# Drift chamber with a c-shaped frame

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## Abstract

We present the construction of a planar drift chamber with wires stretched between two arms of a c-shaped aluminium frame. The special shape of the frame allows to extend the momentum acceptance of the COSY-11 detection system towards lower momenta without suppressing the high momentum particles. The proposed design allows for construction of tracking detectors covering small angles with respect to the beam, which can be installed and removed without dismounting the beam-pipe. For a three-dimensional track reconstruction a computer code was developed using a simple algorithm of hit preselection.

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#### 1 Introduction

The drift chamber which is described in this report was built for the COSY-11 experimental facility operating at the Cooler Synchrotron COSY-Jülich [1]. The COSY-11, described in details in Ref. [2] and shown schematically in Fig. 1, is a magnetic spectrometer for measurements at small angles and is dedicated to studies of near-threshold meson production in proton-proton and proton-deuteron collisions (see e.g. Refs. [3,4,5]). It uses one of the regular COSY dipole magnets for momentum analysis of charged reaction products originating from interaction of the internal COSY beam particles with the nuclei of a cluster beam target [6]. Trajectories of positively-charged particles which are deflected in the dipole magnet towards the center of the COSY-ring are registered with a set of two planar drift chambers indicated as D1 and D2 in Fig. 1. These chambers cover only the upper range of momenta of the outgoing particles what suffices to measure e.g. two outgoing protons in the  $pp \to pp\eta'$  process [5] or  $p - p - K^+$  tracks in the  $pp \to ppK^+K^-$  reaction close to threshold [4]. For tracking positively charged pions appearing in nearthreshold reactions such as  $pp \to pp\pi^+\pi^-$  with momenta by a factor of  $m_\pi/m_p$ smaller then the proton momenta it was necessary to extend the COSY-11 momentum acceptance towards smaller values.

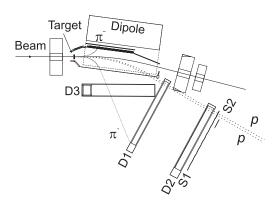


Fig. 1. COSY-11 detection system. Indicated particle tracks correspond to a  $pp \to pp\pi^+\pi^-$  event simulated for the beam momentum exceeding by 1 MeV/c the threshold momentum equal to 1219 MeV/c. The two outgoing protons are registered with a set of two chambers — D1 and D2 and the  $\pi^+$  trajectory is measured with the presently introduced chamber — D3. The scintillation hodoscopes S1 and S2 are used as start detectors and S3 hodoscope placed in a distance of 9.4 m from S1 and not indicated in the figure is used as stop detector for time of flight measurements.

Another important purpose was the detection of positively charged kaons prior

to their decay what is especially important for the measurement of the  $pp \rightarrow$  $ppK^+K^-$  close to threshold due to its small cross section on the level of a few nanobarns. For this, an additional drift chamber was built and installed in the free space along the COSY-11 dipole magnet (see chamber D3 in Fig. 1). The main requirement for the chamber was a shape of the supporting frame which would not interfere with high momentum particles that are registered in the detectors D1 and D2. This demand was fulfilled by choosing the frame of a rectangular form but with one vertical side missing, called c-shaped frame since it resembles the character c. The main design characteristics of the chamber are given in section 2. It was also essential, that the chamber allows for a three-dimensional track reconstruction in order to determine the momentum vectors of registered particles at the target by tracing back their trajectories in the magnetic field of the COSY-11 dipole magnet to the nominal target position. Therefore three different wire orientations were chosen and a track reconstruction program was developed. This program is described in section 3. The chamber calibration and results of the track reconstruction are presented in section 4.

## 2 The chamber construction

The sensitive chamber volume is built up by hexagonal drift cells (see Fig. 2) identical with the structure used in the central drift chamber of the SAPHIR detector [7]. In this type of cells the drift field has approximately cylindrical symmetry, and thus the distance-drift time relation depends only weekly on the particles' angle of incidence. In order to minimize the multiple scattering on wires, gold-plated aluminium [8] is used for the 110  $\mu$ m-thick field wires, whereas the sense wires are made of 20  $\mu$ m-thick gold-plated tungsten.

