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# Input-Reflectionless Low-Pass Filter on Multilayered Diplexer-Based Topology

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**Abstract**—A class of input-reflectionless low-pass filter (LPF) using a multilayered diplexer-based architecture is presented. It consists of two signal-transmission parts: (i) a reflective-type LPF network built with an open-ended microstrip resonator and a shunt microstrip section, and (ii) a resistively-terminated wideband microstrip-to-microstrip vertical transition. Thus, based on the in-band transmission poles of the wideband transition at which the RF-input-signal energy not transmitted by the LPF part is dissipated by the terminating 50-Ω resistor, a higher-selectivity LPF response with broadband reflectionless behavior is attained. To further increase the stopband bandwidth, as well as the attenuation levels and cut-off-slope sharpness, in-series-cascaded multi-LPF-unit designs are engineered. The main RF operational principles and theoretical design examples of the proposed input-reflectionless LPF approach are detailed. Moreover, for practical-validation purposes, a two-layered two-LPF-unit microstrip prototype with extended stopband and broadband input-reflectionless characteristics is designed, fabricated, and tested.

**Index Terms**—Absorptive filter, diplexer-based circuit, input-reflectionless filter, low-pass filter (LPF), microstrip filter, multilayered circuit, vertical transition, wideband filter.

## I. INTRODUCTION

TO ELIMINATE the harmful effects of undesired RF input-signal power reflections in order to assure the robust operation of preceding microwave active circuits, RF absorptive/reflectionless filters are attracting a large interest in practical designs [1]. When compared to traditional reflective-type filters, the non-transmitted RF-input-signal energy at the stopband regions is expected to be fully dissipated inside the absorptive filter instead of being reflected back to the source [2]. Thus, a variety of reflectionless filtering components based on different design methods have been recently proposed, such as low-pass filters (LPFs), single-/multi-passband filters, filtering power dividers, and diplexers [3]–[15]. Regarding reflectionless LPFs, most of the experimental prototypes developed in [3]–[6], [11],

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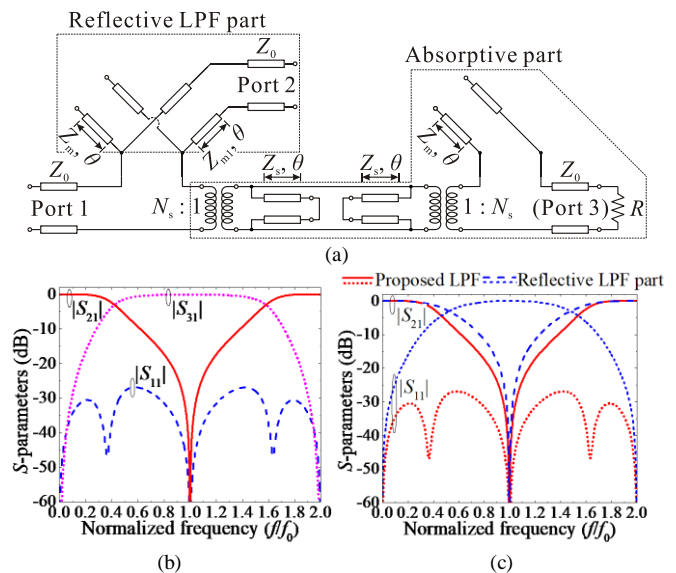


Fig. 1. Proposed input-reflectionless LPF. (a) Diplexer-based equivalent circuit using the resistively-terminated wideband microstrip-to-microstrip vertical transition in [16] when  $Z_m = 31.7 \Omega$ ,  $Z_s = 91.3 \Omega$ ,  $Z_{m1} = 78.1 \Omega$ ,  $N_s = 1$ , and  $R = 50 \Omega$ . (b) Theoretical power transmission ( $|S_{21}|$ ) and input-reflection ( $|S_{11}|$ ) responses of the diplexer-based network without the  $R$  resistor at port 3. (c) Theoretical  $|S_{21}|$  and  $|S_{11}|$  of the input-reflectionless LPF.

and [12] are mainly designed with lumped-element networks and suffer from one or several of the following drawbacks: (i) large in-band power-insertion-loss levels, (ii) lack of multiple stopband power transmission poles in the absorptive-circuit part to attain a broadband reflectionless behavior, (iii) difficult scaling to higher frequency ranges, and (iv) high sensitivity to deviations in the lumped-element component values.

