

# High Performance, Low Power Architecture of 5-stage FIR Filter using Modified Montgomery Multiplier

T. Thanmai, JVR Ravindra

Center for Advanced Computing Research Laboratory (C-ACRL) ,  
Department of Elec. and Comm. Engg.  
Vardhaman College of Engineering  
Shamshabad, Telangana, India  
<ayatsafdar05@gmail.com>, <jvr.ravindra@vardhaman.org>

**Abstract**—In the field of VLSI, enhancement is prominent. Arithmetic circuits are one of the influential sectors in today's end products of electronics, where multipliers are one of the deciding factors of efficiency. Multiplier plays an important role in different applications such as digital signal processing in which it acts as a key hardware block. As time rolls down, the technology exposed the ways for the initiation of many hardware and software implementations of the faster multipliers. One among them is the Montgomery multiplier. The fundamental operation in the Montgomery multiplier is the modular multiplication. It is mainly used in FIR filters, which in-turn has numerous applications such as speech analysis, multi-rate signal processing, adaptive filters, and averaging filters. With the usage of proposed compressor in the conventional design of the multiplier, the number of transistor count has been declined by a significant amount and made the design into an optimal area design. This paper presents a modified Montgomery multiplier design and its implementation in the 5<sup>th</sup> order FIR filter. The entire design simulation is carried out using CMOS and PTL logic in 45 nm technology. There is an escalation in the result outcomes, and the multiplier has an area efficiency of 65% and a power reduction of about 68% in comparison with conventional design.

**Index Terms**— Cryptography, Montgomery Multiplier, Compressor, FIR Filter

## I. INTRODUCTION

In the world of smart technology, data security is a crucial entity for every individual. The techniques for securing data are in high demand and became challenging for the designers to come up with efficient ways based on the requirements. The expanding areas of networks and security demand more number of efficient algorithms for use in cryptography [1]. Many researchers have done phenomenal work and proposed various architectures with the advancements [2]. Encryption is an essential criteria in cryptography for data handling and processing. When explicit information from one environment is to send to the other, then encryption of the data is necessary for security purposes. Cryptography provides pavement for this restraint. It deals with encryption and decryption of the data such that the fundamental information transfer from the sender to the recipient remains confidential. The

cryptographic algorithms which are used in advance systems has motive principles of authentication and data secrecy.

Performing modular multiplication is one of the core operations in cryptography. Given two inputs P and Q of k bits each, where P is the multiplier and Q is the multiplicand and modulus N of k bits, modular multiplication is given by eq. (1), in which C represents the result of the multiplication.

$$\begin{aligned} P &= p_{k-1} \dots p_1 p_0 \\ Q &= q_{k-1} \dots q_1 q_0 \\ N &= n_{k-1} \dots n_1 n_0 \\ C &= P * Q * \text{mod}(N) \end{aligned} \quad (1)$$

In most of the cryptographic applications, modular multiplication algorithm tends to be a time-consuming process. Therefore, for the efficient functioning of the algorithm and to decrease time consumption, modular multiplication reduction is necessary [3]. As the Montgomery multiplication speedup modular multiplication algorithm, it is one of the adaptable choices for the designers as it evades trial division, which is the strenuous algorithm for integer factorization. Embedding the Carry-Save Adders (CSA) reduces the critical path delay [4]. Performing addition and division arithmetic operations by the powers of two substitutes the trial division in Montgomery multiplication. Computing multiplications take a transformation from time-consuming to time-saving process with the Montgomery multiplication as there are no division and subtraction operations involved. Instead, the addition of multiples of N takes place for the reduction of least significant bits and discard them in the final product. The representation of multiplication in Montgomery domain is as eq. (2)

$$C = P * Q * r^{-1} \text{mod}(N) \quad (2)$$

where, r is a positive integer and co-prime of N. The condition of  $r > N$  must be satisfied all the time while performing the multiplication. In general, r is considered as  $2^m$ , where m is a positive integer. This is because shift and bit operations are convenient to consider for the efficient implementation. N is always

an odd prime number. The implementation of modular multiplication consists of 3 steps.

- 1) The first step is the partial product generation for the given inputs P and Q.
- 2) The second step in the process is the division.
- 3) The final step is the reduction of the least significant bits to produce the exact results.

There are several ways to implement the Montgomery multiplication algorithm, and many algorithms are proposed by different designers to scale down the complexity and to improve efficiency. The two ways for the implementation of Montgomery multiplier are bit-serial [5] and bit-parallel. The selection depends on the type of application.

