## Quantum hydrogen-bond symmetrization in the superconducting hydrogen sulfide system

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Hydrogen compounds are peculiar in that the 20 <sup>21</sup> quantum nature of the proton can crucially affect their structural and physical properties. A re-22 markable example is the high-pressure phases [1, 23 24 2] of  $H_2O$ , where quantum proton fluctuations favor symmetrization of the H bond and lower by 25 30 GPa the boundary between asymmetric and 26 27 symmetric structures [3]. Here we show that an analogous quantum symmetrization occurs in 28 the recently discovered [4] sulfur hydride super-29 conductor with a record superconducting critical temperature  $T_c = 203$  K at 155 GPa. Supercon-31 32 ductivity occurs via formation of a structure of <sup>33</sup> stoichiometry  $H_3S$  with S atoms arranged on a body-centered-cubic (bcc) lattice [5–9]. If the H 35 atoms are treated as classical particles, then for  $_{36} P \gtrsim 175$  GPa they are predicted to sit midway  $_{37}$  between two S atoms in a structure with  $Im\bar{3}m$ symmetry. At lower pressures the H atoms move 38 to an off-center position forming a short H-S co-39 valent bond and a longer  $H \cdots S$  hydrogen bond 40 in a structure with R3m symmetry [5–9]. X-ray 41 <sup>42</sup> diffraction experiments confirmed the H<sub>3</sub>S stoi-<sup>43</sup> chiometry and the S lattice sites, but were unable <sup>44</sup> to discriminate between the two phases [10]. Our <sup>45</sup> present *ab initio* density-functional theory (DFT) 46 calculations show that quantum nuclear motion <sup>47</sup> lowers the symmetrization pressure by 72 GPa  $_{48}$  for H<sub>3</sub>S and by 60 GPa for D<sub>3</sub>S. Consequently, we predict that the  $Im\bar{3}m$  phase dominates the <sup>50</sup> pressure range within which a high  $T_c$  was mea-<sup>51</sup> sured. The observed pressure-dependence of  $T_c$ <sup>52</sup> is closely reproduced in our calculations for the  $_{53}$  Im3m phase, but not for the R3m phase. Thus, 54 the quantum nature of the proton fundamentally

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FIG. 1. Crystal structures of the competing phases. Crystal structure in the conventional bcc cell of the R3m and  $Im\bar{3}m$  phases. In the R3m structure the H-S covalent bond of length  $d_1$  is marked with a solid line and the longer  $H \cdots S$  hydrogen bond of length  $d_2$  with a dotted line. In the  $Im\bar{3}m$  phase  $d_1 = d_2$ . In the  $Im\bar{3}m$  structure we mark the lattice parameter a.

## $_{^{55}}$ changes the superconducting phase diagram of $_{^{56}}$ $\mathrm{H}_3\mathrm{S}.$

The discovery of high-temperature superconductivity in compressed hydrogen sulfide [4] has generated intense interest over the last year, and has led to a number of theoretical studies aimed at understanding the phase diagram of the H-S system as well as the origin of the astonishingly high  $T_c$  observed [5–9, 12–18]. The overall consensus is that H<sub>2</sub>S, the only stable compound formed by hydrogen and sulfur at ambient conditions, is metastable at high pressures and its decomposition gives rise to several H-S compounds. High- $T_c$  superconductivity is believed to occur in a structure of H<sub>3</sub>S stoichiometry, and is considered to be conventional in nature, i.e., mediated by electron-phonon interactions [4, 5, 7, 9, 12–17]. Alternatives to conventional superconductivity have also been



FIG. 2. Energetics.  $E_{\rm BO}$ ,  $E_{\rm vib}$ , and  $E = E_{\rm vib} + E_{\rm BO}$ curves are shown as a function of the reaction coordinate Q that transforms the  $Im\bar{3}m$  structure (Q = 0) into the R3m structure (Q = 1), as well as the relative coordinate x that measures the off-centering of the H atoms, defined as  $x = (d_2 - a/2)/(a/2)$ , where  $d_2$  is the length of the hydrogen bond and a the lattice parameter (see Fig. 1). The left-hand axes show the energy scale for  $E_{\rm vib}$  and E, and the righthand axes show the scale for  $E_{\rm BO}$ . Crystal symmetry implies that E(Q) = E(-Q), so that the curves can be fitted to polynomials with only even terms. This guarantees that the transition is second-order according to Landau theory [11]. Results are presented for two different volumes of the primitive bcc lattice;  $V = 97.85a_0^3$  corresponds to approximately 150 GPa and  $V = 102.11a_0^3$  to 130 GPa. The pressure associated with each volume depends on both the isotope and Q(see Extended Data for the equations of states). Black circles represent calculated  $E_{\rm vib}$  points and the black dashed line the fitted  $E_{\rm vib}(Q)$  curve (see Methods). The E(Q) curve is obtained by addition of the fitted  $E_{\rm vib}$  and  $E_{\rm BO}$  curves.