This letter presents input-reflectionless diplexer-based LPFs and their application to realize multi-LPF-unit designs with extended absorptive-stopband bandwidth and/or attenuation levels. The equivalent circuit of the engineered multilayered absorptive LPF is derived from the reflectionless wideband bandpass filters discussed in [15]. To the best of the authors' knowledge, this is the first time that two-layered microstrip-to-microstrip vertical transitions are applied to the development of absorptive/reflectionless LPFs. The theoretical foundations and RF operational principles of the proposed diplexer-based input-reflectionless LPF architecture are detailed. Furthermore, for practical-validation purposes, a microstrip two-LPF-unit prototype with stopband attenuation above 18.5 dB from 3.06 GHz to 14.3 GHz and input-power-matching levels higher than 10 dB from DC to 11.9 GHz is manufactured and characterized.

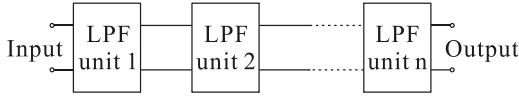


Fig. 2. Block diagram of the proposed extended-stopband input-reflectionless multi-LPF-unit network based on the in-series cascade of  $n$  LPF units as in Fig. 1(a) for  $Z_m = 31.7 \Omega$ ,  $Z_s = 91.3 \Omega$ ,  $Z_{m1} = 78.1 \Omega$ ,  $N_s = 1$ , and  $R = 50 \Omega$ .

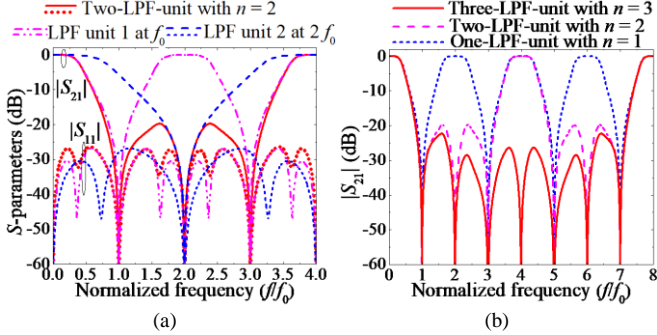


Fig. 3. Theoretical power transmission ( $|S_{21}|$ ) and input-reflection ( $|S_{11}|$ ) responses of the proposed extended-stopband input-reflectionless multi-LPF-unit network. (a) Two-LPF-unit design with transmission-zero frequencies at  $f_0$  and  $2f_0$  for its building LPF units. (b) Multi-LPF-unit designs for  $n = 1, 2, 3$ .

## II. THEORY, ANALYSIS, AND DESIGN

### A. Diplexer-Based LPF Network

Fig. 1(a) depicts the equivalent circuit of the proposed input-reflectionless LPF. As shown, it is composed of two signal-transmission parts: (i) a reflective-type single-pole LPF shaped by an open-ended stub and a shunt transmission-line section and (ii) a wideband microstrip-to-microstrip vertical transition as in [16] terminated by a resistor at the output port (port 3) to dissipate the RF-input-signal energy not transmitted by the LPF part at its stopband range. Here, the open-ended stubs, the short-ended stubs, and the transmission-line section are set with the same electrical length  $\theta$ —quarter-wavelength-long at  $f_0$  as the stopband transmission-zero frequency of the reflective-type LPF—but different line impedances ( $Z_m$ ,  $Z_s$ , and  $Z_{m1}$ ).  $Z_0$  is the  $50\text{-}\Omega$  port impedance and  $R$  is the resistance of the terminating resistor. Due to the existing end effect on the impedance variation of the slotline resonator in practice, two transformers with turns ratios of  $N_s$  are employed to account for it [16].