This paper presents a bit serial modified Montgomery multiplier and its implementation in the 5th order FIR filter with power, area, and delay calculations. The paper is organized as follows: Section-II reviews the conventional digit-serial Montgomery multiplier and section III discuss about Modified Montgomery Multiplier, section-IV discusses proposed 12:6 compressor: Astute Compressor. Section-V evaluates the proposed Montgomery Multiplier design using Astute Compressor. A comparison with previous multipliers is also given in this section. Section-VI reviews the implementation of the modified Montgomery multiplier in a 5<sup>th</sup> order low pass FIR filter. Section-VII concludes this paper.

## II. CONVENTIONAL DIGIT-SERIAL MONTGOMERY MULTIPLIER

The conventional Montgomery multiplier [6] is constructed for  $m=6$  and  $d=3$ , where  $m$  is the digit size of each input and  $d$  is the bit size. The first stage in computing the results of the multiplier, is the processing stage. The partial product generation for the given multiplicand and multiplier takes place in this stage with the combination of And-network and Adder-network. The multiplicand and the multiplier are of 6-bit length each. The individual bit representation of multiplicand, multiplier and modulus N is given by eq. (3). The complete Montgomery multiplication algorithm takes place in 2 cycles. In the first cycle of the algorithm, 6 bits of multiplicand P and first 3 bits of multiplier Q are given as the inputs. In the second cycle, the next 3 bits of the multiplier Q will be acting as the inputs. To choose the bits of multiplier according to the cycle, 2:1 multiplexers are used. For each bit of the Q, a multiplexer is used and based on the selection line, the required bits are chosen. If the selection line is high for all the 3 multiplexers, first 3 bits of Q i.e. ( $q_0, q_1, q_2$ ) will be propagated as inputs. If the selection line is low, the next 3 bits of Q i.e. ( $q_3, q_4, q_5$ ) are propagated as inputs. In the first cycle of the algorithm, all the carry bits which are given as the inputs to the processing element are considered as zeros i.e.  $C=0$ . 6 bits of multiplicand and first 3 bits of the multiplier generates partial products as shown in eq. (4). The outputs of the processing element are the Sum and Carry bits of full adders that are present

in the adder network, and they will be driving the next stage.

$$\begin{aligned} P &= (p_{m-1}, p_{m-2}, \dots, p_0) \\ Q &= ((q_{m-1}, q_{m-2}, \dots, q_{m-d}), (q_{d-1}, q_{d-2}, \dots, q_0)) \\ N &= (n_{m-1}, n_{m-2}, \dots, n_0) \\ C &= 0 \end{aligned} \quad (3)$$

$$C = \sum_{i=0}^d \sum_{j=0}^{m-1} p_j q_i + C \quad (4)$$

The second stage is the division stage. An array of full adders performs the division operation in the algorithm. Bits of N operates as one of the inputs to the full adders and the other inputs are Sum and Carry bits of the adders involved in the successive stages. The outputs of adders after performing the division operation are the Carry bits from  $C_0$  to  $C_6$  and  $Cc_1$  to  $Cc_6$ . The Carry bits will be acting as inputs to the final stage of the design. 3 D-flipflops in which 2 are of 6 bit input size and 1 single D-flipflop are used to store Carry bits generated from the division cell and to give them back as inputs to the processing element in the second stage. The usage of D-flipflops in the circuit reduces the critical path delay. A D-flipflop works under the presence of a clock signal and operates with a delay in input by one clock cycle. After the generation of Carry bits, the second cycle starts and in the second cycle of the multiplier, the next 3 bits of multiplicand and the Carry bits from the D-flipflop will repeat the process and produces the final output of the multiplication from the compressor. The output produced is of 6 bit length which is equal to the bit size of the given inputs to the multiplier.

## III. MODIFIED MONTGOMERY MULTIPLIER

The modified Montgomery multiplier consists of 3 stages as shown in Fig. (1). The first two stages perform the similar operation as in the conventional design [6]. The reduction cell in the conventional design is replaced with the proposed 12:6 Astute Compressor, making the design into a modified one. This modification resulted in area and power efficient multiplier by reducing the complexity involved in the usage and design of multiplexers in the reduction cell of the conventional design and by declining the number of transistor count.

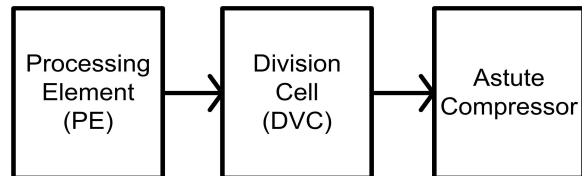


Fig. 1: Block Diagram of Modified Montgomery Multiplier

The modified Montgomery multiplier design works for any 6 bit length input P and Q, but the value of N is restricted to 3 and 7. The results produced by the multiplier are accurate. Using 45 nm technology in the

Cadence Virtuoso tool, the design of modified Montgomery multiplier with a combination of CMOS and PTL logic [7] resulted in low power and area efficient design. The proposed Astute compressor lessened the number transistors to a notable amount.