<sup>71</sup> discussed [18]. According to structural predictions [5–9],  $_{72}$  H<sub>3</sub>S adopts a rhombohedral R3m form between approx-<sup>73</sup> imately 112 and 175 GPa, and a cubic  $Im\bar{3}m$  at higher  $_{95}$  implying that  $Im\bar{3}m$  is at a saddle point of the BOES bepressures. As shown in Fig. 1, the R3m phase is charac-74 75 76 77  $_{10}$  The Im3m phase, in contrast, has full cubic symme-  $_{100}$  phase [3, 19, 20] and other hydrogenated compounds [21], <sup>79</sup> try, with  $d_1 = d_2$  so that each H atom resides midway <sup>101</sup> the quantum nature of the proton can radically alter the  $_{20}$  between the two S atoms, as shown in Fig. 1. The R3m  $_{102}$  pressure at which the second-order phase transition oc-81 82 <sup>84</sup> surface (BOES), has a rhombohedral angle of 109.49° at <sup>106</sup> inclusion of vibrational zero-point energy (ZPE) along- $\approx 150$  GPa, compared to 109.47° for a perfect bcc lattice. 107 side the static BOES energy. However, the presence 86



FIG. 3. Second-order phase transition. (a) For each volume we plot the relative coordinate x that yields the minimum total energy. x measures the off-centering of the H atoms (see caption of Fig. 2). The results are shown in the classical nuclei limit, as well as in the quantum case both for  $H_3S$  and  $D_3S$ . The volume at which x departs from zero marks the second-order phase transition from the  $Im\bar{3}m$  phase to R3mphase. Transition pressures are also indicated, which include the effects of vibrational energies. (b) Phase diagram for the second-order phase transition as a function of pressure. As shown in Ref. 8, below 112 GPa  $H_3S$  adopts a very different  $C_2/c$  phase. We mark the expected emergence of this phase by a box.

<sup>87</sup> structure has a negligible effect on the energy difference <sup>88</sup> between the R3m and  $Im\bar{3}m$  structures. Consequently, we assume a cubic lattice for both phases in the following. 89

The bond-symmetrizing second-order transition from 90  $_{91}$  R3m to  $Im\bar{3}m$  occurs at 175 GPa according to our <sup>92</sup> static lattice calculations. At this pressure, our harmonic <sup>93</sup> phonon calculations show that a  $\Gamma$ -point optical phonon  $_{94}$  of the high-symmetry  $Im\bar{3}m$  phase becomes imaginary,  $_{96}$  tween 112 and 175 GPa, while the R3m phase lies at the terized by covalently bonded SH<sub>3</sub> units with a covalent <sup>97</sup> minimum. Crystal symmetry guarantees that the tran-H-S bond of length  $d_1$ . Each of these H atoms is bonded  $_{98}$  sition is of second-order type (see Extended Data for a to the next S atom by a hydrogen  $H \cdots S$  bond of length  $_{99}$  symmetry analysis). As occurs in the high-pressure ice X structure is nevertheless very close to cubic symmetry, 103 curs and, in the present case, can strongly affect the stafor example, the DFT-relaxed R3m structure, which rep- 104 bility of the R3m phase below 175 GPa. Determining resents the minimum of the Born-Oppenheimer energy 105 the stability ranges of these phases therefore requires the We have verified that imposing a cubic angle on the  $R3m_{108}$  of imaginary phonon frequencies hinders calculations of



FIG. 4. Phonon spectra and superconducting critical temperature. Harmonic and SSCHA anharmonic phonon spectra of the cubic high-symmetry  $Im\bar{3}m$  structure for H<sub>3</sub>S at different pressures: (a) 135 GPa and (b) 157 GPa. (c) Superconducting  $T_c$ 's calculated with the anharmonic phonons for the  $Im\bar{3}m$  structure compared with experimental results obtained after annealing [4].  $T_c$  results obtained with anharmonic phonons for the R3m structure below 175 GPa are also shown. Each pressure takes the vibrational energy into account.

<sup>109</sup> the ZPE, since the quasi-harmonic approximation breaks <sup>135</sup> ZPE contributions:  $E(\mathbf{R}_{c}) = E_{BO}(\mathbf{R}_{c}) + E_{vib}(\mathbf{R}_{c})$ . down, and anharmonicity becomes a crucial ingredient. 110

111 112 113 114 115 116 117 118 <sup>119</sup> presented here are performed at 0 K. Primitive cells for <sup>145</sup> the hydrogen nuclear wave-function and can be associ-<sup>120</sup> the R3m and Im3m structures contain 4 atoms (1 S atom <sup>146</sup> ated with the relative coordinate  $x = (d_2 - a/2)/(a/2)$  $_{121}$  and 3 H atoms), and therefore a particular nuclear con- $_{147}$  that quantifies the length of the H $\cdots$ S hydrogen bond 122 123 124 <sup>125</sup> ration **R** is given by the DFT Born-Oppenheimer energy <sup>151</sup> a cell volume of  $97.85a_0^3$  the  $E_{\rm BO}(Q)$  curve has a shal-126  $_{127}$  approximating the nuclear wave-function by a Gaussian  $_{153}$  only 5.6 meV/H<sub>3</sub>S. However, after adding the  $E_{\rm vib}(Q)$ 128 129 130 <sup>132</sup> sum of the nuclear potential and kinetic energies. In the <sup>158</sup> of E(Q) is also at Q = 0, despite the fact that the one- $_{133}$  following analysis it is convenient to split the SSCHA to- $_{159}$  dimensional Born-Oppenheimer well in  $E_{\rm BO}(Q)$  becomes  $_{134}$  tal energy  $E(\mathbf{R}_{c})$  into static and anharmonic-vibrational-  $_{160}$  deeper, as shown in Fig. 2(c). Repeating these calcula-

