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published in

NIC Workshop 2006, From Computational Biophysics to Systems Biology, Jan Meinke, Olav Zimmermann, Sandipan Mohanty, Ulrich H.E. Hansmann (Editors) John von Neumann Institute for Computing, Jülich, NIC Series, Vol. **34**, ISBN-10: 3-9810843-0-6, ISBN-13: 978-3-9810843-0-6, pp. 169-172, 2006.

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## **Determination of Short-Range Potentials for Physics-Based Protein-Structure Prediction**

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By integrating *ab initio* energy surfaces of the model terminally-blocked amino-acid residues: glycine, alanine, and proline, we calculated the potentials of mean force corresponding to the bending of the  $C^{\alpha} \cdots C^{\alpha} \cdots C^{\alpha}$  virtual-bond angles for the purpose of using them in our united-residue UNRES force field. The potentials for the glycine and alanine residues were found to be bimodal as are the corresponding statistical potentials determined from the Protein Data Bank.

#### 1 Introduction

Local interactions play a very significant role in determining protein structure, because they determine the geometry of secondary-structure elements (e.g., the  $\alpha$ -helices and the  $\beta$ -sheets), as well as that of turns and loop regions. Therefore, accurate representation of local-interaction terms in the empirical force fields for physics-based protein-structure prediction is of utmost importance. In this communication, we present the determination of the potentials of mean forces for the bending of the C<sup> $\alpha$ </sup> ... C<sup> $\alpha$ </sup> ... C<sup> $\alpha$ </sup> virtual-bond angles for the purpose of using them in our united-residue physics-based UNRES force field field<sup>1-4</sup> for protein-structure prediction from *ab initio* energy surfaces of terminallyblocked amino-acid residues, which will replace the statistical potentials determined in our earlier work<sup>2</sup> from PDB statistics.

#### 2 Methods

The model system used to calculate the potentials of mean force corresponding to the bending of virtual-bond angles  $\theta$  is shown in Figure 1. The neighboring amino-acid residues are included because, from the PDB statistics, it follows<sup>2</sup> that the distribution of virtualbond angles  $\theta$  depends on the values of the neighboring virtual-bond dihedral angles  $\gamma$  and, consequently, the bending potentials in UNRES are functions of these angles.

The potentials of mean force of virtual-bond angle bending,  $F_{XYZ}(\theta, \gamma_1, \gamma_2)$  (where X, Y, and Z are the types of residue involved; see Figure 1), were computed in this work from the energy maps of terminally-blocked X, Y, and Z residues based on the theory presented in Ref. 5 extended by applying the harmonic approximation to each point of the map of the central residue Y. We used the energy maps of terminally-blocked Gly, Ala,

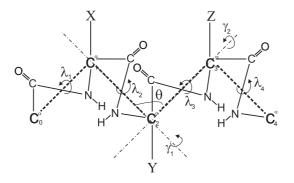


Figure 1. Illustration of a model system for the calculation of the potentials of mean force of the bending of the virtual-bond angles  $\theta$ . The variables to integrate over are the torsional angles of rotation,  $\lambda_1 - \lambda_4$  of the peptide groups about the  $C^{\alpha} \cdots C^{\alpha}$  virtual-bond axes, while the virtual-bond angle  $\theta$  and the virtual-bond dihedral angles  $\gamma_1$  and  $\gamma_2$  are the primary variables

and Pro calculated in Ref. 5 at the *ab initio* MP2/6-31G\*\* level with the grid of 15°; each point of a map corresponds to a structure minimized in all degrees of freedom except the angles  $\lambda$ . In this work, we computed the Hessian matrices at each point of a map and used them together with minimum-energy values to compute  $F_{XYZ}(\theta, \gamma_1, \gamma_2)$ . All potentials of mean force were computed at T=298°K.

#### **3** Results and Discussion

The plots of  $\overline{F}_{Y}(\theta)$  (Boltzmann-averaged over the angles  $\gamma_1$  and  $\gamma_2$  for X=Gly, Ala, and Pro are shown in Figure 2. In this Figure, the statistical potential  $\overline{F}_{Ala}(\theta)$  determined in Ref. 2 is also presented for comparison.

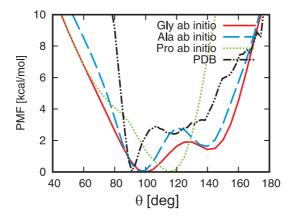


Figure 2. Potentials of mean force of virtual-bond-angle bending Boltzmann-averaged over the virtual-bonddihedral-angles  $\gamma_1$  and  $\gamma_2$  compared with the statistical potential computed from the PDB statistics for Ala-type virtual-bond angles.

It can be seen from Figure 2 that the  $\overline{F}_{Gly}(\theta)$  and  $\overline{F}_{Ala}(\theta)$  potentials have two minima, one for  $\theta = 100^{\circ}$  and the second one for  $\theta = 140^{\circ}$ . Analysis of the complete  $F_{XYZ}(\theta, \gamma_1, \gamma_2)$  potentials shows that the first minimum corresponds to the  $\alpha$ -helical and the second one to the extended region. This finding agrees with the analysis of the statistical potentials from the PDB<sup>2</sup>. However, the second minimum is not pronounced in the statistical potentials which is caused by the fact that most of the data pertained to  $\alpha$ -helical structures. The present potentials are not biased to any organized structure and are, therefore, expected to improve the performance of the UNRES force field.

#### Acknowledgments

Support from the National Institutes of Health (grant GM-14312), the National Science Foundation (grant MCB00-03722), the NIH Fogarty International Center (grant TW7193), the Polish Ministry of Education and Science (grant 3 T09A 134 27) as well as use of supercomputing resources at the National Science Foundation Terascale Computing System at the Pittsburgh Supercomputer Center, the Informatics Center of the Metropolitan Academic Network (IC MAN) in Gdańsk, and the Interdisciplinary Center of Mathematical and Computer Modeling (ICM) at the University of Warsaw is gratefully acknowledged.

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