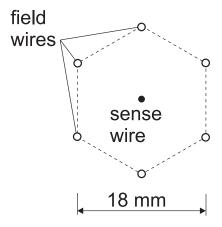


Fig. 2. Hexagonal cell.

The cells are arranged in seven detection planes as indicated in Fig. 3 showing

one of two parallel aluminium endplates between which the wires are stretched. Three detection planes (1, 4 and 7) contain vertical wires, two planes (2, 3) have wires inclined at  $-10^{\circ}$  and the remaining two planes (5, 6) contain wires inclined at  $+10^{\circ}$ . This arrangement makes it possible to reconstruct particle trajectories in three dimensions, also in cases of multi-track events. The relatively small inclination of the wires was chosen since the measurement of particle trajectories in the horizontal plane needs to be much more accurate compared to the vertical plane. This is due to the fact that the particle momenta are determined on the basis of the deflection of their trajectories in an almost uniform vertical magnetic field in the 6 cm gap of the COSY-11 dipole magnet.

Each endplate contains bore holes of  $\emptyset 4$  mm with inserted feedthroughs for mounting the wires. The drilling was done with a CNC jig boring machine assuring a positioning accuracy better than  $\pm 0.01$  mm. The holes for the field wires form equilateral hexagons with a width of 18 mm. In the middle of these hexagons there are the openings for the sense wires. The resulting spacing of the sense wires in the planes with vertical wires is again equal to 18 mm and in the detection planes with wires inclined by  $\pm 10^{\circ}$  is equal to 18 mm× cos  $10^{\circ}$  = 17.73 mm. The chamber contains  $3 \times 80 = 240$  cells with vertical wires,  $2 \times 76 = 152$  cells with wires inclined by  $-10^{\circ}$  and  $2 \times 77 = 154$  cells with wires inclined by  $+10^{\circ}$ .

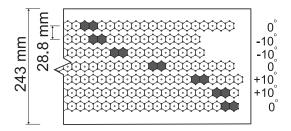


Fig. 3. Upper end-plate with indicated positions of openings for feedthrough used for mounting the wires.

The disturbance of the electric field in the drift cells of a given plane by the cells of the neighboring planes was investigated using the Garfield code [9]. With the chosen spacing of the detection planes equal to 28.8 mm (see Fig. 3) the resulting corrections to the distance-drift time relation determined as a function of position along the sense wires are smaller than 0.05 mm [10] for distances from the sense wire smaller than half of the cell width (9 mm). These corrections were neglected in view of the expected precision of track reconstruction in the order of 0.1 mm. Thus one can assume that the distance-drift time relation is the same for all the cells in a given detection plane, what simplifies the chamber calibration.

The two aluminium endplates for mounting the wires are 15 mm thick and are supported by two c-shaped frames made out of 20 mm thick aluminium (see a three-dimensional view in Fig. 4). The frames hold the total load of about 2.4 kN originating from the mechanical tension of  $\sim 0.2$  kN (=  $546 \times 0.3$  N) of the sense wires and  $\sim 2.2$  kN (=  $2198 \times 1$  N) of the field wires. Prior to mounting the wires, the frames were pre-stressed with a force corresponding to the tension of wires using led bricks uniformly distributed on the upper endplate. This caused a deflection of the endplates at the free ends of 0.7 mm each. The ends of the pre-stressed endplates were fixed together using a steel plate and the bricks were taken away. After mounting the wires the steel plate was removed and we checked that the distance between the ends of the endplates did not change.

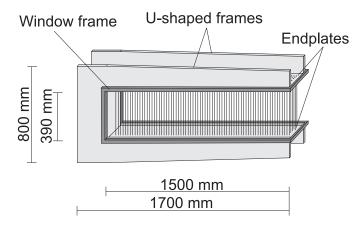


Fig. 4. Schematic three-dimensional view of the chamber frame for mounting the wires. The window for particles is 1500 mm wide and 390 mm high.

