savings rate in equilibrium with firms' private marginal product of capital (in response to the planner's emissions controls), but it is worth noting that, in standard DICE, endogenising the savings rate has been shown to make little difference to the optimal policy (Fankhauser and Tol, 2005; and Nordhaus's laboratory notes on DICE), so our simplification is unlikely to matter.²² In any case, whether households are currently taking into account the effects of climate policy on future consumption prospects when choosing how much to save is unclear.

In model (1.TFP), productivity is endogenous and its equation of motion is

$$\bar{A}_{t+1} = (1 - D_t^A)(1 - \delta^A)\bar{A}_t + \gamma_1 I_t^{\gamma_2}, \quad (3)$$

where $\delta^A = 0.01$ is the rate of depreciation of the stock of TFP, while $\gamma_1 \approx 0.0003$ and $\gamma_2 \approx 0.373$ are parameters of the spillovers function. γ_1 and γ_2 are calibrated so that output in (1.TFP), in the absence of climate damage and emissions abatement costs, is the same as in standard DICE. In model (1.K), TFP is an exogenous time series, so (3) does not apply.

The climate damage function is

$$D_t = 1 - 1/(1 + \pi_1 T_t + \pi_2 T_t^2 + \pi_3 T_t^{6.754}), \quad (4')$$

where $\pi_1 = 0$ and $\pi_2 \approx 0.00284$ throughout. $\pi_3 = 0$ when we compute results for the standard setting (i.e. $D_t = \hat{D}_t$), $\approx 5.07 \times 10^{-6}$ when we use Weitzman's parameterisation, or $\approx 8.19 \times 10^{-5}$ according to our high damage specification, where D_t is assumed to be equal to 0.5 when the atmospheric temperature is 4°C above the pre-industrial level.

Damage is then partitioned between output and capital, or output and TFP, depending on the growth model:

$$D_t^i = f^i \cdot D_t,$$

$$D_t^Y = 1 - \frac{(1 - D_t)}{(1 - D_t^i)}$$

²² See also Mirrlees and Stern (1972), who first illustrated this feature in simple optimal growth models.

where f is the share of damage to $i = A$ or $i = K$. IAMs do not in general explicitly address the allocation of damage between capital and output, and vary widely in what they implicitly assume about it. Nordhaus and Boyer (2000) analysis might be read to suggest that f^K is in the region of 1/3, so 0.3 is the value we choose. The calibration problem is even more acute in the case of allocating damage between output and TFP – there are, as Moyer *et al.* (forthcoming) also point out, currently severe modelling, data and estimation problems in carrying out such an allocation. Moyer *et al.* (forthcoming) consequently explore a range of values of f^A between 1% and 100%. We make the relatively conservative assumption that $f^A = 0.05$.

The total abatement cost function is

$$\Lambda_t = \theta_{1,t} \mu_t^{\theta_2},$$

where $\theta_{1,t}$ is a time-varying coefficient and $\theta_2 = 2.8$, hence marginal abatement costs are increasing in emissions control.

Cumulative industrial carbon dioxide emissions are constrained by remaining fossil fuel reserves,

$$\sum_{t=0}^{T_{\max}} E_t^{\text{IND}} \leq C \text{ Cum},$$

where $C \text{ Cum} = 6000$ gigatonnes of carbon is the constraint, and total emissions of carbon are the sum of industrial emissions of carbon dioxide and exogenous emissions of carbon dioxide from land use:

$$E_t = E_t^{\text{IND}} + E_t^{\text{LAND}}.$$

Industrial carbon dioxide emissions at time t are proportional to gross output in the same period, hence there is a different function depending on the growth model:

$$\begin{aligned} E_t^{\text{IND}} &= \sigma_t (1 - \mu_t) A_t K_t^{\alpha+\beta} L_t^{1-\alpha}, \text{ or} \\ &= \sigma_t (1 - \mu_t) \bar{A}_t \bar{K}_t^{\alpha} \bar{L}_t^{1-\alpha}, \end{aligned}$$

where σ_t is the ratio of uncontrolled emissions to output and is an exogenous, time-varying coefficient. It is assumed that $\partial\sigma/\partial t < 0$, representing autonomous improvements in carbon productivity that arise from technical progress and structural change, and that $\partial^2\sigma/\partial t^2 > 0$.

The atmospheric stock of carbon is driven by total emissions, in a system of three equations representing the cycling of carbon between three reservoirs, the atmosphere M^{AT} , a quickly mixing reservoir comprising the upper ocean and parts of the biosphere M^{UP} , and the lower ocean M^{LO} :

$$\begin{aligned} M_t^{\text{AT}} &= E_t + \phi_{11} M_{t-1}^{\text{AT}} + \phi_{21} M_{t-1}^{\text{UP}} \\ M_t^{\text{UP}} &= \phi_{12} M_{t-1}^{\text{AT}} + \phi_{22} M_{t-1}^{\text{UP}} + \phi_{32} M_{t-1}^{\text{LO}} \\ M_t^{\text{LO}} &= \phi_{23} M_{t-1}^{\text{UP}} + \phi_{33} M_{t-1}^{\text{LO}}. \end{aligned}$$

Cycling is determined by a set of coefficients ϕ_{jk} that govern the rate of transport from reservoir j to k per unit of time.

The change in the atmospheric stock of carbon from the pre-industrial level determines radiative forcing,

$$F_t = F_{2 \times \text{CO}_2} \times \left(\log_2 \frac{M_t^{\text{AT}}}{M^{\text{AT}}} \right) + F_t^{\text{EX}},$$

where \widehat{M}^{AT} is the stock of carbon in the atmosphere before the industrial revolution (i.e. in 1750) and F_t^{EX} is exogenous radiative forcing (capturing among other things the forcing due to greenhouse gases other than carbon dioxide) and is time-dependent. The equation of motion of temperature is given by:

$$T_t = T_{t-1} + \kappa_1 \left[F_t - \frac{F_2 \times \text{CO}_2}{S} (T_{t-1}) - \kappa_2 (T_{t-1} - T_{t-1}^{LO}) \right], \tag{5}$$

where T^{LO} is the temperature of the lower oceans and evolves according to:

$$T_t^{LO} = T_{t-1}^{LO} + \kappa_3 (T_{t-1} - T_{t-1}^{LO}).$$

Appendix B. Further Results

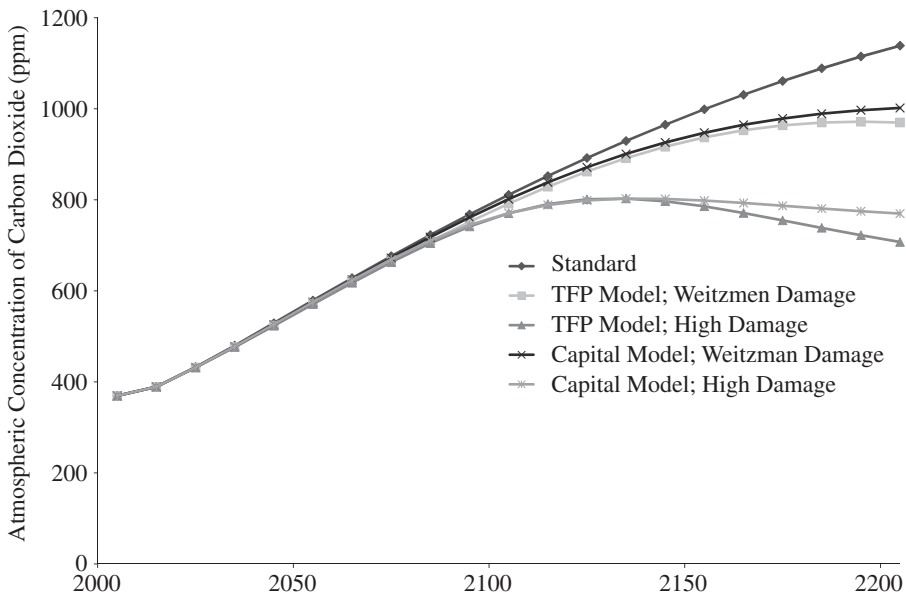


Fig. B1. *Baseline Atmospheric Stock of Carbon Dioxide, 2005–2205. S = 3*

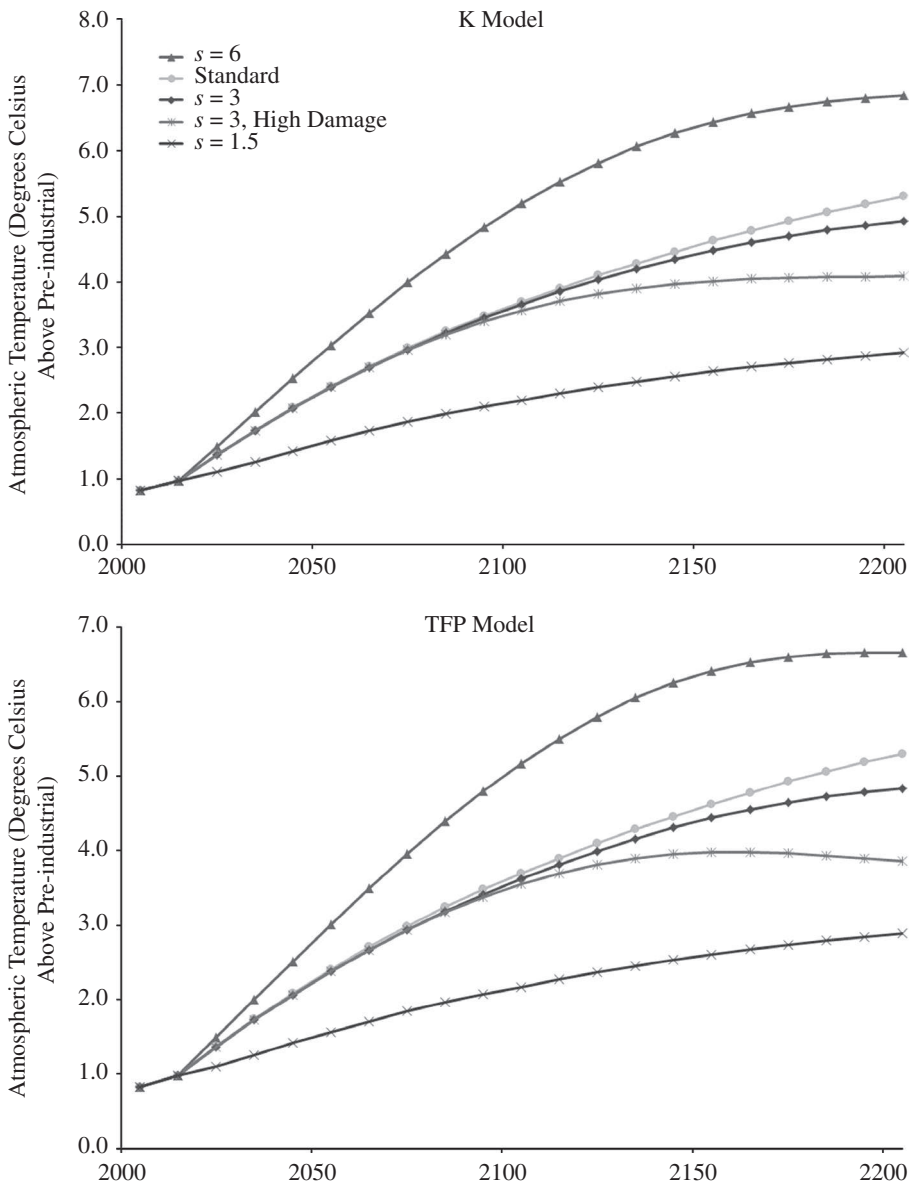


Fig. B2. *Baseline Global Mean Temperature (Degrees Centigrade Above Pre-industrial), 2005–2205*
 Notes. The upper panel corresponds with the model of capital damage, while the lower panel corresponds with the model of TFP damage. The damage function calibration is ‘Weitzman’ unless otherwise indicated.

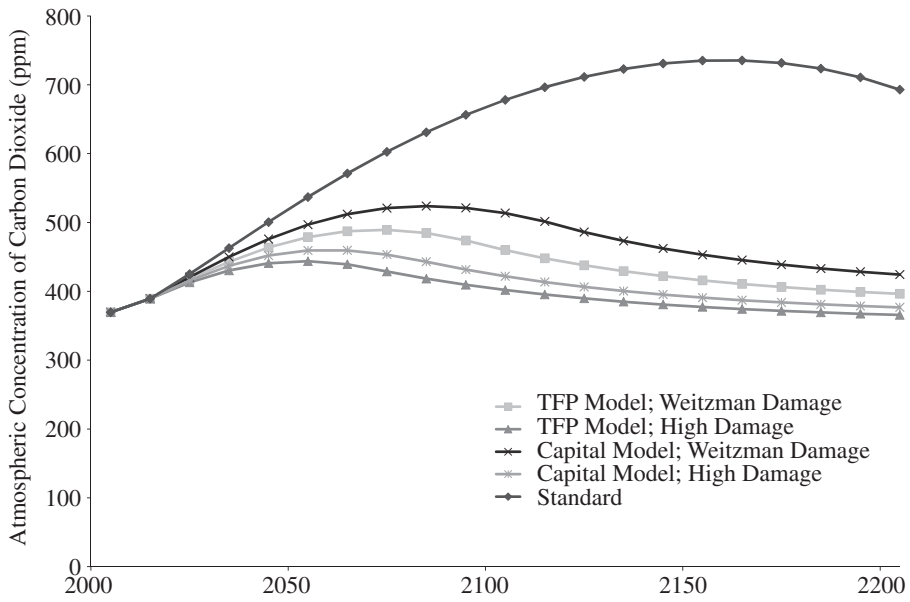


Fig. B3. *Optimal Atmospheric Stock of Carbon Dioxide, 2005–2205. S = 3*

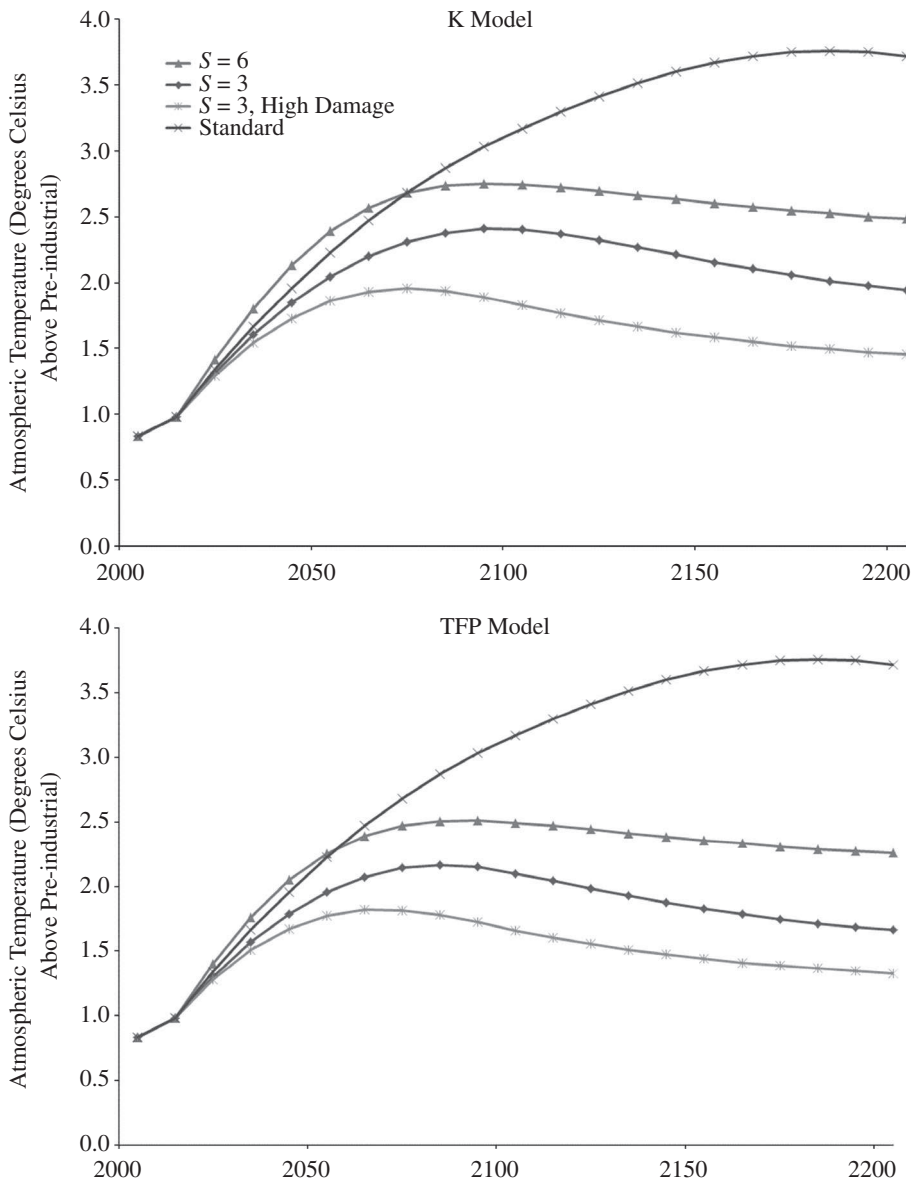


Fig. B4. *Optimal Global Mean Temperature (Degrees Centigrade Above Pre-industrial), 2005–2205*
Notes. The upper panel corresponds with the model of capital damage, while the lower panel corresponds with the model of TFP damage. The damage function calibration is ‘Weitzman’ unless otherwise indicated.