We study the energy landscape  $E(\mathbf{R}_{c})$  along the line 136 To elucidate the role of anharmonicity and quantum  $_{137}$  defined by  $\mathbf{R}_{c}(Q) = \mathbf{R}_{Im\bar{3}m} + Q(\mathbf{R}_{R3m} - \mathbf{R}_{Im\bar{3}m})$ , where effects in the pressure range in which the record  $T_c$  was  $_{138}$   $\mathbf{R}_{Im\bar{3}m}$  and  $\mathbf{R}_{R3m}$  are, respectively, the coordinates corobserved, we make use of the stochastic self-consistent 139 responding to the saddle point and minimum of the harmonic approximation (SSCHA) [22, 23]. The vari- 140 BOES, representing the two different symmetries. Here, ational SSCHA method was devised for calculating the  $_{141}$  Q is a real number describing the reaction coordinate, so free energy and phonon spectra while fully incorporat-  $_{142}$  that at Q = 0 the centroids are located at the atomic ing quantum and anharmonic effects, and it is therefore  $_{143}$  positions of  $Im\bar{3}m$ , and at Q = 1 at the atomic posiperfectly suited for our purpose. All of the calculations  $_{144}$  tions of R3m. Hence, Q measures the off-centering of figuration can be described by a 12-dimensional vector  $\mathbf{R}_{148}$  with respect to the symmetric position (a is the lattice containing the atomic coordinates. In the classical limit <sup>149</sup> parameter). We analyze the curve  $E(\mathbf{R}_{c}(Q)) \equiv E(Q)$  for the ZPE is neglected and the energy of a nuclear configu- 150 a fixed primitive bcc unit cell. As shown in Fig. 2(a) for  $E_{\rm BO}({\bf R})$ . In the SSCHA, the ZPE is accounted for by 152 low double-well structure favoring the R3m structure by centered on a centroid coordinate  $\mathbf{R}_{c}$ , which denotes the  $_{154}$  energy calculated with the SSCHA, the full E(Q) curve average and most probable position of the nuclei. For 155 shows a clear minimum at Q = 0, which favors the  $Im\bar{3}m$ a given  $\mathbf{R}_{c}$ , the width of the Gaussian is obtained by a 156 structure. At a larger volume of 102.11  $a_{0}^{3}$ , which correvariational minimization of the expectation value of the 157 sponds to a pressure of around 130 GPa, the minimum  $_{161}$  tions for D<sub>3</sub>S, we find that the  $Im\bar{3}m$  structure is the  $_{217}$  Eliashberg equations. The phonon frequencies and polar-162 163 164 165 166 167 168 169 170 172 173 174

175 176 177 178 179 180 181 182 183 184 185 sition [24]. Considering that below 112 GPa the  $R3m_{241}$  observed high- $T_c$  superconductivity cannot be explained 186  $_{187}$  phase consisting of isolated H<sub>2</sub>S and H<sub>2</sub> molecules with  $_{243}$  T<sub>c</sub> measured for D<sub>3</sub>S below 150 GPa [4] could be an in-188 H<sub>3</sub>S stoichiometry [8], R3m-H<sub>3</sub>S might not be formed. 244 dication of the symmetry breaking that we predicted at  $_{189}$  However, D<sub>3</sub>S may adopt the R3m structure at pressures  $_{245}$  115 GPa. Indeed, the predicted transition pressure debelow the transition to the  $Im\bar{3}m$  phase. 190

191 192 193 194 195 196 197 199 200 201 203 move towards the neighboring S atoms, which are pre- 260 phase would emerge at that pressure. cisely those modes which drive the second-order phase 261 205 206 207 transition is the origin of the strong anharmonicity. 208

209 210 insulating system, H<sub>3</sub>S is metallic and the symmetriza- 266 induces non-trivial effects that strongly affect the ther-211 calculated electron-phonon coupling and superconduct- 268 and the electron-phonon coupling strength. 212 ing  $T_c$  lend further support to the suggestion that  $Im\bar{3}m$ - 269  $_{214}$  H<sub>3</sub>S yields the record  $T_c$ . We use Wannier interpo-  $_{270}$  items in the online version of the paper for a symme-<sup>215</sup> lated electron-phonon matrix elements in our calcula-<sup>271</sup> try analysis of the phase transition, calculations with