For mounting the field wires brass feedthroughs with a Ø150  $\mu$ m inner opening are used. Since all field wires should have the same ground potential electrical contact of the feedthroughs with the aluminium endplates is assured by usage of a conductive glue. For the sense wires we used isolating feedthroughs made of Delrin, a polyacetal with a high dielectric strength of about 40 kV/mm, with inserted brass feedthroughs containing Ø50  $\mu$ m openings for the positioning of the wires. A schematic drawing of the feedthroughs is shown in Fig. 5. The wires were strung between pairs of feedthroughs and were fixed by means of copper crimp pins. For sealing the feedthroughs and the crimp pins epoxy resin was used. The high voltage was connected to the sense wires through 1 M $\Omega$  resistors soldered directly to the crimp pins on the lower endplate. The signals were read out through 1 nF coupling capacitors connected to the sense wires on the upper endplate (see Fig. 6). The capacitors and resistors were enclosed in hermetical volumes which were dried out with silica aerogel allowing to reduce leakage currents.

For the window for particles penetrating the chamber 20  $\mu m$  thick Kapton foil

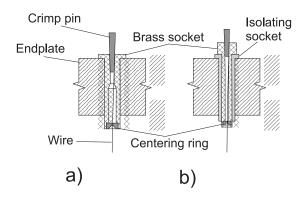


Fig. 5. Section of feedthrough for (a) field wires, and (b) sense wires.

is used glued to an aluminium frame which is screwed on the support frame and sealed with  $\emptyset 3$  mm o-ring gasket.

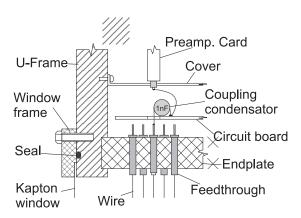


Fig. 6. Section of the upper endplate.

Each of the detection planes is equipped with five 16-channel preamplifier-discriminator cards [11] based on the Fujitsu MB13468 amplifier chip and the LeCroy MVL407S comparator chip. The cards are mounted directly on the chamber. The output pulses in the ECL standard are led by means of 30 m long twisted-pair cables to FASTBUS-TDCs of LeCroy 1879 type working in the common stop mode with the pulses from the discriminators as start signals and the trigger pulse as the common stop.

As chamber gas, P10 mixture (90% argon and 10% methane) at atmospheric pressure is used. The gas flow through the chamber is about 12 l/h. The sense wire potential is +1800 V, whereas the field wires are all grounded. The gas amplification in the chambers is about  $10^5$  and the discrimination threshold set in the preamplifier-discriminator cards corresponds to  $3 \cdot 10^5$  electrons.

## 3 Track reconstruction algorithm

For the reconstruction of particle tracks a simple algorithm was developed and implemented as a computer code written in the C-language. The reconstruction proceeds in three stages:

- finding track candidates in two dimensions, independent for each orientation of the wires,
- matching the two-dimensional solutions in three dimensions,
- three-dimensional fitting in order to obtain optimal track parameters.

In the first stage, track candidates are found in two-dimensions using hits in the detection planes with the same inclination of the wires. For this, all possible combinations of pairs of hits from two different detection planes are taken into account. Due to the left-right ambiguity of the track position with respect to the sense wire, for each pair of hits there are four straight-line solutions possible. These solutions are determined using an iterative procedure. First, the track distance to the sense wire is calculated from the drift time to drift distance relation  $d(t,\theta)$  assuming the track entrance angle  $\theta$  as equal to  $0^{\circ}$ . Note that the time-to-distance function may depend on the angle  $\theta$  (see Fig. 7) and this is taken into account when making a calibration. Thus, the track is defined by a pair of points lying in the corresponding sense wire planes and indicated as P1 and P2 in Fig. 7. In the next step, the inclination of this track is taken for determining new values of the distances from the sense wires and constructing a new pair of points defining the track. These points are indicated as T1 and T2 in Fig. 7. This procedure can be repeated, however, we terminate it already after the second step since further steps give negligible corrections. For each track determined by this method, one subsequently finds hits which are consistent with it within a certain corridor along the track. In this way, hits from neighboring cells with respect to the selected two cells and from other detection planes with the same orientation of wires are taken into account in the reconstruction. For the width of the corridor we take  $\pm 1$  mm which is a few times larger than the position resolution of a single detection plane. With this choice more than 90% of all hits are included in the reconstruction as it is discussed in the next chapter.