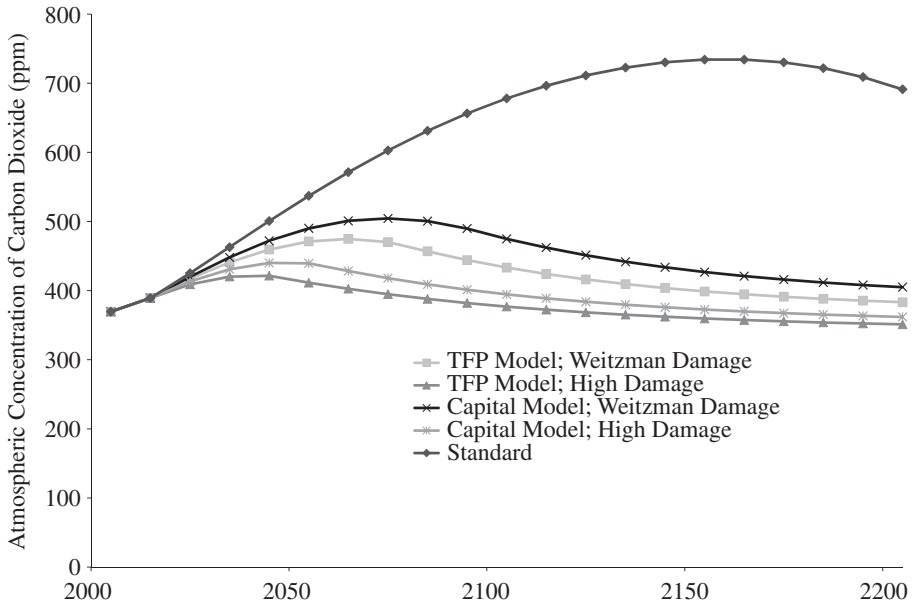


Fig. B5. *Optimal Atmospheric Stock of Carbon Dioxide, 2005–2205, Mean Over Random S*

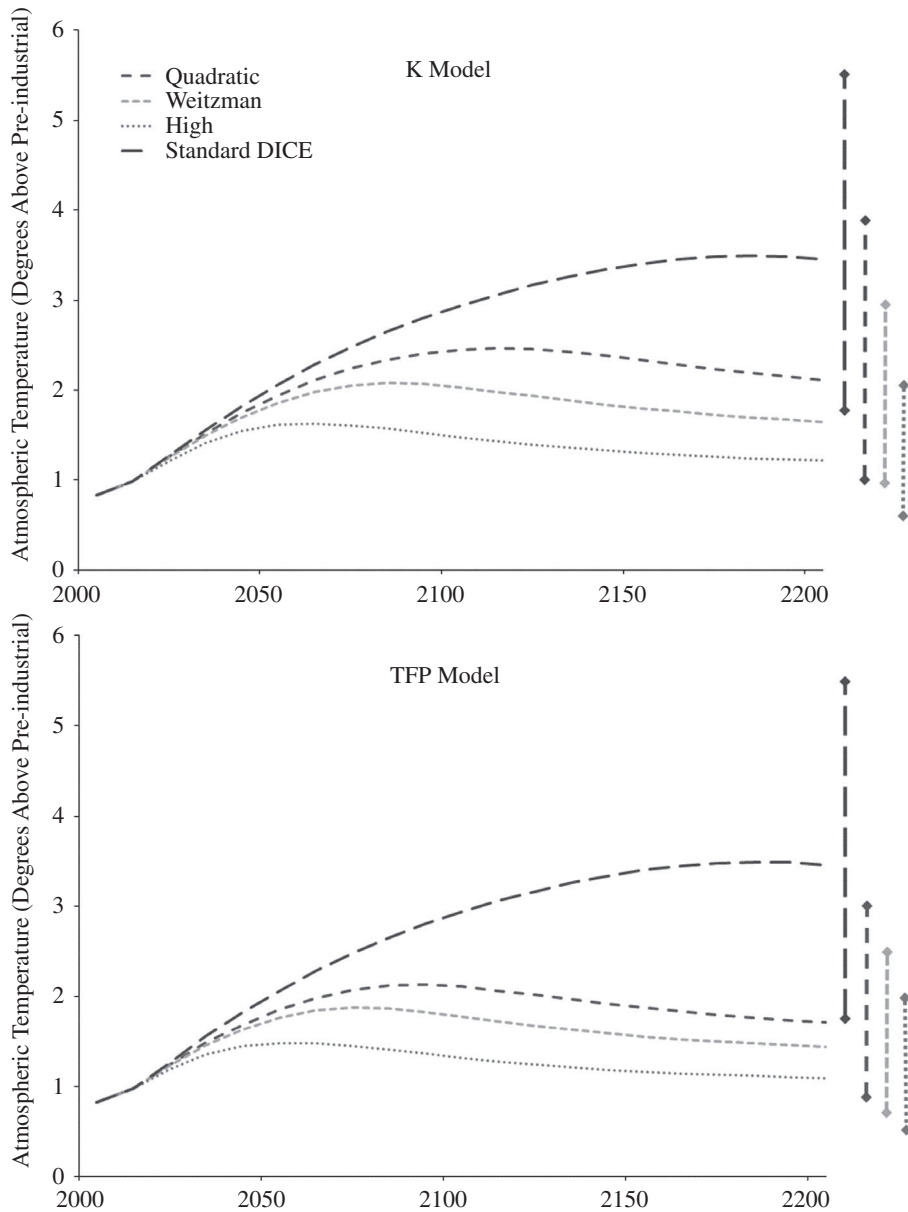


Fig. B6. *Optimal Global Mean Temperature (Degrees Centigrade Above Pre-industrial), 2005–2205, Mean Over Random S*

Notes. The upper panel corresponds with the model of capital damage, while the lower panel corresponds with the model of TFP damage. The bars on the right-hand side give the 90% confidence interval in 2205.

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Appendix C. Nordhaus, W.D. (1991). 'To slow or not to slow: the economics of the greenhouse effect', *ECONOMIC JOURNAL*, vol. 101(407), pp. 920–37.

TO SLOW OR NOT TO SLOW: THE ECONOMICS OF THE GREENHOUSE EFFECT

William D. Nordhaus

I. INTRODUCTION¹

Over the last decade, scientists have studied extensively the greenhouse effect, which holds that the accumulation of carbon dioxide (CO₂) and other greenhouse gases (GHGs) is expected to produce global warming and other significant climatic changes over the next century. Along with the scientific research have come growing alarm and calls for drastic curbs on the emissions of greenhouse gases, as for example the reports of the Intergovernmental Panel on Climate Change (IPCC [1990]) and the Second World Climate Conference (October 1990). To date, these call to arms for forceful measures to slow greenhouse warming have been made without any serious attempt to weigh the costs and benefits of climatic change or alternative control strategies.

The present study presents a simple approach for analyzing policies to slow climate change. We begin by summarizing the elements of an economic analysis of different approaches to controlling greenhouse warming. We then sketch a mathematical model of economic growth that links the economy, emissions, and climate changes and summarize the empirical evidence on the costs of reducing emissions and concentrations of greenhouse gases and on the damages from greenhouse warming, relying primarily on data for the United States. The different sections are then integrated to provide estimates of the efficient reduction of greenhouse gases, after which the final section summarizes the major results.

II. CLIMATE CHANGE: SCIENCE AND ECONOMIC MODELLING

In weighing climate-change policies, the prospects for global warming and the linkage between human activities and the emissions of GHGs form a key building block. This study uses a simplified analytical structure. We have taken existing models and simplified them into a few equations that are easily understood and manipulated.