most favorable once the ZPE has been included. We 218 izations that enter the electron-phonon calculations are therefore conclude that the quantum nature of the nuclei 219 calculated using the SSCHA. Thus, in the present treatsymmetrizes the hydrogen bond and leads to a proton 220 ment we neglect non-linear corrections of the electronwave-function centered at the atomic positions of  $Im3m_{221}$  phonon vertices and non-adiabatic effects that could arise for both  $H_3S$  and  $D_3S$ . To eliminate the possibility that  $_{222}$  from the small mass of H. The results obtained for the the energy minimum occurs beyond the  $\mathbf{R}_{c}(Q)$  line stud- <sup>223</sup> Im $\bar{3}m$  structure using anharmonic phonon frequencies ied, we performed an unconstrained SSCHA minimiza-  $^{224}$  agree well with experimental measurements of  $T_c$  for H<sub>3</sub>S tion, optimizing both the width of the Gaussians and the  $_{225}$  and  $D_3S$  and correctly capture the observed increase in  $\mathbf{R}_{c}$  centroid positions. The results of this minimization  $_{226} T_{c}$  with decreasing pressure. We also find an isotope show again that, within stochastic error, the centroid po-  $_{227}$  coefficient  $\alpha = -[\ln T_c(D_3S) - \ln T_c(H_3S)]/\ln 2$  for  $H \rightarrow D$ sition obtained corresponds to the  $Im\bar{3}m$  structure, in 228 substitution of  $\alpha = 0.35$  at 210 GPa and  $\alpha = 0.40$  at 155 which the H-S covalent and H $\cdots$ S hydrogen bond dis- 229 GPa in good agreement with experiment (see Fig. 4(c)). tances equalize, leading to symmetric hydrogen bonds.  $_{230}$  The electron-phonon coupling constant  $\lambda$ , which scales The difference between the vibrational energies of  $R3m_{231}$  with the phonon frequencies as  $\propto 1/\omega^2$ , is enhanced with and  $Im\bar{3}m$  as a function of the x coordinate is weakly de- 232 decreasing pressure due to the overall softening of the pendent on volume. This allows us to interpolate E(x) 233 phonon modes. This explains the smooth decrease of in a wide volume range and estimate the pressure at  $_{234}$   $T_c$  with increasing pressure. Between approximately 130 which the proton wave-function shifts away from the cen-  $^{235}$  and 150 GPa the increase in  $\lambda$  is compensated by the tered position. Our calculations show that this symme-  $_{236}$  decrease in the average phonon frequency and  $T_c$  satutry breaking occurs at 103 GPa in  $H_3S$  and 115 GPa in 237 rates. We also present SSCHA calculations for the R3m $D_3S$  (see Fig. 3). The higher transition pressure in  $D_3S$  <sup>238</sup> structure keeping the centroids at the Q = 1 position. is due to weaker quantum effects. This isotope effect is  $^{239}$  We find a rapid drop in  $T_c$  with decreasing pressure as similar to the one observed in the ice VII/ice X tran- 240 in previous harmonic calculations [13]. Therefore, the phase is expected to transform into a very different  $C2/c_{242}$  by H<sub>3</sub>S in the R3m phase, although the sudden drop in <sup>246</sup> pends on the choice of the exchange correlation functional The quantum proton symmetrization has an enormous 247 (see Methods). Even if our choice of the PBE exchangeimpact on the phonon spectra of H<sub>3</sub>S. As mentioned ear- 248 correlation functional [30] appears appropriate, based on lier, and shown in Fig. 4, the phonon spectra of  $Im\bar{3}m$ - 249 agreement between the experimentally observed equation H<sub>3</sub>S have several imaginary modes in the harmonic ap- <sup>250</sup> of state [10] and DFT calculations, we cannot exclude a proximation below 175 GPa. The corresponding anhar- 251 small error in the transition pressure. However, the isomonic SSCHA phonon spectra for  $Im\bar{3}m$ -H<sub>3</sub>S show well- <sup>252</sup> topic shift of the transition pressure is independent of the behaved phonon dispersion relations with positive fre-  $^{253}$  functional. Thus, if the drop in  $T_c$  observed experimenquencies in the pressure range of interest (Fig. 4). This  $_{254}$  tally in D<sub>3</sub>S is due to the transition from R3m to  $Im\bar{3}m$ , is analogous to ice X, which has only real positive phonon 255 we predict that a similar drop also occurs in H<sub>3</sub>S but is frequencies once the classical limit predicts symmetriza- 256 shifted to lower pressures by about 12 GPa. Considering tion of the hydrogen bond [25–28]. The anharmonic 257 that the  $Im\bar{3}m$  phase has no Raman active modes, if the renormalization of the phonon energies is huge, especially  $^{258}$  drop in  $T_c$  in D<sub>3</sub>S coincides with the second-order phase for the H-S bond-stretching modes in which H atoms 259 transition, we predict that Raman peaks from the R3m

The recent experiment by Drozdov *et al.* [4] suggests transition between the  $Im\bar{3}m$  and R3m phases. There-  $_{262}$  that room-temperature superconductivity is reachable in fore, the proximity to the second-order quantum phase 263 other hydrogen-rich compounds. Our results show that <sup>264</sup> in such hydrogen-rich materials with prospects for high-While the bond symmetrization in ice X occurs in an  $_{265}$  T<sub>c</sub> superconductivity the quantum motion of the proton tion strongly affects the superconductivity. Indeed, the 267 modynamical stability, the hydrogen chemical bonding,

Online Content See Methods and Extended Data  $_{216}$  tions [29] and estimate  $T_c$  solving the isotropic Migdal- $_{272}$  different exchange-correlation functionals, the equations

273 of state, harmonic and anharmonic phonon spectra of 332  $_{274}$  Im $\bar{3}m$ -D<sub>3</sub>S, anharmonic phonon spectra of the R3m  $_{333}$  $_{275}$  phase, and superconducting properties of both the  $Im\bar{3}m$  $_{276}$  and R3m structures.