The operational principle of the devised LPF, initially assumed to be lossless with  $N_s = 1$ , is next detailed. By removing the terminating resistor at port 3, the wideband  $2f_0$ -frequency-periodic bandpass-type response of the vertical transition (with the specified in-band ripple factor of  $0.002 \text{ dB}$  and phase of  $53.785^\circ$  at the lower cut-off frequency of  $0.598f_0$  or  $Z_m = 31.7 \Omega$  and  $Z_s = 91.3 \Omega$  [16]) is firstly calculated with transmission zeros occurring at  $0, 2f_0, \dots, 2Nf_0$  and transmission poles at  $f_0, 3f_0, \dots, (2N+1)f_0$  ( $N$  is a natural index). Note that two additional sets of transmission poles around  $f_0, 3f_0, \dots, (2N+1)f_0$  are generated when  $z_m z_s > 1$  ( $z_m$  and  $z_s$  are the normalized-to- $Z_0$  line impedances). Thus, the reflective-type first-order LPF part with its first transmission zero at  $f_0$  is designed. Meanwhile,  $Z_{m1} = 78.1 \Omega$  is properly selected to maintain the power matching level  $|S_{11}| \leq -20 \text{ dB}$  within the frequency range  $[0, 2f_0)$  [15]. With these impedance values, the theoretical  $2f_0$ -frequency-periodic frequency responses of the diplexer network are obtained within the frequency range  $[0, 2f_0)$ , as shown in Fig. 1(b). In this

manner, as the terminating resistor  $R = 50 \Omega$  nearly consumes the non-transmitted RF-input-signal energy in the stopband range of the reflective-LPF part (full dissipation at  $f_0, 3f_0, \dots, (2N+1)f_0$ ) and owing to three in-band transmission poles of the wideband transition within  $[0, 2f_0)$ , both a high-selectivity lowpass-filtering-type transmission response and input-power-matching levels above  $25 \text{ dB}$  in a broad band are attained for the devised LPF, as proven in Fig. 1(c). Furthermore, the cut-off frequency of this absorptive LPF is increased for higher values of  $Z_m$  and/or lower values of  $Z_s$ , just in an opposite trend as the passband bandwidth of its wideband-vertical-transition part as discussed in [16].

### B. Multi-LPF-Unit Designs with Extended Stopband

To realize an input-reflectionless low-pass filtering response with extended upper stopband, multiple LPF units as the one in Fig. 1 with spectrally-adjacent attenuated bands can be in-series cascaded as in [17], as shown in Fig. 2. Specifically, the in-series-cascaded LPF units of this multi-LPF-unit approach are designed with  $\theta = 90^\circ$  at different frequencies of their first transmission zero—i.e.,  $f_0, 2f_0, 4f_0, \dots, 2^{n-1}f_0$ , respectively. In this manner, the spectral locations of the out-of-band transmission zeros within its first attenuated band of the overall  $2^n f_0$ -frequency-periodic multi-LPF-unit network realized with  $n$  in-series-cascaded LPF units are  $f_0, 2f_0, 3f_0, \dots, (2^n - 1)f_0$ .

From the above, it is derived that the first stopband of the input-reflectionless multi-LPF-unit network in Fig. 2 can be extended beyond  $(2^n - 1)f_0$ , which is its upper out-of-band transmission-zero frequency. This is due to the joint action of the transmission zeros of its  $n$  building in-series-cascaded first-order LPF units. For illustration purposes, the theoretical power transmission and reflection responses of a two-LPF-unit example (i.e.,  $n = 2$  so that it is  $4f_0$ -frequency-periodic) and its constituent LPF units with transmission zeros at  $f_0$  and  $2f_0$  are drawn in Fig. 3. As shown in Fig. 3(a), based on the predicted transmission zeros, a stopband with attenuation levels above  $20 \text{ dB}$  up to more than  $3f_0$  for the proposed two-LPF-unit network is obtained. Also, owing to the input-absorptive property of the proposed LPF, the input-reflectionless response of the overall two-LPF-unit circuit remains almost the same when compared to the one of the LPF unit 1. Fig. 3(b) compares the out-of-band responses of the multi-LPF-unit networks designed with  $n = 1, 2$ , and  $3$ , respectively. As shown, the first upper stopband of the  $8f_0$ -frequency-periodic three-LPF-unit circuit can be extended beyond  $7f_0$ , which verifies the devised design strategy in Fig. 2.