The scientific basis of the greenhouse effect has been described in the preceding paper by Cline.² As a result of the buildup of a number of GHGs, it is expected that significant climate changes will occur over the next century and beyond. The major GHGs are carbon dioxide, methane, nitrous oxides, and chlorofluorocarbons (CFCs). Table 1 shows the important greenhouse

¹ This paper is a revision of earlier versions (see Nordhaus [1989]), and the author is grateful for insightful comments on early drafts from many people, with particular thanks to Jesse Ausubel, Alan Manne, James Sweeney, and an anonymous referee. This research was supported in part by the National Science Foundation.

² Excellent nontechnical discussions are also contained in National Research Council (1987), Schneider (1989), and IPCC (1990).

Table 1
Estimated contribution of different greenhouse gases to global warming mid-1980s

Greenhouse gas	Relative contribution		Source of emission
	Instantaneous (%)	Total (%)	
CO ₂	53.2	80.3	Largely from combustion of fossil fuels
Methane	17.3	2.2	Poorly known. From a wide variety of biological and agricultural activities
CFC-11 and 12	21.4	8.8	Wholly industrial, from both aerosols and non-aerosols. Being phased out
Nitrous oxides	8.1	8.7	From fertilisers and energy use

Source: Emissions from EPA (1989), vol. 1. Definition of instantaneous and total in text. Estimates of the ratio of total warming potential to instantaneous warming potential from Lashof and Ahuja (1991), with calculations and data explained in Nordhaus (1990). Uses zero discount rate on future warming.

gases along with the sources of emissions and estimates of their contribution to global warming. Current reviews suggest that a doubling of CO₂ or its radiative equivalent, will in equilibrium increase global mean surface temperature by 1° to 5 °C.³

A complication in studying climate change arises from the multitude of GHGs. In the analysis that follows, we translate each of the GHGs into its CO₂ equivalent. We also use a measure of the total warming potential, which is the contribution of a GHG to global warming summed over the indefinite future. A complete dynamic analysis would also incorporate discounting to take into account that the cost of warming is different depending upon the time at which the warming occurs, but this complication is of second-order importance and is ignored here.

Table 1 shows a comparison of the instantaneous (i.e. the relative impact upon warming per unit of concentration) and total warming potential of major GHGs in the mid-1980s.⁴ This shows the dominance of CO₂ in long-term warming from GHG emissions over the next century. Table 2 shows the estimates of CO₂-equivalent emissions of each of the major GHGs in 1985. The first column (production or emissions) shows the CO₂ equivalent of the total production or gross emissions in 1985, while the second column (emissions weighted by change in concentrations) reflects the fact that the increase in atmospheric concentrations is less than production or emissions. For both estimates, CO₂ is approximately 80 percent of the total global CO₂-equivalent emissions of around 8 billion tons. In this study, we measure CO₂ in terms of its carbon content. The ratio of CO₂ weight to carbon weight is $(12 + 16 + 16)/12 = 3.67$.

A final element in estimating the climatic impact of rising GHGs involves the time delay in the reaction of climate to increasing atmospheric concentrations.

³ The sources of uncertainty about future climate change focussing on CO₂ are systematically analysed in Nordhaus and Yohe (1983).

⁴ A non-technical discussion is provided in Nordhaus (1990). The estimates used here rely on the more complete analysis of Lashof and Ahuja (1991).

Table 2
CO₂-equivalent emissions 1985 (millions of metric tons, carbon content of CO₂ per year, total warming potential)

	Emission weights	Concentration weights
Carbon dioxide	6500	6500
Methane	612	181
Nitrogen oxides	549	703
Chlorofluorocarbons	261	714
Total, CO ₂ equivalent	7922	8098

Source: Emissions and changes in concentrations are from EPA (1989). Estimates of total warming potential are described in text and use a zero discount rate.

The average climate responds slowly to increases in radiative inputs, chiefly because of the thermal inertia of the oceans. Estimates of the delay to equilibrium range from 6 to 95 years. In the model used here, we simplify by assuming that the temperature adjustment process takes the following form:

$$\dot{T}(t) = \alpha\{g[M(t)] - T(t)\} \quad (1)$$

$$\dot{M}(t) = \beta E(t) - \delta M(t) \quad (2)$$

where dots over variable represent time derivatives and $t = \text{time}$

$T(t)$ = increase in global mean surface temperature due to greenhouse warming since mid-19th century ($^{\circ}\text{C}$)

$M(t)$ = anthropogenic atmospheric concentration of CO₂ equivalent GHGs (billions of tons of CO₂ equivalent)

$E(t)$ = anthropogenic emissions of CO₂ equivalent GHGs (billions of tons of CO₂ equivalent per year)

$g[\cdot]$ = equilibrium increase in global mean temperature in response to increasing CO₂ equivalent concentration

α = delay parameter of temperature in response to radiative increase (per year)

β = fraction of CO₂ equivalent emissions that enter the atmosphere

δ = rate of removal of CO₂ equivalent from the atmosphere (per year)

The interpretation of these equations is as follows. Equation (1) states that the increase in global temperature rises in response to the difference between the equilibrium temperature increase and the actual increase. Equation (2) is a simplified two-box diffusion model in which a fraction β of emissions goes into the atmosphere and the fraction δ of the quantity in the atmosphere diffuses into the deep ocean, which is a very large sink for CO₂.

We estimate the climate-equation parameters from existing climate models. Hansen estimates a time delay parameter (α), of 0.0181 for a box-diffusion ocean model with a temperature-CO₂ coefficient of 3 $^{\circ}\text{C}$ per doubling, while calculations by Stouffer *et al.* in a coupled atmosphere-deep ocean model (1990) have a time delay parameter of 0.013. These are slightly lower than other estimates and we use $\alpha = 0.02$ in our calculations. For the factor β (the

airborne fraction of GHGs), we estimated the equation with ordinary least squares using data on concentrations and emissions of CO₂ from 1850 to 1986. We use the conventional estimate for δ of 0.005 (representing a residence time of 200 years), and estimate β to be 0.49 with a standard error of 0.0125. We round this to $\beta = 0.50$ for the calculations that follow.

III. ECONOMIC APPROACHES TO CONTROL OF THE GREENHOUSE EFFECT

The economics of the greenhouse effect is a classic case of a public good, in which emissions of GHGs involve a global externality. We can analyse the costs and benefits of the greenhouse effect and policies in terms of two fundamental functions. The *greenhouse damage function* describes the costs to society of the changing climate. This damage function would incorporate, for example, the impact of changing crop yields, land lost to oceans, and so forth. The *abatement cost function* describes the costs that the economy undergoes to prevent or slow the greenhouse effect. The cost function would include the cost of changing from fossil to non-fossil fuels, the substitution of different substances for CFCs, raising coastal structures, and so on.

In what follows, we will concentrate upon *efficient* strategies to reduce the costs of climate change. An efficient strategy is one that maximises overall net economic welfare (call it 'green GNP'), which includes all goods and services, whether or not they are metered by markets, and includes all externalities from economic activity.

Figure 1 depicts the analysis graphically in a static framework. The upward sloping curve is the efficient marginal cost of abatement function, showing the incremental cost of reducing CO₂ or other GHGs by one unit. The wavy line is the marginal damage from greenhouse warming associated with an additional unit of GHGs. The horizontal axis measures GHG emissions as a percent of the uncontrolled quantity. This variable has a value of 0% when GHGs are uncontrolled (i.e. in an unregulated environment). We can derive from economic theory certain properties about the shape of the marginal abatement cost function in a competitive economy with no other externalities and where controls are efficiently designed. First, we know that it has a minimum of zero at the uncontrolled point: *The first units of GHG reduction are virtually free. This is the result of the zero market price on the GHG emissions.* Second, we know that the cost function increases in the level of abatement. Third, society can always do worse than the abatement cost function by inefficiently designing regulations.

Next examine the greenhouse damage function, which measures the cost to the economy of higher levels of GHGs (measured relative to some baseline). In contrast to the cost function, we know little about the shape of the damage function – for this reason, we draw the damage function as a wavy line. We suspect that higher levels of greenhouse gases will hurt the global economy, but because of the fertilization effect of CO₂ or the attractiveness of warm climates, the greenhouse effect might on balance actually be economically advantageous.