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Acknowledgements We acknowledge financial sup-388 port from the Spanish Ministry of Economy and Compet-389 itiveness (FIS2013- 48286-C2-2-P), French Agence Na-390 tionale de la Recherche (Grant No. ANR-13-IS10-0003-391 <sup>392</sup> 01), EPSRC (UK) (Grant No. EP/J017639/1), Cam-<sup>393</sup> bridge Commonwealth Trust, National Natural Science <sup>394</sup> Foundation of China (Grants No. 11204111, 11404148,

<sup>395</sup> and 11274136), and 2012 Changjiang Scholars Program
<sup>396</sup> of China. Work at Carnegie was supported by EFree,
<sup>397</sup> an Energy Frontier Research Center funded by the DOE,
<sup>398</sup> Office of Science, Basic Energy Sciences under Award
<sup>399</sup> No. DE-SC-0001057. Computer facilities were provided
<sup>400</sup> by the PRACE project AESFT and the Donostia Inter<sup>401</sup> national Physics Center (DIPC).

**Author Contributions** I.E., M.C., and F.M. per-403 formed the anharmonic and superconducting calcula-404 tions. All authors contributed to the design of the re-405 search project and to the writing of the manuscript.

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## 412

## **METHODS**

Calculation Details Supercell calculations for the 413 <sup>414</sup> SSCHA [22, 23] and linear response calculations [31] were performed within DFT and the generalized gradient ap-415 proximation functional [30] as implemented in the QUAN-416 TUM ESPRESSO [32] code. We used ultrasoft pseu-417 <sup>418</sup> dopotentials [33], a plane-wave cutoff energy of 60 Ry <sup>419</sup> for the kinetic energy and 600 Ry for the charge den-420 sity. The charge density and dynamical matrices were calculated using a  $32 \times 32 \times 32$  Monkhorst-Pack shifted 421 electron-momentum grid for the unit cell calculations. 422 This mesh was adjusted accordingly in the supercell cal-423 culations. The electron-phonon coupling was calculated 424 by using electron and phonon momentum grids composed 425  $_{426}$  of up to  $42 \times 42 \times 42$  randomly displaced points in the Brillouin zone. The isotropic Migdal-Eliashberg equa-427 tions were solved using 512 Matsubara frequencies and 428 429  $\mu^* = 0.16.$ 

The SSCHA calculations were performed using a 430  $3 \times 3 \times 3$  supercell for both H<sub>3</sub>S and D<sub>3</sub>S in the  $Im\bar{3}m$ 431 <sup>432</sup> phase, yielding dynamical matrices on a commensurate  $_{433}$  3×3×3 q-point grid. The difference between the har- $_{434}$  monic and anharmonic dynamical matrices in the  $3 \times 3 \times 3$ phonon momentum grid was interpolated to a  $6 \times 6 \times 6$ 435 grid. Adding the harmonic matrices to the result, the anharmonic dynamical matrices were obtained on a  $6 \times 6 \times 6$ 437 grid. These dynamical matrices were used for the an-<sup>439</sup> harmonic electron-phonon coupling calculation. The SS-440 CHA calculations for Q = 1 were performed with a  $_{441}$  2×2×2 supercell. For consistency, the vibrational en-<sup>442</sup> ergies presented in Fig. 2 were also calculated using a 443  $2 \times 2 \times 2$  supercell. The electron-phonon calculations for Q = 1 were, however, performed with the SSCHA dy-444 445 namical matrices interpolated to a  $6 \times 6 \times 6$  grid from the  $2 \times 2 \times 2$  mesh. 446

The  $E_{\rm vib}(Q)$  curves in Fig. 2 were obtained as fol-447 448 lows.  $E_{\rm vib}$  was calculated for Q = 0 and Q = 1 with <sup>449</sup> the SSCHA. With the SSCHA calculation at Q = 1, we 450 extracted  $\frac{dE_{\text{vib}}}{dQ}(Q = 1)$  with no further computational 451 effort. Considering that the derivative of the curve at  $_{452} Q = 0$  vanishes by symmetry, we can obtain straightfor-<sup>453</sup> wardly a potential of the form  $E_{\rm vib}(Q) = A + BQ^2 + CQ^4$ .  $_{454}$  The  $E_{\rm vib}$  fit curves presented in Fig. 2 were obtained in 455 this way. The extra point obtained at Q = 0.5 for H<sub>3</sub>S 456 at  $V = 97.85a_0^3$  (see Fig. 2(a)) confirmed the validity of the fitting procedure. The  $E_{\rm BO}(Q)$  BOES energies were 457 calculated for many Q points yielding an accurate fitting 458 curve. Fig. 3 was obtained using a polynomial inter-459 460 polation of the BOES in the volume range shown and <sup>461</sup> adding the  $E_{\rm vib}^{R3m} - E_{\rm vib}^{Im\bar{3}m}(x)$  curves that are practically 462 independent of volume.