## III. IMPLEMENTATION AND DISCUSSION

To validate the experimental viability of the proposed input-reflectionless LPF based on a two-layered diplexer-type structure, a two-LPF-unit circuit with extended stopband up to above  $3f_0$  ( $f_0 = 4 \text{ GHz}$ ) as in Section II.B has been designed, manufactured, and tested. The Roger's 4003C substrate with relative dielectric constant  $\epsilon_r = 3.55$ , dielectric thickness  $h = 0.508 \text{ mm}$ , metal thickness  $t = 35 \mu\text{m}$ , and dielectric loss tangent  $\tan(\delta_D) = 0.0027$  is employed. Fig. 4 depicts the layout as well as the side-view structure of the conceived two-LPF-unit prototype, in which the open-ended stubs, the short-ended stubs, and the cascaded transmission-line sections in Fig. 1 are respectively realized as open-ended microstrip resonators,

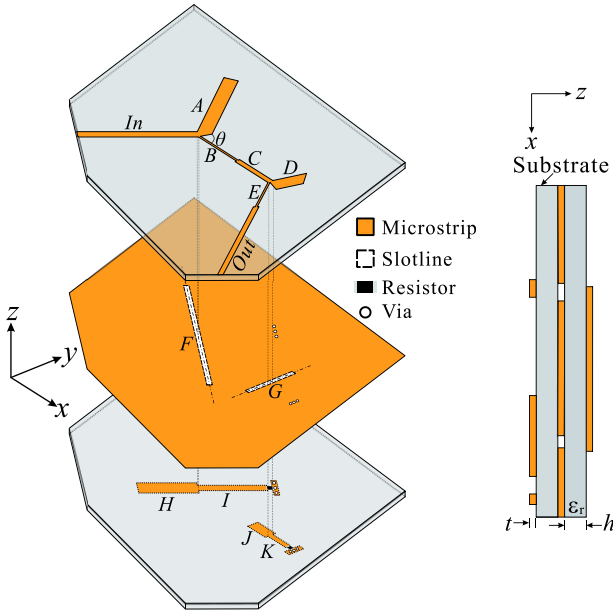


Fig. 4. Layout and side-view structure of the devised input-reflectionless two-LPF-unit prototype using two in-series-cascaded LPF units with different transmission-zero frequencies at 4 GHz and 8 GHz ( $L_{In} = 40$ ,  $L_{Out} = 15$ ,  $L_A = 8.44$ ,  $L_B = 9.9$ ,  $L_C = 7$ ,  $L_D = 3.15$ ,  $L_E = 4.45$ ,  $L_F = 24.4$ ,  $L_G = 12.4$ ,  $L_H = 9.7$ ,  $L_I = 6$ ,  $L_J = 3.88$ ,  $L_K = 4$ ,  $W_{In} = W_{Out} = W_C = W_I = W_K = 1.1$ ,  $W_A = W_D = W_H = W_J = 2.6$ ,  $W_B = W_E = 0.43$ ,  $W_F = 0.5$ ,  $W_G = 0.38$ ,  $h = 0.508$ ,  $t = 0.035$  (unit: mm) and  $\theta = 120^\circ$ ).

slotline resonators, and cascaded microstrip-line sections. As described in Section II.B, the in-series-cascaded LPF units of this devised two-LPF-unit prototype are initially designed with  $Z_m = 31.7 \Omega$ ,  $Z_s = 91.3 \Omega$ ,  $Z_{m1} = 78.1 \Omega$ , and  $N_s = 1$ , but different transmission-zero frequencies at 4 GHz ( $f_0$ ) and 8 GHz ( $2f_0$ ). Nevertheless, due to the previously-mentioned end effect on the impedance variation of the slotline resonators in electromagnetic (EM) simulation, the impedance values of the  $Z_s$  parameters for the two employed LPF units are properly modified with  $Z_{s,1} = 109.03 \Omega$  and  $Z_{s,2} = 116.61 \Omega$  to make the EM-simulated responses fairly meet the theoretical ones. In this manner, the turns ratios of the employed transformers for these two LPF units are determined as  $N_{s,1} = 0.914$  and  $N_{s,2} = 0.885$  [16]. Moreover, two 50- $\Omega$  surface-mounted-device resistors with practically-measured resistances of 51.2  $\Omega$  and 51.6  $\Omega$  are soldered on the bottom layer. On the other hand, in order to avoid the coupling effect coming from the slotlines and the top-layer microstrip lines on the stopband power matching levels, the physical lengths of the 50- $\Omega$  microstrip lines connected with the resistors were carefully adjusted in the design process.