Figure 1 uses the marginal cost and damage concepts to describe different

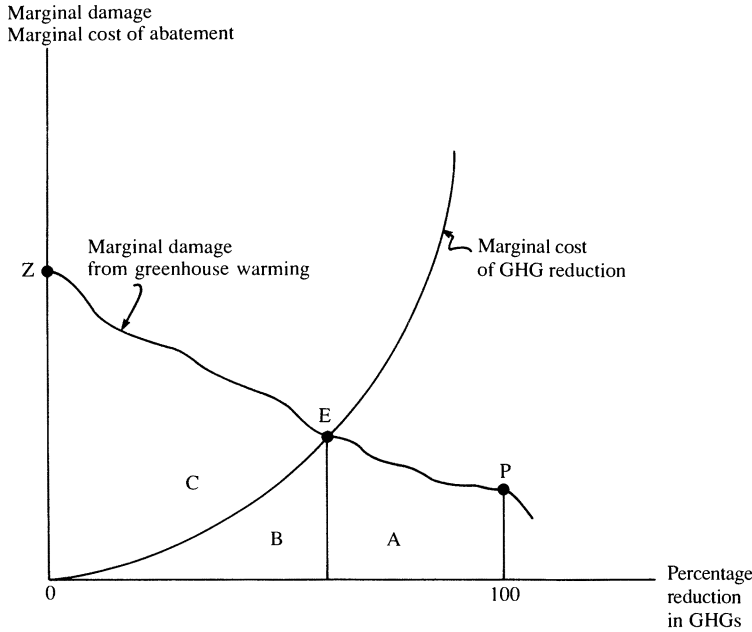


Fig. 1. Marginal costs of GHG reductions and marginal damage from GHG emissions.

policies along with their costs and benefits. We can measure the total cost of an uncontrolled greenhouse effect as the area under the damage curve over the entire range [0, 100]; this area is the sum of regions A + B + C in Figure 1. Reducing GHG levels by one unit from the laissez-faire point Z produces a net gain equal to the reduction of damage of amount Z minus the increase of cost of zero. The efficient level of control is at point E, where the marginal cost of abatement equals the marginal damage of emissions. Relative to the laissez-faire equilibrium, the damages at the optimal-control point E have been reduced by the sum of areas B + C, while the increased abatement costs are given by B, so the net economic gain is given by the area C.

IV. MODELLING OF ECONOMIC AND CLIMATIC DYNAMICS

Because greenhouse policies involve investing today to reduce damages in the distant future, we present a stylised model of the relationship between economic growth and climate change that incorporates the dynamics of climate change and of investing in slowing climate change. The model includes three components: (1) a simplified model of the cycle of greenhouse gases; (2) an economic model that incorporates the tradeoffs involved in reducing greenhouse gases; and (3) a framework for describing how society chooses between alternative consumption paths.

Following Section II’s analysis, it will be convenient to linearise equation (1) as follows:

$$\dot{T}(t) = \alpha\{\mu M(t) - T(t)\} \tag{3}$$

where all variables were defined above except for μ , which is the linearised equilibrium sensitivity of temperature to concentrations of CO₂-equivalent emissions (i.e., $g'(M) = \mu$).

In examining the economics of greenhouse warming, we rely upon a simple general equilibrium model of inputs, outputs, climate, emissions, and consumption. We study the impact of policies upon an economy in the middle of the next century. The key assumption is that the economy is in *resource steady-state*. This signifies that all physical flows in the global economy are constant although the real value of economic activity may be increasing. All emissions and concentrations of greenhouse gases are therefore constant, and the climatic impacts of industrial activity have stabilised. We allow for ‘balanced resource-augmenting technological change’ at rate h ; that is, the useful goods and services produced by the economy will be assumed to grow uniformly in each sector even though the physical throughputs are constant.

In the steady state, per capita consumption is given by

$$c(t) = y^* e^{ht} \{g[E^*] - \phi[T^*]\}. \quad (4)$$

In this equation, the new variables are $c(t)$ = per capita consumption at time t ; y^* is a constant; $y(t) = y^* e^{ht}$ = output before any emissions reduction and with no climate damage; E^* = steady-state emissions; T^* = steady-state temperature increase; $g(E^*)$ = steady state cost function from reduction of emissions; and $\phi(T^*)$ = steady state damage from climate change. The production function is undated to indicate that we are considering a resource steady-state.

We assume that it is desirable to maximize a social welfare function that is the discounted sum of the utilities of per capita consumption. An optimal program for allocating resources over time maximizes the following:

$$V = \int_0^{\infty} u[c(t)] e^{-\rho t} dt. \quad (5)$$

The fundamental policy question involves how much reduction in consumption society should incur today to slow the consumption damages from climate change in the future.

The choice of discount rate is a thorny issue in studies of investment, and this is particularly the case for investments over a century or more. Assuming that the rate of return on investment has been determined appropriately, in our resource steady-state, the real discount rate on goods will be given by $r = \rho + \alpha h$, where ρ = the pure rate of social time preference, $-\alpha$ = the elasticity of the marginal utility with respect to per capita consumption, and h is the growth rate of per capita consumption. In the model used here, the critical parameter is $r - h$, which is the difference between the discount rate on goods and the growth rate of the economy. This will be relevant because, while we discount future damages at r , in our resource steady state the damages will be growing at the rate of economic growth (h). With slow economic growth (h near zero), or with a utility function close to logarithmic (α near 1), $r - h$ will

be close to the pure rate of time preference. In advanced countries today, the real rate of return on capital is estimated to be between 4 and 10% per year while the growth of real output is around 3% per year, so $r-h$ is between 1 and 7% per year. In the calculations that follow, we use estimates of $(r-h)$ that are very low (either 0 or 1% per year) to reflect the possibility that the future equilibrium will come in a low- or no-growth economy with a low rate of time preference; and a case of $r-h = 4%$ per year estimate to reflect the approximate real rate of return in advanced economies today.

To calculate the optimal level of emissions reduction we perform a variational experiment. Starting from the resource steady state, consider a one-shot increase in emissions by ΔE in period 0. This will lead to an increase in concentrations in the future by $\beta \Delta E e^{-\delta t}$. In our stylised economy-climate system, this will lead to an increase in temperature of

$$\Delta T(t) = \Delta E \mu \beta \alpha [e^{-\delta t} - e^{-\alpha t}] / (\alpha - \delta) \tag{6}$$

The present and future impact upon consumption is given by:

$$\Delta c(t) = \begin{cases} y^* g'(E^*) \Delta E, & \text{for } t = 0 \\ -y^* e^{ht} \phi'(T^*) \Delta T(t) & \text{for } t > 0 \end{cases} \tag{7}$$

where $y^* g'(E^*) \Delta E$ is the increase in consumption from allowing higher emissions at time 0 and $y^* e^{ht} \phi'(T^*) \Delta T(t)$ is the damage from the higher concentrations of GHGs in the future. Starting from the reference path that is a resource steady state, with $r-h > 0$, if the original path was optimal, the present value of the change in the emissions path should be zero for small variations. This implies:

$$y^* g'(E^*) \Delta E = \int_0^\infty [y^* e^{ht} \phi'(T^*) \Delta T(t)] e^{-rt} dt$$

Using (6), some manipulation will show that this reduces to

$$g'(E^*) = \mu \beta \phi'(T^*) \alpha [1/(r+\delta-h) - 1/(r+\alpha-h)] / (\alpha - \delta) \tag{8}$$

or

$$g'(E^*) = \mu \beta \phi'(T^*) \Gamma \tag{9}$$

where $\Gamma =$ the present-value factor $= \alpha / [(r+\delta-h)(r+d-h)]$. Equations (8) and (9) state that the optimal degree of reduction of GHGs comes where the current cost of reducing GHG emissions equals the present value of the damage from higher concentrations. Γ can be interpreted as the number of years, in present value, of equilibrium-CO₂-doubling climate damage, which occurs when a one-shot concentration increase, equal to the initial CO₂ concentration, occurs at time zero. For example, say that a doubling of CO₂ in equilibrium reduces world output by 1%. Then a CO₂ emission equal to the initial concentration would produce impacts over the indefinite future whose present value is equal to Γ percent of world output. Column (2) of Table 3

Table 3
Value of present-value factor, and present value of CO₂ emissions

(1)	(2)	(3)	(4)	(5)
Difference between real interest rate on goods and growth rate ($r-h$), % per year	Present-value factor (Γ)	Present value of climate damages from CO ₂ -equivalent emissions (1989 \$ per ton CO ₂ equivalent, carbon weight) for damages as percentage of world output 2	Present value of climate damages from CO ₂ -equivalent emissions (1989 \$ per ton CO ₂ equivalent, carbon weight) for damages as percentage of world output 1 [$\mu\beta\phi'(T^*)\Gamma$]	1/4
		\$	\$	\$
0	200.0	65.94	32.97	8.24
1	44.4	14.65	7.33	1.83
4	7.41	2.44	1.22	0.31

Note: For these calculations, we assume that the lag of temperature behind GHG concentrations is $\alpha = 0.02$ (for a mean lag of 50 years), and that the rate of disappearance of GHGs is 0.005 per year (for an atmospheric residence time of 200 years).