In three dimensions a two-dimensional solution can be represented by a plane containing the track and parallel to the corresponding sense wires. Planes representing the two-dimensional solutions for three different directions of sense wires used in the chamber should intersect along a common line corresponding to the particle track. However, due to the limited spatial resolution of the chamber, the planes intersect along three different lines (see Fig. 8). Two lines —  $l_1$  and  $l_2$  correspond to the intersections of the inclined planes with the vertical plane and the third line —  $l_3$  is an intersection of the inclined planes.

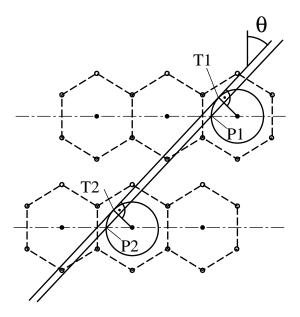


Fig. 7. Illustration of iterative procedure of fitting a straight line to two hits.

In order to quantify the consistency between the two-dimensional solutions, we determine the distances  $h_1$  and  $h_2$  between the crossing points of the lines  $l_1$ ,  $l_2$  with the first and the seventh detection plane, respectively (see Fig. 8). For the three-dimensional reconstruction, we accept only the combinations of two-dimensional solutions for which the distances  $h_1$  and  $h_2$  are both smaller then a certain limit h which is adjusted as a reconstruction parameter. Too large values of h lead to an unnecessary increase of CPU time since too many non-matching combinations are taken into account. On the contrary, too small values of h cause losses of correct combinations and consequently decrease the reconstruction efficiency. In our case, a reasonable value for h is 2 cm.

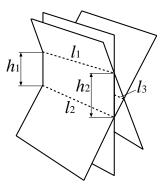


Fig. 8. Crossing of planes representing two-dimensional solutions for three different orientations of wires.

The determination of track parameters in three dimensions proceeds via minimization of the  $\chi^2$  function calculated on the basis of the differences between the measured distances of tracks from sense wires  $d_i$  and the distances of the fitted tracks from the sense wires  $d_i^f$ :

$$\chi^2 = \sum_i \frac{(d_i - d_i^f)^2}{(\delta d_i)^2},\tag{1}$$

where the summation proceeds over all hits assigned to one track and  $\delta d_i$  is an uncertainty of the measured distance  $d_i$ . In the case of the two-dimensional track reconstruction for wires oriented in one direction, the numerator in the above expression can be easily expressed in Cartesian coordinates using the formula:

$$(d_i - d_i^f)^2 = \frac{[x_i - (az_i + b)]^2}{(1 + a^2)},$$
(2)

where a and b are parameters in the straight line equation: x = az + b representing the track, x and z are coordinates perpendicular to the sense wires and  $(x_i, z_i)$  is a point lying in the distance  $d_i$  from the sense wire in the location corresponding to the closest approach to the track (see Fig. 9). For

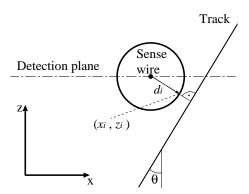


Fig. 9. Definition of the point  $(x_i, z_i)$  used in the two-dimensional track reconstruction

the three-dimensional reconstruction, we use a coordinate system with the y-axis parallel to the vertical wires and the z-axis perpendicular to the detection planes. The origin of the coordinate system is located in the first plane. Particle tracks are parametrized as straight lines in a conventional way:

$$x' = a'z' + b', (3)$$

$$y' = c'z' + d', (4)$$

where a', b', c', d' are the searched track parameters. They can be linked to the parameters a, b corresponding to the two-dimensional solutions using the linear transformation:

$$a = a'\cos\alpha_i + c'\sin\alpha_i,\tag{5}$$

$$b = b' \cos \alpha_i + d' \sin \alpha_i, \tag{6}$$

where  $\alpha_i$  is the angle between the sense wires and the vertical direction. Inserting Eqs. (5) and (6) into (2) and the result into (1), the expression for  $\chi^2$  takes the form:

$$\chi^{2} = \sum_{i} \frac{[x_{i} - (a'\cos\alpha_{i} + c'\sin\alpha_{i})z_{i} - (b'\cos\alpha_{i} + d'\sin\alpha_{i})]^{2}}{[1 + (a'\cos\alpha_{i} + c'\sin\alpha_{i})^{2}](\delta d_{i})^{2}}.$$
 (7)