#### IV. PROPOSED 12:6 COMPRESSOR: ASTUTE COMPRESSOR

The compressor is a circuit that is used to depreciate the area by down turning the transistors count and reduce the overall power and delay for more reliable performance of a design [8]. This paper presents a 12:6 Astute Compressor which compresses 12-bit input to 6-bit output as shown in Fig. (3). The compressor consists of a Half Adder (HA) and a series of Modified Full Adders (MFA). The modified full adder consists of 3 input XOR gate, 2 input OR and AND gates as shown in Fig. (2).

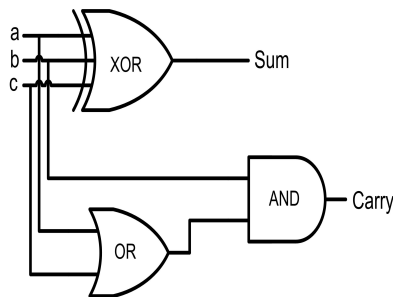


Fig. 2: Modified Full Adder (MFA)

The modified full adder works for all the input combinations except for the input combination of 101 which is binary equivalent of 5. All the adders are connected in series and the Carry of each adder will be propagated to the next successive adder as one of the inputs. The other inputs to the adders are the previous stage Carry bits C0 to C6 and Cc1 to Cc5. Propagation of the Carry bits to the next successive adder takes place till the end. The final adder in the compressor consists of only Sum part and the Carry part is neglected for the exact output of 6 bit length. The output of the compressor is the final output of the multiplier after completion of 2<sup>nd</sup> cycle. The Sum bits of each adder will constitute the output bits. The first adder Sum bit is the Least Significant Bit (LSB) of the final result, and the last adder Sum bit is the Most Significant Bit (MSB). The design of the compressor has been done with a combination of PTL and CMOS logic style with 78 transistors, which is equal to 42% reduction in the transistor count by CMOS logic style. The compressor produces an average power of 0.449 uW and a delay of 4.455 ns. The comparison of the proposed compressor with the other compressors on FPGA [9] in terms of power, delay, and number of logic gates used is shown in Table I. The graphical representation of power and delay comparison of the proposed Astute compressor with the others compressors are shown in Fig. (4), Fig. (5) respectively.