The theoretical, EM-simulated, and measured results of the manufactured two-LPF-unit prototype are depicted in Fig. 5(a). As shown, apart from some minor deviations observed in the upper spectral region of the measured input-power-reflection parameter that are mainly attributed to the frequency-dispersive nature of the substrate, the discontinuous effect of the SMA connectors, the influence of the packaging of the SMD resistors at high frequencies, and fabrication tolerances, a reasonably-close agreement among these frequency responses is obtained. The main performance metrics of the measured circuit are as follows: 1-dB bandwidth from DC to 1.31 GHz, first transmission-zero frequency at 3.97 GHz, 3-dB cut-off frequency of 1.73 GHz, stopband attenuation better than 18.5

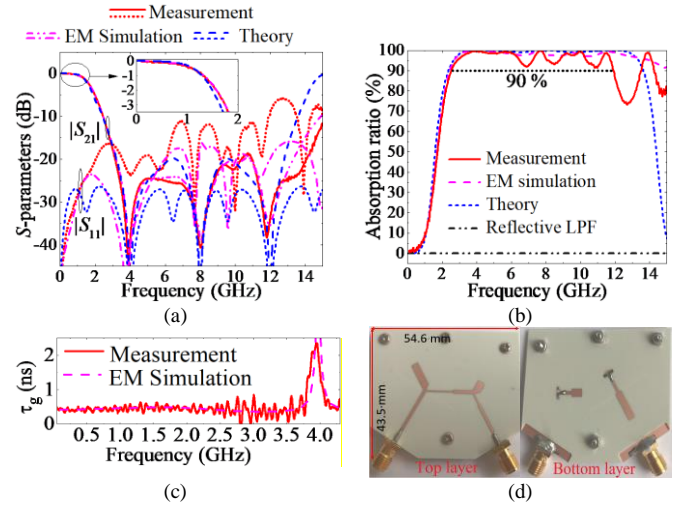


Fig. 5. Manufactured input-reflectionless two-LPF-unit microstrip prototype with layout in Fig. 4. (a) Theoretical, EM-simulated, and measured power transmission ( $|S_{21}|$ ) and input-reflection ( $|S_{11}|$ ) responses. (b) Simulated and measured input-power-absorption ratios (i.e.,  $100 \times (1 - |S_{21}|^2 - |S_{11}|^2)$  (%)). (c) Simulated and measured in-band group-delay ( $\tau_g$ ) responses. (d) Photographs of the assembled LPF prototype with size of  $54.6 \times 43.5 \text{ mm}^2$  or  $0.52\lambda_g \times 0.42\lambda_g$ , where  $\lambda_g$  is the effective guided wavelength at the measured cut-off frequency.

TABLE I  
COMPARISON WITH OTHER PRIOR-ART INPUT-REFLECTIONLESS LPFS

Ref.	1-dB BW (GHz)	RR(GHz)/RL (dB)	SS (GHz)	DT
[3]	DC–0.1	DC–1/≥ 12	0.3–1 (53 dB)	LE
[4] LPF in Fig. 20	DC–0.7	DC–5/≥ 16	1.3–5 (18 dB)	MMIC
[11] LPF in Fig. 17	DC–0.008	DC–0.08/≥ 18	0.01–0.08 (14 dB)	LE
This Work	DC–1.31	DC–11.86/≥ 11.21	3.06–14.3 (18.5 dB)	MS

BW: bandwidth; RR: reflectionless range; RL: return loss; SS: stopband suppression; DT: design technology; LE: lumped element; MMIC: monolithic microwave integrated circuit; MS: microstrip.

dB from 3.06 GHz to 14.3 GHz, and input-power- matching levels above 11.21 dB from DC to 11.86 GHz. Figure 5(b) plots the simulated and measured power-absorption ratios of this LPF. Compared to its reflective-type LPF part, an out-of-band power-absorption ratio above 90% for this LPF prototype is measured from 2.47 GHz to 11.95 GHz (i.e., 7.24 times the 1-dB bandwidth), which means a broad-band input-reflectionless property. The measured maximum in-band group-delay variation is 0.21 ns as depicted in Fig. 5(c), and Fig. 5(d) shows the top- and bottom-layer photographs of this assembled LPF prototype. Furthermore, a detailed comparison between the developed input-absorptive LPF prototype of this work and other prior-art reflectionless LPFs is given in Table I.

#### IV. CONCLUSION

A class of two-layered input-reflectionless diplexer-based LPF is reported in this letter. By using a resistively-terminated wideband microstrip vertical transition by the first time for this application, an input-reflectionless response for the conceived LPF device is realized. The RF operational foundations and theoretical examples of this input-reflectionless LPF design approach have been shown and experimentally verified with the development and characterization of a two-LPF-unit microstrip prototype with extended reflectionless stopband.

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