463 464  $_{465}$  R3m to  $Im\bar{3}m$  is a second-order transition and is driven  $_{521}$  pressure 30 GPa below PBE, while BLYP symmetrizes

466 by the softening of an optical mode at  $\Gamma$ . The mode <sup>467</sup> driving the transition belongs to the irreducible repre-468 sentation  $T_{1u}$ , also denoted as  $\Gamma_4^-$ , whose dimension is 3 [34, 35]. This irreducible representation is compatible  $_{470}$  with a group-subgroup relation between the  $Im\bar{3}m$  and  $_{471}$  R3m space groups. As the mode driving the transition  $_{472}$  is at the  $\Gamma$  point, the transition occurs without increas-473 ing the unit cell size, which contains four atoms in the  $_{474}$  primitive cell of the bcc lattice of the  $Im\bar{3}m$  structure as  $_{475}$  well as in the rhombohedral lattice of the R3m phase.

In a transition from the  $m\bar{3}m$  ( $O_h$ ) point group to the 476  $_{477}$  3m ( $C_{3v}$ ), the most general free energy expansion only <sup>478</sup> contains even terms of the order parameters [36]. There-<sup>479</sup> fore, according to Landau theory [11], the transition must  $_{480}$  be of second-order. Our reaction coordinate Q used to 481 describe the second-order transition is a simplified order 482 parameter. The fact that E(Q) = E(-Q) confirms that 483 the transition is of second-order.

Equations of state In Extended Data Fig. 1 we 485 present the equation of state both for the  $Im\bar{3}m$  and  $_{486}$  R3m phases. The pressure is calculated both with and 487 without the vibrational contribution to the energy, for <sup>488</sup> H<sub>3</sub>S and D<sub>3</sub>S. The latter curves are used to include the 489 vibrational effects on the calculated pressures. The vi-<sup>490</sup> brational energy calculated includes anharmonicity in all <sup>491</sup> cases as calculated by the SSCHA. The vibrational en-<sup>492</sup> ergy has a small contribution to the calculated pressure, 493 which varies slightly with the isotopic mass. The P(V)<sup>494</sup> curve can be efficiently fitted to the third-order Birch-<sup>495</sup> Murnaghan equation. The parameters of the fit are given <sup>496</sup> in Extended Data Table I.

Dependence on the exchange-correlation func-<sup>498</sup> tional All calculations presented in the manuscript are 499 calculated within the generalized gradient approxima-<sup>500</sup> tion (GGA) under the PBE parametrization [30]. How-<sup>501</sup> ever, we have performed additional calculations within <sup>502</sup> the local density approximation (LDA) [37] and the <sup>503</sup> BLYP [38, 39] parametrization of the GGA. The second <sup>504</sup> order phase transition at the static level from  $Im\bar{3}m$  to  $_{505}$  R3m, which occurs at 175 GPa within PBE, is reduced  $_{\rm 506}$  to 145 GPa in the LDA and increased to 257 GPa with <sup>507</sup> the BLYP parametrization. In Extended Data Fig. 2 we 508 compare the relative coordinate  $x = (d_2 - a/2)/(a/2)$  as a  $_{509}$  function of volume, where  $d_2$  is the length of the hydrogen  $_{510}$  bond and a is the lattice parameter. The x coordinate  $_{511}$  is obtained both with the static BOES energy  $E_{\rm BO}$  as  $_{512}$  well as with the total energy  $E = E_{BO} + E_{vib}$ . The vi-<sup>513</sup> brational energy is however assumed to be independent <sup>514</sup> of the functional, and the value obtained with PBE is  $_{515}$  used for estimating  $E_{\rm vib}$  for both LDA and BLYP. We <sup>516</sup> believe this is justified because the differences between <sup>517</sup> the vibrational energies of  $Im\bar{3}m$  and R3m calculated <sup>518</sup> within the SSCHA and using PBE are very weakly vol-Symmetry analysis of the second-order phase <sup>519</sup> ume dependent as shown in Extended Data Fig. 4. At transition The bond-symmetrization transition from 520 the static level, the LDA symmetrizes the structure at a