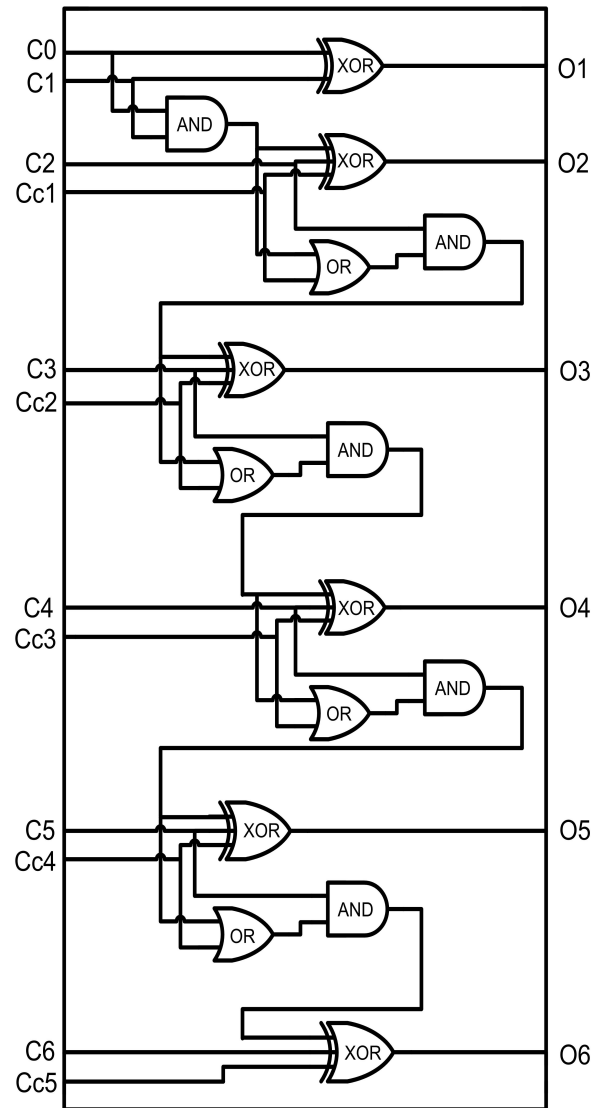


Fig. 3: Proposed 12:6 Compressor: Astute Compressor

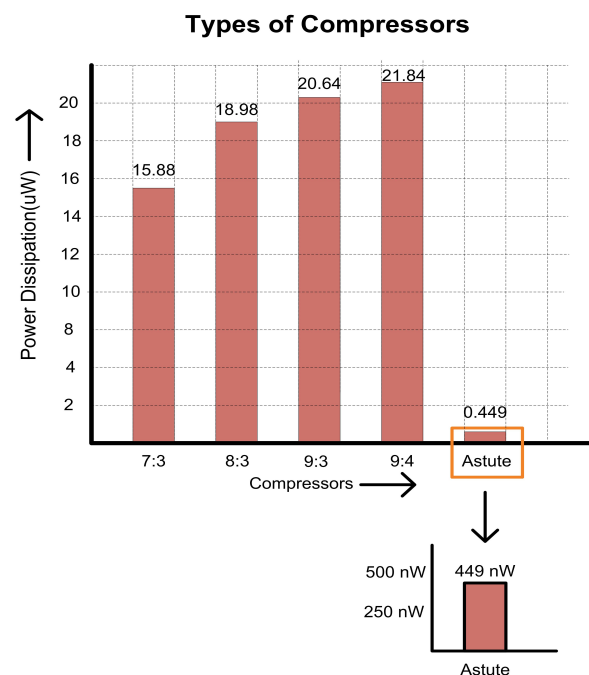


Fig. 4: Power Comparison of Various Compressors

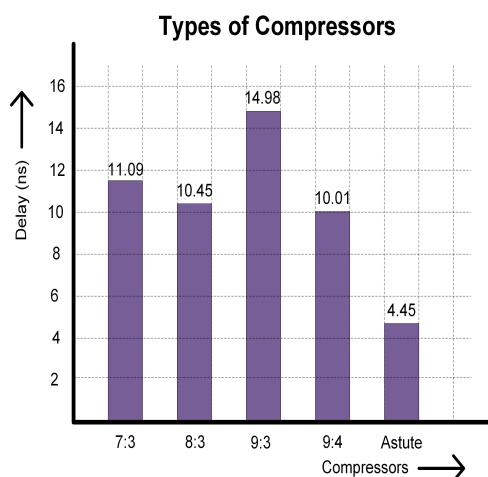


Fig. 5: Delay Comparison of Various Compressors

TABLE I: Comparison of Various Compressors

| Compressors              | Power(uW)    | Delay(ns)   | No of Logic gates used |
|--------------------------|--------------|-------------|------------------------|
| 7:3 Compressor           | 15.88        | 11.09       | 19                     |
| 8:3 Compressor           | 18.98        | 10.45       | 25                     |
| 9:3 Compressor           | 20.64        | 14.98       | 28                     |
| 9:4 Compressor           | 21.84        | 10.01       | 29                     |
| <b>Astute Compressor</b> | <b>0.449</b> | <b>4.45</b> | <b>15</b>              |

TABLE II: Transistor Count and Power Calculations of Various Multipliers

| Multipliers using      | Power(uW) | No. of Transistors |
|------------------------|-----------|--------------------|
| Compressors [10]       | 521.38    | N/A                |
| Carry Propagation [11] | 312.46    | N/A                |
| Barrel shifter [12]    | 642.10    | N/A                |
| GDI Technique [13]     | 301.00    | 748                |
| Montgomery             | 11.38     | 634                |

## V. PROPOSED MONTGOMERY MULTIPLIER DESIGN USING ASTUTE COMPRESSOR

The proposed multiplier is verified with the other multipliers designed using different techniques to demonstrate its effectiveness.

### A. Simulation Results of Modified Montgomery Multiplier

An  $6 \times 6$  modified Montgomery multiplier has been designed by embedding the proposed 12:6 Astute Compressor.

1) *Analysis of Proposed Multiplier in terms of Power Dissipation and transistor count:* The proposed multiplier has been compared with the various multipliers, designed using different techniques in terms of power and number of transistor count as shown in table II. The usage of pass transistor logic in combination with conventional CMOS logic resulted in yielding low power and area efficient design. The proposed multiplier delivered an average power of 11.38 uW and delay of 390.8 ps with a total number of transistor count equals to 634. Fig. (6) shows the graphical representation of power comparison of various multipliers with the proposed one.