The derivative of the dimensionless term in the square bracket in the denominator is of the order of unity and is negligible compared with corresponding derivative of the numerator divided by  $(\delta d_i)^2$  which is of the order of  $z_i/\delta d_i$ . Therefore, during the fitting procedure we regard the numerator just as a constant given by the initial values of the parameters and thus the minimization of  $\chi^2$  is reduced to the linear least squares problem. For the fitting we use the *svdfit* function from "Numerical Recipes in C" [13]. The three-dimensional track fitting is performed for all combinations of two-dimensional track candidates and the solution with the minimal value of  $\chi^2$  is selected. The hits corresponding to this solution are then removed from the set of hits recorded in a given event and the reconstruction is repeated from the beginning until there are no further candidates of tracks. In this way multi-track events can be reconstructed.

## 4 Calibration and reconstruction results

The chamber is calibrated using the experimental data. In a first step an approximate drift time to drift distance relation is determined by integration of the drift time spectra as provided by the uniform irradiation method [12]. A typical spectrum obtained by summing up drift time spectra from all sense wires in one detection plane is shown in Fig. 10a. The width of the drift time distribution is about 300 ns which with the corresponding half of the cell width equal to 9 mm results in a mean drift velocity of 0.03 mm/ns. However, the space-time relationship obtained by integration of the drift time spectrum is not strictly linear (see Fig. 10b); its slope increases slightly in the neighborhood of the sense wire. In the next step, corrections to this calibration are determined using an iterative procedure. For this, the average deviations between the measured and fitted distances of the tracks from the sense wires are calculated. These deviations are determined as a function of the drift time  $t_j$  corresponding to the TDC channel j and the track entrance angle  $\theta_k$  from the range  $(0^{\circ}, 90^{\circ})$  divided into 9 intervals numerated by the index k:

$$\Delta d(t_j, \theta_k) = \langle d^f(t_j) \rangle - d(t_j, \theta_k), \tag{8}$$

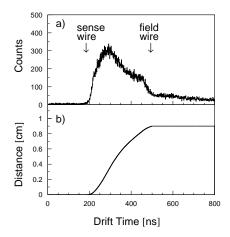


Fig. 10. Drift time spectrum for the first detection plane (a) and space-time relationship obtained by integration of the drift time spectrum in the time interval indicated by the arrows (b). The tail on the right hand side of the drift time spectrum originates from electrons drifting from the space between the detection planes.

where the average <> is taken over all hits which were recorded in the TDC channel j and correspond to the track entrance angle interval k. The spacetime relation used in the first iteration is then corrected by the above deviation:

$$d'(t_j, \theta_k) = d(t_j, \theta_k) + \Delta d(t_j, \theta_k). \tag{9}$$

After performing the reconstruction of tracks with the new space-time relation new corrections are calculated and so on. This procedure is repeated until the corrections become smaller than the position resolution of the chamber. This occurs in our case after 2-3 iterations. Fig. 11 shows differences  $\Delta d$  of the measured and fitted distances calculated as a function of the drift time for three subsequent iterations. The mean value of  $\Delta d$  deviates from zero only after the first iteration (upper panel in Fig. 11) and the corresponding correction to the space-time relation is of the order of 0.3 mm. For higher iterations the corrections are negligible. The standard deviation of  $\Delta d$  is about 0.2 mm and is a measure of the single wire resolution.