<sup>522</sup> it at a pressure 82 GPa above PBE. When including the <sup>575</sup> vibrational contribution as described above, the transi-576 523 tion between  $Im\bar{3}m$  and R3m occurs at 170 GPa for H<sub>3</sub>S 577 524 578 and 185 GPa for  $D_3S$  within BLYP. The shift of the tran-525 579 sition pressure induced by the zero-point energy and its 526 580 527 isotope dependence is similar for PBE and BLYP. The 581 fully symmetric  $Im\bar{3}m$  H<sub>3</sub>S structure is always favoured 528 582 within the LDA for H<sub>3</sub>S over the pressure range studied, 583 529 and it only becomes unfavorable below 89 GPa for  $D_3S$ . 584 530 585 Although the choice of exchange-correlation functional 531 586 adds some uncertainty to the predicted transition pres-532 587 sure, we believe PBE is the most appropriate choice. This 533 588 statement is based on the fact that PBE best reproduces 534 589 the experimental equation of state results of Einaga et 590 [37] 535 al. [10]. BLYP overestimates the volume, specially when 536 591 the vibrational contribution is considered (see Extended 592 537 Data Fig. 3). Indeed, it is well known that BLYP vastly 538 overestimates the equilibrium volumes in metals [40] and, 595 therefore, it is not the best choice for  $H_3S$ . On the con-540 trary, when including the vibrational contribution to the 541 597 pressure, which is calculated in all cases using the PBE 598 542 functional, the PBE equation of state is in rather good 599 543 agreement with experimental results [10] and certainly 544 performs better than LDA and BLYP. 545

<sup>546</sup> **Phonons of**  $Im\bar{3}m$ -**D**<sub>3</sub>**S** In Extended Data Fig. 5 we <sup>547</sup> show the harmonic and anharmonic phonon spectra of <sup>548</sup> **D**<sub>3</sub>**S** in the  $Im\bar{3}m$  phase at two different pressures.

Anharmonic phonon dispersion in the R3m 549 phase In Extended Data Fig. 6 we show the SSCHA 550 phonon spectra calculated for the R3m phase at two dif-551 ferent pressures. Here the centroid position of the SS-552 CHA is placed at the minimum of the BOES, which is 553 not a minimum of the total energy as discussed in the 554 manuscript. The Raman active modes of the R3m phase 555 are listed in Extended Data Table II. 556

<sup>557</sup> **Superconducting properties** In Extended Data <sup>558</sup> Table III we summarize the calculated values of the <sup>559</sup> electron-phonon coupling constant  $\lambda$ , logarithmic fre-<sup>560</sup> quency average  $\omega_{\log}$ , and superconducting  $T_c$ .

In Extended Data Fig. 7 we show the Eliashberg function  $\alpha^2 F(\omega)$  and integrated electron-phonon coupling constant  $\lambda(\omega)$  of the  $Im\bar{3}m$  phase at two different pressures calculated using the SSCHA phonons. The  $\alpha^2 F(\omega)$ in the anharmonic case for the R3m structure is given in Extended Data Fig. 6.

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562 (2001).

Extended Data Table I. Birch-Murnaghan fit to the equation of state. Parameters of the  $P(V) = \frac{3}{2}B_0\left[(V_0/V)^{7/3} - (V_0/V)^{5/3}\right]\left[1 + \frac{3}{4}(B'_0 - 4)[(V_0/V)^{2/3} - 1]\right]$  fit to the equation of state for  $Im\bar{3}m$  with classical nuclei, and with vibrational contributions for both H<sub>3</sub>S and D<sub>3</sub>S.

|                  | $B_0$ (GPa) | $V_0 (a_0^3)$ | $B'_0$ |
|------------------|-------------|---------------|--------|
| Classical nuclei | 129.8       | 158.4         | 3.6    |
| $H_3S$           | 86.63       | 176.4         | 3.9    |
| $D_3S$           | 87.81       | 174.8         | 3.9    |



Extended Data Figure 1. Equations of state. Pressure as a function of volume calculated from the static energy  $E_{BO}$  that represents the classical nuclei limit as well as including the vibrational contribution within the SSCHA for both H<sub>3</sub>S and D<sub>3</sub>S.



Extended Data Figure 2. Bond symmetrization within LDA and BLYP. For each volume the relative coordinate  $x = (d_2 - a/2)/(a/2)$ , where  $d_2$  is the length of the hydrogen bond and a is the lattice parameter, obtained at the energy minimum is marked. When x = 0 the covalent and hydrogen bond have the same length and the structure is fully symmetric. The energy is calculated at the static level without any vibrational contribution as derived from the BOES, and including the quantum anharmonic vibrational contribution both for H<sub>3</sub>S and D<sub>3</sub>S. The pressure below which the cubic structure distorts is given in each case.



Extended Data Figure 3. Functional dependence of the equation of state. The equation of state is calculated with different exchange correlation functionals with and without the vibrational contribution to the pressure. At each volume the pressure of the structure with minimum energy is given, which depends on whether or not the vibrational contribution is included (see Extended Data Fig. 2). The results are compared with the two curves obtained experimentally [10].



Extended Data Figure 4. Vibrational energy. SSCHA anharmonic vibrational energy calculated as a function of the relative coordinate  $x = (d_2 - a/2)/(a/2)$  for different volumes.



Extended Data Figure 5. Phonons of  $Im\bar{3}m$ -D<sub>3</sub>S. Comparison between the harmonic and anharmonic phonons of  $Im\bar{3}m$  at two different pressures for D<sub>3</sub>S.



Extended Data Figure 6. Anharmonic phonons of R3m-H<sub>3</sub>S at two different pressures. The Eliashberg functions  $\alpha^2 F(\omega)$  are also shown.