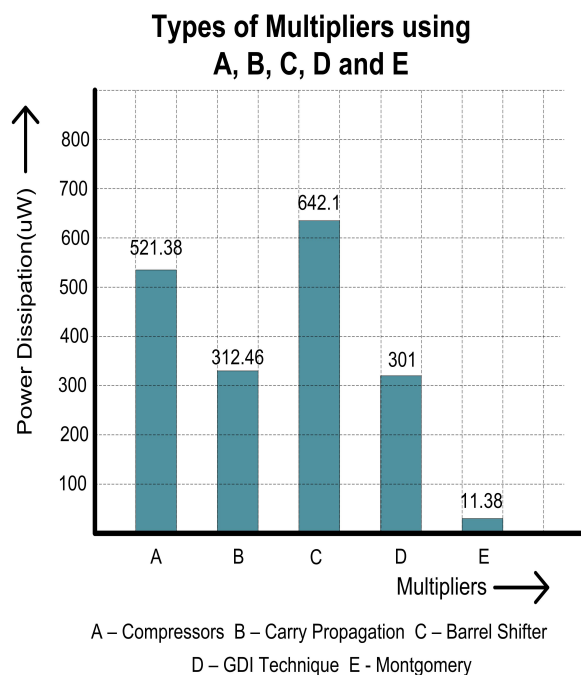


Fig. 6: Power Comparison of Various Multipliers

## VI. APPLICATION OF THE PROPOSED MULTIPLIER

In the epoch of propelling technology, processing of the signal to establish proper communication plays a pivotal role [14]. To have better communication, one must take many factors into account. Usage of filters in digital signal processing can reduce the complexity and helps to achieve better performance in various factors such as noise cancellation, removal of unwanted signals, and proper attenuation. Restoration and separation of the signals while signal processing are the two important undertakings by a filter. The classification of filters depends on whether it is an analog or digital filter. The digital filters can be classified into Finite Impulse Response (FIR) filters and Infinite Impulse Response (IIR) filters. The analog filters can be classified into Butterworth filter, Chebyshev filter etc. A filter can be extended to any number of stages based on the requirement. The complexity depends on number of stages present. More number of stages results in high complexity filter design. With increase in complexity, the cost of the filters will also increase. Therefore, the design of higher order filters with reduced complexity and cost, is on high demand in the market.

A 5<sup>th</sup> order low pass FIR filter is adopted for the implementation of the proposed multiplier in this paper. FIR filters are mainly used in the applications where there is a need for linear phase response. In general, FIR filters are stable filters. To design a FIR filter, one must choose the design method. Three methods are known for the design of FIR filter namely,

- 1) Frequency sampling techniques
- 2) window methods
- 3) optimal filter design methods

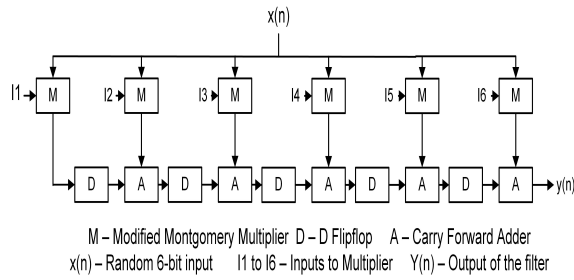


Fig. 7: 5th Order Low Pass FIR Filter

$$y(n) = I1.x(n) + I2.x(n-1) + \dots + I6.x(n-5) \quad (5)$$

The general equation of the filter is given by eq. (5). The filter design consists of multipliers, D-flipflops, and a carry-forward adder [15] as the main elements as shown in Fig. (7). D-flipflop is used in order to reduce the critical path delay of the filter. The carry forward adder which is used in the filter consists of a half adder and full adders as its functional elements in which carry of each adder is propagated to the next adder in series. The inputs to the adder are the multiplier output and the D-flipflop output each of 6-bit length each. The adder produces a 6-bit output, and the final output of the circuit is the output of last adder present in the filter. The complete filter design has been done with 4254 transistor count and the filter produced an average power of 216 uW and a delay of 1.09 ns.

## VII. CONCLUSION

In today's smart products of electronics and their applications in different fields, the speed and area constraints are met by the different multipliers proposed by several designers. The upgrading technology still demands the efficient design of the multipliers in different constraints. A modified Montgomery multiplier, which plays a crucial role in cryptography, has been proposed in this paper with low complexity and enhancements in power and area factors. The design of the multiplier by embedding the proposed Astute compressor made it into a modified one and an area-efficient design. The combination of CMOS and pass transistor logic for designing the logic gates involved in the multiplier declined the number of transistors and yielded in low power design. A 5th order low pass FIR

filter is designed with the proposed multiplier and the results are very encouraging.

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