For testing the track reconstruction we used single tracks of protons scattered elastically on the COSY-11 hydrogen target of the cluster-jet type at a beam momentum of 3.3 GeV/c. Events of the elastic proton-proton scattering were registered as coincidences between the scintillation hodoscope S1 detecting the forward scattered protons and the monitor scintillator placed in the target region on the opposite side of the beam, measuring the recoil protons. Additionally, we required firing of the seventh detection plane in order to assure that the proton tracks pass through the chamber. The detection efficiency per detection plane was estimated on the basis of multiplicities of coincidences between the detection planes. In 97% of cases all seven planes fire (see Fig. 12) which means that the detection efficiency in a single detection plane is

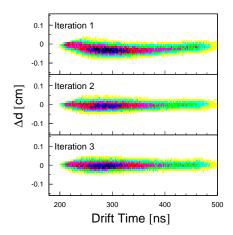


Fig. 11. Differences of the measured and fitted distances calculated as a function of the drift time for the first detection plane and the angular bin  $\theta \in (50^{\circ}, 60^{\circ})$  in three subsequent iterations of the calibration procedure.

close to 100%. The multiplicity of hits shown in Fig. 13a is peaked around

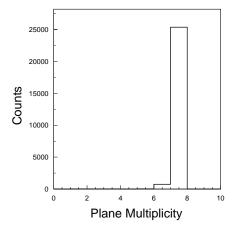


Fig. 12. Multiplicity of coincidences between the detection planes for single tracks of elastically scattered protons.

the value of 14 which is due to the fact that most of tracks are inclined with respect to the chamber and mostly two neighbouring cells from one detection plane fire for each track. For the reconstruction we used an "effective" position resolution of 220  $\mu$ m for which the mean value of  $\chi^2$  per degree of freedom is in the vicinity of 1. The reconstruction was treated as successful when the  $\chi^2$  per degree of freedom was smaller than 5. This was the case for 95% of events triggered as elastic p-p scattering. For selected events in which all seven detection planes fired, the reconstruction was successful in 97%. In the reconstruction most of the registered hits were used for the fitting as one can see by comparison of Fig. 13a and Fig. 13b. The precision of the track parameters a, b, c, d was extracted from the diagonal elements of the corresponding covariance matrix. For typical track entrance angles of about  $50^{\circ}-60^{\circ}$  the resulting uncertainty of track position along the x- and y-axis is equal to  $\delta b = 0.3$  mm

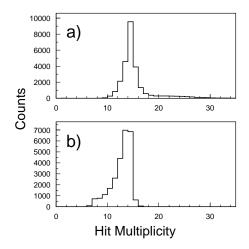


Fig. 13. Multiplicity of hits for events of the elastic proton-proton scattering (a) and of hits preselected and used in successful reconstruction of single tracks (b).

and  $\delta d = 3$  mm, respectively. The uncertainty of the track inclination in the horizontal and vertical plane is about 1 mrad and 10 mrad, respectively.

## 5 Conclusions

A drift chamber with a c-shaped frame was constructed for the COSY-11 experimental facility. The special shape of the frame allows for the detection of low momentum particles without disturbing the high momentum ejectiles which are registered in other detector components. This kind of chamber can be applied if no frame elements are allowed in the sensitive area of the detection system. An example of a possible further application — besides the one discussed here — could be the detection of particles scattered at small angles with respect to the beam. In this case, two such chambers placed symmetrically with respect to the beamline could be used for covering the forward angles. The chambers can be installed and removed without dismounting the beam-pipe contrary to an alternative solution of one chamber with a central hole for the beam-pipe.

The track reconstruction algorithm which was developed for the chamber can also be used for other planar drift chambers containing cells with an electric field which has approximately cylindrical symmetry. It is required, however, that the chamber contains wires oriented at least in three different directions and for each direction there are at least two detection planes necessary.

The chamber allows to determine the track position and inclination in the horizontal plane with an accuracy of about 0.3 mm and 1 mrad, respectively. In the vertical direction these accuracies are worse by about an order of magnitude, which is in accordance with the design values. For the tracking in the

vertical magnetic field of the COSY-11 dipole magnet no higher precision was envisaged. For other applications the precision can be improved by choosing a larger inclination of the wires.

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