Extended Data Table II. **Raman and infrared active modes.** Phonon modes at the  $\Gamma$  point for the  $Im\bar{3}m$  and R3m phases at different pressures calculated including anharmonicity within the SSCHA. The results for R3m are obtained keeping the centroid position at the minimum of the BOES. Raman (R) and Infrared (I) activity is indicated for each mode.

| $Im\overline{3}m$ | Mode  | Dogonoracy | B or Lactive?             | (1) (moV)      |                |                |         |  |  |
|-------------------|---|------------|---------------------------|----------------|----------------|----------------|---------|--|--|
|                   | moue  | Degeneracy | It of 1 active:           | $\omega$ (meV) |                |                | S       |  |  |
|                   |   |            |                           | 135 GPa        | 35<br>157 GPa  | 133 GPa        | 155 GPa |  |  |
|                   | $T_1$   | 3          | T                         | 79.6           | 87.6           | 46.7           | 54.1    |  |  |
|                   | $T_1^{1u}$  | 3          | I                         | 131.0          | 159.1          | 95.4           | 100.8   |  |  |
|                   | $T_1u$<br>$T_2$                                       | 3          | 1                         | 151.0<br>177.3 | 182.1          | 125.8          | 109.0   |  |  |
| - P3m             | 12u   | 0          |                           | 111.0          | 102.0          | 120.0          | 123.0   |  |  |
| 113111            | Modo  | Doconoracy | R or Lactive?             |                | ( ) ( n        | $(\mathbf{V})$ |         |  |  |
|                   | mode  | Degeneracy | n of factive:             | ц              | ູຊ ພ (1        |                | S       |  |  |
|                   |   |            |                           | 122 CDa        | 30<br>153 CDa  | 122 CPa        | 152 CDa |  |  |
|                   | F   | 2          | $\mathbf{P} + \mathbf{I}$ | 100 GI a       | 100 GF a       | 100 GI a       | 73.7    |  |  |
|                   | 12<br>A.  | 2          | R+I                       | 115.4          | 112.2<br>114.7 | 74.4           | 73.7    |  |  |
|                   | F   | 1          | n+1<br>P+1                | 149.4          | 114.7          | 19.0<br>105.6  | 105.0   |  |  |
|                   |   | ∠<br>1     | n+1<br>D+1                | 142.4          | 144.0          | 100.0          | 105.9   |  |  |
|                   | $A_1$   | 1          | K+1                       | 108.7          | 105.0          | 123.2          | 115.0   |  |  |
|                   | $A_2$   | 1          | DII                       | 1/8.0          | 185.3          | 125.1          | 130.7   |  |  |
|                   | E   | 2          | R+I                       | 181.0          | 186.7          | 127.0          | 131.7   |  |  |
|                   |   |            |                           |                |                |                |         |  |  |
|                   |   |            |                           |                |                |                |         |  |  |
|                   |   |            |                           |                |                |                |         |  |  |
|                   | 3   |            |                           |                |                | 1 1            | ]       |  |  |
|                   | 2.5   | _          |                           |                | 135 (          |                | _       |  |  |
|                   |   |            |                           |                |                |                |         |  |  |
|                   | $15 - \alpha (\omega)$ $\gamma - 4 - 157 \text{ GPa}$ |            |                           |                |                |                |         |  |  |
|                   | 1   | λ(α        | )) (1)                    |                |                |                |         |  |  |
|                   | 0.5   | -          | from                      |                |                |                |         |  |  |
|                   | 0.5   |            |                           |                | MY L           | -<br>-         | -       |  |  |
|                   | 0   | 50         | 100 1                     | 50 2           | 200 2          | 50 3           | 300     |  |  |
|                   | 0   | 20         | ω                         | meV)           |                |                |         |  |  |

Extended Data Figure 7. Superconducting properties of  $Im\bar{3}m$ -H<sub>3</sub>S. Anharmonic Eliashberg function  $\alpha^2 F(\omega)$  and integrated electron-phonon coupling constant  $\lambda(\omega)$  of the  $Im\bar{3}m$  phase at two different pressures.

Extended Data Table III. Superconducting parameters. Calculated  $\lambda$ ,  $\omega_{\log}$  and  $T_c$ . The pressure given includes the vibrational contribution.

|                    | Compound | P (GPa) | λ    | $\omega_{\log}(\text{meV})$ | $T_c$ (K) |
|--------------------|----------|---------|------|-----------------------------|-----------|
| SSCHA $Im\bar{3}m$ |          |         |      |                             |           |
|                    | $H_3S$   | 135     | 2.10 | 104.9                       | 214       |
|                    | $H_3S$   | 157     | 1.94 | 113.8                       | 216       |
|                    | $D_3S$   | 133     | 2.45 | 70.5                        | 163       |
|                    | $D_3S$   | 155     | 2.08 | 82.9                        | 163       |
| SSCHA $R3m$        |          |         |      |                             |           |
|                    | $H_3S$   | 133     | 1.62 | 105.8                       | 163       |
|                    | $H_3S$   | 153     | 1.93 | 109.3                       | 205       |
|                    | $D_3S$   | 132     | 1.64 | 79.8                        | 123       |
|                    | $D_3S$   | 152     | 2.00 | 81.4                        | 155       |
|                    |          |         |      |                             |           |