Present-value factor in column (2) is defined in the text. Calculation of present value of climate damages is defined in the text (Section VI) and is made as follows: Damage is percent of output per year, where 1989 world output is equal to \$20,000 billion US dollars. Total CO₂ equivalent emissions in 1989 are estimated to be 8.0 billion metric tons of CO₂, carbon weight. Therefore the total damage is the present value factor from column (2) times the damage in the upper column divided by initial value of atmospheric concentrations, measured in present value of future damages per ton CO₂ equivalent emission.

shows numerical values of the present-value factor Γ for different values of the underlying parameters. To find the efficient or optimal amount of reduction of GHGs, we return to equation (9), which shows that the optimal degree of steady-state control comes where $g'(E^*) = \mu\beta\phi'(T^*)\Gamma$.

V. EMPIRICAL ESTIMATES OF THE COSTS OF SLOWING WARMING

This section presents the estimates of the costs of GHG reduction while the next estimates the damages that may arise from warming. The experiment that is conducted below examines a ‘snapshot’ of emissions, concentrations, and economic costs and damages at a point in time.⁵ They are then converted into the relevant economic magnitudes using the tools introduced in the last section. More precisely, for *impacts* we examine the consequences of doubling of the CO₂-equivalent concentrations of GHGs in the atmosphere. For the *costs* we estimate the costs of reducing the emissions of CO₂ in today’s economy. The rationale for these two snapshots is that the lag of impacts behind emissions is in the order of 30 to 80 years, so we need to understand the impacts in the future of changes in GHG emissions today.

Clearly, this economic calculation is oversimplified. First, it abstracts from the intricate economic and climatic dynamics by considering the resource steady state in which the economy is growing while the physical flows are remaining constant. Second, in extrapolating the sectoral composition of the United States economy, there are two problems with opposite signs. On the one

⁵ A preliminary analysis of a non-steady-state trajectory incorporating several regions and growth of emissions is contained in Nordhaus (1990a).

Table 4
Alternative responses to the threat of greenhouse warming

1. Slow or prevent greenhouse warming: reduce emissions and concentrations of greenhouse gases.
Reduce energy consumption
Reduce GHG emissions per unit of energy consumption or GNP
Shift to low-CO ₂ fuels
Divert CO ₂ from entering atmosphere
Shift to substitutes for CFCs
Remove greenhouse gases from atmosphere
Grow and pickle trees
2. Offset climatic effects.
Climatic engineering
Shoot particles into the stratosphere
Fertilise the ocean with trace iron
3. Adapt to warmer climate.
Decentralised/market adaptations
Movement of population and capital to new temperate zones
Corn belt migrates toward Canada and Siberia
Central/governmental policies
Build dikes to prevent ocean's invasion
Land-use regulations
Research on drought-tolerant crops

hand, the sectoral composition of developing countries is generally more resource-intensive than the United States; on the other hand, during the process of economic growth economies tend to become less resource intensive. The net effect of these two forces is unclear. Third, the calculations omit other potential market failures, such as ozone depletion or air pollution; these complementary market failures are particularly important for the CFCs, which have already been severely curbed for reasons unrelated to greenhouse warming. While these oversimplifications are necessary at this stage, they have the virtue of allowing greater transparency than would be possible in a model with full spatial and temporal resolution.

How can nations cope with the threat of greenhouse warming? Table 4 lays out some of the options. A first option, taking preventive policies to slow or prevent greenhouse warming, has received the greatest public attention. Most policy discussion has focussed on reducing energy consumption or switching to non-fossil fuels. A second option is to offset the climatic warming through climatic engineering. Among recent proposals are putting trace iron in the North Pacific and Antarctic oceans and shooting particulate matter into the stratosphere. One estimate finds that 100,000 kilograms of carbon can be offset by 1 kilogram of particles. Careful analysis of these proposals is only just beginning, but a number of cost-effective ones have already been identified. A final option is to adapt to the warmer climate. This could take place gradually on a decentralized basis through the automatic response of people, institutions, and markets as the climate warms and the oceans rise. If particular areas become unproductive, labour and capital would migrate to more productive regions. If sea level rises, settlements would gradually retreat upland unless protected. In addition, governments could take steps to pre-empt possible

harmful climatic impacts by land-use regulations or investing in research on living in a warmer climate.

In what follows, I will examine mainly the first strategy, slowing greenhouse warming through reduction of atmospheric concentrations of greenhouse gases. This option is most relevant for policy because preventive steps must be taken today while adaptive steps and climate engineering can be taken later as climate changes. Clearly, a complete policy analysis would need to investigate the entire range of responses.

There are numerous estimates of the cost of reducing GHGs, and for this purpose I present the results of a recent survey.⁶ This survey examines the cost of GHG reductions through three of the most discussed and significant strategies: (1) reducing CFC emissions, (2) reducing CO₂ emissions, and (3) increasing the carbon locked up in trees.

There are at this time more than a dozen different estimates of the costs of reducing CO₂. These often differ by a factor of two or three, although the general shapes of the cost curves are similar. The costs of CFC reduction are not terribly controversial. By contrast, the estimates of reforestation options are highly controversial and not well documented. In addition, a number of other possible options, such as treatment of methane-producing ruminants or rice paddies, are ignored here.

We show in Figure 2 the estimates of the marginal cost curve for each option and a total marginal cost curve for reducing GHGs. The curve marked ‘Marginal cost: All GHGs’ in Figure 2 is calculated as the (efficient) marginal

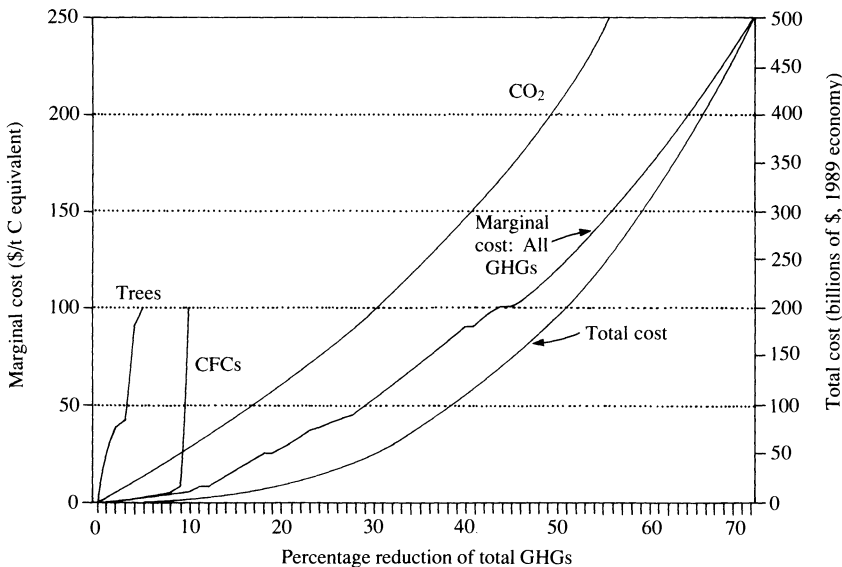


Fig. 2. Marginal and total costs of GHG reduction.

⁶ See Nordhaus (1991).

cost curve of all options. We also show the same result in terms of the *total* global cost of GHG reduction (in billions of 1989 dollars at the 1989 level of world economic activity) for different levels of reduction of GHG emissions. Columns (2) and (3) of Table 7 show our estimates of the marginal and total costs of reducing GHGs. These suggest that a modest reduction of greenhouse gas emissions can be obtained at low cost. After 10% reduction, however, the curve rises as more costly measures are required. A 50% reduction in GHG emissions is estimated to cost almost \$200 billion per year in today's economy, or around 1% of world output. This estimate is understated to the extent that the implementing policies are inefficient or that they are implemented in a crash program.

VI. ESTIMATING THE DAMAGES FROM GREENHOUSE WARMING

We now move from the *terra infirma* of climate change to the *terra incognita* of the social and economic impacts of climate change. Studies of the impacts of climate change are in their infancy, and at this stage we can only hope to obtain an order-of-magnitude estimate of impact of greenhouse warming upon the global economy. Before presenting the estimates, two points should be noted. First, it must be recognised that human societies thrive in a wide variety of climatic zones. For the bulk of economic activity, non-climate variables like labour skills, access to markets, or technology swamp climatic considerations in determining economic efficiency. Second, although this analysis focuses primarily upon globally averaged surface temperature, this variable is chosen because it is a useful *index* (in the nature of a sufficient statistic) of climate change that tends to be associated with most other important changes rather than because it is the most important factor in determining impacts.

Table 5 shows a sectoral breakdown of United States national income, where the economy is subdivided by the sectoral sensitivity to greenhouse warming. The most sensitive sectors are likely to be those, such as agriculture and forestry, in which output depends in a significant way upon climatic variables. At the other extreme are activities, such as cardiovascular surgery or microprocessor fabrication in 'clean rooms', which are undertaken in carefully controlled environments that will not be directly affected by climate change. Our estimate is that approximately 3% of United States national output is produced in highly sensitive sectors, another 10% in moderately sensitive sectors, and about 87% in sectors that are negligibly affected by climate change. In the damage estimates that follow, we will make the simplifying assumption that the damage applies to world GNP in 2050, and that the composition of 2050 world GNP is the same as United States GNP in 1981. Table 6 presents a rough set of estimates of the impact of greenhouse warming upon United States national income. The major findings are:

□ Most studies suggest that greenhouse warming will lower yields in agriculture. This impact is, however, offset by the fertilisation effect of higher levels of CO₂. An assessment in the EPA report (1988) finds an overall impact

Table 5
Breakdown of economic activity by vulnerability to climatic change, U.S. 1981

Sector	National income	
	Value (billions)	Percentage of total
Total national income	2415.1	100.0
Potentially severely impacted		
Farms	67.1	2.8
Forestry, fisheries, other	7.7	0.3
Moderate potential impact		
Construction	109.1	4.5
Water transportation	6.3	0.3
Energy and utilities		
Energy (electric, gas, oil)	45.9	1.9
Water and sanitary	5.7	0.2
Real estate		
Land-rent component	51.2	2.1
Hotels, lodging, recreation	25.4	1.1
Negligible effect		
Manufacturing and mining	627.4	26.0
Other transportation and communication	132.6	5.5
Finance, insurance, and balance real estate	274.8	11.4
Trade and other services	674.6	27.9
Government services	337.0	14.0
Rest of world	50.3	2.1

Sources and notes: Data are based on the United States National Accounts, *Survey of Current Business*, July 1984.

on all crops for the United States is plus or minus \$10 billion, with the difference between these estimates arising from the magnitude of the climate change.

□ There is great uncertainty about the impact of climate change upon sea-level change. Recent scientific views are in the range of 30 to 60 cm over the next century. EPA (1988) estimates the cost of a 50 cm sea-level rise for the United States will fall in three categories: land loss of around 4000 square miles, protection costs (by levees and dikes) of high-value property, and miscellaneous protection of open coasts. The total capital value is in the order of \$50 billion, which is approximately 0.05% of projected cumulative gross private domestic investment over the period 1985–2050.

□ Many other sectors are likely to be affected, although numerical estimates of the effects are incomplete. Greenhouse warming will increase the demand for space cooling and decrease the demand for space heating, with but a small net impact on the energy sector. The forest products industry may benefit from CO₂ fertilisation. Water systems (such as runoff in rivers or the length of ice-free periods) may be significantly affected, but the costs are likely to be determined more by the rate of climate change than the new equilibrium climate. Construction in temperate climates will be favourably affected because of a longer period of warm weather. For recreation and water transportation, the outlook is mixed depending upon the initial climate. Cold

regions may gain while hot regions may lose; investments in water skiing will appreciate while those in snow skiing will depreciate. But for the bulk of the economy – manufacturing, mining, utilities, finance, trade, and most service industries – it is difficult to find major direct impacts of the projected climate changes over the next 50 to 75 years.

□ A wide variety of non-marketed goods and services escape the net of the national income accounts and might affect the calculations. Among the areas of importance are human health, biological diversity, amenity values of everyday life and leisure, and environmental quality. I am aware of no studies that point to major costs, but further analysis will be required to determine whether these omitted sectors will significantly affect the assessment of the cost of greenhouse warming. An important area for future research is to use broader measures of national output, such as those in Nordhaus and Tobin (1972) and Eisner (1985), to determine whether the conclusions for the market sector would be modified. One particular area of importance is the amenities of everyday life; one thorough study suggests major amenity benefits from global warming.⁷

The overall assessment of the cost of greenhouse warming in the United States is shown in the bottom of Table 6. We estimate that the net economic

Table 6
Impact estimates for different sectors, for doubling of CO₂, U.S. (positive number indicates gain; negative number loss)

Sectors	Billions (1981 \$)
Severely impacted sectors	
Farms	
Impact of greenhouse warming and CO ₂ fertilisation	– 10.6 to +9.7
Forestry, fisheries, other	Small + or –
Moderately impacted sectors	
Construction	+
Water transportation	?
Energy and utilities	
Energy (electric, gas, oil)	
Electricity demand	– 1.65
Non-electric space heating	1.16
Water and sanitary	–?
Real estate	
Land-rent component	
Estimate of damage from sea level rise	
Loss of land	– 1.55
Protection of sheltered areas	– 0.90
Protection of open coasts	– 2.84
Hotels, lodging, recreation	?
Total	
Central estimate	
Billions, 1981 level of national income	– 6.23
Percentage of national income	– 0.26

Sources for Table 6: Underlying data on impacts are summarised in EPA (1988). Translation into national-income accounts by author. Details are available on request.

⁷ See National Research Council (1978).

damage from a 3° warming is likely to be around $\frac{1}{4}\%$ of national income for the United States in terms of those variables we have been able to quantify. This figure is clearly incomplete, for it neglects a number of areas that are either inadequately studied or inherently unquantifiable. We might raise the number to around 1% of total global income to allow for these unmeasured and unquantifiable factors, although such an adjustment is purely *ad hoc*. It is not possible to give precise error bounds around this figure, but my hunch is that the overall impact upon human activity is unlikely to be larger than 2% of total output.

A full assessment of the impact of greenhouse warming must, of course, include regions outside the United States. To date, studies for other countries are fragmentary, and it is not possible to make any firm conclusions at this time. A preliminary reading of the evidence is that other advanced industrial countries will experience modest impacts similar to those of the United States. On the other hand, small and poor countries, particularly ones with low population mobility in narrowly restricted climatic zones, may be severely affected. Much more work on the potential impact of climate change on developing countries needs to be done.

These remarks lead to a surprising conclusion. Climate change is likely to produce a combination of gains and losses with no strong presumption of substantial net economic damages. This is not an argument in favour of climate change or a *laissez-faire* attitude to the greenhouse effect. Rather, it suggests that a careful weighing of costs and damages will be necessary if a sensible strategy is to be devised.

VII. AN EFFICIENT POLICY FOR SLOWING GREENHOUSE WARMING

We can now provide estimates of an efficient policy for slowing greenhouse warming,⁸ where this is described in equations (7) through (9). In this analysis, we assume a baseline in which there are no greenhouse policies in place. This approach is taken because few countries have actually decided upon their greenhouse policies and because we are attempting to determine a 'zero-base', most efficient policy.

We begin by tabulating in Table 7 the calculated costs and damages that are drawn from the findings above. Column (1) shows the percentage reduction in GHGs from an uncontrolled level. Columns (2) and (3) show the costs of GHG reductions from Figure 2. The final column displays the estimated total discounted damages associated with the given level of reduction of GHG emissions, this figure being derived from the estimates in Table 3.

The efficient level of GHG reduction is shown in Table 7 for the middle level of damages and for a discount rate that is 1% above the growth rate (that is,

⁸ In order to make the damage estimates comparable with the cost estimates, we need to put them into the same units. The conversion is made using the analysis of section IV. Recall that the present value of damages from a unit of GHG emissions is given by the relationship that marginal damage per unit of GHG emission = $\mu\beta\phi'(T^*)\Gamma\Delta E$, where the variables are defined in section (IV). Table 3 shows alternative estimates of the damage from CO₂-equivalent emissions for different values of the discount rate and the damage function.

Table 7
Calculation of costs and benefits for different levels of reduction of greenhouse gas emissions

(1) Reduction of GHG emissions (as percentage of base level)	(2) Marginal cost of reduction (\$ per t C)	(3) Total cost of reduction (\$ billion/yr)	(4) Total benefit of reduction (\$ billion/yr)
0	0.0	0.0	0.0
1	0.5	0.04	0.6
2	1.0	0.12	1.2
3	1.5	0.24	1.8
4	2.0	0.40	2.4
5	2.6	0.61	3.0
10	5.3	2.2	5.9
* 11	8.0	2.9	6.5
15	16.3	6.8	8.9
20	28.0	16.3	11.9
25	40.2	30.7	14.8
30	53.3	49.5	17.8
40	89.9	108.0	23.7
50	120.0	191.0	29.6
60	171.0	309.0	35.6
75	285.0	581.0	44.4

* Most efficient level of control of GHG emissions for medium damage level.

Source: For both costs and benefits, calculations use 1989 levels of world greenhouse gas emissions and world output. Cost estimates shown in Fig. 3. Estimates of benefits assume parameters given in Table 3.

$r-h = 0.01$ per year). This estimate corresponds to the middle damage estimate in column (4) of Table 3 of \$7.33 per ton of CO₂ equivalent. Equating the marginal damage with the marginal cost leads to an efficient level of control, shown with the asterisk in Table 7, of 11% of GHG emissions. At the efficient control level, the total cost of reducing emissions is around \$3 billion per year while the total benefit is estimated to be around \$6 billion per year.

The same outcome is illustrated in Figure 3, which puts together the empirical marginal costs and damage curves. The horizontal axis shows the reduction in GHGs. The curve marked 'MC: All GHGs' is our estimate of the marginal cost of GHG reduction shown in Figure 2. The horizontal curves marked Low, Medium, and High Damage correspond to damage estimates in Table 3 of \$1.83, \$7.33, and \$66 per ton of CO₂ equivalent. The low, medium, and high damage curves are, respectively, (i) economic costs actually identified in this study ($\frac{1}{4}$ % of total output), (ii) the costs raised to 1 percentage point to allow for a significant amount of potential unmeasured damage, and (iii) an estimate of 2% to allow for maximum plausible damages. The first two figures use the middle discount rate of $(r-h)$ equal to 1%, while the third uses a value of $r-h$ of 0.

The efficient policy is found at the intersection of the relevant damage curve with the marginal cost curve. The medium case was shown in Table 7 and leads to a current reduction of 11% of GHG emissions. At the low damage estimate,

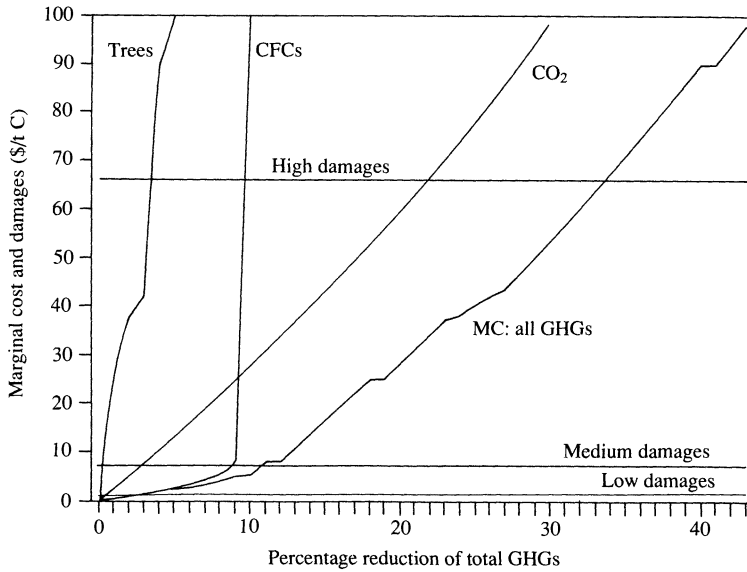


Fig. 3. Marginal cost and damages.

there is very little GHG emission reduction for its own sake. At the extreme end of the high damage estimate, about one-third of total GHG emissions would be reduced.

The same figure also presents the results for the high and medium policies in a manner that allows us to determine the contribution of different GHGs to the total reduction. For the medium damage estimate, the efficient policy totals about 11% reduction in CO₂-equivalent emissions. Of this virtually none comes from trees, 2% from the reduction of CO₂, and 9% comes from the reduction in CFC emissions. All options suggest a significant reduction in the use of CFCs and that little can be realised through forestry options. The main difference among the policies is the extent to which CO₂ emissions are reduced.⁹

VIII. CONCLUSIONS

The present study has investigated strategies for coping with the likelihood of significant greenhouse warming over the coming century. It has focussed primarily upon data based on the United States and extrapolated to the rest of the world. The principal conclusions are as follows.

First, an efficient strategy for coping with greenhouse warming must weigh the costs and benefits of different policies. We have surveyed the economic literature on the costs of abatement and the damages from greenhouse warming. Estimates of both costs and damages are highly uncertain and

⁹ This study assumes that damages are linear in concentrations; this assumption makes the optimal policy independent of the steady-state concentrations. A more plausible approach, for which there is some evidence, would be that increases in marginal damages are rising in the extent and rate of climate change. If the damage function is quadratic, then the marginal damage would be proportional to concentrations. The estimates in this paper are then easily adjusted by multiplying the damage estimates in columns (3) to (5) of Table 3 by the ratio of steady-state temperature increase to the CO₂-doubling temperature increase.

incomplete, and our estimates are therefore highly tentative. We investigate the impact of climate change coming from an equilibrium doubling of CO₂-equivalent atmospheric concentrations, which we take to be a 3 °C rise in global mean surface temperature along with the associated changes in climate. The flow of damages identified from this climate change is estimated to be about $\frac{1}{4}$ % of output for today's United States economy. There are clearly unmeasured and unmeasurable impacts, which might raise this impact to 1%, or at most 2% of total global output, although these higher figures are no more than an informed hunch.

Second, we examined three different policy measures (reducing CO₂ emissions, CFC reduction, and afforestation), and have calculated an overall marginal cost of GHG reduction. We find that about 10% of GHG emissions can be reduced at extremely low cost; above that level, the marginal cost of abatement rises sharply. Using today's economy as a base, the long-run marginal cost of reducing GHG emissions is estimated to be \$40 per ton C for a 25% reduction and \$120 per ton for a 50% reduction. The total global costs of these reductions are about \$2 billion per year for a 10% reduction, \$31 billion for a 25% reduction, and \$191 billion per year for a 50% reduction.

Third, putting together our marginal cost and marginal damage schedules, we can calculate the efficient greenhouse policy. For the low damage function – which includes only identified costs and uses a middle discount rate – we estimate the marginal damage of greenhouse gases to be about \$1.83 per ton of C in CO₂ equivalent, which suggests very little CO₂ abatement. For the medium damage function, which assumes damage from greenhouse warming of 1% of GNP, the cost is reckoned at \$7.33 per ton carbon; in this case, the efficient reduction is 11% of total GHG emissions. In this case, CFCs are substantially reduced, and CO₂ emissions are reduced by about 2%. In the high damage case, with damages taken to be 2% of total output and with no discounting, GHG emissions are reduced by about one-third.

Fourth, the appropriate level of control depends critically upon three central parameters of the climate-economic system: the cost of control of GHGs, the damage to the human societies from greenhouse warming, and the time dynamics as reflected in the rate of discount of future goods and services along with the time lags in the reaction of the climate to emissions. The efficient degree of control of GHGs would be essentially zero in the case of high costs, low damages, and high discounting; by contrast, in the case of no discounting and high damages, the efficient degree of control is close to one-third of GHG emissions.

Finally, it should be emphasised that this analysis has a number of important oversimplifications. It simplifies enormously many of the intricate economic and climatic complexities by taking a global view of economic activity and a simple dynamic specification of emissions, concentrations, and economic growth. It also bases the economic damage assumptions upon the 1981 sectoral composition of the United States economy and assumes that this composition will hold for the global economy in the mid-21st century. In addition it ignores other routes for investing society's resources – such as factories, education,

research, and health – and focusses on a single tradeoff between future and present consumption. Moreover, the calculations omit other potential market failures, such as ozone depletion or air pollution, which might reinforce or weaken the logic behind greenhouse gas reduction. And finally, it ignores the issues of uncertainty, in which risk aversion and the possibility of learning may modify the stringency and timing of control strategies.

Notwithstanding these simplifications, the approach laid out here may help clarify the questions and help identify the scientific, economic, and policy issues that must underpin any rational decision. Once the fundamental concepts are clear, it is relatively straightforward to move to a more detailed disaggregated approach so as to fine tune the calculations. But whether we use simple approaches like the present one or more elaborate models, we must balance costs and damages if we are to preserve our precious time and resources for the most important threats to our health and happiness.

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